

31 1. INTRODUCTION

32 Fires in European tunnels, e.g., in the Mont Blanc tunnel (France/Italy) in 1999 or in the Tauern
33 tunnel (Austria) in 1999, have clearly shown the risks and consequences of high thermal loads on
34 reinforced concrete (RC) structures. The mechanical behaviour of such structures subjected to a
35 fire depends on many different factors, such as the constitutive behaviour of concrete and steel and
36 the type of structural member affected. Therefore, the investigation and understanding of RC
37 structures exposed to fire has always been a challenge¹⁻⁸.

38 Comprehensive experimental research at material level has been carried out in recent decades
39 to test normal-strength concrete (NSC) subjected to elevated temperatures⁹⁻²⁰. The use of high-
40 strength concrete (HSC) has become increasingly popular compared to NSC due to its greater
41 stiffness and strength (70–120 MPa). However, HSC is more sensitive to high temperatures due to
42 its low porosity, which favours steam pressure build-up and increased susceptibility to explosive
43 spalling. To avoid this, one commonly adopted solution is to add polypropylene (PP)
44 microfibres^{21,22}.

45 When concrete is exposed to elevated temperatures, its mechanical properties (such as strength
46 and stiffness) are usually adversely affected²³. However, the increased material deformability,
47 another consequence of exposure to high temperatures, may help redistribute the stress at a
48 structural level. Therefore, the considerable decrease in the mechanical properties of concrete may
49 not directly result in a drastic decrease in the ultimate load-carrying capacity of the structural
50 member^{6,24}. Characterization of the material at elevated temperatures is therefore insufficient.

51 The literature contains many studies that have investigated the effect of fire on RC structural
52 members, such as beams²⁵⁻³⁰, slabs³¹⁻³⁴ or tunnel linings³⁵⁻³⁸. Despite all the research available,
53 new recommendations and approaches for the design and assessment of concrete structures and

54 structural components to protect against fire are still being published to this day^{8,39-42}. Clearly the
55 subject is a complex one, not yet fully investigated.

56 The investigation of RC slabs subjected to elevated temperatures is also of great interest for the
57 Norwegian Public Roads Administration's *Ferry-free coastal route E39* project. This project is
58 aimed at establishing a coastal highway route without ferry connections. New large concrete
59 structures, including a submerged floating tunnel (SFT)⁴³, need to be built to cross the wide and
60 deep fjords along the coast. It is then of interest to evaluate the combined action of fire and blast
61 loads inside tunnels⁴⁴. Due to the complexity of such extreme load conditions, this represents a
62 great challenge.

63 In this context, RC slabs can be a representative component of the SFT concrete structure. A
64 first and fundamental step is to achieve a full understanding of slab behaviour at elevated
65 temperatures under static loading conditions. The following experimental programme consisting
66 of three phases was therefore defined to investigate: i) the mechanical characterization of concrete
67 at high temperatures²³, ii) the impact of the combination of fire and static loading on RC circular
68 slabs (present study), and iii) the impact of the combination of fire and dynamic loading on RC
69 circular slabs⁴⁵. The findings will make it possible to do the risk analysis and the feasibility study
70 for the SFT in the E39 project.

71 Fire curves are used in the design of RC structures; e.g., the hydrocarbon fire curve is typically
72 used for the design of tunnels⁴⁶. In the event of a hydrocarbon fire, stresses due to large thermal
73 gradients during heating induce thermal damage to the structural member. Such damage is
74 irreversible in concrete material, and may even increase during the cooling phase due to the
75 appearance of additional thermal stresses^{47,48}. In an accidental fire scenario inside a tunnel, the
76 most thermally damaged part corresponds to the compressive side of the structural member's

77 cross-section⁴¹. Testing in residual conditions, i.e., with a cooling phase after heating, the steel
78 reinforcement recovers all its mechanical properties after cooling while the concrete undergoes
79 irreversible degradation. Testing with both the fire and the static load on the same side of the
80 specimen, is therefore generally more conservative, since it represents a worst-case scenario for
81 the overall structural behaviour.

82 The main objective of this research was to investigate the influence of high temperatures on the
83 load-bearing capacity of RC slabs. For this purpose, the structural response of RC circular slabs
84 subjected to a static load in residual conditions, after exposure to a hydrocarbon fire, was
85 investigated. Although the situation examined experimentally may be different to those observed
86 in practice (Load Induced Thermal Strain –LITS– were not taken into account in this study), the
87 experimental data presented in this work aims to define a reliable benchmark for numerical models
88 which, upon numerical upscaling, will be instrumental for the design of tunnels under exceptional
89 load conditions. Simplified mechanical models were used to understand the behaviour of the
90 specimen during the tests. The yield-line approach was used to evaluate the effect of high
91 temperatures on the bending capacity of the slab. The contribution of the arching mechanism and
92 tensile membrane action on the structural response of the slab was also investigated.

93 **2. METHODOLOGY**

94 **2.1. Experimental programme**

95 This study investigated the structural response of RC circular slabs after exposure to hydrocarbon
96 fire. A total of six specimens were tested under static loading. Four of them were subjected to fire
97 exposure prior to the static test. Two reference non-exposed specimens were used for comparison.
98 Two fire exposure times were considered ($t = 60$ and 120 min). Thermocouples embedded in two

99 specimens were used to measure the temperature distribution across the thickness. Ultrasonic pulse
100 velocity (UPV) measurements were obtained in the specimens before and after exposure to the
101 fire. All the slabs were tested at room temperature under quasi-static load conditions and the load-
102 deflection response was measured. Table 1 summarizes the whole experimental campaign. The
103 nomenclature of the specimens is defined as $ST-n$, where T is the fire exposure time (0, 60 or 120),
104 and n is the number of the nominally identical test (1 or 2).

105 **2.2. Materials**

106 Grade C45/55 concrete was used, with a water-cement ratio (w/c) of 0.42, and a maximum
107 aggregate size (d_{\max}) of 16 mm. Table 2 details the concrete mix design and proportions. The
108 aggregates (siliceous rock) included granite, gneiss, sandstone and siltstone. Polypropylene
109 microfibres were also added to the mix (1 kg/m^3). The density (ρ) at 28 days after casting was
110 2370 kg/m^3 . The compressive strength of the concrete was 73 MPa, calculated as the mean strength
111 of three cylinders (100×200) at 202 days after casting.

