

Local control of improper ferroelectric domains in YMnO₃

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Improper ferroelectrics are described by two order parameters: a primary one, driving a transition to long-range distortive, magnetic or otherwise non-electric order, and the electric polarization, which is induced by the primary order parameter as a secondary, complementary effect. Using low-temperature scanning probe microscopy, we show that improper ferroelectric domains in YMnO₃ can be locally switched by electric field poling. However, subsequent temperature changes restore the as-grown domain structure as determined by the primary lattice distortion. The backswitching is explained by uncompensated bound charges occurring at the newly written domain walls due to the lack of mobile screening charges at low temperature. Thus, the polarization of improper ferroelectrics is in many ways subject to the same electrostatics as in their proper counterparts, yet complemented by additional functionalities arising from the primary order parameter. Tailoring the complex interplay between primary order parameter, polarization, and electrostatics is therefore likely to result in novel functionalities specific to improper ferroelectrics.

I. INTRODUCTION

In improper ferroelectrics, the spontaneous polarization emerges as subordinate effect to a primary order parameter which can be a lattice distortion, a magnetization or another non-electric quantity¹⁻⁴. This dependence can lead to properties not observed in their polarization-driven proper ferroelectric counterparts. Improper ferroelectrics can be expected to be more robust towards extrinsic influences, such as depolarizing fields, allowing domain configurations with unusual head-to-head or tail-to-tail polarization geometries at the domain walls^{5,6}. Such domain configurations can have technologically relevant properties, ranging from local conductance enhancement⁷⁻⁹ to functionalities of advanced circuit elements^{10,11}.

Both order parameters of improper ferroelectrics, the primary one and the induced polarization, can in principle influence the domain structure, but while it appears obvious that the primary order parameter sets the initial domain structure when crossing the transition temperature, the role played by the secondary order parameter and the associated electrostatics is not as clear. In the case of the hexagonal manganites ($RMnO_3$, with $R = Sc, Y, In, Dy - Lu$), one of the most established classes of improper ferroelectrics, a lattice-trimerizing distortion as primary order parameter dominates the formation of domains, but only the secondary order parameter is susceptible to poling in an electric field¹². Therefore, a key question is if, and how, domains formed in association with the emergence of the primary order parameter at the transition temperature T_c may differ from those created by electric field poling acting on the secondary order parameter within the ordered phase far below T_c . In

previous studies on the emergence and manipulation of ferroelectricity in the hexagonal manganites, the topology and the distribution of the resulting domains was considered^{5,6,12}, but not the material-specific dynamics of the poling process. Even though a detailed understanding of this issue is crucial for the functionalization of improper ferroelectrics, this aspect has not received much attention.

Here, we investigate electric-field poling at the nanometer scale in hexagonal YMnO₃. In this material, uniform tilting of the MnO₅ bipyramids in the unit cell and a concomitant shift of the yttrium ions occur at 1258 K. This lattice-trimerizing distortive transition drives an improper ferroelectric polarization of $5.6 \mu\text{C cm}^{-2}$ along the hexagonal axis^{2,6,13-15}. The resulting domain structure consists of six trimerization-polarization domain states forming vortex-like meeting points with alternating polarization around the vortex core^{5,6,16}.

We use atomic force microscopy (AFM) to apply local electric fields at cryogenic temperatures, where non-intrinsic effects due to barrier layer capacitances are negligible^{17,18}, creating polarization domains at the nanoscale. We compare these written domains to the domains formed via the primary order parameter at T_c . We find that despite the secondary nature of the electric polarization, this polarization dominates the poling behavior just as in conventional ferroelectrics. Domains can be created at will by locally applied electric-fields. Thermal annealing cycles, however, return the samples to the as-grown domain configuration. This recovery is explained by uncompensated bound charges at the domain walls and the surface, which arise due to decreasing availability of mobile carriers at cryogenic temperature. Hence,

