1	Characteristics of Calcium-Aluminate Slags and Pig Iron Produced from
2	Smelting-reduction of Low Grade Bauxites
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14	Abstract
15	Low grade bauxite ores are not favorable in the conventional Bayer process for alumina production,
16	as they are producing more bauxite residue (red mud) and accompanying lower alumina yield than
17	high grade ores. In the present work, the thermodynamics and characterization of calcium aluminate
18	slags and pig iron produced from smelting-reduction of high iron and silica-containing bauxites are
19	studied. Coke and limestone are used to reduce the iron oxide and adjust the basicity of slag during
20	smelting. There is evidence that complete iron separation from bauxite is feasible through smelting-
21	reduction process, and up to 99.9 pct of iron can be eliminated. Moreover, it is shown that silicon,
22	titanium and other elements partial separation from the $\mathrm{Al}_2\mathrm{O}_3$ -containing slag occurs. The phase
23	compositions and the distribution of elements between the metal and slag phases provides information
24	about the high temperature behavior of the bauxite components during smelting-reduction. Employing
25	electron microscopy analysis, it is indicated that the morphology of CaO·Al ₂ O ₃ , 12CaO·7Al ₂ O ₃ ,
26	$2CaO \cdot Al_2O_3 \cdot SiO_2$, and $CaO \cdot Al_2O_3 \cdot SiO_2$ phases in the slag, as well as the complex oxides of Ca-Al-
27	Si-Ti in slag behave differently as the mass ratio of $Al_2O_3/(Fe_2O_3 + SiO_2)$ in the bauxite changes. It is

also shown that the phases of slag produced from smelting-reduction below 5 $K \cdot s^{-1}$ of cooling rate are proper for further leaching process.

30

31 I. Background

32 Data from alumina processing industry shows a global average production of bauxite residue (red 33 mud) as 1-1.5 ton per ton of alumina, or about 150 million ton of red mud is produced annually [1]. 34 Lot of efforts have been made to valorize this most abundant industrial by-product in the world in 35 building materials [2], using as the rare earth element's source [3], making green direct reduced iron 36 (DRI) [4], consuming in inorganic polymers and pozzolanic material [5], and so on. However, none of 37 those has moved to a large-scale commercial production due to economic reasons and particular 38 challenges in processing the red mud. Thus, this caustic material is a prominent environmental issue 39 and is a major concern on most of alumina refineries in the world, and obviously increasingly lower 40 grade of bauxite (high iron and silica content) makes the situation even more challenging. In the Bayer process, the iron present in the ore is the main component involved in the production of red 41 42 mud, while silica causes loss of caustic soda to the solvent due to the high reactivity of the compound. 43 The compositions of the bauxite are important in determining the amount of lime that should be added in the mixtures and, eventually, the ratios of CaO/Al₂O₃ (C/A) in the slags. 44

45

46 In 1927, Harald Pedersen [6] patented a method to extract alumina from bauxite without yielding any 47 red mud; an overall illustration of the process is shown in Fig. 1. This process was run commercially 48 in Høyanger, Norway, during 1928-1969 with 17,000 ton of annual production before closing down 49 [7]. During that period, other researchers had adapted the patent for utilizing ferruginous bauxite in 50 Albany, [8] and a pilot-plant of alumina production from non-bauxitic source (clay) in Tennessee [9]. 51 Years later, Miller and Irgens [10] also made preliminary studies on alumina refinery plant with 52 200,000 tons of annual production, based on the same process. The Pedersen process shows a 53 promising potential for the prevention of red mud production, however, as per to date this process has 54 been abandoned more than four decades. Lack of literature and scientific evidence, especially in smelting-reduction part, lead the present authors to investigate the process thoroughly. 55

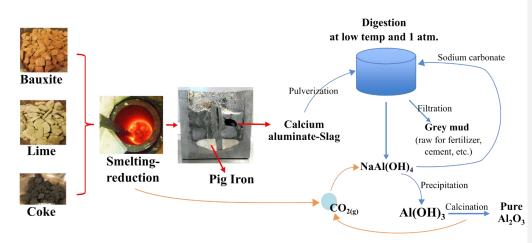






Fig. 1. An overview of Pedersen process.

60 II. Experimental Procedure

This section describes the applied experimental activities about the pyro-metallurgical part of the
Pedersen process for treating selected low-grade bauxites. Consecutively, the procedure consists of
materials preparation and characterization, and the details of smelting-reduction treatment.

64

65 II.1. Materials preparation and characterization

Mixture comprises bauxite ore, lime, and coke was prepared in laboratory scale. Three low grade of bauxite ores, named B-, G-, and I-Bauxite were used in different mixture. The characteristics of lime and coke based on the provider information is given in Table 1. The amounts of lime and coke used were based on the characteristics of the bauxites, and the lime/bauxite ratios for B-, G-, and I- are 0.55, 0.8, and 0.44, respectively.

71

Pig iron and slag are the products of the smelting-reduction treatment. For the targeted slag compositions, the CaO/Al₂O₃ (C/A) mass ratios were in the range of 0.65 to 0.75. This C/A ratio range is proper to obtain slag phases that has good leaching properties, as was reported in literatures [11] [12]. The amounts of coke in current work are 1.5 times larger than the stoichiometric needs to

assure the complete reduction of iron oxides. Coke was dried in an oven at 373 K (100 °C) for 12
hours before use to remove any free-moisture content.

