# A synthesis of feasible control methods for floating wind turbines

Kamran Ali Shah<sup>a,b,c,\*</sup>, Ye Li<sup>a,b,c</sup>, Ryozo Nagamune<sup>d</sup>, Dr. Fantai Meng<sup>a,b,c</sup>, Yarong Zhou<sup>a,b,c</sup>

<sup>a</sup>School of Naval Architecture, Ocean & Civil Engineering, Shanghai Jiao Tong University, Shanghai 200240, China

<sup>b</sup>Multi-function Towing Tank, Shanghai Jiao Tong University, Shanghai 200240, China

<sup>c</sup>State Key Laboratory of Ocean Engineering, School of Naval Architecture, Ocean & Civil Engineering, Shanghai Jiao Tong University, Shanghai 200240, China

<sup>d</sup>Department of Mechanical Engineering, The University of British Columbia, Vancouver, BC, Canada V6T1Z4

### Abstract

Wind energy has become a viable renewable energy source, and it has abundant potential in both onshore and offshore regions. The wind turbine is encouraged to implement in the deep waters with the support of floating platforms for better wind profile and larger potential than onshore wind. However, the wave load acting on the platform, coupled with varying wind load, introduces a dominant disturbance to its stability. During the operation, the motion uncertainty of the platform tends to compromise the system's performance in terms of power maximization, power regulation, and load mitigation. Various controllers are reported in the literature to deal with the platform instability of floating wind turbines. However, it is a great challenge to achieve optimal power, power regulation, and acceptable load mitigation in the presence of incident wind and waves. This paper presents a review of the published control algorithms used to suppress the platform's motion and evaluates their performance with respect to platform motion minimization, load mitigation, power optimization, and regulation. Potential controller performance improvement based on predicted incident wind and wave is discussed. Recommendations and suggestions for further research are also provided at the end.

*Keywords:* Floating Offshore Wind Turbines, Floating Platforms, Wind turbine control, Wind energy

Preprint submitted to Renewable and Sustainable Energy Reviews

<sup>\*</sup>Corresponding author Email address: ye.li@sjtu.edu.cn (Ye Li)

## 1 Nomenclature

- <sup>2</sup> ANFIS Adaptive Neuro-Fuzzy Inference System
- 3 ANN Artificial Neural Network
- 4 AR Auto-Regressive
- 5 ARIMA Auto-Regressive Integral Moving Average
- 6 ARMA Auto-Regressive Moving Average
- 7 BEM Blade Element Momentum
- 8 CBP Collective Blade Pitch
- 9 CBPC Collective Blade Pitch Control
- 10 DOF Degree of freedom
- <sup>11</sup> DAC Disturbance Accommodating Control
- 12 DMD Dynamic Mode Decomposition
- 13 EMD Ensemble Mode Decomposition
- 14 ESPRIT Estimation of Signal Parameters via Rotational Invariance Techniques
- 15 ELM Extreme Learning Machine
- <sup>16</sup> FAST Fatigue Aerodynamics Structures and Turbulence
- 17 FOWT Floating Offshore Wind Turbine
- 18 GSPI Gain-Scheduled Proportional-Integral
- 19 GP Gaussian Process
- 20 HAR Hammerstein Auto-Regressive
- <sup>21</sup> HAWC2 Horizontal Axis Wind Turbine Code-Second generation
- 22 HAWT Horizontal Axis Wind Turbine

- 23 HMD Hybrid Mass Damper
- 24 IBP Individual Blade Pitch
- 25 IBPC Individual Blade Pitch Control
- 26 IEA International Energy Agency
- 27 LSSVM Least Square Vector Support Machine
- 28 LCOE Levelized Cost of Energy
- <sup>29</sup> LIDAR Light detection and ranging
- 30 LPV Linear Parameter Varying
- 31 LQR Linear Quadratic Regulator
- 32 MLC Machine learning control
- 33 MPC Model Predictive Control
- 34 MBS Multi-Body System
- 35 MIMO Multi-Input Multi-Output
- 36 NREL National Renewable Energy Lab
- $_{37}$   $P_{rated}$  Rated Power
- 38 PI Proportional Integral
- $_{39}$   $V_{rated}$  Rated Wind Speed
- 40 RNN Recurrent Neural Network
- 41 SISO Single-Input Single-Output
- 42 SINDy Sparse Identification of Nonlinear Dynamics
- 43 SMC Sliding Mode Control
- 44 SC Structural Control

- 45 SVM Support Vector Machine
- 46 TRL Technology Readiness Level
- 47 TLP Tension leg platform
- 48 TMD Tune Mass Damper
- <sup>49</sup> TLD Tuned Liquid Damper
- $_{50}$   $V_{cut-in}$  Cut-in wind speed
- $_{51}$   $V_{cut-off}$  Cut-off wind speed
- $_{52}$   $V_{rated}$  Rated wind speed
- 53  $V_{wind}$  Wind speed

### 54 1. Introduction

Wind energy is one of the leading commercial renewable energy resources, and it has significant 55 potential in both onshore and offshore areas [1, 2]. There is a rapid increase in global wind power 56 (onshore and offshore) production in the last decade to utilize this potential, as shown in Figure 1. 57 The total installed capacity for onshore wind turbines has increased from 159GW to 651GW in the 58 last decade. Moreover, an increase in the annual installed offshore wind energy capacity is reported, 59 with a record capacity addition of 6.1GW annual offshore wind energy in 2019. An estimate of new 60 annual offshore installed capacity may exceed 30 GW in 2030, with a compound annual growth rate 61 of 18.6% for the first half and 8.2% during the latter part of the decade, as shown in Figure 2. 62

# 63 1.1. Outlook of Offshore wind

Wind characteristics in the deep sea are more steady, streamlined, and it has a higher annual mean speed than onshore wind [3, 4].Superior wind quality improves wind energy generation of wind turbines operating in the deep sea. 80% offshore wind energy potential of Europe lies in a water field deeper than 60 meters [5], and therefore, arises a need to install the wind turbine in the deep sea. Additionally, it is encouraged to utilize the offshore wind potential to ease the transition towards renewable energy resources and keep the global temperature at 1.5 degrees Celsius, according to the Intergovernmental Panel's recommendation on Climate Change (IPCC) [6]. The onshore wind
farms pose environmental harm to human beings and wildlife (i.e., visual and noise impacts) [7–9].
The hazards caused by the land-based wind farms and the low characteristics of onshore wind may
be avoided by installing the wind turbines in the deep offshore regions

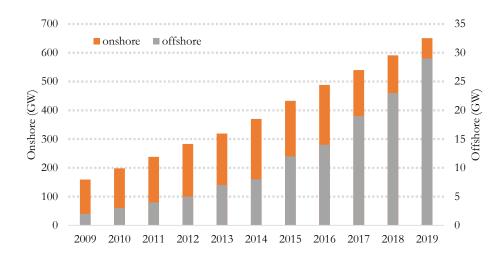


Figure 1: Cumulative installed (onshore and offshore) wind energy capacity of the world (data obtained from [10])

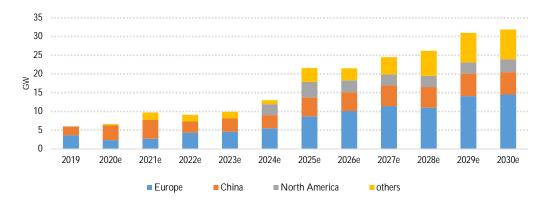


Figure 2: New annual installation prediction until 2030 (data obtained from [11])

### 74 1.2. Floating platform and associated problems

Wind turbine placed on top of a floating platform is a feasible solution to operate in deep-sea 75 as the economic constraint hinders the development of a fixed bottom support structure for wind 76 turbines operating beyond 60m water depth. Building a fixed bottom platform for a wind turbine 77 in the deep sea would likely increase the overall cost. Offshore oil and gas exploration in the deep 78 sea greatly relies on floating platforms [12]. Similarly, wind turbines may be operated in the deep 79 ocean using a floating platform attached to the sea bottom. Several concepts exist in the literature 80 to achieve platform stability for FOWT such as Barge, Tension leg platform (TLP), Spar-buoy and 81 Semi-submersible, as shown in Figure 3. These concepts include buoyancy stabilized platforms, 82 mooring lines stabilized platforms, and ballast stabilized platforms. Buoyancy stabilized platforms 83 use submerged body volume to achieve stability, e.g., Barge and Semi-submersible platforms. The 84 tension leg platform (TLP) is a typical example of mooring lines stabilized platform, where the 85 platform is stabilized using mooing lines. In comparison, the spar-buoy is an example of ballast 86 stabilized platform that benefits from the heavy ballasting of the platform's bottom to stabilize 87 the structure. There are two type of wind turbines that are used to generate wind energy i.e., 88 Horizontal axis wind turbines (HAWTs) and Vertical axis wind turbines (VAWTs), however the 89 scope of this paper is limited to the HAWTs operating in deep-sea. 90

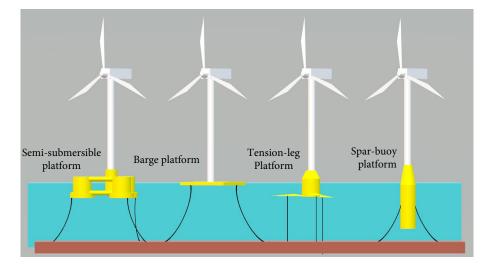


Figure 3: FOWT platforms (Semi-submersible platform, Barge, Tension-leg, and Spar-buoy)

<sup>91</sup> Using these floating platforms, wind turbine extract energy from the superior offshore wind

operating in the deep ocean. However, floating platforms introduce additional loadings (hydrodynamic loading, mooring loading) due to incident wave along with the aerodynamic loading on wind turbine. Incident wave associated loadings of floating offshore wind turbine (FOWT) leads to additional 6 degree-of-freedom (DOF) motion compared to the fixed bottom WTs, as shown in Figure 4 where a FOWT is stabilized using a TLP base. The stability of the floating platform is one of the dominant concerns of FOWT technology which may directly impact the performance and safety of FOWTs, leading to increased cost [13].

The performance of a FOWT system can be significantly compromised due to the motion of a 99 floating platform. An unstable platform may decrease the nominal wind turbine area and affect 100 energy generation. Platform motions may also increase tower loads compared to fixed bottom 101 wind turbines and negatively impact the system's structural life. Furthermore, it also increases 102 the cost and weakens the economic advantage as compared to onshore wind turbines. Various 103 control algorithms attempt to achieve efficiency and platform motion suppressions by controlling the 104 blade pitch actuator and generator torque of wind turbine. There have been numerous controllers 105 designed to address the shortcomings of floating platform using a range of controllers, such as 106 Proportional Integral (PI), Linear Quadratic Regulator (LQR), Linear Parameter Varying (LPV), 107 and Model Predictive Control (MPC) [14–29]. Some advanced control algorithms utilize the blade 108 pitch mechanism by actuating blades identically (Collective blade pitch) or separately (Individual 109 blade pitch) to provide the wind turbine required aerodynamic thrust to suppress platform motions, 110 maximize power generation and load mitigation. In comparison, Tuned Mass Damper (TMD) 111 based structural control systems [30–33] introduce an extra degree of freedom and decouple the 112 pitching mechanism from providing the required thrust to reduce the pitching phenomena. Advance 113 controllers like MPC based on Light Detection and Ranging (LIDAR) information [25] incorporate 114 the incident wind disturbance before reaching the wind turbine, thus enhancing the performance 115 compared to traditional feedback controllers that function after experiencing incident disturbance. 116 However, the levelized cost of energy cost of energy (LCOE) of FOWT is still higher than the fixed 117 bottom wind turbines. Improved control mechanism may elevate the performance of a FOWT that 118 would lead to reduction in LCOE. 119

The performance of advanced controllers can be improved by incorporating wind and wave forecast techniques. Predicted wind and wave information ahead of its encounter with the wind turbine can provide preview based advanced controllers enough time to respond to incoming disturbances

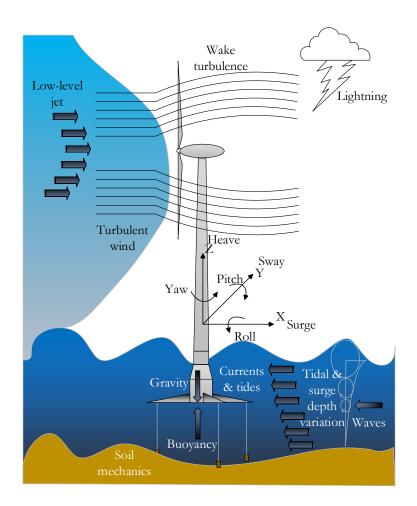


Figure 4: Floating offshore wind turbine in its surroundings

and orient wind turbine for optimal and efficient performance. The wind turbine industry is al-123 ready benefiting from the wind forecast for wind farm planning, operation, and grid integration 124 [34]. Numerous forecasting techniques for wind and wave are present in the literature, ranging from 125 long-term (3 days - 1 week or more) to short-term(few seconds – 30 minutes) prediction horizons 126 [35–50]. However, the controller response time for FOWT falls in the short-term prediction horizon 127 category [51, 52]. An accurate short-term disturbance prediction incorporated in modern control 128 systems, e.g., feed-forward control or MPC, can enhance the performance in terms of platform 129 stability and loadings and deal with the incident disturbance better than the counterpart feedback 130

<sup>131</sup> controllers, resulting in further lowering the LCOE.