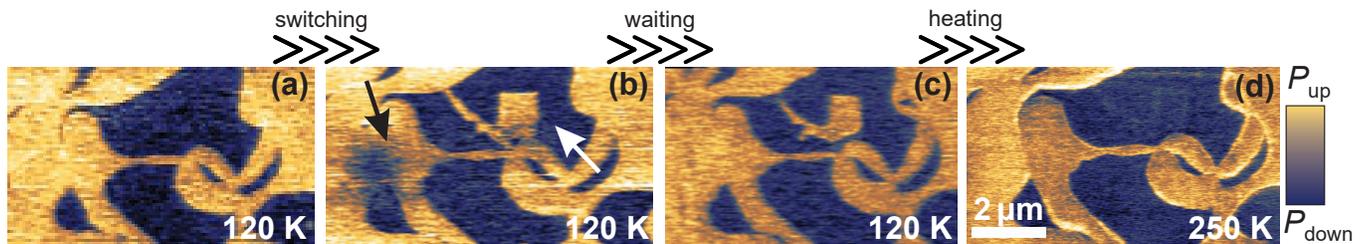


FIG. 1. Creation of improper ferroelectric domains in YMnO_3 by local cryogenic temperature electric-field poling. (a) Pristine domain structure measured by PFM at 120 K. (b) A square-shaped area (white arrow) of reversed polarization is created by scanning while applying +45 V to the AFM tip in contact with the surface. The bright line protruding from the lower end of the square was caused by moving the AFM tip into position for the poling with the poling voltage applied. When the same voltage is applied to an area polarized in the direction of the applied voltage, surface charging results in a diffuse change of contrast (black arrow). (c) The same area of the sample surface imaged after remaining at 120 K for 6 days after the poling. The artificially created domain is still present, whereas the surface-charged area has disappeared. (d) At 250 K the domain structure abruptly reverts to the original configuration in (a). A minor variation in contrast between panels (a)-(d) is due to differences in scan speed and tip wear over the duration of six days.

90 despite the secondary nature of the ferroelectric order,
 91 the electrostatic conditions overrule the primary lattice
 92 trimerization. Quite strikingly, we thus find that im-
 93 proper ferroelectrics retain key characteristics of proper
 94 ferroelectrics, yet complemented by functionalities intro-
 95 duced by the secondary nature of the electric order.

96 II. METHODS

97 Experiments were performed on YMnO_3 single crys-
 98 tals grown by the floating-zone method^{16,19}. The crys-
 99 tals were cut into platelets with a thickness of approx-
 100 imately 500 μm perpendicular to the hexagonal axis.
 101 They were lapped with an Al_2O_3 solution and pol-
 102 ished with silica slurry, yielding a surface roughness of
 103 approximately 1 nm, suitable for AFM measurements.
 104 We thus obtained out-of-plane-polarized samples whose
 105 trimerization-polarization domains at the surface are sep-
 106 arated by nominally uncharged 180° side-by-side domain
 107 walls⁵⁻⁷.

108 Dielectric measurements were performed using a Novo-
 109 control Alpha analyser (at 1 Hz to 1 MHz) and a TF2000
 110 Aixact system (hysteresis loops, at 1 Hz) in combina-
 111 tion with a high-voltage booster for voltages up to 2 kV.
 112 Measurements were conducted at 50 K to 300 K in a
 113 closed-cycle refrigerator with samples in vacuum to avoid
 114 electrical discharge. The properties of semiconduct-
 115 ing materials are often superimposed by extrinsic bar-
 116 rier layer contributions²⁰ which may affect polarization
 117 measurements^{21,22}. For YMnO_3 , a temperature of 120 K
 118 and a frequency of 1 Hz avoid barrier layer capacitances
 119 and allow detecting the genuine ferroelectric properties
 120 of the material both in bulk and AFM experiments^{17,18}.

121 AFM measurements were performed at 120 K to 250 K
 122 in an attoLiquid 2000 AFM setup (attocube GmbH, Ger-
 123 many) with ANSCM-PT Pt/Ir-coated conductive tips
 124 (AppNano Inc., USA) in two different modes:

125 On the one hand, we directly imaged the distribu-
 126 tion of the polarization by piezoresponse force microscopy
 127 (PFM)²³⁻²⁵. In this mode, the AFM tip is brought into
 128 contact with the sample surface and an alternating volt-
 129 age is applied to the tip. The instrument detects the con-
 130 traction and expansion of the sample due to the piezo-
 131 electric effect. A contraction in phase or in antiphase
 132 with the excitation voltage corresponds to polarization
 133 in the upward or downward direction, respectively.