78

Part of the ores and products were ground by ring mill into powder size for phase identification using 79 Bruker D8 A25 DaVinciTM X-ray Diffraction (XRD) with CuKα radiation, 10 - 75° diffraction angle, 80 0.01° step size, and 2.5° for both primary and secondary soller slit. The slag and pig iron samples 81 were mounted in epoxy, polished, and carbon coated before employing Hitachi SU6600TM Scanning 82 83 Electron Microscope (SEM) to capture the secondary electron (SE) and backscattered electron (BSE) images, X-ray element mapping, and use of Energy Dispersive Spectroscopy (EDS). X-ray 84 85 Fluorescence (XRF) analysis was used to identify the overall composition of the ores and pig iron and slag products. Moreover, a JXA-8500FTM Electron Probe Micro-Analyzer (EPMA), supported by 86 87 Wavelength Dispersive Spectroscopy (WDS), was applied for high accuracy on quantitative analysis 88 of elements in selected phases of the products.

89

90 II.2. Smelting-reduction treatment

91 The mixture of starting materials was set into an open graphite crucible with 115 mm of inner 92 diameter. The crucible was placed in a 75-kVA induction furnace and heated slowly at the rate of 5 93 K.s⁻¹ until it reached 1923 K (1650 °C). The partial pressure of gas (O₂, N₂, CO, CO₂, etc.) inside of 94 the crucible was not measured during the smelting trial. However, an oxidizing atmosphere during 95 smelting reduction process can be considered to exist because the experiments were in the open furnaceHowever, an oxidizing atmosphere which contains partially CO₂ (g) and O₂ (g) may exist 96 because of the oxidation of coke and crucible inside of the open furnace. The smelting-reduction 97 98 duration was one hour at 1923 K (1650 °C), while the top of crucible was partially closed by 99 refractories to minimize dissipation of the heat. However, the top was opened at intervals to crush the sintered materials or a solidified foamy-slag, while stirring of the melts was proper due to the 100 101 induction in pig iron and gas bubbles movements in the slag. To compensate the heat loss, the mixture 102 was heated until 2023 K (1750 °C) for the last ten minutes of the treatment. Consecutively, the mean

103	and standard deviation of mean smelting temperature of B-, G-, and I-Bauxite smelting temperature is
104	1937 ± 44 K-(1664-°C), 1935 ± 54 K-(1662-°C), and 1910 ± 38 K-(1637-°C), respectively.

The crucible was then cooled to the room temperature inside the furnace while the power was off. To measure the temperature during the treatment a tungsten/rhenium thermocouple (type C), inside a graphite rod, and an encapsulating alumina insulation tube was used. About two- thirds of the materials smelted in the first one hour of treatment, and after it cooled down to room temperature the rest of materials were added and another one hour of treatment was started. For further analysis, the solidified materials and crucible were crushed to separate slag and metal from the crucible.

112

113 III. Results

114 Results comprises of four major parts; analysis of bauxites, smelting-reduction treatment, overall115 chemical compositions, and phase analysis in products.

116

117 III.1. Characteristics of bauxites

An XRD analysis of the bauxites are presented in Fig. 2. The mineralogy of B-Bauxite comprises of kaolinite, gibbsite, cristobalite, goethite, anatase, and magnetite. The first three shown as the dominant phases. G-Bauxite predominant phases are diaspore, boehmite, calcite, and hematite. It also has anatase as one of the gangue mineral. I-Bauxite is high in kaolinite and hematite, with relatively low in diaspore and boehmite compare to G-Bauxite. It is worth noting that I-Bauxite has the highest intensity of anatase peaks compared to the other two.

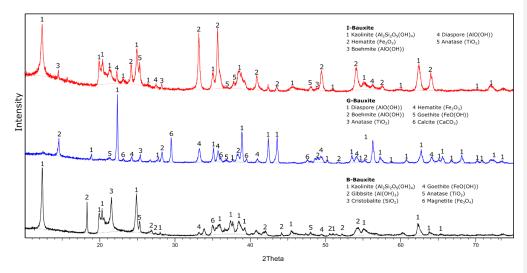




Fig. 2. XRD analysis of B-, G-, and I-Bauxites.

Table 2 shows the normalized XRF analysis result of B-, G-, and I-Bauxites. Three major elements that contribute to the bauxite leaching extent are aluminum, iron and silicon. These elements formed as either a hydroxide or oxide in bauxite as seen in XRD analysis presented above. The Loss of Ignition (LOI) content may decompose to air during smelting trial.

132

Prior to smelting, bauxite is obviously calcined at lower temperatures. Al₂O₃ and SiO₂ in calcined Band I-Bauxite are formed as Al₂O₃·2SiO₂, which is known as meta-kaolinite or aluminosilicate; a decomposed phase of kaolinite at high temperature. According to Kyriakogona et. al. [13] the degree of decomposition (dehydroxylation) is up to 98 pct when the calcination occurs at 1123 K (850 °C) in 60 min. Table 3 shows the normalized XRF analysis of the calcined bauxites, determined based on both XRF and XRD results.

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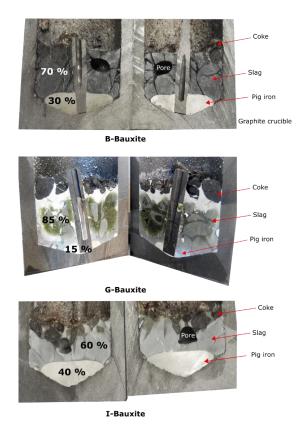
140 III.2. Smelting-reduction behavior

The measurement of cooling rate was done from 1873 K (1600 °C) to 1573 K (1300 °C). As seen later
in the CaO-Al₂O₃-SiO₂ ternary phase diagram, the latter temperature corresponds with the solidus
line, which expectedly means no solidification occurs upon cooling to this temperature. The mean

measured cooling rate is 4.9, 4.8, and 5 $K \cdot s^{-1}$ for B-, G-, and I-Bauxite, respectively. These cooling rates are well correlated with the masses (slag + iron) in the crucible where higher total mass shows slower cooling rate under similar conditions.