132 1.3. Objective

This paper reviews the controllers designed for FOTWs aiming at the platform stability enhancement, maximum power generation and structural life extension. A detailed discussion is presented, and potential improvements based on the reviewed controllers are provided. The paper outline is as followed: Section 2 presents the system overview. Control structure and methodologies used for FOWTs are discussed in Section 3. In Section 4, the wind and wave prediction for the control design is introduced. The discussion and the summary is presented in Section 5 and Section 6, respectively.

# <sup>140</sup> 2. System description

FOWT operates in the deep sea with an extension of a floating platform attached to the sea bottom with mooring lines. However, the foundation of a FOWT exhibits 6 degrees of motion due to incident wave, as shown in Figure 4. The performance and operation of the wind turbine is coupled with the platform motion. Therefore, it is essential to minimize the platform motions during the operation of FOWT. A description of the operation of the FOWT is provided below.

#### 146 2.1. Wind turbine

<sup>147</sup> Wind turbines deployed in the deep sea operate similarly to land-based wind turbines to extract <sup>148</sup> kinetic energy from the wind. Air passes through the blades and causes the rotor to rotate. The <sup>149</sup> rotor is connected to a generator which produces energy. The maximum possible energy extracted <sup>150</sup> from wind is 59.3%, known as the Betz limit [53]. Maximum power ( $P_{max}$ ) generated by a wind <sup>151</sup> turbine in a given scenario can be calculated by the following formula, as shown in Figure 5.

$$P_{\max} = \frac{1}{2} \rho A v^3 C_p(\lambda, \beta) \tag{1}$$

152

$$\lambda = \frac{\Omega R}{v} \tag{2}$$

153 where

•  $\rho = \text{Air density}$ 

- A =Swept Area
- $C_p$  = Power coefficient (based on tip-speed ratio ( $\lambda$ ) and blade pitch angle  $\beta$ )
- R = Rotor radius
- $\Omega$  = Angular speed
- v = Wind speed

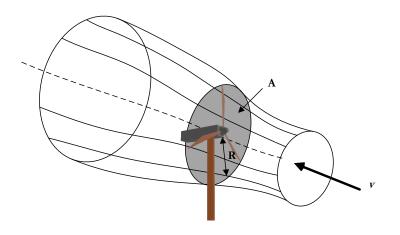


Figure 5: Wind energy extraction using wind turbine

The incoming wind speed is an essential factor in the control system design, control objectives 160 and operation of wind turbines. The operating spectrum of a wind turbine is divided into three 161 significant regions, as shown in Figure 6. In region I, the wind speed is less than the cut-in wind 162 speed  $(V_{cut-in})$ , and the wind turbine is in parked condition. In region II, the wind speed value is 163 less than the rated value  $(V_{Rated})$ . The control objective focuses on the maximum energy extraction 164 from the wind by keeping the blade pitch at an optimal angle. In region III, where the wind speed 165 value surpasses the (V<sub>Rated</sub>), the objective shifts towards regulating generated power with pitch 166 angle activity. When the wind speed reaches cut-off wind speed  $(V_{cut-off})$  the mechanical brakes are 167 applied for the safety of wind turbine. In the case of FOWTs, the number of control objectives are 168 increased with the consideration of platform motion. For a FOWT, the floating platform, regardless 169 of being tied to the seabed, may generate significant problems due to incident waves and wind loads. 170

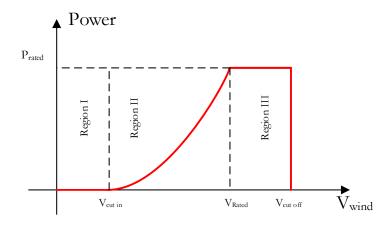


Figure 6: Operating regions of a wind turbine

# 171 2.2. Framework of FOWT control systems

FOWTs are prone to platform motions due to floating base which leads to performance deterioration. However, an effective control system may deal with the platform motions and achieve optimal wind energy generation. Existing control mechanisms for fixed bottom wind turbine are rendered infeasible for FOWTs due to the additional platform motion of FOWT. However, fixed-bottom wind turbine controllers maybe modified to include the platform motion suppression objective.

Majority of the FOWT controllers are based on feedback control mechanism. In addition, there are advanced feed-forward controllers available in the literature as well. A detail discussion on these controllers is given in the Section 3. The benefit of feedforward mechanism may be further extrapolated by using incident wind and wave forecast to improve the controller performance. An account of incident wind and wave forecast is given in Section 4.

### 182 **3. FOWT Control structure**

Control system of a wind turbine is responsible for handling the aerodynamic wind load and converts the wind energy into electric power. In general, there are multiple control levels to deal with the wind turbine operation. The primary-level supervisory control level deals with the startup and shutdown of the wind turbine. The wind turbine is only started up when there is enough wind, and shutdown is triggered in the presence of excessive wind, as it may harm the wind turbine structure. The second-level operational control is dedicated to achieving control objectives based

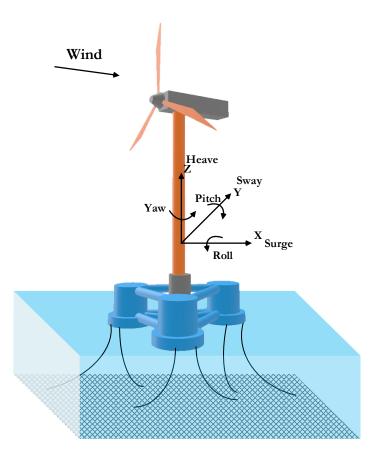


Figure 7: Associated platform motions of FOWT

on the wind turbine operating region, as shown in Figure 6. In comparison, the third-level control is concerned with the yaw and pitch actuation system and related electronic units. The scope of this paper is limited to the second-level operational control of a wind turbine. Later in this section, the control objectives and control methodologies used to achieve these objectives for FOWTs are discussed in detail.

### <sup>194</sup> 3.1. Control objectives

Control objectives of a wind turbine vary based on the operating regions, namely maximum 195 power generation operating in region II and power regulation in III, as shown in Figure 6. There 196 are generally two control loops to achieve these control objectives, as shown in Figure 8. Operating 197 in region II, the torque control loop of the wind turbine is used to maximize the generated power 198 by operating near the optimal  $C_p$  by using fixed blade-pitch angle to an optimal value, based 199 on equation 3. In region III, the objective shifts towards regulating the generated power at the 200 rated value. The blade-pitch control loop regulates the aerodynamic loads and generated power 201 by manipulating the blade pitch value. There are two standard pitching strategies for the region 202 III pitch control loop, pitch-to-stall and pitch-to-feather [54]. The generator torque control while 203 operating in region III, is calculated based on the relationship in equation 3. 204

However, the major problem associated with FOWT occurs due to platform motion while operating in region III. The wind turbine structure undergoes undesired pitching phenomena, often called negative pitching [55]. The frequency of the platform is coupled with the blade pitch mechanism while operating in region III, causing a surge in the pitching motions of the platform leading to issues like poor power quality and increased loads. Therefore, an adequate control mechanism to achieve the standard wind turbine control objectives and deal with the platform pitching phenomena associated with floating platform of FOWT is needed.

$$T_{gen} = \frac{\pi \rho R_{rotor}^5 C_{p,\max}}{2\lambda_o^2 N^3} \omega_{gen}^2 = K \omega_{gen}^2 \tag{3}$$

$$T_{gen} = \frac{P_{rated}}{\eta_{gen}\omega_{gen}} \tag{4}$$

212 where

- $T_{gen}$ =Generator torque
- $\rho$ = Air density
- $R_{rotor} = \text{Rotor radius}$
- N = Gear box ratio
- $C_{p,\max}$  = Maximum power coefficient

- $\lambda_o = \text{tip speed ratio related to } C_{p,\max}$
- $\omega_{gen}$  = Generator rotational speed
- $\eta_{gen}$  = Generator efficiency
- $P_{rated}$  = Rated generated power

A range of system models are available in the literature, that are used to develop control schemes for FOWT and preview the outcome without running the actual wind turbines. Appendix A contains the details of these simulation codes for the readers further interested in FOWT system models.

### 226 3.2. Control methodologies

Control methodologies for FOWT to deal with the undesired platform associated motions while operating the wind turbine at optimal level are based on traditional single-input single-output (SISO) and advanced multi-variable multiple-input-multiple-output (MIMO) mechanisms. This section provides a discussion on the range of these controllers reported in the literature.

### 231 3.2.1. Traditional FOWT controllers

The traditional FOWT controllers are simple and easy to design control mechanisms that are based on the single-input single-output (SISO) principle. Independent control loops are applied in parallel to achieve multiple control objectives, as shown in Figure 8.

Platform pitching motion of FOWT was minimized by keeping the frequency of the blade pitch mechanism lower than the resonance frequency of the platform by Larsen et. al [14]. For region 2, a variable speed control loop was used to maximize the generated power. A region of constant speed was introduced between regions 2 and 3, followed by a constant torque loop in region 3. Pitching action is determined by a gain-scheduled proportional-integral (GSPI) controller for region 3. Improved platform pitching was achieved using less aggressive control methodology at the cost of lowered power quality and poor rotor speed regulation.

Another GSPI controller based solution for negative platform damping problem of barge based FOWT was provided by Jonkman [15]. Two independent SISO controls were designed; A generatortorque controller to generate maximum power in region 2 and keep the power captured at the rated value in region 3. A GSPI controller was considered to adjust rotor speed as a function of blade pitch

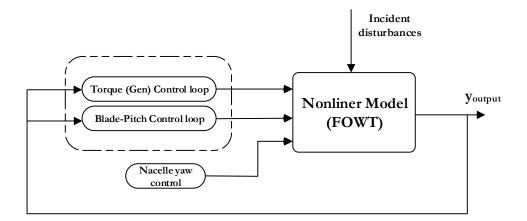


Figure 8: Wind turbine standard control loops

activity based on the collective blade pitch (CBP). Jonkman et al. [15] designed additional control loops upon facing complications regarding platform oscillations and power fluctuation during the early design synthesis. Tower-top feedback control, active pitch-to-stall control and a controller based on detuned gains were the additional loops included in the original design mechanism. These additional loops were proposed to minimize the fore-aft motion of the tower, instability of platform yaw, and excessive barge motions, respectively. Tower top feedback control failed to improve the pitching motions of the platform.

Furthermore, active pitch-to-stall control was found good at power regulation for the barge platform at the expense of increased platform pitching motion. Whereas, detuned gains proved to be the most suited controller among others, as it reduced the blade activity and addressed the platform pitching issue. This configuration is used for testing newly designed controllers and labeled as baseline FOWT control [56]. The use of individual blade pitch (IBP) and multiple-inputmultiple-output (MIMO) state-space controllers were suggested to enhance performance further.

Baseline controller designed by Jonkman et al. [15] was analyzed for different platforms by Matha et al. [57]. The TLP, Barge, and Spar-buoy floating concepts were compared concerning fatigue loads and platform stability. Matha et al [57] modified the baseline controller for the sparbuoy platform. Constant torque control was designed to improve the platform pitching motion while operating in region 3, contrary to a constant power controller originally designed by Jonkman et al. <sup>264</sup> [15]. Meanwhile, the controller's bandwidth was kept low to avoid coupling with the frequency of <sup>265</sup> the platform. It was noticed that the barge platform is cost-effective, but its inability to withstand <sup>266</sup> incident loads may cause stability issues. The spar-buoy platform showed resistance towards tower <sup>267</sup> loading as compared to the barge platform. However, the deployment of the spar-buoy platform <sup>268</sup> is costly due to its intricate design and assembly. In comparison, TLP was found to have better <sup>269</sup> performance among the compared concepts. However, it was found that the anchoring system of <sup>270</sup> TLP may increase the cost.

Platform instability was addressed by using the pitching velocity as an input to regulate the generator rated speed in region 3 [16]. The generator speed was used to provide the counter thrust to suppress the platform pitch motion and achieve platform stability. This unique control methodology reduced negative damping and blade pitch activity at the cost of acceptable rotor speed fluctuations and power variation. In a subset simulation, Individual blade pitch control (IBPC) was implemented using the Coleman transformation [58] to reduce blade loads. However, the IBPC increased the blade pitch activity resulting in inadequate blade load reduction.

A control strategy based on the estimation of wind speed to suppress the negative damping for the Hywind concept platform [55] was proposed by Skaare et al. [17]. The control mechanism designed by Skaare et al. [17] improved the tower loading and the nacelle oscillations. Simultaneously, the poor rotor speed regulation and the reduced power generated were observed compared to the conventional blade pitch mechanism. Moreover, since the strategy was based on the estimated form of wind in region 3, this control scheme's effectiveness was mainly governed by the wind estimation quality.

### 285 3.2.2. Advanced control methods

The classical SISO controllers are easy to realize controllers, however may not be a suitable op-286 tion for highly coupled multi-objective systems like FOWTs. The design process of SISO controllers 287 requires a thorough understanding of the system and careful tuning of control loops separately. Oth-288 erwise, multiple control loops may couple with each other and affect the overall system operation. 289 As suggested by Jonkman et al. in [15], advanced controllers based on multi-input multi-output 290 (MIMO) may further improve the performance of FOWT due to its inherent ability to deal with 291 short comings of SISO control. Multi-variable MIMO control schemes such as Linear Quadratic 292 Regulator Control (LQR), Linear Parameter Varying control (LPV), Model Predictive Control 293

<sup>294</sup> (MPC), used for FOTWs reported in the literature are described below.

