1	An investigation of using CO ₂ heat pumps to charge PCM storage
2	tank for domestic use
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13	Abstract
14	Current investigations mainly focused on onefold phase change material (PCM) storage tank
15	charging process, while the integration between a heat-source device and a PCM storage tank
16	has been seldom considered. The investigation of using a carbon dioxide (CO ₂) heat pump to
17	charge PCM storage tank is unique because PCM can enhance the system efficiency due to the
18	delay of the outlet water temperature increase of the PCM storage tank. However, a systematic
19	investigation about this charging process is still lacking. Therefore, this study conducted the
20	performance investigation about the system using CO ₂ heat pumps to charge the PCM storage
21	tank. The charging process was simulated by the integration of the heat pump and PCM storage
22	tank models. The reliabilities of these models were validated by experimental data. The effects
23	of different expansion valve opening, PCM types, and tank arrangements on the system
24	performance were analyzed. Both air-source and water-source CO ₂ heat pumps were considered.
25	The optimal parameters were identified by maximizing the overall performance considering the
26	balance between the charging time and system coefficient of performance. For the system using
27	water-source CO ₂ heat pump with optimal parameters, charging time and system coefficient of
28	performance were 0.29 h, and 3.48, respectively.
29	

30 Keywords: CO₂ heat pump; PCM storage tank; Charging process; Performance investigation

Nomenclature		gs	gas cooler
Ε	electricity energy use	h	enthalpy
EX	exergy	in	initial
Μ	mass	it	inlet
'n	mass flowrate	lt	least preferred situation
0	opening	mt	most preferred situation
Q	energy amount	ot	outlet
Q	heating capacity	0V	overall performance
SR	score	pc	РСМ
Т	temperature	pm	pump
tt	moment	rs	released
Ŵ	power	sa	starting
		sd	supplied
Abbreviations		sm	system
CO ₂	carbon dioxide	st	stored
СОР	coefficient of performance	t	time
РСМ	phase change material	tl	total
		wt	water
Subscripts		Ζ	evaporator
ab	ambient		
С	specific heat	Greek symbol	ls
сс	charging	β	weight factor
chp	CO ₂ heat pump	δ_0	a coefficient
ср	compressor	δ_1	a coefficient
dc	discharging	δ_2	a coefficient
dg	designed	δ_3	a coefficient
en	ending	σ	time span
ex	expansion valve	η	efficiency
ey	exergy		

32 **1. Introduction**

33 Rapid society development intensifies the population increase and urbanization, resulting in energy crisis [1] and environmental pollutions [2]. Therefore, it is needed to develop the 34 sustainable energy technologies for dealing with these problems. Since heat pumps can 35 36 effectively collect heat from ambient environments [3], they are known as one sustainable 37 energy technology and have been utilized in many applications including residential heating 38 [4], desalination [5], waste heat recovery [6], and air conditioning [7]. Dongellini et al. [8] 39 performed the performance comparison between a hybrid heat pump system and a gas boiler 40 system. They found that the former one could save up to 22% energy use in comparison with 41 the latter one. Wang et al. [9] concluded that in comparison with traditional air-source heat 42 pumps, the payback period of the system applying both air-source and water-source heat pumps 43 was 3.66 years. Vivian et al. [10] proposed a new operating strategy for the heat pump systems 44 for both space heating and domestic hot water purposes. It was reported that the maximum peak-power reduction could reach 35% when the strategy was applied. Kosmadakis et al. [11] 45 46 investigated a high-temperature heat pump utilizing the waste heat, and they found that the 47 shortest payback period of the system could be around 3 years.

48

49 Using CO₂ as refrigerant in heat pumps can weaken the ozone depletion caused by 50 chlorofluorocarbons and furnish high-temperature water [12]. Dai et al. [13] concluded that at 51 the ambient temperature of -20° C the maximum coefficient of performance (COP) for the CO₂ 52 heat pump was 2.13 when the vapor injection technique was applied. Ahsaee and Askari [14] 53 found that the COP of the ground-source CO_2 heat pump could be improved by 16.5% when 54 the injector was applied. Wang et al. [15] designed a novel CO₂ heat pump for satisfying both heating and cooling demands. It was concluded that the average COP of the system was 3.27. 55 56 Chung et al. [16] found that the heating and cooling COP of CO₂ heat pump could be 57 respectively improved by 7.1% and 6.8%, when the injector with optimal injection ratio was 58 applied.

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Heat pumps are usually integrated with storage tanks in various applications, which can bring significant profits including the operating expense reduction [17]. Phase change material (PCM) has high storage density [18], which contributes to its extensively utilization in various fields including thermal management [19], photovoltaic systems [20], ventilation [21], domestic hot water use [22], and free cooling systems [23], etc. One important function of PCM is to improve the thermal capacity of storage tank. Carmona et al. [24] found that the energy and exergy efficiencies could be enhanced when PCMs were applied in the tank. Pop and Balan [25] concluded that the storage tank volume could be reduced by 25% when the PCM was applied. Kozelj et al. [26] reported that the heat storage capacity could be enhanced by approximately 70% when the PCM was applied in the water tank. Huang et al. [27] investigated a solar system with PCM storage tank, and they found that the solar fraction could be increased by around 30% when the PCM storage tank replaced the pure water tank in the system.

73 Many scholars have performed the studies about charging PCM storage tanks. Zhao et al. [28] 74 found that the charging time (σ_{cc}) of PCM storage tank with 90% porosity graphite foam was 75 41.68% of that without graphite form. Li et al. [29] reported that increasing the mass flowrate 76 of heat transfer fluid contributed to reducing σ_{cc} of PCM storage tank. Gorzin et al. [30] 77 concluded that σ_{cc} could be reduced by 52% when the optimal PCM was applied. Alhusseny 78 et al. [31] found that σ_{cc} could be effectively reduced when the metal foam was added in the 79 PCM. Sodhi and Muthukumar [32] reported that σ_{cc} could be reduced by 24.5% when the 80 non-uniform fin distribution was used in the PCM storage tank.

81

82 It could be found from the above literature summary that seldom investigations presented the 83 behaviour about using the CO₂ heat pump to charge the PCM storage tank. As shown in Fig. 1, 84 current investigations mainly aim to study the heat transfer process of charging the PCM storage 85 tank, and seldom studies considered the issue of the integration between the heat-source device 86 and PCM storage tank. This might cause the consideration of onefold evaluation principle for 87 the charging process, i.e., σ_{cc} . Therefore, for proper integrations, it is very meaningful to 88 consider more evaluation principles, e.g., σ_{cc} and the system coefficient of performance 89 (COP_{sm}) . However, the systematic investigation of this issue was still lacking. As shown in Fig. 90 2 (a), the temperature of the CO_2 leaving the compressor is very high. To improve the heat 91 exchange effect between the CO₂ and the water from the PCM storage tank, the temperature of 92 the water from the PCM storage tank should be low. As shown in Fig. 2 (b), during the charging 93 process of the PCM, the PCM will go through the solid phase, solid-liquid two phase, and liquid 94 phase. The solid-liquid two phase of the PCM will delay the temperature increase of the outlet 95 water of the PCM storage tank, which will improve the energy efficiency of the CO₂ heat pump. 96 However, the mechanisms about the effects of PCM types, tank arrangements, and expansion 97 valve opening (o_{ex}) on the system performance are still unknown.





