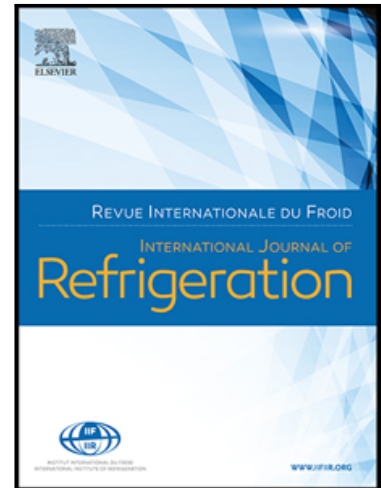


Journal Pre-proof

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Highlights:

- The model obtained CO₂ outlet temperature with an absolute mean error of 1.14 K.
- The heat transfer rate of fluted tube-in-tube gas cooler was generally higher.
- The improvement of maximum COP could be up to 29.41% by using the fluted tube.
- The COP improvement could be impaired to 6.30% at water inlet temperature of 40°C.

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**Investigation on the performance of fluted tube-in-tube gas cooler in
transcritical CO₂ heat pump water heater**

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Abstract

The utilization of fluted inner tube in tube-in-tube heat exchangers is an effective way to improve the heat transfer performance. Based on the segmented model, the performance of a fluted tube-in-tube gas cooler (FTGC) in the transcritical CO₂ heat pump water heater was studied in this paper. The simulation model was validated and adopted to numerically investigate the effects of different parameters on the heat transfer performance of the gas cooler, which was compared to the smooth tube-in-tube gas cooler (STGC) with the same geometric parameters. The results showed that the FTGC had higher heat transfer capacity in most conditions. The heat transfer rate first increased and then decreased as the CO₂ inlet pressure increased. The temperature difference at the pinch point in the FTGC was lower than that in the STGC. In the FTGC, the pinch point position was mainly influenced by the CO₂ inlet pressure and water inlet and outlet temperatures. Regarding the system COP, the improvement of maximum COP could be up to 29.41% by using the FTGC compared to STGC when the water inlet temperature was 10°C and the water outlet temperature was 80°C. However, when the water inlet temperature was 40°C, the improvement of COP could be impaired to 12.98%. Through changing the designs of the FTGC with the fixed total heat transfer area, when the water inlet and outlet temperatures were 10°C and 60°C, the highest maximum COP could be obtained with the design used in the experiments.

Keywords

transcritical CO₂ heat pump water heater; fluted tube-in-tube gas cooler; simulation model; coefficient of performance

Nomenclature*Symbols*

A	Area [m ²]
c_p	Isobaric specific heat [kJ·(kg·K) ⁻¹]
D	Diameter [m]
e	Flute depth [m]
e^*	Nondimensional flute depth [-]
f	Frictional factor [-]
h	Enthalpy [kJ·kg ⁻¹]
k	Thermal conductivity [W·(m·K) ⁻¹]
L	Length of tube [m]
m	Mass flow rate [kg·s ⁻¹]
N	Number [-]

Nu	Nusselt number [-]
p	Flute pitch [m]
p^*	Nondimensional flute pitch [-]
P	Pressure [MPa]
Pr	Prandtl number [-]
Q	Heat transfer rate [kW]
R	Thermal resistance [$\text{m}^2 \cdot \text{K} \cdot \text{W}^{-1}$]
Re	Reynolds number [-]
T	Temperature [$^{\circ}\text{C}$]
u	Flow velocity [$\text{m} \cdot \text{s}^{-1}$]
U	Overall heat transfer coefficient [$\text{W} \cdot (\text{m}^2 \cdot \text{K})^{-1}$]
V	Displacement [$\text{m}^3 \cdot \text{h}^{-1}$]
Vol	Volume [m^3]
x	Position [m]
α	Heat transfer coefficient [$\text{W} \cdot (\text{m}^2 \cdot \text{K})^{-1}$]
δ	Wall thickness [m]
ΔP	Pressure drop [MPa]
ΔT	Temperature difference [K]

η	Efficiency [-]
θ	Helix angle [rad]
θ^*	Nondimensional helix angle [-]
μ	Dynamic viscosity [Pa·s]
ρ	Density [$\text{kg}\cdot\text{m}^{-3}$]

Abbreviations

AOP	Above optimal pressure
BOP	Below optimal pressure
COP	Coefficient of performance
EEV	Electronic expansion valve
FTGC	Fluted tube-in-tube gas cooler
OP	Optimal pressure
STGC	Smooth tube-in-tube gas cooler
ZF	Zoom factor

Subscripts

ave	Average
b	Bulk
c	CO ₂

CE	Cold end
com	Compressor
d	Discharge
f	Film
flute	Flute
i	Inside
in	Inlet
max	Maximum
o	Outside
opt	Optimal
out	Outlet
p	Pinch point
pc	Pseudo-critical
s	Suction
v	Volumetric
vi	Volume based inner diameter
vo	Volume based outer diameter
w	Water

wall Wall

1. Introduction

More and more attention has been paid to the issues of energy and environment as the improvement of people's living standard (Liu et al., 2019). For space and hot water heating, air source heat pump is an energy-efficient and reliable solution, but most of them are charged with HFC refrigerants, like R410A or R134a (Dai et al., 2020a). The use of HFCs is restricted according to the Kyoto Protocol due to their great adverse effect on the greenhouse effect (Breidenich et al., 1998). For China, the production and consumption of HFCs will be frozen in 2024 and phased down by 80% in 2045. Therefore, it is necessary to look for the replacement of HFCs in the field of air source heat pump (Dai et al., 2019). As a natural refrigerant, CO₂ has attracted attention from researchers and industries in the fields of refrigeration, air conditioning and heat pump due to its non-toxicity, incombustibility, safety, low cost and environmentally benign (Ehsan et al., 2018). Due to the low critical temperature, the transcritical CO₂ cycle is generally applied (Lorentzen and Pettersen, 1993) and recent studies have demonstrated the enormous energy-saving potential by implementing transcritical CO₂ system (Dai et al., 2020b). Especially for the water heating application with a large temperature lift, the transcritical CO₂ cycle presents a unique superiority compared to the traditional HFC refrigerants (Austin and Sumathy, 2011). The temperature glide in the supercritical exothermic process can diminish the entropy generation and enhance the system performance (Zhang et al., 2018).

In CO₂ systems, the gas cooler is an important component that greatly impacts the system efficiency (Yang et al., 2016), and many relevant studies have been carried out. Fronk and Garimella (2011a, b) conducted an experimental and analytical study on microchannel water-CO₂ gas coolers with a general counter-flow configuration. Tsamos et al. (2017) experimentally studied the performance of finned-tube CO₂ gas coolers/condensers with different designs in a CO₂ booster system. Wang et al. (2019a) investigated a compact microchannel gas cooler applied in an automobile CO₂ heat pump system. Then, they also studied the series gas cooler configuration and found that the application of series gas cooler configuration can result in an average 33.7% increase of heating capacity and an average 35% increase of COP (Wang et al., 2019b). Lata and Gupta (2020) adopted a modified evaporative cooling system in gas cooler/condenser of supermarket CO₂ booster refrigeration systems with various configurations. Zendeboudi et al. (2021) researched the heat transfer and pressure drop of brazed plate heat exchangers that belong to a tri-partite CO₂ gas cooler which can simultaneously fulfill the demands of domestic hot water and space heating.

Moreover, the tube-in-tube heat exchanger is a widely used solution for water-CO₂ gas coolers. Yu et al. (2012) modeled a tube-in-tube CO₂ gas cooler and pointed out that the heat transfer of CO₂ near the pseudo-critical region showed a very small temperature variation. Chen (2016) carried out the pinch point analysis for smooth tube-in-tube gas cooler and found the critical flow ratios of water to CO₂ that influence the temperature difference at the pinch point. Zhang et al. (2018) proposed a

thermodynamic optimization method based on temperature glide matching and applied it to a CO₂ heat pump water heater using tube-in-tube gas cooler. Yang and Ning (2019) studied the effects of operating parameters on heat transfer performance of evaporator in a transcritical CO₂ heat pump with tube-in-tube gas cooler and evaporator. Peng et al. (2020) developed simulation models of the transcritical CO₂ vapor-injection heat pump system, which utilized tube-in-tube gas cooler and evaporator, and investigated the effect of operating parameters on heating performance.

To improve the performance of the tube-in-tube heat exchanger, some researchers have tried different types of inner tubes, such as multi-twisted tubes (Yang et al., 2016) and corrugated tubes (Ndiaye, 2017). The fluted tube is a type that is extensively used in the design of tubular heat exchangers (Srinivasan and Christensen, 1992). Wang et al. (2000) introduced the carbon steel fluted tube for replacing the copper smooth tube and found that the total heat transfer coefficient of the carbon steel fluted tube was close to that of the copper smooth tube. Zhu et al. (2010), Park (2010) and Wang et al. (2017) numerically investigated the film condensation on fluted tubes. Qi et al. (2017) experimentally studied the characteristics of TiO₂-water nanofluids flowing in a fluted tube and a smooth tube. They found that compared to the laminar flow in the fluted tube, the turbulent flow had a larger increase in heat transfer and a smaller increase in frictional factors. Yu et al. (2020) numerically researched the supercritical CO₂ cooling in the fluted tube and obtained an optimal

geometric structure under a certain condition.