<sup>295</sup> Most of the advanced controller designed for FOWT are based on State-space control. State-<sup>296</sup> space control design involves linearizing the non-linear system model at an operating point  $x_{op}$  such <sup>297</sup> that state x transforms into the deviation  $\Delta x$  around the  $x_{op}$ . Later, linear control theory is applied <sup>298</sup> to design a controller to achieve the given objectives. State-space equation is shown below,

$$\Delta \dot{x} = A \Delta x + B \Delta u + B_d \Delta u_d$$

$$\Delta y = C \Delta x + D \Delta u + D_d \Delta u_d$$
(5)

- 299 where
- $\bullet x = x_{op} + \Delta x$
- $_{301}$  y = Measurement matrix
- u = Actuator matrix
- $\Delta u_d$  = Disturbance matrix
- A =State matrix
- B =Actuator Gain matrix
- $B_d$  = Disturbance gain matrix
- C = Output matrix
- D = Feed-through inputs
- $D_d$  = feed-through disturbance

Several advanced controllers were designed using MIMO state-space methodology on Barge, 310 TLP, and Spar-Buoy platform based FOWT [20–22]. The collective blade pitch controller (CBPC) 311 and IBPC were designed for a barge platform [20]. The IBPC and wind disturbance-based Dis-312 turbance Accommodating Control (DAC) were designed for FOWTs on a barge, and TLP [22]. 313 The controllers designed for Barge and TLP were later used to investigate the performance of the 314 Spar-buoy platform [21]. In region 3, the CBPC scheme for FOWT showed improvements in better 315 speed regulation, mainly due to constant power control instead of constant torque control and the 316 platform pitch motion reduction. 317

<sup>318</sup> IBPC was utilized to deal with the overlapping blade pitch commands issued for the rotor speed <sup>319</sup> control and the platform pitch minimization [21]. IBPC mechanism improved tower loading for the <sup>320</sup> barge platform. In comparison, the performance of IBPC was found limited due to the relatively <sup>321</sup> lower platform frequency spar-buoy platform. On the other hand, DAC has an advantage due to <sup>322</sup> improved rotor and power regulation based on increased blade pitch actuation for the spar-buoy <sup>323</sup> platform.

Controller-based on IBP achieved improvements when applied to the Barge platform compared to the CBP control [20]. DAC was rendered not useful for barge platform because the barge platform is mainly influenced by waves; however, DAC is used to influence wind disturbances. [22]. IBPC was shown to have improvements regarding rotor speed and power regulations for Barge and TLP, but for Spar-buoy, when dealing with the platform pitching, this scheme was not as effective due to the low natural frequency of the platform. Further improvements related to power and speed regulations were achieved using DAC for the TLP platform.

A study was conducted on the input-output relation of the 10MW FOWT to find out the 331 frequencies with a substantial impact on the output with the least control variable impact by F. 332 Lemmer et al. [23]. The wave information was added to produce a realistic environment and 333 representation of the coupled frequencies with the parametric wave excitation model from [59]. 334 Wind and wave disturbances with significant impact on the output due to the minimum control 335 actuation were chosen. This information was used to design an LQR controller based on input blade 336 pitch angle and generator torque, and a comparison to a conventional PI controller was made. The 337 designed controller was noticed to have improvements concerning system response reduction and 338 damping various resonances. However, the control mechanism could not completely overcome the 339 effect of incoming wave disturbance. 340

Gain scheduled output feedback H-infinity control based on collective blade pitch approach for FOWT operating in region 3 was designed by T. Bakka et al. [18]. A simplified model is generated based on significant FAST model dynamics for control synthesis, namely, the rotor generator and tower. Linear models are generated at multiple operating points based on output feedback H-infinity control, and a scheduling mechanism is developed. Substantial improvements were found in terms of the tower loadings and rotor speed regulation.

Linear Parameter Varying (LPV) and Linear Quadratic Regulator (LQR) developed by using gain-scheduled (GS) blade pitch controller for a barge platform-based FOWT [19]. The objective was to regulate the generated power and minimize structural loadings while operating in region 3. The LPV was further modified with the state feedback and output feedback control mechanisms and compared with the baseline wind turbine [15, 60]. It was found that the GS-LPV and GS-LQR controllers performed better in terms of power regulation and platform pitch minimization. Whereas, LPV-GS controller with state-feedback has shown superior improvements in platform pitch motion damping than the rest of the controllers.

Input/output feedback linearization (IOFL) and Sliding Mode Control (SMC) methods were 355 used to analyze the effects of incident disturbance on platform motions and regulate generator 356 speed and of FOWTs operating in region 3 [24]. A simplified model based on the DOFs of blade 357 pitch and generator speed, and platform pitch was obtained. Later, a simplified non-linear model 358 based on series of linearized simplified models is designed. The switching mechanism between these 359 linear models is obtained based on the LPV model as a blade pitch angle function. Compared 360 with the baseline model, SMC showed improvements regarding generator speed regulation, while 361 the platform pitch motions were on a similar level as for the baseline wind turbine. The reason 362 for speed regulation was, the wind speed was considered for control design. However, the platform 363 motions were observed without adding to the control design. Contrary to SMC, IOFL control 364 causes increased platform pitching motion when compared with the baseline controller. Another 365 important finding was observed that the performance of the developed controller was degraded 366 when implemented on complex models. 367

Model predictive control (MPC) is an advanced control method that predicts future action 368 based on the internal system model's available information fulfilling a set of constraints. Numerous 369 examples are available in the literature regarding the use of MPC for fixed bottom wind turbines. 370 [61–64]. D. Schlipf et al. [25] designed a non-linear-MPC (NMPC) for FOWTs operating in region 371 3 based on the simplified Sander model [65]. The incident wind and the wave preview was used 372 for the controller design based on CBP and generated torque. The control objective was to keep 373 the generated power and rotor speed steady based on an ideal estimation of the wind and the 374 wave preview [61]. The designed controller was later used on the baseline FOWT [15] placed on 375 a spar-buoy platform under an intense wave and wind profiles. The controller showed satisfactory 376 results regarding the generated power and speed regulation error, including the blade load reduction; 377 However, the NMPC controller requires higher computational resources. 378

<sup>379</sup> Following the CBP-based non-linear MPC design for FOWT in [25], S. Raach et al. [26] came

<sup>380</sup> up with an extended version of NMPC based on the IBP mechanism. The IBPC-NMPC included <sup>381</sup> the rotor and the blade load reductions alongside the existing benefits of the original CBP-NMPC, <sup>382</sup> platform pitch reduction and rotor speed regulation. After the controller design, its successful <sup>383</sup> implementation on the baseline wind turbine exposed to the turbulent loads was achieved. The <sup>384</sup> rotor's fatigue loads were reduced significantly by using the extended NMPC based on the IBP <sup>385</sup> mechanism.

An optimal linear MPC implemented on a 10 MW FOWT by F. Lemmer et al. [27]. A tunable controller was designed to provide early-stage design assistance during the fabrication of FOWT. The linear-MPC based on the MIMO system was designed to operate in region 3 to regulate the power to a constant value and minimize the structural loads. In comparison, maximum power generation was the primary objective for region 2. Linear-MPC showed adequate improvement than a PI controller for the rotor speed and generator power regulation. Moreover, the tower top movement and negative platform pitch were also minimized.

### 393 3.2.3. LIDAR based advanced control

Reduction in LCOE of FOWT may be achieved through enhanced structural performance 394 against incident loads. For this purpose, we have discussed several feedback controllers. One 395 major drawback is that these control mechanisms are designed to respond to the incident impact 396 after its interaction with the system structure. For FOWT, wind turbine structure experiences the 397 incoming wind and wave and feedback control system is activated after the interaction of incoming 398 wind and waves with the system. Such interaction may degrade the structural life over a period 399 of time. Thus traditional controllers may not achieve extended structural life and would increase 400 LCOE subsequently. 401

To circumvent the shortcomings of feedback controllers, the researchers may use feedforward 402 control loops to deal with the incident disturbances before contacting the wind turbine. LIDAR is 403 used to measure the incoming wind disturbance. There have been numerous attempts made to use 404 LIDAR for fixed-bottom wind turbines. [66–68], LIDAR is based on Doppler's principle, where a 405 laser beam is spread out which upon reflection is received [69]. The wavelength of the transmitted 406 and received beam is used to estimate the incoming wind speed. Two types of LIDARs are available 407 based on the wind speed calculation methods, i.e., continuous and pulsed wave. The continuous 408 wave LIDAR uses a laser beam focused at the focal point while the pulsed wave LIDAR calculates 409

<sup>410</sup> wind speed at multiple distances [66].

Unlike fixed-bottom wind turbines, preview-based LIDAR assisted control for FOWT is still 411 under development. An extended version of feedforward collective blade pitch control, initially used 412 for fixed-bottom wind turbines in [70], was designed for FOWT using H-infinity control synthesis 413 by S.T. Navalkar et al. [28]. Based on the combination feedforward-feedback newly formulated 414 CBPC was found useful at minimizing the loads and generator speed oscillations. D. Schlipf et al. 415 [29] designed a CBP-feedforward controller for FOWTs based on LIDAR data. The feedforward 416 control was designed using a simplified non-linear model for ideal wind preview and used along with 417 the traditional feedback controller designed by Jonkman et al. [56]. Later, the design procedure 418 was followed by using nacelle-based LIDAR information instead of ideal preview wind. With the 419 addition of wind uncertainty, a realistic feedforward controller proved useful compared with the 420 standalone baseline controller to minimize rotor speed and power fluctuation and reduce blade, 421 rotor shaft, and tower loads, respectively. 422

### 423 3.2.4. Structural control

There is another approach reported in the literature to minimize the structure loadings, and 424 external influences called structural control (SC). In this methodology, extra DOFs are introduced 425 to influence the structural behavior of the system. This methodology has been vastly used to 426 minimize the oscillations and vibrations of mechanical structure efficiently, and systems [71-74]. 427 For FOWTs, the aim of using the SC is to damp the platform oscillations and tower loading. The 428 critical advantage of the SC for the FOWT is observed while operating in region 3. Blade pitch 429 mechanism is not required to regulate the platform stability, a significant issue observed in region 3, 430 and SC addresses the platform's pitching phenomenon. The SC is based on passive, semi-active, and 431 active control approaches [75]. Passive structural control systems use a set of constant parameters 432 to damp the oscillations. Whereas, the semi-active controllers are mainly tunable over a period of 433 time. Contrary to the passive control approach, active structural control differs based on generating 434 the restoring force with dedicated actuators to address the structure loading and oscillation. 435

Passive and active structural control schemes based on two independent Tuned Mass Dampers
(TMDs) to deal with the loading and damp the platform oscillation were designed by M. Lackner
et al. [30]. These TMDs were placed in the nacelle of a floating barge, operating in region 2 and
3. M. Lackner et al. [30] modified the baseline wind turbine [15] by integrating TMD systems

and incorporating passive, semi-active active structural control synthesis. Based on input-output 440 data, a high order design model is created using system identification. The control synthesis is 441 achieved based on the loop shaping mechanism. It was observed that both techniques reduced wind 442 turbine loadings when compared with the baseline wind turbine. On the other hand, the complexity 443 and overall cost were increased due to the addition of TMDs. Moreover, active structural control 444 outperformed in reducing the tower's fore-aft fatigue load at the expense of energy consumption, 445 which may be obtained from the high wind while operating in region 3. However, in region 2, 446 active structural control proved costly, and for this purpose, a hybrid mass damper (HMD) was 447 incorporated to work as passive TMD while operating in region 2. 448

<sup>449</sup> Nacelle-based TMD system used Lackner et al. [30] is redesigned by Namik et al. [31]to <sup>450</sup> examine the impact of actuator dynamics on TMDs. Load reduction and power consumption were <sup>451</sup> also investigated for the passive and active control strategies on a barge platform-based FOWT. <sup>452</sup> Although the newly designed controllers followed the simulation trends as shown by Lackner et al. <sup>453</sup> [30] concerning load reduction, the redesigned TMD system achieved platform pitch minimization <sup>454</sup> by consuming relatively less average power.

Simplified models of the Mono-pile, Barge, Hywind Spar-buoy, and TLP were used to design an optimal passive TMD based on genetic algorithm by Stewart et al. [32]. This TMD was found to reduce the side-to-side tower fatigue load, which is one of the main components of fatigue loads of FOWTs, better for barge and mono-pile than the TLP and Spar buoy platforms.

