

# Performance analysis of a system with integrated CO<sub>2</sub> heat pumps and a PCM tank in different charging standards

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## Abstract

Performance investigation of a system with an integrated heat pump and a phase change material (PCM) tank is seldom conducted in current studies, and the issue of identifying the optimal setting values of key variables in different charging standards and combinations of criteria is ignored. Therefore, in this study, we consider a system that integrates air- and water-source CO<sub>2</sub> heat pumps and a PCM tank as a case study to address this issue. Experimentally validated CO<sub>2</sub> heat pump and PCM tank models were used to simulate the system, and T-charging, Q-charging, and t-charging standards were considered. We concluded that the system coefficient of performance reduced by 10.5%, 12.2%, and 14.4% when the setting stored energy was increased from 2.1 kWh to 4.5 kWh, setting outlet water temperature of PCM tank was increased from 28 °C to 34 °C, and setting charging time was increased from 0.5 h to 1.7 h in the Q-charging, T-charging, and t-charging standards, respectively. Multicriteria optimization was performed in different cases to determine the optimal setting values of the key variables. The optimal setting charging time is 1.7 h when weight factors of charging time and stored energy are 0.3 and 0.7, respectively. Thus, this study provides a distinctive perspective for investigating a system by integrating a heat pump and PCM tank by considering different charging standards.

**Keywords:** CO<sub>2</sub> heat pump; PCM tank; Performance analysis; Charging standard

**Nomenclature***E* Electricity use (kWh)*OS* Score (-)*Q* Energy amount (kWh)*T* Temperature (°C)*t* Moment (h)*Abbreviations*ACHP Air-source CO<sub>2</sub> heat pump (-)

COP Coefficient of performance (-)

PCM Phase change material (-)

WCHP Water-source CO<sub>2</sub> heat pump (-)*Subscripts**cp* Case considering  $\varepsilon_{ct}$  and  $COP_{st}$  (-)*cr* Compressor (-)*cs* Case considering  $\varepsilon_{ct}$  and  $Q_{se}$  (-)*cst* Case considering  $\varepsilon_{ct}$ ,  $Q_{se}$ , and  $E_{tu}$  (-)*ct* Charging (-)*em* Ending (-)*lf* Least preferred case (-)*mf* Most preferred case (-)*ot* Outlet water of PCM tank (-)*pe* Pump at the evaporator side (-)*pg* Pump at the gas cooler side (-)*sm* Starting (-)*se* Stored (-)*st* System (-)*sv* Setting value (-)*tu* Total (-)*Greek symbols* $\alpha$  Weigh factor (-) $\varepsilon$  Time span (h)

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## 34 **1. Introduction**

### 35 1.1. Background and motivation

36 Heat pumps that obtain heat from natural media, such as air [1] and water [2], are utilized in many  
37 fields, including household hot water utilization [3], drying [4], space heating [5], district heating  
38 [6] and cooling [7], waste heat recovery [8], rail transportation [9], and zero-emission vehicles [10].  
39 CO<sub>2</sub>, which is non-flammable, easy available, and environmentally friendly, is considered to be an  
40 ideal refrigerant in heat pumps. Owing to its transcritical refrigeration cycle, a CO<sub>2</sub> heat pump can  
41 produce high-temperature water [11]. Thermal energy storage improves the effectiveness and  
42 flexibility of energy utilization [12] and has been applied in many fields, including building  
43 envelopes [13], passive cooling [14], food supply chains [15], frozen products [16], thermal  
44 management [17], photovoltaic systems [18], hot water production [19], and solar stills [20]. PCM  
45 was added to the water tank to form a PCM tank with enhanced energy storage density. Thus, it is  
46 a significant component of heat-pump systems.

### 48 1.2. Research context

49 Wang et al. [21] investigated a heat pump system absorbing heat from the air and sun. They  
50 concluded that compared with the air-source heat pump system, the total electricity consumption  
51 ( $E_{tu}$ ) could be reduced by 73.6%. Du et al. [22] also investigated a heat pump system absorbing  
52 heat from the air and sun. They found that the coefficient of performance (COP) of the system  
53 ( $COP_{st}$ ) could reach 3.44. Shin et al. [23] performed a study of a water-source heat pump system.  
54 They found that the lifecycle cost of the system was 20.2% lower than that of the traditional system.  
55 Zhang et al. [24] reported that the COP of a solar-assisted heat pump was 50% higher than that of  
56 an air-source heat pump. Deng et al. [25] concluded that  $COP_{st}$  could be enhanced by 18.7% when  
57 a varying flowrate of heat transfer fluid at the evaporator side was applied in the ground-source  
58 heat pump system.

59  
60 Ge et al. [26] concluded that the COP of a CO<sub>2</sub> heat pump with tube-in-tube heat exchanger could  
61 reach 4.47 when the ambient air temperature was 40 °C. Li et al. [27] conducted an investigation  
62 of a water-source CO<sub>2</sub> heat pump (WCHP) for domestic use. They found that the COP of the  
63 WCHP could reach 3.99 when the expansion valve opening was 28%. They also proposed a model-  
64 based sizing method that can identify the optimal gas cooler area to maximize the indicator,

65 considering the COP and cost. Sazon and Nikpey [28] reported that 5% increase in discharge  
66 pressure in a solar-assisted ground-source CO<sub>2</sub> heat pump could contribute to 5% reduction in the  
67 levelized cost of heating. Duarte et al. [29] found that increasing the inlet water temperature at the  
68 gas cooler side from 15 °C to 35 °C would cause the COP of the solar-assisted CO<sub>2</sub> heat pump to  
69 decrease by 45.8%. Zanetti et al. [30] found that electricity production can be increased by 8%  
70 when a photovoltaic-thermal solar collector was combined with a CO<sub>2</sub> heat pump.

71  
72 Huang et al. [31] experimentally investigated the performance of a solar chimney with phase  
73 change material (PCM). They found that the PCM melting time was 13.3% longer when the  
74 inclination angle was 30° than that when it was 60°. Guermat et al. [32] concluded that the indoor  
75 temperature could be reduced by 3.95 °C when PCM was applied in the building envelope. Khan  
76 et al. [33] found that the output power could be enhanced by 9.69% when PCM was utilized in a  
77 photovoltaic system. Maghrabie et al. [34] concluded that the output power could be increased by  
78 15.8% when a 3 cm thick PCM panel was utilized in a photovoltaic system. Zheng et al. [35]  
79 reported that  $E_{tu}$  of a solar heating system could be reduced by 35.7% when the PCM floor was  
80 used.

81  
82 Qv et al. [36] concluded that the COP of a solar-assisted heat pump with a PCM tank was 65%  
83 higher than that of an air-source heat pump. Zou et al. [37] reported that the energy storage density  
84 increased by 14% when the PCM tank was utilized in a heat pump system. Long and Zhu [38]  
85 concluded that the COP of a system integrating a heat pump and PCM tank could reach 3.08.  
86 Moreno et al. [39] found that additional cooling of 14.5% could be supplied when the PCM tank  
87 was applied to a heat pump system for space cooling purposes. Qiu et al. [40] concluded that the  
88 charging time ( $\epsilon_{ct}$ ) of the PCM tank could be reduced by 29.8% when the nanoparticle and  
89 orthogonal fin were applied. Issa and Thirunavukkarasu [41] found that the storage efficiency could  
90 reach 82% when copper cylindrical capsules were utilized in the PCM tank. Peng et al. [42]  
91 reported that the charging rate of the PCM tank can be increased by 20% when fins are applied.  
92 Shu et al. [43] found that  $\epsilon_{ct}$  of the PCM tank could be reduced by 56% when the temperature was  
93 increased from 65 °C to 85 °C.

94  
95 Although scholars have paid attention to investigating heat pump systems with PCM tanks, few

96 studies have systematically focused on the performance of the charging process with the integration  
 97 of the heat pump and PCM tank. When the PCM tank was integrated with the heat pump, the  
 98 increase in the outlet water temperature of the PCM tank ( $T_{ot}$ ) slowed owing to the phase-change  
 99 process. This contributes to the enhancement of energy efficiency. However, scholars have ignored  
 100 this issue. The charging process of PCM in this study was open-loop.  $\varepsilon_{ct}$ , stored energy ( $Q_{se}$ ), and  
 101  $T_{ot}$  were considered as performance indicators. However, the charging process with the integration  
 102 of the PCM tank and heat pump was a closed loop.  $E_{tu}$  and  $COP_{st}$  were considered as performance  
 103 indicators.

104  
 105 As depicted in Table 1, unlike current studies, this work focuses on investigating the charging  
 106 process at system level, and  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  are considered as performance indicators. The  
 107 knowledge gaps for investigating the system integrating CO<sub>2</sub> heat pumps with a PCM tank are as  
 108 follows. a) The performance investigation of the system in different charging standards is seldom  
 109 considered in current studies; b) The systematic investigation of different setting variables in  
 110 different charging standards on  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  is still lacking; c) The approach for  
 111 identifying optimal setting variables in different charging standards to maximize the overall  
 112 performance of the system requires much-needed development; d) The influence mechanism of  
 113 different combinations of setting variables on the performance of the system is still unknown.

114  
 115 **Table 1** Comparison between current studies and this work

References	System level	Component level	Charging process	$\varepsilon_{ct}$	$Q_{se}$	$E_{tu}$	$COP_{st}$
[36]	√	×	×	×	×	×	√
[37]	√	×	×	×	×	×	√
[38]	√	×	×	×	×	×	√
[39]	√	×	×	√	√	×	×
[40]	×	√	√	√	×	×	×
[41]	√	×	√	√	√	×	×
[42]	×	√	√	√	×	×	×
[43]	×	√	√	√	×	×	×
This work	√	×	√	√	√	√	√

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117

### 118 1.3. Contributions

119 The contributions or novelties of this study are as follows. a) The influence of different charging  
120 standards on the performance of the system integrating CO<sub>2</sub> heat pumps with PCM tank was  
121 analyzed. This remedies the research gap in the field of system integration in different charging  
122 standards; b) The influence of  $Q_{se,sv}$  in the Q-charging standard,  $T_{ot,sv}$  in the T-charging standard,  
123 and  $\varepsilon_{ct,sv}$  in the t-charging standard on  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  were analyzed. This overcomes  
124 the limitations in current studies that the influencing factor in the aspects of integrating the PCM  
125 tank with CO<sub>2</sub> heat pumps is simple; c) A multi-criteria approach was established to identify  
126 optimal  $Q_{se,sv}$ ,  $T_{ot,sv}$ , and  $\varepsilon_{ct,sv}$  in the Q-charging, T-charging, and t-charging standards,  
127 respectively. Unlike current studies, this study can guide engineers to design optimal systems  
128 integrating CO<sub>2</sub> heat pumps with a PCM tank in different charging standards; d) Three multi-  
129 criteria cases in which the combinations of  $\varepsilon_{ct}$  and  $Q_{se}$ , combinations of  $\varepsilon_{ct}$ ,  $E_{tu}$ , and  $Q_{se}$ , and  
130 combinations of  $\varepsilon_{ct}$  and  $COP_{st}$  were considered to enable better operation of the system integrating  
131 CO<sub>2</sub> heat pumps with a PCM tank in different aspects.

132

### 133 1.4. Paper organization

134 The remainder of this paper is organized as follows. In Section 2, the material and methods of this  
135 study are presented. The description of the case study is presented in Section 3. In Section 4, we  
136 present the results and analysis in different charging standards. The conclusions are presented in  
137 Section 5. Finally, in Section 6, we present the future prospects.

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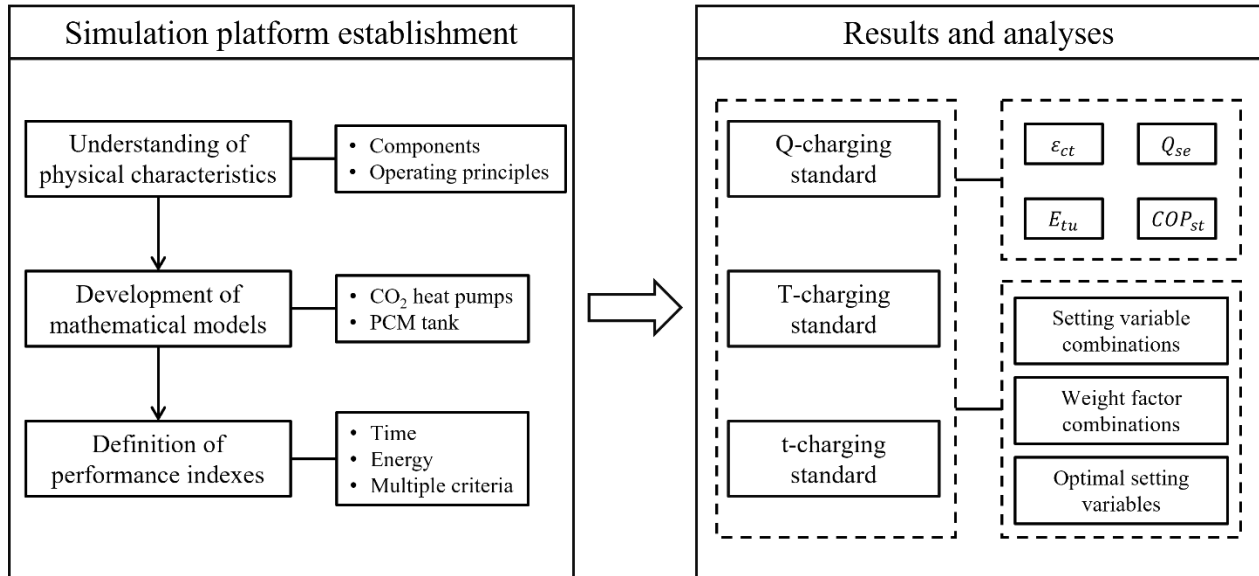
## 139 **2. Material and methods**

140 The influence of charging standards, i.e., how to judge whether the charging process is completed,  
141 on the performance of the system has seldom been considered in current studies. In this study,  $T_{ot}$   
142 was monitored using a temperature sensor. The charging process is considered complete when  $T_{ot}$   
143 reaches the setting value of  $T_{ot}$  ( $T_{ot,sv}$ ). This charging standard is known as the T-charging standard.  
144 However, limited thermal energy is sometimes required from the PCM tanks. In this study,  $Q_{se}$   
145 was monitored using an energy meter. The charging process is considered complete when  $Q_{se}$   
146 reaches the setting value of  $Q_{se}$  ( $Q_{se,sv}$ ). This charging standard is known as the Q-charging  
147 standard. In the other cases, the time required to charge the PCM tank was limited. The charging  
148 process is considered as being completed when  $\varepsilon_{ct}$  reaches the setting value of  $\varepsilon_{ct}$  ( $\varepsilon_{ct,sv}$ ). This

149 charging standard is known as the t-charging standard. The final two charging standards are not  
150 considered in current studies. Additionally, the influence of combinations of setting variables on  
151 the system performance is unclear.