In terms of the fluted tube applied in heat exchangers, Rousseau et al. (2003) described a model to simulate fluted tube condenser by using smooth tube correlations combined with the modification based on helical coils and empirical data for fluted tube condensers. For CO₂ gas coolers, the models were mainly built by the segmented method (Li et al., 2017; Qin et al., 2020) and the moving boundary method (Bahman et al., 2020) due to the supercritical CO₂ properties. Xu et al. (2011) developed a segmented CO₂ gas cooler model that consisted of a fluted tube and helically coiled tubes embedded in the groove of the fluted tube. They found that with a decrease of the inner fluted tube diameter, the heating capacity increased and the CO₂ pressure drop changes slightly. Huang et al. (2014) presented a generalized finite volume model for the tube-in-tube heat exchanger. To calculate the two-phase flow in the fluted tube annuli, they applied empirical two-phase flow multipliers onto existing fluted tube single-phase correlations. Chen et al. (2016) proposed helically-coiled fluted tube heat exchangers for use in fluoride-salt-cooled high temperature reactor systems. Zhu et al. (2019) investigated the heat transfer characteristics of supercritical CO₂ cooling in the fluted tube-in-tube heat exchanger and developed a new correlation for it. However, they did not study the influence of the fluted tube-in-tube heat exchanger on the system performance of CO₂ heat pump.

As mentioned above, the fluted tube is a promising solution from the heat

transfer improvement point of view, and it has already been applied in some tube-in-tube heat exchangers. However, for the supercritical CO₂ gas cooler, the publication about the application of the fluted tube is still very limited. Moreover, the effect of the higher pressure drop caused by the special geometric structure of the fluted tube on the performance of heat exchanger has not been reported yet. To fill the research gap, a simulation model considering the pressure drop of supercritical CO₂ was developed to investigate the fluted tube-in-tube gas cooler (FTGC). After the model validation, compared to the smooth tube-in-tube gas cooler (STGC) with the same geometric parameters, the effects of different parameters on the heat transfer performance were analyzed. Furthermore, the investigation on the system performance of CO₂ heat pump using the FTGC has not been published as well. Thus, this paper evaluated the COP of systems with FTGC and STGC, and the different designs of the FTGC were calculated to optimize the heat exchanger.

2. Experimental setup

2.1 Tested system

The studied FTGC was installed in a transcritical CO₂ heat pump water heater, which is shown in Fig. 1. The characteristics of the components are displayed in Table 1. The information on the FTGC will be introduced in Section 2.2. Through adjusting the opening of the EEV, the discharge pressure and temperature would accordingly change, which generated different CO₂ inlet conditions of the FTGC. The regulating

valve could manipulate the water flow rate to reach the targeted water outlet temperature. The water inlet temperature was controlled by devices of the laboratory.

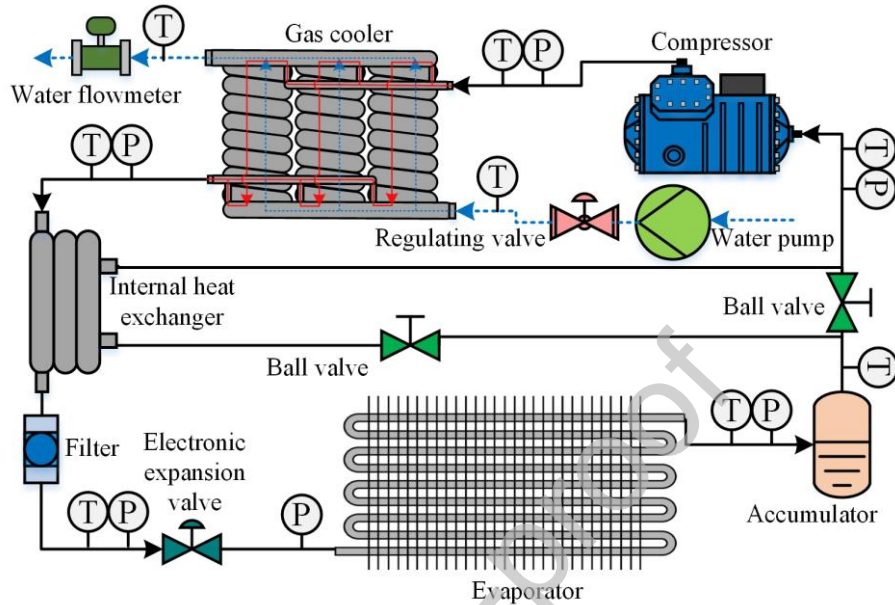


Fig. 1. Schematic of transcritical CO₂ heat pump.

Table 1 Characteristics of the components.

Component	Characteristic
Compressor	Type: Semi-hermetic reciprocating Rated rotational speed: 1450 rpm
Evaporator	Rated displacement: 11.69 m ³ ·h ⁻¹ Type: Finned-tube Tube: Φ7 mm×0.7 mm copper tube Tube length: 1600 mm Fin type: Aluminum, Wavy Fin spacing: 2.4 mm

	Fin thickness: 0.2 mm
	Number of heat exchanger: 2 (V-shaped arrangement)
	Number of rows per heat exchanger: 4
	Number of copper tubes per row: 48
Internal heat exchanger	Number of refrigerant circuits per heat exchanger: 12
	Type: Fluted tube-in-tube
	Flow type: Counter flow
	Outside tube: $\Phi 33 \text{ mm} \times 1.5 \text{ mm}$ stainless steel tube
	Inside tube: Fluted copper tube
	Total heat transfer area: 0.27 m^2
Electronic expansion valve	Type: Stepper motor
Accumulator	Inside volume: 9.5 L

2.2 Fluted tube-in-tube gas cooler

The FTGC was made of three same heat exchangers in parallel. In each heat exchanger, as Fig. 1 shows, the water generally flowed from the bottom to the top along the tube, while the CO_2 flowed from the top to the bottom. The fluted tube-in-tube structure and the key geometric parameters are displayed in Fig. 2. The outer tube was a stainless-steel circular tube with the inner diameter denoted as D_o , and the inner tube was a fluted copper tube. The water and CO_2 flowed in the tube side and the annulus side, respectively.

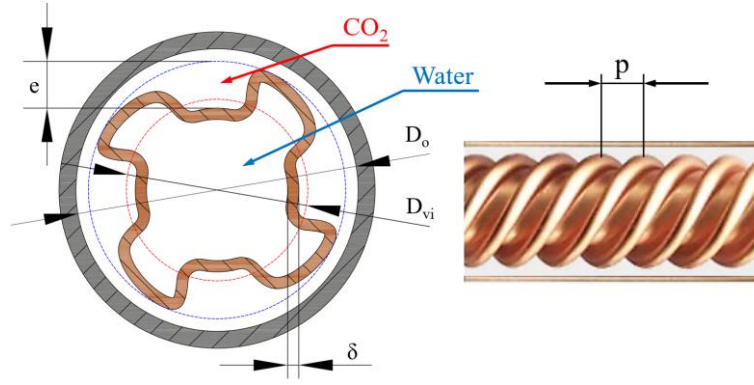


Fig. 2. Details of the fluted tube-in-tube structure.

Due to the complex shape of the fluted tube, the volume based inner diameter D_{vi} was adopted and can be expressed as (Rousseau et al., 2003):

$$D_{vi} = \sqrt{\frac{4 \cdot Vol}{\pi L}} \quad (1)$$

where Vol is the volume enclosed inside the fluted tube. The volume based outer diameter D_{vo} can be calculated as:

$$D_{vo} = D_{vi} + 2\delta \quad (2)$$

In terms of the fluted structure, the flute depth e and the flute pitch p are important parameters. The nondimensional parameters (e^* and p^*) are respectively determined by e and p dividing with D_{vi} . The helix angle θ can be calculated by:

$$\theta = \arctan\left(\frac{\pi D_{vo}}{N_{flute} p}\right) \quad (3)$$

where N_{flute} is the number of flutes and equals to 4. The nondimensional helix angle θ^*

is calculated by θ dividing with $\pi/2$. The geometric parameters of the fluted tube-in-tube structure are summarized in Table 2.

Table 2 Geometric parameters of the fluted tube-in-tube structure.

Parameter	Description	Value
D_o	Inner diameter of outer tube [mm]	25
D_{vi}	Volume based equivalent inner diameter of inner tube [mm]	16.07
D_{vo}	Equivalent outer diameter of inner tube [mm]	18.07
δ	Wall thickness of inner tube [mm]	1
e	Flute depth [mm]	4.16
p	Flute pitch [mm]	13
θ	Helix angle [rad]	0.829
L	Length of tube [m]	18
e^*	Dimensionless flute depth [-]	0.259
p^*	Dimensionless flute pitch [-]	0.809
θ^*	Dimensionless helix angle [-]	0.528
A_i	Inside heat transfer area of the inner tube [m ²]	1.307
A_o	Outside heat transfer area of the inner tube [m ²]	1.421

2.3 Measurement devices

The environmental laboratory, which could provide different ambient temperature and water inlet temperature, consisted of water adjusting system, air adjusting system, electric control system, data acquisition system and environmental room. The positions of the temperature and pressure sensors are shown in Fig. 1. Type T thermocouples and thermal resistances PT100 were adopted. The measurement range of the temperature sensors was -200–350°C, and the accuracy was $\pm 0.2^\circ\text{C}$. The

CO₂ pressure was measured by pressure transmitters with a measurement range of 0–16 MPa and an accuracy of $\pm 0.25\%$ of full span. The water volumetric flow rate was measured by an electromagnetic flowmeter with a measurement range of 0–6 m³·h⁻¹ and an accuracy of $\pm 0.5\%$ of full span. When the steady state in which the parameters barely changed for 5 minutes was reached, all the measurements were collected to obtain the performance by time-averaged. The ranges of the experimental parameters are summarized in Table 3.