A Semi-active TMD placed in the nacelle of a wind turbine was used to minimize the incident 459 loads for two platforms: a fixed bottom mono-pile and a TLP, while operating in region 2 and 3 460 [33]. The designed semi-active TMD has a low power energy source, and it swiftly switches between 461 active and passive modes. This mechanism minimizes the side-to-side tower loading of mono-pile 462 and slackline incidents regarding TLP. A platform-based TMD for barge platform FOWT is used 463 to minimize the platform motions and tower loading while operating in region 2, and 3 [76]. A 464 simple static output-feedback mechanism was proposed to generate the stroke, using generalized 465  $H\infty$  control. Input-output linear model was obtained using system identification. Improved results 466 were obtained in terms of fatigue load and generator power error reduction, while upon comparison, 467 the generalized  $H\infty$  control overperforms  $H\infty$  structural control. Similarly, a Multi-layered Tuned 468 liquid damper (TLD) was developed in [77] for a spar-buoy floating platform and was found useful 469 to minimize platform motions. 470

The traditional passive TMD system's performance was improved by introducing an inerter in 471 the system [78]. The proposed TMD system was placed in the nacelle of the FOWT attached to 472 a barge. The improvement was evaluated in the presence of real incident disturbances, waves and 473 wind. This novel extension of the TMD was found helpful in reducing tower loading. In a relatively 474 similar approach, a STAM (sewing thread artificial muscle) based on thermal actuation attached to 475 mooring lines of the TLP platform was proposed to minimize platform pitching and tower loading 476 for regions 2 and 3 [79]. The active mooring method showed improved results regarding tower 477 loading and pitching motions. 478

#### 479 4. Wind and wave forecast algorithms for FOWT control

Incident disturbance forecast is an essential feature of advanced control algorithms like predictive 480 model control and feedforward control. Unlike feedback control, where the controller responds to 481 the disturbance after the system interacts with it, feedforward controllers react to the preview of 482 incoming disturbance ahead of its contact with the system. This approach elevates the performance 483 because the incident disturbance preview provides the controller enough time to respond to the 484 incoming disturbance and adjust parameters to achieve control objectives. Preview-enabled control 485 also enhances the system's structural life as it responds to the incident disturbances ahead of its 486 contact with the system structure. 487

FOWTs are exposed to incident wind and wave disturbance operating in the deep sea. A lot of 488 controllers are designed to stabilize the platform and achieve the control objectives by minimizing 489 the effects of wind and wave disturbances. However, the performance and structural life of FOWTs 490 is still lagging behind when compared with the fixed bottom offshore wind turbines, as most of these 491 control systems are feedback control systems. The incident wind and wave prediction may effectively 492 improve the performance, loading, and structural life of FOWTs with the help of advanced control 493 algorithms like MPC or feedforward control, as proven by the LIDAR based incident wind preview 494 enabled feedforward controllers [29]. 495

There are several forecast techniques for wind and wave are reported in the literature, which could be used for preview-based advanced controllers. However, there are issues concerning the prediction horizon length and the forecast quality are to be considered when using these prediction mechanisms. In this section, wind and wave forecast algorithms are discussed.

#### 500 4.1. Wind forecast

The wind turbine industry extensively employs the wind forecast to examine a region's seasonal 501 power production, grid integration, and wind farm design [80]. Based on its application, the length 502 of the prediction horizon of wind forecast ranges from few hours to months, namely; short, medium, 503 and long-term. However, the prediction horizon length for individual wind turbine control systems 504 based on preview information is few seconds. Advanced controllers such as feedforward control 505 require a preview time of a few seconds [51]. Similarly, MPC uses a 5-10s long horizon to compute 506 the input values for system response [52]. Therefore the scope of this paper is limited to the wind 507 forecast for wind turbine control, referred to as ultrashort wind forecast in this paper. An overview 508 of models and devices used for ultra-short wind forecasts is provided below. 509

Statistical time-series models used for wind forecasts are based on the historical site data. Based on the historical wind data, these models tend to learn the underlying patterns in the available data and calculate the future values ahead of time. Widely used conventional statistical models for wind forecast includes autoregressive model (AR) [42, 43], autoregressive moving average model (ARMA) [44], autoregressive integral moving average (ARIMA) [45], fractional-ARIMA [46], and Hammerstein auto-regressive (HAR) [47] etc. Statistical methods heavily rely on historical wind data thus may provide faulty wind forecasts in the absence of enough historical site data.

Machine learning (ML) techniques rely on historical data and consider the atmospheric variables 517 that affect the wind speed, such as humidity, elevation, and atmospheric pressure for wind forecast. 518 Therefore, ML methods deal with the nonlinearity of wind better than the statistical methods. ML 519 non-linear prediction methods include artificial neural networks (ANNs) [81, 82], recurrent neural 520 networks (RNN) [83], support vector machine (SVM) [84, 85], least-square support vector machine 521 (LSSVM) [86, 87], Gaussian process (GP) [88], Bayesian networks [89], and extreme learning ma-522 chine (ELM) [90]. Overfitting and minimum local existence are major drawbacks of ANNs [91]. 523 Whereas ELM is proven to have better performance than conventional ANNs and is used for both 524 speed estimation and power forecasting [90, 92, 93]. Hybrid models, a combination of existing 525 model techniques, are also reported in the literature for improved performance. For example, A 526 linear ARIMA and a non-linear ANN are used in a combination for improved wind forecast [94]. 527 Similarly, a combination of ELM and ARIMA is shown to have enhanced performance for wind 528 forecast [95]. 529

LIDAR is used in the wind turbine industry for several applications such as wind power es-

timation and site analysis [96]. They are also used to provide the preview of incident wind for an ultrashort scale horizon upstream of the wind turbine. Wind speed is calculated based on the reflected lasers from the incoming wind particles emitted from LIDAR. Preview measurement of incoming wind speed for FOWT control is discussed in Section 3]. LIDAR-based forecasting techniques are reported to outperform forecasting techniques like ARIMA and persistent methods [97, 98]. However, the higher cost and weather-dependent performance are challenges yet to be further researched.

#### 538 4.2. Wave forecast

Incident wave accounts for a significant part of FOWT loads when minimizing the platform motions. Therefore, it is also an essential feature to be considered alongside the incident wind in the preview-based FOWT control. Feedforward controllers based on the wind and wave preview may improve the FOWTs loading and platform stability compared to feedback controllers by providing the system enough time to deal with the incoming disturbances. Many wave forecast methods are reported in the literature, such as physics-based models, statistical models, and machine learning models. A discussion on these models is given below.

Physics-based models are numerically designed models that solve the complexity of waves based 546 on the physics behind wave mechanics. Physics-based wave forecast models include WAVEWATCH 547 III (WW3) [99], European Center for Medium-range Weather Forecasts (ECMWF) [100], and 548 SWAN (Simulating Waves Nearshore) [101]. These models are generally used for long-term pre-549 diction horizons over an extensive area. In contrast to the physics-based theory-driven models, 550 data-driven statistical and machine learning provide accurate predictions based on the historical 551 site data. These time-series algorithms extrapolate the past values to provide future wave predic-552 tions. Statical wave prediction models for wave prediction reported in the literature includes AR, 553 ARMA, ARIMA [48–50]. As compared to statistical models, machine learning prediction models 554 provide improved nonlinear trends identifications in time series wave data. ANN, RNN, CNN, and 555 ANFIS based prediction models [102–106] are some of the examples of machine learning models 556 used for wave prediction in the literature. A comparison of time series-based models and physics-557 based model (ECMWF) at multiple sites highlights the weakness and strengths of these models 558 [107]. Physics based model performs better for longer prediction horizons, whereas the time series 559 models are better for a shorter prediction horizon. Combinations of physics-based and data-driven 560

statistical models are also reported in the literature [108, 109].

# 562 5. Discussion

FOWT technology is still in the pre-commercial phase as compared to the fixed-bottom offshore wind turbines. The primary concern of FOWT development is the associated cost of energy production and the potential to achieve a cost-effective advantage compared to the fixed-bottom, which is deteriorated by the floating base of FOWT. However, an efficient control mechanism may deal with the shortcoming of the platform, making it economically feasible. These control methods aim to lower LCOE while operating the region below and above the rated wind speed, making it economically feasible. Several control schemes are recently developed for this purpose.

## 570 5.1. Comparison between traditional SISO and advanced controllers

The conventional SISO feedback controllers are a natural choice for FOWTs by manipulating 571 the aerodynamic wind load using blade pitch angle and generator torque. Its simple design and 572 easy realization make them a suitable option for fixed-bottom wind turbines. However, the floating 573 platform's natural frequency is lower than the fixed-bottom wind turbines foundation, which causes 574 negative platform damping operating in region III [14]. Controllers designed for fixed-bottom wind 575 turbines may increase the negative platform damping when used for FOWT. Several SISO control 576 strategies are reported in the literature to deal with this issue: refer to Table 1 for details. For 577 example, negative platform damping is addressed by reducing control bandwidth; however, power 578 and speed variations were observed [14]. B. Skaare et al. [17] came up with wind speed estimator-579 based blade pitch control to deal with the platform's floating motions. Improvement in terms 580 of platform motion damping was achieved at the cost of rotor speed and power output deviation. 581 Jonkman et al. [15] utilized Gain scheduled SISO controller with detuned gains to deal with negative 582 platform damping on a barge platform. However, achieved performance is likely to increase using 583 MIMO controllers, suggested by Jonkman et al. [15]. The coupling between the unmodelled DOF 584 and SISO control loops of FOWT causes inadequate platform motion minimization, power and 585 rotor speed regulation. 586

<sup>587</sup> On the other hand, advanced MIMO controllers can deal with cross-coupling between the un-<sup>588</sup> modeled DOF and control loops better than SISO controllers. These controllers are based on the

linearized system model and exhibit superior performance compared with the baseline SISO con-589 troller. The conflicting blade pitch commands for the platform and rotor regulation are dealt with 590 Individual blade pitch control (IBPC) by creating asymmetric rotor load. However, the platform 591 properties affect the performance of MIMO controllers, as shown in the Table 4. For example, the 592 Barge platform is prone to increased loads due to the inherent platform motion inducing incident 593 waves. MIMO control based on Individual blade pitch control (IBPC) used for barge results in 594 lowered tower loads and platform motion. However, the rotor and power regulation are at a similar 595 level compared to the baseline controller. The reduction in loads is due to increased blade pitch 596 activity. DAC is seen to have no further improvement as it is mainly responsible for lowering the 597 wind disturbances, and the barge platform is mainly affected by incident wave load [22]. Due to its 598 lowered pitch frequency, the Spar-buoy platform is observed to have a slight improvement in the 599 use of IBP based MIMO control compared to other platforms. DAC control effectively reduced the 600 wind disturbance for Spar-buoy, thus leading to better rotor regulation. However, DAC negatively 601 affects the platform motions based on the increased blade pitch activity [21] For the case of TLP, 602 the platform is less affected by the incident waves. IBPC improves the tower loads and platform 603 motions. A significant improvement is observed in the rotor and power regulation which may be 604 attributed to the platform's inherent stability due to tensioned mooring lines. Subsequently, the 605 DAC controller incurs additional improvement by reducing incoming wind disturbance [22]. 606

Most of the MIMO controllers for FOWTs are designed around a single operating point. The controller performs well around the operating point; however, moving away from the operating point may lead to performance degradation. To overcome this obstacle, a gain-scheduled controller based on a series of linearized models on a range of operating points improves power regulation and platform motions. LPV controllers offer another switching mechanism to incorporate multiple linear models for a range of operations and deal with the limitation of linearized MIMO models that are only valid around linearization points.

Advanced controllers like MPC controllers improve performance while dealing with uncertainties and unmodeled system dynamics. Based on preview wind and wind measurements, MPC corrects the control trajectory based on the plant model at every step. It also allows designers to include the constraints on inputs and states in control design, thus effectively avoiding physical saturations. However, MPC is a computationally demanding control mechanism for complex systems like FOWTs. Advanced controllers based on preview information of incident disturbance are superior

alternatives to feedback controllers. LIDAR is a valuable addition to improving fixed-bottom wind 620 turbines; however, LIDAR performance is yet to be evaluated for FOWTs are exposed to wave 621 disturbances. Details of advanced MIMO controllers is provided in Table 2. 622

Structural controllers based on TMDs adequately reduce the pitching phenomena and reduce 623 the wind turbine loads, mainly operating in region 3. Controllers we have discussed until now are 624 mainly based on blade pitch mechanism control. However, structural controllers include additional 625 DOF that deals with platform motions and tower loading. This way, controller mechanisms ease the 626 high blade pitch activity and provide a further performance improvement. However, the addition 627 of TMDs causes an increase in the complexity of the FOWTs. Moreover, the power required to 628 generate a heavy stroke in active dampers requires further investigation regarding cost-effectiveness 629 on an industrial scale. List of existing structural controllers is provided in Table 3. 630

Table	1:	Traditional	control	methods

Method	Model	Platform	Description	Economic viability	OF
CBP- GSPI [14]	HAWC2/ SIMO -	Spar-buoy	Region-dependent control based on	Improved tower stability. however,	2,3
	RIFLEX	(Hywind)	simple switching process, pitching	degraded power quality and poor	
			controller of frequency lower than	rotor speed regulation.	
			the platform pitching frequency is		
			employed for region 3.		
CBP-GSPI [15, 57]	FAST	Barge, TLP,	Feedback loop based on Tower-	Only detuned gains control im-	2,3
		Spar - buoy	top movement,pitch-to-stall regula-	proves the negative damping issue.	
			tion and detuned gains.	Further use of MIMO control is sug-	
				gested including IBPC.	
Simple Platform Pitch	FAST	Barge	Platform pitch velocity based gener-	Reduced negative damping and	3
Control [16]			ator speed control in region 3. Also	blade pitch activity at the cost of	
			used IBPC.	the rotor speed fluctuations and	
				power variation. IBPC showed in-	
				adequate load reduction.	
Control based on esti-	HAWC2/ SIMO -	Spar-buoy	Estimator based control mechanism.	Tower Loading, nacelle oscillation	3
mated wind speed [17]	RIFLEX	(Hywind)		and rotor loads are found reduced.	
				However, poor rotor speed regula-	
				tion and reduced power generated	
				are observed.	