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Fig. 1. Theoretical schematics of (a) current investigations and (b) this investigation



Fig. 2. (a) Temperature-entropy diagram of the refrigeration cycle in CO₂ heat pump and (b) temperature
 variation curve of PCM during the charging process

105 Hence, this study aimed to clarify the mechanisms about the effects of PCM types, tank 106 arrangements, and o_{ex} on the system performance. This study conducted the investigation 107 about the system of using the air-source and water-source CO₂ heat pumps to charge the PCM 108 storage tank. The charging process was modelling by the integration of the CO₂ heat pump and 109 PCM storage tank models. The experimental data were applied to validate the reliability of the models. The effects of different PCM types, tank arrangements, and o_{ex} on the system 110 111 performance were analyzed. σ_{cc} and COP_{sm} were selected as the performance indicators. 112 Based on the results, the multi-criterion optimization approach was performed to identify the 113 optimal operating parameters, PCM types, and tank arrangements.

115 The novelties of this investigation are the followings: (a) This investigation considers the 116 charging process integrating the heat-source device and PCM storage tank in the closed loop 117 and thereby overcomes the limitations of traditional studies, which only considers the charging 118 process of PCM storage tank in the open loop; (b) Two key performance indicators, i.e., 119 charging time (σ_{cc}) and system coefficient of performance (COP_{sm}), are considered in this study. 120 This overcomes the limitations of traditional studies which only consider σ_{cc} as the 121 performance indicator, realizing the consideration of energy use of pumps and CO₂ heat pumps 122 in the closed loop; (c) A multi-criterion optimization approach is established to determine the 123 optimal o_{ex} , PCM types, and tank arrangements. This approach can well guide engineers to 124 conduct the design for the charging system with the integration of heat-source device and PCM 125 storage tank; (d) Both air-source and water-source CO₂ heat pumps are considered in the 126 investigation of the charging process. These case studies play a demonstration role in the aspects 127 of how to study the charging performance of the system integrating the advanced heat-source 128 devices and PCM storage tank. The rest of this paper is given as the following. The 129 methodology is introduced in Section 2. Section 3 presents the results and analysis in different 130 expansion valve opening, PCM types, and tank arrangements. Section 4 depicts the discussion. 131 Conclusions are given in Section 5.

132

133 2. Methodology

134 2.1 System description

135 Fig. 3 depicts the schematic for the systems of using (a) an air-source and (b) a water-source 136 CO₂ heat pump to charge the PCM storage tank. The investigated systems were mainly 137 comprised of the circulation pump, the expansion valve, the compressor, the liquid receiver, the 138 evaporator, the internal heat exchanger, the gas cooler, and the PCM storage tank. The CO₂ in 139 the evaporator will obtain heat from the mixture, composed of water and glycol for freezing 140 protection. The CO₂ in the heat pump will go through a typical trans-critical refrigeration cycle. 141 As shown in Fig. 2 (a), the CO₂ will evaporate in the evaporator. The CO₂ leaving the evaporator 142 will exchange heat with that leaving the gas cooler in the internal heat exchanger. Then, CO₂ 143 will be compressed and throttled in the compressor and expansion valve, respectively. Finally, 144 the CO₂ will give heat to the water from the PCM storage tank in the gas cooler. The circulation 145 pump will circulate the water between the gas cooler and the PCM storage tank. The hot water 146 leaving the gas cooler will enter the PCM storage tank, and the cold water leaving the PCM 147 storage tank will return the gas cooler. Normally, the charging process will be completed when

- 148 the outlet water temperature of the PCM storage tank reaches the set value. This set value should
- 149 be low (e.g., lower than 30°C), because the high return water temperature will reduce the COP
- 150 of the CO_2 heat pump, and even cause the shutdown of the CO_2 heat pump.
- 151



154 Fig. 3. Schematic for the systems of using (a) air-source and (b) water-source CO₂ heat pump to charge 155 PCM storage tank for domestic use

- 156
- 157 2.2 System models
- 158 2.2.1 CO₂ heat pump model

159 The integration of MATLAB and REFPROP was applied to establish the CO₂ heat pump models. 160 Mass and energy governing equations where several assumptions including one-dimension 161 model without pressure drop and heat loss were applied to established the gas cooler, internal 162 heat exchanger, and evaporator with liquid receiver models, referring to the study of Rasmussen 163 et al. [33]. The evaporator in the air-source CO₂ heat pump was fin-tube heat exchanger. The calculations of heat transfer coefficients for the air, single-phase CO₂, and two-phase CO₂ in 164 165 the fin-tube heat exchanger referred to the study of Deng et al. [34]. Expect the evaporator in 166 the air-source heat pump, other heat exchangers in the air-source and water-source CO₂ heat 167 pump were plate heat exchangers. The calculations of heat transfer coefficients for the single-

- 168 phase and two-phase fluids referred to the study of Mota et al. [35] and Lee et al. [36]. The 169 compressor model referred to the study of Wang et al. [37], and it was utilized to calculate the CO₂ mass flowrate through the compressor and compressor power (\dot{W}_{cp}). The relationships 170 171 between the compressor efficiencies (i.e., volumetric, mechanical, and isentropic efficiencies) 172 and pressure ratio that were applied in this model were constructed by the measured data in our 173 previous study [38]. The expansion valve model referred to the study of Eames et al. [39], and 174 it was used to calculate the CO₂ mass flowrate through the expansion valve. The relationship 175 between the flow factor and expansion value opening (o_{ex}) that was applied in this model was 176 constructed by the measured data in our previous study [38].
- 177

178 2.2.2 PCM storage tank model

Several assumptions were applied for establishing the PCM storage tank model. The suggested model contained unchanged PCM temperature during the melting process, no heat loss to ambient, one dimensional model, and water properties that were not influenced by temperature [40]. The PCM was encapsulated inside the tubes that were install in the tank. Governing equations of the PCM storage tank model are depicted in our previous study [41]. The water and PCM Nusselt numbers were calculated referring to Watanabe et al.'s study [42].

185

186 2.3 Validation

187 The experimental setup for the CO₂ heat pump installed in the Energy and Indoor Environment 188 Laboratory at the Norwegian University of Science and Technology has been established to 189 validate the reliability of the developed CO₂ heat pump model. The detailed information of the 190 gas cooler, evaporator, liquid receiver, internal heat exchanger, compressor, and expansion 191 valve were presented in our previous study [43]. The accuracy of the sensors in the experimental 192 setup were also shown in our previous study [43]. Nine cases where the discharge pressure was 193 maintained from 7,100 kPa to 8,700 kPa with the interval of 200 kPa were conducted. The 194 measured outlet fluid temperature in the evaporator and the gas cooler were compared with the 195 simulated values under the same operating conditions.