Table 3 Ranges of the experimental parameters.

Parameter	Unit	Range
CO ₂ inlet pressure	MPa	7.89-12.60
CO ₂ inlet temperature	°C	56.75-144.78
CO ₂ mass flow rate	kg·s ⁻¹	0.089-0.405
CO ₂ outlet pressure	MPa	7.43-11.83
CO ₂ outlet temperature	°C	7.45-55.75
Water inlet temperature	°C	6.93-55.65
Water outlet temperature	°C	42.48-90.78
Water volumetric flow rate	m ³ ·h ⁻¹	0.297-2.390

2.4 Data reduction

The heat transfer rate of the gas cooler can be expressed as:

$$Q_{gc} = m_w c_{pw} (T_{w,out} - T_{w,in}) \quad (4)$$

Based on the heat transfer balance, the mass flow rate of CO₂ can be determined

by:

$$m_c = \frac{Q_{gc}}{h_{c,in} - h_{c,out}} \quad (5)$$

The CO₂ pressure drop can be expressed as:

$$\Delta P_c = P_{c,in} - P_{c,out} \quad (6)$$

Based on the method proposed by Moffat (1988), the uncertainty analysis was conducted. The uncertainties of Q_{gc} , m_c and ΔP_c are 3.59%, 4.22% and 7.86%, respectively.

3. Simulation model

3.1 Correlations used in the simulation model

3.1.1 Water side

For the water heating inside the fluted tube, the correlations from Rousseau et al. (2003) were used. The Nusselt number can be calculated by:

$$Nu_w = \begin{cases} 0.014 Re_w^{0.842} Pr_w^{0.4} (e^*)^{-0.067} (p^*)^{-0.293} (\theta^*)^{-0.705}, & Re_w \leq 5000 \\ 0.064 Re_w^{0.773} Pr_w^{0.4} (e^*)^{-0.242} (p^*)^{-0.108} (\theta^*)^{0.599}, & Re_w > 5000 \end{cases} \quad (7)$$

The Reynolds number Re , Prandtl number Pr and heat transfer coefficient α can be expressed as:

$$Re = \frac{\rho u D}{\mu} \quad (8)$$

$$Pr = \frac{c_p \mu}{k} \quad (9)$$

$$\alpha = \frac{Nuk}{D} \quad (10)$$

The frictional factor can be determined by:

$$f_w = \begin{cases} 0.554 \left(\frac{64.0}{Re_w - 45.0} \right) (e^*)^{0.384} (p^*)^{-1.454 + 2.083e^*} (\theta^*)^{-2.426}, & Re_w \leq 1500 \\ 1.209 Re_w^{-0.261} (e^*)^{1.26 - 0.05p^*} (p^*)^{-1.66 + 2.033e^*} (\theta^*)^{-2.699 + 3.67e^*}, & Re_w > 1500 \end{cases} \quad (11)$$

For the water flowing inside the smooth tube, the correlation from Gnielinski (1976) was adopted:

$$Nu_w = \frac{(f_w / 8)(Re_w - 1000) Pr_w}{1 + 12.7(f_w / 8)^{1/2} (Pr_w^{2/3} - 1)} \quad (12)$$

$$f_w = (1.82 \log Re_w - 1.64)^{-2} \quad (13)$$

3.1.2 Supercritical CO₂ side

For the supercritical CO₂ cooling and flowing in the fluted annulus, the Nusselt number can be calculated based on the correlation from Zhu et al. (2019):

$$Nu_b = \begin{cases} 1.85Nu_0 \left(\frac{Pr_b}{Pr_{wall}} \right)^{1.5128} \left(\frac{\rho_b}{\rho_{wall}} \right)^{-0.7115} \left(\frac{c_{p,b}}{\bar{c}_p} \right)^{-2.2726} \left(\frac{D_{vo}}{p} \right)^{0.447}, & T_b \leq T_{pc} \\ 3.7Nu_0 \left(\frac{Pr_b}{Pr_{wall}} \right)^{0.0479} \left(\frac{\rho_b}{\rho_{wall}} \right)^{0.9577} \left(\frac{c_{p,b}}{\bar{c}_p} \right)^{-0.2729} \left(\frac{D_{vo}}{p} \right)^{0.447}, & T_b > T_{pc} \end{cases} \quad (14)$$

where Nu_0 is calculated using the correlations from Gnielinski (1976) as shown in equation (12). The averaged specific heat \bar{c}_p can be determined by:

$$\bar{c}_p = \frac{\int_{T_b}^{T_{wall}} c_p dT}{T_{wall} - T_b} = \frac{h_{wall} - h_b}{T_{wall} - T_b} \quad (15)$$

With the best knowledge of the authors, there is no correlation for the frictional factor of supercritical CO₂ flowing in the fluted annulus. Therefore, a correlation was proposed based on the experimental data:

$$f_c = (0.653 \log Re_b - 2.415)^{-2.537} \quad (16)$$

For the supercritical CO₂ cooling in the smooth annulus, the correlation from Dang and Hihara (2004) was used:

$$Nu_b = \frac{(f_c / 8)(Re_b - 1000) Pr_c}{1.07 + 12.7(f_c / 8)^{1/2} (Pr_c^{2/3} - 1)} \quad (17)$$

$$Pr_c = \begin{cases} c_{p,b} \mu_b / k_b, & \text{for } c_{p,b} \geq \bar{c}_p \\ \bar{c}_p \mu_b / k_b, & \text{for } c_{p,b} < \bar{c}_p \text{ and } \mu_b / k_b \geq \mu_f / k_f \\ \bar{c}_p \mu_f / k_f, & \text{for } c_{p,b} < \bar{c}_p \text{ and } \mu_b / k_b < \mu_f / k_f \end{cases} \quad (18)$$

$$f_c = (1.82 \log Re_f - 1.64)^{-2} \quad (19)$$

$$Re_b = \frac{\rho_b u D}{\mu_b} \quad (20)$$

$$Re_f = \frac{\rho_b u D}{\mu_f} \quad (21)$$

where the subscript f denotes the film temperature, and the film temperature is the average of wall temperature and bulk temperature.

3.2 Calculation method

In the gas cooler, the heat transfer happens with significant changes of temperature and thermodynamic properties. To ensure the calculation accuracy, the gas cooler was divided into a series of segments with the same length for the simulation (Yu et al., 2012). The thermophysical properties of CO₂ and water were calculated based on NIST REFPROP 9.1 (Lemmon et al., 2013). The simulation model was programmed in the MATLAB.

The following assumptions were adopted:

- (1) The flows were considered as homogeneous and one-dimensional steady;
- (2) The heat loss to the ambient air was neglected;
- (3) The thermal conduction in the axis direction of the tube was ignored;
- (4) The pressure drops caused by the gravitation and the ports were neglected.

Fig. 3 shows the flow chart of the model calculation method. After the input of the condition parameters of CO₂ and water and the geometric parameters of the heat exchanger, the states at the hot end, i.e. the CO₂ inlet and water outlet of the first segment, could be determined. After that, the water mass flow rate was assumed. Then, for each segment, the heat transfer coefficients and the frictional factors of water and CO₂ side was obtained based on equation (7) - (21). The overall $(UA)_j$ can be obtained by:

$$(UA)_j = \frac{1}{\frac{1}{\alpha_{c,j} A_{o,j}} + R_{i,j} + \frac{\ln(D_{vo}/D_{vi})}{2\pi k_{wall} L_j} + R_{o,j} + \frac{1}{\alpha_{w,j} A_{i,j}}} \quad (22)$$

where $R_{i,j}$ and $R_{o,j}$ are the thermal resistances caused by inner and outer fouling of the fluted tube. The local heat transfer rate at each segment Q_j can be expressed as:

$$Q_j = (UA)_j \Delta T_j \quad (23)$$

The states at the CO₂ outlet of the j^{th} segment can be determined based on the heat transfer balance:

$$Q_j = m_c (h_{c,in,j} - h_{c,out,j}) = m_w c_{pw} (T_{w,out,j} - T_{w,in,j}) \quad (24)$$

During the in-sequence calculation of the segments, if the water inlet temperature of the j^{th} segment was lower than the input water inlet temperature, the calculation could be immediately stopped and iterated with a larger water mass flow rate. When the states of all segments were obtained, comparing the calculated and input water

inlet temperature of the gas cooler, the water mass flow rate was iterated until the error was acceptable. Finally, the CO₂ outlet parameters, water mass flow rate and temperature profiles could be output.