134 On the other hand, we used the presence of uncom-
 135 pensated charges on the surface to image the domain
 136 structure by electrostatic force microscopy (EFM)^{26,27}.
 137 Due to a difference in strength of the pyroelectric effect,
 138 the surface charge differs between domains and domain
 139 walls, which is detected as contrast in EFM measure-
 140 ments. This contrast is further affected by structural and
 141 chemical defects, which show a propensity to accumulate
 142 at domain walls, locally enhancing the conductivity and
 143 thus reducing the surface charge. In our EFM experi-
 144 ment, the AFM tip is grounded so that mirror charges
 145 are induced on the tip by charges on the sample surface.
 146 In this way, the EFM measurement is sensitive to the
 147 density of surface charges, but not their polarity. For
 148 details of the EFM measurement, see Supplementary In-
 149 formation.

150 Local domain switching was achieved at 120 K by ap-
 151 plying DC bias voltages to the AFM tip in contact with
 152 the sample surface while line-scanning the surface at a
 153 constant speed of 2 $\mu\text{m s}^{-1}$.

154 III. RESULTS

155 PFM measurements at 120 K showed the typi-
 156 cal trimerization-induced improper ferroelectric domain
 157 structure of the hexagonal manganites (Fig. 1(a)). We
 158 then created a new domain by applying a voltage of
 159 +45 V to the AFM tip while scanning a window of

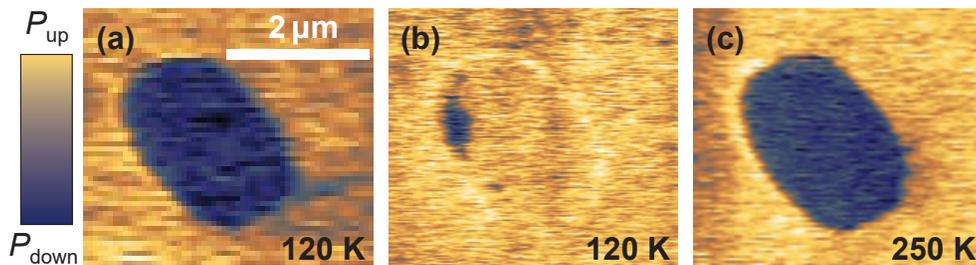


FIG. 2. Elimination of improper ferroelectric domains in YMnO_3 by local low-temperature electric-field poling. (a) A down-polarized as-grown bubble domain in an up-polarized environment measured by PFM at 120 K. (b) The polarization of the bubble domain is reversed by scanning a window of $2\ \mu\text{m} \times 2\ \mu\text{m}$ covering the bubble with +45 V applied to the AFM tip. Note that the outline of the original domain is still visible in the PFM image. (c) When increasing the temperature to 250 K, the original bubble domain in (a) is reestablished.

160 $1\ \mu\text{m} \times 1\ \mu\text{m}$ (Fig. 1 (b)). This resulted in a square-shaped
 161 domain of upwards polarization within a down-polarized
 162 domain (white arrow). The black arrow points to a re-
 163 gion where the same poling procedure was applied to an
 164 area which was already polarized upwards. The latter
 165 led to the injection of surface charges, visible as a dif-
 166 fuse dark region because the surface charge screens the
 167 applied voltage and hence leads to a reduced piezore-
 168 sponse, even though the intrinsic piezoelectric coefficient
 169 itself does not change. When a negative voltage of -45 V
 170 is applied, the effects on up- and down-polarized domains
 171 are reversed (see Supplementary Information). At 120 K,
 172 the written domain was stable over a period of more than
 173 six days, whereas the space charges disappeared within
 174 a few hours (Fig. 1 (c)). Finally, we found that when
 175 the sample was heated to 250 K, the domain structure
 176 reverted to its original configuration, *i.e.*, the electric-
 177 field-induced square domain disappeared (Fig 1 (d)).

178 In order to investigate how the ferroelectric do-
 179 main structure reverts to its previous configuration, we
 180 recorded a series of PFM images at higher spatial res-
 181 olution. Figure 2 (a) shows a down-polarized as-grown
 182 bubble domain within an up-polarized environment. Af-
 183 ter scanning a window of $2\ \mu\text{m} \times 2\ \mu\text{m}$ covering the entire
 184 bubble with +45 V applied to the tip, the polarization
 185 was mostly reversed so that the bubble disappeared. A
 186 faint outline, however, was still observable where the pre-
 187 vious as-grown domain wall had been located (Fig. 2 (b)).
 188 This outline is possibly caused by the presence of oxy-
 189 gen interstitials, which are known to accumulate at neu-
 190 tral walls¹¹, but are immobile at low temperature²⁸ and
 191 hence cannot follow the displacement of the domain wall.
 192 These defects are visible in the PFM measurement, be-
 193 cause they cause a local difference in Schottky barrier
 194 and hence change the effective applied voltage. When the
 195 sample was heated to 250 K, the original domain struc-
 196 ture was recovered as depicted in Fig. 2 (c). A minor
 197 change in overall contrast in the poled region is due to
 198 the removal of residual dirt from the surface by scanning
 199 with high load and applied voltage.