147

148 The cross section view of the solidified slag and pig iron in crucible after smelting-reduction trials are 149 displayed in Fig. 3. The unreacted coke remaining on top of the slag is also illustrated. The separation 150 of slag and iron produced from B-, G-, and I-Bauxite due to density differences is clearly seen. 151 Obviously, coke particles are floating over the molten slag phase at elevated temperatures and 152 thereafter. The different color appearance of the slags is mostly related to their different compositions. 153 The volume pct of slag and pig iron produced from different bauxites also roughly measured by visual 154 observation. As mentioned in experimental setup, the order of lime/bauxite mass ratio from the lowest 155 to the highest is I-Slag, B-Slag, and G-Slag. It appears that the pct of slag increases and of pig iron 156 decreases, considerably with increasing lime/bauxite mass ratio.



159 Fig. 3. Cross section view of the solidified slag and pig iron produced from B-, G-, and I-Bauxite.

160

161 In large-scale experiments, a useful performance indicator will be masses of slag and metal (pig iron) 162 produced from a given mass and composition of raw materials. Mass change characteristics, 163 including the correlation between losses of mass with the extent of smelting-reduction reaction are 164 accordingly of great importance as a reference to large-scale experiments. Table 4 shows the changes 165 of mass in different setups after smelting trial. Total mass loss pct for B-, G-, and I-Setup is 16.3, 166 15.4, and 6.1 pct, respectively. However, it becomes more interesting to see only the mass loss of 167 starting materials during reaction and exclude the loss from both graphite crucible and rod. As can be 168 seen, the estimated mass loss of materials after smelting trial is considerably high; 41.5, 39.4, and 169 21.2 pct for B-, G-, and I-Bauxite setup, respectively. Materials mass loss after the experiment might be caused by their LOI property, solid-gas transformation, i.e. $C \rightarrow CO_{(g)}$ or $CO_{2(g)}$, $CaCO_3 \rightarrow CaO +$ 170

171 $CO_{2(g)}$, and oxides phase reduction, i.e. $Fe_xO_y + yC \rightarrow xFe + yCO_{(g)}$, $SiO_y + yC \rightarrow Si + yCO_{(g)}$, $TiO_2 + 2C \rightarrow Ti + 2CO_{(g)}$.

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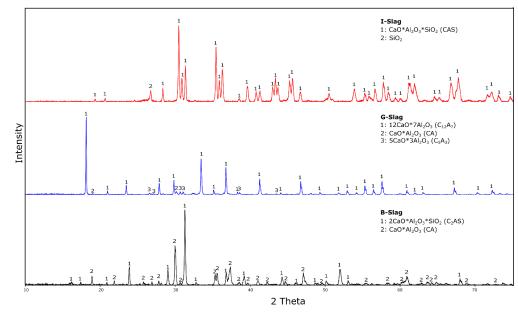
174 III.3. Chemical compositions of products

175 The result of XRF analysis of the produced slags in Table 5 shows the mass balance and smelting of 176 mixtures was done properly as the C/A ratio on each slag is in the expected range, as mentioned in 177 experimental procedure. It is worth noting here the low FeO_x content in the slag, which agrees with 178 our previous result [14]. Most of the reduced iron oxide becomes metal that saturated with carbon; pig 179 iron. As seen in Table 6, the B-, G-, and I-Pig iron contains 89.9 - 92.7 wt pctFe and are saturated in 180 carbon, and contain 0.2 - 4.0 wt pctSi, low trace of titanium and minor elements, i.e. V, Cr, P, S, are 181 also observed. Most of the minor elements are derived from coke and lime. The saturated carbon 182 content is estimated here based on the silicon content and the reliable solubility data for carbon in Fe-183 Si-C melts [15].

184

185 III.4. Phase and microstructural analysis of the products

Phase identification of the slags resulted from XRD analysis is shown in Fig. 4. B-Slag has 2CaO·Al₂O₃·SiO₂ (C₂AS) and CaO·Al₂O₃ (CA) as the primary and secondary phases, respectively. However, the latter phase seems to have another polymorph that bonds SiO₂ and MgO as be precisely identified later on BSE image. XRD analysis of G-Slag shows that the primary and secondary phase of the slag are 12CaO·7Al₂O₃ (C₁₂A₇), CA and 5CaO·3Al₂O₃ (C₅A₃), respectively. The latter phase is considered as an unstable phase that may be reformed to C₁₂A₇ phase at high temperature [16] [17]. In I-Slag, CAS phase appears as the dominant phase, followed by small fraction of silica phase.



194 195

Fig. 4. XRD analysis on B-, G-, and I-Slag.



