PRIMASS visits Hilda and Cybele groups



M.N.De Prá^a, N. Pinilla-Alonso^b, J. M. Carvano^a, J. Licandro^{c,d}, H. Campins^e, T. Mothé-Diniz^f, J. De

Abstract 11

1

The Cybele and Hilda dynamical groups delimit the outer edge of the asteroid belt. Their compositional 12 distribution is a key element to constrain evolutionary models of the Solar System. In this paper, we present 13 a compositional analysis of these populations using spectroscopic observations, SDSS and NEOWISE data. 14 As part of the PRIMASS (Primitive Asteroids Spectroscopic Survey), we acquired visible spectra of 18 15 objects in Hilda or Cybele groups with the Goodman High Throughput Spectrometer at the 4.1m SOAR 16 telescope and 20 near-IR spectra of Hilda objects with Near Infrared Camera Spectrograph at the 3.56m 17 TNG. The sample is enlarged with spectra taken from the literature in order to increase our statistical 18 analysis. The spectra were inspected for aqueous alteration bands and other spectral features that can be 19 linked to compositional constraints. The analysis shows a continuous distribution of compositions from the 20 main-belt to the Cybele, Hilda and Trojan regions. We also identify a population in the Trojans group not 21 present in Hilda or Cybele objects. 22

Keywords: asteroids, hilda, cybele, trojan, SOAR, TNG, SDSS 23

1. Introduction 24

The outskirts of the asteroid belt can be divided into three main groups: the Cybele, between 3.3 and 25 3.7 au, in the external region of the Hecuba gap (i.e., the 2:1 mean motion resonance with Jupiter), the 26 Hilda at ~ 4.0 AU in the 3:2 mean motion resonance with Jupiter, and the Trojan population around the 27 L4 and L5 equilibrium points of Jupiter. 28

Due to their heliocentric distances, asteroids belonging to these groups would have experienced less 29 heating and should be of more pristine composition than objects in inner regions of the main belt (Rivkin 30 et al., 2015; Krot et al., 2015). Therefore they are considered to be transitional populations between icy 31 and rocky objects. 32

Early investigations of the composition of members of the outer belt populations (Tedesco & Gradie, 33 Gradie 1989, Gradie 1979) showed a predominance of asteroids with low albedo and featureless spectra, 34 whose colors vary from gray to red. In the Tholen's taxonomic classification (Tholen, 1984) this corresponds 35 to the C-, P-, or D-type. The red color in primitive class asteroids is often associated with the presence of complex organics on their surfaces (Gaffey et al., 1989; Vilas et al., 1994). Moreover, Emery et al. (2006) 37 detected fine grained anhydrous silicates on the surface of D-/P-type Trojan asteroids by their thermal 38 emission. Although these taxonomic classes are observed across the whole asteroid belt, Carvano et al. 39 (2003) pointed out, based on visible spectroscopy, that inner belt D-type objects often have concave spectral 40 shapes and higher albedo compared to the outer belt D-types, suggesting that they may be compositionally 41 different. 42

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Number	Name	Date	UT	Airmass	m_v	α	T_{EXP}	Slit	SA*
		start				(o)	sec	(")	
225	Henrietta	2011-01-31	05:32	1.11	14.93	5.60	270.0	1.03	1
229	Adelinda	2012-03-28	00:43	1.623	14.94	6.45	330.0	1.68	$1,\!4,\!5$
401	Ottilia	2011-01-31	07:35	1.22	15.02	14.60	240.0	1.03	1
528	Rezia	2012-03-28	09:10	1.163	15.40	16.63	360.0	1.68	$1,\!4,\!5$
790	Pretoria	2012-03-29	00:05	1.257	14.57	14.63	240.0	1.68	$1,\!3,\!5$
909	Ulla	2011-01-31	01:28	1.353	14.89	17.38	180.0	1.03	1
940	Kordula	2011-02-01	07:26	1.363	16.04	14.59	540.0	1.03	1
1177	Gonnessia	2012-03-28	00:01	1.213	14.53	11.86	240.0	1.68	$1,\!4,\!5$
1280	Baillauda	2012-03-29	01:45	1.363	16.04	13.21	360.0	1.68	$1,\!3,\!5$
6039	Parmenides	2011-02-01	05:22	1.187	17.13	4.66	600.0	1.03	1
334	Chicago	2011-01-31	05:13	1.51	13.11	0.12	73.333	1.03	1
1144	Oda	2011-02-08	06:11	1.387	16.41	11.84	540.0	1.03	1
1269	Rollandia	2011-02-01	03:48	1.603	14.14	5.45	180.0	1.03	1
1439	Vogtia	2012-03-28	03:26	1.253	15.73	4.21	360.0	1.68	$1,\!4,\!5$
1902	Shaposhnikov	2012-03-27	06:46	1.193	15.72	14.30	240.0	1.68	1,2,3,4
3202	Graff	2011-02-01	01:02	1.338	16.43	10.79	510.0	1.03	1
3577	Putilin	2011-02-01	04:10	1.49	14.98	2.81	180.0	1.03	1
3843	Oisca	2011-01-31	04:39	1.75	16.48	5.91	480.0	1.03	1
7394	Xan thomalitia	2012-03-29	00:33	1.373	17.52	12.35	600.0	1.68	$1,\!3,\!5$

Table 1: Asteroids observational conditions - Visible

*Solar Analogs: (1) L102-1081, (2) L107-684, (3) L107-998, (4) HD44594, (5) HD144584

Furthermore, Dahlgren and Lagerkvist (1995) and Dahlgren et al. (1997) investigated visible spectra 43 of 43 objects in the Hilda group. They reported 64% of the Hilda asteroids belonged to the D-class, while 44 28% and 2% were P- and C-types, respectively (the remaining percentage belonged to ambiguous classes). 45 In addition, a relation between spectral slope and asteroid size was found. The authors argued that this 46 could be the result of a size dependent surface composition where the P-types dominate at larger sizes. 47 A possible explanation is given by their mutual collisions, if D-types are more fragile than P-types, this 48 will favor disruptive collisions among D-type precursors. In this case, a larger fraction of the smaller body 49 population can be collisional fragments from a few shattered large D-type precursors resulting in a large 50 fraction of small D-type asteroids, as observed. 51

Investigations on Cybele asteroids composition have been carried out by Lagerkvist et al. (2005). They obtained visible spectra of 20 Cybele asteroids and found that the D-type Cybele objects tend to be smaller than P- and C-type objects, which is similar to the aforementioned behavior for the Hilda group. Additionally, they note the presence of one large S-type among the Cybele objects and a larger fraction of C-types than in Hilda population.

The results of Dahlgren et al. (1997) were obtained using reflectance spectra of asteroids with absolute magnitude $H_V < 11.3$, which means diameters D > 35 km assuming an albedo of $p_V = 0.05$, and the results of Lagerkvist et al. (2005) were obtained using reflectance spectra of Cybele asteroids with absolute magnitude $H_V < 11.9$, which means D > 20 km assuming the same p_V . Both samples correspond only to the large end of the size distribution of the Cybele and Hilda asteroids.

Gil-Hutton and Brunini (2008) and Gil-Hutton and Licandro (2010) searched for photometric data of Hilda and Cybele asteroids, respectively, in the Moving Object Catalogue of the Sloan Digital Sky Survey to find the spectrophotometric characteristics of small members of both groups. They found that the correlation between size and spectral slope previously suggested for Hilda and Cybele asteroids was correct only for large objects (H < 12) but it was not supported by data obtained from the small ones. The authors propose that the observed trend could be the result of a combination of the space weathering and resurfacing due to a collisional process modified by a truncation of the population size distribution.

While several tens of visible spectra of Cybele and Hilda asteroids have been published, there are only a few of them in the near-infrared region. Dumas et al. (1998) reported spectra of 1 Cybele and 8 Hilda ⁷¹ asteroids in the 0.8-2.5 μ m spectral region together with the spectra of another 9 low albedo asteroids. The ⁷² selected targets belonged to the P- or D-types in the taxonomy classification of Tholen (1984), all objects ⁷³ presented slightly red and featureless spectra.

Recently, Takir and Emery (2012) published spectra of 6 Cybele and 3 Hilda asteroids among 28 primitive 74 asteroids with a semi-major axis of 2.5 - 4.0au covering the $0.5 - 4.0\mu$ m region, aiming to examine the 75 distribution and abundance of hydrated minerals (any mineral that contains H_2O or OH associated). They 76 identified four groups on the basis of the shape and band center of the 3 μ m feature: (1) the "sharp" group, 77 that exhibits a sharp 3 μ m feature, attributed to hydrated minerals (phyllosilicates); (2) the "Ceres-like" 78 group, that like asteroid Ceres, exhibits a 3 μ m feature with a band center of ~ 3.05 which is superimposed 79 on a broader absorption feature from 2.8 to 3.7 μ m; (3) the "Europa-like" group, that exhibits a 3 μ m 80 feature with a band center of $3.15 \pm 0.01 \,\mu\text{m}$; (4) the "rounded" group, that are characterized by a rounded 81 shape feature, attributed to H_2O ice already identified in the infrared spectra of (24) Themis (Campins 82 et al., 2010; Rivkin and Emery, 2010), (65) Cybele (Licandro et al., 2011) and (107) Camilla (Hargrove 83 et al., 2012). Unlike the sharp group, the rounded group did not experience aqueous alteration. In the Cybele group, five out of six objects presented a 3.0 μ m band that were classified in the "rounded" group, 85 only one belonged to the "sharp" group. While in the Hildas there were three in the "rounded" group and 86 one in the "sharp" group. 87

Table 2: Asteroids observational conditions - IR

Number	Name	Date	UT	Airmass	m_v	α	T_{EXP}	Slit	SA*
		start				(o)	sec	(")	
190	Ismene	2001-08-04	01:00:32	2.0	14.6	10.5	$30 \ge 4$	1.5	5
		2001-09-01	22:21:33	1.2	15.2	11.1	$60 \ge 8$	1.5	2
334	Chicago	2001-08-05	06:45:30	1.3	14.6	13.7	$50\ge 4$	1.5	$2,\!5,\!4$
1202	Marina	2001-08-05	04:46:41	1.5	14.9	5.7	$30 \ge 8$	1.5	$2,\!5,\!4$
1269	Rollandia	2001-08-05	06:30:06	1.1	15.7	14.2	$50\ge 4$	1.5	$2,\!5,\!4$
1754	Cunningham	2001-08-05	05:29:15	1.1	15.8	12.6	$50\ge 4$	1.5	$2,\!5,\!4$
2067	Aksnes	2001-08-31	21:51:18	1.6	17.8	12.2	$60 \ge 8$	1.5	2
		2001-09-01 195	21:57:56	1.6	17.8	12.3	$60 \ge 4$	1.5	2
2624	Samitchell	2001-09-29	01:06:48	1.3	16.2	7.8	$60 \ge 4$	1.5	2
3557	Sokolsky	2001-08-05	05:07:45	1.1	16.5	18.9	$50\ge 4$	1.5	$2,\!5,\!4$
3561	Devine	2001-08-05	05:50:33	1.2	16.9	12.8	$50\ge 4$	1.5	$2,\!5,\!4$
4317	Garibaldi	2001-09-30	03:15:38	1.1	17.0	9.5	$60 \ge 8$	1.5	$2,\!5,\!4$
5368	Vitagliano	2001-09-30	03:43:34	1.2	17.3	12.8	$60\ge11$	1.5	$2,\!5,\!4$
5661	Hildebrand	2001-09-29	23:43:08	1.2	15.9	6.4	$60 \ge 41$	1.5	$2,\!5,\!4$
5711	Eneev	2001-09-29	01:26:39	1.3	16.1	7.0	$60\ge10$	1.5	2
6237	Chikushi	2001 - 10 - 05	23:12:22	1.2	17.3	3.6	$60 \ge 8$	1.5	$2,\!4,\!3$
9121	Stefanovalentini	2001 - 10 - 05	20:32:34	1.4	17.1	10.8	$60 \ge 8$	1.5	$2,\!4,\!3$
11750		2001-10-06	05:41:49	1.2	18.5	8.8	$60\ge 32$	1.5	2,4,3
15417	Babylon	2001-10-05	21:37:36	1.4	17.7	9.3	$60\ge 20$	1.5	$2,\!4,\!3$
15505		2001-10-06	04:55:42	1.0	18.1	9.5	$60\ge 24$	1.5	2,4,3
15540		2002-04-26	05:36:33	1.2	17.9	12.6	$60\ge 8$	1.5	1,2,5

*Solar Analogs: (1) L102-1081, (2) L110-361 (3) L98-978, (4)L93-101, (5) 112-1333

Even though the spectral analysis of the 3.0 μm region can provide a clue to the presence of water ice 88 or hydrated minerals on a primitive asteroid surface, in the visible and near-infrared regions (up to 2.4 μ m) 89 the lack of specific spectral features prevents an unique compositional interpretation. Even if weak minor 90 absorption bands has been reported in these regions, their interpretation is not clear (Mothé-Diniz, 2010). 91 At present, the general outline for the composition of these asteroids is a mixture of organics, anhydrous 92 silicates, opaque materials and ice (Bell, 1989; Gaffey et al., 1989; Vilas et al., 1994). It is very difficult to 93 define the composition of these objects since no analogous meteorites for P-type asteroids has been found 94 and there is only one analogous meteorite for D-types: the Tagish Lake, a very red and opaque meteorite 95 (Hiroi et al., 2001). 96

Considerable interest in studying the Hilda and Cybele populations is also due to their possible relation with dormant comets (Licandro et al., 2008). Di Sisto et al. (2005) shows that a considerable amount of the Jupiter family comets could have actually been originated from the Hilda population.