112 An extensive research on the mechanical properties of this type of concrete in residual
113 conditions after single thermal cycles at elevated temperatures was previously performed by the
114 same authors²³. In that research, the evolution of the mechanical properties for four different
115 temperatures (20, 200, 400 and 600 °C) was evaluated. Standard concrete cylinders (100×200 mm)
116 were subjected to uniaxial compressive testing (UCT) to measure the change in their modulus of
117 elasticity, using the standard ISO procedure⁴⁹, and their compressive strength. Uniaxial tensile
118 testing (UTT) was also carried out on concrete cylinders (100×100 mm) to measure the evolution
119 of direct tensile strength. Three nominally identical specimens were tested for each temperature
120 level in the UCT, while two specimens were tested in the UTT. Further details on the test set-up
121 and instrumentation can be found in Arano et al.²³.

122 The UCT and UTT were displacement-controlled, so complete stress-strain and crack opening
123 displacement (COD) curves were obtained. This enabled the investigation of additional material
124 properties, such as the specific compression and tension fracture energy at elevated temperatures
125 and the evolution of internal damage. For the sake of brevity, these results are not given here, but
126 they are extensively discussed in Arano et al.²³. In the same paper²³, the relationship between the
127 damage of concrete material and the ultrasonic pulse velocity (UPV) measurements is presented.

128 Traditional B450 steel was used for the reinforcement bars ($\text{Ø}6$). The mechanical properties of
129 this type of steel were evaluated after single thermal cycles at elevated temperatures (200, 400 and
130 600 °C). Eight steel reinforcing bars were tested in uniaxial tension in accordance with ISO
131 standards⁵⁰, using an INSTRON machine with a maximum capacity of 200 kN. Two nominally
132 identical specimens were tested for each temperature level, where the yielding and ultimate
133 strengths were measured. After the tests, the elongation at failure was measured in accordance with
134 ISO standards⁵⁰. The tests were displacement-controlled using a high-accuracy transducer with a
135 gauge length of 50 mm placed in the central part, which measured the elongation of the rebar until
136 it reached 2%. An internal transducer in the machine was then used to follow the test until complete
137 failure of the specimen.

138 Table 3 summarizes the average results of the main mechanical properties for both concrete and
139 steel materials at different high temperatures. As seen, the compressive ($f_{c,T}$) and tensile ($f_{ct,T}$)
140 strengths and the modulus of elasticity ($E_{c,T}$) of this type of concrete all decrease considerably
141 after exposure to high temperatures, unlike the results of the yielding ($f_{y,T}$) and ultimate strength
142 ($f_{t,T}$) of the steel rebar, which confirms the strong recovery of the mechanical properties of this
143 type of steel during the cooling phase.

144 **2.3. Geometry of the slabs**

145 In the present study, the specimens tested were RC circular slabs of 690 mm diameter and 70 mm
146 thickness. The slabs were reinforced with two orthotropic grids ($\text{Ø}6/60$ mm in both x and y
147 directions) top and bottom with a cover of 10 mm. Fig. 1 shows the geometry and pictures of the
148 specimen during preparation and after casting.

149 The specimen size and reinforcement layout were dictated by the dimensions of the equipment
150 used for the dynamic experimental testing part of the programme, which is reported in Colombo
151 et al.⁴⁵.

152 **2.4. Description of the tests**

153 *2.4.1. UPV measurements*

154 Direct UPV measurements were taken to quantify the stiffness reduction produced by the thermal
155 exposure across the thickness of the specimen (Fig. 2). UPV measuring devices (E49, CONTROLS
156 Group, Italy), with two piezoelectric transducers (emitter and receiver) located on opposite
157 surfaces of the slab, as shown in Fig. 2b, were used. Gel was added between the transducer and
158 the specimen's surface to ensure full acoustic contact. The measurements for each specimen were
159 taken at six different locations (U1–U6) across the slab surface, before and after the fire tests.
160 Points U1–U3 were located at 50 mm from the centre of the specimen, and points U4–U6 were
161 located at 170 mm from the centre; see Fig. 2a.

162 *2.4.2. Fire Tests*

163 Four specimens were exposed to fire prior to the static tests (Table 1). Hydrocarbon fire, typical
164 of tunnels⁴⁶, was applied by means of an electric gas burner to a centred circular region (diameter
165 360 mm) of what had been the top surface of the specimen during casting. A thermal sensor inside
166 the burner was used to automatically regulate the intensity of the flame to achieve the predefined

167 curve. Two fire cases were considered, with fire durations of 60 and 120 min, respectively. A fire
168 exposure time of 120 min corresponds to the case of a tunnel as the primary structure with tanker
169 truck traffic⁴⁶. The specimens were able to freely expand during the tests and were naturally cooled
170 in an open environment after the duration of the fire. Fig. 3 presents the set-up for the fire tests,
171 and a picture of the burner equipment. The test set-up required the specimens to be arranged
172 vertically.

173 One of the two specimens in each fire exposure case was fitted with four temperature sensors
174 (T1–T4) to measure the temperature distribution across the thickness of the slab. *Type-K chromel-*
175 *alumel thermocouples* (0.91 mm thick) were embedded at three different depths during preparation
176 of the specimens. Thermocouples T1–T3 were located at the centre of the specimen, at a distance
177 of 54, 35 and 16 mm from the “hot surface”, while T4 was located at 150 mm from the centre at
178 16 mm from the “hot surface”, see Fig. 3a. Temperature measurements were acquired with a time
179 step of 1.146 s, obtaining an almost continuous temperature evolution throughout the tests.

180 2.4.3. *Static Tests*

181 Static tests were performed to evaluate the structural behaviour of the six RC slabs. Two nominally
182 identical tests were performed for each fire duration (60 and 120 min), in addition to two tests on
183 the non-exposed specimens (see Table 1). The tests were displacement-controlled by means of an
184 electromechanical jack with a maximum capacity of 400 kN. The displacement rate was 50 $\mu\text{m/s}$
185 up to a load of 100 kN and 80 $\mu\text{m/s}$ up to failure. The vertical deflection of the specimens was
186 measured by a linear variable differential transformer (LVDT) located at the centre of the rear
187 surface.

188 A circular steel ring of 320 mm in major diameter (d_e) was used to apply the load. The
189 specimens were loaded on the surface where the fire was previously applied (top surface during

190 casting). A thin layer of neoprene was placed under the loading ring to distribute the load at the
191 contact point between the steel ring and the specimen surface. The specimens were simply
192 supported on a circular steel ring of 550 mm in minor diameter. Both rings had a radial thickness
193 of 30 mm. Fig. 4 shows the set-up for the static tests.