197 The X-ray element mapping element mapping of B-, G-, and I-Slag is shown in Fig. 5, Fig. 6, and Fig. 7, respectively. These figures show clearly the concentration extent of several elements in every 198 199 structure that co-exists in slag. In B-Slag, calcium and silicon are more concentrated in the bright 200 structure, which is later shown to be C2AS phase. Aluminum is more concentrated in the dark area 201 within the lamellar structure. Whereas, titanium and magnesium are dispersed uniformly. In G-Slag, 202 the main structure ($C_{12}A_7$ phase) has more concentration of aluminum than other structures. Silicon 203 and titanium are densely populated between large $C_{12}A_7$ grains. As can be seen there are structures 204 that have complex oxides between Ca-Si-Ti elements. In contrast with B-Slag, magnesium is 205 concentrated in spots. The X-ray element mapping of I-Slag shows that titanium, aluminum, and 206 magnesium are highly concentrated in the dark structure. Obviously, bright structure has more 207 concentration of calcium and silicon than the dark one. Two phases co-exist between the C12A7 208 particles in G-Slag. Therefore, it is necessary to examine the structures in higher magnification and 209 analyze the composition by using SEM and EDS as the obtained results by these techniques are

- 210 shown in Fig. 8. It shows that the area with bright and dark structure has more concentration of
- 211 titanium than other structures in slag.
- 212
- 213

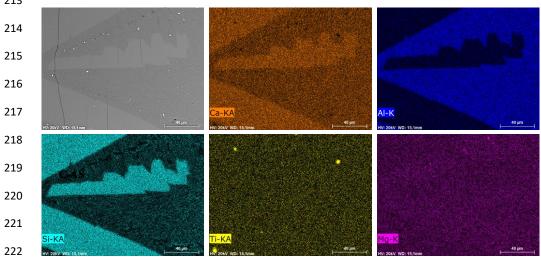


Fig. 5. X-ray element mapping of B-Slag.

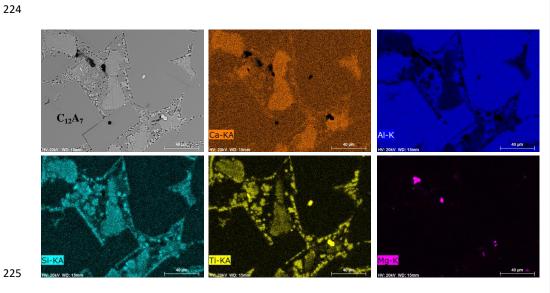




Fig. 6. X-ray element mapping of G-Slag.

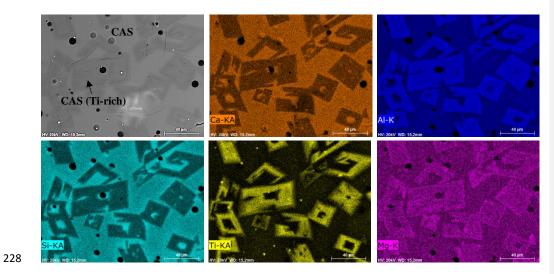




Fig. 7. X-ray element mapping of I-Slag.

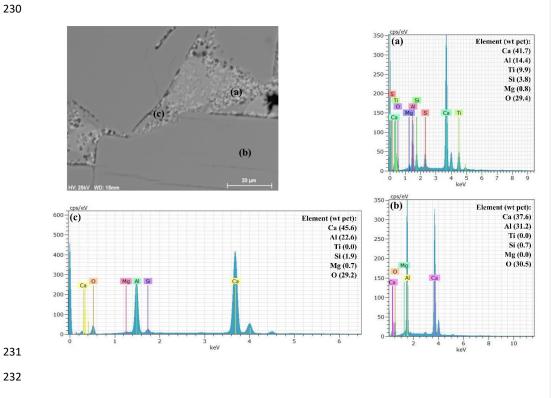
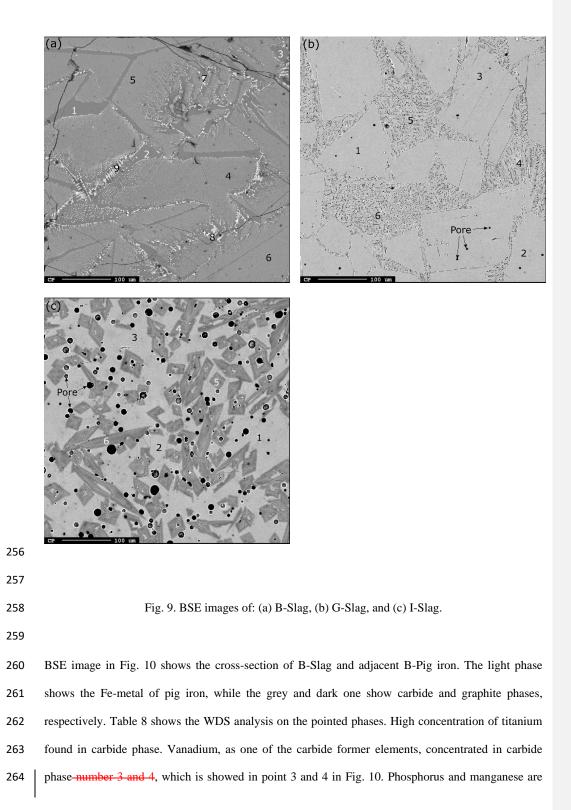
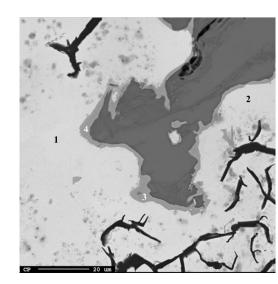


Fig. 8. BSE image of G-Slag with the corresponding EDS quantified analysis at (a), (b), and (c) area..