152  
153 Overall, a systematic investigation of the charging process with the integration of a heat pump and  
154 PCM tank considering different charging standards and combinations of setting variables is lacking.  
155 Therefore, in this study, we considered a charging process with the integration of CO<sub>2</sub> heat pumps  
156 and a PCM tank as a case study to illustrate the influence of the charging standards and  
157 combinations of setting variables on the performance of the system. An air-source CO<sub>2</sub> heat pump  
158 (ACHP) and WCHP were considered. The experimentally validated CO<sub>2</sub> heat pump and PCM tank  
159 models were used to simulate the charging process. T-charging, Q-charging, and t-charging  
160 standards were considered. Additionally, three multi-criteria cases, which included the  
161 combinations of  $\varepsilon_{ct}$  and  $Q_{se}$ ,  $\varepsilon_{ct}$ ,  $E_{tu}$ , and  $Q_{se}$ , and  $\varepsilon_{ct}$  and  $COP_{st}$ , were considered. Through  
162 multi-criteria optimization, optimal  $T_{ot,sv}$ ,  $Q_{se,sv}$ , and  $\varepsilon_{ct,sv}$  were determined in the T-charging, Q-  
163 charging, and t-charging standards, respectively.

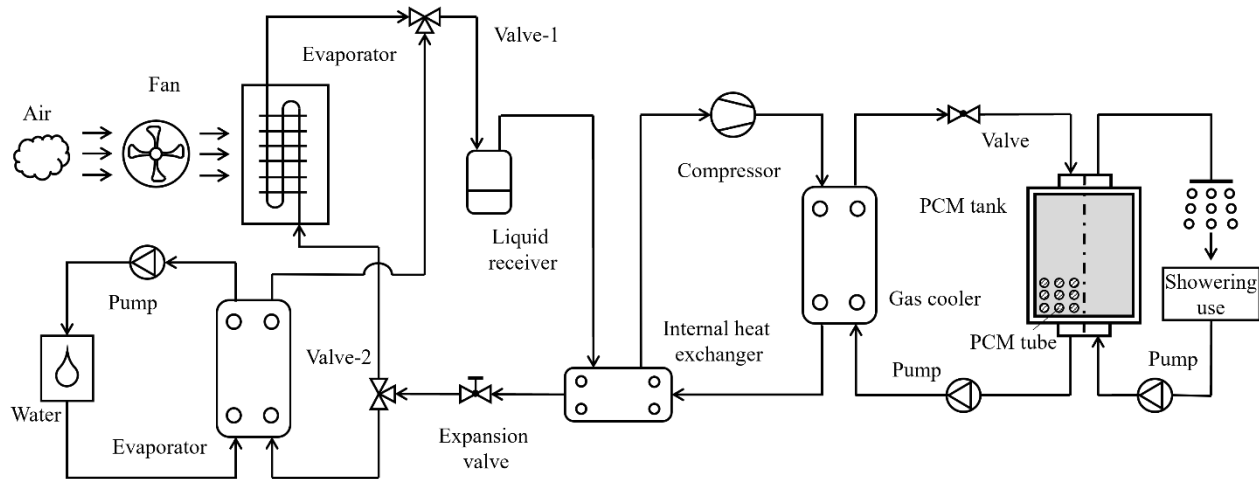
164  
165 Fig. 1 illustrates the research methodology. The main parts of this study include the establishment  
166 of the simulation platform, results, and analyses. Part of the simulation platform is composed of an  
167 understanding of the physical characteristics, development of mathematical models, and definition  
168 of performance indexes. To understand the physical characteristics of the system integrating the  
169 CO<sub>2</sub> heat pumps and PCM tank, the components and operating principles of the system were  
170 determined. The main mathematical models of the system included the CO<sub>2</sub> heat pump and PCM  
171 tank models. In the CO<sub>2</sub> heat pump model, an evaporator, liquid receiver, internal heat exchanger,  
172 compressor, and gas cooler were considered. The performance indices were defined by considering  
173 time and energy. Multiple criteria have been proposed to evaluate the performance of the system.  
174 Three charging standards: Q-charging, T-charging, and t-charging, were considered in the results  
175 and analyses. For each charging standard, the influence of setting variables on  $\varepsilon_{ct}$ ,  $E_{tu}$ ,  $Q_{se}$ , and  
176  $COP_{st}$  were analyzed. Different combinations of setting variables and weight factors were  
177 considered in the multi-criteria optimization, and the optimal setting variables in each case were  
178 obtained.



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180  
181  
182 **Fig. 1.** Research methodology of this study

183 2.1. Understanding of physical characteristics

184 Fig. 2 shows a diagram of the system with the integration of CO<sub>2</sub> heat pumps and a PCM tank.  
185 ACHP and WCHP systems were considered. Valve-1 and valve-2 were utilized to realize the  
186 switch between the ACHP and WCHP. The gas cooler, compressor, evaporator, expansion valve,  
187 and liquid receiver are the main components of the CO<sub>2</sub> heat pumps. Water and air provided heat  
188 for the CO<sub>2</sub>, which was throttled and compressed in the expansion valve and compressor,  
189 respectively. CO<sub>2</sub> evaporates in the evaporator. The internal heat exchanger increases the CO<sub>2</sub>  
190 temperature at the compressor inlet by acquiring heat from the CO<sub>2</sub> leaving the gas cooler. The  
191 water in the PCM tank was heated from the gas cooler by driving the pump.



192  
193 **Fig. 2.** Diagram of the system with integrated CO<sub>2</sub> heat pumps and a PCM tank for household use



## 194 2.2. Development of mathematical models

195 The system was simulated by integrating the CO<sub>2</sub> heat pump and PCM tank models. The  
196 assumptions for constructing the CO<sub>2</sub> heat pump and PCM tank models were presented by  
197 Rasmussen et al. [44] and Li et al. [45], respectively. The formulas for calculating the heat transfer  
198 coefficients of the heat exchangers in the CO<sub>2</sub> heat pump model are described in studies of Deng  
199 et al. [46], Lee et al. [47], and Mota et al. [48]. The formulas for the compressor and expansion  
200 valve models are presented in the studies of Wang et al. [49] and Eames et al. [50], respectively.  
201 The formulas for calculating the Nusselt number in the PCM tank model were presented by  
202 Watanabe et al. [51]. Validations of CO<sub>2</sub> heat pump and PCM tank models were presented by Li et  
203 al. [2]. The mean difference between simulated and experimental outlet water temperatures on the  
204 gas cooler side was 1.4 K, and the error of the PCM tank model was 3.97%, which proves the  
205 reliability of these models.

206

## 207 2.3. Definition of performance indexes

208  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  were utilized as performance indexes.  $\varepsilon_{ct}$  is calculated using Eq. (1) [52]:

$$209 \varepsilon_{ct} = t_{em} - t_{sm} \quad (1)$$

210 where  $t_{em}$  and  $t_{sm}$  denote the ending and starting moments, respectively.  $E_{tu}$  was calculated using  
211 Eq. (2) [53]:

$$212 E_{tu} = E_{cr} + E_{pe} + E_{pg} \quad (2)$$

213 where  $E_{cr}$ ,  $E_{pe}$ , and  $E_{pg}$  are the electricity used by the compressor, and pumps at the evaporator  
214 and gas cooler sides, respectively.  $COP_{st}$  was calculated using Eq. (3) [2]:

$$215 COP_{st} = \frac{Q_{se}}{E_{tu}} \quad (3)$$

## 216 **3. Case study**

217 The water source evaporator, which has a plate width of 0.101 m, has 40 plates. The air-source  
218 evaporator has a fin thickness, spacing, and height of 0.24 mm, 5 mm, and 3.5 mm, respectively.  
219 The heat transfer fluid was a mixture of water and propylene glycol in the ratio of 70:30. The gas  
220 cooler, which had a plate width of 0.1195 m, had 30 plates. The internal heat exchanger had a plate  
221 width of 0.076 m and 12 plates. The PCM used in this study was paraffin. The melting temperature,  
222 thermal conductivity, latent heat, density, and solid and liquid specific heat were 18 °C, 0.17  
223 W/(m·K), 236 kJ/kg, 780 kg/m<sup>3</sup>, 1.65 kJ/(kg·K) and 2.1 kJ/(kg·K), respectively [2].

224 A multicriteria method was used to determine the optimal setting values for different charging  
 225 standards [54]. In the Q-charging, T-charging, and t-charging standards,  $Q_{se,sv}$ ,  $T_{ot,sv}$ , and  $\varepsilon_{ct,sv}$   
 226 were considered as optimization variables, respectively. The aim of optimization was to maximize  
 227 the overall performance score by identifying the optimal setting values. Three cases were  
 228 considered when the multi-criteria method was used. In the first case,  $\varepsilon_{ct}$  and  $Q_{se}$  were considered.  
 229 The overall performance score in this case ( $OS_{cs}$ ) was calculated using Eq. (4):

$$230 \quad OS_{cs} = \alpha_{\varepsilon_{ct}} \cdot OS_{\varepsilon_{ct}} + \alpha_{Q_{se}} \cdot OS_{Q_{se}} \quad (4)$$

231 where  $\alpha_{\varepsilon_{ct}}$  and  $\alpha_{Q_{se}}$  are user-specified weight factors. Note that the sum of  $\alpha_{\varepsilon_{ct}}$  and  $\alpha_{Q_{se}}$  is 1. In  
 232 the second case,  $\varepsilon_{ct}$ ,  $Q_{se}$ , and  $E_{tu}$  were considered. The overall performance score ( $OS_{cst}$ ) was  
 233 calculated using Eq. (5):

$$234 \quad OS_{cst} = \alpha_{\varepsilon_{ct}} \cdot OS_{\varepsilon_{ct}} + \alpha_{Q_{se}} \cdot OS_{Q_{se}} + \alpha_{E_{tu}} \cdot OS_{E_{tu}} \quad (5)$$

235 where  $\alpha_{E_{tu}}$  is the user-specified weight factor. Note that the sum of  $\alpha_{\varepsilon_{ct}}$ ,  $\alpha_{Q_{se}}$ , and  $\alpha_{E_{tu}}$  is 1. In the  
 236 third case,  $\varepsilon_{ct}$  and  $COP_{st}$  were considered. The overall performance score ( $OS_{cp}$ ) was calculated  
 237 using Eq. (6):

$$238 \quad OS_{cp} = \alpha_{\varepsilon_{ct}} \cdot OS_{\varepsilon_{ct}} + \alpha_{COP_{st}} \cdot OS_{COP_{st}} \quad (6)$$

239 where  $\alpha_{COP_{st}}$  is the user-specified weight factor. Note that the sum of  $\alpha_{\varepsilon_{ct}}$  and  $\alpha_{COP_{st}}$  is 1. For the  
 240 formulas for calculating the overall performance score in different cases, i.e., Eqs. (4)–(6), refer to  
 241 the studies of Li et al. [2, 54]. In [2], the formula for calculating the overall performance score was  
 242 the same as Eq. (6). In [54], the formula for calculating the overall performance score considered  
 243 the initial cost, total electricity use ( $E_{tu}$ ), thermal discomfort ratio, and operating cost.

244

245  $OS_{\varepsilon_{ct}}$ ,  $OS_{Q_{se}}$ ,  $OS_{E_{tu}}$ , and  $OS_{COP_{st}}$  are respectively determined using Eqs. (7)–(10):

$$246 \quad OS_{\varepsilon_{ct}} = \frac{\varepsilon_{ct} - \varepsilon_{ct,lf}}{\varepsilon_{ct,mf} - \varepsilon_{ct,lf}} \quad (7)$$

$$247 \quad OS_{Q_{se}} = \frac{Q_{se} - Q_{se,lf}}{Q_{se,mf} - Q_{se,lf}} \quad (8)$$

$$248 \quad OS_{E_{tu}} = \frac{E_{tu} - E_{tu,lf}}{E_{tu,mf} - E_{tu,lf}} \quad (9)$$

$$249 \quad OS_{COP_{st}} = \frac{COP_{st} - COP_{st,lf}}{COP_{st,mf} - COP_{st,lf}} \quad (10)$$

250 where  $lf$  and  $mf$  represent the least and most preferred circumstances, respectively. For the  
 251 formulas for calculating  $OS_{\varepsilon_{ct}}$ ,  $OS_{Q_{se}}$ ,  $OS_{E_{tu}}$ , and  $OS_{COP_{st}}$ , i.e., Eqs. (7)–(10), which are normalized

252 as  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$ , respectively, refer to the studies of Li et al. [2, 54]. In [2],  $\varepsilon_{ct}$  and  
253  $COP_{st}$  are normalized. In [54], the initial cost,  $E_{tu}$ , thermal discomfort ratio, and operating cost  
254 were normalized.