194 The dimensions of the support ring were chosen in accordance with the dimensions of the
195 support scheme of the dynamic tests. This is why no neoprene layer was placed between the slab
196 surface and the support ring. In the dynamic tests, the load is applied as a pressure wave, i.e., a
197 uniformly distributed load on the slab surface. Due to the difficulty of reproducing a uniformly
198 distributed load under displacement control in a static test, the equivalent linear ring load was
199 adopted to postpone the punching failure which would typically result from a concentrated load.
200 A preliminary numerical investigation, which results are not shown here for the sake of brevity,
201 was performed to determine the dimensions of the loading ring required to obtain a load-deflection
202 behaviour similar to the result of a distributed load, resulting in a loading ring with an external
203 diameter $d_e = 320$ mm.

204 **3. EXPERIMENTAL RESULTS**

205 **3.1. Fire tests results**

206 Fig. 5 presents the results of the temperature evolution measured during the fire tests on specimens
207 S60-1 and S120-1. The different colours represent each of the four thermocouples (T1–T4)
208 embedded in the specimens (Fig. 3). The figure also shows the fire curve (in black) for each test.
209 In the 60-min fire test, temperatures of about 680, 640, 480 and 360 °C were reached at locations
210 T3, T4, T2 and T1, respectively (Fig. 5a). In the 120-min fire exposure, the maximum temperatures
211 measured at the same locations were about 870, 800, 690 and 480 °C (Fig. 5b). The measured

212 temperature evolution up to 60 min was very similar in the two fire exposures, which indicates
213 good repeatability in the tests.

214 The values from T1–T3 were interpolated to obtain the temperature distribution across the
215 whole thickness of the slab at different instants of time (t_i). Eq. (1) shows the exponential fit used,
216 which describes the corresponding temperature value T for each point at a distance h from the
217 “cold surface”, across the thickness of the slab. The coefficients a_i and b_i were calibrated from the
218 experimental data and are shown in Table 4.

$$T = e^{\left(\frac{h-b_i}{a_i}\right)} \quad (1)$$

219 Fig. 6 shows the evolution of the temperature profile throughout the heating phase of the 60-
220 and 120-min fire tests at the central cross-section (T1–T3). Each colour denotes a different instant
221 during the test ($t_i = 30, 60, 90$ and 120 min). The experimental measurements are shown as filled
222 circles, while the continuous line corresponds to the fitted values. The temperature values obtained
223 at T4 are also shown for comparison, displayed as empty circles. The maximum experienced
224 concrete temperature at the bottom and top surfaces as well as the steel temperatures (see sensors
225 T1 and T3) can be read from Fig. 6.

226 As expected, a hydrocarbon fire curve leads to a nonlinear temperature profile across the cross-
227 section due to the rapid increase in temperature. The results from the two cases investigated show
228 that the profile remains nonlinear throughout the whole test, though with a slight tendency towards
229 a linear shape if $t_i = 30$ and $t_i = 120$ min in Fig. 6b are compared. A big thermal gradient is
230 observed between the two surfaces of the specimen, reaching a temperature difference of about
231 720 °C for the 60-min fire exposure and about 790 °C for the 120-min exposure time.

232 The large thermal gradient across the thickness and in the radial direction leads to non-
233 homogeneous thermal expansion which induces additional stresses. Fig. 7 shows the visible crack

234 pattern for the different specimens after the fire tests. A similar crack pattern can be seen for all
235 the specimens tested. On the exposed surface, radial cracks start some distance from the centre and
236 extend towards the edge of the slab in all directions. The non-exposed side, however, presents
237 tensile cracks localized in the centre of the specimen surface. Despite the presence of
238 polypropylene microfibres, minor explosive spalling was observed during the first minutes of the
239 tests. The spalling was localized in a region of the exposed surface as highlighted in Fig. 7.

240 Direct UPV measurements were taken across the thickness of the specimens, before and after
241 exposure, to quantify the stiffness reduction caused by the fire. Table 5 summarizes the average
242 pulse velocity before (v_0) and after the fire test (v_t), for both exposure times ($t = 60$ and 120 min),
243 together with the standard deviation (SD) of the six points evaluated (U1–U6). The ratio between
244 the two velocities is also shown.

245 The average pulse velocity before the fire test was 4.70 km/s. After the fire exposure, the pulse
246 velocity has considerably decreased, especially after the longer exposure. The average pulse
247 velocity of the specimens subjected to a 60-min fire test decreased to 2.61 km/s, while it decreased
248 to 2.21 km/s after an exposure of 120 min. These represent reductions of about 45% and 53%, with
249 respect to their values before the fire exposure. These UPV decreases quantify the cross-section
250 stiffness reduction due to the material degradation under fire exposure.

251 **3.2. Static tests results**

252 Fig. 8 shows the complete load-deflection response for all the slabs subjected to the static test.
253 Each nominally identical test is denoted with a different line type (solid or dashed), while the
254 different colours represent the three fire exposure cases (0, 60 and 120 min).

255 The load-deflection curves show two peaks corresponding to two separate mechanisms. The
256 peak of the stiffer mechanism (point D) corresponds to the arching mechanism, while the peak of

257 the ultimate load (point F) is related to tensile membrane action (TMA). The different stages of
258 such mechanisms are indicated in the load-deflection curve of specimen S0-2 in Fig. 8. Prior to
259 cracking, the behaviour of the slab is elastic (from A to B), until the first cracks appear at point B.
260 In the intervals B–C and C–D, the slab exhibits an elastic-plastic phase, in which the arching
261 mechanism is fully developed. The visible change of slope at point C is caused by the yielding of
262 reinforcement. The maximum arching effect is achieved at Point D. After the rupture of the arch,
263 the load considerably decreases. The remaining capacity (point E) corresponds to the pure bending
264 capacity of the slab. TMA develops in the last stage (from E to F), increasing the load until the
265 steel rebars reach their ultimate strain⁵¹. The behaviour described was very similar for all the tested
266 specimens, indicating that the same mechanisms were also at work in the slabs subjected to fire
267 exposure.

268 Fig. 9a shows a close-up of the load-deflection results. Fig. 9b shows the relative average value
269 of the arch peak load ($P_{u,t}$) and the deflection at the arch peak load ($\delta_{1,t}$) for the different exposure
270 cases, with respect to the average values for the non-exposed specimens ($P_{u,0}$ and $\delta_{1,0}$).

271 The values of $P_{u,t}$ and $\delta_{1,t}$ are lower after fire exposure for all the specimens. The average arch
272 peak load was 327 kN for the non-exposed slabs. This load was down to 210 and 179 kN after
273 exposure to the 60- and 120-min fire tests, respectively. These values represent decreases of 36%
274 and 45% in the peak load. The average deflection at such a load for the non-heated case is 14.4
275 mm. After fire exposure, the deflection was reduced to 7.9 and 7.7 mm, respectively representing
276 decreases of 45% and 47%.