235 Fig. 9 (a), (b), and (c) show the BSE images of B-, G-, and I-Slag, respectively. As seen, three 236 structures co-exist in the B-Slag and the two main structures are seen in each G- and I-Slag. 237 Composition of each structure was measured by WDS analysis at 2 - 3 locations shown in Fig. 9. 238 Table 7 presents the WDS analysis of the observed phases in Fig. 9. In average, concentration of CaO, 239 Al₂O₃, SiO₂ constitute more than 95 wt pct of the slags. On the other hand, FeO content is low in all 240 structures of slags, averaging around 300 ppm, which is in agreement with low measured FeO 241 concentrations by XRF (Table 65). Numbers (a)1 - 3, (a)4 - 6, and (a)7 - 9, are WDS results for the 242 dark, fine lamellar and bright structure that are present in B-Slag (Fig. 9 (a)), respectively. Dark 243 structure is composed by 43 wt pctCaO, 35 wt pctAl₂O₃, and 22 wt pctSiO₂ in average. Fine lamellar 244 has similar composition as the dark structure has, which is 43 wt pctCaO, 35 wt pctAl₂O₃, and 21 wt 245 pctSiO₂ in average. While bright structure is predominantly composed of 55 wt pctCaO and 31 wt 246 pctTiO₂ in average. Number (b)1 - 3 and (b)4 - 6 are consecutively the composition of the bright-247 coarse grain and smaller grain which adjacent to a darker structure that showed in G-Slag (Fig. 9 (b)). 248 The first structure has 50 wt pctCaO and 49 wt pctAl₂O₃ in average. The latter one has 49 wt pctCaO, 249 43 wt pctAl₂O₃, 3 wt pctSiO₂, and 4 wt pctTiO₂. Number (c)1 - 3 and (c)4 - 6 show the bright and 250 dark structure in I-Slag (Fig. 9 (c)), respectively. In average, the bright structure is composed by 31 wt 251 pctCaO, 32 wt pctAl₂O₃, 34 wt pctSiO₂, and 1 wt pctTiO₂. The dark structure shows that it has less 252 CaO and more TiO₂ than the bright one has; 28 wt pctCaO, 34 wt pctAl₂O₃, 33 wt pctSiO₂, and 3 wt 253 pctTiO₂. BSE in I-Slag indicates it has significant number of pores, which are not observed in the B-254 and G-Slags.

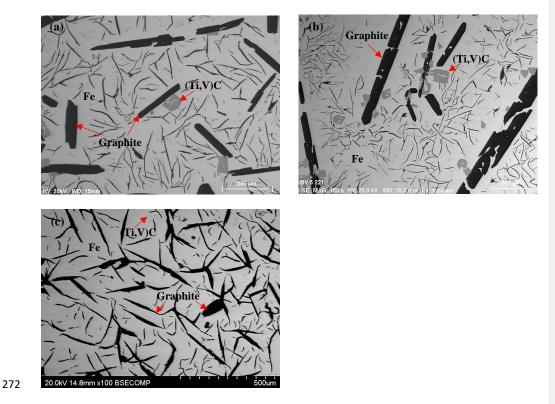


detected in Fe-metal matrix with 0.2 and 1.1 wt pct in average. Most of the manganese oxide is reduced to pig iron as it has low presence in slags, which is 800 ppm in average. Other trace elements showed in table are recognized as potassium and calcium. In addition, the lower magnification BSE image in Fig. 11 shows the metal matrix and co-existing phases in the produced metals.



270 271

Fig. 10. BSE image of cross-section of B-Slag and adjacent B-Pig iron.



273 Fig. 11. BSE images showing the main co-existing phases in (a) B-; (b) G-; and (c) I-Pig iron samples.

IV. 275 Discussion

276 In this section, mass changes before and after of experiment, thermochemistry of the reactions,

distribution of elements in slag and pig iron, and slag characteristics are discussed. 277

278

279 IV.1. Mass balance

280 From the LOI data of each bauxite presented in Table 2, we can calculate the mass losses in B-, G-, 281 and I-Bauxite due to the ignition, which is 0.28, 0.25, and 0.12 kg for the amounts used, respectively. 282 The LOI data for lime due to the decomposition of lime into CO2 (g) can be calculated based on the 283 carbonate amount in the same table, which is 0.45, 0.66, and 0.23 kg for B-, G-, and I-Bauxite setup, 284 respectively. While the moisture content of coke is removed after pre-heating in the oven before use, the LOI of coke is 1.53 wt pct as shown in Table 1, which gives loss as much as 2.10^{-3} kg. 285 286

Total loss due to transformation of C to CO $_{(g)}$ and oxides phase reduction can be calculated and given as 0.16, 0.21, and 0.16 kg for B-, G-, and I-Bauxite, respectively. This gives the theoretical mass loss for B-, G-, and I-Bauxite is, consecutively, 0.9, 1.13, and 0.52 kg. As seen in Table 9, the theoretical mass loss with the measured one shows proper correlation, in particular for G- and I-Bauxite. The difference between theoretical and measured mass loss in B-Bauxite might be due to the losses of SiO (g). Details of the explanation will be discussed in section IV.4.