255

#### 256 **4. Results and discussion**

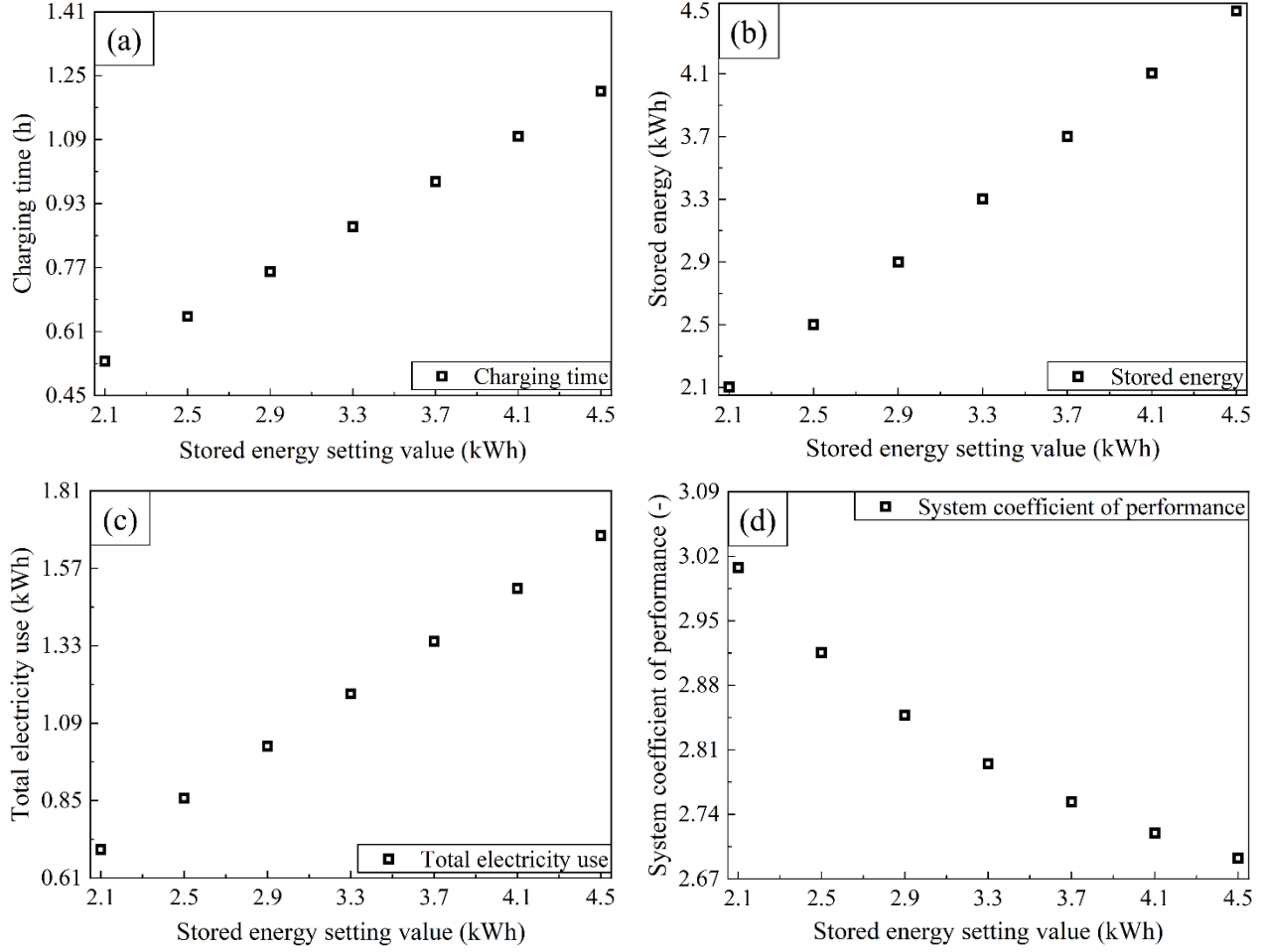
257 This section presents the results and discussion in Q-charging, T-charging, and t-charging  
258 standards.  $Q_{se,sv}$ ,  $T_{ot,sv}$ , and  $\varepsilon_{ct,sv}$  are considered as decision variables in Q-charging, T-charging,  
259 and t-charging standards, respectively.  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  are considered as performance  
260 indicators.

261

##### 262 4.1. Results and discussion in the Q-charging standard

263 In this section, we analyze the effects of  $Q_{se,sv}$  on  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  in the Q-charging  
264 standard. Fig. 3 depicts the variations of  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  with  $Q_{se,sv}$  when ACHP is  
265 utilized. In Fig. 3(a),  $\varepsilon_{ct}$  linearly increased with the increase in  $Q_{se,sv}$ . This implies that more time  
266 is required to complete the charging process to satisfy higher energy demands. As shown in Fig.  
267 3(b),  $Q_{se}$  increased linearly with an increase in  $Q_{se,sv}$ . The  $Q_{se}$  values were almost identical to  
268 those of  $Q_{se,sv}$ , indicating that the Q-charging standard was successfully achieved. As shown in  
269 Fig. 3(c),  $E_{tu}$  increases linearly with  $Q_{se,sv}$ . This means that more electricity is required to satisfy  
270 higher energy demands. As shown in Fig. 3(d),  $COP_{st}$  reduced as  $Q_{se,sv}$  increased. According to  
271 Eq. (3), this phenomenon implies that the degree of increase in  $Q_{se}$  with  $Q_{se,sv}$  is smaller than that  
272 of  $E_{tu}$  with  $Q_{se,sv}$ . For instance,  $Q_{se}$  was 2.1 kWh and 2.5 kWh when  $Q_{se,sv}$  was 2.1 kWh and 2.5  
273 kWh, respectively.  $E_{tu}$  was 0.7 kWh and 0.86 kWh when  $Q_{se,sv}$  was 2.1 kWh and 2.5 kWh,  
274 respectively. Thus, when  $Q_{se,sv}$  increased from 2.1 kWh to 2.5 kWh,  $Q_{se}$  and  $E_{tu}$  increased by 19%  
275 and 22.8%, respectively. This indicates that the increasing degree of  $Q_{se}$  with  $Q_{se,sv}$  is smaller than  
276 that of  $E_{tu}$  with  $Q_{se,sv}$ . According to Eq. (3),  $COP_{st}$  was 3 and 2.92 when  $Q_{se,sv}$  was 2.1 kWh and  
277 2.5 kWh, respectively. Thus, the phenomenon of the increasing degree of  $Q_{se}$  with  $Q_{se,sv}$  was  
278 smaller than that of  $E_{tu}$  with  $Q_{se,sv}$  caused that  $COP_{st}$  reduced as  $Q_{se,sv}$  increased.

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**Fig. 3.** (a)  $\varepsilon_{ct}$ , (b)  $Q_{se}$ , (c)  $E_{tu}$ , and (d)  $COP_{st}$  in different  $Q_{se,sv}$  when ACHP is utilized

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Fig. 4 depicts the variations in  $OS_{CS}$ ,  $OS_{Cst}$ , and  $OS_{Cp}$  with  $Q_{se,sv}$  when ACHP is utilized. In Fig. 4(a), the optimal  $Q_{se,sv}$  were 4.5 kWh and 2.1 kWh in situations when  $\alpha_{\varepsilon_{ct}} : \alpha_{Q_{se}}$  were 0.3:0.7 and 0.7:0.3, respectively. When  $\alpha_{\varepsilon_{ct}} : \alpha_{Q_{se}}$  was 0.5:0.5, the variation of  $OS_{CS}$  with  $Q_{se,sv}$  was small; the optimal  $Q_{se,sv}$  was 3.3 kWh. Thus, the larger  $\alpha_{\varepsilon_{ct}}$  would cause the optimal  $Q_{se,sv}$  to occur at a smaller value. In Fig. 4(b), the optimal  $Q_{se,sv}$  was 2.1 kWh when  $\alpha_{\varepsilon_{ct}} : \alpha_{Q_{se}} : \alpha_{E_{tu}}$  were 0.2:0.3:0.5 and 0.3:0.4:0.3. When  $\alpha_{\varepsilon_{ct}} : \alpha_{Q_{se}} : \alpha_{E_{tu}}$  was 0.2:0.5:0.3, the variation of  $OS_{Cst}$  with  $Q_{se,sv}$  was small; the optimal  $Q_{se,sv}$  was 3.3 kWh. Thus, it seemed that the smaller  $\alpha_{Q_{se}}$  would cause the optimal  $Q_{se,sv}$  to occur at the smaller value. In Fig. 4(c), the optimal  $Q_{se,sv}$  is 2.1 kWh irrespective of  $\alpha_{\varepsilon_{ct}} : \alpha_{COP_{st}}$  being 0.3:0.7, 0.5:0.5, or 0.7:0.3. Thus, regardless of whether  $\varepsilon_{ct}$  had a larger or smaller weighting than  $COP_{st}$ , the optimal  $Q_{se,sv}$  occurred at a smaller value.

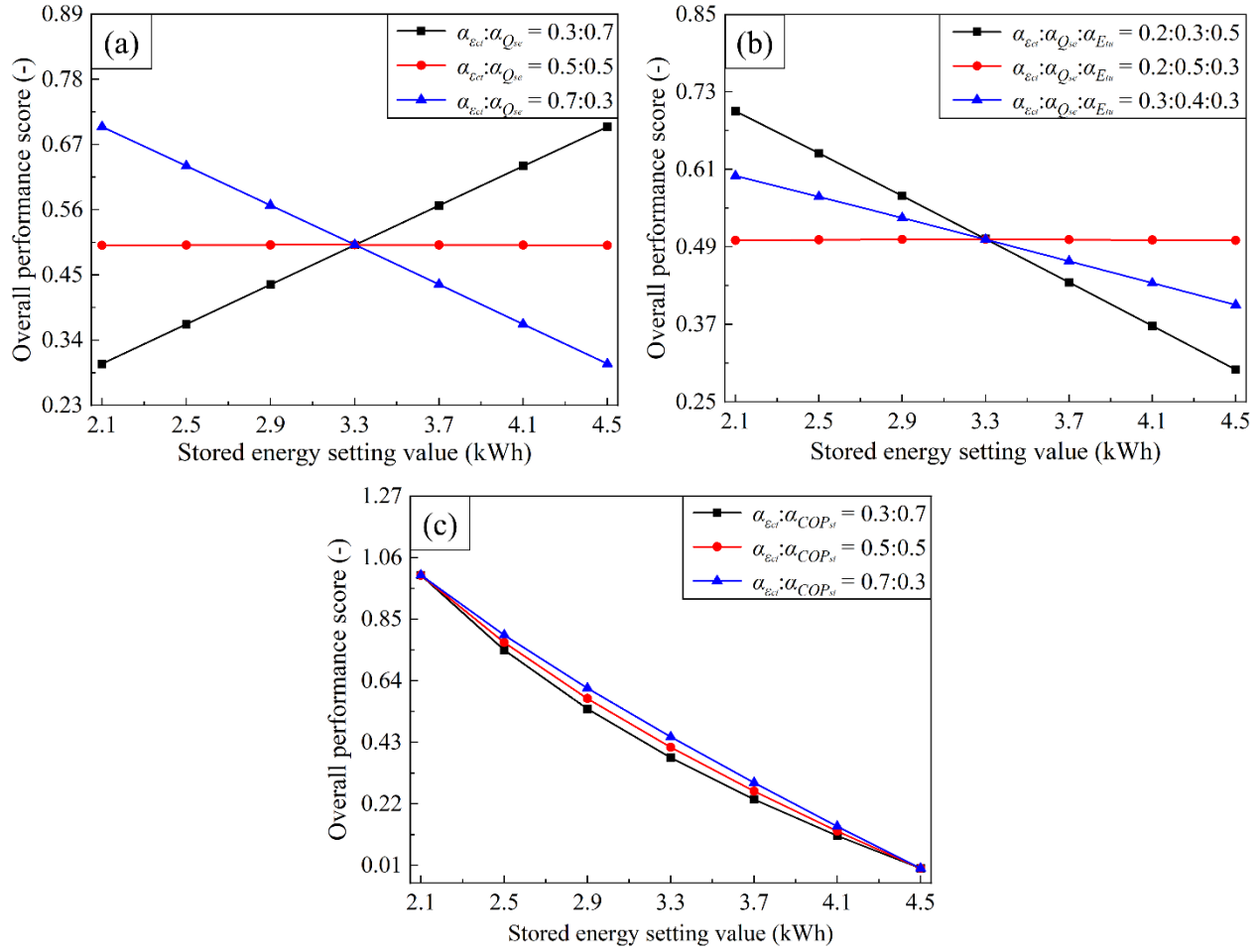
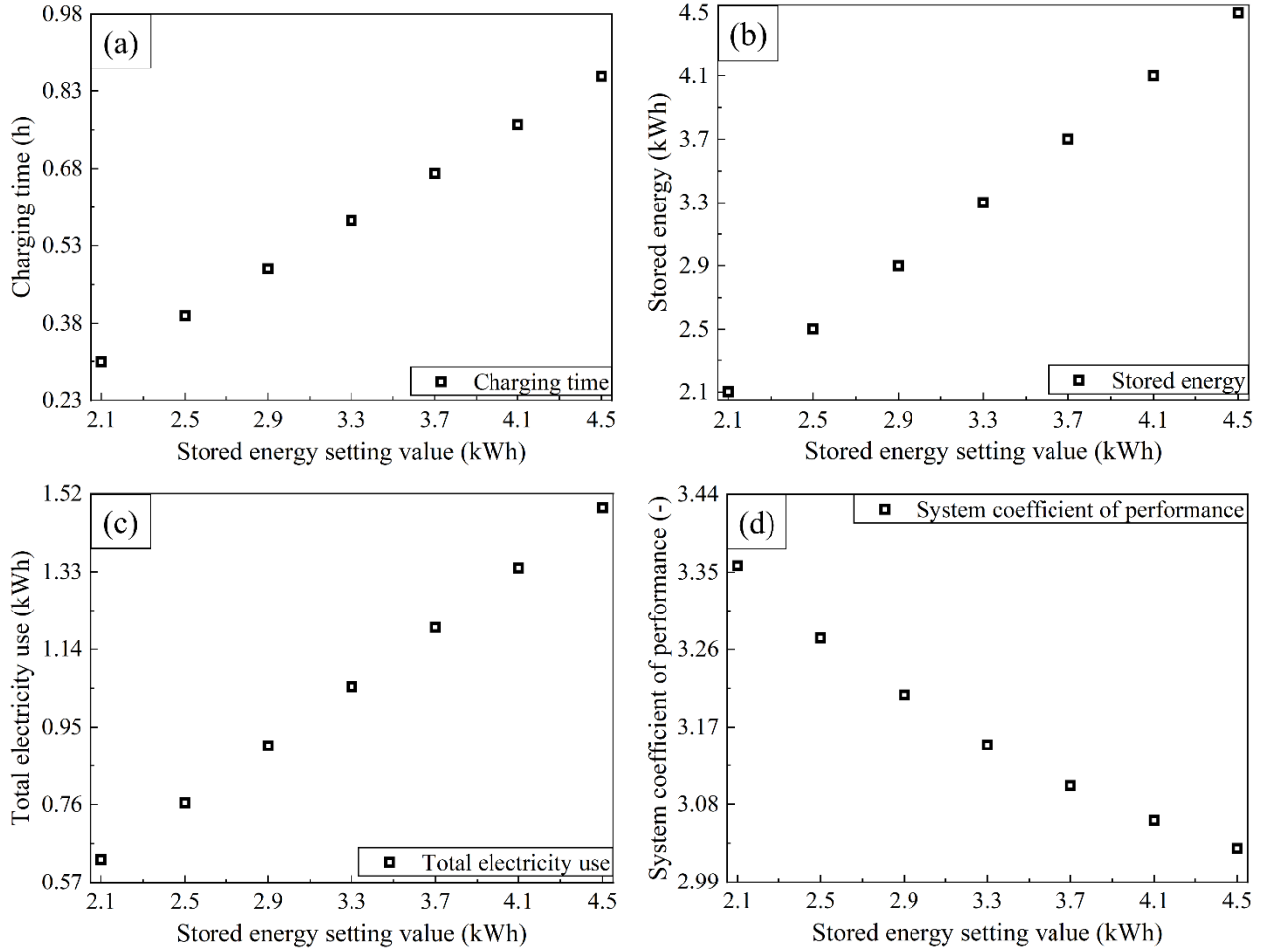