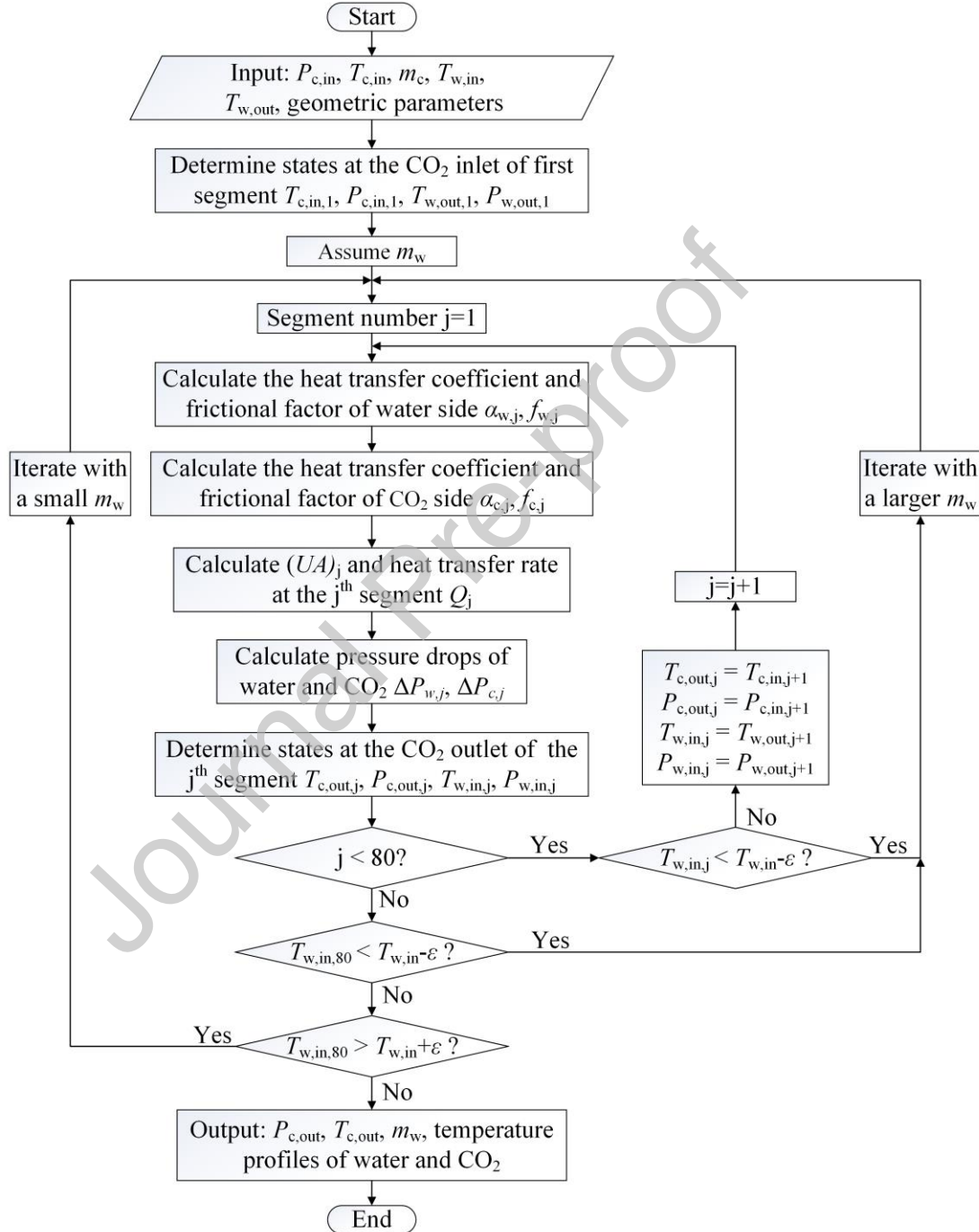


Fig. 3. The flow chart of the model calculation method.

Although the calculation would be more accurate when the number of segments was very large, the calculation time accordingly increased. To determine the number of segments, a sensitivity analysis was conducted. Fig. 4 shows the variations of calculated results with the increase of segment number in the FTGC. When the number was large, the variations of results were slight. The relative deviation of heat transfer rate was 0.142% when the results with the segment number of 80 and 110 were compared. In this paper, the segment number of 80 was used to balance the time and accuracy.

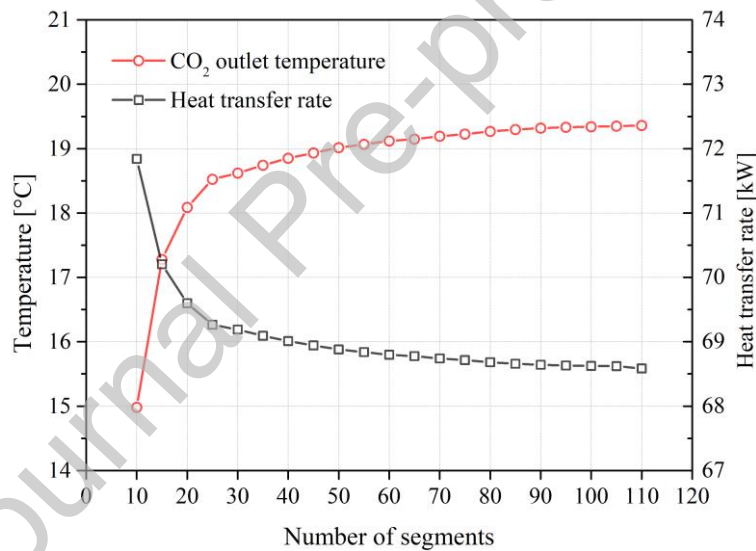


Fig. 4. Variations of calculated CO₂ outlet temperature and heat transfer rate in the FTGC with the increase of segment number.

3.3 Model validation

The comparison between the experimental and calculated heat transfer rates of the FTGC is shown in Fig. 5. The CO₂ inlet pressure, CO₂ inlet temperature, CO₂

mass flow rate, water inlet temperature and water outlet temperature were the input, while the CO₂ outlet pressure, CO₂ outlet temperature and water flow rate were the output. As shown in Fig. 5, the calculated values agreed with the experimental values within an error of 8%. Regarding the output parameters, the absolute mean relative errors of the CO₂ outlet pressure and the water flow rate were 1.99% and 2.95%, respectively; the absolute mean error of the CO₂ outlet temperature was 1.14 K. Hence, the simulation model could obtain the results with acceptable accuracy and could be applied for further investigation. As for the validation of the STGC model, the correlations used in the STGC model were commonly used in the literature (Li et al., 2013; Minetto, 2011; Yang et al., 2016; Yu et al., 2012; Zhu et al., 2019), and the reliability of the model has been verified by them.

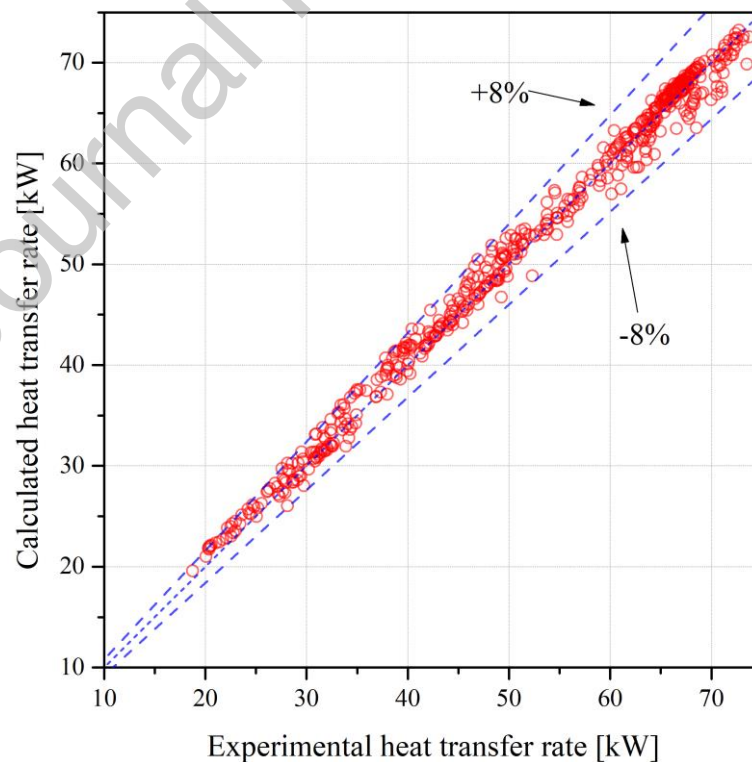


Fig. 5. Comparison between the experimental and calculated heat transfer rates of the FTGC.

4. Results and discussion

4.1 Effects of different parameters on the heat transfer performance

In this section, the performance of the FTGC was analyzed through simulation. Besides, the STGC with the same geometric parameters was also simulated to show the difference.

4.1.1 CO₂ side conditions

Fig. 6 shows the temperature profiles of CO₂ and water along the length of the heat transfer tube under different CO₂ inlet pressures ($P_{c,in}$). The positions of pinch points, where the temperature difference between CO₂ and water reached the minimum, are displayed. The temperature differences at the cold end (ΔT_{CE}) are also shown. Since the water mass flow rate was iterated to match the temperature lift, the ratio of mass flow rate (m_c/m_w) is used to denote the condition of water mass flow rate.

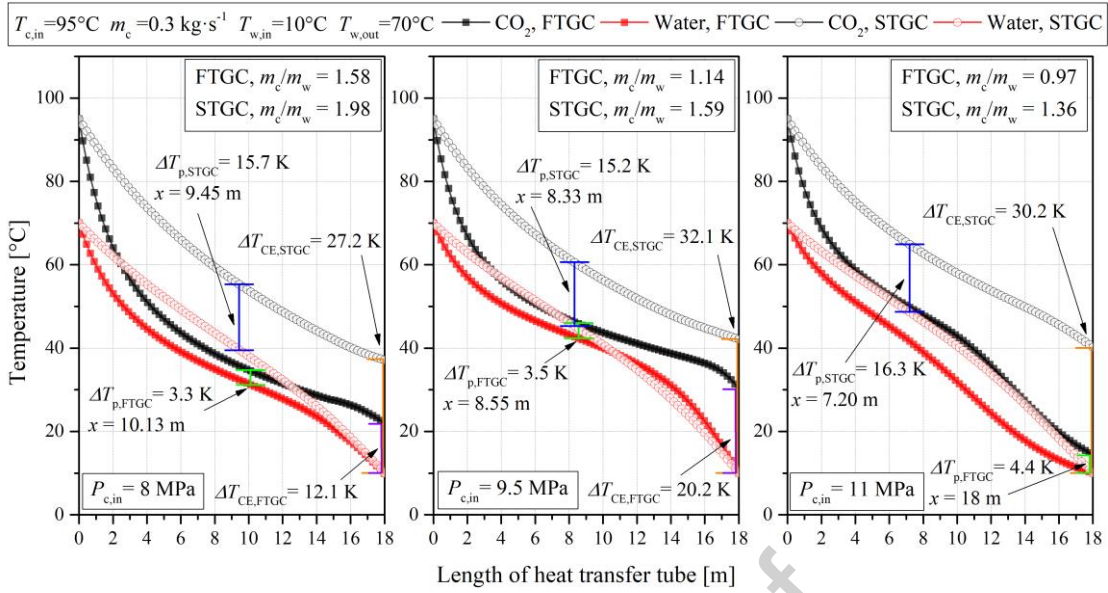


Fig. 6. Temperature profiles of CO₂ and water along the length of the heat transfer tube under different CO₂ inlet pressures.