200 Complementary to the local measurements, we per-
 201 formed bulk dielectric spectroscopy and ferroelectric hys-

202 tersis loop measurements to characterize the retention of
 203 the YMnO_3 polarization and test for signatures of back-
 204 switching at the macro-scale. Measurements of the di-
 205 electric constant ϵ' shown in Fig. 3 (a) revealed a step-
 206 like increase of ϵ' with temperature, indicating an in-
 207 trinsic dielectric constant masked by barrier-layer capac-
 208 itance effects^{20,29}. Therefore, we chose our measurement
 209 temperature such that we could probe the intrinsic fer-
 210 roelectric polarization^{17,18,20} (left of the dashed lines in
 211 Fig. 3 (a)). Specifically, we performed all experiments
 212 at or below 140 K. For confirmation, we measured a
 213 ferroelectric hysteresis loop at 120 K with an electrical
 214 poling field oscillating at 1 Hz (inset of Fig. 3 (b)). The
 215 shape of the loop and the saturation polarization are in
 216 perfect agreement with theory¹⁵ and values of previous
 217 experiments^{5,12,18,30}, confirming that only the true po-
 218 larization was measured.

219 To measure the retention behavior, first a pre-poling
 220 pulse with an applied electric field of $120\ \text{kV cm}^{-1}$ was
 221 used to saturate the sample polarization. After a delay
 222 time ranging from 1 s to 3.6×10^5 s, positive-up-negative-
 223 down (PUND) measurements with the first pulse in the
 224 same electric-field direction as the pre-poling pulse and a
 225 peak electric field of $120\ \text{kV cm}^{-1}$ were performed. From
 226 these, we determined the remaining fraction of the satu-
 227 rated polarization $p_r(t) = P_{\text{meas}}(t)/P_{\text{sat}}$, where P_{sat} de-
 228 notes the initial polarization created by the pre-poling
 229 pulse and P_{meas} the measured polarization after the de-
 230 lay time t . Figure 3 (b) shows p_r as a function of the
 231 delay time t measured at three different temperatures.
 232 The equilibrium state towards which the system relaxes
 233 corresponds to $p_r = 50\%$, *i.e.*, an equal fraction of up-
 234 and down polarized regions. At 140 K, the polarization
 235 reverted quickly to this equilibrium state after poling,
 236 whereas at 120 K the value of polarization surplus was
 237 retained for several days. Despite this stability, however,
 238 minor relaxation effects in the domain structure were ob-
 239 served even at 120 K. These results are consistent with
 240 the local switching experiments in Figs. 1 and 2, showing
 241 near-perfect stability of the electric-field induced domain
 242 structure at 120 K and fast relaxation at higher temper-
 243 atures.