Fig. 4. (a)  $OS_{CS}$ , (b)  $OS_{Cst}$ , and (c)  $OS_{Cp}$  in different  $Q_{se,sv}$  when ACHP is utilized

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 298  
 299 Fig. 5 depicts the variations of  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  with  $Q_{se,sv}$  when WCHP is utilized. In Fig.  
 300 5(a),  $\varepsilon_{ct}$  linearly increased as  $Q_{se,sv}$  increased. This implies that more time is required to complete  
 301 the charging process to satisfy higher energy demands. As shown in Fig. 5(b),  $Q_{se}$  increased  
 302 linearly with an increase in  $Q_{se,sv}$ . The  $Q_{se}$  values were almost identical to those of  $Q_{se,sv}$ ,  
 303 indicating that the Q-charging standard was successfully achieved. As shown in Fig. 5(c),  $E_{tu}$   
 304 increased linearly with  $Q_{se,sv}$ . This means that more electricity is required to satisfy higher energy  
 305 demands. As shown in Fig. 5(d),  $COP_{st}$  decreases as  $Q_{se,sv}$  increases. According to Eq. (3), this  
 306 phenomenon implies that the degree of increase in  $Q_{se}$  with  $Q_{se,sv}$  is smaller than that of  $E_{tu}$  with  
 307  $Q_{se,sv}$ . For instance,  $Q_{se}$  was 2.1 kWh and 2.5 kWh when  $Q_{se,sv}$  was 2.1 kWh and 2.5 kWh,  
 308 respectively.  $E_{tu}$  was 0.63 kWh and 0.76 kWh when  $Q_{se,sv}$  was 2.1 kWh and 2.5 kWh, respectively.  
 309 Thus, when  $Q_{se,sv}$  increased from 2.1 kWh to 2.5 kWh,  $Q_{se}$  and  $E_{tu}$  increased by 19% and 22.1%,

310 respectively. This indicates that the increasing degree of  $Q_{se}$  with  $Q_{se,sv}$  is smaller than that of  $E_{tu}$   
 311 with  $Q_{se,sv}$ . According to Eq. (3),  $COP_{st}$  was 3.36 and 3.27 when  $Q_{se,sv}$  was 2.1 kWh and 2.5 kWh,  
 312 respectively. Thus, the phenomenon of the increasing degree of  $Q_{se}$  with  $Q_{se,sv}$  was smaller than  
 313 that of  $E_{tu}$  with  $Q_{se,sv}$  caused that  $COP_{st}$  reduced as  $Q_{se,sv}$  increased.

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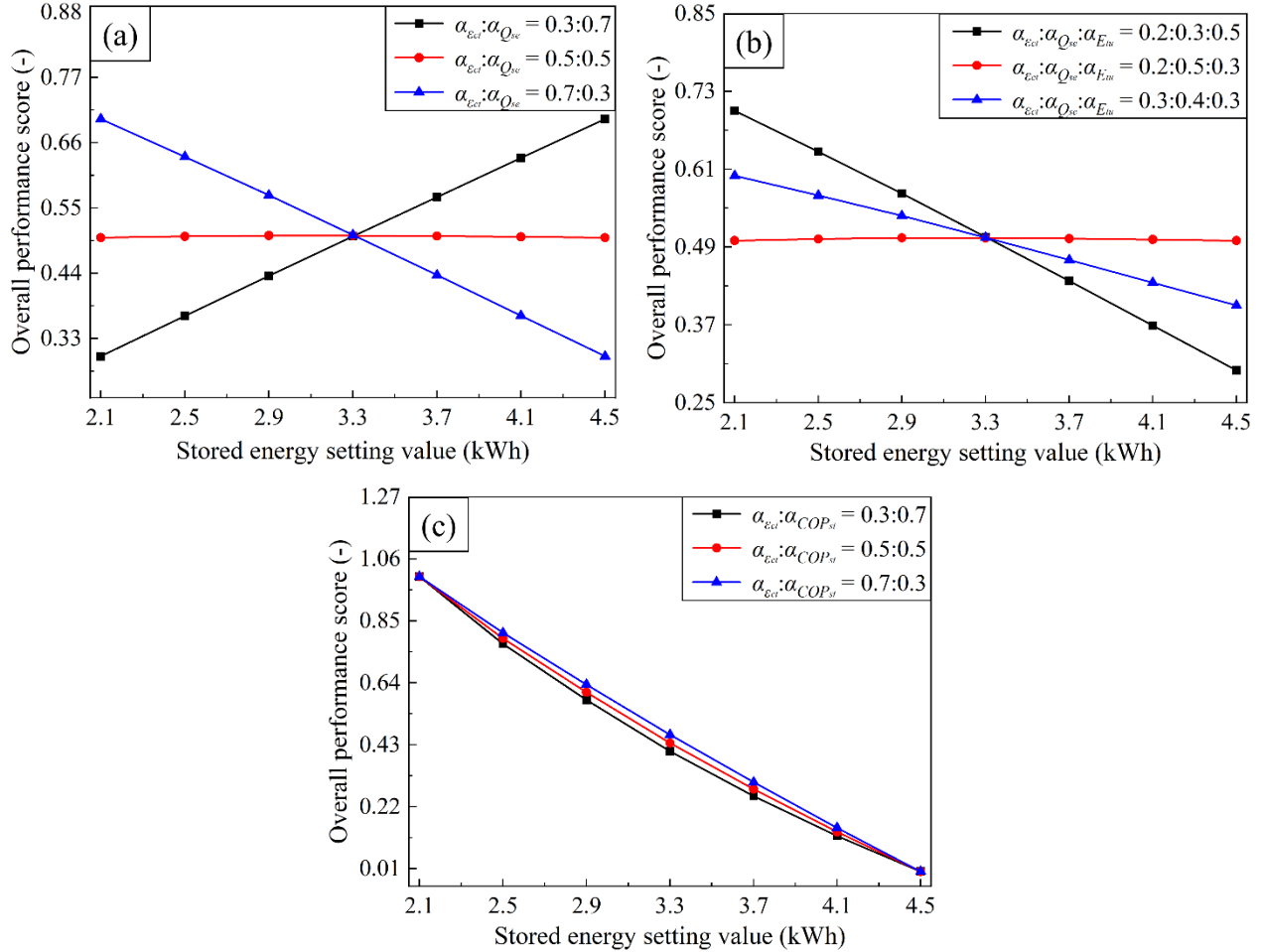
**Fig. 5.** (a)  $\varepsilon_{ct}$ , (b)  $Q_{se}$ , (c)  $E_{tu}$ , and (d)  $COP_{st}$  in different  $Q_{se,sv}$  when WCHP is utilized

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319 Fig. 6 depicts the variations in  $OS_{cs}$ ,  $OS_{cst}$ , and  $OS_{cp}$  with  $Q_{se,sv}$  when the WCHP system is  
 320 utilized. In Fig. 6(a), the optimal  $Q_{se,sv}$  were 4.5 kWh and 2.1 kWh in situations when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$   
 321 were 0.3:0.7 and 0.7:0.3, respectively. Although in the situation when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$  was 0.5:0.5, the  
 322 variation of  $OS_{cs}$  with  $Q_{se,sv}$  was small; the optimal  $Q_{se,sv}$  was 2.9 kWh. Thus, larger  $\alpha_{\varepsilon_{ct}}$  might  
 323 cause the optimal  $Q_{se,sv}$  to occur at a lower value. In Fig. 6(b), the optimal  $Q_{se,sv}$  was 2.1 kWh in  
 324 situations when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}:\alpha_{E_{tu}}$  was 0.2:0.3:0.5 and 0.3:0.4:0.3. Although when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}:\alpha_{E_{tu}}$

325 was 0.2:0.5:0.3, the variation of  $OS_{cst}$  with  $Q_{se,sv}$  was small. The optimal  $Q_{se,sv}$  was 2.9 kWh.  
 326 Thus, the smaller  $\alpha_{Q_{se}}$  would cause the optimal  $Q_{se,sv}$  to occur at the lower value. In Fig. 6(c), the  
 327 optimal  $Q_{se,sv}$  is 2.1 kWh irrespective of  $\alpha_{\varepsilon_{ct}}:\alpha_{COP_{st}}$  being 0.3:0.7, 0.5:0.5, or 0.7:0.3. Thus,  
 328 regardless of whether  $\varepsilon_{ct}$  had a larger or smaller weighting than  $COP_{st}$ , the optimal  $Q_{se,sv}$  occurred  
 329 at a lower value.

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**Fig. 6.** (a)  $OS_{CS}$ , (b)  $OS_{cst}$ , and (c)  $OS_{cp}$  in different  $Q_{se,sv}$  when WCHP is utilized

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For the ACHP,  $\varepsilon_{ct}$ ,  $Q_{se}$ , and  $E_{tu}$  increased by 126.1%, 114.2%, and 139.3%, respectively, when  $Q_{se,sv}$  increased from 2.1 kWh to 4.5 kWh.  $COP_{st}$  was reduced by 10.5% when  $Q_{se,sv}$  increased from 2.1 kWh to 4.5 kWh. For the WCHP,  $\varepsilon_{ct}$ ,  $Q_{se}$ , and  $E_{tu}$  increased by 181.8%, 114.2%, and 137.5%, respectively, when  $Q_{se,sv}$  increased from 2.1 kWh to 4.5 kWh.  $COP_{st}$  was reduced by 9.8% when  $Q_{se,sv}$  increased from 2.1 kWh to 4.5 kWh. For ACHP and WCHP, in the multi-criteria

340 optimization considering  $\varepsilon_{ct}$  and  $Q_{se}$ , the effect of  $\alpha_{\varepsilon_{ct}}$  on the optimal  $Q_{se,sv}$  was almost the same  
341 as that of  $\alpha_{Q_{se}}$  on the optimal  $Q_{se,sv}$ . In the multi-criteria optimization considering  $\varepsilon_{ct}$ ,  $Q_{se}$ , and  
342  $E_{tu}$ , the effect of  $\alpha_{Q_{se}}$  on the optimal  $Q_{se,sv}$  was larger than that of  $\alpha_{\varepsilon_{ct}}$  and  $\alpha_{E_{tu}}$  on the optimal  
343  $Q_{se,sv}$ . In the multi-criteria optimization considering  $\varepsilon_{ct}$  and  $COP_{st}$ , the optimal  $Q_{se,sv}$  was not  
344 affected by  $\alpha_{Q_{se}}$  and  $\alpha_{COP_{st}}$ .

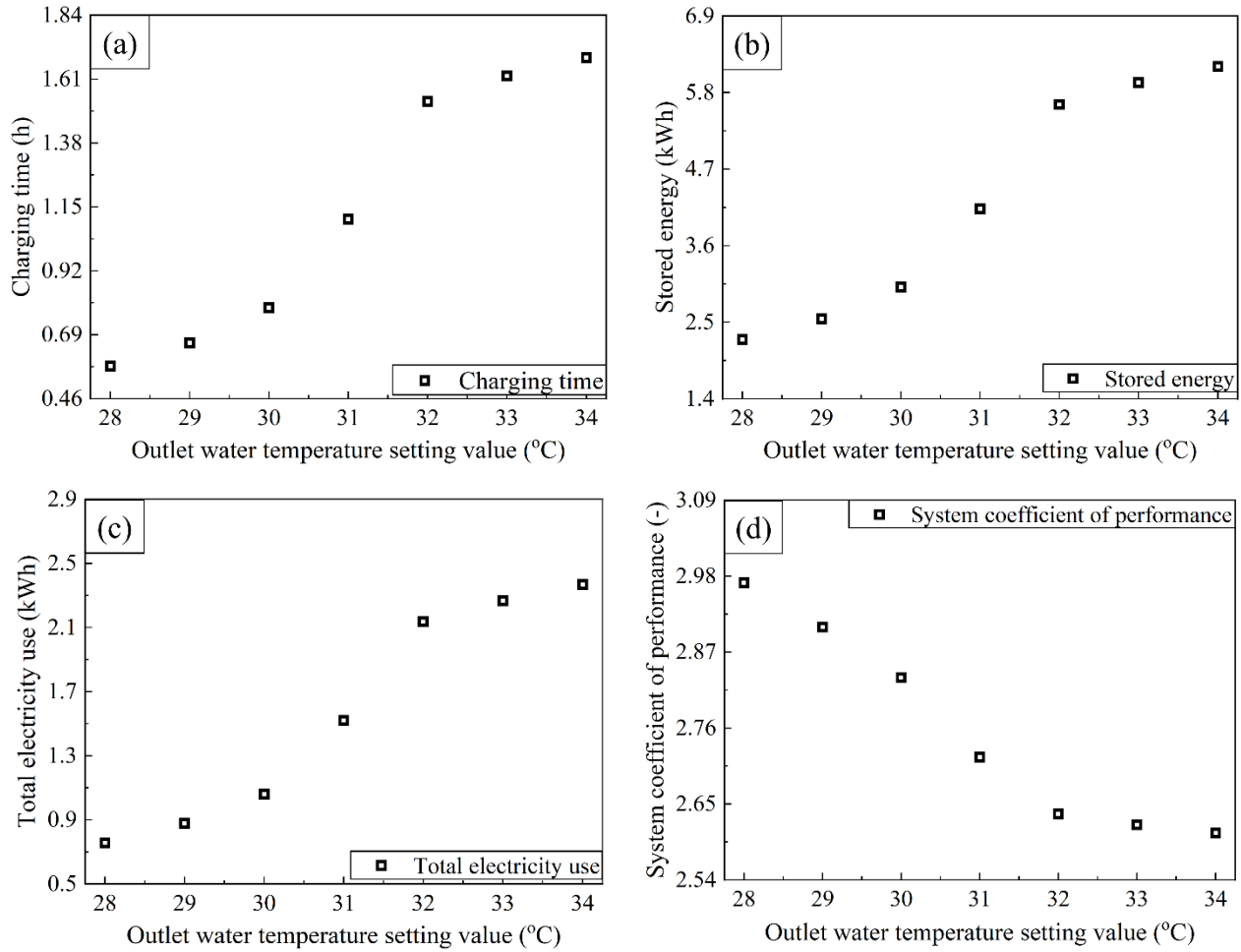
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#### 346 4.2. Results and discussion in the T-charging standard