196

197 The comparisons between the experimental and simulated outlet mixture temperature in the 198 evaporator and outlet water temperature in the gas cooler in these nine cases are presented in 199 Fig. 4. Both the simulated outlet mixture temperature in the evaporator and outlet water 200 temperature in the gas cooler well agreed with the experimental ones. The average temperature 201 difference between the experimental and simulated values for the outlet mixture temperature in 202 the evaporator and outlet water temperature in the gas cooler were 2.1 K and 1.4 K, respectively. 203 This indicated that the developed water-source CO₂ heat pump model was reliable. The reasons 204 resulting in these temperature difference might be the measurement error of the sensors and the 205 utilization of quasi-dynamic modelling approach. The experimental data from the literature has 206 been compared with the simulated data of the PCM storage tank in our previous study [41]. The 207 average relative error for the PCM storage tank model was 3.97%. The results showed that the 208 simulated data agreed well with the experimental data, which indicated that the PCM storage 209 tank model was reliable. Thus, the models applied to simulate the process of using CO_2 heat 210 pump to charge the PCM storage tank were reliable.





Fig. 4. Comparisons between experimental and simulated (a) outlet mixture temperature in evaporator and
 (b) outlet water temperature in gas cooler

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216 2.4 Performance indicators

217 Two performance indicators including σ_{cc} and COP_{sm} were applied in this investigation. σ_{cc} 218 was defined as Eqn. (1):

219

$$\sigma_{cc} = tt_{en} - tt_{sa} \tag{1}$$

220 where tt_{en} and tt_{sa} denote the ending and starting moments for charging the PCM storage 221 tank, respectively.

222

224

223 COP_{sm} was defined as Eqn. (2):

$$COP_{sm} = \frac{Q_{st}}{E_{tl}} \tag{2}$$

where Q_{st} denotes the stored energy. E_{tl} denotes the total electricity energy use, which was calculated by Eqn. (3):

227

$$E_{tl} = E_{cp} + E_{pm,z} + E_{pm,gs} \tag{3}$$

where E_{cp} , $E_{pm,z}$, and $E_{pm,gs}$ denote the electricity energy use of compressor, pumps in the evaporator and the gas cooler, respectively. They were calculated by Eqns. (4) to (6):

$$E_{cp} = \int_{tt_{en}}^{tt_{sa}} \dot{W}_{cp} dt \tag{4}$$

$$E_{pm,z} = \int_{tt_{en}}^{tt_{sa}} \dot{W}_{pm,z} dt$$
(5)

$$E_{pm,gs} = \int_{tt_{en}}^{tt_{sa}} \dot{W}_{pm,gs} dt$$
(6)

where $\dot{W}_{pm,z}$ denotes the pump power in the evaporator, which was assumed to be 100 W. $\dot{W}_{pm,gs}$ denotes the pump power in the gas cooler, which was calculated by Eqn. (7):

235
$$\frac{\dot{W}_{pm,gs}}{\dot{W}_{pm,gs,dg}} = \delta_0 + \delta_1 \frac{\dot{m}_{gs,wt}}{\dot{m}_{gs,wt,dg}} + \delta_2 (\frac{\dot{m}_{gs,wt}}{\dot{m}_{gs,wt,dg}})^2 + \delta_3 (\frac{\dot{m}_{gs,wt}}{\dot{m}_{gs,wt,dg}})^3$$
(7)

where dg denotes the designed value. δ_0 , δ_1 , δ_2 , and δ_3 denote the coefficients, which were 0, 0.0016, 20.0037, and 0.9671, respectively [44]. $\dot{W}_{pm,gs,dg}$ and $\dot{m}_{gs,wt,dg}$ were 50 W and 0.044 kg/s, respectively.

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242

The multi-criteria approach was applied to conduct the optimization for identifying the optimal parameters [3]. The score of the overall performance (SR_{ov}) was defined as Eqn. (8):

$$SR_{ov} = \beta_{\sigma_{cc}} \cdot SR_{\sigma_{cc}} + \beta_{COP_{sm}} \cdot SR_{COP_{sm}}$$
(8)

243 where *SR* denotes the score. β denotes the weight factor. $SR_{\sigma_{cc}}$ and $SR_{COP_{sm}}$ were 244 respectively calculated by Eqns. (9) and (10):

245
$$SR_{\sigma_{cc}} = \frac{\sigma_{cc} - \sigma_{cc,lt}}{\sigma_{cc,mt} - \sigma_{cc,lt}}$$
(9)

$$SR_{COP_{sm}} = \frac{COP_{sm} - COP_{sm,lt}}{COP_{sm,mt} - COP_{sm,lt}}$$
(10)

where *lt* and *mt* denote the least-preferred and most-preferred situations, respectively. $\beta_{\sigma_{cc}}$ and $\beta_{cOP_{sm}}$ were user-specified, and the relationship between them should satisfy Eqn. (11):

 $\beta_{\sigma_{cc}} + \beta_{COP_{sm}} = 1 \tag{11}$

250 251

252 **3. Results and analysis**

The results and analysis about the influence of different expansion valve opening (o_{ex}) , PCM types, and tank arrangements on the system performance are presented in this section. Charging time (σ_{cc}), stored energy (Q_{st}), total electricity energy use (E_{tl}), and system coefficient of performance (COP_{sm}) are considered as performance indicators. The optimal o_{ex} , PCM type, and tank arrangement are identified according to the results of σ_{cc} and COP_{sm} . When the identifying optimal cases according to σ_{cc} and COP_{sm} are different, the score of the overall performance (SR_{ov}) will be applied to determine the final optimal case.

- 260
- 261 3.1 Results and analysis in different expansion valve opening

262 This section presents the results and analyses about the effect of different expansion valve 263 opening (o_{ex}) on the system performance. The performance indicators included charging time 264 (σ_{cc}) , stored energy (Q_{st}) , total electricity energy use (E_{tl}) , and system coefficient of performance (COP_{sm}). Fig. 5 depicts the variations of σ_{cc} , Q_{st} , E_{tl} , and COP_{sm} with 265 266 different o_{ex} using the air-source heat pump. In Fig. 5 (a), σ_{cc} increased as o_{ex} increased. 267 This might be caused by that lower o_{ex} resulted in higher discharge pressure and the higher 268 CO_2 temperature to the gas cooler, leading to faster completion of charging process. When o_{ex} 269 increased from 40% to 70%, σ_{cc} varied from 0.79 h to 2.31 h, increased by 193.1%. In Fig. 5 270 (b), Q_{st} increased as o_{ex} increased. Increasing o_{ex} resulted in the increase of σ_{cc} , which led 271 to the increase of Q_{st} . When o_{ex} increased from 40% to 70%, Q_{st} varied from 3 kWh to 5.64 272 kWh, increased by 88.1%. In Fig. 5 (c), E_{tl} increased as o_{ex} increased. When o_{ex} increased 273 from 40% to 70%, E_{tl} varied from 1.06 kWh to 2.83 kWh, increased by 166.9%. In Fig. 5 (d), 274 COP_{sm} reduced as o_{ex} increased. When o_{ex} increased from 40% to 70%, COP_{sm} varied 275 from 2.83 to 2, decreased by 29.5%. According to the Eqn. (2), this phenomenon might be 276 explained by that the increasing degree of Q_{st} varied with o_{ex} was smaller than the 277 increasing degree that E_{tl} varied with o_{ex} . It could be concluded that 40% was the optimal 278 o_{ex} , because σ_{cc} in the case when o_{ex} was 40% was smaller than σ_{cc} in the other case and 279 COP_{sm} in the case when o_{ex} was 40% was higher than COP_{sm} in the other case.