277 Despite the strong effect of fire exposure on the arching mechanism, Fig. 8 shows a similar
278 load-deflection trend when TMA develops, with the exception of specimen S0-1. The ultimate
279 load was 286 kN for the other non-exposed slab (S0-2), which was similar to the average ultimate

280 load reached by the exposed specimens (294 and 272 kN, respectively), regardless of the fire
281 exposure time. This is further evaluated in Section 5.2.

282 Fig. 9a shows a change in the initial stiffness of the slab after fire exposure. While non-exposed
283 specimens show an initial slope corresponding to elastic stiffness, the specimens that have been
284 exposed to fire have reduced stiffness. When a specimen is subjected to fire, the material across
285 the thickness is progressively exposed to high temperatures, and therefore the thermal damage
286 increases across the thickness. The decrease in the initial stiffness can be quantified by analysing
287 the initial slope of the load-deflection curve. The results show an average decrease of about 35%
288 after a fire exposure of 60 min, and about 50% after 120 min. These reductions are slightly lower
289 than those obtained from the direct UPV measurements (Table 5) because they also consider the
290 contribution of the steel reinforcement, which is characterized by negligible damage since the tests
291 were performed in residual conditions. It is worth to note that the reduction on the UPV
292 measurements does not consider the strain profile of a bent cross-section but simply gives an
293 average of the concrete degradation over the thickness.

294 Fig. 10 shows pictures of all the specimens after the static tests. These pictures confirm that the
295 same arch failure mechanism occurred for all the different tests, as highlighted in the comparison
296 of the load-deflection responses.

297 **4. SIMPLIFIED APPROACH**

298 **4.1. Description of analytical model**

299 In order to comprehend and explain the results from the experimental tests, analytical calculations
300 with simplified mechanical models were carried out. The yield-line method, first presented by
301 Johansen⁵², was used, since it is a well-known approach commonly used for the moment analysis

302 of RC slabs⁵³. The yield-line pattern depends on the geometry and load conditions of the structure.
303 In the case of the simply supported circular RC slabs evaluated in the present work, the yield
304 pattern is shown in Fig. 11.

305 The principle of virtual work is commonly used when applying the yield-line method to
306 calculate the ultimate load. This method is based on the equilibrium between the work from the
307 external loads and internal actions, when a virtual displacement δ is assumed at a certain point in
308 the slab. Following this procedure, the ultimate load P_f for the given slab is presented in Eq. (2).
309 Since this method is widely used, the whole procedure is not described here for the sake of brevity.

$$P_f = \pi \left(1 + \frac{R^*}{\bar{R}} \right) (m_x + m_y) \delta \quad (2)$$

310 In Eq. (2), \bar{R} and R^* are the distances from the support to the load ring ($\bar{R}=115$ mm) and from
311 the load to the centre of the slab ($R^*=160$ mm), respectively. The moments m_x and m_y are the
312 resistance moments of the section in the two directions, which are the same in the case of an
313 orthotropic reinforcement grid, characterized by the same reinforcement ratios $\rho_x = \rho_y$, neglecting
314 the small difference between the reinforcement distance from the top surface $d_x \cong d_y = 54$ mm
315 ($m_x = m_y = m$).

316 This method was applied for the three fire scenarios ($t = 0, 60$ and 120 min). Assuming, as a
317 simplification, no variation in the yield pattern, the moment resistance (m) of the cross-section is
318 the only changing variable between the scenarios. The moment resistance was calculated under
319 the support, where the circular yield-line is located. The thermal damage was accounted for by
320 including the temperature distribution measured experimentally in the calculation of the moment
321 resistance. The moment obtained was assumed for the whole yield pattern.

322 The specimens were tested in residual conditions, with a cooling phase after the fire exposure.
323 As previously described, steel material properties experience a great recovery for temperatures up

324 to 600 °C. Full recovery of the material performance was considered for both reinforcement layers,
 325 which is reasonable if evaluating the temperature results obtained, especially for the lower steel
 326 grid. Concrete properties, in contrast, differ considerably depending on the maximum temperature
 327 reached. The different thermal damage was then accounted for by dividing the compressive zone
 328 into several layers and defining the stress value for each layer depending on the temperature and
 329 strain level.

330 A stress-strain relationship based on uniaxial compressive tests was used for each temperature,
 331 following the procedure of the new draft of the Eurocode 2 Part 1–2⁵⁴. In the code, the response
 332 of concrete to uniaxial compression at elevated temperatures is described using the relationship
 333 presented in Eq. (3), where $f_{c,\theta}$ and $\varepsilon_{c1,\theta}$ are respectively the compressive strength and strain at
 334 maximum stress at a temperature θ .

$$\varepsilon \leq \varepsilon_{c1,\theta}: \sigma(\theta) = \frac{3 \varepsilon f_{c,\theta}}{\varepsilon_{c1,\theta} \left(2 + \left(\frac{\varepsilon}{\varepsilon_{c1,\theta}} \right)^3 \right)} \quad (3)$$

335 This relationship describes the concrete behaviour up to $\varepsilon_{c1,\theta}$. The descending branch can be
 336 treated as linear until the ultimate limit concrete strain at the evaluated temperature, $\varepsilon_{cu,\theta}$. This
 337 material model was used, adopting the experimental values of $f_{c,\theta}$, $\varepsilon_{c1,\theta}$ and $\varepsilon_{cu,\theta}$ presented in
 338 Arano et al.²³. Fig. 12a shows the good agreement between the adapted model and the experimental
 339 curves available for 200, 400 and 600 °C. For the other temperatures, $\varepsilon_{c1,\theta}$ was exponentially fitted,
 340 as also reported by Felicetti et al.¹¹, while $\varepsilon_{cu,\theta}$ was linearly fitted. Fig. 12b shows the resulting
 341 simplified 3D constitutive matrix.

342 A linear strain distribution in the sectional analysis of the cross-section was assumed, defining
 343 the maximum compressive strain in the concrete at the edge of the cross-section (ε_{c0}) as $\varepsilon_{c1,\theta}$, and
 344 using the maximum temperature reached at that point. Eurocode 2 proposes a similar procedure⁵⁴,

345 alternatively estimating ε_{c0} as 40% higher than the strain at peak stress for the mean temperature
346 reached across the section. The moment resistance of the cross-section for each fire case was then
347 obtained, determining the bending capacity of the RC slab.

348 **4.2. Analytical results**

349 This subsection presents a comparison between the bending capacity calculated for the different
350 fire exposure cases using the yield-line method with the experimental results.