347 In this section, we analyze the effects of  $T_{ot,sv}$  on  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  in the T-charging  
348 standard. Fig. 7 depicts the variations of  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  with  $T_{ot,sv}$  when ACHP was  
349 utilized. In Fig. 7(a),  $\varepsilon_{ct}$  increased as  $T_{ot,sv}$  increased. This implies that more time is required to  
350 complete the charging process to satisfy the higher outlet water temperature demands. As shown  
351 in Fig. 7(b),  $Q_{se}$  increased as  $T_{ot,sv}$  increased. As shown in Fig. 7(c),  $E_{tu}$  increases as  $T_{ot,sv}$   
352 increases. This means that more electricity is required to satisfy the higher outlet water temperature  
353 demands. As shown in Fig. 7 (d),  $COP_{st}$  reduced as  $T_{ot,sv}$  increased. According to Eq. (3), this  
354 phenomenon implies that the degree of increase in  $Q_{se}$  with  $T_{ot,sv}$  is smaller than that of  $E_{tu}$  with  
355  $T_{ot,sv}$ . For instance,  $Q_{se}$  was 2.2 kWh and 2.5 kWh when  $T_{ot,sv}$  was 28 °C and 29 °C, respectively.  
356  $E_{tu}$  was 0.76 kWh and 0.88 kWh when  $T_{ot,sv}$  was 28 °C and 29 °C, respectively. Thus, when  $T_{ot,sv}$   
357 increased from 28 °C to 29 °C,  $Q_{se}$  and  $E_{tu}$  increased by 13.3% and 15.8%, respectively. This  
358 indicates that the increasing degree of  $Q_{se}$  with  $T_{ot,sv}$  is smaller than that of  $E_{tu}$  with  $T_{ot,sv}$ .  
359 According to Eq. (3),  $COP_{st}$  was 2.97 and 2.9 when  $T_{ot,sv}$  was 28 °C and 29 °C, respectively. Thus,  
360 the phenomenon of the increasing degree of  $Q_{se}$  with  $T_{ot,sv}$  was smaller than that of  $E_{tu}$  with  $T_{ot,sv}$   
361 caused that  $COP_{st}$  reduced as  $T_{ot,sv}$  increased.

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**Fig. 7.** (a)  $\varepsilon_{ct}$ , (b)  $Q_{se}$ , (c)  $E_{tu}$ , and (d)  $COP_{st}$  in different  $T_{ot,sv}$  when ACHP is utilized

367 Fig. 8 shows the variations in  $OS_{cs}$ ,  $OS_{cst}$ , and  $OS_{cp}$  with  $T_{ot,sv}$  when the WCHP system was  
 368 utilized. In Fig. 8(a), the optimal  $T_{ot,sv}$  values were 34 °C and 28 °C when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$  were 0.3:0.7  
 369 and 0.7:0.3, respectively. When  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$  was 0.5:0.5, the variation of  $OS_{cs}$  with  $T_{ot,sv}$  was small;  
 370 the optimal  $T_{ot,sv}$  was 31 °C. Thus, the larger  $\alpha_{\varepsilon_{ct}}$  might cause the optimal  $T_{ot,sv}$  to occur at a lower  
 371 value. In Fig. 8(b), the optimal  $T_{ot,sv}$  was 28 °C when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}:\alpha_{E_{tu}}$  was 0.2:0.3:0.5 and  
 372 0.3:0.4:0.3. When  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}:\alpha_{E_{tu}}$  was 0.2:0.5:0.3, the variation of  $OS_{cst}$  with  $T_{ot,sv}$  was small; the  
 373 optimal  $T_{ot,sv}$  was 31 °C. Thus, it seemed that the smaller  $\alpha_{Q_{se}}$  would cause the optimal  $T_{ot,sv}$  to  
 374 occur at a lower value. In Fig. 8(c), the optimal  $T_{ot,sv}$  was 28 °C irrespective of  $\alpha_{\varepsilon_{ct}}:\alpha_{COP_{st}}$  being  
 375 0.3:0.7, 0.5:0.5, or 0.7:0.3. Thus, regardless of whether  $\varepsilon_{ct}$  had a higher or lower weight than  $COP_{st}$ ,  
 376 the optimal  $T_{ot,sv}$  had a lower value.

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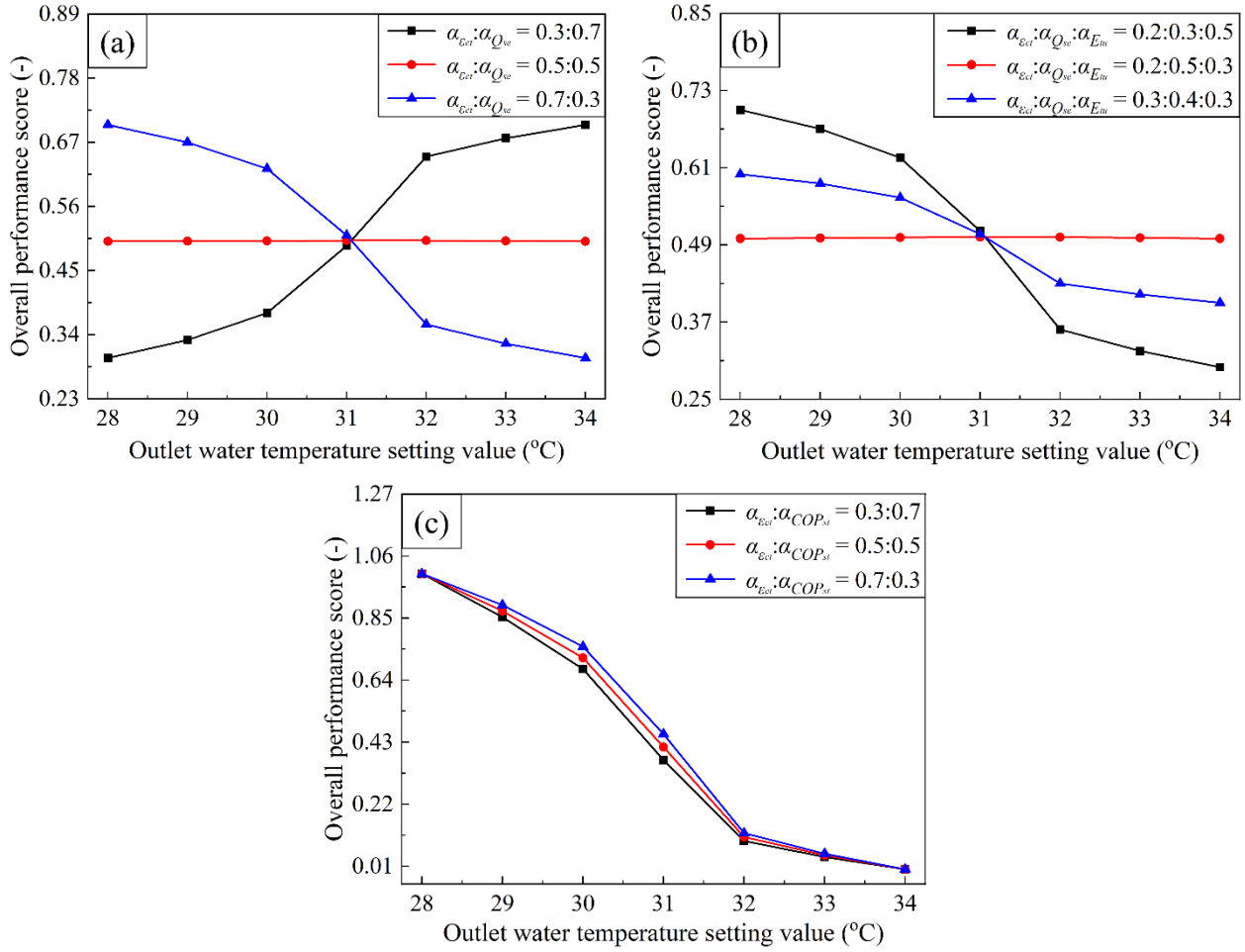


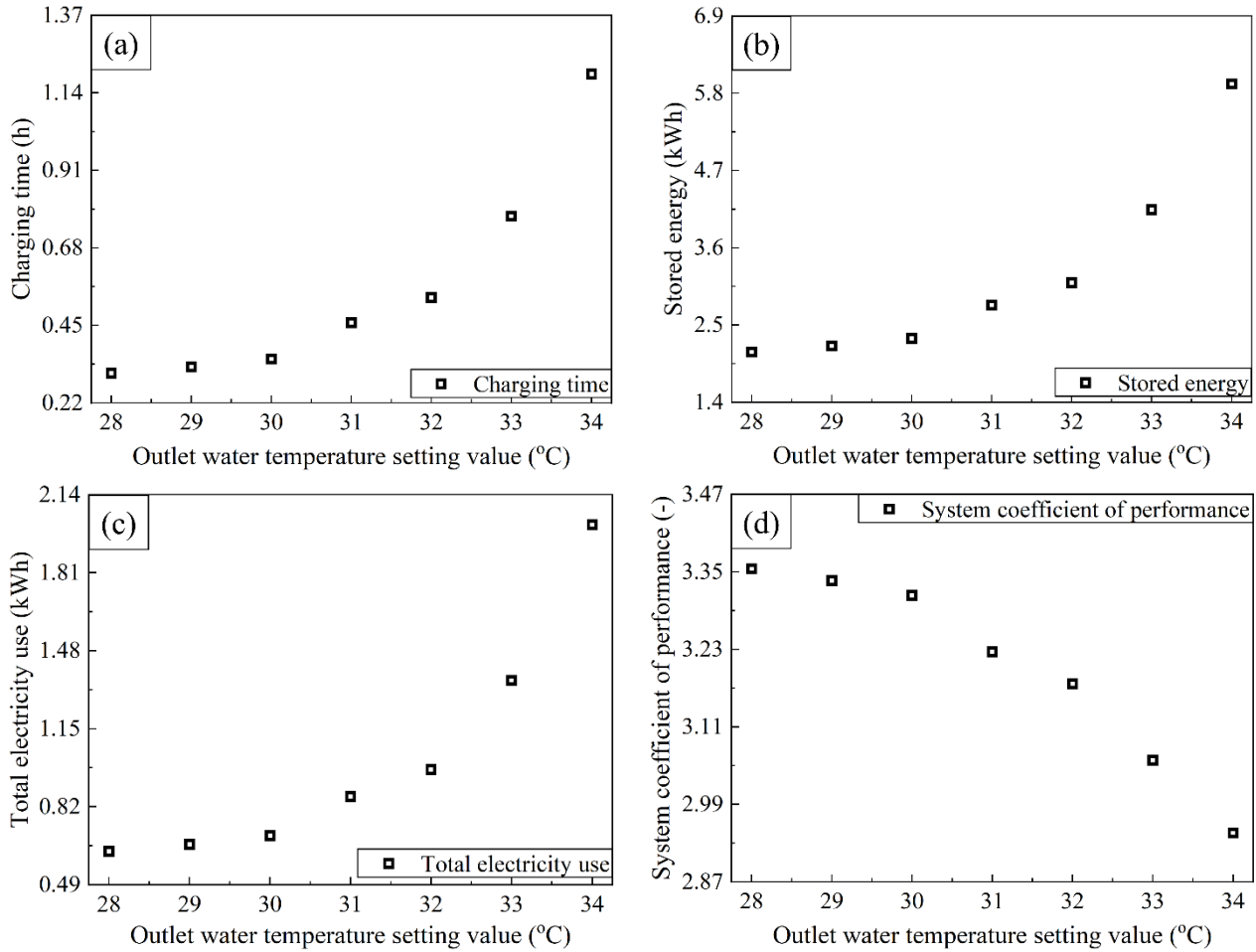
Fig. 8. (a)  $OS_{CS}$ , (b)  $OS_{CST}$ , and (c)  $OS_{CP}$  in different  $T_{ot,sv}$  when ACHP is utilized

In previous studies [2], T-charging standard was not considered, and  $T_{ot,sv}$  was fixed at 30 °C. In Fig. 8(a), when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$  was 0.3:0.7,  $OS_{CS}$  was 46.1% smaller when  $T_{ot,sv}$  was 30 °C than that at 34 °C. When  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$  was 0.7:0.3,  $OS_{CS}$  was 10.8% smaller when  $T_{ot,sv}$  was 30 °C than that at 28 °C. In Fig. 8(b), when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}:\alpha_{E_{tu}}$  was 0.2:0.5:0.3 and 0.3:0.4:0.3, the respective  $OS_{CS}$  values were 10.6% and 6.1% smaller when  $T_{ot,sv}$  was 30 °C than that at 28 °C. In Fig. 8(c), when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$  were 0.3:0.7, 0.5:0.5, and 0.7:0.3,  $OS_{CS}$  values were 32.2%, 28.4%, and 24.7% smaller when  $T_{ot,sv}$  was 30 °C than that at 28 °C, respectively.