Planetary migration models, such as the Nice model (Gomes et al., 2005; Morbidelli et al., 2005; Tsiganis 100 et al., 2005), posit that a strong dynamical evolution would have occurred in the early Solar System, mainly 101 due to interactions between Jupiter and Saturn. In particular, the Hilda and Cybele populations would 102 be directly affected by the orbital configuration and evolution of the giant planets. Such a scenario would 103 destabilize the Jovian Trojan and Hilda populations, repopulating them later during the same phase of the 104 dynamical evolution with planetesimals scattered inward from the region beyond the ice giants (Gomes et al. 105 2005; Roig and Nesvorný, 2015; Morbidelli et al., 2005; Brož and Vokrouhlický, 2008). The Cybele asteroids 106 are the last stable region of the main belt, before the resonant populations. Levison and Duncan (1993) 107 showed that some objects originating in the primitive trans-Neptunian belt may have also been inserted in 108 the outer regions of the main belt, during the same period. From these models, therefore it is expected that 109 Hilda and Trojan's populations show a similar compositional distribution, while the Cybele group should 110 present a broader distribution of surfaces since it would have objects with origin both in the main belt and 111 in the trans-Neptunian belt. 112

In this paper we present new spectroscopic data of Cybele and Hilda asteroids in the visible and near-IR. We also analyze the visible and near-infrared (near-IR) spectra in the literature. In section 2 we describe the observation and reduction processes, and in section 3 the parametrization and analysis. The results for the spectroscopic analysis are presented in section 4. In section 5 we perform an extended analysis using data of Hilda and Cybele groups available in large public databases, such as SDSS and NEOWISE. The

discussion of our results is presented in section 6, and finally the conclusions on section 7



Figure 1: Result from wavelet technique to filter out fringing effects from the spectra using grating 300 l/mm. Top image shows the spectrum of (790) Pretoria; Middle image shows the spectrum after wavelet filtering and bottom image the residuals.

¹¹⁹ 2. Observation and data reduction

120 2.1. Visible

We collected low-resolution spectra of 18 asteroids in the Cybele and Hilda populations (Table 1). The 121 data were obtained through the Goodman High Throughput Spectrograph (GTHS) at the 4.1m SOAR 122 telescope on Cerro-Pachón, Chile. We used a setup with the grating of 300 lines/mm and the slits of 123 1.03" in 2011 and 1.68" in 2012 with no second order blocking filter, which provides an effective spectral 124 interval of 0.4-0.87 μ m. Observations were made in a total of 6 nights, split in semesters 2011A and 2012B. 125 We also obtained two sequences of calibration quartz lamps, just before and after the acquisition of the 126 target. Acquiring them with the same configuration as the target enabled us to account for flexures of the 127 instrument. At least one solar analog was observed during each night, at different airmasses. 128

The quartz lamps were used to do the flat-field correction of the images, while the HgAr lamps were used for the wavelength calibration. We applied standard reduction techniques: images were bias and flat-field corrected using quartz lamp flat. In sequence, the sky background was subtracted and each one-dimensional spectrum was extracted with variable aperture, depending on the conditions of the night. The spectra were wavelength calibrated with HgAr lamps. This procedure was repeated for the three sub-exposures of each target. The spectra were then averaged to produce a final object spectrum.

To obtain asteroid reflectance spectra, we divided the object spectrum by the spectra of Solar Analogs. 135 Before comparing the spectra of the target with the spectra of the solar analogs to remove the signature of 136 the Sun, we analyzed the spectra of the standard stars to detect small differences in color introduced during 137 the observations, e.g. by inconsistent centering of the star in the slit. These differences could propagate into 138 the spectrum of the target through the reduction process. To quantify these errors, we divided, for each 139 night, all of the spectra of the solar analogs by one that we take as reference (the one at lower airmass), after 140 applying an atmospheric extinction correction. The extinction of the sky is dependent on the wavelength, 141 with shorter wavelengths experiencing greater extinction. To minimize the spectral extinction effect from 142 the difference in airmass between the stars and the target, we applied color correction to the spectra of 143 the object and the stars. In the absence of extinction coefficients for Cerro Pachón, we used the mean 144 extinction coefficients for La Silla, since this observatory is located relatively close and at similar altitude 145 from Cerro Pachón. A study of the variation of extinction coefficients from different sites suggested the 146 extinction is mostly influenced by the altitude of the site. The result of dividing the spectrum of a solar 147 analogs by another should be a straight line with spectral slope S' = 0. This procedure enable us to discard 148 observations of stars with a bad behavior induced by systematic errors and estimate the error in the slope. 149 Finally, all reflectance spectra were normalized to 1 at 0.55μ m. 150

The data reduction was made by combining scientific Python with $IRAF^{1}$ tasks, called through the PyRAF² library.

¹⁵³ 2.1.1. Fringing correction

The final spectra presented a strong fringing pattern towards the red part of the spectrum. The pattern is still noticeable even after the flat field correction. In order to attenuate this fringing contribution, we applied a wavelet technique based on Mallat (1999). This type of algorithm is typically used for signal denoising, i.e. decreasing the intensity of high frequencies in the wavelet decomposition. Our approach was to establish a bandpass algorithm that decrease intensity of medium-high frequencies, without removing the high frequencies (noise). We applied a coiflet wavelet with hard thresholding with an up and low threshold. A typical result is shown on Figure 1.

161 2.2. Near-infrared

Low resolution near-infrared spectra were taken with the 3.56 m Telescopio Nazionale Galileo (TNG) using the low resolution mode of NICS (Near Infrared Camera Spectrograph), based on an Amici prism

 $^{^{1}}$ IRAF is distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.

 $^{^{2}}$ PyRAF is a product of the Space Telescope Science Institute, which is operated by AURA for NASA.

disperser that covers the 0.8-2.4 μ m region (Oliva 2000). The slit was oriented in the parallactic angle, and we used differential tracking that follows the asteroid motion. The width of the slit used was 1.5" and corresponds to a spectral resolving power R ~ 34 quasi-constant along the spectra. The observational method and reduction procedure followed that described in Licandro et al. (2002a).



Figure 2: Visible spectra of Hilda and Cybele asteroids, acquired with GHTS-SOAR during the campaigns presented in this work. All spectra were normalized to unity at 0.55 μ m

The acquisition consisted of a series of short exposure images in one position of the slit (position A) 168 and then offsetting the telescope by 10" in the direction of the slit (position B), and obtaining another 169 series of images. This process was repeated and a number of ABBA cycles were acquired. The total on-170 object exposure time is listed in Table 2. The two-dimensional spectra were extracted, and collapsed to 171 one dimension. The wavelength calibration was performed using a look-up table which is based on the 172 theoretical dispersion predicted by ray-tracing and adjusted to best fit the observed spectra of calibration 173 sources and telluric absorptions. To correct for telluric absorption and to obtain the relative reflectance, 174 several G2 stars from the list of Landolt (1992) were observed during the same night at airmass similar to 175 that of the asteroids. These Landolt stars have been observed on previous nights together with the solar 176 analogue star P330E (Colina & Bohlin 1997) and they are intensively used as solar analogs. 177

Finally, the spectra of the asteroids were divided by the spectra of the solar analogue stars, and the so obtained reflectance spectra averaged, obtaining the final reflectance spectrum of each object. Sub-pixel offsetting was applied when dividing the two spectra to correct for errors in the wavelength calibrations due to instrumental flexure. By comparing the reflectance spectra of the same asteroid obtained with different solar analogues we determined that the uncertainty in the slope is smaller than $1\%/0.1 \ \mu$ m.



Figure 3: (a) - Parametrization for visible spectra in asteroid (940) Kordula. We measure four features: Visible Slope, UV-slope, Turn-off point (red lines) and the Hydration band (green lines) (b) - Parametrization schema for near-IR spectra in asteroid (1269) Rollandia. Some spectra present a turn in the slope towards the red. We identify this behavior by measuring two slopes: IR-slope1 is measured in the 1.0-1.75 μ m interval, while IR-slope2 in the 1.95-2.3 μ m.

183 3. Analysis

184 3.1. Visible

¹⁸⁵ We present nine spectra of Hilda asteroids and nine spectra of Cybele asteroids (Figure 2). All of them ¹⁸⁶ (but one) are red, only (225) Henrietta shows a blue spectral slope. The majority of them are featureless, ¹⁸⁷ only (940) Kordula shows a broad absorption band centered at 0.7 μ m (Figure 3). While, Some of them ¹⁸⁸ also show a clear drop of reflectance bellow 0.5 μ m.

For the characterization of these spectra we defined 4 parameters (Figure 3): the presence of a 0.7 μ m absorption band, the visible slope, the presence of a turn-off point around 0.5 μ m and, in case of the existence of the turn-off point, we also measure the near-ultraviolet (near-UV) slope. We also determined the taxonomic classification of these objects in the Bus and Binzel (2002) scheme.

In order to increase the sample for the statistical analysis of the populations we collected visible spectra 193 of Cybele and Hilda objects in the literature. From the spectroscopic surveys S3OS2 (Lazzaro et al., 2004). 194 SMASS (Bus and Binzel, 2002) and Vilas et al. (1998), we gathered: 5 spectra from each dataset for the 195 Hilda group, and 35,11,15 for the Cybele group, respectively. We also added 30 spectra from Dahlgren et al. 196 (1997) and Dahlgren and Lagerkvist (1995) for the Hilda population; and 18 spectra from Lagerkvist et al. 197 (2005) for the Cybele population. Therefore, the total sample of visible data consists in 88 spectra of 55 198 objects for the Cybele population and 54 spectra of 37 objects for the Hilda population. It is important to 199 note that the spectral coverage of these works are slightly different from the one obtained with GHTS-SOAR; 200 S30S2 has a spectral coverage of 0.5-0.9 μ m; SMASS of 0.4-0.9 μ m; Vilas 0.5-0.9 μ m; Dahlgren et al. (1997) 201 and Dahlgren and Lagerkvist (1995); 0.4-0.9 μ m or 0.4-0.7 μ m, and Lagerkvist et al. (2005) of 0.4-0.9 μ m. 202

All literature spectra were re-analyzed with the aforementioned parametrization, for the sake of homogeneity, although due to the varying spectral coverage, there are cases where some of the parameters could not be measured.

206 3.1.1. Taxonomy

The taxonomic classification was made using the on-line tool for modeling spectra of asteroids, M4AST (Popescu et al., 2012). We first performed a polynomial adjust, with varying order, that represents the spectrum of the asteroid. Then, the tool compared this fit to templates of each class defined by the DeMeo et al. (2009) taxonomy at the corresponding wavelengths. The adopted taxonomic class is the one with the



Figure 4: Near-IR spectra of 20 Hilda objects, observed at 3.6m TNG. Some of the objects were observed more than once.

smallest chi-squared. Then we checked the classification of all objects and for the specific targets where the taxonomic result is related to one feature that does not appear in the wavelength range of study, we reclassified them in the Bus and Binzel (2002) taxonomy in cases where the result was an specific class of the DeMeo et al. (2009).

215 3.1.2. Visible slope

Given that these are primitive asteroids, the majority of them are featureless, i.e. they show no absorption bands in their visible spectra. The only feature that can be measured in all asteroids of this sample is the visible spectral slope.

To calculate the slope, we follow the definition of the spectral gradient (S') in Jewitt (2002). We make a liner fit to the spectrum in the wavelength range 0.55 - 0.86 μ m, where the reflectance is well represented by a linear fit. We normalize the fit by the mean value of the reflectance in the adopted range, in units of %/1000Å.