351 Fig. 13 shows an example of the sectional analysis performed to compute the ultimate unitary
352 bending moment of the cross-section, corresponding to the 60-min fire case. The temperature,
353 strain and stress profiles are illustrated in Fig. 13(a–c). In the figure, $T_{c,j}$, $\varepsilon_{c,j}$ and $\sigma_{c,j}$ denote the
354 temperature, strain, and stress value, respectively, for each layer (j) of the concrete compressive
355 zone, while the tensile contribution of concrete is neglected according to the traditional RC theory.
356 The neutral axis (*N.A.*) is also shown. The strains and stresses in the two reinforcement layers are
357 denoted ε_s and σ_s for the grid on the cold side, and ε_s' and σ_s' for the grid on the exposed side.
358 Fig. 13d is a close-up of the compressive zone to illustrate $\sigma_{c,j}$.

359 Following the analytical procedure described, the calculated moment resistance was 14.42,
360 10.23 and 9.19 kNm/m for the unexposed, 60-min fire, and 120-min fire cases, respectively. The
361 yield-line solution presented in Eq. (2) was then applied and the bending failure loads equal to
362 217, 154, and 138 kN for the three cases, respectively, were found.

363 Fig. 14 shows a comparison between the predicted values, represented as horizontal lines, and
364 the experimental curves from the static tests. The values obtained using the analytical approach
365 were very similar to the plateau stage of the experimental curves. As previously mentioned, the
366 remaining capacity after the arching mechanism fails corresponds to the bending capacity of the

367 slab, which is why there is good agreement between the analytical values and the experimental
368 results.

369 **5. DISCUSSION OF RESULTS**

370 The results obtained during the fire and static tests are discussed separately in this section. An
371 evaluation of the crack patterns obtained during the fire tests is firstly carried out. The influence
372 of the high temperatures on the load-carrying capacity of RC slabs is then discussed by
373 investigating the various stages of the load-deflection response.

374 **5.1. Cracking profile after the fire test**

375 In this study, four RC slabs were exposed to a hydrocarbon fire applied in the central area of the
376 specimen surface (Fig. 3). The elevated temperatures induce an expansion of concrete and steel
377 materials, which causes the formation of cracks across the specimens. The visible crack profile
378 after the test can be divided into tensile and radial cracking.

379 Tensile cracks on the non-exposed surface commonly appear due to self-equilibrating stresses.
380 A hydrocarbon fire, with its rapid increase of temperature, causes a nonlinear temperature
381 distribution across the thickness of the specimen. Virtually free thermal strain is thermal expansion
382 at every point of the cross-section due to the temperature distribution. Since plane sections tend to
383 remain plane, however, the actual deformation of the section is linear. The difference between the
384 actual linear strain and the free nonlinear thermal strain is restrained, causing self-equilibrating
385 stresses⁵⁵. When the fire is acting on the specimen, the nonlinear distribution induces compressive
386 stresses at both edges of the cross-section and tensile stresses in the middle. During the cooling
387 phase, on the other hand, the two surfaces of the specimen undergo faster cooling, while the centre
388 of the section remains “hot”, inducing the opposite stresses. When the tensile stresses are higher

389 than the concrete tensile strength, cracking occurs. As shown in Fig. 7, these cracks are limited to
390 the central area of the cold surface.

391 On the exposed hot surface, the tested specimens presented radial cracks. The origin of these
392 cracks can be found if we examine the set-up used during the fire tests (see Fig. 3). The fire was
393 applied in the central area ($\text{Ø}360$ mm) of the total specimen surface ($\text{Ø}690$ mm). The inner part is
394 therefore subjected to a considerably higher temperature, and its greater thermal expansion
395 induces, because of compatibility, a pressure on the outer part, causing tensile stresses. When these
396 stresses reach the tensile strength of concrete, a crack occurs in the outer part of the surface and
397 propagates towards the edge.

398 This phenomenon can be illustrated with the following simplified model to calculate the
399 temperature difference necessary to form the first crack in the outer part. The model refers to the
400 force method and adopts the superposition principle to compute the internal stress of the specimen.
401 As mentioned, the specimen is divided into two parts: an inner “hot” (H) area and an outer “cold”
402 (C) area. Each part is assumed to have a uniform constant temperature and the difference between
403 the two parts is defined as ΔT . The radius of the inner part can be determined experimentally by
404 analysing the average radius (R_{avg}) of the visible starting point of the various radial cracks in the
405 tested specimens, as shown in Fig. 15a. The radius is 225 mm. It can be seen that the crack initiation
406 is very consistent between the different specimens.

407 Fig. 15b shows a simplified sketch of the different contributions that have been considered in
408 the application of the superposition principle. The inner core radius tends to enlarge (Δr_t) due to
409 thermal expansion and applies, because of compatibility, a pressure (p) on the outer part that is
410 colder and therefore characterized by less thermal expansion. This pressure causes a radial
411 displacement in the outer (δ_o) and inner part (δ_i), which can be determined using the Lamé

412 equations for thick-walled solids subjected to internal and external pressure, respectively⁵⁶.
 413 Imposing the inner radius as $r_i = R_{avg}$, the displacements δ_o and δ_i for a unit pressure ($p=1$) are
 414 obtained through Eqs. (4) and (5). The radius variation due to a thermal expansion is shown in Eq.
 415 (6), where a negative sign is added since it acts in the direction opposite to δ_i . In Eqs. (4) and (5),
 416 E_o and ν_o are the modulus of elasticity and Poisson's ratio of the outer part, while the modulus of
 417 elasticity and Poisson's ratio of the inner part are denoted as E_i and ν_i .

$$\delta_o = \frac{R_{avg}}{E_o} \left(\frac{r_o^2 + R_{avg}^2}{r_o^2 - R_{avg}^2} + \nu_o \right) \quad (4)$$

$$\delta_i = \frac{R_{avg}}{E_i} (1 - \nu_i) \quad (5)$$

$$\Delta r_t = -\alpha \Delta T R_{avg} \quad (6)$$

418 Since the two parts constitute the same solid specimen, the compatibility shown in Eq. (7) must
 419 be fulfilled between the radius variation due to the pressure, and that due to the thermal expansion.

$$(\delta_o + \delta_i) p + \Delta r_t = 0 \quad (7)$$

420 The tensile stress at point R_{avg} can then be evaluated and imposed on the tensile strength of
 421 concrete (f_{ct}). Doing this means that the gradient of temperature which produces the first crack
 422 (ΔT_I) can be obtained. If the same material properties are assumed for the whole specimen ($\nu_o =$
 423 $\nu_i = \nu$ and $E_o = E_i = E$), which would be the case for lower temperatures (approximately below
 424 200 °C), the value of the thermal gradient is obtained as in Eq. (8).