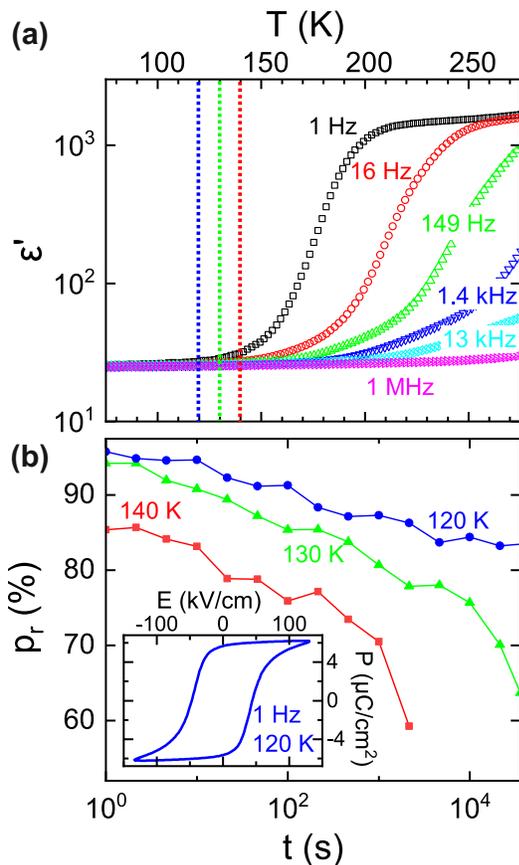


FIG. 3. Spatially integrated bulk ferroelectric properties of YMnO_3 . (a) Temperature-dependent dielectric constant for selected frequencies measured by dielectric spectroscopy. The dashed lines denote the temperatures below which the intrinsic ferroelectric properties of the sample can be measured. (b) Time-dependent decay of the saturated polarization ($p_r(t) = P_{\text{meas}}(t)/P_{\text{sat}}$, see text). At 120 K, the polarization is retained for several days, whereas at 140 K $p_r(t)$ relaxes towards equilibrium, *i.e.*, $p_r = 50\%$, within a few hours. Inset: ferroelectric hysteresis loop measured at 120 K and 1 Hz.

The domain walls of as-grown and electric-field-induced polar domains also showed different behavior when observed in EFM measurements. Because the overall conductivity is very low at 120 K, the domain wall conductance cannot be measured directly by conductive AFM. However, EFM allows to image the electrostatics of domain walls even under insulating conditions (see Ref. 27 and Supplementary Information). Fig. 4 (a) shows a PFM scan of the sample surface where a surface domain was created by poling at 120 K (arrow). Here, in contrast to the measurements in which the AFM tip was scanned over a defined area with an applied voltage, the tip was stationary on the sample surface while applying the writing voltage. This resulted in the creation of a domain of about 300 nm diameter as shown in Fig. 4 (a).

Figure 4 (b) shows an EFM image of the same area, measured at 120 K after the sample had been heated to

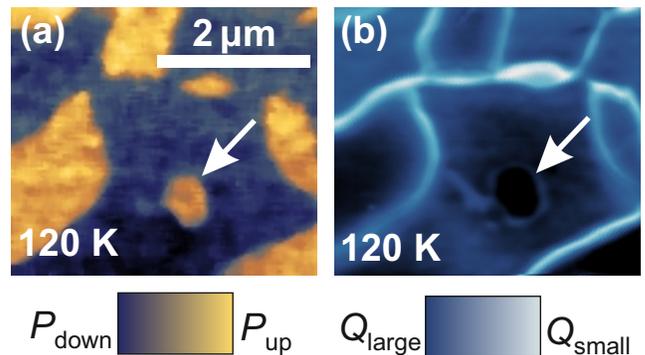


FIG. 4. Electrostatic contrast at as-grown and electric-field-induced domain walls at 120 K. (a) PFM scan of the sample surface. An electric-field-induced surface domain is highlighted by the white arrow. (b) EFM scan of the same area as in (a). Even though the PFM contrast is the same for both as-grown and electric-field-induced domains, the EFM contrast of the respective domain walls differs strongly between the two differently generated domains. Some domains which, appear disconnected in the PFM image, are in fact connected by channel-like domains below the resolution limit. This can be seen in the EFM image where the topological domain structure becomes evident.

200 K. This temperature sequence creates an EFM contrast due to the pyroelectric effect associated with the temperature change, but preserves the written domain pattern because the temperature is not high enough for fast relaxation (see Supplementary Information for details). A pronounced EFM contrast was observed at as-grown domain walls, which is consistent with their enhanced conductivity attributed to the presence of oxygen interstitials¹¹. At the domain walls associated with the written domains, however, the EFM contrast was weaker by a factor of 2.5 on average (as obtained from a number of representative line profiles), suggesting lower electronic conductance and, hence, a lower density of oxygen defects compared to the as-grown walls. In the PFM measurements, however, the as-grown and the electric-field-induced domains exhibited the same brightness.