Fig. 5. Variations of (a) charging time, (b) stored energy, (c) total electricity energy use, and (d) system coefficient of performance with different expansion valve opening using the air-source heat pump

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285 Fig. 6 depicts the variations of σ_{cc} , Q_{st} , E_{tl} , and COP_{sm} with different expansion value 286 opening (o_{ex}) using the water-source heat pump. In Fig. 6 (a), σ_{cc} increased as o_{ex} increased. This might be caused by that lower o_{ex} resulted in higher discharge pressure, which might 287 288 increase the CO₂ temperature in the gas cooler, leading to faster completion of charging process. When o_{ex} increased from 40% to 70%, σ_{cc} varied from 0.35 h to 1.06 h, increased by 202.1%. 289 290 In Fig. 6 (b), Q_{st} increased as o_{ex} increased. Increasing o_{ex} resulted in the increase of σ_{cc} , 291 which led to the increase of Q_{st} . When o_{ex} increased from 40% to 70%, Q_{st} varied from 292 2.31 kWh to 3.85 kWh, increased by 67.1%. Thus, the increasing degree of σ_{cc} was higher 293 than that of Q_{st} . In Fig. 6 (c), E_{tl} increased as o_{ex} increased. When o_{ex} increased from 40% 294 to 70%, E_{tl} varied from 0.7 kWh to 1.38 kWh, increased by 98.3%. In Fig. 6 (d), the variations 295 of COP_{sm} with o_{ex} was irregular. According to the Eqn. (2), this phenomenon might be 296 explained by that in some cases the increasing degree that Q_{st} varied with o_{ex} was smaller 297 than the increasing degree that E_{tl} varied with o_{ex} , while in some cases the increasing degree

298 that Q_{st} varied with o_{ex} was larger than the increasing degree that E_{tl} varied with o_{ex} . The 299 maximum COP_{sm} was 3.31, occurring at the case when o_{ex} was 40%. The minimum COP_{sm} 300 was 2.79, occurring at the case when o_{ex} was 70%. COP_{sm} at the case when o_{ex} was 40% 301 was 1.19 times as high as COP_{sm} at the case when o_{ex} was 70%. It could be concluded that 302 40% was the optimal o_{ex} , since σ_{cc} in the case when o_{ex} was 40% was smaller than σ_{cc} in 303 the other case and COP_{sm} in the case when o_{ex} was 40% was higher than COP_{sm} in the other 304 case.

305



306 Fig. 6. Variations of (a) charging time, (b) stored energy, (c) total electricity energy use, and (d) system 307 coefficient of performance with different expansion valve opening using the water-source heat pump

309 It could be seen from Fig. 5 and Fig. 6 that COP_{sm} when the water-source CO₂ heat pump was 310 applied was higher than COP_{sm} when the air-source CO_2 heat pump was applied. The higher 311 COP_{sm} might cause higher charging speed, which led to shorter σ_{cc} . The shorter σ_{cc} might 312 result in less energy stored in the PCM storage tank, which meant that Q_{st} might be less. Thus, 313 σ_{cc} when the air-source CO₂ heat pump was applied was longer than σ_{cc} when the water-

- source CO₂ heat pump was applied, while Q_{st} when the air-source CO₂ heat pump was applied
- 315 was larger than Q_{st} when the water-source CO₂ heat pump was applied.
- 316
- 317 3.2 Results and analysis in different PCM types
- 318 This section presents the results and analysis of the system performance for different PCM types. 319 The thermal properties of different PCM were depicted in Table 1. The PCM-1, PCM-2, PCM-320 3, PCM-4, PCM-5, and PCM-6 have the melting temperature of 16°C, 17°C, 18°C, 19.6°C, 321 20.4°C, and 21.3°C, respectively. The latent heat of PCM-3 that is 236 kJ/kg is the maximum, 322 while the latent heat of PCM-4 that is 86 kJ/kg is the minimum. The solid thermal conductivity 323 of PCM-2 that is 1 W/(m·K) is the maximum, while the solid thermal conductivity of PCM-4 324 that is 0.05 W/($m \cdot K$) is the minimum. The liquid thermal conductivity of PCM-2 that is 0.5 325 $W/(m \cdot K)$ is the maximum, while the liquid thermal conductivity of PCM-4 that is 0.05 W/(m \cdot K) is the minimum. Both of the solid and liquid density of PCM-2 that are 1,800 kg/m³ are the 326 maximum, while both of the solid and liquid density of PCM-4 that are 694 kg/m³ are the 327 328 minimum. The solid specific heat of PCM-2 that is 2.5 kJ/(kg·K) is the maximum, while the 329 solid specific heat of PCM-3 that is $1.65 \text{ kJ/(kg \cdot K)}$ is the minimum. The liquid specific heat of 330 PCM-1 that is 2.3 kJ/(kg·K) is the maximum, while the liquid specific heat of PCM-2 that is 331 $1.5 \text{ kJ/(kg \cdot K)}$ is the minimum.
- 332
- 333

 Table 1 Thermal properties of different PCM

	PCM-1	PCM-2	PCM-3	PCM-4	PCM-5	PCM-6
	[45]	[46]	[47]	[48]	[49]	[50]
Melting temperature (°C)	16	17	18	19.6	20.4	21.3
Latent heat (kJ/kg)	213	145	236	86	138.8	152
Solid thermal conductivity	0.18	1	0.17	0.05	0.6	0.182
(W/(m·K))						
Liquid thermal conductivity	0.18	0.5	0.17	0.05	0.3	0.182
(W/(m·K))						
Solid density (kg/m ³)	830	1,800	780	694	881	884
Liquid density (kg/m ³)	800	1,800	780	694	881	960
Solid specific heat	2.3	2.5	1.65	1.7	2	1.67
$(kJ/(kg \cdot K))$						
Liquid specific heat	2.3	1.5	2.1	1.7	2	2.09
(kJ/(kg·K))						

Fig. 7 (a) depicts the charging time (σ_{cc}) and system coefficient of performance (COP_{sm}) in 334 different PCM types using the air-source heat pump. When the PCM-1, PCM-2, PCM-3, PCM-335 336 4, PCM-5, and PCM-6 were used, σ_{cc} were 1.56 h, 2.31 h, 0.79 h, 0.46 h, 1.25 h, and 0.61 h, respectively. Thus, σ_{cc} was the minimum when the PCM-4 was utilized, while σ_{cc} had its 337 338 maximum when the PCM-2 was utilized. σ_{cc} when the PCM-2 was used was 5.02 times as 339 high as σ_{cc} when the PCM-4 was used. These phenomena might be explained by that the 340 density of the PCM-2 was the highest among the observed PCMs, while the density of the PCM-4 was the minimum among the PCMs. In addition, although the latent heat of the PCM-2 was 341 342 lower than that of the PCM-3, the effect of the thermal capacity (i.e., multiplication of the 343 specific heat and density) of the PCM-2 was higher than that of the PCM-3. The latent heat of 344 the PCM-4 was evidently smaller than that of the other PCM. When the PCM-1, PCM-2, PCM-345 3, PCM-4, PCM-5, and PCM-6 were used, *COP_{sm}* were 2.7, 2.81, 2.83, 3.01, 2.76, and 2.93, 346 respectively. Thus, COP_{sm} had its maximum when the PCM-4 was utilized, while COP_{sm} had 347 its minimum when the PCM-1 was utilized. COP_{sm} when the PCM-4 was used was 1.11 times 348 as high as COP_{sm} when the PCM-1 was used. It could be concluded that the PCM-4 was the 349 optimal PCM because σ_{cc} in the case when the PCM-4 was applied was smaller than that when 350 the other PCM was applied and COP_{sm} when the PCM-4 was applied was higher than that 351 when the other PCM was applied.