The systematic error in the slope is estimated by the standard deviation of the distribution of slopes 223 calculated in the solar analogs analysis, as explained in section 2.1. Unfortunately, for the majority of the 224 spectra in the literature, we have no information on the systematic error associated with the solar analogs. 225 In this case, we assumed a systematic error of 1%. Another source of error is the computation of the slope. 226 To estimate this, we performed a Monte-Carlo model to fit the slope of the asteroid, by doing a thousand 227 iterations, and removing randomly 20% of the points, the error assumed is the one-sigma of the distribution. 228 The final error of the slope, included in table 3 is the quadratic sum of the systematic and the Monte-Carlo 229 produced errors, and is strongly dominated by the systematic one, specially with a high signal to noise 230 regime. Whenever an asteroid is observed more than once, we take the mean value for the slope and the 231 error is chosen between the standard deviation of the mean or the error propagation, whichever is higher. 232

$_{233}$ 3.1.3. Hydration: The 0.7 μm band and the turn-off point

The presence of aqueously altered minerals on asteroid surfaces can be inferred by the presence of a shallow absorption band centered at $0.7\mu m$ (See figure 3, panel a). This band is strongly correlated with the unambiguous hydration indicator, the 3.0 μm absorption band (Fornasier et al., 2014; Vilas et al., 1994).

We search for the presence of this feature in our sample applying a methodology similar to the one in 237 Carvano et al. (2003) and Morate et al. (2016). First we calculate the continuum with a linear fit within the 238 0.55-0.58 and $0.83-0.86 \ \mu m$ intervals. We then divide the spectra by the continuum, and fit a fourth-order 239 spline in the 0.58-0.83 μ m range. For objects that present the feature, we characterize its depth and central 240 wavelength. It is important to note that the aqueous alteration absorption band is centered around 0.7 μ m. 241 Objects with spectra like (401) or (1144) present a concave spectra (Figure 2), that could be explained by 242 the presence of an absorption band, but not centered near 0.7 μ m, but, at much lower wavelengths, where 243 no hydration band is expected. We therefore do not include these objects in the list of aqueously altered 244 asteroids. 245

For the error estimation we ran a Monte-Carlo model with 1000 iterations, randomly removing 20% of the points, and measured the band depth at each iteration. The final value for the band depth is the center of the resultant distribution and the error is the variance.

Another possible indicator of hydration is a decrease in reflectance shortward of 0.5 μ m. Vilas (1995) states that the reflectance spectra of asteroids believed to contain iron-bearing silicates in their surface materials show a strong UV absorption feature believed to be caused by a a ferric oxide intervalence charge transfer transition (IVCT) centered in the UV. C-, B-, and G- generally exhibit a spectral turnover near 0.5 μ m. It is believed that the presence of opaque materials in the surface of the low-albedo asteroids masks this IVCT in the 0.5-0.75 μ m region and slightly lowers the absorption in the blue/UV spectral region.

We will refer to the presence of this feature by the characterization of the "turn-off point". First we perform a linear fit using just ten points at the beginning and at the end of the spectral coverage. Then we measure the distance between the spectral points and the fit over all the spectral coverage (red line in Figure 3-a). The distance of the farthest away point should surpass a minimal value of 3.5% to consider the turn-off. This threshold was defined by trial and error and visual analysis.

260 3.2. Near-Infrared

Figure 4 shows the 20 near-IR spectra of 19 Hilda asteroids. All objects present a red near-IR spectra with no strong absorption, except for a slope change towards redder wavelengths in some cases, e.g. (1269), (2624) and others. A similar behavior was observed in the near-infrared spectrum of the meteorite Alias (Cloutis et al., 2011a), a CI-class meteorite, and in a few CM-class meteorites (Cloutis et al., 2011b).
 The authors explained the feature with the presence of the mineral Berthierine, a phyllosilicate from the serpentine group.

The same methodology described in sections 3.1.1 and 3.1.2 were used for the taxonomic classification and slope calculation. We choose to calculate the near-IR slope in two separate intervals: IR-slope1 in the 1.0-1.75 μ m range; IR-slope2 in the 1.95-2.3 μ m range. Objects with slope variation higher than 1.5 %/1000Å are considered to present a turn-off in the near-infrared spectrum, around 1.9 μ m. We excluded the 1.35-1.45 and 1.75-1.95 μ m regions, due to the strong noise caused by Earth's atmosphere absorption.

We searched the literature in order to increase our sample and extend the near-IR analysis to the Cybele group. We collected 4 spectra from SMASSII, 9 from Takir and Emery (2012) and 2 from Reddy et al (2016). The final sample contains an amount of 40 spectra for 31 objects in the Hilda population and 9 spectra of 6 in the Cybele.

The slope error for objects in our sample is described in section 2.2 In this case all the errors are assumed to be 1%/1000A plus the Monte-Carlo produced error, applying the same methodology as in section 3.1.2. For objects with more than one observation the slopes are averaged and the error is chosen between the standard deviation or the propagated error, whichever is higher.

280 4. Results



Figure 5: Visible spectral slope versus diameter for Hildas (*left*) and Cybele (*right*) populations. Grey stars are SDSS slopes while black points are spectral slopes.

The results for the analysis of the visible spectra are shown in Table 3 for Cybele and Hilda objects of our sample and in table 4, for the Cybele and in table 5 for the Hilda objects in the literature. Features that could not be measured due to the spectral interval are marked with a star ('*') symbol, and where it could be measured, but the feature was not detected with a dash ('-') symbol.

For an extended analysis, we add information optical geometric albedo and diameters, obtained from the current release of the NEOWISE dataset (Mainzer et al.) [2016). Tables 8 and 9 list proper elements (Nesvorny, 2015) and geometric albedo for the objects in our Cybele and Hilda samples, respectively.

Figure 5 shows the scatter plots of spectral slope versus diameter for the Cybele and Hilda objects. The enlarged samples show a trend that had been previously noted by other authors Lagerkvist et al. (2005) and Dahlgren et al. (1997), in which the larger objects in those populations tend to present intermediate values for the spectral slope, and that the scatter in that parameter increases for smaller diameters.

The bottom panels of Figure 6 shows the histograms of spectral slope for the Cybele and Hilda asteroids. On both populations it is possible to detect a bimodality on the spectral slope distribution, which had also



Figure 6: Top: Albedo-Slope distribution of Hilda and Cybele asteroids. The blue squares represents the clusters as described in section [5] using the SDSS and WISE data. Yellow points are objects with UV-drop, green are objects with 0.7 μ m absorption band, and red are objects that present both features. *Bottom*: Histogram for visible slope distribution in the dynamical groups. Red lines represent Gaussian fitted profiles for the bimodal distributions.

been pointed out in the literature (Gil-Hutton and Brunini, 2008; Gil-Hutton and Licandro, 2010). On 294 the top panels of this figure we show scatter plots of geometric albedo versus spectral slope. It is possible 295 to assure the presence of two clusters: the first, centered at ~ 4.2%/1000Å, consists of X-class asteroids, 296 while the redder group, centered at $\sim 9.4\%/1000$ Å, is dominated by the D-class. For the Cybele group, 297 the first cluster is centered at $\sim 2.3\%/1000$ Å, with a mix of the C-class and X-class objects, with a clear 298 separation for the redder D-class, centered at $\sim 8.8\%/1000A$. On both groups the clusters with higher 299 spectral slopes tend also to present slightly higher albedo than the clusters with lower spectral slope. Bauer 300 et al. (2013) and Duffard et al. (2014) observed a similar behavior in the Centaur population, which also 301 present a bimodal color distribution. Although, it is worthy to notice the redder group in the Centaur 302 population is substantially redder than a typical D-type asteroid. 303

The Cybele group shows a wider variety of colors and taxonomic classes, but predominantly primitive classes (see Tables 4 and 5). We stress the presence of two S-type objects: (679) Hippodamia with a diameter D = 42 km and (3675) Kemstach with D = 18 km, according to NEOWISE data. Gil-Hutton and Licandro (2010) showed other five potentially S or Q-types with SDSS data, although these are smaller objects.

It is also important to note the distribution of objects with signs of hydration in the Cybele and Hilda 309 groups. The 0.7 μm absorption band is only detected in seven of the 55 Cybele asteroids, and none is 310 observed within the Hildas. All but one are C-class objects (940 is a Xc). The UV-drop is detected in 311 six Cybele objects, and only one Hilda: (334) Chicago. There are two Cybele objects that present both 312 features, (121) Hermione and (168) Sibylla. The asteroids (334) and (121) are the only objects in the Hilda 313 and the Cybele group, respectively, in Takir and Emery (2012) to show a "sharp" shape for the 3 μ m feature, 314 which is also associated to the presence of hydrated minerals. For objects that present the turn-off, we also 315 measured the UV-slope. Since only a small amount of objects presents this feature, no relevant information 316 was found for the UV-slope. 317

The results for the near-IR analysis for TNG spectra are presented in Table 6 and in Table 7 for the literature Hilda and Cybele objects. The majority of objects in the Hilda group present a reddish IRslope1 and are classified as D-type objects. No D-type is observed in the Cybele group (consisting of six objects), however, this is somehow to be expected. According to DeMeo and Carry (2013), the dominant class for objects larger than 100 km is the P-type (equivalent to the X-type for our purpose), with very small contribution from D-type. In our sample, five out of six objects are larger than 150 km, therefore the absence of this class in our sample is consistent with the previous results. Figure 7 suggests that the clusters in the near-infrared slope reflect in the albedo distribution, redder objects tends to higher albedo, accordantly to the behavior in figure 6. Objects with a significant difference from IR-slope1 to the IR-slope2 (higher than 1.5 %/1000Å) are observed in both groups.

³²⁸ 5. Extended analysis with large public datasets

In this section we use data from large public databases in order to interpret our spectra within the 329 broader context of the distribution of physical properties of the objects in the Cybele and Hilda regions, 330 and then compare them with the physical properties of the objects in the inner edge of the 2:1 resonance, 331 and also with the Trojan population. For spectral slope and taxonomic classification we use data from 332 the Sloan Digital Sky Survey Moving Object Catalog (Ivezic et al., 2010) that were classified by Carvano 333 et al. (2010) and Hasselmann et al. (2011) into a taxonomic scheme designed to be compatible with the 334 Bus classification, within the limits imposed by the spectral resolution of the SDSS data. Optical geometric 335 albedo and diameter were obtained from the current release of the NEOWISE dataset (Mainzer et al., 2016), 336 and lists of members of the dynamic asteroid families in the regions were taken from Nesvorny (2015) 337

To calculate the spectral slope from the asteroid reflectance spectra listed in Hasselmann et al. (2011) in 338 a way that is compatible with the procedure described in section 3.2.2 we made a linear fit to the reflectances 339 in the q, r, and i SDSS filters (centered at 0.47, 0.62 and 0.76 μ m), normalized to q. To calculate the slope 340 uncertainties we created 1000 clones of each observation by drawing random values for the reflectance in 341 each filter using normal distributions with means equal to the listed reflectance value and variances equal 342 to the listed uncertainties. The resultant spectral slope distribution was then fitted with a Gaussian curve, 343 whose mean and variance were then adopted as the final value for the spectral slope and its uncertainty, 344 respectively, expressed in units of %/1000Å. 345

Using 3.3 < a < 3.7 au and 3.7 < a < 4.5 au to define Cybele and Hilda groups, we obtained a total of 255 asteroids listed in Nesvorny (2015) in the Cybele and 297 in the Hilda region with SDSS observations. Of these, 179 objects in the Cybele and 208 in the Hilda region also had tabulated albedos and diameters from Mainzer et al. (2016). Nesvorny (2015) defines two families in the Cybele region, Sylvia and Ulla, and two in the Hilda region, Hilda and Schubart. In the Cybele families there were 20 objects from Sylvia and 2 from Ulla with both SDSS data and NEOWISE albedo. Similarly, 58 from Hilda and 31 from Schubart,



Figure 7: Albedo *versus* IR-slope1 for Hildas (dots) and Cybele (square) objects. Asteroids that show a decay towards redder wavelengths are labeled in blue.



Figure 8: Histogram for Hilda and Cybele populations with SDSS data. Blue histogram show groups with families removed

in the Hilda region. Rejecting the object with indication of olivine/pyroxene absorption bands (members of
 the S complex), we are left with 177 objects in the Cybele region with slope and albedo, and 118 objects in
 the Hilda region.

In order to compare with the inner and outer edge of the Cybele and Hilda populations, we also consider the slope and albedo distributions for the Trojans and for the members of the Themis family. The later is taken here as representative of the material of the inner border of the 2:1 mean motion resonance with Jupiter. We consider 575 and 330 objects with both albedo and slope from Themis dynamical family and Trojans, respectively.

Figure 8 shows the slope distribution of the featureless asteroids on Cybele and Hilda populations, with and without family members. The distribution of slopes in these regions are clearly bimodal, as discussed in the previous section. The Hilda and Schubart dynamical families contributed strongly to the peak at lower spectral slopes, but an excess of objects with small spectral slopes remain even after the removal of the listed family members. On the other hand, the removal of nominal family members does not affect significantly the slope distribution in the Cybele region. In what follows thus we will remove members of the families from the Hilda region, but we will keep the family members in the Cybele region.