5.2. Impact of the platform on the controllers performance 633

So far, we have discussed a range of controllers designed for FOWTs for their pros and cons. 634 SISO and advanced MIMO controllers are incorporated to deal with shortcomings associated with 635 the platform motions. However controller performance may vary based on the type of platform 636 used for the operation. We have compared several advanced controllers based on the utilized 637 platform type and their performance in Table 4. Comparison is made in terms of improvement 638

in tower loading, power regulation and platform motions damping to give readers an overview of 639 how control performance may vary based on different platform types. Controllers for the barge 640 platform improved tower loadings and platform motions; however, they perform poorly in terms 641 of power regulations. The TLP platform has inherent stability over its counterpart platforms thus 642 we see improvement compared to the barge platform. MIMO controller based on the IBPC with 643 an extension of DAC ranks higher because it manages to minimize the incident wind disturbance 644 better for the TLP than the barge. Due to lower platform frequency, the spar-buoy platform may 645 not perform well enough, although it has better power regulation, which is mainly due to increased 646 blade pitch activity. However, advanced controllers like MPC and preview-enabled feed-forward 647 controllers exhibit superior performance, especially for the case of power regulations. MPC has a 648 higher ranking also due to the ability to deal with the input and system state constraints. 649

#### 650 6. Summary

The control mechanisms we have discussed are all based on model-based design. In complex 651 systems like FOWTs, accurate system modeling is essential for dealing with model uncertainties 652 and complex incident disturbances – wind and wave. In an ideal situation, the plant represents the 653 actual systems and actuators, whereas, in reality, it is a fair approximation of the system. There are 654 expected errors that may result from a poor understanding of the system and un-modeled dynamics, 655 leading to a compromise of system performance. In this case, the model-free control approach may 656 be utilized to represent the plant model and deal with the shortcomings not addressed by first-657 principle mathematical modeling. Input-output data may be used to deduce a plant representation 658 for the respective controller design after careful assessment and performance evolution. Unlike the 659 model-based design, the data-driven model-free controllers don't rely on the system characteristics, 660 eliminating the need for controller dependency on the plant model. Furthermore, unlike the model-661 based control approach, in the model-free methodology, the system stability is not relying on the 662 model accuracy [110]. Machine learning techniques may address this issue by finding the optimal 663 control laws by mapping the sensor's output to control actuators. These techniques are based on 664 bio-inspired computational methods, including Genetic Algorithm and Reinforcement and Iterative 665 learning [111]. These algorithms may be used to minimized constraint-based cost functions designed 666 according to the control objectives. One such example of MLC usage for complex structures like 667 FOWTs is reported in the literature [112]. Input-output data is correlated to for a control law 668

u = k(y) and evaluated using a cost function J, as shown in schematic Figure 9. It shows improved performance compared to the baseline controller and demonstrates a viable solution for further research for complex control synthesis for FOWTs.

Control methods	Model	Platform	Description	Economic viability	OR
MIMO-CBP [20]	FAST	Barge	CBP based Rotor thrust is used to regulate platform pitch and rotor speed.	Poor power and rotor regu- lation compared with baseline controller. Improved tower	3
MIMO-IBPC [20– 22]	FAST	Barge, TLP, Spar-Buoy	Asymmetric rotor aerodynamic load is used to regulate the platform pitch and rotor speed.	loading, platform motions. Tower loads are decreased for the barge, however poor rotor and power regulation. TLP, compared to the Barge and spar-buoy, exhibits less plat- form movement when IBPC. Due to the lower natural plat- form frequency, IBPC on Spar- buoy is not useful regardless of the improved rotor regulation	3
IBPC-DAC [21, 22]	FAST	Barge, TLP, Spar-Buoy	DAC is used as an extension of IBPC with an additional wind disturbance rejection.	the improved rotor regulation. DAC has no further improve- ment on the barge compared to the IBPC applied on a barge. Whereas, when it is utilized on TLP, power and speed regula- tion are improved with a reduc- tion in side-to-side loads. DAC used on spar-buoy improves ro- tor speed but increases the blade pitch activity and loads.	3
MIMO (LQR) [23]	DTU- 10MW	Spar-Buoy Triple Spar	Effects of the control inputs are analyzed based on how they af- fects the output for a floating wind turbine in an open loop scenario and an LQR based on observations is synthesized.	Damped various resonances, but observed not being able to suppress the wave excitations entirely.	3
GS-Output feed- back H∞ [18]	FAST	Barge	Generator speed is regulated at the rated value using a gain scheduled controller to keep drive train and tower oscilla- tions low.	Improvements in platform stability and reduced fatigue loads, LPV based GS con- troller is suggested for further improvements.	3
LPV and LQR based GS [19]	FAST	Barge	GS-LPV and GS-LQR based on output feedback and state feedback are employed.	Improved power regulation and platform pitch minimization is achieved.	3

Table 2:	Advanced	$\operatorname{control}$	methods	
----------	----------	--------------------------	---------	--

SMC and IOFL [24]	FAST	Barge	Methods based on LPV control are implemented; to regulate generator speed, and to ana- lyze the effects of incident dis- turbance on platform motions.	SMC is found to have achieved generator speed regulation bet- ter than IOFL for simplified wind turbine models and per- formance degraded when com- plex wind turbine models are	3
NMPC (CBP) [25]	Sand- ner Model	Spar-buoy	NMPC based on CBP mecha- nism and generator torque is employed.	utilized. Enhanced performance in terms of rotor regulation, platform motion minimization and improved loads. However, the computational cost is significantly higher.	3
N-MPC (IBP) [26]	Sand- ner Model	Spar-buoy	IBP mechanism is extended based on the collective blade pitch approach.	Lowered pitch and yaw mo- tion, improved speed regula- tion and reduction of the loads	3
Linear - MPC (CBP) [27]		Modified Spar	Linear-MPC based MIMO sys- tem is deigned using CBC ap-	on blades. Speed and generated power regulation. Improved negative	2,3
LIDAR (FF- CBPC) [28]		TLP	proach. Feed-forward controller based on CBP mechanism is intro- duced for wind speed regula-	platform pitch motions. Improved speed regulation and minimized the loads.	3
LIDAR (FF- CBPC) [29]	FAST	Spar-buoy	tion. CBP FF controller is formu- lated based on ideal wind speed estimation.	Improved rotor speed and power regulation, along with blades, rotor, and tower load reductions.	3

The complex nature of incoming wind and wave limits the control design for FOWTs. Instanta-672 neous changes in these disturbances, such as wind and wave gusts, may affect the control systems' 673 design for FOWTs. Moreover, if not considered, these flows' stochastic nature may also degrade the 674 structural life and performance of wind turbines. Incoming disturbances may be modeled to circum-675 vent these issues. However, it is challenging to design perfect mathematical models of incident wind 676 and wave due to the inherent complicated properties and high dimensions. Data-driven machine 677 learning plays a promising role in solving complex real-life problems. Dynamic Mode Decomposition 678 (DMD) [113], Sparse Identification of Non-linear Dynamics (SINDy) [114], and Koopman Operator 679 Theory [115] are some of the data-driven methods that may be used to understand complex tur-680 bulent flows and interpret the underlying behaviors. Simplified models of the incident disturbance 681 - wind and wave - may improve the incoming disturbance prediction and estimation process based 682 on these techniques. The LCOE of large FOWT can be reduced by better understanding the effect 683

<sup>684</sup> of incident disturbances on FOWT and subsequent efficient control design.

In this review paper, we have reviewed a range of control mechanisms listed in the literature to deal with the shortcomings of FOWT associated with floating platform. SISO and MIMO controllers are discussed based on their improvements in the control objectives of FOWT. structural controllers are analyzed for their unique way of dealing with FOWT loadings. The possibility of utilizing forecasting techniques and model-free control is drawn as well.

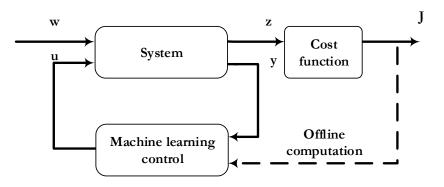


Figure 9: Machine learning control

	Control methods	Model	Platform	Description	Economic viability	OR
	Active and passive	FAST-	Barge/ Fixed	TMD placed in the nacelle,	Reduced tower loading, In-	$^{2,3}$
	TMD [30]	$\mathbf{SC}$	bottom	$\mathrm{H}\infty$ based loop shaping con-	creased complexity and power	
			monopole	trollers.	consumption due to active-	
					TMDs.	
	Improved Active	FAST-	Barge	Nacelle based redesigned	Fore-aft loads reduction and	$^{2,3}$
	and passive TMD	$\mathbf{SC}$		TMDs taking actuator model	tower base bending minimiza-	
	[31]			into consideration.	tion.	
	Optimal Passive	FAST-	Mono-pile,	Optimal passive TMD is de-	Fatigue loads are found re-	$^{2,3}$
	TMD [32]	$\mathbf{SC}$	barge , Hywind	veloped based on available	duced for barge and mono-	
			spar-buoy and	platforms using genetic algo-	pile better than the TLP and	
			TLP	rithm.	Spar buoy.	
	Semi active TMD	FAST-	Mono-pile and	Nacelle based semi-active	Minimized side-to-side tower	$^{2,3}$
690	[33]	Or-	TLP (Pelastar)	TMD.	loading of mono-pile and	
		caflex			slackline incidents of TLP.	
	Active TMD [76]	FAST-	Barge	Platform-based TMD, A	Fatigue load and generator	$^{2,3}$
		$\mathbf{SC}$		static output-feedback mech-	power error is reduced while	
				anism is proposed using a	reliability and robustness is-	
				generalized ${\rm H}\infty$ control	sues of controller designed are	
					found.	
	TLD [77]	Nu-	Spar-buoy	Nacelle based single and mul-	Enhanced platform pitching	-
		merical		tilayer TLDs are examined	motion based on Multilayer	
		meth-		and validated.	TLD than single layer TLD.	
		ods	D			
	Passive TMD [78]	FAST-	Barge	TMD placed in nacelle, In-	Effectively reduced wind and	2
		$\mathbf{SC}$		erter based damping mecha-	wave induced loads in com-	
				nism.	parison with similar tradi-	
	Active Mooring	FAST	TLP	STAM-integrated mooring	tional TMD control. Platform motions (pitch and	$^{2,3}$
	line control based			lines.	roll) and tower bending mo-	
	on STAM [79]				ment, are minimized.	
	<b>T</b> 1 11/2			1.6 11 1 1 1		

#### Table 3: Structural control methods

691

The different aspects of FOWTs reviewed for controller design lay a foundation for future work with the following recommendations: 692

• Most of the research on the control design concerns the wind disturbance and neglects the 693 wave disturbance. It may be advantageous to include the wave information in the control 694 design and the wind disturbance to improve performance further. 695

• Structural controllers may be further investigated as a viable solution for pitching phenomena 696 and wind turbine loading. Its ability to minimize the platform pitching phenomena without 697 using blade pitch can give designers more freedom to design controllers. However, a cost-698 effective approach and subsequent validation studies are needed. 699

		Tower Loads	Power regulation	Platform motions	$\operatorname{Cost}$
	IBPC	3	1	3	2
Barge	IBPC- DAC	3	1	3	2
TLP	IBPC	2	3	3	3
1 LF	IBPC- DAC	2	4	4	5
	IBPC	2	3	3	3
	IBPC- DAC	2	4	2	3
Spar-buoy	FF-CB	2	5	2	4
	NMPC-CBP	2	5	3	5
	NMPC-IBPC	2	5	3	5
5 = Massive improvement					
4 = Major improvement					
2 Min on improvement					

Table 4: Performance comparison of MIMO control schemes compared to baseline controller

3= Minor improvement

2 = Slight improvement

1 =Decrease in performance

• The effectiveness of the LIDAR for FOWTs needs to be experimentally validated. Moreover, a device capable of sensing waves similar to LIDAR may help designers include wave preview information alongside wind preview in advanced control mechanisms like MPC.

Further development is suggested in the use of prediction algorithms together with advanced controllers. Developing models based on machine learning tools would be of significant advanced vantage, especially in understanding the underlying behaviors and designing optimal control laws.

# 707 7. Acknowledgment

The authors would like to thank Dr. Xiaoni Wu, and Dr. Zeeshan Qaiser for constructive feedback. This work was supported by the National Natural Science Foundation of China [grant no. 51761135012].

#### <sup>711</sup> Appendix A. Simulation codes and models for FOWTs

The existing system models designed for the fixed-bottom WTs may not be able to reflect the performance of FOWTs. It is mainly due to the moving base of FOWTs and associated motions. Therefore, a system model is required to analyze the FOWTs that incorporates all the significant DOFs, including the floating base. A brief description of some of the major simulation codes used is given below.