293

294 IV.2. Smelting-reduction thermochemistry

Based on the XRD results in Fig. 2, B- and I-Bauxite are constructed mainly from kaolinite. This phase is found in either bauxite or non-bauxitic source; clay. Many works have been done to extract alumina from kaolinite with acid or alkaline solution [18] [19] [20]. In the Bayer process this is a major problem as the kaolinite is dissolved by sodium hydroxide solution which leads to high loss of caustic soda according to the following reaction:

300

$$301 \qquad Al_2Si_2O_5(OH)_{4(s)} + 6NaOH_{(l)} = 2Na_2SiO_{3(l)} + 2NaAl(OH)_{4(l)} + H_2O_{(l)}$$
(1)

302

303 Furthermore, precipitation of the desilication products, i.e. sodalite (Na₈(Al₆Si₆O₂₄)Cl₂), cancrinite 304 (Na₆Ca₂((CO₃)₂Al₆Si₆O₂₄)·2H₂O), etc. occur at elevated temperatures that are energy consuming. 305 Low-grade of bauxites typically characterized with low Al₂O₃/SiO₂ mass ratio [18] [21] [22], and/or 306 Al₂O₃/Fe₂O₃ mass ratio [23]. As both SiO₂ and Fe₂O₃ could be present in particular ore we may 307 classify the low-grade bauxite based on its low $Al_2O_3/(Fe_2O_3 + SiO_2)$ mass ratio. According to the 308 concentrations of calcined bauxites in Table 3, this ratio for B-, G-, and I-Bauxite is 0.8, 2.4, and 0.6, 309 respectively. These bauxites also have certain amount of TiO_2 that later in the slag phase might affect 310 the slag chemistry, its self-disintegration, and leachability [24]. The effect of MgO content of slag on 311 leachability has also been reported as it becomes the main impurity in blast furnaces' slag [25]. 312 However, in the present work the composition of Mg and remaining elements considered as trace 313 elements that give least effect on the slag properties. According to the obtained XRF results presented 314 in Table 5, 94.8 - 99.9 pct of Fe and Mn have been removed from the Al₂O₃-containing slag, together

315	with parts of Si and Ti. Coke produces CO gas and	l dissolved carbon in molten iron, and carbon in		
316	both forms is the reductant for oxides in bauxite. In addition, the usage of graphite crucibles makes an			
317	additional carbon source for the carbothermic reduc	tion. Based on the ores characteristics, the main		
318	smelting-reduction reactions that may take place are:			
319				
320	$3Fe_{2}O_{3\ (s)}+C\ _{(s,\ dissolved)}=2Fe_{3}O_{4\ (s)}+CO\ _{(g)}$	(2)		
321				
322	$3Fe_{2}O_{3(s)}+CO_{(g)}=2Fe_{3}O_{4(s)}+CO_{2(g)}$	(3)		
323				
324	$Fe_{3}O_{4(s)} + C_{(s, dissolved)} = 3(FeO) + CO_{(g)}$	(4)		
325				
326	$Fe_{3}O_{4(s)} + CO_{(g)} = 3(FeO) + CO_{2(g)}$	(5)		
327				
328	$(FeO) + C_{(s, dissolved)} = Fe_{(l)} + CO_{(g)}$	(6)		
329				
330	$(SiO_2) + 2\underline{C} = \underline{Si} + 2CO_{(g)}$	(7)		
331				
332	$(SiO_2) + CO_{(g)} = SiO_{(g)} + CO_{2(g)}$	(8)		
333				
334	$(SiO_2) + \underline{Si} = 2SiO_{(g)}$	(9)		
335				
336	$SiO_{(g)} + \underline{C} = \underline{Si} + CO_{(g)}$	(10)		
337				
338				
339	$(\underline{\text{Ti}}_{2}^{\frac{1}{2}}(\underline{\text{Ti}}O_{2}) + \underline{2}C_{\text{(solid, dissolved)}} = \frac{\underline{1}}{\underline{1}} + \underline{2}CO_{\text{(g)}}$	(11)	F	ormatted: English (U.S.)
340			F	ormatted: Underline
		(10)		ormatted: Underline ormatted: Underline
341	$(MnO) + \underline{C} = Mn + CO_{(g)}$	(12)	Ľ	omatted. ondenine

$$343 \qquad C_{(s)} = \underline{C} \tag{13}$$

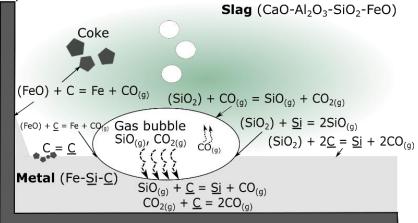
 $CO_{2(g)} + C = 2CO_{(g)}$

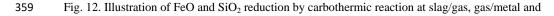
The underline "" and parenthesis "()" notations denote the element or phase that is dissolved in the Fe-liquid solution and slag at known temperature, respectively. It is emphasized here that the reduction of Fe_2O_3 and Fe_3O_4 by CO $_{(g)}$ through reactions (3) and (5) is more feasible than reactions (2) and (4). FeO and even Fe can be also formed in solid state; however, we here assume that Fe is mainly produced from FeO in the slag. Reactions (6-10) show the reduction mechanism of FeO and SiO₂ at slag/gas, gas/metal, and slag/metal interfaces as observed by Pomfret and Grieveson [26], Teasdale and Hayes [27], and Safarian et al. [28]. A simple illustration can be given as in Fig. 12, where mass transport of the gaseous species (CO, CO₂, SiO) in gas bubbles at the slag/metal interface are very important.

(14)









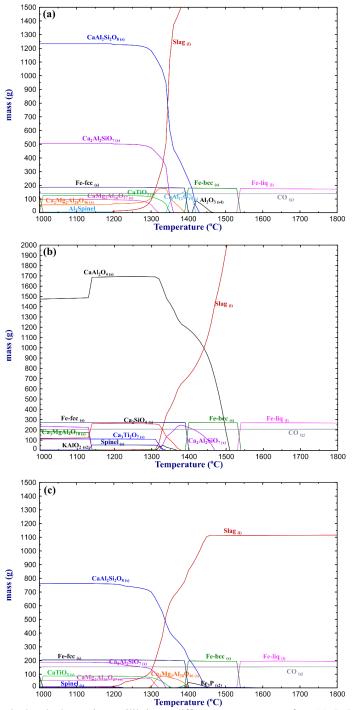
slag/metal interface.