These characteristics on the slope and albedo distribution on both populations had already been reported 36 and discussed (Wong and Brown, 2017; Kasuga et al., 2012; Grav et al., 2012; Ryan and Woodward, 2011; 368 Gil-Hutton and Licandro, 2010; Gil-Hutton and Brunini, 2008), but no extensive analysis of the joined 369 distributions of these two compositional indicators had been performed in the literature so far. To do so, 370 we use scatter plots of slope versus albedo to construct weighted density plots. This is done by considering 371 that each measurement of both albedo and slope defines a gaussian function with a mean value equal to the 372 measured value and variance equal to its uncertainty, with the total density at each possible value of slope 373 and albedo given by the sum of the gaussians of all measurements. Peaks on these density plots correspond 374 thus to the probability of finding members of each population on given points of the slope-albedo space. 375 Figure 9 shows the scatter and density plots for all populations. A number of clusters can be seen on the 376 density plots. In the Cybele region (Fig. 9) the bimodality is apparent in the albedo-slope space. The lower 377 slope peak clearly defined against the lower density cluster at higher slopes. The cluster at lower slopes 378 concentrated a slightly lower albedos than the higher slope clusters. Also, the lower slope peak appears to 379 consist of two subclusters that were not distinguishable from the spectral analysis (Section 4, Fig. 6), the 380 most dense concentrated at lower spectral slopes and slightly higher albedos than the less dense one. In 381 the Hilda region the slope bimodality is also apparent on the density plots, with the lower spectral slope 382 population also appearing at slightly lower albedos than the higher slope population that dominates the 383 region, though the removal of the objects that belong to a collisional family vastly diminish the population 384 of objects in the first cluster. Again, in the Trojan region (Figure 9) the bimodality on slopes also seem to 385



Figure 9: Scatter and density plots for Themis collisional family, Cybele, Hilda and Trojan populations

correlate with albedo, but with the lower slope group having higher albedos than the dominant higher slope

387 group. Finally, the Themis family plots as a dense single cluster in the slope-albedo space.



Figure 10: Weighted averages and standard deviation for p_v and *slope* of objects in the Themis family and on the Hilda, Cybele and Trojan region. Sizes on scatter plots are related to proportion of member in each cluster, for each population.

We then proceed to define limits for each cluster. This is done visually, using the density plots (Fig. 388 9). For Cybele and Hilda populations this can be done simply by defining limits in slope for each cluster. 389 The three main groups in the Cybeles are thus defined with S' < 2.5, 2.5 < S' < 7.5%/1000Å, and 390 S' > 7.5%/1000Å. The two clusters in Hilda group can also be defined using 7.5%/1000Å as limiting value. 391 The Trojans, on the other hand, are better separated by a straight line given by $p_v = 0.055 - 0.1575(S' - 7)$. 392 We can then calculate the weighted average for p_v and *slope* for each cluster and the corresponding standard 393 deviations (Table 10). Figure 10 shows the distribution of these clusters. Given that those clusters are defined 394 mostly by ranges in the spectral gradient, they can be associated loosely with the equivalent Tholen's classes, 395

³⁹⁶ in order to facilitate the qualitative comparison with previous works. Therefore we will be referring to the ³⁹⁷ lower slope clusters as "C-cluster", to the the intermediate slope cluster as "P-cluster" and the higher slope ³⁹⁸ clusters as "D-cluster". In Figure ⁶ we show the specific clusters of the Cybele and Hilda groups (blue ³⁹⁹ boxes) for a comparison with the spectroscopic data analysis. Although these clusters are defined visually ⁴⁰⁰ we can see they correlate to the boxes defined in figure 5 of DeMeo and Carry (2013) for the C, X and D ⁴⁰¹ types.

Table 10: Weighted averages and standard deviation for p_v and *slope* of clusters in the Themis family and on the Hilda, Cybele and Trojan region.

Population	Cluster	ρ_g	$\rho_{g(std)}$	S'	S_{std}'
Themis	С	0.066	0.021	0.63	1.64
Cybele	\mathbf{C}	0.059	0.014	1.03	0.92
Cybele	Р	0.055	0.023	4.35	1.18
Cybele	D	0.072	0.026	10.86	2.03
Hilda	Р	0.057	0.020	4.65	1.83
Hilda	D	0.062	0.017	11.17	1.86
Trojan	PD	0.090	0.027	6.32	2.04
Trojan	D	0.064	0.013	11.71	1.83

402 6. Discussion

The joint analysis of the spectroscopic data, which represents larger objects, and spectrophotometric data, for small objects, reveals the diversity of surfaces in each group. We found two clusters in the albedo versus slope space of the Hilda group and three in the Cybele group. Although the subdivision of the lower slope cluster is only apparent using the larger SDSS sample. The bimodality is also observed in near-infrared properties. Each of this clusters might be related to different sets of compositions or processes that alter the surface of the asteroids, such as resurfacing and space weathering.

The larger variety of taxonomic classes, colors and albedo distribution reflects a wider range of possible compositions for the Cybele asteroids than Hilda asteroids. The presence of high-albedo objects ($\rho_g > 0.1$) and even S-type asteroids among them suggest a contribution of objects formed in closer to Sun than their current positions.

The presence of two high-albedo objects among the Hilda also suggests that there is some contribution 413 from the main belt objects to the population, as proposed by Grav et al. (2012). We investigated if the high 414 albedos of these two objects can be explained by possible biases in their radiometric diameters and/or H 415 magnitudes. (1162) Larissa has two groups of thermal IR observations by WISE (Mainzer et al., 2011) and 416 also by AKARI (see Usui et al. (2011)), so we recomputed diameters using the NEATM implementation 417 of Alí-Lagoa et al. (2016). Our fits to all four groups of observations are very similar to those reported by 418 NEOWISE, and the albedos remain higher than 0.11 even if we increase the value of the H magnitude by 419 0.3 mag. We also reproduce the reported size and albedo for (3843) OISCA, but in this case we can reach 420 a reasonably lower albedo of 0.08 ± 0.02 if we increase the H-value by 0.3 mag (in fact, Vereš et al. (2015)) 421 obtained H= 10.9 ± 0.3), so the high-p_n value is less robust for this object. 422

The hydration band in the visible spectra has been shown common in primitive objects of other regions of the main asteroidal belt. Fornasier et al. (2014) finds that 45% of C-complex asteroids presents the band in contrast with 4.5% for P-type in the Tholen taxonomy. For the Cybele group, we found the absorption band in only $\sim 30\%$ of the C-types. The asteroid (940) Kordula was classified both in the Cgh and in Xc, based on the spectra obtained in this work and in Vilas et al. (2006), respectively. Figure 6 shows that these objects are mostly related to the C-cluster in Cybele group, and the object (334) Chicago is on the left edge of the P-cluster in the Hilda group.

The small amount of hydrated objects among the Cybele asteroids and single presence of the object (334) Chicago, which presents a turn-off point in the visible, and a "sharp" 3.0 μ m band (Takir and Emery).

2012), the only hydrated asteroid found in the Hilda group, points to a scenario where hydration did not 432 act strongly in these groups. In Fornasier et al. (2014), the authors analyze a dataset of over 600 spectra 433 of primitive asteroids in the literature and conclude that the aqueous alteration process is dominant in the 434 2.1 - 3.1 AU range, at smaller heliocentric distances than proposed by Vilas et al. (1994). Morate et al. 435 (2016) and Morate et al. (in prep.) shows families in the inner belt with a high amount of hydrated objects. 436 Conjointly, thermal modeling by Grimm and McSween (1993) proposes the hydration process to act in the 437 2.5 - 3.3 AU range, just before the Cybele region. Thus, the Cybele group may delimit the region where 438 aqueous alteration process could have occurred. However, it seems that the process acts predominantly at 439 smaller heliocentric distances than those at where the Cybele and Hilda groups are located, and it can not 440 be ruled out that the few hydrated objects found might also be contribution of objects originated in the 441 main-belt. 442

We confirm the trend for larger objects in both groups presenting a more neutral color. In order to explain 443 this scenario, Lagerkvist et al. (2005) and Dahlgren et al. (1997) proposed that D-types objects could be 444 more fragile than P-types, and therefore, they can be more affected by disruptive events, and would be more numerous as smaller objects. In Gil-Hutton and Brunini (2008) and Gil-Hutton and Licandro (2010), the 446 authors emphasized that the trend is not seen in the small objects, observed with SDSS. They argue in favor 447 of a combination of space weathering and resurfacing effects as the main explanation for this phenomenon. 448 Ion-irradiation experiments on samples of Tagish-Lake meteorite tends to neutralize the spectral slope in 449 the visible and near infrared spectral ranges (Vernazza et al., 2013; Lantz et al., 2017). If the surfaces of 450 D-type asteroids are optically dominated by similar materials, i.e., dark red hydrocarbon minerals, space 451 weathering effects favor the evolution to a P-type surface. On the other hand, collisional disruption or 452 collisional resurfacing would expose unweathered D-type material. Therefore they argue that the larger 453 bodies, which did not experience catastrophic disruption or significant collisional resurfacing have more 454 neutral colors, since their surfaces have been exposed to ion flux for longer times. On the contrary, the 455 observed smaller objects could be fragments of larger asteroids recently disrupted by catastrophic collisions, 456 showing fresh and more red surfaces, or have more neutral colors due to the combination of the effect 457 produced by the ion bombardment and lack of small projectiles in the population to disrupt or resurface it, 458 producing a color diversity in the observable small end of the size distribution. 459

Though, Vernazza et al. (2013) and Lantz et al. (2017) also stated that the space weathering has a 460 brightening effect on Tagish Lake samples. In opposition, we note that in visible and near-infrared spectra, 461 D-cluster objects presents slightly higher albedo than less-red objects. Carvano et al. (2003) analyzed a 462 sample of 460 featureless spectra asteroids from all regions of the main belt and found a similar behavior. 463 The ambient effects, such as space weathering and collisional resurfacing should diversify more the spectral 464 gradient in the smaller objects than in the larger ones for the reasons pointed in Gil-Hutton and Brunini 465 (2008) and Gil-Hutton and Licandro (2010), but the same trend can also be explained if there is more than 466 one compositional group in the population. 467

The red color objects are commonly hypothesized to be similar in composition to the Tagish Lake meteorite, that presents a red spectrum and a very low albedo. On Takir and Emery (2012), the authors argue that all the observed D- and P-types located in the 3.0 < a < 4.0 au region exhibit a rounded shape $3.0 \ \mu\text{m}$. They give a possible explanation for the feature with a thin layer of water frost in the surface of these asteroids. The presence of ice in the surface of the objects could also explain the higher albedo of D-types objects than Tagish Lake meteorite, though it is not clear how the presence of frost in the asteroid surface should alter the spectral slope.

To compare these groups to the neighboring populations, we analyzed the Themis and Trojan colors and 475 albedo distribution. Figure 10 shows the measured center for each cluster in the Themis family, and in the 476 Cybele, Hilda and Trojans populations. The values can be seen in Table 10. There is a clear match for the 477 three clusters in the Cybele group, which presents objects similar to those of Themis family and both groups 478 observed in the Hildas. In the Jupiter Trojans it is possible to identify that the D-cluster matches objects 479 480 with a cluster in Cybele and Hilda, but there is one group of objects which is not statistically strong in any of previous populations. We shall call it DP-cluster. Trojans DP-cluster seems to be redder and present 481 higher albedo than the P-cluster in the Hilda and Cybele groups. A Two-dimensional Kolmogorow-Smirnov 482 test rejects the hypothesis that the DP-cluster of the Trojan population comes from a similar distribution 483

 $_{484}$ of the P-cluster of the Hilda os Cybele populations, providing a p-value <<0.01.

Planetary migration models suggests a common origin to Hilda and Trojans groups. Though, despite the 485 fact that both populations presents a bimodal distribution, as also discussed in Wong and Brown (2017), 486 in the slope versus albedo space, they do not seem to be matching groups. A possible explanation is 487 that Trojans asteroids may suffer resurfacing more frequently than Hilda asteroids, and present a generally 488 younger surface. Davis et al. (2002) argues that the current intrinsic collisional probability and impact 489 velocities are significantly lower for the Hildas than for the Trojans. Though, one of the Trojans groups is 490 in good agreement with one of the Hilda clusters. Another possible explanation is that Hilda and Trojans 491 have objects of different compositions and origins. The apparent continuity of asteroids surfaces and density 492 objects from the Themis family to the Cybele, Hilda and Trojan populations may suggest a gradient of 493 composition. This scenario would impose an obstacle for planetary migration models. 494

495 **7.** Conclusions

We obtained 18 visible and 22 near-infrared spectra of Cybele and Hilda populations at the outer edge of asteroid belt, in order to study their surface properties distributions. The sample was enlarged with literature spectra, resulting in a total of 85 visible and nine near-infrared spectra for Cybele group, and 83 visible and 35 near-infrared spectra for Hilda group. The analysis was enhanced with NEOWISE and SDSS data, for information on the optical geometrical albedo and spectrophotometric properties of the small size objects in these populations. We conclude that:

• The Hilda population shows a bimodal distribution of surface properties, while in the Cybele we could identify three predominant groups of objects. The Cybele population shows a wider contribution of neutral color objects than the Hilda. The bimodality is also observed in the near-infrared analysis, where we observe a trend of redder objects showing higher albedo.