$$\Delta T_I = \frac{f_{ct}}{\alpha E} \left(1 + \frac{r_o^2 - R_{avg}^2}{r_o^2 + R_{avg}^2} \right) = \frac{3.6}{1 \cdot 10^{-5} \cdot 27609} \left(1 + \frac{345^2 - 225^2}{345^2 + 225^2} \right) = 18.3 \text{ °C} \quad (8)$$

425 As we have seen, the first crack occurs relatively early for a low thermal gradient. As cracking
 426 occurs, the membrane stiffness of the outer part decreases, and so does the internal pressure
 427 between the two parts (Eq. (7)). A new and reduced value for the pressure can be determined with
 428 the cracked stiffness. Since the stress generated with this new configuration is below the tensile

429 strength of concrete, additional temperature gradient (ΔT) can be applied until the second crack
430 occurs at another point at the same distance R_{avg} from the centre. By repeating this process and
431 reaching the maximum temperature applied in the fire tests (1200 °C), a multiple radial cracks
432 formation configuration can be determined.

433 The mechanism described is not constant across the thickness since the nonlinear temperature
434 distribution leads to different thermal gradients. However, this is a dominant action across the
435 cross-section, and some of the radial cracks are also visible from the non-exposed side, see Fig. 7.

436 This simplified model could be further developed to predict beforehand the dimension of the
437 radial crack formation radius and the total number of cracks. Additional considerations would need
438 to be taken into account, such as the decrease in the modulus of elasticity and tensile strength of
439 concrete at high temperatures in hot conditions, or variation in the Poisson's ratio. However, this
440 is beyond the scope of this discussion, which was intended to explain the origin of the cracks
441 related to high temperatures and the behaviour of the specimen when subjected to a fire test with
442 this test set-up.

443 **5.2. Structural behaviour of RC slabs**

444 In this section, the influence of the fire on the load-bearing capacity and structural behaviour of
445 the RC slabs is discussed. Based on the load-deflection curves obtained, four main topics are here
446 investigated. First, the effect of high temperatures on the yield point of the steel reinforcement and
447 the bending capacity of the slabs is examined. The contribution of the arching mechanism and
448 TMA to the response of the slab, and the effect that fire exposure has on them is then discussed.

449 *5.2.1. Yielding of reinforcement*

450 A close-up of the complete set of experimental load-deflection curves obtained for all the
451 specimens is presented in Fig. 9a. The curves present a clear change of slope, which corresponds
452 to the instant when the reinforcement starts to yield. Exposure to fire leads to a decrease in the
453 yielding load, which was between 170–190 kN for the non-exposed slabs, but decreased to about
454 140 and 125 kN in the other slabs after exposure to a fire for a duration of 60 and 120 min,
455 respectively.

456 Initially, one might attribute such a decrease in yielding load to possible thermal damage to the
457 bottom steel grid caused by exposure to elevated temperatures. However, the experiments were
458 undertaken in residual conditions, with a cooling phase prior to the static test. The centroid of the
459 reinforcement on the non-exposed side was located at the same level as thermocouple T1. Fig. 6
460 shows that the maximum temperature reached at that point was about 500 °C. Results from tests
461 on the mechanical properties of this type of steel in residual conditions showed a great recovery
462 during the cooling phase²³, in which the yielding strength after exposure to 600 °C and cooling
463 was comparable to that at 20 °C. It is therefore reasonable to assume that the yielding strength in
464 the tensile reinforcement grid was similar in all three cases investigated.

465 The decrease in the yielding load can be explained by considering the whole cross-section of
466 the RC slab. The reduction in both stiffness and strength of concrete and the almost negligible
467 damage experienced by steel reinforcement need a lower neutral axis to guarantee the translational
468 equilibrium of the cross-section. This means that the internal lever arm, and therefore the bending
469 moment, decrease with fire exposure despite the fact that the tensile strength of steel reinforcement
470 is almost constant.

471 5.2.2. *Bending capacity*

472 The bending capacity of the slab was calculated for the three cases using the sectional moment
473 resistance. For the specimens subjected to fire exposure, reduced material properties were used.
474 The evolution of material properties with temperature was taken from Arano et al.²³ where a
475 detailed mechanical characterization of the same concrete material at high-temperature is reported.
476 The measured temperature distribution was assumed equal throughout the yield pattern. This is
477 obviously a simplification, since lower temperatures can be expected in regions far from the fire
478 application. Another assumption is that the steel properties recovered their full performance after
479 the cooling phase, which has been proved to be valid for temperatures up to 600 °C. As shown in
480 Fig. 6, temperatures up to 800 °C were measured at T4, which was also the centroid of the
481 reinforcement on the exposed side. The properties of steel here could therefore be slightly lower
482 than those assumed, in some parts of the slab. A more refined approach could be developed to get
483 a complete overview of the temperature field across the slab. Numerical simulations of the fire
484 tests could provide the temperature distribution across the thickness at every point of the specimen.

485 Despite the simplifications, good agreement was obtained in this study between the predicted
486 values of bending capacity using the yield-line method and the experimental results from the static
487 tests. The success of the analytical approach is mostly due to the behaviour of the material at
488 elevated temperatures being well understood. An extensive characterization, such as provided in
489 Arano et al.²³ is needed both for simplified hand calculations and for advanced numerical
490 simulations. In the literature, experimental studies investigating a specific type of material rarely
491 cover a wide range of temperatures, which is why experimental tests, such as those presented in
492 this study, are vitally needed to validate assumptions and simplified approaches in terms of
493 material performance and overall structural behaviour.

494 *5.2.3. Arching mechanism*

495 The yield-line method is a widely studied approach, but in practice some RC slabs have a higher
496 resistance than initially predicted. This may be due to the arching effect, where the formation of
497 concrete struts between the load application and the supports results in an increase in the bending
498 capacity of the structural member. In the present study, the appearance of the arching mechanism
499 was due to the geometry of the specific test set-up used, and not caused by compressive membrane
500 action.

501 The arching effect was observed in all the tested specimens. The average arch peak load reached
502 by the RC slab was 327 kN for the non-exposed slabs, while it was 210 and 179 kN for the heat-
503 damaged specimens. In comparison with the predicted bending capacity (217, 154 and 138 kN),
504 the arching effect resulted in a load enhancement of 51% for the non-exposed specimens, but only
505 36% and 30% for the specimens exposed to 60 and 120 min, respectively.