Fig. 9 depicts the variations of  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  with  $T_{ot,sv}$  when WCHP was utilized. In Fig. 9(a),  $\varepsilon_{ct}$  increased as  $T_{ot,sv}$  increased. This implies that more time is required to complete the charging process to satisfy the higher outlet water temperature demands. As shown in Fig. 9(b),

393  $Q_{se}$  increased as  $T_{ot,sv}$  increased. As shown in Fig. 9(c),  $E_{tu}$  increases as  $T_{ot,sv}$  increases. This  
 394 means that more electricity is required to satisfy the higher outlet water temperature demands. As  
 395 shown in Fig. 9(d),  $COP_{st}$  reduced as  $T_{ot,sv}$  increased. According to Eq. (3), this phenomenon  
 396 implies that the degree of increase in  $Q_{se}$  with  $T_{ot,sv}$  is smaller than that of  $E_{tu}$  with  $T_{ot,sv}$ . For  
 397 instance,  $Q_{se}$  was 2.1 kWh and 2.2 kWh when  $T_{ot,sv}$  was 28 °C and 29 °C, respectively.  $E_{tu}$  was  
 398 0.63 kWh and 0.66 kWh when  $T_{ot,sv}$  was 28 °C and 29 °C, respectively. Thus, when  $T_{ot,sv}$   
 399 increased from 28 °C to 29 °C,  $Q_{se}$  and  $E_{tu}$  increased by 4% and 4.6%, respectively. This indicates  
 400 that the increasing degree of  $Q_{se}$  with  $T_{ot,sv}$  is smaller than that of  $E_{tu}$  with  $T_{ot,sv}$ . According to  
 401 Eq. (3),  $COP_{st}$  was 3.35 and 3.34 when  $T_{ot,sv}$  was 28 °C and 29 °C, respectively. Thus, the  
 402 phenomenon of the increasing degree of  $Q_{se}$  with  $T_{ot,sv}$  was smaller than that of  $E_{tu}$  with  $T_{ot,sv}$   
 403 caused that  $COP_{st}$  reduced as  $T_{ot,sv}$  increased.

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**Fig. 9.** (a)  $\varepsilon_{ct}$ , (b)  $Q_{se}$ , (c)  $E_{tu}$ , and (d)  $COP_{st}$  in different  $T_{ot,sv}$  when WCHP is utilized

409 Fig. 10 shows the variations in  $OS_{CS}$ ,  $OS_{Cst}$ , and  $OS_{CP}$  with  $T_{ot,sv}$  when the WCHP system was  
 410 utilized. In Fig. 10(a), the optimal  $T_{ot,sv}$  were 34 °C and 28 °C when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$  were 0.3:0.7 and  
 411 0.7:0.3, respectively. When  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$  was 0.5:0.5, the variation of  $OS_{CS}$  with  $T_{ot,sv}$  was small; the  
 412 optimal  $T_{ot,sv}$  was 32 °C. Thus, the larger  $\alpha_{\varepsilon_{ct}}$  might cause the optimal  $T_{ot,sv}$  to occur at a lower  
 413 value. In Fig. 10(b), the optimal  $T_{ot,sv}$  was 28 °C when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}:\alpha_{E_{tu}}$  was 0.2:0.3:0.5 and  
 414 0.3:0.4:0.3. When  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}:\alpha_{E_{tu}}$  was 0.2:0.5:0.3, the variation of  $OS_{Cst}$  with  $T_{ot,sv}$  was small; the  
 415 optimal  $T_{ot,sv}$  was 32 °C. Thus, it seemed that the smaller  $\alpha_{Q_{se}}$  would cause the optimal  $T_{ot,sv}$  to  
 416 occur at the lower value. In Fig. 10(c), the optimal  $T_{ot,sv}$  was 28 °C irrespective of  $\alpha_{\varepsilon_{ct}}:\alpha_{COP_{st}}$   
 417 being 0.3:0.7, 0.5:0.5, or 0.7:0.3. Thus, regardless of whether  $\varepsilon_{ct}$  had a larger or smaller weighting  
 418 than  $COP_{st}$ , the optimal  $T_{ot,sv}$  occurred at a lower value.

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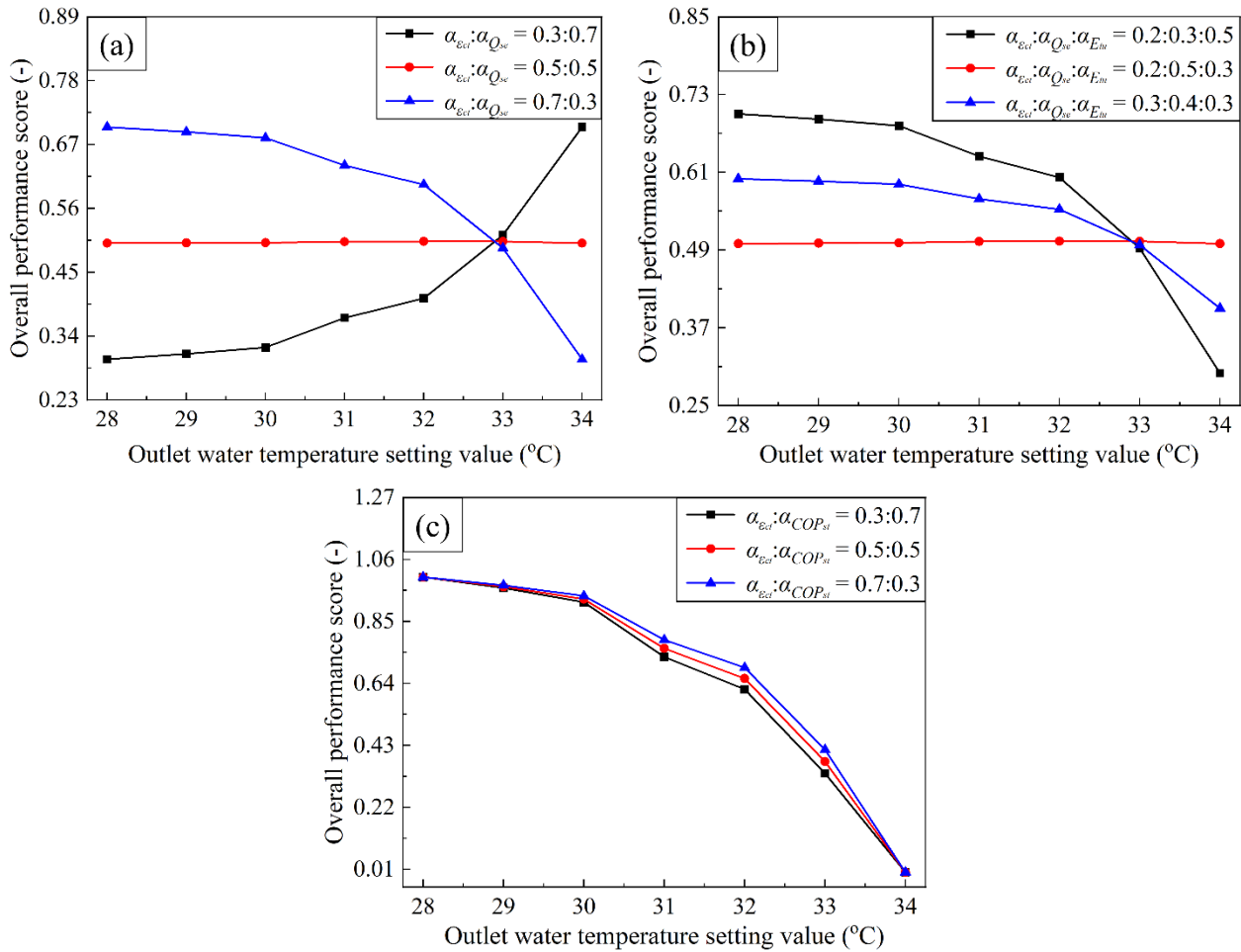


Fig. 10. (a)  $OS_{CS}$ , (b)  $OS_{Cst}$ , and (c)  $OS_{CP}$  in different  $T_{ot,sv}$  when WCHP is utilized

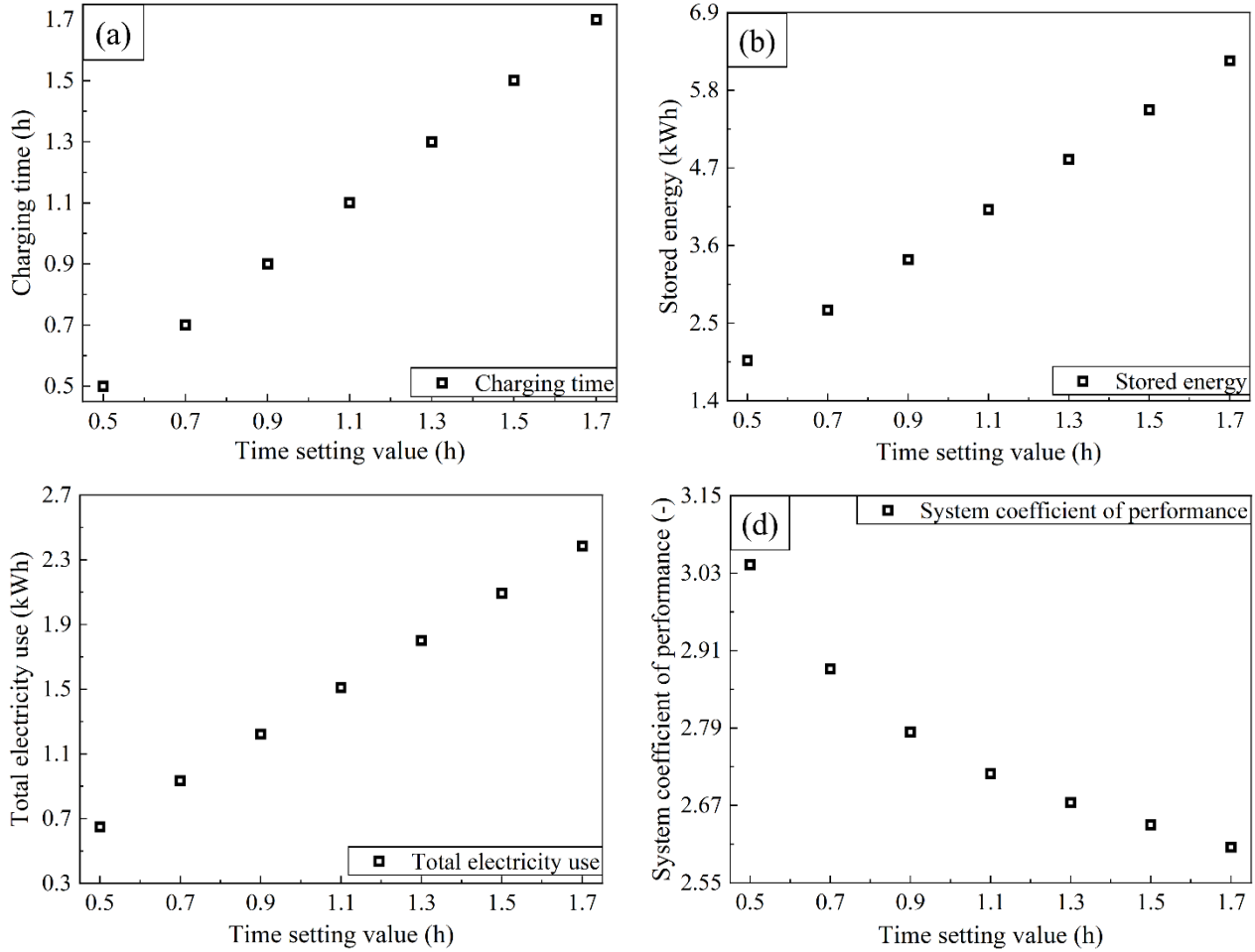
424 In previous studies [2], T-charging standard was not considered, and  $T_{ot,sv}$  was fixed at 30 °C. In  
 425 Fig. 10(a), when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$  was 0.3:0.7,  $OS_{CS}$  was 54.2% smaller when  $T_{ot,sv}$  was 30 °C than that  
 426 at 34 °C. When  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$  was 0.7:0.3,  $OS_{CS}$  was 2.7% smaller when  $T_{ot,sv}$  was 30°C than that at  
 427 28 °C. In Fig. 10(b), when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}:\alpha_{E_{tu}}$  was 0.2:0.5:0.3 and 0.3:0.4:0.3, the respective  $OS_{CS}$   
 428 values were 2.6% and 1.4% when  $T_{ot,sv}$  was 30 °C than that at 28 °C, respectively. In Fig. 10(c),  
 429 when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$  were 0.3:0.7, 0.5:0.5, and 0.7:0.3,  $OS_{CS}$  values were 8.5%, 7.4%, and 6.4% smaller  
 430 when  $T_{ot,sv}$  was 30 °C than that at 28 °C, respectively.

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 432 For the ACHP,  $\varepsilon_{ct}$ ,  $Q_{se}$ , and  $E_{tu}$  increased by 192.5%, 174.4%, and 212.5%, respectively, when  
 433  $T_{ot,sv}$  increased from 28 °C to 34 °C.  $COP_{st}$  was reduced by 12.2% when  $T_{ot,sv}$  increased from  
 434 28 °C to 34 °C. For the WCHP,  $\varepsilon_{ct}$ ,  $Q_{se}$ , and  $E_{tu}$  increased by 288.2%, 180.2%, and 219.1% when  
 435  $T_{ot,sv}$  increased from 28 °C to 34 °C.  $COP_{st}$  was reduced by 12.2% when  $T_{ot,sv}$  increased from  
 436 28 °C to 34 °C. For ACHP and WCHP, in the multi-criteria optimization considering  $\varepsilon_{ct}$  and  $Q_{se}$ ,  
 437 the effect of  $\alpha_{\varepsilon_{ct}}$  on the optimal  $T_{ot,sv}$  was almost the same as that of  $\alpha_{Q_{se}}$  on the optimal  $T_{ot,sv}$ . In  
 438 the multi-criteria optimization considering  $\varepsilon_{ct}$ ,  $Q_{se}$ , and  $E_{tu}$ , the effect of  $\alpha_{Q_{se}}$  on the optimal  $T_{ot,sv}$   
 439 was larger than that of  $\alpha_{\varepsilon_{ct}}$  and  $\alpha_{E_{tu}}$  on the optimal  $T_{ot,sv}$ . In the multi-criteria optimization  
 440 considering  $\varepsilon_{ct}$  and  $COP_{st}$ , the optimal  $T_{ot,sv}$  was not affected by  $\alpha_{Q_{se}}$  and  $\alpha_{COP_{st}}$ .