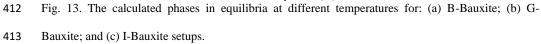
362			
363	As lime flux was used for slag making, the main reactions that occur in th	e process through high	
364	temperature sintering and smelting can be expressed in reaction (15-22).		
365			
366	$CaO_{(s)} + Al_2O_{3(s)} = (CaO \cdot Al_2O_3)$	(15)	
367			
368	CaO _(s) + $\frac{1}{3}$ Al ₂ O _{3(s)} = $\frac{1}{3}$ (3CaO·Al ₂ O ₃)	(16)	
369			
370	CaO _(s) + $\frac{7}{12}$ Al ₂ O _{3 (s)} = $\frac{1}{12}$ (12CaO·7Al ₂ O ₃)	(17)	
371			
372	$\frac{1}{3}(3\text{CaO}\cdot\text{Al}_2\text{O}_3) + \frac{1}{4}\text{Al}_2\text{O}_{3\ (s)} = \frac{1}{12}(12\text{CaO}\cdot7\text{Al}_2\text{O}_3)$	(18)	
373			
374	$CaO_{(s)} + Al_2O_{3(s)} + SiO_{2(s)} = (CaO \cdot Al_2O_3 \cdot SiO_2)$	(19)	
375			
376	$CaO_{(s)} + Al_2O_{3(s)} + 2SiO_{2(s)} = (CaO \cdot Al_2O_3 \cdot 2SiO_2)$	(20)	
377			
378	CaO _(s) + $\frac{1}{2}$ Al ₂ O _{3(s)} + $\frac{1}{2}$ SiO _{2(s)} = $\frac{1}{2}$ (2CaO·Al ₂ O ₃ ·SiO ₂)	(21)	
379			
380	$CaO_{(s)} + TiO_{2(s)} = (CaTiO_3)$	(22)	
381			

Here we do not consider the FeO-containing phases in the slag, as we do not have much of it left in the final slag. For the sake of simplicity, the compounds that composing the slag are denoted as follows: CaO = C, $Al_2O_3 = A$, and $SiO_2 = S$. In thermodynamic perspective, the above reactions of pig iron and slag making formation and their competition are dependent on the Gibbs energy changes at particular temperature. The calculated Gibbs energy changes of the formation of the metal and slag components in pure state by using HSC^{TM} software. The reduction of pure iron oxides may occur below 1273 K (1000 °C). While silica and titania are phases that could be reduced by carbon at 389 relatively high temperature, which means these two phases separation out of bauxite consume more 390 energy than iron. Moreover, the reduction of silica by CO (g) is unlikely to occur, as the Gibbs energy 391 changes is positive at any given temperature. The slag-making reactions (reaction (15-22)) are viable 392 at low temperature and there is a large driving force for slag formation upon the heating of bauxite + 393 lime to elevated temperatures. The WDS results in both slag and pig iron (Table 7 and Table 8) show 394 the main phases are in solid solution form with certain solubility, instead of the pure ones. However, HSCTM calculation is for pure substances and the real Gibbs energy changes for the slag making 395 396 reactions may be even more negative than calculations.

397

398 The equilibrium phases in different mixtures that co-exist during and after the smelting-reduction can be calculated by thermodynamic software, FactSageTM, at temperatures between 1273 - 2073 K (1000 399 400 - 1800 °C) with an increment of 283 K (10 °C) and 0.70 \pm 0.05 of C/A ratios. As the calculation 401 results in Fig. 13 indicate, the Fe-fcc phase co-exists with solidified slag of B, G, and I at 1273 K 402 (1000 °C) to 1663 K (1390 °C). The lattice changes to Fe-bcc phase at about 1663 - 1803 K (1390 -403 1530 °C) before it starts to melt. In the meantime, liquid slag phase appears at around 1473 K (1200 404 °C) and its amount increases significantly at 1673 - 1773 K (1400 - 1500 °C). B- and I-Slag should 405 have similar solid slag phases that are stable at temperature below 1573 K (1300 °C) as seen in the 406 Fig. 13. Consecutively, from highest to the lowest fraction of phase is CAS₂, C₂AS, CaTiO₃, 407 CaMg₂Al₁₆O₂₇, Ca₂Mg₂Al₂₈O₄₆, and spinel. In addition, B-Slag has CaAl₁₂O₁₉ phase as well at 1673 K 408 (1400 °C). The calculation of co-existing equilibrium phases in B- and I-Slag is not in agreement with 409 the XRD results presented in section III. The reason of the disagreement might be related with the 410 elements distribution during smelting-reduction trial that will be discussed in section IV.5.