The CO₂ temperature decreased fast near the CO₂ inlet because of the large temperature difference and lower specific heat. In the FTGC, the heat transfer coefficients in both water and CO₂ sides were improved, and thus the CO₂ temperature was cooled down more and the CO₂ outlet temperature ($T_{c,out}$) was always lower than that in STGC. It could be found that the temperature difference at the pinch point (ΔT_p) in the FTGC was significantly lower than that in the STGC. In the FTGC, the pinch point moved to the cold end when $P_{c,in}$ increased to 11 MPa, which was the desired situation to maximize the enthalpy difference of the gas cooler and achieve the high COP in the CO₂ heat pump (Ye et al., 2020).

Fig. 7 shows the temperature profiles under different CO₂ inlet temperatures ($T_{c,in}$). With the increase of $T_{c,in}$, the decrease of CO₂ temperature near the CO₂ inlet

was more rapid due to the increase of temperature difference and the decrease of specific heat. However, the CO₂ temperature curves on the subsequent heat transfer process were similar under different $T_{c,in}$. It indicated that $T_{c,in}$ mainly influenced the temperature profiles near the hot end. In both FTGC and STGC, ΔT_p increased with the increase of $T_{c,in}$. In addition, the pinch point in the STGC moved toward the hot end as $T_{c,in}$ increased; while the pinch point in the FTGC basically located at the middle of the heat transfer tube.

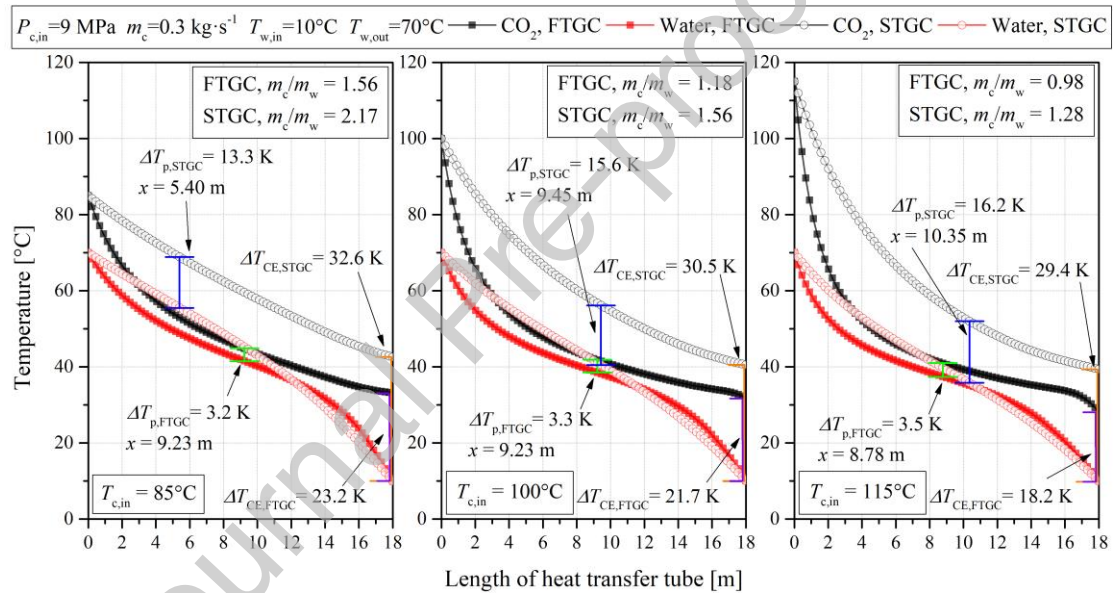


Fig. 7. Temperature profiles of CO₂ and water along the length of the heat transfer tube under different CO₂ inlet temperatures.

Fig. 8 shows the temperature profiles under different CO₂ mass flow rates (m_c). It could be seen that the change of m_c had no significant influence on the temperature profiles in the STGC. As for the FTGC, the effect was obvious near the cold end. ΔT_p increased with the increase of m_c , but the position of the pinch point was slightly

affected by m_c . On one hand, the increase of m_c enhanced the heat transfer coefficients; on the other hand, the higher m_c also enlarged the heat capacity, which required more heat transfer rate for the same temperature change. Hence, the combined effect of the heat transfer coefficients and the specific heat capacity made the temperature profiles change insignificantly.

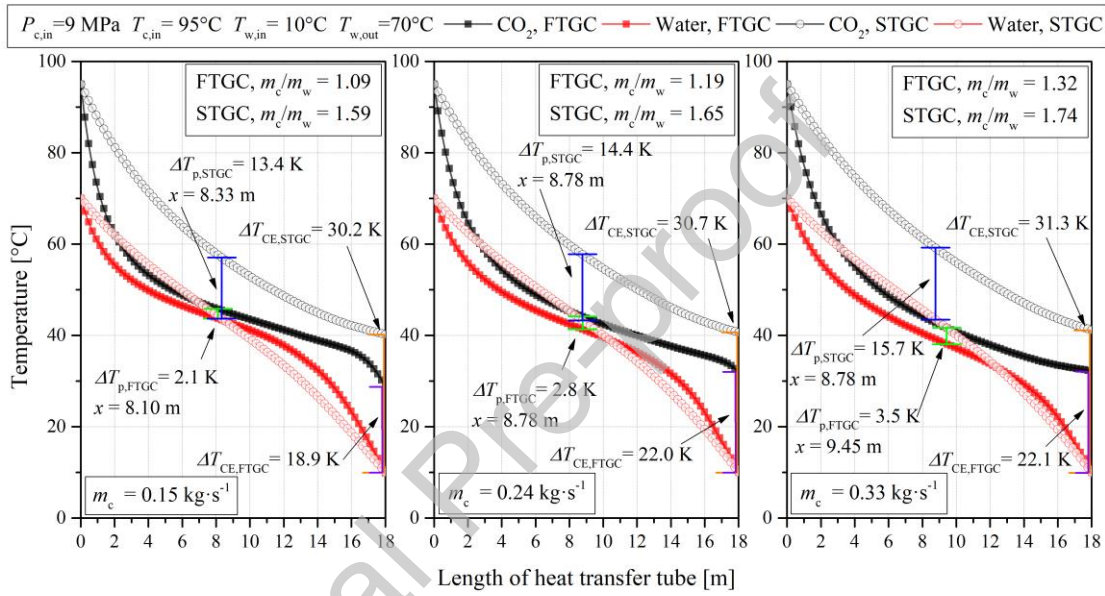


Fig. 8. Temperature profiles of CO₂ and water along the length of the heat transfer tube under different CO₂ mass flow rates.

Fig. 9 shows the variations of the heat transfer rate (Q_h), $T_{c,out}$ and CO₂ outlet pressure ($P_{c,out}$) with the changes of $P_{c,in}$, $T_{c,in}$ and m_c . When $P_{c,in}$ was relatively low, $T_{c,out}$ in both FTGC and STGC was at a high level (respectively up to 32.4°C and 42.4°C) that was significantly higher than the water inlet temperature $T_{w,in}$. This was because the pinch point occurred in the middle part of the heat exchanger and constrained the cooling down of CO₂. With the increase of $P_{c,in}$, Q_h first increased and

then decreased. Moreover, Q_h of FTGC was always higher than that of STGC, and the maximum Q_h of FTGC was 31.2% higher than that of STGC. It proved the heat transfer improvement of the fluted geometry. But the fluted geometry also led to a larger pressure drop, which could be seen from the lower $P_{c,out}$ in the FTGC.

With the increase of $T_{c,in}$, Q_h increased with an approximately linear trend due to the increase of CO₂ inlet enthalpy. $T_{c,out}$ reduced, which could also benefit to the improvement of Q_h , because the increase of $T_{c,in}$ enhanced the heat transfer temperature difference and the water mass flow rate, and then accelerated the cooling of CO₂ from the inlet. For instance, the positions in which the CO₂ temperature in the FTGC reached 40°C in Fig. 7 were respectively 12.22 m, 10.52 m and 9.46 m at $T_{c,in}$ of 85°C, 100°C and 115°C. More portion of the heat transfer tube could be used for further cooling when $T_{c,in}$ was higher.

As m_c increased, $T_{c,out}$ marginally increased in the STGC. In the FTGC, although $T_{c,out}$ showed a trend with increase first and then decrease, the change was still small. Q_h showed a proportional increase with the increase of m_c . Besides, there was an obvious decrease of $P_{c,out}$ in the FTGC with the increase of m_c , i.e. the CO₂ pressure drop in the FTGC significantly increased. When m_c increased from 0.15 kg·s⁻¹ to 0.30 kg·s⁻¹, the CO₂ pressure drop in the FTGC increased by 123.6%.