352

353 Fig. 7 (b) depicts the stored energy (Q_{st}) and total electricity energy use (E_{tl}) for different PCM 354 types using the air-source heat pump. When the PCM-1, PCM-2, PCM-3, PCM-4, PCM-5, and 355 PCM-6 were used, Q_{st} were 5.69 kWh, 8.73 kWh, 3 kWh, 1.8 kWh, 4.71 kWh, and 2.35 kWh, 356 respectively. Thus, Q_{st} was the minimum when the PCM-4 was utilized, while Q_{st} was the 357 maximum when the PCM-2 was utilized. Q_{st} when the PCM-2 was used was 4.85 times as 358 high as Q_{st} when the PCM-4 was used. These phenomena might be explained by the thermal properties of the PCM-4 and PCM-2 including the latent heat, density, and specific heat. When 359 360 the PCM-1, PCM-2, PCM-3, PCM-4, PCM-5, and PCM-6 were used, E_{tl} were 2.11 kWh, 3.11 361 kWh, 1.06 kWh, 0.6 kWh, 1.7 kWh, and 0.8 kWh, respectively. Thus, E_{tl} had its minimum 362 when the PCM-4 was utilized, while E_{tl} had its maximum when the PCM-2 was utilized. E_{tl} 363 when the PCM-2 was used was 5.18 times as high as E_{tl} when the PCM-4 was used. This 364 might be caused by the corresponding σ_{cc} when the different PCM were applied. 365



Fig. 7. (a) Charging time and system coefficient of performance, and (b) stored energy and total electricity
 energy use in different PCM types using the air-source heat pump

369 Fig. 8 (a) depicts the charging time (σ_{cc}) and system coefficient of performance (COP_{sm}) in 370 different PCM types using the water-source heat pump. When the PCM-1, PCM-2, PCM-3, 371 PCM-4, PCM-5, and PCM-6 were used, σ_{cc} were 0.37 h, 1.53 h, 0.35 h, 0.29 h, 0.8 h, and 372 0.34 h, respectively. Thus, σ_{cc} was the minimum when the PCM-4 was utilized, while σ_{cc} 373 was the maximum when the PCM-2 was utilized. σ_{cc} when the PCM-2 was used was 5.28 374 times as high as σ_{cc} when the PCM-4 was used. These phenomena might be explained by that 375 the density of the PCM-2 was the maximum among these PCM, while the density of the PCM-376 4 was the minimum among these PCM. When the PCM-1, PCM-2, PCM-3, PCM-4, PCM-5, and PCM-6 were used, COP_{sm} were 3.23, 2.32, 3.31, 3.48, 3.03, and 3.27, respectively. Thus, 377 378 COP_{sm} was the maximum when the PCM-4 was utilized, while COP_{sm} was the minimum 379 when the PCM-2 was utilized. COP_{sm} when the PCM-4 was used was 1.5 times as high as COP_{sm} when the PCM-2 was used. It could be concluded that the PCM-4 was the optimal PCM 380 381 since σ_{cc} in the case when the PCM-4 was applied was smaller than that when the other PCM 382 was applied and COP_{sm} in the case when the PCM-4 was applied was larger than that when 383 the other PCM was applied.

384

Fig. 8 (b) depicts the stored energy (Q_{st}) and total electricity energy use (E_{tl}) in different PCM types using the air-source heat pump. When the PCM-1, PCM-2, PCM-3, PCM-4, PCM-5, and PCM-6 were used, Q_{st} were 2.41 kWh, 8.7 kWh, 2.31 kWh, 1.98 kWh, 4.5 kWh, and 2.28 kWh, respectively. Thus, Q_{st} had its minimum when the PCM-4 was utilized, while Q_{st} was the maximum when the PCM-2 was utilized. Q_{st} when the PCM-2 was used was 4.39 times as high as Q_{st} when the PCM-4 was used. These might be caused by the thermal properties of the PCM-4 and PCM-2. When the PCM-1, PCM-2, PCM-3, PCM-4, PCM-5, and PCM-6 were used, E_{tl} were 0.75 kWh, 3.74 kWh, 0.7 kWh, 0.57 kWh, 1.49 kWh, and 0.7 kWh, respectively. Thus, E_{tl} had its minimum when the PCM-4 was utilized, while E_{tl} had its maximum when the PCM-2 was utilized. E_{tl} when the PCM-2 was used was 6.56 times as high as E_{tl} when the PCM-4 was used. This might be caused by the corresponding σ_{cc} when the different PCM were applied.

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For the system using the air-source and water-source CO₂ heat pumps, the optimal PCM type was PCM-4. When the PCM-4 was applied in the systems using air-source or water-source CO₂ heat pumps, σ_{cc} had its minimum, and COP_{sm} had its maximum. The good thermal properties of PCM-4 led to be that it could contribute to realizing the charging process within a shorter period and better energy performance.

406

407 3.3 Results and analysis in different tank arrangements

This section presents the results and analysis of the system performance in different tank arrangements. PCM-4 was applied in this section. The number of tubes in each column and row in different cases were depicted in Table 2. The number of tubes in each column in Case 1, Case 2, Case 3, Case 4, Case 5, and Case 6 were 21, 20, 19, 21, 20, and 19, respectively. The number of tubes in each row in Case 1, Case 2, Case 3, Case 4, Case 5, and Case 6 were 6, 6, 6, 5, 5, and 5, respectively.

- 414
- 415

Table 2 Number of tubes in each column and row in different cases

	Case 1	Case 2	Case 3	Case 4	Case 5	Case 6
Number of tubes in each column (-)	21	20	19	21	20	19

Number of tubes in each row (-)	6	6	6	5	5	5	
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417 Fig. 9 (a) depicts the charging time (σ_{cc}) and system coefficient of performance (COP_{sm}) in 418 different tank arrangements using the air-source heat pump. σ_{cc} in Case 1, Case 2, Case 3, 419 Case 4, Case 5, and Case 6 were 0.62 h, 0.58 h, 0.55 h, 0.49 h, 0.46 h, and 0.43 h, respectively. 420 Thus, σ_{cc} in Case 1 was the maximum, while σ_{cc} in Case 6 was the minimum. σ_{cc} in Case 421 1 was 1.44 times as high as σ_{cc} in Case 6. COP_{sm} in Case 1, Case 2, Case 3, Case 4, Case 5, 422 and Case 6 were 3.011, 3.0104, 3.0099, 3.0142, 3.0141, and 3.014, respectively. The difference 423 of COP_{sm} between different cases was very small. According to the results of σ_{cc} in different 424 cases, the tank arrangement in Case 6 was optimal because σ_{cc} in Case 6 was smaller than that 425 in the other case. However, according to the results of COP_{sm} in different cases, the tank arrangement in Case 4 was optimal because COP_{sm} was slightly higher than that in the other 426 427 case. Thus, it was important to identify the optimal tank arrangements based on the results in 428 Fig. 9 (a). Further analysis for identifying the optimal tank arrangements is presented in the Fig. 429 10.