### 717 Fatigue, Aerodynamics, Structures, and Turbulence (FAST)

The National Renewable Energy Lab (NREL) has designed a modular computer-aided engineer-718 ing (CAE) open-source software testFatigue, Aerodynamics, Structures, and Turbulence (FAST) to 719 simulate WTs at the desired operating conditions [116]. The FAST code may be used to model WTs 720 by inflow wind, structural dynamics, aerodynamics, and for the case of offshore scenario, mooring 721 line dynamics, hydrodynamics, etc. [117]. FAST uses a Multi-body/modal system (MB/Mod) rep-722 resentation. The aerodynamics module is based on the Blade element momentum (BEM) theory 723 (quasi-static). At the same time, the hydrodyn modules offer modeling based on Potential flow 724 (PF) and Morison's equation (ME). Furthermore, models based on FAST can generate linearized 725 models useful for the linear control design. 726

A standard multi-megawatt fictitious model of a FOWT is designed based on FAST to assist the development of FOWTs, named NREL 5MW baseline WT [56]. This utility-scale WT is developed based on the publicly available data of existing WTs and simulation models such as WindPACT [118], RECOFF [119], and DOWEC [120].

# 731 Horizontal Axis Wind Turbine Code-Second generation (HAWC2)

Horizontal Axis Wind Turbine Code-Second generation (HAWC2) is a time-domain commercially available code that is mainly used to study the dynamics of fixed bottom WTs operating under externals loads [121]. The structural dynamics is based on MBS, whereas the aerodynamic module relies on BEM theory. The WT with a floating base is simulated using the SIMO/RIFLEX code coupled with HAWC2 [55], where SIMO/RIFLEX is used to model the floating foundation and mooring lines, whereas the rotor, blades, and nacelle are designed in HAWC2.

A next-generation 10 MW reference WT based on HAWC2 [122] similar to 5 MW baseline WT
[56] is also available for the research and development. It was originally designed for the project
INNWIND.EU [123].

### 741 Bladed

Bladed is a commercial software to simulate WTs for both onshore and offshore sites [124]. The FOWTs may be modeled using Bladed by considering the dynamics and the complexity of the system parameters. Bladed code also considers incident wave and wind loads, structural dynamics, aerodynamics, and suitable controller response.

The structural dynamics of the Bladed code are based on the multi-body modal (ModMB) sys-746 tem representation. The aerodynamic module uses both the momentum and blade element model. 747 Simultaneously, an extended version of this model is used to consider models such as Prandtl's tip 748 and root losses, dynamic wake models, and Glauert skew wake model. The hydrodynamic module 749 utilizes the penal method and Morison equation. With a built-in Light detection and ranging (LI-750 DAR) module, Bladed code may be used to develop advanced control designs based on the LIDAR 751 preview information. The Bladed code can generate the linearized model and state-space matrices, 752 an essential part of linear control theory. 753

As a part of LEANWIND project [125] an 8 MW reference WT [126] is designed based on data available online of WTs and validated using Bladed.

# 756 SIMPACK

SIMPACK code is designed to simulate a range of industrial applications such as robotics, automotive aerospace, and railway [127]. It a general-purpose software based on MBS and is applicable for the WTs as well. An extension to the existing code is used for FOWT, connecting HydroDyn and SIMPACK with the help of SIMHydroDyn [128]. These additional modules are to deal with the hydrodynamics and the mooring lines of FOWTs.

A comparison of the parameters and properties of the 5 MW, 8 MW and 10 MW reference wind turbines is given in Table Appendix A1.

764

Table Appendix A1: Summary of 5, 8 and 10 MW reference wind turbines

	Turbine Name	NREL (5MW)	LEANWIND (8MW)	DTU $(10MW)$
765	Number of blades and rotor orientation	3 blades, Upwind	3 blades, Upwind	3 blades, Upwind
	Rotor Diameter (meters)	126	164	178.3
	Tower and Hub height (meters)	90, 87.6	110, 106.3	119,115.6
	Cut in, cut out and rated wind speed $(\mathrm{m/s})$	3, 25, 11.4	4, 25, 12.5	4, 25, 11.4
	Rotor speed range (rpm)	6.9, 12.1	6.3, 10.5	6, 9.6
	Hub Nacelle and blade mass (tons)	56.8, 240, 17.7	90, 285, 35	105.5,  446,  41.7

766 Simplified models

To minimize external disturbances, achieve platform stability, and improved power quality, com-767 plex simulation codes like FAST are considered an appropriate choice. However, the complex nature 768 of these models may cause problems in the control design process. To circumvent shortcomings as-769 sociated with the complex models, a simple yet accurate model can be developed to model the 770 essential dynamics and behavior of a FOWT with high accuracy. The effectiveness of simplified 771 models for FOWTs in designing useful controllers has been proven [129]. To facilitate the sim-772 ple control design process, researchers have produced simplified FOWT models. Below are a few 773 noticeable models available in the literature. 774

## 775 Betti model

To address the complexity of the existing simulation models for the FOWTs, a simplistic control-776 oriented 2-D rigid model is proposed by Betti et al. [130]. Betti model is designed with 7 states, 777 whereas incident wind and wave disturbances are considered acting in 2-D plane. The schematic 778 of this model is given in Figure Appendix A1. This model may also generate linearized models at 779 various locations within the operating range. Unlike FAST, this model may also be used to calculate 780 the wave disturbance matrix, which provides the incident wave information into the advanced 781 control design process. The Betti model is used for the controller synthesis on a TLP based 5 MW 782 FOWT considering 2-D incident disturbances. However, it was found that the model had a small 783 effect on the platform motions and generated power despite the accurate 2-D motion representation 784 [129, 130].785

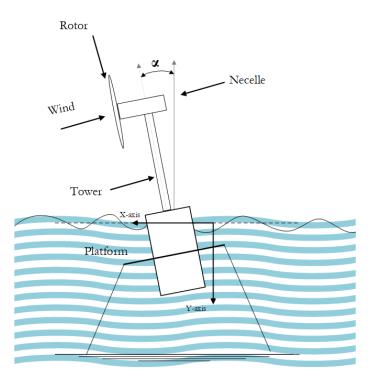


Figure Appendix A1: Adapted layout of Betti model [129]

## 786 Sander Model

Sandner et al. [65] designed a less-complex FOWT model for a spar buoy platform as shown 787 in Figure Appendix A2. The DOFs of this model includes platform motion, rotor speed, nacelle 788 movement, and pitching angle of the blades. The Sander model has a 2-D structure similar to Betti 789 model [130] and it's performance is found accurate when compared with the complex FAST model. 790 However, Sander model may not be used to study FOWT based on other platforms because it is 791 designed for a spar boy platform, where there is less hydrodynamics involved due to its unique 792 geometry. Moreover, Sandner model is only used for the 2-D disturbances, and its effectiveness in 793 a 3-D scenario is yet to be assessed. 794

## 795 Homer model

Homer et al. [131] proposed a simplified and effective control-oriented 3-D design for advanced control synthesis of a FOWT, as shown in Figure Appendix A3. Like other similar models, the Homer model also has fewer DOFs (15/16), and it may also be used to generate linearized models

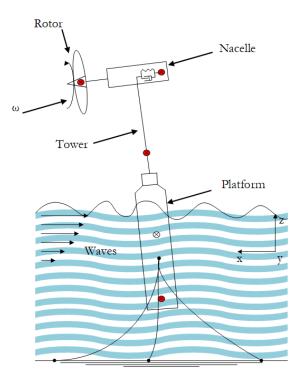


Figure Appendix A2: Adapted layout of Sander model [65]

<sup>799</sup> at a given operating point. The model is capable of reflecting 3-D motion, and assist controller <sup>800</sup> synthesis to eliminate or reduce the effect of wind and wave disturbances. Furthermore, the Homer <sup>801</sup> model also comes with an ability to generate wave disturbance matrix. The simplified models are <sup>802</sup> compared with complex model FAST in terms of their particular characteristics in Table Appendix <sup>803</sup> A2.

804

Table Appendix A2: Model comparison of existing FOWTs controllers

	Model	Nature	DOFs	Incorporates incident wind/wave in controller synthesis
805	Jonkman [116]	Flexible 3-D	22/24	Wind only
	Betti [130]	Rigid 2-D	7	Wind and Wave
	Sandner [65]	Flexible 3-D	18	Wind and Wave
	Homer $[131]$	Rigid 3-D	15/16	Wind and Wave

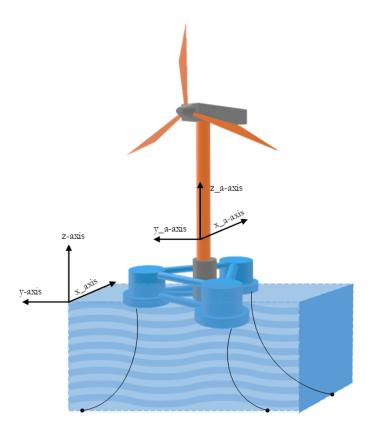


Figure Appendix A3: Adapted layout of Hommer model

## 806 References

- <sup>807</sup> [1] G. W. Statistics, Global wind energy council, Washington, DC, USA.
- <sup>808</sup> [2] U.S. Energy Information Administration, Cost and Performance Characteristics of New Gen-<sup>809</sup> erating Technologies, Annual Energy Outlook 2019 (2019).
- [3] J. K. Kaldellis, M. Kapsali, Shifting towards offshore wind energy—Recent activity and future
   development, Energy Policy 53 (2013) 136–148. doi:http://dx.doi.org/10.1016/j.enpol.
   2012.10.032.
- [4] J. Wang, S. Qin, S. Jin, J. Wu, Estimation methods review and analysis of offshore extreme
   wind speeds and wind energy resources (2015). doi:10.1016/j.rser.2014.09.042.
- [5] Wind Europe, Floating Offshore Wind Vision Statement, Tech. Rep. June (2017).

- <sup>816</sup> [6] IPPC, Global Warming of 1.5 °C (2018).
- URL https://www.ipcc.ch/sr15/
- [7] K. Borch, N.-E. Clausen, G. Ellis, Environmental and social impacts of wind energy, Tech.
   rep. (2014).
- [8] K. Dai, A. Bergot, C. Liang, W. N. Xiang, Z. Huang, Environmental issues associated with
   wind energy A review, Renewable Energy 75 (2015) 911–921. doi:10.1016/j.renene.
   2014.10.074.
- [9] D. Y. Leung, Y. Yang, Wind energy development and its environmental impact: A review,
   Renewable and Sustainable Energy Reviews 16 (1) (2012) 1031–1039. doi:10.1016/j.rser.
   2011.09.024.
- [10] J. Lee, F. Zhao, GWEC Global Wind Report, Tech. rep. (2020).
   URL www.gwec.net
- [11] L. Joyce, Z. Feng, Global Offshore Wind Report 2020, Tech. Rep. August (2020).
   URL https://gwec.net/global-offshore-wind-report-2020/www.gwec.net
- <sup>830</sup> [12] NOAA Ocean Explorer: Types of offshore oil and gas structures.
- URL http://appliedmechanicsreviews.asmedigitalcollection.asme.org/article.
   aspx?doi=10.1115/1.4031175
- [13] A. R. Henderson, D. Witcher, Floating offshore wind energy a review of the current status
   and an assessment of the prospects, Wind Engineering 34 (1) (2010) 1–16. doi:10.1260/
   0309-524X.34.1.1.
- [14] T. J. Larsen, T. D. Hanson, A method to avoid negative damped low frequent tower vibrations
   for a floating, pitch controlled wind turbine, Journal of Physics: Conference Series 75 (1)
   (2007) 012073. doi:10.1088/1742-6596/75/1/012073.
- [15] J. M. Jonkman, Dynamics Modeling and Loads Analysis of an Offshore Floating Wind Tur bine, Ph.D. thesis, National Renewable Energy Laboratory (2007). doi:10.2172/921803.
- [16] M. A. Lackner, Controlling Platform Motions and Reducing Blade Loads for Floating Wind
   Turbines, Wind Engineering 33 (6) (2009) 541–554. doi:10.1260/0309-524X.33.6.541.