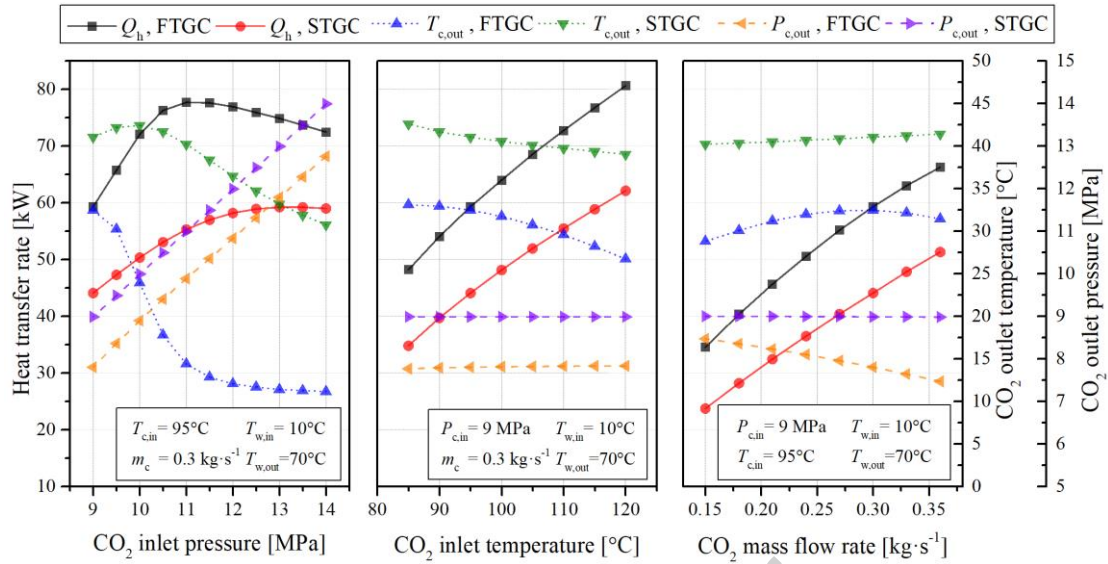


Fig. 9. Variations of the heat transfer rate, CO₂ outlet temperature and CO₂ outlet pressure with the changes of CO₂ inlet pressure, CO₂ inlet temperature and CO₂ mass flow rate.

4.1.2 Water side conditions

Fig. 10 shows the temperature profiles under different $T_{w,in}$. When $T_{w,in}$ was higher, the water temperature changed with a lower speed in the STGC; while the change of water temperature near the cold end declined in the FTGC. The increase of $T_{w,in}$ also reduced the cooling down of CO₂. For example, the positions where the CO₂ in the FTGC reached 40°C were 10.77 m, 11.39 m and 12.35 m at the $T_{w,in}$ of 5°C, 20°C and 35°C, respectively. Regarding the position of the pinch point, in both FTGC and STGC, the pinch point moved toward the cold end as $T_{w,in}$ increased. Furthermore, ΔT_p obviously reduced and even reached 0.6 K in the FTGC when $T_{w,in}$ was 35°C.

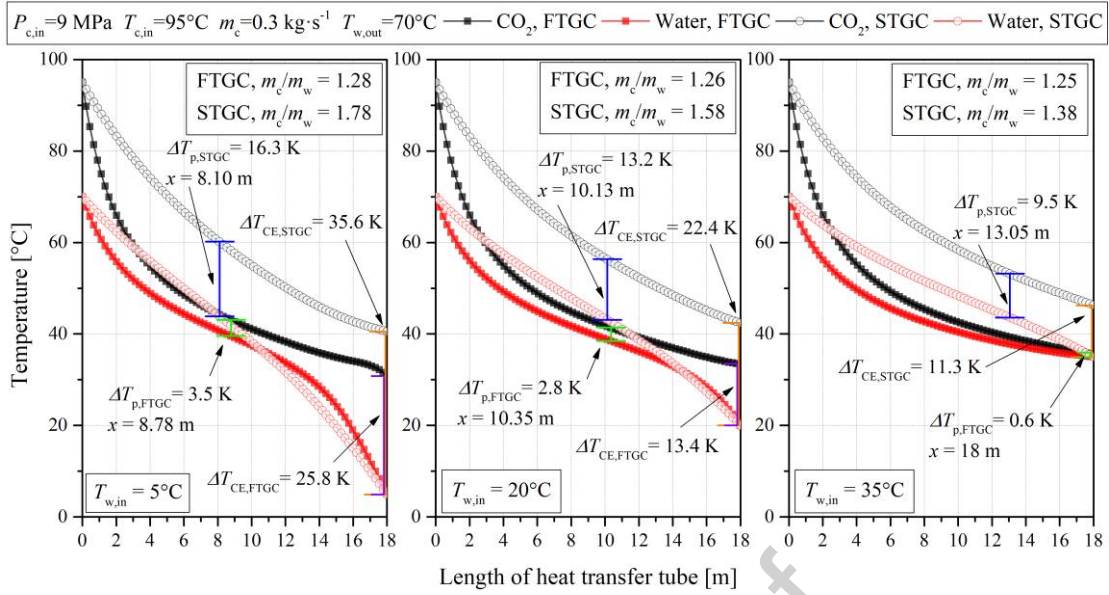


Fig. 10. Temperature profiles of CO₂ and water along the length of the heat transfer tube under different water inlet temperatures.

Fig. 11 shows the temperature profiles under different $T_{w,out}$. The temperature profiles varied more complicatedly when $T_{w,out}$ was low. The significant change of specific heat of supercritical CO₂ with the change of temperature made the temperature show a strongly nonlinear trend. When $T_{w,out}$ was 45°C, the pinch points in FTGC and STGC were at the cold end, and ΔT_p was lower than the values under higher $T_{w,out}$. As $T_{w,out}$ increased, the pinch point moved to the inside of the heat transfer tube.

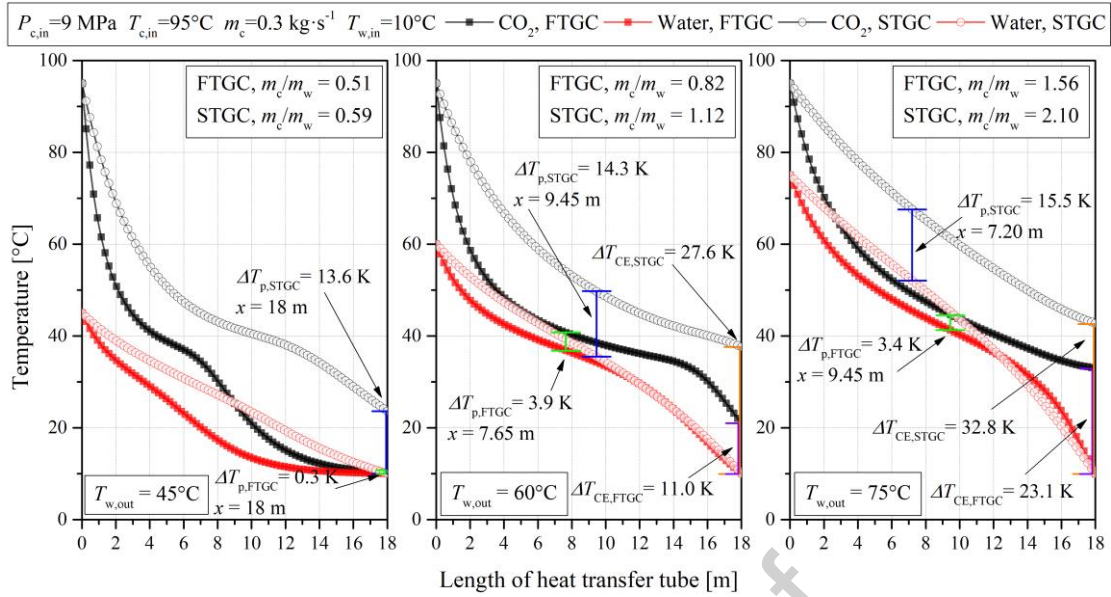


Fig. 11. Temperature profiles of CO₂ and water along the length of the heat transfer tube under different water outlet temperatures.

Fig. 12 displays the variations of Q_h , $T_{c,out}$ and $P_{c,out}$ with the changes of $T_{w,in}$ and $T_{w,out}$. The varying trend of $T_{c,out}$ was different from that of ΔT_{CE} when $T_{w,in}$ was changing. An line for $T_{w,in}$ is added in Fig. 12 to show ΔT_{CE} better. With the increase of $T_{w,in}$, $T_{c,out}$ increased and ΔT_{CE} decreased. When $T_{w,in}$ was larger than 35°C, $T_{c,out}$ in the FTGC was very close to $T_{w,in}$. It indicated that the FTGC had a superfluous heat transfer capacity when $T_{w,in}$ was high. Q_h decreased with the increase of $T_{w,in}$. When $T_{w,in}$ was 10°C, Q_h in the FTGC was 34.47% higher than that in the STGC. However, as $T_{w,in}$ increased, the difference between Q_h in FTGC and STGC dropped. Moreover, when $T_{w,in}$ was 45°C, Q_h in FTGC was even 0.09% lower than that in STGC. It suggested that the benefit of the higher heat transfer coefficients in the FTGC was suppressed when the maximum possible heat transfer rate was small. Furthermore, the

higher pressure drop in the FTGC would lead to a lower Q_h than that in the STGC when $T_{w,in}$ increased further. With the increase of $T_{w,out}$, $T_{c,out}$ increased and Q_h decreased. When $T_{w,out}$ was low (45-55°C), Q_h in the FTGC decreased more slowly because the pinch point located at the cold end and $T_{c,out}$ was close to $T_{w,in}$.