506 The arching mechanism is typically obtained in RC beams with a low slenderness ratio (λ)
507 between the load application position and the support, and it also depends on the amount of
508 reinforcement⁵⁷. It can be expected to occur in an RC slab with this geometry, with a strut-and-tie
509 system between the load application and the supports, as shown in Fig. 16a. Equilibrium in the top
510 node of the strut-and-tie system is achieved between the load applied and the compressive forces
511 from the two concrete struts. The diagonal strut transfers the compressive force towards the
512 support, which provides its vertical component. The tensile grid reinforcement acts as a tie
513 equilibrating the horizontal forces in the bottom node. The mechanism fails when either the
514 concrete strut on the top or the steel grid reaches the maximum capacity. Applying this mechanism
515 to the whole RC slab, the struts from the load application to the support are formed in all directions
516 along the circumference, resulting in a truncated cone shape, see Fig. 16b. The cone shape can be
517 partially observed in Fig. 10(e and f).

518 As illustrated in Fig. 9a, the load-deflection curve shows an almost linear first stage, until the
519 yielding of the reinforcement, which is followed by a clearly nonlinear stage. This can be explained
520 by taking into consideration the redundancy of the structure and, with it, the stress-redistribution.
521 In this case, the circular geometry plays an important role. It is intuitive that the first point to yield
522 is the central point of the reinforcement grid. Then, due to the circular geometry, all points located
523 at the same distance from the central point will yield. Since the area of the yielding surface
524 increases, a higher load can be applied. In this way, the yielding surface in the steel plate
525 progressively increases together with the load that can be applied to the slab. The increased yield
526 surface is transformed into a reduction in the stiffness of the plate, which leads to larger deflections.
527 This explains the nonlinear change in stiffness once the yielding of the reinforcement grid starts.

528 The reinforcement used was an orthotropic grid, which could cause the stiffness reduction to
529 behave slightly differently for each load increase. Theoretically, the reinforcement might even
530 resist further load increase, until the total surface yielded. However, the experimental results
531 indicate that what actually happened was that a failure of the concrete strut occurred when it
532 reached a stress equal to the compressive strength of concrete.

533 Future research should include the frictional forces in the contact surface between the concrete
534 and the steel support ring since they may contribute to the arching effect. A numerical model could
535 be developed by means of finite element software, including temperature-dependent material
536 properties for the concrete and the steel. The fire exposure and static tests could be simulated and
537 the results could be compared with the experimental findings. However, this falls outside the scope
538 of the present study.

539 *5.2.4. Tensile membrane action – Ultimate load*

540 Conventional structural design is focused on the evaluation of a global failure, such as bending
541 failure or tensile membrane action. The former type of failure generally occurs at an early stage
542 with small deflections, so TMA seems of little interest. In extreme loads like fire, however, the
543 strength reserve of concrete structures plays an important role, allowing larger deflections. This is
544 where tensile membrane or catenary action is of major interest, giving rise to a relevant research
545 topic with respect to robustness analyses⁵⁸.

546 Fig. 8 shows the complete load-deflection response from the static tests. After the arch peak
547 load is reached, the load rapidly decreases, which in this relatively thick slab can be attributed to
548 the crushing of concrete⁵¹. As the deformations increase, the load-displacement curve enters a
549 tensile membrane region where the load is almost entirely carried by tension in the reinforcement
550 bars until the ultimate strain is reached⁵⁹. In this vertically supported slab with no lateral restraint,
551 the load at large deflections is carried by the TMA taking place at the centre of the specimen, while
552 a compressive supporting “ring” is formed around the perimeter of the slab by means of the
553 compressive membrane action⁶⁰, as schematically shown in Fig. 17a. Load-deflection responses
554 presented in Fig. 8 have a similar trend to the typical relationship for restrained slabs presented in
555 Guice and Rhomberg⁶¹ (Fig. 17b), where the distinct phases of behaviour are highlighted and the
556 flexural and arching contributions are identified.

557 The influence of elevated temperatures on the TMA mechanism after cooling does not follow
558 the trend of the arching mechanism previously described. In contrast to the anticipated arch failure,
559 both in load and deformation, the tensile membrane stage and ultimate load was only slightly
560 affected by the fire exposure. As shown in Fig. 8, similar values of ultimate load were reached in
561 the various fire cases (286, 294 and 272 kN, respectively). This is a result of the almost negligible
562 damage in the steel rebars after the fire exposure, combined with the fact that TMA mainly depends

563 on the steel rebars behaviour. This small influence is very relevant in terms of global resistance.
564 While the fire exposure caused a decrease in the arch peak load (36% and 45% for the 60- and
565 120-min exposures, respectively), the ultimate load was 103% and 95% of the load obtained for
566 the reference case (S0-2). This is a crucial aspect when considering safety and structural reliability.

567 In this study, the compressive “ring” was outside the fire region, so it was not strongly affected
568 by the elevated temperatures. In an alternative scenario, the fire could act on the whole surface of
569 the specimen, also damaging the concrete material in the perimeter. To study the possible effect
570 on the TMA, we must evaluate the stress in the compressive “ring” for the tested slabs. Maximum
571 stress is achieved when the ultimate load is reached. Assuming the compressive “ring” extends
572 from the support to the edge, across the whole thickness, and using the steel yielding strength
573 described in Section 2.2, a maximum stress of about 11 MPa is obtained in the concrete. As
574 reported in Arano et al.²³, this type of concrete withstands such stress for temperatures up to 800
575 °C. So, considering the average temperature from the temperature distribution shown in Fig. 6b, a
576 similar ultimate load would probably be achieved in this RC slab due to TMA, even with a
577 damaged compressive “ring”.

578 **6. CONCLUSIONS**

579 This study investigated the influence of high temperatures on the load-bearing capacity of RC
580 circular slabs in residual conditions. Fire tests were performed, applying a hydrocarbon fire with
581 two different exposure times (60 and 120 mins) to one side of the specimens. Static tests were then
582 performed on all the specimens, including the non-exposed reference slabs. The temperature
583 distribution across the thickness and the load-deflection response were measured during the tests.
584 Direct UPV measurements were made before and after the fire tests to quantify the cross-section
585 stiffness reduction caused by the high temperatures. In addition, simplified mechanical models

586 were used to discuss the effect of fire exposure on the structural response of the slab. Based on this
587 research, the following conclusions were drawn:

- 588 • The maximum measured temperatures across the thickness ranged between 360 and 680
589 °C after the 60-min fire exposure, and between 480 and 870 °C after the 120-min fire
590 exposure. A temperature difference between the two surfaces of the slab of some 720 and
591 790 °C was reached after 60- and 120-min fire tests, respectively. Nonlinear temperature
592 distributions, characterized by large thermal gradients across the thickness, caused a similar
593 tensile crack pattern on the non-exposed surface of all the fire-exposed specimens.
- 594 • After the fire tests, the specimens presented radial cracks on the exposed surface, which
595 were caused by the temperature difference between the furnace area and the region of the
596 specimen closer to the edge. Simplified calculations confirmed that a small thermal
597 difference of about 15–20 °C between the two regions was enough to explain the initiation
598 and propagation of these radial cracks.
- 599 • An arching mechanism was obtained for all the specimens tested, resulting in a first peak
600 in the load-deflection response. The arch peak load corresponded to a bending capacity
601 enhancement of 51%, 36% and 30% respectively for the three exposure cases. The arching
602 mechanism was negatively affected in the presence of fire. The average arch peak load in
603 the non-exposed slabs was 327 kN. After 60- and 120-min fire exposure, the peak load was
604 reduced to 210 and 179 kN, respectively, which represents a decrease of 36% and 45%.
605 The average results of deflection at the arch peak load were 14.4 mm for the non-heated
606 case, and 7.9 and 7.7 mm after the 60- and 120-min fire exposure, representing reductions
607 of 45% and 47%, respectively.

- 608 • Tensile membrane action (TMA) enhanced the ultimate load of the slab. This mechanism
609 was not greatly affected by the fire exposure, resulting in a similar average ultimate load
610 for all three fire cases investigated (280, 294 and 272 kN, respectively), and confirming
611 the robustness and structural reliability of this RC slab in residual conditions.
- 612 • Simplified calculations using the yield-line method showed good agreement with the
613 experimental results after the loss of the arching mechanism. The use of temperature-
614 dependent stress-strain curves of concrete for the sectional analysis proved to be a good
615 approach for calculating the reduced bending capacity of the slab after exposure to fire.
- 616 • The experimental data presented in this paper are valuable in defining a reliable benchmark
617 for the numerical models which, with numerical upscaling, will be instrumental for the
618 design of the E39 submerged floating tunnel (SFT) under exceptional load conditions.

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LIST OF TABLES

Table 1. Summary of the experimental campaign (UPV: ultrasonic pulse velocity)

Specimen ID	UPV test	Fire exposure (min)			Thermocouples (number)	Static test
		0	60	120		
S0-1	–	Y	–	–	–	Y
S0-2	–	Y	–	–	–	Y
S60-1	Y	–	Y	–	Y(4)	Y
S60-2	Y	–	Y	–	–	Y
S120-1	Y	–	–	Y	Y(4)	Y
S120-2	Y	–	–	Y	–	Y

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Table 2. Concrete mix design

Material	Content (kg/m ³)
CEM II/B-M 42.5R	223.40
CEM II/A-V 42.5N	193.33
Silica fume	12.89
Water	174.13
Aggregate 0-8	1026.48
Aggregate 8-16	754.95
Acrylic superplasticizer	3.06
Set retarding admixture	0.64
Polypropylene microfibres	1.00

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Table 3. Evolution of mechanical properties of concrete and steel after exposure at high temperatures.

T (°C)	$f_{c,T}$ (MPa)	$f_{ct,T}$ (MPa)	$E_{c,T}$ (MPa)	$f_{y,T}$ (MPa)	$f_{t,T}$ (MPa)	$\varepsilon_{su,T}$ (-)
20	73.0	3.6	27609.4	500.9	648.8	0.32
200	64.7	4.5	25777.1	585.2	699.9	0.25
400	37.3	2.4	15139.7	565.2	660.7	0.31
600	21.3	1.2	7577.9	508.4	611.7	0.37

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764 **Table 4.** Coefficients of the exponential fit of the temperature distribution across the thickness of the slab.

t_i (min)	Fire test: 60 min		Fire test: 120 min	
	a_i	b_i	a_i	b_i
30	35.95	-165.41	34.71	-163.59
60	48.12	-259.37	48.22	-266.20
90	–	–	58.34	-339.80
120	–	–	61.31	-363.01

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766 **Table 5.** Average pulse velocity measurements (standard deviation in parentheses).

Specimen ID	Velocity before fire test, v_0 (km/s)	Velocity after fire test, v_t (km/s)	Relative value v_t/v_0 (%)
S60-1	4.64 (0.04)	2.54 (0.33)	54.74
S60-2	4.73 (0.11)	2.68 (0.15)	56.66
S120-1	4.72 (0.33)	2.23 (0.38)	47.25
S120-2	4.71 (0.12)	2.20 (0.10)	46.71

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FIGURE CAPTIONS

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770 **Fig. 1.** a) Geometry of the RC slab; b) preparation of specimen, and c) specimen after casting (units: mm).
771 **Fig. 2.** a) Location UPV measurements, and b) direct UPV acquisition (units: mm).
772 **Fig. 3.** a) Fire test set-up, with close-up of thermocouple positions, and b) burner equipment (units: mm).
773 **Fig. 4.** a) Static test set-up, and b) picture during static test (units: mm).
774 **Fig. 5.** Temperature measurements from thermocouples T1–T4 in fire tests: a) S60-1, and b) S120-1.
775 **Fig. 6.** Temperature distribution evolution across the thickness for a) 60-min, and b) 120-min fire test.
776 **Fig. 7.** Crack pattern after fire tests: a) S60-1, b) S60-2, c) S120-1 and d) S120-2.
777 **Fig. 8.** Complete load-deflection curve results for each static test.
778 **Fig. 9.** a) Close-up of load-deflection curves, b) comparison of average failure load and deflection at failure
779 load for each exposure time.
780 **Fig. 10.** Failed specimens a) S0-1, b) S0-2, c) S60-1, d) S60-2, e) S120-1, and f) S120-2, after static tests.
781 **Fig. 11.** Yield line pattern for circular RC slab concentrically loaded.
782 **Fig. 12.** a) Comparison between experimental curves²³ and the model adapted from Eurocode 2⁵⁴; and b)
783 generalized constitutive behaviour for all temperatures.
784 **Fig. 13.** Sectional analysis for 60-min fire exposure: a) temperature, b) strain, and c) stress profiles, and d)
785 close-up of the compressive zone.
786 **Fig. 14.** Comparison between analytical values and experimental results.
787 **Fig. 15.** a) Average crack initiation radius R_{avg} , and b) simplified model for evaluating the radial cracks.
788 **Fig. 16.** Sketch of the a) sectional and b) global arching mechanism.
789 **Fig. 17.** (a) Sketch of the tensile membrane action (TMA) mechanism and (b) typical load-deflection
790 relationship for a restrained slab (adapted from Guice and Rhomberg⁶¹)