- The Cybele group presents only 9 out 55 asteroids with evidence of hydrated minerals on their surfaces, while in the Hilda group only in the object (334) Chicago the presence of aqueous altered minerals in the surface can be confirmed. Therefore, the Cybele population could possibly delimit the outer edge where the aqueous alteration process can act strongly.
- We identify a continuity of surface properties from the Themis family to the Cybele, Hilda and Trojan populations. The last two populations shows distinct distribution of surface properties. This result could be related to a compositional gradient.

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Table 3. Results for the analysis of the visible parameters in Cybele and Hilda populations for objects observed in SOAR with GHTS.

Number	$\begin{array}{c} 0.7 \ \mu \mathrm{m} \\ \mathrm{depth}(\%) \end{array}$	$\begin{array}{c} 0.7 \ \mu \mathrm{m} \\ \mathrm{Central} \\ \mathrm{wavelenght}(\mu \mathrm{m}) \end{array}$	$\begin{array}{c} \text{Turn point} \\ (\mu \text{m}) \end{array}$	Visible slope S'%/1000	Visible slope unc	Uv Slope S'%/1000	Uv Slope unc	Taxonomy	Group
225	-	-	4979.05 ± 10.96	-5.62	1.25	-2.907	0.592	В	Cybele
229	-	-	5242.28 ± 7.44	3.06	0.92	14.139	0.244	Xc	Cybele
401	-	-	-	4.01	1.26	-	-	$^{\rm Cb}$	Cybele
528	-	-	-	1.89	0.92	-	-	$^{\rm Cb}$	Cybele
790	-	-	-	2.77	0.42	-	-	Х	Cybele
909	-	-	-	2.99	1.23	-	-	Х	Cybele
940	1.81 ± 0.01	7004.11 ± 3.82	5160.79 ± 6.24	1.96	0.53	13.337	0.414	Cgh	Cybele
1177	-	-	-	2.89	0.92	-	-	x	Cybele
1280	-	-	5339.43 ± 10.70	1.55	0.42	12.909	0.247	\mathbf{C}	Cybele
6039	-	-	-	9.69	0.54	-	-	D	Cybele
334	-	-	5251.87 ± 11.34	2.87	1.23	23.125	0.622	Xc	Hilda
1144	-	-	-	11.85	0.60	-	-	D	Hilda
1269	-	-	-	9.08	0.53	-	-	D	Hilda
1439	-	-	-	3.33	0.93	-	-	Х	Hilda
1902	-	-	-	2.76	0.92	-	-	Х	Hilda
3202	-	-	-	13.63	0.56	-	-	D	Hilda
3577	-	-	-	9.33	0.53	-	-	D	Hilda
3843	-	-	-	5.04	1.25	-	-	Х	Hilda
7394	-	-	-	7.67	0.45	-	-	D	Hilda

Table 4. Results for the analysis of the visible parameters in Cybele population for objects extracted from the literature. The '*' symbol is placed when the wavelenght coverage is not suitable for measuring the determined feature, while the symbol '-' is used for indicating that the wavelengh coverage is appropriated, but the feature was not identified. References: (1) [Lagerkvist et al. (2005); (2) SMASS [Bus] and Binzel (2004); (3) S3OS2 [Lazzaro et al. (2004); (4) [Vilas et al.] (2006)

Number	$0.7 \mu m$	0.7. µm	Turn point	Visible	Цv	Taxonomy	Reference
Number	$0.7 \mu \text{m}$	C_{emtral}	(um)	visible	Slowe	Taxonomy	itelefence
	depth	Central	(μm)	siope	Slope		
	(%)	wavelenght(μm)		(S'%/1000A)	(S'%/1000A)		
65			*	0.07 ± 1.02	*	C	9
05	-	-	*	0.97 ± 1.02 2.11 \pm 1.07	*	v	3
	-	-	0.000 1.0.000	3.11 ± 1.07	7 00 1 1 50		4
	-	-	0.664 ± 0.003	0.81 ± 1.06	7.96 ± 1.56	Xk a	2
76	-	-	*	1.54 ± 1.02	*	Сь	4
	-	-	0.593 ± 0.006	1.24 ± 1.02	4.62 ± 1.92	\mathbf{C}	2
87	-	-	-	3.02 ± 1.04	-	\mathbf{Xc}	2
	-	-	*	3.66 ± 1.02	*	Х	3
107	-	-	*	2.01 ± 1.02	*	$^{\rm Cb}$	3
	-	-	0.654 ± 0.004	1.24 ± 1.06	2.45 ± 2.22	Xk	2
121	2.20 ± 0.09	0.685 ± 0.001	*	1.66 ± 1.03	*	Cgh	4
	2.32 ± 0.05	0.719 ± 0.002	0.551 ± 0.001	0.24 ± 1.06	10.99 ± 2.52	Cgh	2
1.68	1.83 ± 0.03	0.706 ± 0.011	0.552 ± 0.001	1.10 ± 1.05	3.60 ± 1.65	Ch	
1.00	1.05 ± 0.21	0.700 ± 0.011	0.002 ± 0.000	-1.13 ± 1.03	3.00 ± 1.05	Carb	2
0.05	2.30 ± 0.04	0.091 ± 0.001	*	1.01 ± 1.02 1.02 ± 1.05	*	Cgn	3
220	-	-		1.03 ± 1.05	-1-	CD	4
229	-	-	*	0.75 ± 1.02	*	Сь	3
260	-	-	*	3.11 ± 1.02	*	Xc	3
414	-	-	$0.6 {\pm} 0.002$	0.72 ± 1.05	13.15 ± 2.45	Cg	2
	1.79 ± 0.03	0.723 ± 0.001	*	1.30 ± 1.03	*	Cgh	3
420	-	-	-	6.85 ± 1.04	-	D	1
483	-	-	*	9.36 ± 1.09	*	L	4
522	-	-	-	4.46 ± 1.03	-	Х	1
	-	_	*	2.99 ± 1.02	*	x	3
528	_	_	*	1.07 ± 1.02	*	Ch	4
536	-	-		3.77 ± 1.05		v	1
550	-	-	- *	3.77 ± 1.03 2.02 ± 1.01	-	A V	1
500	-	-	*	2.95 ± 1.01	*	A	3
566	-	-		2.79 ± 1.02		A T	4
570	-	-	-	5.62 ± 1.05	-	\mathbf{T}	2
	-	-	*	11.65 ± 1.04	*	D	4
643	-	-	-	3.99 ± 1.05	-	Х	1
	-	-	*	4.81 ± 1.06	*	X	4
692	-	-	*	4.73 ± 1.09	*	\mathbf{S}	4
	-	-	*	6.12 ± 1.09	*	\mathbf{S}	3
713	-	-	-	0.97 ± 1.03	-	С	2
	1.34 ± 0.06	0.765 ± 0.001	*	1.42 ± 1.02	*	č	3
721	1.01 ± 0.00	0.1001	_	8.79 ± 1.02	_	Ď	1
121	-	-	*	6.79 ± 1.04	*	T	2
799	-	-	*	0.25 ± 1.03	*	Ch	3
133	-	-		2.15 ± 1.02		CD	4
790		-	*	3.87 ± 1.02	*	X	3
940	2.35 ± 0.10	0.69 ± 0.003	*	2.51 ± 1.03	*	Xc	4
1004	-	-	-	5.70 ± 1.02	-	Т	1
	-	-	*	4.44 ± 1.02	*	X	3
1028	-	-	*	1.25 ± 1.02	*	$^{\rm Cb}$	3
1154	-	-	*	3.67 ± 1.03	*	Х	3
1167	-	-	*	9.19 ± 1.04	*	D	4
1177	-	-	*	1.09 ± 1.03	*	С	3
1266		_	_	$4 19 \pm 1.04$	_	Xe	1
1200	_	_	*	6.18 ± 1.02	*	T	3
1990	-	-	*	4.14 ± 1.02	*	v	2
1200	-	-	*	4.14 ± 1.01	*		3
1526	-	-		12.52 ± 1.04		D	3
1373	-	-	-	3.55 ± 1.07	-	Ae	2
1390			*	5.39 ± 1.08	*	T	4
1467	4.65 ± 0.18	0.684 ± 0.003	*	2.69 ± 1.06	*	С	4
	4.97 ± 0.03	0.705 ± 0.001	*	-0.88 ± 1.04	*	Ch	3
1556	-	-	*	5.44 ± 1.02	*	Т	3
1574	-	-	-	9.56 ± 1.03	-	D	1
	-	-	*	9.72 ± 1.02	*	D	3
1579	-	-	*	-1.19 ± 1.02	*	В	3
1796			*	1.80 ± 1.02	*	Ċh	3
1100	-	-	0.63 ± 0.01	-0.438 ± 1.05	9.114 ± 9.390	C	ວ ຈ
1941	-	-	0.05 ± 0.01 *	-0.430 ± 1.07	2.114 I 2.309 *	v	4
1041	-	-	*	3.00 ± 1.04	*		3
2266	-	-	*	8.64 ± 1.02	*	D	3
2634	-	-	-	5.36 ± 1.03	-	T	1
	-	-	*	2.90 ± 1.02	*	Х	3
2891	-	-	*	8.83 ± 1.02	*	D	3

Number	$\begin{array}{c} 0.7 \ \mu \mathrm{m} \\ \mathrm{depth} \\ (\%) \end{array}$	$\begin{array}{c} 0.7 \ \mu \mathrm{m} \\ \mathrm{Central} \\ \mathrm{wavelenght}(\mu \mathrm{m}) \end{array}$	Turn point (μm)	Visible slope (S'%/1000Å)	Uv Slope (S'%/1000Å)	Taxonomy	Reference
3015	-	-	-	4.34 ± 1.06	-	Х	1
	-	-	*	6.59 ± 1.02	*	D	3
3095	-	-	-	8.20 ± 1.04	-	D	1
3141	-	-	*	9.22 ± 1.04	*	D	3
3622	-	-	-	10.10 ± 1.04	-	D	1
3675	-	-	-	3.67 ± 1.08	-	S	1
4003	-	-	-	7.09 ± 1.06	-	\mathbf{L}	1
4158	-	-	-	4.69 ± 1.05	-	Т	1
4973	-	-	-	8.31 ± 1.04	-	D	1
5301	$4.346 {\pm} 0.065$	$0.759 {\pm} 0.002$	*	1.19 ± 1.07	*	Ch	3
5362	-	-	*	6.69 ± 1.04	*	Т	3
5780	-	-	$0.559 {\pm} 0.005$	1.79 ± 1.10	22.55 ± 2.16	\mathbf{C}	1
5833	-	-	-	5.16 ± 1.07	-	Х	1
5914	-	-	*	7.88 ± 1.03	*	D	3
6057	-	-	*	2.50 ± 1.05	*	Xc	3

Table 4 (cont'd)

Table 5. Results for the analysis of the visible parameters in Hilda population for objects extracted from the literature. The '*' symbol is placed when the wavelenght coverage are not suitable for measuring the determined feature, while the symbol '-' is used for indicating that the wavelengh coverage is appropriated, but the feature was not identified.. References: (1) Dahlgren et al. (1997) and Dahlgren et al. (1997); (2) SMASS (Bus and Binzel, 2004); (3) S3OS2 (Lazzaro et al., 2004); (4) Vilas et al. (2006)