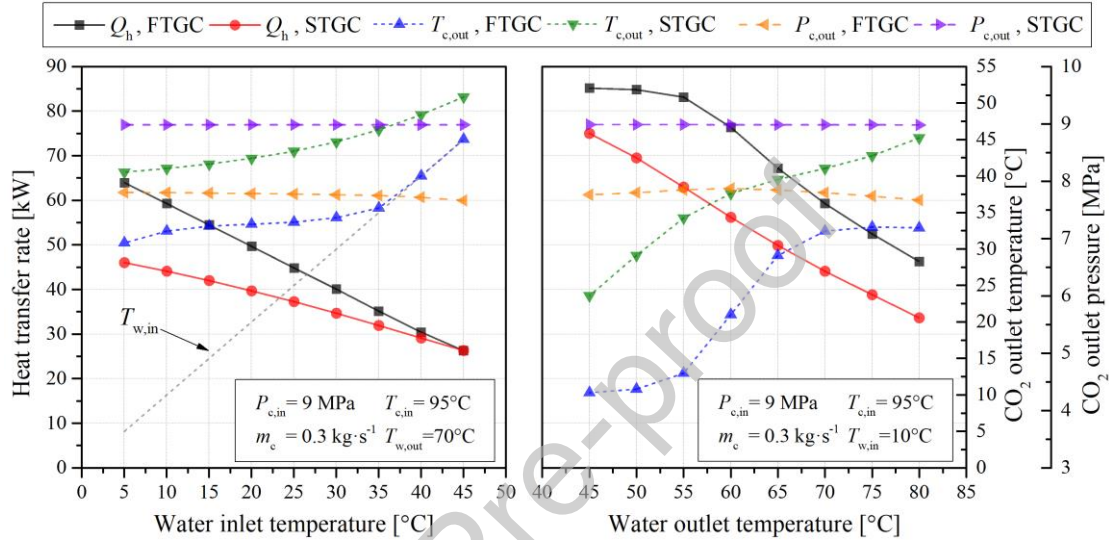


Fig. 12. Variations of the heat transfer rate, CO₂ outlet temperature and CO₂ outlet pressure with the changes of water inlet and outlet temperatures.

4.2 System COP under different conditions

The performance of FTGC and STGC was analyzed above, but the impact on the system COP was also an important issue that should be considered. In this section, the thermodynamic analysis was conducted to study the COP of transcritical CO₂ heat pump cycle without internal heat exchanger under different conditions. During the thermodynamic analysis, the evaporation temperature was 0°C; the superheat degree was 5 K; the throttling process was considered as isenthalpic; the displacement of the

compressor was set as $11.69 \text{ m}^3 \cdot \text{h}^{-1}$ which was the rated value in the tested system; the isentropic and volumetric efficiencies were from Wang et al. (2013). The COP can be defined as:

$$COP_H = \frac{h_{gc,in} - h_{gc,out}}{h_{com,out} - h_{com,in}} \quad (25)$$

4.2.1 System COP with FTGC and STGC

Fig. 13 shows the variation of COP at $T_{w,in}$ of 10°C and 40°C . The COP first increased and then decreased with the increase of compressor discharge pressure (P_d). Therefore, there was optimal discharge pressure (P_{opt}) for maximizing COP. At the same condition, the COP with FTGC was higher than that with STGC, except when $T_{w,in}$ was 40°C , $T_{w,out}$ was 60°C and P_d was lower than 9.4 MPa . The exceptional condition was because the large pressure drop in the FTGC increased the CO_2 outlet enthalpy of gas cooler and limited the heating capacity. When $T_{w,in}$ was 10°C , the maximum COP with FTGC was 27.57% and 29.41% higher than that with STGC at $T_{w,out}$ of 60°C and 80°C , respectively; While when $T_{w,in}$ was 40°C , the improvement reduced (6.30% and 12.98% at $T_{w,out}$ of 60°C and 80°C). Moreover, P_{opt} with FTGC was lower than that with STGC because the larger temperature difference in the STGC required higher P_d to make the pinch point move to the cold end, where the CO_2 gas cooler outlet temperature was close to $T_{w,in}$ and the system COP could be optimized (Chen, 2019).

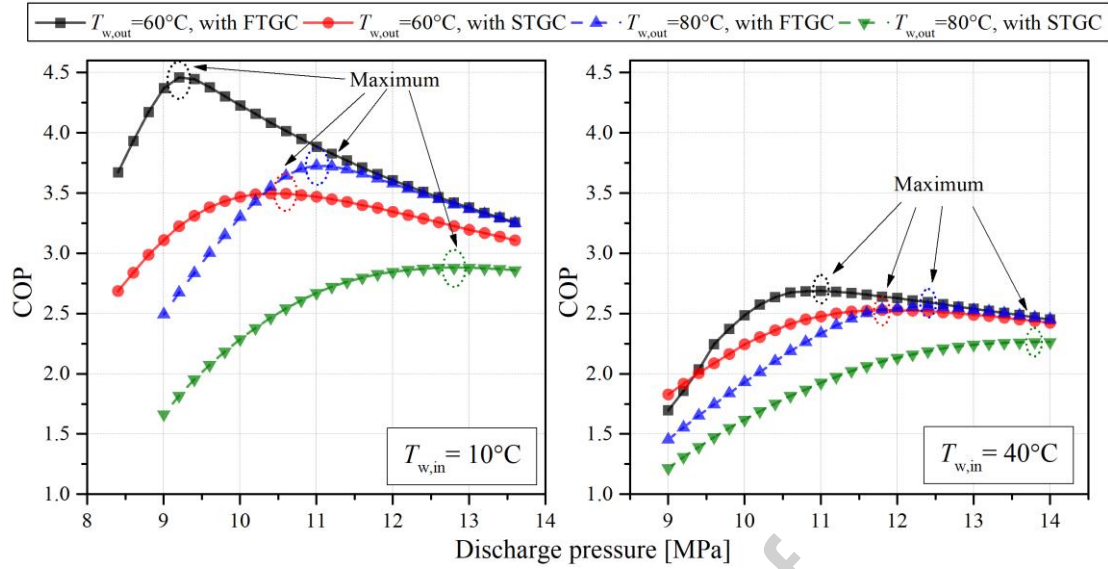


Fig. 13. Variation of COP with the change of discharge pressure at water inlet temperature of 10°C and 40°C.

Fig. 14 shows the system cycles under the situations of below optimal pressure (BOP), optimal pressure (OP) and above optimal pressure (AOP) at $T_{w,in}$ of 10°C. It could be noticed that the gas cooler outlet temperature decreased as P_d increased. This reduction was more significant in the system with FTGC. The larger reduction of gas cooler outlet temperature was the reason why the COP with FTGC increased faster in Fig. 13. However, because the gas cooler outlet temperature was close to $T_{w,in}$ at P_{opt} , the heating capacity could not further increase, which resulted in the larger decrease of COP. Besides, from the process line of the gas cooler, it could be seen that the pressure drop in the FTGC was obviously higher than that in the STGC, which was the side effect of the enhanced heat transfer caused by the complex structure.

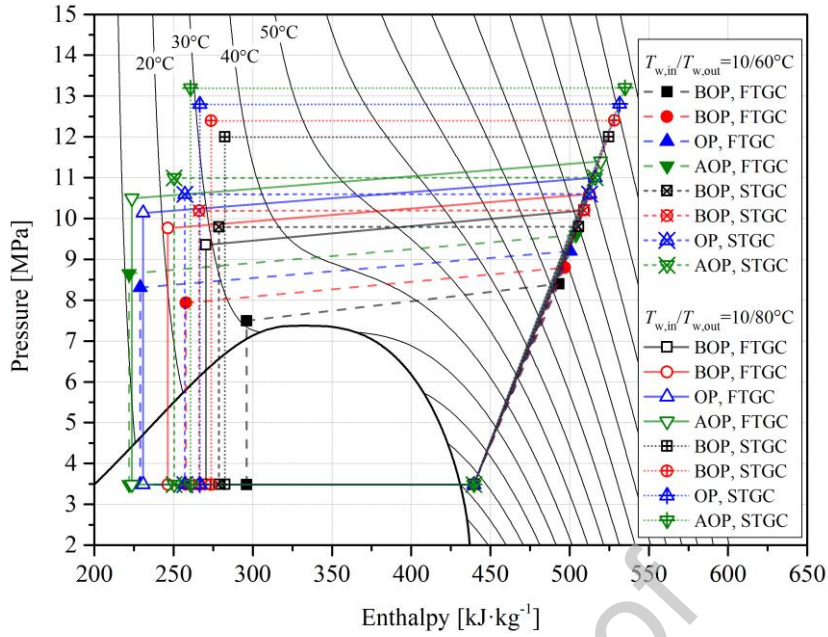


Fig. 14. System cycles at the water inlet temperature of 10°C.

4.2.2 System with different designs of the FTGC

Although the benefit of the FTGC to the system COP was proved, the pressure drop of FTGC was an issue that can be investigated to improve the system performance. In the FTGC, the number of parallel heat exchangers (N_{parallel}) and the tube diameter influences the pressure drop, which was discussed in this section.