#### 441 442 4.3. Results and discussion in the t-charging standard

443 In this section, we analyze the effects of  $\varepsilon_{ct,sv}$  on  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  in the t-charging  
 444 standard. Fig. 11 depicts the variations of  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  with  $\varepsilon_{ct,sv}$  when ACHP is  
 445 utilized. In Fig. 11 (a),  $\varepsilon_{ct}$  linearly increased with the increase of  $\varepsilon_{ct,sv}$ . The  $\varepsilon_{ct}$  values were almost  
 446 the same as those of  $\varepsilon_{ct,sv}$ . This means that the t-charging standard was successfully achieved. In  
 447 Fig. 11(b),  $Q_{se}$  linearly increased with the increase of  $\varepsilon_{ct,sv}$ . This meant that more energy would  
 448 be stored if  $\varepsilon_{ct}$  was longer. In Fig. 11(c),  $E_{tu}$  linearly increased with the increase of  $\varepsilon_{ct,sv}$ . This  
 449 meant that more electricity would be utilized if  $\varepsilon_{ct}$  was longer. In Fig. 11(d),  $COP_{st}$  reduced as  
 450  $\varepsilon_{ct,sv}$  increased. According to Eq. (3), this phenomenon implies that the degree of increase in  $Q_{se}$   
 451 with  $\varepsilon_{ct,sv}$  is smaller than that of  $E_{tu}$  with  $\varepsilon_{ct,sv}$ . For instance,  $Q_{se}$  was 2 kWh and 2.7 kWh when  
 452  $\varepsilon_{ct,sv}$  was 0.5 h and 0.7 h, respectively.  $E_{tu}$  was 0.65 kWh and 0.93 kWh when  $\varepsilon_{ct,sv}$  was 0.5 h and  
 453 0.7 h, respectively. Thus, when  $\varepsilon_{ct,sv}$  increased from 0.5 h to 0.7 h,  $Q_{se}$  and  $E_{tu}$  increased by 36.2%

454 and 43.9%, respectively. This indicates that the increasing degree of  $Q_{se}$  with  $\varepsilon_{ct,sv}$  is smaller than  
 455 that of  $E_{tu}$  with  $\varepsilon_{ct,sv}$ . According to Eq. (3),  $COP_{st}$  was 3.04 and 2.88 when  $\varepsilon_{ct,sv}$  was 0.5 h and  
 456 0.7 h, respectively. Thus, the phenomenon of the increasing degree of  $Q_{se}$  with  $\varepsilon_{ct,sv}$  was smaller  
 457 than that of  $E_{tu}$  with  $\varepsilon_{ct,sv}$  caused that  $COP_{st}$  reduced as  $\varepsilon_{ct,sv}$  increased.  
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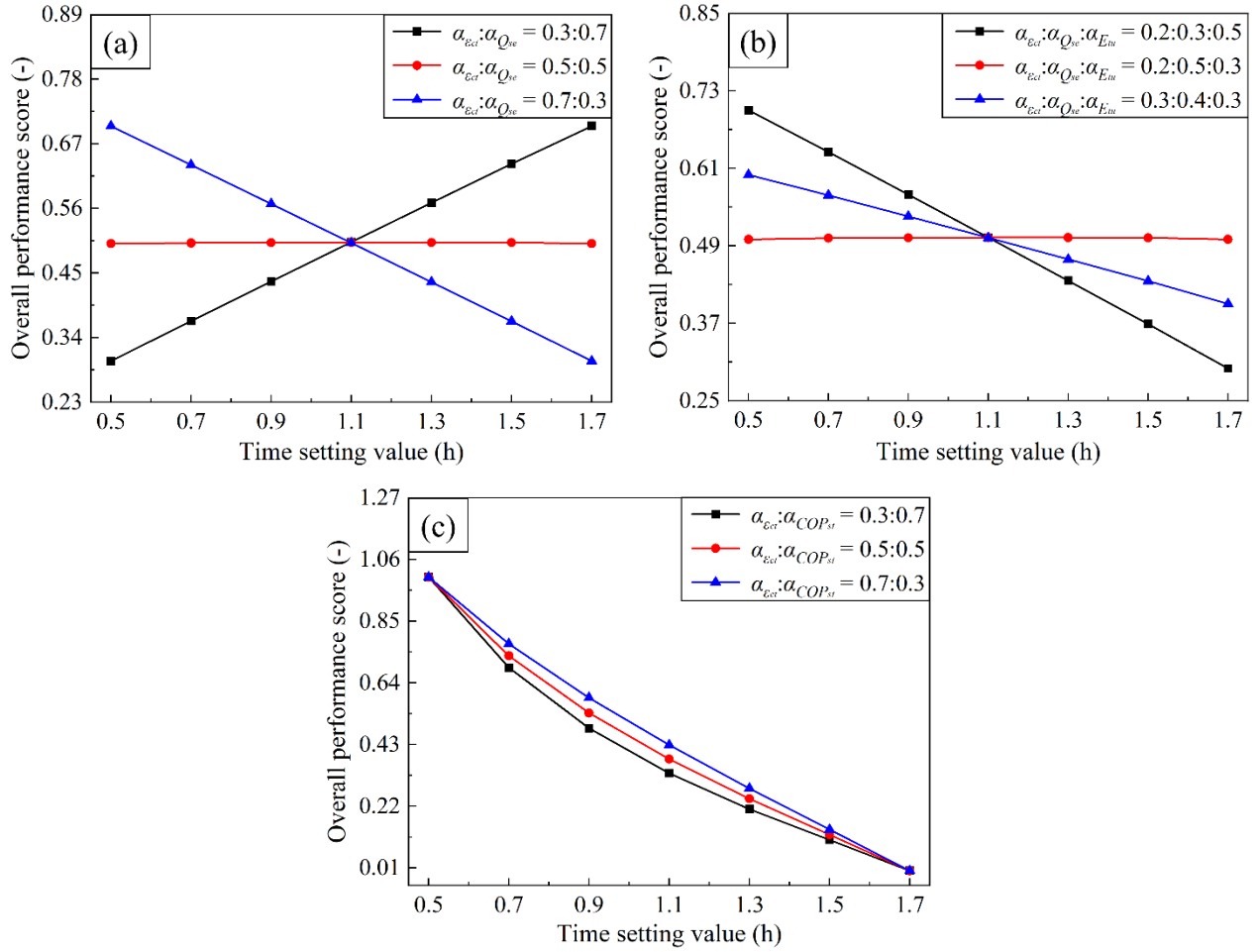


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 460  
 461 **Fig. 11.** (a)  $\varepsilon_{ct}$ , (b)  $Q_{se}$ , (c)  $E_{tu}$ , and (d)  $COP_{st}$  in different  $\varepsilon_{ct,sv}$  when ACHP is utilized  
 462

463 Fig. 12 depicts the variations of  $OS_{cs}$ ,  $OS_{cst}$ , and  $OS_{cp}$  with  $\varepsilon_{ct,sv}$  when ACHP is utilized. In Fig.  
 464 12(a), the optimal  $\varepsilon_{ct,sv}$  were 1.7 h and 0.5 h when  $\alpha_{\varepsilon_{ct}} : \alpha_{Q_{se}}$  were 0.3:0.7 and 0.7:0.3, respectively.  
 465 When  $\alpha_{\varepsilon_{ct}} : \alpha_{Q_{se}}$  was 0.5:0.5, the variation of  $OS_{cs}$  with  $\varepsilon_{ct,sv}$  was small; the optimal  $\varepsilon_{ct,sv}$  was 1.3  
 466 h. Thus, the larger  $\alpha_{\varepsilon_{ct}}$  might cause the optimal  $\varepsilon_{ct,sv}$  to occur at the lower value. In Fig. 12(b), the  
 467 optimal  $\varepsilon_{ct,sv}$  was 0.5 h when  $\alpha_{\varepsilon_{ct}} : \alpha_{Q_{se}} : \alpha_{E_{tu}}$  was 0.2:0.3:0.5 and 0.3:0.4:0.3. When  
 468  $\alpha_{\varepsilon_{ct}} : \alpha_{Q_{se}} : \alpha_{E_{tu}}$  was 0.2:0.5:0.3, the variation of  $OS_{cst}$  with  $\varepsilon_{ct,sv}$  was small; the optimal  $\varepsilon_{ct,sv}$  was

469 1.1 h. Thus, it seemed that the smaller  $\alpha_{Q_{se}}$  would cause the optimal  $\varepsilon_{ct,sv}$  to occur at the lower  
 470 value. In Fig. 12(c), the optimal  $\varepsilon_{ct,sv}$  is 0.5 h irrespective of  $\alpha_{\varepsilon_{ct}} : \alpha_{COP_{st}}$  being 0.3:0.7, 0.5:0.5, or  
 471 0.7:0.3. Thus, regardless of whether  $\varepsilon_{ct}$  had a larger or smaller weighting than  $COP_{st}$ , the optimal  
 472  $\varepsilon_{ct,sv}$  occurred at a lower value.

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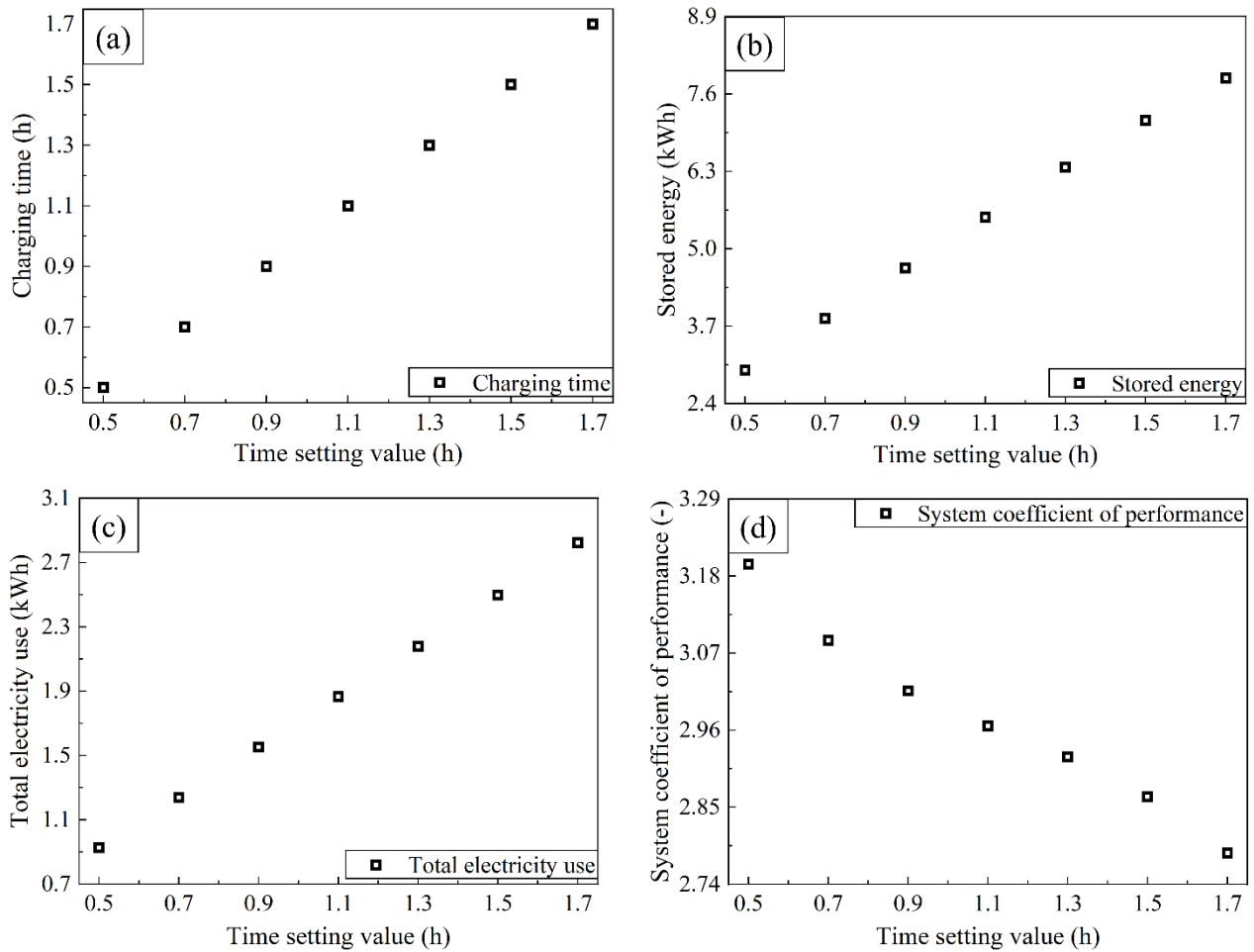
**Fig. 12.** (a)  $OS_{CS}$ , (b)  $OS_{CST}$ , and (c)  $OS_{CP}$  in different  $\varepsilon_{ct,sv}$  when ACHP is utilized

477

478 Fig. 13 depicts the variations of  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  $E_{tu}$ , and  $COP_{st}$  with  $\varepsilon_{ct,sv}$  when WCHP is utilized. In Fig.  
 479 13(a),  $\varepsilon_{ct}$  linearly increased with the increase of  $\varepsilon_{ct,sv}$ . The  $\varepsilon_{ct}$  values were almost the same as  
 480 those of  $\varepsilon_{ct,sv}$ . This meant that the t-charging standard was successfully achieved. In Fig. 13(b),  
 481  $Q_{se}$  linearly increased as  $\varepsilon_{ct,sv}$  increased. This meant that more energy would be stored if  $\varepsilon_{ct}$  was  
 482 longer. In Fig. 13(c),  $E_{tu}$  linearly increased as  $\varepsilon_{ct,sv}$  increased. This meant that more electricity  
 483 would be utilized if  $\varepsilon_{ct}$  was longer. In Fig. 13(d),  $COP_{st}$  reduced as  $\varepsilon_{ct,sv}$  increased.