- [17] B. Skaare, T. D. Hanson, F. G. Nielsen, Importance of Control Strategies on Fatigue Life of
   Floating Wind Turbines, in: 26th International Conference on Offshore Mechanics and Arctic
   Engineering, San Diego, California, 2007, pp. 1–8.
- [18] T. Bakka, H. R. Karimi, N. A. Duffie, Gain Scheduling for Output H∞ Control of Offshore
   Wind Turbine, in: Twenty-second (2012) International Offshore and Polar Engineering Con ference, Rhodes, Greece, 2012, pp. 496–501.
- [19] O. Bagherieh, R. Nagamune, Gain-scheduling control of a floating offshore wind turbine
   above rated wind speed, Control Theory and Technology 13 (2) (2015) 160–172. doi:10.
   1007/s11768-015-4152-0.
- [20] H. Namik and K. Stol, Individual blade pitch control of floating offshore wind turbines, Wind
   Energy 13 (1) (2010) 74–85.
- [21] H. Namik, K. Stol, Individual blade pitch control of a spar-buoy floating wind turbine, IEEE
   Transactions on Control Systems Technology 22 (1) (2014) 214–223. doi:10.1109/TCST.
   2013.2251636.
- [22] H. Namik, K. Stol, Performance analysis of individual blade pitch control of offshore wind
   turbines on two floating platforms, Mechatronics 21 (4) (2011) 691-703. doi:10.1016/j.
   mechatronics.2010.12.003.
- [23] F. Lemmer, D. Schlipf, P. W. Cheng, Control design methods for floating wind turbines for
   optimal disturbance rejection, in: Journal of Physics: Conference Series, Vol. 753, 2016, p.
   092006. doi:10.1088/1742-6596/753/9/092006.
- [24] O. Bagherieh, K. Hedrick, R. Horowitz, Nonlinear Control of Floating Offshore Wind Turbines
   Using Input/Output Feedback Linearization and Sliding Control, in: Asme Dynamic Systems
   & Control Conference, 2014, p. 10.
- [25] D. Schlipf, F. Sandner, S. Raach, D. Matha, P. W. Cheng, Nonlinear Model Predictive Control
   of Floating Wind Turbines, in: the Twenty-third (2013) International Offshore and Polar Engineering, Anchorage, Alaska, USA, 2013, pp. 440—446. doi:10.1109/ACC.2014.6858718.
- [26] S. Raach, D. Schlipf, F. Sandner, D. Matha, P. W. Cheng, Nonlinear model predictive control
   of floating wind turbines with individual pitch control, in: Proceedings of the American

- <sup>871</sup> Control Conference, Portland, Oregon, USA, 2014, pp. 4434–4439. doi:10.1109/ACC.2014.
   <sup>872</sup> 6858718.
- [27] F. Lemmer, S. Raach, D. Schlipf, P. W. Cheng, Prospects Of Linear Model Predictive Control
   On A 10MW Floating Wind Turbine, in: the ASME 2015 34th International Conference on
   Ocean, Offshore and Arctic Engineering, 2015, pp. 1–11. doi:10.1115/0MAE2015-42267.
- [28] S. T. Navalkar, J.-W. van Wingerden, P. A. Fleming, G. A. M. van Kuik, Integrating robust
  lidar-based feedforward with feedback control to enhance speed regulation of floating wind
  turbines, in: American Control Conference, IEEE, 2015, pp. 3070–3075.
- [29] D. Schlipf, E. Simley, F. Lemmer, L. Pao, P. W. Cheng, Collective Pitch Feedforward Control
   of Floating Wind Turbines Using Lidar, in: Twenty-fifth (2015) International Ocean and
   Polar Engineering Conference, Vol. 2, Kona, Big Island, Hawaii, 2015, pp. 324–331. doi:
   10.17736/jowe.2015.arr04.
- [30] M. A. Lackner, M. A. Rotea, Structural control of floating wind turbines, Mechatronics 21 (4)
   (2011) 704-719. doi:10.1016/j.mechatronics.2010.11.007.
- [31] H. Namik, M. Rotea, M. Lackner, Active Structural Control with Actuator Dynamics on
   a Floating Wind Turbine, in: American Institute of Aeronautics and Astronautics, New
   Horizons Forum and Aerospace Exposition, no. January, 2013, pp. 1–16. doi:10.2514/6.
   2013-455.
- [32] G. Stewart, M. Lackner, Offshore wind turbine load reduction employing optimal passive
   tuned mass damping systems, IEEE Transactions on Control Systems Technology 21 (4)
   (2013) 1090-1104. doi:10.1109/TCST.2013.2260825.
- [33] A. R. Tsouroukdissian, S. Park, P. Pourazarm, W. L. Cava, M. Lackner, S. Lee, J. Cross Whiter, Smart Novel Semi-Active Tuned Mass Damper for Fixed-Bottom and Floating Off shore Wind, in: Offshore Technology Conference, 2016, pp. 1–17. doi:10.4043/26922-MS.
- <sup>895</sup> [34] Harsh S. Dhiman, Machine Learning in Wind Forecasting, 2020.
- [35] S. Karasu, A. Altan, Z. Saraç, R. Hacioğlu, Prediction of wind speed with non-linear autoregressive (NAR) neural networks, in: 2017 25th Signal Processing and Communications
   Applications Conference (SIU), IEEE, 2017, pp. 1–4.

- [36] S. Karasu, A. Altan, Z. Saraç, R. Hacioğlu, Estimation of fast varied wind speed based on
   NARX neural network by using curve fitting, International Journal of Energy Applications
   and Technologies 4 (3) (2017) 137–146.
- [37] S. Karasu, A. Altan, Z. Saraç, R. Hacıoğlu, Estimation of wind speed by using regression
   learners with different filtering methods, in: 1st International Conference on Energy Systems
   Engineering, Karabuk, Turkey, 2017.
- [38] L. Li, Z. Yuan, Y. Gao, Maximization of energy absorption for a wave energy converter using
   the deep machine learning, Energy 165 (2018) 340–349.
- [39] L. Li, Z. Yuan, Y. Gao, X. Zhang, Wave force prediction effect on the energy absorption of
  a wave energy converter with real-time control, IEEE Transactions on Sustainable Energy
  10 (2) (2018) 615–624.
- [40] L. Li, Y. Gao, D. Z. Ning, Z. M. Yuan, Development of a constraint non-causal wave energy
  control algorithm based on artificial intelligence, Renewable and Sustainable Energy Reviews
  (2020) 110519.
- [41] A. Altan, S. Karasu, E. Zio, A new hybrid model for wind speed forecasting combining long
  short-term memory neural network, decomposition methods and grey wolf optimizer, Applied
  Soft Computing 100 (2021) 106996.
- [42] U. Schlink, G. Tetzlaff, Wind Speed Forecasting from 1 to 30 Minutes, Theoretical and Applied
   Climatology 60 (1) (1998) 191–198. doi:10.1007/s007040050043.
- [43] T. Gneiting, K. Larson, K. Westrick, M. G. Genton, E. Aldrich, Calibrated Probabilistic Forecasting at the Stateline Wind Energy Center, Journal of the American Statistical Association
  101 (475) (2006) 968–979. doi:10.1198/01621450600000456.
- [44] J. L. Torres, A. Garcia, M. De Blas, A. De Francisco, Forecast of hourly average wind speed
  with ARMA models in Navarre (Spain), Solar Energy 79 (1) (2005) 65–77.
- [45] A. Sfetsos, A novel approach for the forecasting of mean hourly wind speed time series,
  Renewable energy 27 (2) (2002) 163–174.

- [46] R. G. Kavasseri, K. Seetharaman, Day-ahead wind speed forecasting using f-ARIMA models,
   Renewable Energy 34 (5) (2009) 1388–1393.
- [47] O. Ait Maatallah, A. Achuthan, K. Janoyan, P. Marzocca, Recursive wind speed forecasting
   based on Hammerstein Auto-Regressive model, Applied Energy 145 (2015) 191–197. doi:
   10.1016/j.apenergy.2015.02.032.
- [48] F. Fusco, J. V. Ringwood, Short-Term Wave Forecasting for Real-Time Control of Wave
   Energy Converters, IEEE TRANSACTIONS ON SUSTAINABLE ENERGY 1 (2) (2010)
   99–106. doi:10.1109/TSTE.2010.2047414.
- [49] Y. Pena Sanchez, J. Ringwood, A Critical Comparison of AR and ARMA Models for Short term Wave Forecasting, Proceedings of the Twelfth European Wave and Tidal Energy Con ference (2017) 9611—-9616.
- <sup>936</sup> [50] M. Ge, E. C. Kerrigan, Short-term ocean wave forecasting using an autoregressive moving
  <sup>937</sup> average model, in: 2016 UKACC 11th International Conference on Control (CONTROL),
  <sup>938</sup> IEEE, 2016, pp. 1–6.
- <sup>939</sup> [51] F. Dunne, L. Y. Pao, D. Schlipf, A. K. Scholbrock, Importance of Lidar Measurement Tim <sup>940</sup> ing Accuracy for Wind Turbine Control \*, 2014 American Control Conference (2014) 3716–
   <sup>941</sup> 3721doi:10.1109/ACC.2014.6859337.
- [52] D. Schlipf, D. J. Schlipf, M. Kühn, Nonlinear model predictive control of wind turbines using
  LIDAR, Wind Energy 16 (2013) (2013) 1107–1129. doi:10.1002/we.
- <sup>944</sup> [53] A. Betz, Introduction to the theory of flow machines, Introduction to the Theory of Flow
   <sup>945</sup> Machines (1966) 5–6.
- <sup>946</sup> [54] A. E. Samani, J. D. de Kooning, N. Kayedpour, N. Singh, L. Vandevelde, The impact of
  <sup>947</sup> pitch-to-stall and pitch-to-feather control on the structural loads and the pitch mechanism of
  <sup>948</sup> a wind turbine, Energies 13 (17). doi:10.3390/en13174503.
- <sup>949</sup> [55] B. Skaare, T. D. Hanson, F. G. Nielsen, R. Yttervik, A. M. Hansen, Integrated Dynamic Anal<sup>950</sup> ysis of Floating Offshore Wind Turbines, in: European Wind Energy Conf. and Exhibition,
  <sup>951</sup> Milan, Italy, 2007.

- <sup>952</sup> [56] J. Jonkman, S. Butterfield, W. Musial, G. Scott, Definition of a 5-MW Reference Wind
  <sup>953</sup> Turbine for Offshore System Development, Tech. Rep. February, National Renewable Energy
  <sup>954</sup> Laboratory (2009).
- <sup>955</sup> [57] D. Matha, Model Development and Load Analysis of an Offshore Wind Turbine, Tech. rep.,
   <sup>956</sup> University of Colorado Boulder (2010). doi:10.2172/973961.
- <sup>957</sup> [58] G. Bir, Multi-blade coordinate transformation and its application to wind turbine analysis,
  <sup>958</sup> in: 46th AIAA aerospace sciences meeting and exhibit, 2008, p. 1300.
- [59] F. Lemmer, S. Raach, D. Schlipf, P. W. Cheng, Parametric Wave Excitation Model for
  Floating Wind Turbines, in: 13th Deep Sea Offshore Wind R&D Conference, EERA DeepWind'2016, 20-22 January 2016, Vol. 94, 2016, pp. 290–305. doi:10.1016/j.egypro.2016.
  09.186.
- [60] H. Namik, Individual blade pitch control of floating offshore wind turbines, Ph.D. thesis, The
   University of Auckland (2012).
- [61] D. Schlipf, D. J. Schlipf, M. Kühn, Nonlinear model predictive control of wind turbines
  using LIDAR, Wind Energy 16 (7) (2013) 1107-1129. arXiv:arXiv:1006.4405v1, doi:
  10.1002/we.
- [62] S. J, E.A Nederkoorn, K. S, R. R, N. E, Optimised Aerodynamics and Control by Nonlinear
   Model based Predictive Control, in: European Wind Energy Association Conference, 2013,
   pp. 1–9.
- [63] A. Körber, R. King, Model predictive control for wind turbines, in: Proc. of European Wind
   Energy Conference, 2010, pp. 1–7.
- <sup>973</sup> [64] C. P. Schlipf D, Fleming P, Haizmann F, Scholbrock A, Hofsäß M, Wright A, Field Testing
  of Feedforward Collective Pitch Control on the CART2 Using a Nacelle-Based Lidar Scanner,
  Journal of Physics: Conference Series 555 (1) (2014) 12090. doi:10.1088/1742-6596/555/
  <sup>976</sup> 1/012090.
- <sup>977</sup> [65] F. Sandner, D. Schlipf, D. Matha, R. Seifried, P. W. Cheng, Reduced Nonlinear Model of a
  <sup>978</sup> Spar-mounted Floating Wind Turbine, in: Proceedings of the German Wind Energy Confer<sup>979</sup> ence (DEWEK), Bremen, Germany, 2012, p. 4.

- [66] E. A. Bossanyi, A. Kumar, O. Hugues-Salas, Wind turbine control applications of turbine mounted LIDAR, Journal of Physics: Conference Series 555 (1) (2014) 12011.
- [67] F. Dunne, L. Y.Pao, A. D.Wright, B. Jonkman, N. Kelley, Adding Feedforward Blade Pitch
   Control to Standard Feedback Controllers for Load Mitigation in Wind Turbines, Mechatron ics 21 (4) (2011) 682–690.
- [68] D. Schlipf, S. Schuler, P. Grau, K. Martin, Look-Ahead Cyclic Pitch Control Using LIDAR, in:
   The Science of Making Torque from Wind, Greece, 2010, pp. 1–7. doi:10.18419/opus-4538.
- [69] T. Mikkelsen, Lidar-based Research and Innovation at DTU Wind Energy A Review, Jour nal of Physics: Conference Series 524 (1) (2014) 012007. doi:10.1088/1742-6596/524/1/
   012007.
- [70] F. Dunne, L. Pao, A. Wright, B. Jonkman, N. Kelley, Combining standard feedback controllers
   with feedforward blade pitch control for load mitigation in wind turbines, in: 48th AIAA
   Aerospace Sciences Meeting Including the New Horizons Forum and Aerospace Exposition,
   Orlando, Florida, 2010, p. 18.
- <sup>994</sup> [71] B. F. Spencer, M. K. Sain, Controlling buildings: a new frontier in feedback, The Shock and <sup>995</sup> vibration digest 30 (4) (1998) 267–281.
- <sup>996</sup> [72] H. Li, X. Jing, H. R. Karimi, Output-feedback-based H $\infty$  control for vehicle suspension <sup>997</sup> systems with control delay, IEEE Transactions on Industrial Electronics 61 (1) (2014) 436– <sup>998</sup> 446.
- <sup>999</sup> [73] W. He, S. Zhang, S. S. Ge, Adaptive control of a flexible crane system with the boundary <sup>1000</sup> output constraint, IEEE Transactions on Industrial Electronics 61 (8) (2014) 4126–4133.
- [74] H. Li, J. Yu, C. Hilton, H. Liu, Adaptive sliding-mode control for nonlinear active suspension
   vehicle systems using T–S fuzzy approach, IEEE Transactions on Industrial Electronics 60 (8)
   (2013) 3328–3338.
- [75] B. F. Spencer Jr, S. Nagarajaiah, State of the art of structural control, Journal of structural engineering 129 (7) (2003) 845–856.