Number	$0.7 \ \mu m$ depth	$0.7 \ \mu m$ Central	Turn point (μm)	Visible slope	Uv Slope	Taxonomy	Reference
	(%)	wavelenght(μm)		(S'%/1000Å)	(S'%/1000Å)		
153	-	_	-	2.08 ± 1.04	-	Х	2
	-	-	-	3.02 ± 1.04	-	Х	1
	-	-	*	3.77 ± 1.03	*	Х	4
190	-	-	-	1.58 ± 1.04	-	Xc	2
	-	-	-	2.83 ± 1.02	-	Х	1
334	-	-	-	2.37 ± 1.04	-	\mathbf{C}	1
	-	-	*	2.79 ± 1.03	*	Xc	4
361	-	-	-	6.23 ± 1.02	-	Т	1
	-	-	*	6.57 ± 1.02	*	D	3
449	-	-	-	3.14 ± 1.05	-	Х	1
748	-	-	*	4.82 ± 1.05	*	Т	4
958	-	-	-	8.19 ± 1.02	-	D	1
1038	-	-	-	8.56 ± 1.05	-	D	1
	-	-	-	8.96 ± 1.04	-	D	1
1162	-	-	*	3.66 ± 1.04	*	Х	4
1180	-	-	*	4.78 ± 1.02	*	Х	3
1202	-	-	-	8.42 ± 1.03	-	D	1
1212	-	-	-	2.71 ± 1.06	-	X	2
	-	-	-	5.35 ± 1.08	-	X	1
	-	-	-	6.30 ± 1.06	-	Т	1
1268	-	-	-	6.35 ± 1.05	-	T	1
1045	-	-	-	10.69 ± 1.08	-	D	1
1345	-	-	-	3.03 ± 1.07	-	AC	1
1439	-	-	-	2.12 ± 1.09	-	C	1
1512	-	-	-1-	5.01 ± 1.03		X D	4
1529	-	-	-	9.25 ± 1.05 0.67 ± 1.02	-	D	1
1754	-	-	-	9.07 ± 1.03 2.76 ± 1.02	- *	D V	1
1704	-	-		5.70 ± 1.02 6.72 \pm 1.07			3
2240	-	-	-	0.73 ± 1.07 11.88 \pm 1.05	-	D	2
2465	-	-	-	11.00 ± 1.00	- *	D	1
2939	-	-		9.92 ± 1.07 10.53 ± 1.05			1
3134	_	_	_	8.13 ± 1.03		D	1
3254	_		_	5.55 ± 1.02		D	2
3/15	_	_	_	9.72 ± 1.06	_	D	1
0410	_		_	11.63 ± 1.00		D	1
3514	_		_	9.37 ± 1.07		Ď	1
3561	_	-	_	8.01 ± 1.01	_	D	1
3655	-	-	-	9.10 ± 1.00	-	D	1
3694	-	-	-	10.68 ± 1.04	-	Ď	1
3843	-	-	-	3.49 ± 1.06	-	ž	1
	-	-	-	4.43 ± 1.06	-	x	1
3923	-	-	-	3.24 ± 1.07	-	x	1
	-	-	-	6.08 ± 1.07	-	T	1
3990	-	-	*	10.80 ± 1.03	*	D	3

Number	IR Slope $S'\%/1000$	IR Slope unc	mIR Slope $S'\%/1000$	mIR Slope unc	Taxonomy
190	0.886	1.052	1.138	1.447	Cg
334	1.835	1.041	-0.268	1.173	x
1202	4.044	1.065	2.068	1.502	D
1269	4.461	1.081	-0.453	1.234	D
1754	2.193	1.029	2.825	1.387	Х
2067	4.123	1.148	3.225	1.226	D
	4.561	1.078	0.201	1.479	D
2624	5.259	1.103	-0.364	1.435	D
3557	4.246	1.065	0.965	1.548	D
3561	4.176	1.086	1.871	1.436	D
4317	5.013	1.087	2.725	1.579	D
5368	4.675	1.073	0.873	1.552	D
5661	4.574	1.111	0.725	1.356	D
5711	5.861	1.109	3.115	1.676	D
6237	2.652	1.101	-1.93	1.773	Х
9121	4.488	1.083	2.715	1.318	D
11750	4.411	1.078	3.025	1.356	D
15505	4.471	1.071	2.469	1.681	D
15417	5.160	1.202	-0.24	1.712	D
15540	4.022	1.110	6.012	1.797	D

Table 6. Results for Hildas near-IR spectra obseved with TNG

 Table 7.
 Results for near-IR parametrization for objects extracted from the literature. Reference:(1)

 Reddy and Sanchez (2016); (2) SMASS II (Bus and Binzel, 2004); (3) Takir and Emery (2012)

Number	IR Slope $S'\%/1000$	IR Slope unc	mIR Slope S'%/1000	mIR Slope unc	Taxonomy	Group	Reference
76	2.197	1.013	1.835	1.013	Х	Cybele	3
	1.838	1.152	2.344	1.243	Х	,	2
87	1.038	1.013	1.771	1.021	Xc	Cybele	1
107	1.229	1.012	1.647	1.012	С	Cybele	3
121	0.778	1.016	0.164	1.022	\mathbf{L}	Cybele	1
	2.001	1.011	-0.134	1.022	Κ	,	2
	1.850	1.014	0.030	1.023	Κ		3
401	2.226	1.022	1.614	1.033	Х	Cybele	3
790	1.931	1.022	1.451	1.040	Х	Cybele	3
153	2.221	1.010	1.782	1.042	Х	Hilda	2
	2.240	1.012	1.813	1.034	Х		3
190	1.823	1.016	1.605	1.046	Х	Hilda	3
334	1.397	1.009	1.551	1.068	Xc	Hilda	2
	1.580	1.018	1.545	1.118	Х		3
361	3.156	1.021	2.623	1.074	Х	Hilda	3