430

431 Fig. 9 (b) depicts the stored energy (Q_{st}) and total electricity energy use (E_{tl}) in different tank 432 arrangements using the air-source heat pump. Q_{st} in Case 1, Case 2, Case 3, Case 4, Case 5, 433 and Case 6 were 2.41 kWh, 2.28 kWh, 2.15 kWh, 1.91 kWh, 1.8 kWh, and 1.7 kWh, 434 respectively. Thus, Q_{st} in Case 1 had its maximum, while Q_{st} in Case 6 had its minimum. 435 Q_{st} in Case 1 was 1.42 times as high as Q_{st} in Case 6. E_{tl} in Case 1, Case 2, Case 3, Case 4, 436 Case 5, and Case 6 were 0.8 kWh, 0.76 kWh, 0.72 kWh, 0.63 kWh, 0.6 kWh, and 0.56 kWh, 437 respectively. Thus, E_{tl} in Case 6 had its minimum, while E_{tl} in the Case 1 had its maximum. E_{tl} in Case 1 was 1.43 times as high as E_{tl} in Case 6. According to the structure parameters 438 439 in Table 2, the volume of PCM storage tank in Case 1 and Case 6 had its maximum and 440 minimum, respectively. Therefore, the difference of PCM storage tank volume might explain 441 the difference of Q_{st} and E_{tl} in different tank arrangements.



Fig. 9. (a) Charging time and system coefficient of performance, and (b) stored energy and total electricity
energy use in different tank arrangements using the air-source heat pump

446 Fig. 10 depicts the score of the overall performance (SR_{ov}) in different tank arrangements using 447 the air-source heat pump. PCM-4 was applied in this section. When the weight factor for σ_{cc} 448 $(\beta_{\sigma_{cc}})$ and the weight factor for COP_{sm} ($\beta_{COP_{sm}}$) were 0.4 and 0.6, SR_{ov} in Case 1, Case 2, 449 Case 3, Case 4, Case 5, and Case 6 were 0.16, 0.14, 0.14, 0.88, 0.94, and 0.97, respectively. 450 Thus, the tank arrangement in the Case 6 was optimal because SR_{ov} was the highest. When 451 $\beta_{\sigma_{cc}}$ and $\beta_{COP_{sm}}$ were 0.6 and 0.4, SR_{ov} in Case 1, Case 2, Case 3, Case 4, Case 5, and Case 452 6 were 0.11, 0.15, 0.22, 0.83, 0.91, and 0.98, respectively. Thus, the tank arrangement in the 453 Case 6 was optimal because SR_{ov} was the highest. It could be seen that no matter that σ_{cc} had a higher weighting or COP_{sm} had a higher weighting, the tank arrangement in Case 6 was 454 455 optimal. This meant that the balance of σ_{cc} and COP_{sm} in Case 6 could be better established 456 than that in the other cases.

457



458

459 Fig. 10. Overall performance score in different tank arrangements using the air-source heat pump

461 Fig. 11 (a) depicted the charging time (σ_{cc}) and system coefficient of performance (COP_{sm}) in 462 different tank arrangements using the water-source heat pump. PCM-4 was applied in this section. σ_{cc} in Case 1, Case 2, Case 3, Case 4, Case 5, and Case 6 were 0.38 h, 0.36 h, 0.33 h, 463 464 0.31 h, 0.29 h, and 0.27 h, respectively. Thus, σ_{cc} in Case 1 had its maximum, while σ_{cc} in 465 Case 6 had its minimum. σ_{cc} in Case 1 was 1.41 times as high as σ_{cc} in Case 6. COP_{sm} in 466 Case 1, Case 2, Case 3, Case 4, Case 5, and Case 6 were 3.4847, 3.466, 3.4704, 3.4787, 3.4793, 467 and 3.4624, respectively. The difference of COP_{sm} among different cases was small. However, 468 it could be still found that COP_{sm} in Case 1 was the highest, while COP_{sm} in Case 6 was the 469 lowest. According to the results of σ_{cc} for different cases, the tank arrangement in Case 6 was 470 optimal because σ_{cc} was smaller than that in the other case. However, according to the results 471 of COP_{sm} in different cases, the tank arrangement in Case 1 was optimal because COP_{sm} was 472 slightly bigger than that in the other case. Thus, it was necessary to identify the optimal tank 473 arrangement according to the results in Fig. 11 (a). Further analysis for identifying the optimal 474 tank arrangement is presented in Fig. 12.

475

476 Fig. 11 (b) depicts the stored energy (Q_{st}) and total electricity energy use (E_{tl}) in different tank 477 arrangements using the water-source heat pump. Q_{st} in Case 1, Case 2, Case 3, Case 4, Case 478 5, and Case 6 were 2.55 kWh, 2.41 kWh, 2.27 kWh, 2.09 kWh, 1.98 kWh, and 1.86 kWh, 479 respectively. Thus, Q_{st} in Case 1 was the maximum, while Q_{st} in Case 6 was the minimum. 480 Q_{st} in Case 1 was 1.37 times as high as Q_{st} in Case 6. E_{tl} in Case 1, Case 2, Case 3, Case 4, 481 Case 5, and Case 6 were 0.73 kWh, 0.7 kWh, 0.66 kWh, 0.6 kWh, 0.57 kWh, and 0.54 kWh, 482 respectively. Thus, E_{tl} in Case 6 had its minimum, while E_{tl} in Case 1 had its maximum. E_{tl} 483 in Case 1 was 1.35 times as high as E_{tl} in Case 6. The PCM storage tank volume in Case 1 484 and Case 6 were the maximum and minimum among these cases, respectively. This might be 485 the reason why Q_{st} and E_{tl} had its maximum in Case 1, and Q_{st} and E_{tl} had its maximum 486 in Case 6.



Fig. 11. (a) Charging time and system coefficient of performance, and (b) stored energy and total electricity
 energy use in different tank arrangements using the water-source heat pump

491 Fig. 12 depicts the score of the overall performance (SR_{ov}) in different tank arrangements using 492 the water-source heat pump. PCM-4 was applied in this section. When the weight factor of σ_{cc} $(\beta_{\sigma_{cc}})$ and weight factor of COP_{sm} $(\beta_{COP_{sm}})$ were 0.4 and 0.6, SR_{ov} in Case 1, Case 2, Case 493 3, Case 4, Case 5, and Case 6 were 0.6, 0.18, 0.38, 0.71, 0.79, and 0.4, respectively. Thus, the 494 495 tank arrangement in Case 5 was optimal because SR_{ov} was the highest. When $\beta_{\sigma_{cc}}$ and 496 $\beta_{COP_{sm}}$ were 0.6 and 0.4, SR_{ov} in Case 1, Case 2, Case 3, Case 4, Case 5, and Case 6 were 497 0.4, 0.19, 0.39, 0.69, 0.8, and 0.6, respectively. Thus, the tank arrangement in Case 5 was 498 optimal because SR_{ov} was the highest. It could be seen that no matter that σ_{cc} had a higher 499 weighting or COP_{sm} had a higher weighting, the tank arrangement in Case 5 was optimal. This 500 meant that the balance of σ_{cc} and COP_{sm} in Case 5 could be better established than that in 501 the other case.