- [76] X. Li, H. Gao, Load mitigation for a floating wind turbine via generalized H $\infty$  structural control, IEEE Transactions on Industrial Electronics 63 (1) (2016) 332–342. doi:10.1109/ TIE.2015.2465894.
- [77] M. Ha, C. Cheong, Pitch motion mitigation of spar-type floating substructure for offshore
   wind turbine using multilayer tuned liquid damper, Ocean Engineering 116 (2016) 157–164.
   doi:10.1016/j.oceaneng.2016.02.036.
- [78] Y. Hu, M. Z. Q. Chen, Passive structural control with inerters for a floating offshore wind
   turbine, in: 36th Chinese Control conference, 2017, pp. 9266–9271. doi:10.23919/ChiCC.
   2017.8028833.
- [79] Y. Li, Z. Wu, Stabilization of floating offshore wind turbines by artificial muscle based active
   mooring line force control, in: Proceedings of the American Control Conference, 2016, pp.
   2277–2282. doi:10.1109/ACC.2016.7525257.
- [80] H. S. Dhiman, D. Deb, A Review of Wind Speed and Wind Power Forecasting Techniques,
   arXivarXiv:2009.02279.
- [81] Z.-h. Guo, J. Wu, H.-y. Lu, J.-z. Wang, A case study on a hybrid wind speed forecasting method using BP neural network, Knowledge-based systems 24 (7) (2011) 1048–1056.
- [82] G. Li, J. Shi, On comparing three artificial neural networks for wind speed forecasting, Applied
   Energy 87 (7) (2010) 2313–2320.
- [83] T. G. Barbounis, J. B. Theocharis, Locally recurrent neural networks for long-term wind speed and power prediction, Neurocomputing 69 (4-6) (2006) 466–496.
- [84] M. A. Mohandes, T. O. Halawani, S. Rehman, A. A. Hussain, Support vector machines for
  wind speed prediction, Renewable Energy 29 (6) (2004) 939–947.
- [85] A. Gani, K. Mohammadi, S. Shamshirband, T. A. Altameem, D. Petković, A combined
  method to estimate wind speed distribution based on integrating the support vector machine
  with firefly algorithm, Environmental Progress & Sustainable Energy 35 (3) (2016) 867–875.
- [86] J. Zhou, J. Shi, G. Li, Fine tuning support vector machines for short-term wind speed fore casting, Energy Conversion and Management 52 (4) (2011) 1990–1998. doi:10.1016/j.
   enconman.2010.11.007.

- [87] D. Petković, S. Shamshirband, N. B. Anuar, H. Saboohi, A. W. A. Wahab, M. Protić, E. Zal nezhad, S. M. A. Mirhashemi, An appraisal of wind speed distribution prediction by soft com puting methodologies: a comparative study, Energy conversion and Management 84 (2014)
   133–139.
- [88] H. Mori, E. Kurata, Application of gaussian process to wind speed forecasting for wind power
   generation, in: 2008 IEEE International Conference on Sustainable Energy Technologies,
   ICSET 2008, IEEE, 2008, pp. 956–959. doi:10.1109/ICSET.2008.4747145.
- [89] G. Li, J. Shi, Applications of Bayesian methods in wind energy conversion systems, Renewable
   Energy 43 (2012) 1–8.
- [90] H. Liu, H.-q. Tian, Y.-f. Li, Four wind speed multi-step forecasting models using extreme
   learning machines and signal decomposing algorithms, Energy conversion and management
   100 (2015) 16–22.
- [91] Z. Guo, W. Zhao, H. Lu, J. Wang, Multi-step forecasting for wind speed using a modified
   EMD-based artificial neural network model, Renewable Energy 37 (1) (2012) 241–249.
- [92] V. Nikolić, S. Motamedi, S. Shamshirband, D. Petković, S. Ch, M. Arif, Extreme learning
   machine approach for sensorless wind speed estimation, Mechatronics 34 (2016) 78–83.
- [93] S. Shamshirband, K. Mohammadi, C. W. Tong, D. Petković, E. Porcu, A. Mostafaeipour,
  S. Ch, A. Sedaghat, Application of extreme learning machine for estimation of wind speed
  distribution, Climate dynamics 46 (5-6) (2016) 1893–1907.
- [94] E. Cadenas, W. Rivera, Wind speed forecasting in three different regions of Mexico, using a
  hybrid ARIMA–ANN model, Renewable Energy 35 (12) (2010) 2732–2738.
- [95] J. Wang, J. Hu, K. Ma, Y. Zhang, A self-adaptive hybrid approach for wind speed forecasting,
   Renewable Energy 78 (2015) 374–385.
- [96] E. Simley, L. Pao, R. Frehlich, B. Jonkman, N. Kelley, Analysis of wind speed measurements
   using continuous wave LIDAR for wind turbine control, in: 49th AIAA Aerospace Sciences
   Meeting including the New Horizons Forum and Aerospace Exposition, 2011, p. 263.

- [97] L. Valldecabres, A. Peña, M. Courtney, L. von Bremen, M. Kühn, Very short-term forecast
   of near-coastal flow using scanning lidars, Wind energy science 3 (1) (2018) 313–327.
- [98] E. Simon, M. Courtney, N. Vasiljevic, Minute-scale wind speed forecasting using scanning
   lidar inflow measurements, Wind Energy Science Discussions (2018) 1–30.
- 1064 [99] WAVEWATCH III (WW3).
- 1065 URL https://polar.ncep.noaa.gov/waves/wavewatch/
- 1066 [100] Forecasts ECMWF.
- 1067 URL https://www.ecmwf.int/en/forecasts
- 1068 [101] SWAN.
- 1069URLhttps://www.tudelft.nl/citg/over-faculteit/afdelingen/1070hydraulic-engineering/sections/environmental-fluid-mechanics/research/swan
- [102] M. C. Deo, C. S. Naidu, Real time wave forecasting using neural networks, Ocean engineering
   26 (3) (1998) 191–203.
- [103] T. Sadeghifar, M. Nouri Motlagh, M. Torabi Azad, M. Mohammad Mahdizadeh, Coastal
   wave height prediction using Recurrent Neural Networks (RNNs) in the south Caspian Sea,
   Marine Geodesy 40 (6) (2017) 454–465.
- [104] C. Ni, X. Ma, Y. Bai, Convolutional Neural Network based power generation prediction of
   wave energy converter, in: 2018 24th International Conference on Automation and Computing
   (ICAC), IEEE, 2018, pp. 1–6.
- [105] A. Akpınar, M. Özger, M. I. Kömürcü, Prediction of wave parameters by using fuzzy inference
   system and the parametric models along the south coasts of the Black Sea, Journal of Marine
   Science and Technology 19 (1) (2014) 1–14.
- [106] M. Wu, C. Stefanakos, Z. Gao, S. Haver, Prediction of short-term wind and wave conditions for
   marine operations using a multi-step-ahead decomposition-ANFIS model and quantification
   of its uncertainty, Ocean Engineering 188 (2019) 106300.
- <sup>1085</sup> [107] G. Reikard, P. Pinson, J.-R. Bidlot, Forecasting ocean wave energy: The ECMWF wave <sup>1086</sup> model and time series methods, Ocean Engineering 38 (10) (2011) 1089–1099.
- 1087 URL http://www.sciencedirect.com/science/article/pii/S0029801811000837

- <sup>1088</sup> [108] F. Woodcock, C. Engel, Operational consensus forecasts, Weather and forecasting 20 (1) <sup>1089</sup> (2005) 101–111.
- <sup>1090</sup> [109] F. Woodcock, D. J. M. Greenslade, Consensus of numerical model forecasts of significant wave <sup>1091</sup> heights, Weather and Forecasting 22 (4) (2007) 792–803.
- [110] Z. S. Hou, Z. Wang, From model-based control to data-driven control: Survey, classification
   and perspective, Information Sciences 235 (2013) 3–35. doi:10.1016/j.ins.2012.07.014.
   URL http://dx.doi.org/10.1016/j.ins.2012.07.014
- [111] S. L. Brunton, B. R. Noack, Closed-Loop Turbulence Control: Progress and Challenges,
   Applied Mechanics Reviews 67 (5) (2015) 050801. doi:10.1115/1.4031175.
- <sup>1097</sup> URL http://appliedmechanicsreviews.asmedigitalcollection.asme.org/article.
  <sup>1098</sup> aspx?doi=10.1115/1.4031175
- [112] M. B. Kane, Machine Learning Control for Floating Offshore Wind Turbine Individual Blade
   Pitch Control, Proceedings of the American Control Conference 2020-July (2020) 237–241.
   doi:10.23919/ACC45564.2020.9147912.
- [113] P. J. Schmid, Dynamic mode decomposition of numerical and experimental data, Journal of
   fluid mechanics 656 (2010) 5–28.
- [114] S. L. Brunton, J. L. Proctor, J. N. Kutz, Discovering governing equations from data by
   sparse identification of nonlinear dynamical systems, Proceedings of the National Academy
   of Sciences 113 (15) (2016) 3932–3937.
- <sup>1107</sup> [115] J. L. Proctor, S. L. Brunton, J. N. Kutz, Generalizing Koopman theory to allow for inputs <sup>1108</sup> and control, SIAM Journal on Applied Dynamical Systems 17 (1) (2018) 909–930.
- [116] J. M. Jonkman, M. L. B. Jr, FAST User 's Guide, Tech. rep., National Renewable Energy
  Laboratory (2005).
- [117] B. J. Jonkman, J. M. Jonkman, FAST v8.16.00a-bjj User's Guide, Tech. rep., National Re newable Energy Laboratory (2016).
- [113] D. J. Malcolm, A. C. Hansen, WindPACT turbine rotor design study, National Renewable
   Energy Laboratory, Golden, CO 5.

<sup>1115</sup> [119] Recommendations for design of offshore wind turbines (RECOFF).

1116 URL https://cordis.europa.eu/project/id/ENK5-CT-2000-00322

- 1117 [120] F. Goezinne, Terms of reference DOWEC, NEG-Micon. Bunnik.
- <sup>1118</sup> [121] T. J. Larsen, A. M. Hansen, How 2 HAWC2, the user's manual.
- 1119 [122] C. Bak, F. Zahle, R. Bitsche, T. Kim, A. Yde, L. C. Henriksen, M. H. Hansen, J. P. Blasques,
- M. Gaunaa, A. Natarajan, The DTU 10-MW reference wind turbine, in: Danish Wind Power
   Research, Fredericia, Denmark, 2013.
- 1122 [123] Innwind.eu.
- 1123 URL http://www.innwind.eu/
- <sup>1124</sup> [124] Wind turbine design software Bladed DNV GL.
- 1125 URL https://www.dnvgl.com/services/wind-turbine-design-software-bladed-3775
- 1126 [125] LEANWIND.
- 1127 URL http://www.leanwind.eu/
- [126] C. Desmond, J. Murphy, L. Blonk, W. Haans, Description of an 8 MW reference wind turbine,
  in: Journal of Physics: Conference Series, Vol. 753, 2016. doi:10.1088/1742-6596/753/9/
  092013.
- <sup>1131</sup> [127] SIMPACK MBS Software Wind.
- 1132 URL http://www.simpack.com/industrial\_sectors\_wind.html
- [128] D. Matha, F. Beyer, Offshore wind turbine hydrodynamics modelling in SIMPACK, SIM PACK news, July.
- [129] G. Betti, M. Farina, G. A. Guagliardi, A. Marzorati, R. Scattolini, Development of a Control Oriented Model of Floating Wind Turbines, IEEE Transactions on Control Systems Technol ogy 22 (1) (2014) 69–82. doi:10.1109/TCST.2013.2242073.
- [130] G. Betti, M. Farina, A. Marzorati, R. Scattolini, G. A. Guagliardi, Modeling and control of a
  floating wind turbine with spar buoy platform, in: 2nd IEEE International Energy Conference
  and Exhibition, ENERGYCON 2012, 2012, pp. 189–194. doi:10.1109/EnergyCon.2012.
  6347749.

[131] J. R. Homer, R. Nagamune, Physics-Based 3-D Control-Oriented Modeling of Floating Wind
 Turbines, IEEE Transactions on Control Systems Technology 26 (1) (2018) 14–26. doi:
 10.1109/TCST.2017.2654420.