IV. DISCUSSION

We now discuss why electric-field-induced domains tend to return to their as-grown, trimerization-controlled configuration upon heating. We emphasize that even though the electric-field poling acts on the polarization, the trimerization has to follow this reorientation because of the rigid coupling between secondary and primary order parameter³¹. Thus, we can exclude that the observed backswitching is due to an unswitched residue of the trimerized state. In addition, in all PFM measurements, electric-field induced and as-grown domains showed the same domain contrast, and in bulk measurements electric-field poling yields the expected saturation

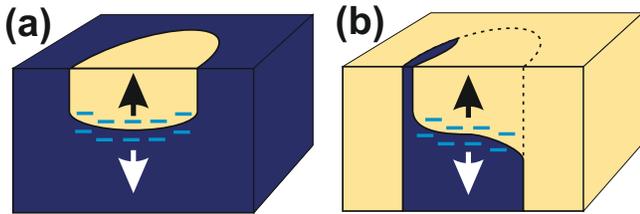


FIG. 5. Schematic cross section of tip-electric-field-induced domain configurations and distribution of uncompensated charges ($-$). Arrows denote the polarization direction of the respective domains. (a) Creation of a new domain at the surface, as described in Fig. 1. (b) Deleting an as-grown bubble domain from the surface, as described in Fig. 2. Vertical dimensions not to scale.

polarization. Our measurements are thus consistent with electric-field induced and as-grown domains exhibiting the same properties, specifically the same polarization.

When the polarization at the sample surface is locally influenced by the AFM tip, it is affected only to a depth of a few hundreds of nanometers away from the surface due to field-focusing below the AFM tip. Hence, the bulk polarization below the field-induced square domain in Fig. 1 remained unswitched. At the newly created buried domain wall below, the polarizations meet in a tail-to-tail configuration, resulting in uncompensated charges as is illustrated in Fig. 5 (a). At elevated temperatures, such a configuration would be readily screened by charge carriers, but in the cryogenic environment of our experiment, this screening process becomes slower than the timescale of the experiment. Since the presence of uncompensated charges at the domain wall is energetically unfavorable, the material returned to its initial configuration when heated.

As-grown domains, on the other hand, exhibit no uncompensated charges and are therefore stable. An as-grown domain wall which had been erased by external electric fields was restored to its original shape by a temperature increase (Fig. 2). We conclude that defects, which show a propensity to accumulate at domain walls at room temperature, but are mostly immobile at cryogenic temperatures²⁸, could remain at their original location when a domain wall is displaced and serve as localized potential energy minima for the recovery of the domain structure. This hypothesis is corroborated by the remanent outline of the erased domain in Fig. 2 (b) and the difference in domain-wall contrast between as-grown and electric-field-induced domain walls in Fig. 4 (b), which can both be explained by a difference in defect density. A minor migration of defects to domain walls may occur even at cryogenic temperatures, which explains the very faint outline of the previously poled region observed in Fig 1 (d). Note that a similar dissociation of domain walls and defects during switching was previously found in BiFeO_3 ³².

The intriguing consequence of this mechanism is that the electrostatic forces in the improper ferroelectric

YMnO_3 are strong enough to reverse not only the secondary, but also the primary order parameter, leading to the striking situation that the allegedly weaker order parameter controls the stronger one.

Note that in all our local probe experiments, the topological protection of the domain structure by the primary order parameter did not play a role, because only domains within existing domains at the surface were created and erased, whereas the topological domain vortex meeting points were not affected. Therefore, we observed a behavior resembling that of proper ferroelectrics.

In our bulk switching experiments, on the other hand, the topological constraints imposed by the primary order parameter affected the poling behavior. Specifically, electric-field poling cannot destroy the topological domain vortices and therefore the sample cannot be transferred into a single-domain state^{5,6}. These unswitched remnants of the unfavored polarization direction then served as nuclei and memory in the relaxation of the polarization, a behavior not observed in proper ferroelectrics.

V. SUMMARY AND CONCLUSIONS

We have shown that despite their origin in a non-polar, primary order parameter, the manipulation of polar domains in improper ferroelectric YMnO_3 is guided by the same electrostatics as in proper ferroelectrics. In particular, the improper ferroelectric domain configuration can be manipulated by electric fields, and its dynamics upon heating is driven by the migration of electric charges to domain walls. On the other hand, bulk measurements indicate that the topological protection of the domain configuration due to the primary order parameter prevents the sample from reaching the single-domain configuration of a proper ferroelectric, with consequences for the nucleation, pinning and conductance of the remaining ferroelectric domain walls. We thus conclude that with regard to external fields and charges, improper ferroelectrics behave like a proper ferroelectric in many respects, but the existence of the primary order parameter leads to intriguing additional functionalities.

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389 H. performed the dielectric spectroscopy measurements.

390 E.P. grew the YMnO_3 samples. L.K., S.K., T.L, M.T.,

391 D. M. and M.F. designed the experiment and supervised
 392 the study.

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