502



503

504 Fig. 12. Overall performance score in different tank arrangements using the water-source heat pump

For the system using the air-source and water-source CO₂ heat pumps, the optimal cases about the tank arrangements were Case 6 and Case 5, respectively. According to the Eqn. (8), the identification of optimal cases was related to σ_{cc} , COP_{sm} , $\beta_{\sigma_{cc}}$, and $\beta_{COP_{sm}}$. It might be difficult to determine the optimal tank arrangements according to the single factor. However, this section gave guidelines how to identify the optimal tank arrangements, which was significant in the engineering applications.

512

513 **4. Discussion**

514 The performance of the system utilizing the CO₂ heat pumps to charge the PCM storage tank 515 was studied, considering charging time (σ_{cc}) and system coefficient of performance (COP_{sm}) as indicators. The effects of expansion valve opening (o_{ex}) , PCM types, and tube arrangements 516 517 on σ_{cc} , COP_{sm} , stored energy (Q_{st}) and total electricity energy use (E_{tl}) were analyzed. The 518 multi-criteria optimization approach was applied to identify the optimal o_{ex} , PCM types, and 519 tube arrangements. This study considered two kinds of CO₂ heat pumps (i.e., air-source and 520 water-source CO₂ heat pumps) as case studies. This study broke the traditional research paths 521 about the charging performance studies of PCM storage tank, which only studied the charging 522 process in the open loop and applied σ_{cc} as the indicator. This study established a different 523 research path, which considered the charging process in the closed loop, and applied both σ_{cc} and COP_{sm} as the indicators. This study not only filled the research gap of the investigations 524 525 of the system applying CO₂ heat pumps to charge the PCM storage tank, but also gave a 526 guideline for engineers to well determine optimal parameters of the system. Based on our study, 527 the future studies on the following topics may be initiated: (a) more advanced heat-source 528 devices (e.g., ground-source and solar-assisted CO₂ heat pumps) should be considered in the 529 investigations for the charging performance of the PCM storage tank in the closed loop. The 530 effects of different parameters (e.g., borehole depth in the ground-source CO₂ heat pump and 531 solar collector area in the solar-assisted CO₂ heat pump) on the system performance should be 532 considered; (b) different PCM types should be considered in the investigation of the charging 533 process. A dataset of PCM types should be established and applied in different charging systems. 534 The optimal PCM types for different charging systems could be better to be determined; (c) 535 optimal operating strategies (e.g., artificial neural network-based and self-adaptive optimal 536 control methods) for different charging systems should be constructed for obtaining smaller σ_{cc} and larger COP_{sm} . Our study gave a start point how to present and compare the results for 537 538 different improvements and specific system adjustments.

539 **5.** Conclusions

The performance investigation of using the CO₂ heat pumps to charge the PCM storage tank 540 541 was performed in this study. The modelling of the charging process was constructed by the 542 integration of the heat pump and PCM storage tank models. Experimental data were applied for 543 validating the reliability of these models. The influence of different expansion valve opening 544 (o_{ex}) , PCM types, and tube arrangements on the system performance were analyzed. Both the air-source and the water-source CO₂ heat pumps were considered in this study. The optimal 545 546 parameters were identified by maximizing the overall performance considering the balance 547 between the charging time (σ_{cc}) and system coefficient of performance (COP_{sm}). For the 548 systems using both air-source and water-source CO₂ heat pumps, σ_{cc} increased with the increase of o_{ex} . The optimal o_{ex} was 40% because σ_{cc} in was the shortest and COP_{sm} was 549 550 the highest. COP_{sm} in the cases when o_{ex} was 40% using the air-source and the water-source 551 CO₂ heat pumps were 2.83 and 3.31, respectively. For the systems using both the air-source and 552 the water-source CO₂ heat pumps, the optimal PCM was the PCM-4 with the melting 553 temperature of 19.6°C and the latent heat of 86 kJ/kg. COPsm when the PCM-4 was applied 554 using the air-source and the water-source CO₂ heat pumps were 3.01 and 3.48, respectively. For 555 the system using the air-source CO₂ heat pump, the optimal tank arrangement occurred at Case 556 6, in which the number of tubes in each column and row were 19 and 5, respectively. COP_{sm} 557 in Case 6 when the air-source CO_2 heat pump was applied was 3.014. For the system using the 558 water-source CO₂ heating pump, the optimal tank arrangement occurred at Case 5, in which the 559 number of tubes in each column and row were 20 and 5, respectively. COP_{sm} in Case 5 when 560 the water-source CO_2 heat pump was applied was 3.4793. In sum, for the systems using both 561 air-source and water-source CO₂ heat pumps, PCM-4 was the most suitable. For the system 562 using the air-source and water-source CO₂ heat pumps, the optimal cases about the tank 563 arrangements were Case 6 and Case 5, respectively. The identification of optimal cases was related to σ_{cc} , COP_{sm} , $\beta_{\sigma_{cc}}$, and $\beta_{COP_{sm}}$. It might be hard to determine the optimal tank 564 565 arrangement according to the single factor. However, this study could guide engineers to 566 identify the optimal o_{ex} , PCM types, and tank arrangements, which was significant in the 567 engineering applications.

568

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- 575

576 Appendix A. Performance analysis of discharging process

577 Fig. A1 (a) depicts the discharging time (σ_{dc}) and released energy (Q_{rs}) in different PCM types. When the PCM-1, PCM-2, PCM-3, PCM-4, PCM-5, and PCM-6 were used, σ_{dc} were 1.09 h, 578 579 1.5 h, 0.86 h, 1.06 h, 0.82 h, and 0.98 h, respectively. Thus, σ_{dc} was the minimum when the 580 PCM-5 was utilized, while σ_{dc} had its maximum when the PCM-2 was utilized. σ_{dc} when 581 the PCM-2 was utilized was 1.83 times as high as σ_{dc} when the PCM-5 was utilized. When 582 the PCM-1, PCM-2, PCM-3, PCM-4, PCM-5, and PCM-6 were used, Q_{rs} were 2.33 kWh, 3.2 583 kWh, 2.14 kWh, 1.92 kWh, 2.31 kWh, and 2.24 kWh, respectively. Thus, Q_{rs} had its maximum when the PCM-2 was utilized, while Q_{rs} had its minimum when the PCM-4 was 584 585 utilized. Q_{rs} when the PCM-4 was utilized was 1.67 times as high as Q_{rs} when the PCM-2 586 was utilized. It could be seen that in Table 1 the density of PCM-2 was higher than that of other 587 PCMs, and the density of PCM-4 was lower than that of other PCMs. The degree that the density 588 of PCM-2 was higher than that of other PCMs was evident, which caused that PCM-2 has higher 589 thermal capacity (i.e., multiplication of the specific heat and density). Meanwhile, PCM-4 has 590 lower latent heat. Thus, thermal properties of these PCMs might explain the difference of σ_{dc} 591 and Q_{rs} in different PCM types.