Fig. 15 shows the COP with FTGC that had various N_{parallel} . The condition at low $T_{w,\text{in}}$ was chosen because the heat transfer capacity of FTGC was not excessive in this case. Two situations were considered: (1) fixed total heat transfer area and (2) fixed tube length of parallel heat exchangers (18 m). In situation 1, to maintain the same heat transfer area, the length of tube was accordingly changed when N_{parallel} changed; while in situation 2, the total heat transfer area varied with the change of N_{parallel} . The

increase of N_{parallel} reduces the CO_2 mass flow rate and flow velocity in each heat exchanger and decrease the pressure drop and heat transfer coefficient at the same time. When N_{parallel} increased from 3 to 6 with fixed total heat transfer area at $T_{\text{w,out}}$ of 60°C and P_{d} of 10 MPa, the pressure drop decreased from 0.99 MPa to 0.29 MPa. With the fixed total heat transfer area, the maximum COP was highest ($\text{COP}_{\text{max}} = 4.46$) when N_{parallel} equaled to 3 at $T_{\text{w,out}}$ of 60°C ; while at $T_{\text{w,out}}$ of 80°C , the highest maximum COP ($\text{COP}_{\text{max}} = 3.75$) was obtained with N_{parallel} of 2. When N_{parallel} increased to more than 3, the maximum COP kept decreasing. For example, at $T_{\text{w,out}}$ of 60°C , the maximum COP decreased from 4.46 to 4.17 when N_{parallel} increased from 3 to 6. It suggested that the advantage of reducing pressure drop could not neutralize the influence of decreasing heat transfer coefficient. However, when the tube length of parallel heat exchangers was fixed, the maximum COP increased with the increase of N_{parallel} , but the improvement reduced with the increase of N_{parallel} as well. Compared to that with N_{parallel} of 2, the maximum COP with N_{parallel} of 6 was 11.18% and 9.03% higher at $T_{\text{w,out}}$ of 60°C and 80°C , respectively.

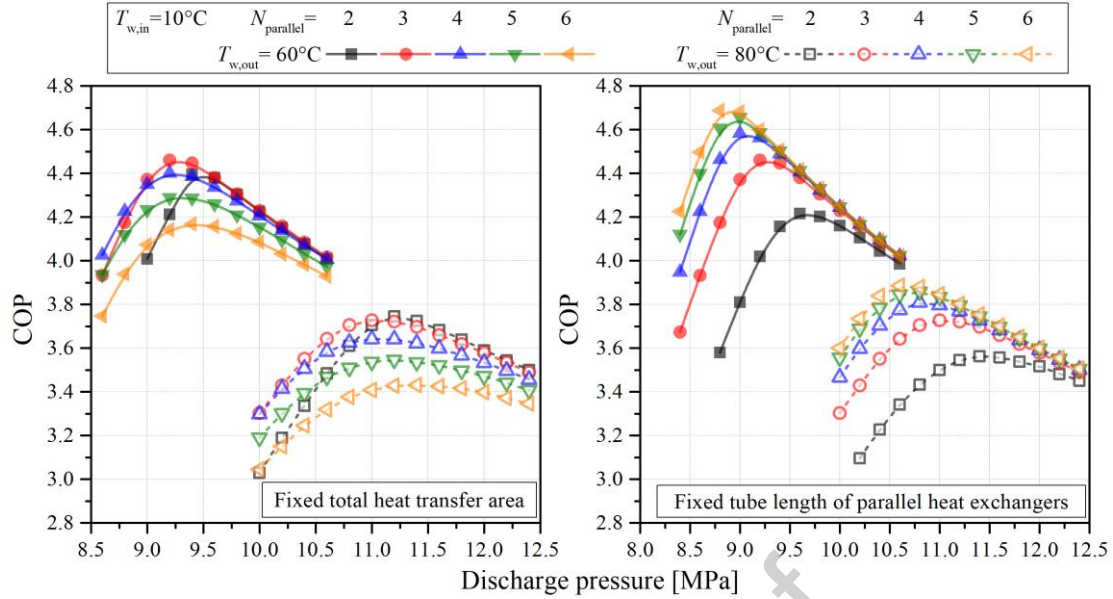


Fig. 15. COP of system with FTGC that had various numbers of parallel heat exchangers.

Fig. 16 displays the COP of system with FTGC that had various zoom factors of tube diameter. Since the simulation model was only validated based on the experimental data with the shape shown in Fig. 2, the zoom factor (ZF) was adopted to study the effect of tube diameter with the same cross-section shape. The cross-section was zoomed up and down with a scale of ZF but the shape was not changed. When $T_{w,out}$ was 60°C with fixed total heat transfer area, the highest maximum COP ($\text{COP}_{\max} = 4.46$) was achieved at ZF of 1.0. Compared to those with ZFs of 0.8 and 1.2, the maximum COP with ZF of 1.0 was higher by 2.31% and 1.96%, respectively. When $T_{w,out}$ was 80°C , the ZF of 0.9 showed the best maximum COP ($\text{COP}_{\max} = 3.74$). Therefore, when $T_{w,out}$ was 80°C with fixed total heat transfer area, it was beneficial for improving the maximum COP to increase the heat transfer

coefficient in spite of the increase of pressure drop through reducing N_{parallel} and ZF slightly. Besides, similar to the effect of N_{parallel} , the increase of ZF with the fixed tube length could improve the maximum COP but the improvement declined evidently. The maximum COP with ZF of 1.2 was 5.27% and 2.45% higher than that with ZF of 0.8 when $T_{\text{w,out}}$ was 60°C and 80°C, respectively.

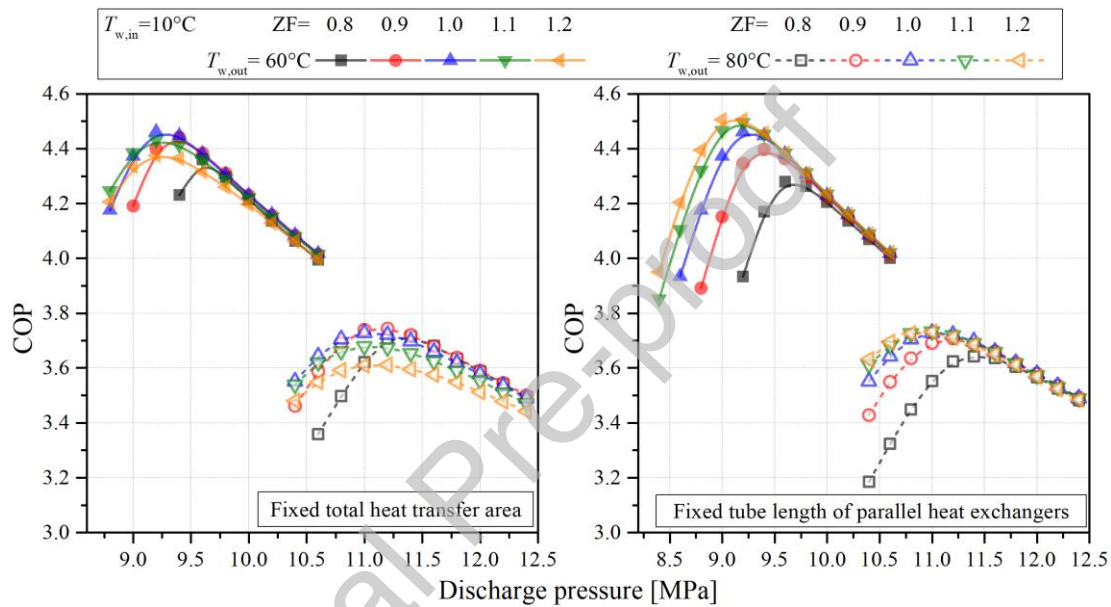


Fig. 16. COP of system with FTGC that had various zoom factors of tube diameter.

5. Conclusions

In this research, the fluted tube-in-tube gas cooler (FTGC) in the transcritical CO_2 heat pump water heater was investigated through simulation. The model validation proved that the proposed model can predict the performance of FTGC in a wide range, which can provide reference for similar applications. For comparison, the smooth tube-in-tube gas cooler (STGC) with the same geometric parameters was also

simulated and discussed. The effects of different parameters on the heat transfer performance were analyzed, and the system COP under different conditions was evaluated. Several conclusions could be drawn:

(1) Generally, the heat transfer rate of the FTGC was higher than that of the STGC. With the enlarged CO₂ inlet pressure, the heat transfer rate first increased and then decreased and the maximum heat transfer rate of FTGC was 31.2% higher than that of STGC. As the CO₂ inlet temperature and CO₂ mass flow rate increased, the heat transfer rate presented a proportional increasing trend.

(2) With the increase of water inlet and outlet temperatures, the heat transfer rate decreased. When the water inlet temperature was 10°C, the heat transfer rate of FTGC was 34.47% higher than that of STGC, and this improvement reduced when the water inlet temperature increased. The position of the pinch point in the FTGC was mainly influenced by the CO₂ inlet pressure and water inlet and outlet temperatures.

(3) The benefit of the FTGC to the system COP was verified in most conditions. The maximum COP in the system with FTGC was always higher. The improvement of the maximum COP could be up to 29.41% when the water inlet temperature was 10°C and the water outlet temperature was 80°C. However, the improvement would be impaired to 12.98% when the water inlet temperature increased to 40°C.

(4) With fixed total heat transfer area, the best maximum COP could be achieved

at the water inlet and outlet temperatures of 10°C and 60°C with the FTGC that had the configuration used in the experiments; when the water outlet temperature was 80°C, the decrease of parallel heat exchanger number to 2 or zoom factor of tube diameter to 0.9 could contribute to the enhancement of maximum COP.

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Declaration of interests

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

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