Number Name a_p c_p sin i_p Family H p_V p_V p_V D_V D_{err} 65 Cibele 3.429 0.111 3.563 - 6.62 0.059 0.039 276.584 7.4.487 76 Freia 3.411 0.166 2.122 - 7.90 0.058 0.004 145.423 1.287 87 Sylvia 3.485 0.054 0.171 Sylvia 6.94 0.046 0.004 25.66 3.212 121 Hermione 3.447 0.134 7.598 - 7.31 0.076 0.034 16.6422 8.807 1225 Henrietta 3.389 0.264 20.873 - 8.72 0.062 0.009 87.803 0.434 1225 Henrietta 3.444 0.15 6.416 - 8.97 0.444 0.041 0.038 0.435 120 Huberta 3.444 0.0152 0.035	NT 1	NT.				D 11	77			D	
	Number	Name	(a_p)	e_p	$\sin \imath_p$	Family	, H	p_V	p_{Verr}	D	D_{err}
65 Cibele 3.429 0.111 3.563 - 6.62 0.059 0.039 276.584 74.487 87 Sylvia 3.485 0.054 0.171 Sylvia 6.94 0.046 0.004 125.351 2.953 107 Camilla 3.486 0.072 4.666 - 7.31 0.076 0.031 16.6242 8.807 168 Silyla 3.379 0.072 4.666 - 7.34 0.056 0.012 14.5366 3.219 225 Henrietta 3.489 0.264 20.873 - 8.72 0.062 0.009 87.830 0.341 141 Lirlope 3.340 0.035 0.077 1.508 - 9.13 0.035 0.007 10.539 0.941 101 Citila 3.446 0.012 1.788 - 8.40 0.027 0.003 8.76 2.169 222 Helga 3.63 0.058 1.41 0.044 <td></td> <td></td> <td>(au)</td> <td></td> <td></td> <td></td> <td>(mag)</td> <td></td> <td></td> <td>(κm)</td> <td>(κm)</td>			(au)				(mag)			(κm)	(κm)
76Freiz Freiz 3.445 0.064 0.171 $Sylvia$ 0.944 0.088 0.004 145.423 12.873 107 Camilla 3.486 0.093 0.169 Sylvia 7.08 0.066 0.004 $221.0.37$ 8.326 101 Herniceta 3.437 0.072 4.666 -7.31 0.076 0.034 166.242 8.807 125 Henricta 3.339 0.072 4.666 -7.94 0.076 0.038 166.242 8.807 225 Adelinda 3.241 0.139 2.079 $ 9.13$ 0.035 0.007 105.912 1.779 226 Adelinda 3.441 0.115 6.146 $ 8.97$ 0.044 0.01 105.39 0.941 401 Ortilia 3.346 0.036 5.972 $ 9.20$ 0.052 0.009 87.803 0.435 414 Liriope 3.504 0.072 5.584 $ 9.49$ 0.027 0.033 8.876 2.169 420 Bertholda 3.417 0.031 6.887 $ 8.40$ 0.044 0.066 9.1766 6.524 528 Rezia 3.430 0.086 19.441 $ 8.2$ 0.048 0.066 9.466 0.361 526 Herga 3.242 0.168 1.769 $ 9.18$ 0.066 9.7968 0.876 721 Tabora 3.55 0.164 10.36 $-$ <td>65</td> <td>Cibele</td> <td>3.429</td> <td>0.111</td> <td>3.563</td> <td>-</td> <td>6.62</td> <td>0.059</td> <td>0.039</td> <td>276.584</td> <td>74.487</td>	65	Cibele	3.429	0.111	3.563	-	6.62	0.059	0.039	276.584	74.487
sylvia 3.485 0.054 0.171 Sylvia 6.94 0.046 0.004 253.051 2.93.3 107 Camilla 3.485 0.093 0.169 Sylvia 7.08 0.069 0.012 2.10.37 8.326 121 Henriene 3.447 0.134 7.598 - 7.34 0.066 0.012 1.46.366 3.219 1225 Henrietta 3.349 0.264 20.873 - 8.72 0.066 0.012 1.66.391 1.779 260 Haberta 3.444 0.115 6.416 - 8.97 0.044 0.003 8.876 2.449 410 Urtipe 3.341 0.035 4.417 - 8.40 0.044 0.004 87.869 3.449 420 Bertpolda 3.417 0.058 1.417.96 5.524 4.417 - 8.40 0.044 7.496 5.524 528 Rega 3.439 0.018 1.4766 5.524 <td>76</td> <td>Freia</td> <td>3.411</td> <td>0.166</td> <td>2.122</td> <td>_</td> <td>7.90</td> <td>0.058</td> <td>0.004</td> <td>145.423</td> <td>1.287</td>	76	Freia	3.411	0.166	2.122	_	7.90	0.058	0.004	145.423	1.287
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	87	Svlvia	3.485	0.054	0.171	Sylvia	6.94	0.046	0.004	253.051	2.953
121 Hermione 3.47 0.134 7.58 -1.000 7.31 0.076 0.034 166.242 8.807 168 Sibylla 3.379 0.072 4.666 - 7.94 0.066 0.012 1.46.366 3.219 225 Henricita 3.349 0.264 20.873 - 8.72 0.066 0.012 1.46.366 3.219 220 Adelinda 3.441 0.115 6.416 - 8.97 0.044 0.015 0.03 0.339 0.343 414 Liriope 3.610 0.036 5.072 - 9.40 0.027 0.013 85.699 3.446 420 Bertholda 3.417 0.036 1.417 - 8.40 0.044 0.006 91.966 0.361 528 Rezia 3.400 0.018 1.2685 - 9.14 0.046 0.044 - 8.52 0.524 576 Merapia 3.426 0.12 1	107	Camilla	3.486	0.093	0.169	Sylvia	7.08	0.059	0.012	210.37	8.326
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	121	Hermione	3 447	0.134	7 598	-	7.31	0.076	0.034	166 242	8 807
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	168	Sibylla	3 379	0.101	4 666	_	7.94	0.056	0.001	145 366	3 219
Adelinda 3.421 0.139 2.079 - 9.13 0.005 0.007 105.913 1.779 260 Huberta 3.444 0.115 6.416 - 8.97 0.044 0.01 101.539 0.941 401 Ottilia 3.364 0.022 9.558 - 9.49 0.022 0.003 88.76 2.169 414 Liriope 3.504 0.021 9.558 - 9.49 0.027 0.003 88.76 2.169 522 Heiga 3.63 0.081 12.4655 - 9.14 0.046 0.006 91.966 0.361 570 Kythera 3.429 0.081 13.769 - 9.70 0.055 0.029 42.771 0.633 713 Luscinia 3.392 0.164 10.36 - 8.97 0.048 0.006 7.998 0.876 721 Tabora 3.55 0.116 8.323 - 9.26 0.041	225	Henrietta	3 380	0.012	20.873		8 72	0.000	0.012	95 934	1 249
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	220	Adelinda	3 421	0.204	20.010		9.12	0.002	0.003	105 912	1.249
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	260	Huberta	3 444	0.115	6.416	_	8.97	0.044	0.001	101 539	0.941
brim 3.70 0.072 0.557 - 9.49 0.027 0.003 88.76 0.126 414 Liriope 3.601 0.072 9.558 - 9.40 0.027 0.003 88.76 0.138 522 Helga 3.63 0.085 4.417 - 9.00 0.057 0.0133 83.7 4.85 528 Merapi 3.403 0.018 12.685 - 9.14 0.046 0.005 147.066 5.524 570 Kythera 3.426 0.12 1.788 - 8.81 0.069 0.048 8.786 0.784 643 Scheherezade 3.361 0.158 2.6079 - 9.18 0.205 0.029 42.771 0.633 713 Luscinia 3.355 0.116 3.232 - 9.26 0.048 0.006 74.791 0.525 790 Pretoria 3.412 0.151 20.527 - 8.00 0.041	401	Ottilia	3 3/6	0.110	5 972		9.20	0.044	0.01	87 803	0.435
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	414	Liriope	3 504	0.030 0.072	9 558		9.20	0.002 0.027	0.003	88 76	2 169
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	420	Bertholda	3 417	0.072	6.687		8.40	0.021	0.003	138 699	3 446
528Regin 5.05 6.05 14.285 $ 9.14$ 0.046 0.006 91.966 0.361 536 Merapi 3.499 0.086 19.424 $ 8.2$ 0.048 0.005 147.066 5.524 643 Scheherezade 3.361 0.058 11.788 $ 8.81$ 0.069 0.004 87.486 0.784 643 Scheherezade 3.361 0.058 11.788 $ 8.81$ 0.069 0.004 87.486 0.784 692 Hippodamia 3.383 0.17 26.079 $ 9.18$ 0.205 0.029 42.771 0.633 713 Luscinia 3.392 0.164 10.36 $ 8.97$ 0.048 0.006 74.791 0.525 790 Pretoria 3.412 0.151 20.527 $ 8.00$ 0.041 0.029 163.4 53.372 909 Ulla 3.543 0.05 0.308 Ulla 8.95 0.037 0.001 113.13 1.48 1028 Lydina 3.402 0.087 2.979 $ 9.99$ 0.028 0.001 79.83 1.33 1127 Gonnesia 3.349 0.071 4.533 $ 10.51$ 0.036 0.008 55.715 0.5 1177 Gonnesia 3.349 0.051 17.185 $ 9.41$ 0.053 0.005 75.47 0.523 128 Devota 3.506 $0.$	522	Helma	3 63	0.001	4 417	_	9.00	0.057	0.0133	83.7	4.85
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	528	Bozia	3 /03	0.000	12 685		9.14	0.001	0.0100	91 966	0.361
570Kythera3.4260.0331.784-0.240.0440.0441.7840.664643Scheherezade3.3610.05813.769-9.700.0580.013 64.997 0.382692Hippodamia3.3830.1726.079-9.180.2050.02942.7710.633713Luscinia3.3920.16410.36- 8.97 0.0480.00597.9680.876721Tabora3.550.1168.323-9.260.0440.00991.8520.574909Ulla3.5430.050.308Ulla 8.95 0.0370.001113.131.48940Kordula3.3760.1726.21-9.550.0410.00979.8520.5041028Lydina3.4080.1079.393-9.430.0380.00685.5260.7621154Astronomia3.390.05117.185-9.430.0360.00575.470.5231280Baillauda3.4150.056.459-9.990.0460.00575.470.5231280Baillauda3.4470.10915.748-9.090.0460.00553.6970.721373Cincinnati3.4220.5117.78-9.990.0440.00553.6970.721281Devota3.5060.1355.765-10.090.046 <td>536</td> <td>Merani</td> <td>3 /00</td> <td>0.010</td> <td>19 494</td> <td></td> <td>82</td> <td>0.040</td> <td>0.000</td> <td>147.066</td> <td>5 524</td>	536	Merani	3 /00	0.010	19 494		82	0.040	0.000	147.066	5 524
	570	Kythera	3 426	0.000	1 788		8.81	0.040	0.000	87 486	0.784
	643	Schohorozado	3 361	0.12	13 760	-	0.01	0.005	0.004	64 007	0.382
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	602	Uippodemie	2 2 2 2 2	0.038	26.070	-	9.70	0.008	0.013	49 771	0.382
1131.15.11113.15.120.10410.3010.1300.10430.00091.4050.010721Tabora3.5120.15120.527-8.000.0410.029163.453.372909Ulla3.5430.050.308Ulla8.950.0370.001113.131.48940Kordula3.3760.1726.21-9.550.0410.00979.8520.5041004Belopolskya3.4020.0872.979-9.990.0280.00179.831.331028Lydina3.4080.1079.333-9.430.0380.00688.5260.7621154Astronomia3.390.0714.533-10.510.0360.00855.7150.51177Gonnessia3.3490.03115.069-9.9660.0320.016104.6313.7281280Baillauda3.4150.056.459-9.990.0450.00153.6970.4811373Cincinnati3.4220.31438.029-11.370.1550.03619.4480.1751467Mashona3.3840.13121.947-8.570.0360.01489.160.7281556Wingolfia3.4270.10915.748-10.670.0930.01233.882.121574Meyer3.5370.03514.478-9.900.	713	Luccipio	3 300	0.17	10.36	-	8.07	0.205	0.025	97.068	0.055
121140043.330.110 6.323 - 3.20 0.0410.02016.419.10.023909Ulla 3.543 0.050.308Ulla 8.95 0.0370.001113.131.48940Kordula 3.376 0.1726.21- 9.55 0.0410.00979.8520.5041004Belopolskya 3.402 0.087 2.979 - 9.99 0.0280.00179.831.331028Lydina 3.408 0.107 9.393 - 9.43 0.0380.006 85.526 0.7621154Astronomia 3.39 0.071 4.533 - 10.51 0.0360.008 85.715 0.51177Gonnessia 3.349 0.031 15.069 - 9.66 0.0320.016 104.631 33.728 1280Baillauda 3.415 0.05 6.459 - 9.99 0.0450.001 53.97 0.721328Devota 3.506 0.135 5.765 - 10.90 0.0460.005 53.697 0.4811373Cincinnati 3.422 0.35 14.78 - 10.67 0.933 0.014 89.16 0.7281574Mashona 3.384 0.131 21.947 - 8.57 0.083 0.014 89.16 0.7281574Meyer 3.537 0.057 22.585 - 9.84 0.044 0.005 40.52 1579Herrick<	713	Tabora	2.592	0.104	\$ 202	-	0.97	0.048	0.005	97.908 74 701	0.870
	721	Destania	2.00	0.110	0.323	-	9.20	0.040	0.000	162 4	52.279
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	790	Fretoria	3.412 2 = 42	0.151	20.327	- TIL	8.00	0.041	0.029	103.4	1 49
940Kordula 3.376 0.112 0.21 $ 9.53$ 0.041 0.009 19.852 0.304 1004Belopolskya 3.402 0.078 2.979 $ 9.99$ 0.028 0.001 79.83 1.33 1028Lydina 3.402 0.078 2.979 $ 9.99$ 0.028 0.001 79.83 1.33 1028Lydina 3.449 0.031 15.069 $ 9.66$ 0.032 0.006 88.526 0.762 1266Tone 3.359 0.051 17.185 $ 9.41$ 0.053 0.005 75.47 0.523 1280Baillauda 3.415 0.05 6.459 $ 9.99$ 0.0445 0.001 53.697 0.721 1373Cincinnati 3.422 0.314 $38.u929$ $ 11.37$ 0.155 0.036 19.448 0.772 1467Mashona 3.384 0.131 21.947 $ 8.57$ 0.033 0.014 89.16 0.728 1579Herrick 3.437 0.127 8.762 $ 10.67$ 0.093 0.012 33.88 2.12 1574Meyer 3.537 0.035 14.478 $ 9.90$ 0.442 0.011 57.785 0.435 1796Riga 3.356 0.57 22.585 $ 9.84$ 0.044 0.005 68.167 0.298 1841Masaryk 3.422 0.17 2.62 <td< td=""><td>909</td><td>Ulla Vandula</td><td>3.343</td><td>0.05 0.179</td><td>0.308</td><td>Ulla</td><td>8.95</td><td>0.037</td><td>0.001</td><td>113.13</td><td>1.48</td></td<>	909	Ulla Vandula	3.343	0.05 0.179	0.308	Ulla	8.95	0.037	0.001	113.13	1.48
	940	Rordula	3.370	0.172	0.21	-	9.55	0.041	0.009	79.652	0.504
1028Lydina3.4080.1079.393-9.430.0380.00688.5260.7621154Astronomia3.390.0714.533-10.510.0360.00885.7150.51177Gonnessia3.3490.03115.069-9.660.0320.016104.63133.7281266Tone3.3590.05117.185-9.9410.0530.00575.470.5231280Baillauda3.4150.056.459-9.990.0450.00153.970.721328Devota3.5060.1355.765-10.090.0460.00553.6970.4811373Cincinnati3.4220.31438.u929-11.370.1550.03619.4480.1751467Mashona3.3840.13121.947-8.570.0830.01489.160.7281576Wingolfia3.4270.10915.748-10.670.0930.01233.882.121579Herrick3.4370.1278.762-10.770.0430.00646.9250.4051579Herrick3.4520.172.2585-9.840.0440.00568.1670.2981841Masaryk3.4220.12.62-10.940.0520.00531.7260.4882891McGetchin3.3550.1369.296-11.050.0	1004	Belopolskya	3.402	0.087	2.979	-	9.99	0.028	0.001	79.83	1.33
1154Astronomia 3.39 0.071 4.333 $ 10.51$ 0.036 0.008 55.715 0.57 1177Gonnessia 3.349 0.031 15.069 $ 9.66$ 0.032 0.016 104.631 33.728 1266Tone 3.359 0.051 17.185 $ 9.41$ 0.053 0.005 75.47 0.523 1280Baillauda 3.415 0.05 6.459 $ 9.99$ 0.045 0.001 53.97 0.72 1328Devota 3.506 0.135 5.765 10.09 0.046 0.005 53.697 0.481 1373Cincinnati 3.422 0.134 $38.u929$ $ 11.37$ 0.155 0.036 19.448 0.175 1467Mashona 3.344 0.135 5.748 $ 10.67$ 0.093 0.012 33.88 2.12 1574Meyer 3.537 0.035 14.478 $ 9.90$ 0.042 0.011 57.785 0.435 1579Herrick 3.437 0.127 8.762 $ 10.77$ 0.005 40.24 0.504 2266Tchaikovsky 3.44 0.182 13.247 $ 10.88$ 0.044 0.005 33.796 0.448 2891McGetchin 3.355 0.136 9.296 $ 11.0$ 0.061 0.005 33.996 0.418 3015Candy 3.355 0.173 17.403 $-$ <	1028	Lydina	3.408	0.107	9.393	-	9.43	0.038	0.006	88.526	0.762
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1154	Astronomia	3.39	0.071	4.533	-	10.51	0.036	0.008	55.715	0.5
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1177	Gonnessia	3.349	0.031	15.069	-	9.66	0.032	0.016	104.631	33.728
1280Baillauda 3.415 0.05 6.459 $ 9.99$ 0.045 0.001 53.97 0.72 1328Devota 3.506 0.135 5.765 $ 10.09$ 0.046 0.005 53.697 0.481 1373Cincinnati 3.422 0.314 $38.u929$ $ 11.37$ 0.155 0.036 19.448 0.175 1467Mashona 3.384 0.131 21.947 $ 8.57$ 0.083 0.012 33.88 2.12 1574Meyer 3.537 0.035 14.478 $ 9.90$ 0.042 0.011 57.785 0.435 1579Herrick 3.437 0.127 8.762 $ 10.77$ 0.043 0.006 46.925 0.405 1796Riga 3.356 0.057 22.585 $ 9.84$ 0.044 0.005 68.167 0.298 1841Masaryk 3.422 0.11 2.62 $ 10.94$ 0.052 0.005 40.24 0.504 2266Tchaikovsky 3.4 0.182 13.247 $ 10.88$ 0.045 0.002 43.58 0.69 2634James Bradley 3.457 0.049 6.422 $ 10.50$ 0.07 0.005 33.726 0.488 2891McGetchin 3.355 0.173 17.403 $ 11.45$ 0.107 0.002 33.86 0.231 3141Buchar 3.4 0.077 1	1266	Tone	3.359	0.051	17.185	-	9.41	0.053	0.005	75.47	0.523
1328Devota 3.006 0.135 5.765 $ 10.09$ 0.046 0.005 53.697 0.481 1373Cincinnati 3.422 0.314 $38.u929$ $ 11.37$ 0.155 0.036 19.448 0.175 1467Mashona 3.384 0.131 21.947 $ 8.57$ 0.083 0.012 33.88 2.12 1556Wingolfia 3.427 0.109 15.748 $ 10.67$ 0.093 0.012 33.88 2.12 1574Meyer 3.537 0.035 14.478 $ 9.90$ 0.042 0.011 57.785 0.435 1579Herrick 3.437 0.127 8.762 $ 10.77$ 0.043 0.006 46.925 0.405 1796Riga 3.356 0.057 22.585 $ 9.84$ 0.044 0.005 68.167 0.298 1841Masaryk 3.422 0.11 2.62 $ 10.94$ 0.052 0.005 40.24 0.504 2664Tchaikovsky 3.4 0.182 13.247 $ 10.88$ 0.045 0.002 43.58 0.69 2634James Bradley 3.457 0.136 9.296 $ 11.00$ 0.061 0.005 33.996 0.418 3015Candy 3.385 0.173 17.403 $ 11.45$ 0.107 0.017 24.517 0.47 3095Omarkhayyam 3.502 0.075 <td>1280</td> <td>Baillauda</td> <td>3.415</td> <td>0.05</td> <td>6.459</td> <td>-</td> <td>9.99</td> <td>0.045</td> <td>0.001</td> <td>53.97</td> <td>0.72</td>	1280	Baillauda	3.415	0.05	6.459	-	9.99	0.045	0.001	53.97	0.72
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	1328	Devota	3.506	0.135	5.765	-	10.09	0.046	0.005	53.697	0.481
1467Mashona3.3840.13121.947-8.570.0830.01489.160.7281556Wingolfia3.4270.10915.748-10.670.0930.01233.882.121574Meyer3.5370.03514.478-9.900.0420.01157.7850.4351579Herrick3.4370.1278.762-10.770.0430.00646.9250.4051796Riga3.3560.05722.585-9.840.0440.00568.1670.2981841Masaryk3.4220.12.62-10.940.0520.00540.240.5042266Tchaikovsky3.40.18213.247-10.500.1070.00533.7260.4882891McGetchin3.3550.1369.296-11.00.0610.00533.9960.4183015Candy3.3850.17317.403-11.450.1070.01724.5170.473095Omarkhayyam3.5020.0752.966-10.800.0430.00429.3680.2313622Ilinsky3.3890.0434.935-11.800.1020.02321.880.4583675Kemstach3.690.08810.857-11.300.0540.00935.1390.2864158Santini3.4010.0196.17-11.600.172<	1373	Cincinnati	3.422	0.314	38.u929	-	11.37	0.155	0.036	19.448	0.175
1556Wingolfia 3.427 0.109 15.748 $ 10.67$ 0.093 0.012 33.88 2.12 1574Meyer 3.537 0.035 14.478 $ 9.90$ 0.042 0.011 57.785 0.435 1579Herrick 3.437 0.127 8.762 $ 10.77$ 0.043 0.006 46.925 0.405 1796Riga 3.356 0.057 22.585 $ 9.84$ 0.044 0.005 68.167 0.298 1841Masaryk 3.422 0.1 2.62 $ 10.94$ 0.052 0.005 40.24 0.504 266Tchaikovsky 3.4 0.182 13.247 $ 10.88$ 0.045 0.002 43.58 0.69 2634James Bradley 3.457 0.049 6.422 $ 10.50$ 0.107 0.005 33.726 0.488 2891McGetchin 3.355 0.136 9.296 $ 11.0$ 0.061 0.005 33.996 0.418 3015Candy 3.385 0.173 17.403 $ 11.45$ 0.107 0.017 24.517 0.47 3095Omarkhayyam 3.502 0.075 2.966 $ 10.949$ 0.663 0.009 29.007 0.335 3141Buchar 3.4 0.077 10.995 $ 11.80$ 0.102 0.23 21.88 0.458 4003 Schumann 3.427 0.094 <t< td=""><td>1467</td><td>Mashona</td><td>3.384</td><td>0.131</td><td>21.947</td><td>-</td><td>8.57</td><td>0.083</td><td>0.014</td><td>89.16</td><td>0.728</td></t<>	1467	Mashona	3.384	0.131	21.947	-	8.57	0.083	0.014	89.16	0.728
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	1556	Wingolfia	3.427	0.109	15.748	-	10.67	0.093	0.012	33.88	2.12
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1574	Meyer	3.537	0.035	14.478	-	9.90	0.042	0.011	57.785	0.435
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1579	Herrick	3.437	0.127	8.762	-	10.77	0.043	0.006	46.925	0.405
1841Masaryk 3.422 0.1 2.62 $ 10.94$ 0.052 0.005 40.24 0.504 2266Tchaikovsky 3.4 0.182 13.247 $ 10.88$ 0.045 0.002 43.58 0.69 2634James Bradley 3.457 0.049 6.422 $ 10.50$ 0.107 0.005 33.726 0.488 2891McGetchin 3.355 0.136 9.296 $ 11.0$ 0.061 0.005 33.996 0.418 3015Candy 3.385 0.173 17.403 $ 11.145$ 0.107 0.017 24.517 0.47 3095Omarkhayyam 3.502 0.075 2.966 $ 10.949$ 0.063 0.009 29.007 0.335 3141 Buchar 3.4 0.077 10.995 $ 11.80$ 0.043 0.004 29.368 0.231 3622 Ilinsky 3.389 0.043 4.935 $ 11.80$ 0.102 0.023 21.88 0.458 3675 Kemstach 3.369 0.088 10.857 $ 11.30$ 0.054 0.009 35.139 0.286 4158 Santini 3.401 0.019 6.17 $ 11.60$ 0.172 0.013 16.797 0.181 4973 Showa 3.426 0.077 18.924 $ 11.50$ 0.068 0.011 20.97 0.298 5361 Infotaine 3.346 <	1796	Riga	3.356	0.057	22.585	-	9.84	0.044	0.005	68.167	0.298
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1841	Masaryk	3.422	0.1	2.62	-	10.94	0.052	0.005	40.24	0.504
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2266	Tchaikovsky	3.4	0.182	13.247	-	10.88	0.045	0.002	43.58	0.69
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2634	James Bradley	3.457	0.049	6.422	-	10.50	0.107	0.005	33.726	0.488
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2891	McGetchin	3.355	0.136	9.296	-	11.0	0.061	0.005	33.996	0.418
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3015	Candy	3.385	0.173	17.403	-	11.145	0.107	0.017	24.517	0.47
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3095	Omarkhayyam	3.502	0.075	2.966	-	10.949	0.063	0.009	29.007	0.335
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3141	Buchar	3.4	0.077	10.995	-	10.80	0.043	0.004	29.368	0.231
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3622	Ilinsky	3.389	0.043	4.935	-	11.80	0.102	0.023	21.88	0.458
$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	3675	Kemstach	3.369	0.088	10.857	-	11.10	0.181	0.018	18.825	0.184
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	4003	Schumann	3.427	0.094	5.059	-	11.30	0.054	0.009	35.139	0.286
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	4158	Santini	3.401	0.019	6.17	-	11.60	0.172	0.013	16.797	0.181
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	4973	Showa	3.426	0.077	18.924	-	11.50	0.068	0.01	27.958	0.423
	5301	Novobranets	3.362	0.102	10u.047	-	12.10	0.058	0.011	20.97	0.298
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	5362	1978 CH	3.389	0.024	6.146	-	11.70	0.085	0.013	21.865	0.253
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	5780	Lafontaine	3.346	0.131	8.677	-	12.365	0.055	0.004	22.593	0.119
	5833	Peterson	3.491	0.032	19.381	-	11.587	0.105	0.021	27.077	0.435
6039 Parmenides 3.411 0.057 13.11 - 11.90 0.076 0.004 22.03 0.157 6057 Robbia 3.329 0.1 17.863 - 11.90 0.043 0.004 29.368 0.231	5914	Kathywhaler	3.543	0.069	0.162	Sylvia	11.283	0.062	0.01	38.097	0.224
6057 Robbia 3.329 0.1 17.863 - 11.90 0.043 0.004 29.368 0.231	6039	Parmenides	3.411	0.057	13.11	-	11.90	0.076	0.004	22.03	0.157
	6057	Robbia	3.329	0.1	17.863	-	11.90	0.043	0.004	29.368	0.231