484 According to Eq. (3), this phenomenon implies that the degree of increase in  $Q_{se}$  with  $\varepsilon_{ct,sv}$  is  
 485 smaller than that of  $E_{tu}$  with  $\varepsilon_{ct,sv}$ . For instance,  $Q_{se}$  was 3 kWh and 3.8 kWh when  $\varepsilon_{ct,sv}$  was 0.5  
 486 h and 0.7 h, respectively.  $E_{tu}$  was 0.93 kWh and 1.2 kWh when  $\varepsilon_{ct,sv}$  was 0.5 h and 0.7 h,  
 487 respectively. Thus, when  $\varepsilon_{ct,sv}$  increased from 0.5 h to 0.7 h,  $Q_{se}$  and  $E_{tu}$  increased by 29% and  
 488 33.6%, respectively. This indicates that the increasing degree of  $Q_{se}$  with  $\varepsilon_{ct,sv}$  is smaller than that  
 489 of  $E_{tu}$  with  $\varepsilon_{ct,sv}$ . According to Eq. (3),  $COP_{st}$  was 3.2 and 3.09 when  $\varepsilon_{ct,sv}$  was 0.5 h and 0.7 h,  
 490 respectively. Thus, the phenomenon of the increasing degree of  $Q_{se}$  with  $\varepsilon_{ct,sv}$  was smaller than  
 491 that of  $E_{tu}$  with  $\varepsilon_{ct,sv}$  caused that  $COP_{st}$  reduced as  $\varepsilon_{ct,sv}$  increased.

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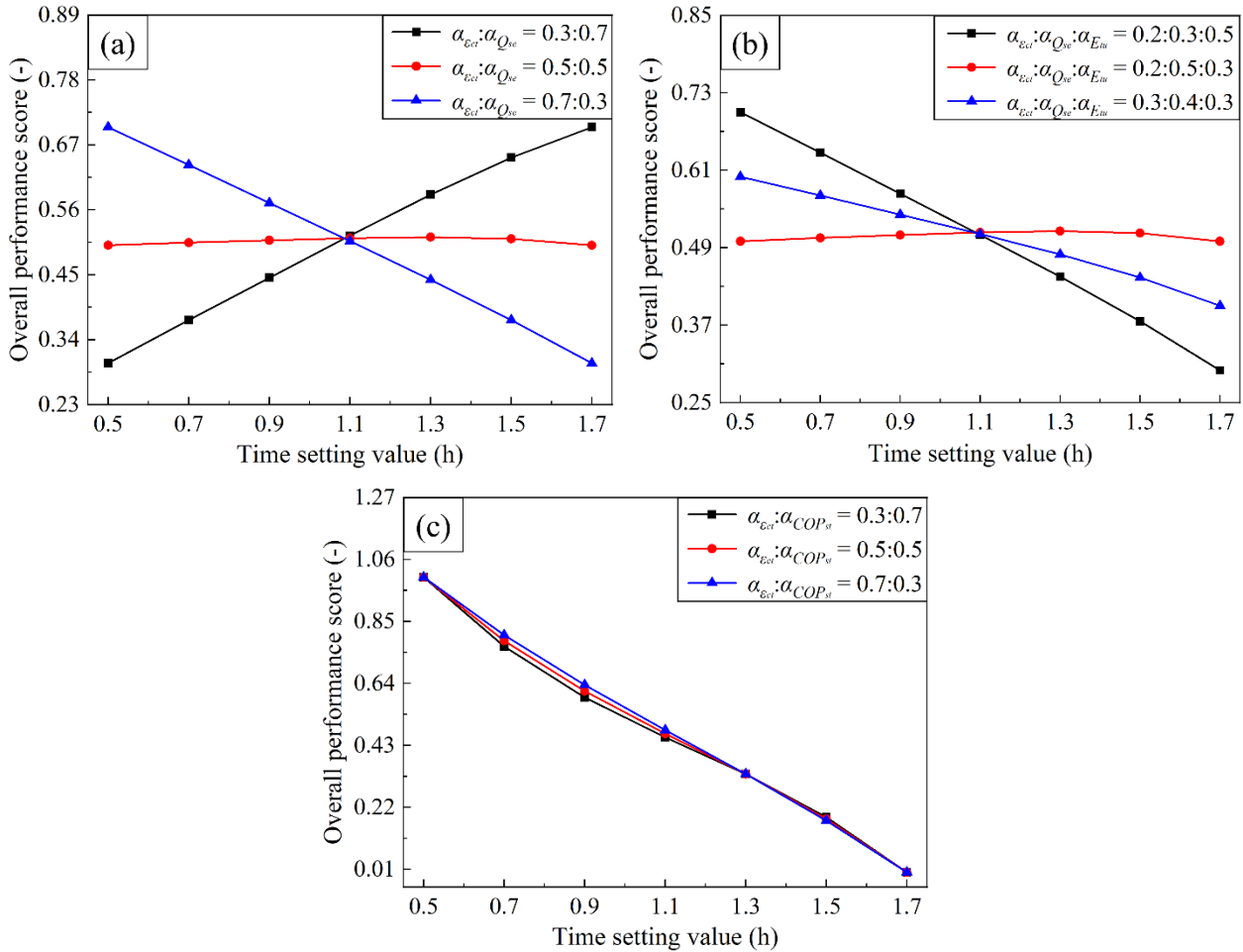
495 **Fig. 13.** (a)  $\varepsilon_{ct}$ , (b)  $Q_{se}$ , (c)  $E_{tu}$ , and (d)  $COP_{st}$  in different  $\varepsilon_{ct,sv}$  when WCHP is utilized

496

497 Fig. 14 depicts the variations of  $OS_{cs}$ ,  $OS_{cst}$ , and  $OS_{cp}$  with  $\varepsilon_{ct,sv}$  when WCHP is utilized. In Fig.  
 498 14(a), the optimal  $\varepsilon_{ct,sv}$  were 1.7 h and 0.5 h when  $\alpha_{\varepsilon_{ct}} : \alpha_{Q_{se}}$  were 0.3:0.7 and 0.7:0.3, respectively.



499 When  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}$  was 0.5:0.5, the variation of  $OS_{CS}$  with  $\varepsilon_{ct,sv}$  was small. The optimal  $\varepsilon_{ct,sv}$  was 1.3  
500 h. Thus, the larger  $\alpha_{\varepsilon_{ct}}$  might cause the optimal  $\varepsilon_{ct,sv}$  to occur at the lower value. In Fig. 14(b), the  
501 optimal  $\varepsilon_{ct,sv}$  was 0.5 h when  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}:\alpha_{E_{tu}}$  was 0.2:0.3:0.5 and 0.3:0.4:0.3. When  
502  $\alpha_{\varepsilon_{ct}}:\alpha_{Q_{se}}:\alpha_{E_{tu}}$  was 0.2:0.5:0.3, the variation of  $OS_{cst}$  with  $\varepsilon_{ct,sv}$  was small; the optimal  $\varepsilon_{ct,sv}$  was  
503 1.3 h. Thus, it seemed that the smaller  $\alpha_{Q_{se}}$  would cause the optimal  $\varepsilon_{ct,sv}$  to occur at the lower  
504 value. In Fig. 14(c), the optimal  $\varepsilon_{ct,sv}$  was 0.5 h irrespective of the situation when  $\alpha_{\varepsilon_{ct}}:\alpha_{COP_{st}}$  was  
505 0.3:0.7, 0.5:0.5, or 0.7:0.3. Thus, regardless of whether  $\varepsilon_{ct}$  had a larger or smaller weighting than  
506  $COP_{st}$ , the optimal  $\varepsilon_{ct,sv}$  occurred at a lower value.  
507



508  
509 **Fig. 14.** (a)  $OS_{CS}$ , (b)  $OS_{CST}$ , and (c)  $OS_{CP}$  in different  $\varepsilon_{ct,sv}$  when WCHP is utilized

510 For the ACHP,  $\varepsilon_{ct}$ ,  $Q_{se}$ , and  $E_{tu}$  increased by 240%, 214.9%, and 267.7%, respectively, when  
511  $\varepsilon_{ct,sv}$  increased from 0.5 h to 1.7 h.  $COP_{st}$  was reduced by 14.4% when  $\varepsilon_{ct,sv}$  increased from 0.5 h  
512

514 to 1.7 h. For the WCHP,  $\varepsilon_{ct}$ ,  $Q_{se}$ , and  $E_{tu}$  increased by 240%, 165.2%, and 204.5%, respectively,  
515 when  $\varepsilon_{ct,sv}$  increased from 0.5 h to 1.7 h.  $COP_{st}$  was reduced by 12.9% when  $\varepsilon_{ct,sv}$  increased from  
516 0.5 h to 1.7 h. For ACHP and WCHP, in the multi-criteria optimization considering  $\varepsilon_{ct}$  and  $Q_{se}$ ,  
517 the effect of  $\alpha_{\varepsilon_{ct}}$  on the optimal  $\varepsilon_{ct,sv}$  was almost the same as that of  $\alpha_{Q_{se}}$  on the optimal  $\varepsilon_{ct,sv}$ . In  
518 the multi-criteria optimization considering  $\varepsilon_{ct}$ ,  $Q_{se}$ , and  $E_{tu}$ , the effect of  $\alpha_{Q_{se}}$  on the optimal  $\varepsilon_{ct,sv}$   
519 was larger than that of  $\alpha_{\varepsilon_{ct}}$  and  $\alpha_{E_{tu}}$  on the optimal  $\varepsilon_{ct,sv}$ . In the multi-criteria optimization  
520 considering  $\varepsilon_{ct}$  and  $COP_{st}$ , the optimal  $\varepsilon_{ct,sv}$  was not affected by  $\alpha_{Q_{se}}$  and  $\alpha_{COP_{st}}$ .

521

## 522 **5. Conclusions**

523 To illustrate the influence of charging standards and combinations of setting variables on the  
524 performance of the closed-loop charging system, a system integrating CO<sub>2</sub> heat pumps and a PCM  
525 tank was investigated. Furthermore, ACHP and WCHP were considered. The system was simulated  
526 using an experimentally validated CO<sub>2</sub> heat pump and PCM tank model. The effects of  $T_{ot,sv}$ ,  
527  $Q_{se,sv}$ , and  $\varepsilon_{ct}$  on the performance of the system in the T-charging, Q-charging, and t-charging  
528 standards were analyzed, respectively. We found that for ACHP,  $COP_{st}$  was reduced by 10.5%  
529 when  $Q_{se,sv}$  increased from 2.1 kWh to 4.5 kWh.  $COP_{st}$  reduced by 12.2% when  $T_{ot,sv}$  increased  
530 from 28 °C to 34 °C.  $COP_{st}$  reduced by 14.4% when  $\varepsilon_{ct,sv}$  increased from 0.5 h to 1.7 h. For WCHP,  
531  $COP_{st}$  reduced by 9.8% when  $Q_{se,sv}$  increased from 2.1 kWh to 4.5 kWh.  $COP_{st}$  reduced by 12.2%  
532 when  $T_{ot,sv}$  increased from 28 °C to 34 °C.  $COP_{st}$  reduced by 12.9% when  $\varepsilon_{ct,sv}$  increased from  
533 0.5 h to 1.7 h.

534

535 Additionally, the multi-criteria optimization was performed in three cases where the combinations  
536 of  $\varepsilon_{ct}$  and  $Q_{se}$ ,  $\varepsilon_{ct}$ ,  $E_{tu}$ , and  $Q_{se}$ , and  $\varepsilon_{ct}$  and  $COP_{st}$  were considered. The optimal  $T_{ot,sv}$ ,  $Q_{se,sv}$ ,  
537 and  $\varepsilon_{ct,sv}$  were identified in the T-charging, Q-charging, and t-charging standards, respectively.  
538 We concluded that for ACHP and WCHP, in the multi-criteria optimization considering  $\varepsilon_{ct}$  and  
539  $Q_{se}$ , the effect of  $\alpha_{\varepsilon_{ct}}$  on the optimal  $\varepsilon_{ct,sv}$  was almost the same as that of  $\alpha_{Q_{se}}$  on the optimal  $\varepsilon_{ct,sv}$ .  
540 In the multi-criteria optimization considering  $\varepsilon_{ct}$ ,  $Q_{se}$ , and  $E_{tu}$ , the effect of  $\alpha_{Q_{se}}$  on the optimal  
541  $\varepsilon_{ct,sv}$  was larger than that of  $\alpha_{\varepsilon_{ct}}$  and  $\alpha_{E_{tu}}$  on the optimal  $\varepsilon_{ct,sv}$ . In the multi-criteria optimization  
542 considering  $\varepsilon_{ct}$  and  $COP_{st}$ , the optimal  $\varepsilon_{ct,sv}$  was not affected by  $\alpha_{Q_{se}}$  and  $\alpha_{COP_{st}}$ . Hence, this  
543 study provides a different perspective for investigating a system with an integrated heat pump and

544 PCM tank by considering different charging standards and multiple criteria.

545

## 546 **6. Future works**

547 The limitations of this study and corresponding future developments are summarized below. First,  
548 the physical characteristics of the ground-source CO<sub>2</sub> heat pump differed from those of ACHP and  
549 WCHP systems. Therefore, a system integrating a ground-source CO<sub>2</sub> heat pump with a PCM tank  
550 should be investigated. The influence of tube diameter, borehole depth, and diameter on  $\varepsilon_{ct}$ ,  $Q_{se}$ ,  
551  $E_{tu}$ , and  $COP_{st}$  in different charging standards should be analyzed in the future. Second, the PCM  
552 tank was assumed to have no heat exchange with the ambient environment. The heat loss  
553 coefficient of the PCM tank may affect the optimization results when a multi-criteria approach was  
554 applied. The influence of the PCM tank heat-loss coefficient on the system performance under  
555 different charging standards should be considered in the future. Finally, the surrogate models for  
556 describing relationships between  $\varepsilon_{ct}$  and setting variables and between  $COP_{st}$  and setting variables  
557 contribute to identifying optimal setting variables more accurately. Reliable surrogate models  
558 should be developed using advanced methods, such as machine learning, in the future.

559

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