592

593 Fig. A1 (b) depicts σ_{dc} and Q_{rs} in different tank arrangements. σ_{dc} in Case 1, Case 2, Case 594 3, Case 4, Case 5, and Case 6 were 1.28 h, 1.23 h, 1.18 h, 1.1 h, 1.06 h, and 1.01 h, respectively. 595 Thus, σ_{dc} in Case 1 was the maximum, while σ_{dc} in Case 6 was the minimum. σ_{dc} in Case 596 1 was 1.27 times as high as σ_{dc} in Case 6. Q_{rs} in Case 1, Case 2, Case 3, Case 4, Case 5, and 597 Case 6 were 2.45 kWh, 2.33 kWh, 2.21 kWh, 2.02 kWh, 1.92 kWh, and 1.82 kWh, respectively. 598 Thus, Q_{rs} in Case 1 had its maximum, while Q_{rs} in Case 6 had its minimum. Q_{rs} in Case 1 599 was 1.35 times as high as Q_{rs} in Case 6. According to the structure parameters in Table 2, the 600 volume of PCM storage tank in Case 1 had its maximum, while the volume of PCM storage 601 tank in Case 6 had its minimum. Thus, the difference of PCM storage tank volume might 602 explain the difference of σ_{dc} and Q_{rs} in different tank arrangements.





606

Fig. B1 (a) depicts the variations of heating capacity (\dot{Q}_{gs}) , compressor power (\dot{W}_{cp}) , and 608 609 coefficient of performance of CO_2 heat pump (COP_{chp}) with different ambient air temperature 610 (T_{ab}) using the air-source heat pump. \dot{Q}_{gs} increased with the increase of T_{ab} . This might be 611 caused by that the increase of T_{ab} led to the increasing temperature difference between the 612 ambient air and CO₂ in the evaporator, which improved the heat transfer effect. When T_{ab} increased from 18°C to 24°C, \dot{Q}_{gs} varied from 3,488 W to 4,586.8 W, increased by 24%, 613 respectively. The variation trend was almost linear. \dot{W}_{cp} increased with the increased of T_{ab} . 614 615 When T_{ab} increased from 18°C to 24°C, \dot{W}_{cp} varied from 971 W to 1,069.5 W, increased by 9.2%. COP_{chp} increased with the increased of T_{ab} . The reason of this phenomenon might be 616 that the increasing degree of \dot{Q}_{gs} was larger than that of \dot{W}_{cp} . When T_{ab} increased from 18°C 617 618 to 24°C, COP_{chp} varied from 3.59 to 4.29, increased by 16.2%. 619

Appendix B. Effect of ambient temperature on performance of CO₂ heat pump



Fig. B1. Variations of (a) heating capacity, (b) compressor power, and (c) coefficient of performance with
 different ambient air temperature using the air-source heat pump

Fig. B2 (b) depicts the variations of \dot{Q}_{gs} , \dot{W}_{cp} , and COP_{chp} with different inlet mixture 625 626 temperature in evaporator $(T_{it,z})$ using the water-source heat pump. \dot{Q}_{gs} increased with the 627 increase of $T_{it,z}$. The reason might be the enhancement of the heat transfer effect caused by the 628 increasing temperature difference between the inlet mixture and CO₂ in the evaporator. When $T_{it,z}$ increased from 18°C to 24°C, \dot{Q}_{gs} varied from 4,721.5 W to 7,075.8 W, increased by 629 630 49.9%, respectively. \dot{W}_{cp} increased with the increased of $T_{it,z}$. When $T_{it,z}$ increased from 18°C to 24°C, \dot{W}_{cp} varied from 1,082.5 W to 1,310 W, increased by 21%. COP_{chp} increased 631 with the increased of $T_{it,z}$. This might be caused by that the increasing degree of \dot{Q}_{gs} was 632 larger than that of \dot{W}_{cp} . When $T_{it,z}$ increased from 18°C to 24°C, COP_{chp} varied from 4.36 633 634 to 5.4, increased by 23.8%.



Fig. B2. Variations of (a) heating capacity, (b) compressor power, and (c) coefficient of performance with
 different inlet mixture temperature in evaporator using the water-source heat pump

641 Appendix C. Exergy analysis

642 The exergy efficiency of the PCM storage tank (η_{ey}) was calculated by Eqn. (C1):

643

$$\eta_{ey} = \frac{EX_{st}}{EX_{sd}} \tag{C1}$$

644 where EX_{st} and EX_{sd} denote the stored and supplied exergy by the water, respectively. The 645 calculation of EX_{st} and EX_{sd} referred to the study of Cheng et al. [51]. EX_{st} was calculated 646 by Eqn. (C2):

647

$$EX_{st} = EX_{wt} + EX_{pc} \tag{C2}$$

648 where EX_{wt} and EX_{pc} denote the exergy stored in the water and PCM, respectively. EX_{wt} 649 was calculated by Eqn. (C3):

650 $EX_{wt} = \sum_{i} M_{wt,i} c_{wt} (T_{ab} ln \frac{T_{in}}{T_{wt,i}} + T_{wt,i} - T_{in})$ (C3)

651 where *M* and *c* denote the mass and specific heat, respectively. EX_{pc} was calculated by Eqn. 652 (C4):

$$EX_{pc} = \sum_{i} \int_{T_{in}}^{T} M_{pc,i} \left(\frac{T_{ab}}{T} - 1\right) dh(T)$$
(C4)

654 where *h* denotes the enthalpy. EX_{sd} was calculated by Eqn. (C5):

655
$$EX_{sd} = \int_0^t \dot{m}_{wt} c_{wt} (T_{ab} ln \frac{T_{wt,ot}}{T_{wt,it}} - T_{wt,ot} + T_{wt,it}) dt$$
(C5)

656

657 Fig. C1 depicts the variations of exergy efficiency (η_{ev}) with different PCM types and tank 658 arrangements using the air-source heat pump. When the PCM-1, PCM-2, PCM-3, PCM-4, 659 PCM-5, and PCM-6 were used, η_{ey} were 14.2%, 15.9%, 18.7%, 31.8%, 22.7%, and 41.2%, 660 respectively. Thus, η_{ey} was the minimum when the PCM-1 was utilized, while η_{ey} was the maximum when the PCM-6 was utilized. η_{ey} when the PCM-6 was utilized was 2.9 times as 661 662 high as η_{ey} when the PCM-1 was utilized. η_{ey} in Case 1, Case 2, Case 3, Case 4, Case 5, and 663 Case 6 were 38.2%, 36.3%, 33.3%, 32%, 31.7%, and 30.7%, respectively. Thus, η_{ev} in Case 664 6 had its minimum, while η_{ev} in Case 1 had its maximum. η_{ev} in Case 1 was 1.24 times as 665 high as η_{ey} in Case 6. According to the Eqn. (C1), the variation of η_{ey} was determined by 666 the variations of EX_{st} and EX_{pc} . When the increasing degree of EX_{st} was larger than that of 667 EX_{pc} , η_{ey} would increase, and vice versa.



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high as η_{ey} when the PCM-2 was utilized. η_{ey} in Case 1, Case 2, Case 3, Case 4, Case 5, and Case 6 were 55.1%, 55.1%, 55%, 55.8%, 55.7%, and 55.5%, respectively. Thus, η_{ey} in Case 3 had its minimum, while η_{ey} in Case 4 had its maximum. η_{ey} in Case 4 was 1.01 times as high as η_{ey} in Case 3. According to the Eqn. (C1), the relative increasing or decreasing degree of EX_{st} and EX_{pc} were the reason for the variations of η_{ey} in different PCM types and tank arrangements.





Fig. C2. Variations of exergy efficiency with different (a) PCM types and (b) tank arrangements using the water-source heat pump

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