 Table 8.
 Cybele properties table

Number	Name	${a_p \atop (au)}$	e_p	$\sin i_p$	Family	H (mag)	p_V	p_{Verr}	$D \ (km)$	D_{err} (km)
153	Hilda	3.965	0.174	0.155	Hilda	7.67	0.038	0.016	218.844	3.637
190	Ismene	3.986	0.166	6.177	-	7.59	0.035	0.001	214.664	8.608
334	Chicago	3.895	0.022	4.641	-	7.70	0.041	0.013	198.77	5.668
361	Bononia	3.96	0.214	12.626	-	8.22	0.038	0.008	154.334	2.69
449	Hamburga	2.551	0.173	3.085	-	9.47	0.033	0.009	80.827	17.91
748	Simeisa	3.944	0.188	2.259	-	9.01	0.041	0.007	103.725	1.034
958	Asplinda	3.986	0.186	5.63	-	10.49	0.045	0.005	45.117	0.091
1038	Tuckia	3.965	0.164	0.143	Hilda	10.60	-	-	-	-
1144	Oda	3.748	0.094	9.743	-	10.00	0.061	0.014	56.347	0.194
1162	Larissa	3.93	0.109	1.887	-	9.42	0.169	0.012	42.243	0.111
1180	Rita	3,985	0.158	7.199	-	9.14	0.058	0.009	82.308	0.418
1202	Marina	3 996	0.166	3 334	_	10.09	-	-	-	-
1212	Francette	3 967	0.100	0.126	Hilda	9.54	0.046	0.007	76 395	0.155
1268	Libva	3 975	0.20	4 427	-	9.12	0.040	0.007	96 708	0.100
1260	Bollandia	3 906	0.102	2 758	_	8.82	0.043	0.005	104 893	0.694
1345	Potomac	3 080	0.183	11 300	-	0.73	0.043	0.008	72 075	0.024
1345	Vortin	4.002	0.100	4 202	-	9.75	0.043	0.008	12.913 50.549	0.403
1439	Vogua	4.005	0.118	4.203	-	10.45	0.040	0.007	50.54Z	0.140
1512	Oulu	3.907	0.147	0.491	-	9.02	0.050	0.005	19.222	0.241
1529	Oterma	3.904	0.104	0.157	niida	10.05	0.034	0.005	30.327	0.280
1/04	Cunningnam	3.941	0.109	12.153	-	9.77	-	-	-	1 700
1902	Snaposnnikov	3.900	0.222	12.496	-	9.51	0.04	0.012	83.443	1.723
2067	Aksnes	3.964	0.182	3.08	-	10.55	0.054	0.003	40.003	0.701
2240	Bowell	3.958	0.094	0.495	-	10.56	0.045	0.012	48.424	0.429
2483	Guinevere	3.972	0.278	4.499	-	10.90	0.067	0.011	35.687	0.18
2624	Samitchell	3.948	0.117	2.797	-	10.80	-		-	-
2959	Scholl	3.943	0.275	5.234	-	11.10	0.054	0.015	32.783	0.319
3134	Kostinsky	3.966	0.184	0.156	Hilda	10.50	0.037	0.004	50.389	0.403
3202	Graff	3.936	0.115	11.107	-	11.311	0.055	0.013	35.914	0.244
3254	Bus	3.951	0.165	4.446	-	11.20	0.073	0.002	31.104	0.895
3415	Danby	3.963	0.249	1.367	-	11.304	0.063	0.006	36.582	0.124
3514	Hooke	3.954	0.191	3.505	-	11.70	0.084	0.012	22.037	0.073
3557	Sokolsky	4.003	0.173	6.049	-	10.90	-	-	-	-
3561	Devine	3.962	0.133	0.149	Hilda	11.10	-	-	-	-
3577	Putilin	3.948	0.197	3.741	-	10.56	0.051	0.003	49.138	0.313
3655	Eupraksia	4.014	0.2	3.823	-	11.13	0.063	0.01	36.66	0.207
3694	Sharon	3.933	0.206	4.976	-	10.50	0.058	0.004	46.036	0.345
3843	OISCA	3.993	0.144	3.926	-	10.94	0.108	0.023	30.768	0.3
3923	Radzievskij	3.966	0.196	0.05	Schubart	11.60	0.05	0.005	29.87	0.163
3990	Heimdal	3.965	0.168	0.167	Hilda	10.90	0.067	0.021	35.679	0.33
4317	Garibaldi	3.967	0.213	0.159	Hilda	10.90	0.052	0.01	38.611	0.224
5368	Vitagliano	3.974	0.083	6.262	-	11.2	0.058	0.017	34.812	0.061
5661	Hildebrand	3.966	0.234	13.311	-	11.10	-	-	-	-
5711	Eneev	3.942	0.164	6.371	-	11.10	-	-	-	-
6237	Chikushi	3.935	0.073	5.362	-	11.50	-	-	-	-
7394	Xanthomalitia	3.933	0.033	8.61	-	11.57	0.061	0.006	32.472	0.125
9121	Stefanovalentini	3.885	0.041	4.647	-	11.30	-	-		-
11750	1999 NM33	3.981	0.053	2.678	-	12.40	0.07	0.007	18.244	0.336
15505	1999 RF56	3.966	0.179	0.144	Hilda	11.76	0.079	0.008	24.789	0.38
15417	Babylon	3,933	0.053	3,185	-	11.80	-	-	-	-
15540	2000 CE18	2 080	0.113	16 088		12.20	0.08	0.008	10 528	0.20

Table 9. Hildas properties table