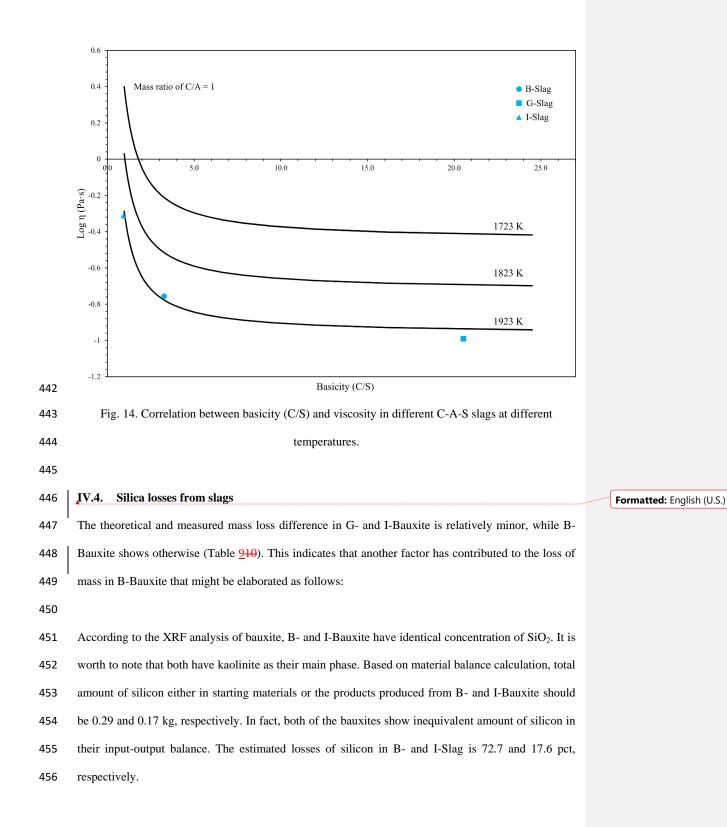
415 G-Slag has CA phase constitutes about 70 wt pct of the slag phase, followed by low amount of C_2AS , Ca₃MgAl₄O₁₀, Ca₂SiO₄, Ca₃Ti₂O₇, spinel and KAlO₂. FactSageTM does not recognize C₁₂A₇ phase in 416 417 its database and it is the reason that this phase is absent in the equilibrium phases of G-Slag. Aside 418 from $C_{12}A_7$ phase, the presence of CA phase is in agreement with the G-Slag XRD result. It is worth 419 to note that the amount of TiO_2 and MgO of all obtained slags as in Table 5 is considerably low, 420 which causes to not observe CaTiO₃, CaMg₂Al₁₆O₂₇, etc. in XRD analysis. However, the 421 thermodynamic calculations here show that such phases may co-exist with the main recognized 422 phases in the slags.

423

424 IV.3. Slag viscosity effect on porosity

425 The significant number of pores that appear in I-Slag in Fig. 9 (c) give strong indication of the gas 426 formation during the oxides reduction by the mechanism illustrated in Fig. 12. The pores have been 427 formed from the trapped gas that might come from the reduction reactions at the slag/metal interface. 428 I-Slag has the highest amount of SiO₂ compared to others and the basicity based on CaO/SiO₂ (C/S) 429 mass ratio is 0.9, which is relatively acidic. This slag forms networking oxides in melts that increases the viscosity and hinder the gas movement. In order to clarify this FactSageTM was applied to calculate 430 431 the viscosities of the obtained B-, G-, and I-Slags produced at 1923 K (1650 °C) and viscosities as 432 0.17, 0.10, and 0.48 Pa·s were obtained as shown in Fig. 14. The figure shows the correlation between different C/S mass ratios with the viscosity at 1723 K (1450 °C), 1823 K (1550 °C), and 1923 K 433 434 (1650 °C) where C/A mass ratio equals to 1. It can be seen that by decreasing the temperature the viscosity is significantly increase especially at the C/S mass ratio less than 3. That is to say, the gas 435 436 bubbles forming and leaving the slag/metal interface have more difficulties to rise in I-Slag than the 437 others as the I-Slag has more gas hold-up capacity. It is worth mentioning that during the smelting-438 reduction experiments more foaming of the slag I was observed than the others, which is supporting 439 the viscosity effect.

440



457 Silicon could be loss as a gas phase SiO $_{(g)}$, which is produced from reaction between SiO₂ in slag 458 with carbon in the metal, as in reaction (23). Then it is leaving out from the slag when the gas bubble 459 rises to the surface.

460

461
$$(SiO_2) + \underline{C} = SiO_{(g)} + CO_{(g)}$$
 (23)

462

The Gibbs energy change of formation in reaction (23) at 2023 K (1750 °C) is -2.2 kJ, which shows that high temperature is important factor in the silica gas production of the slag. As mentioned in the experimental procedure, the mean smelting temperature of B- is higher than of I-Bauxite. Silica loss could explain one of the reason why the concentration of silica in B- compare to I-Slag is lower, although the mixture setup before the smelting trial has identical C/(A+S) mass ratio that is 0.36 and 0.34 for B- and I-Bauxite, respectively.

469

470 IV.5. The distribution of elements between slag and pig iron

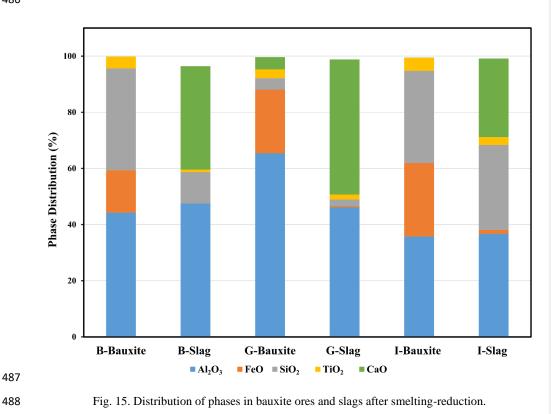
Based on equilibrium calculations in Fig. 13, the main phase of B- and I-slags at low temperature should be CAS₂ and C₂AS phase. In contrary, the XRD result in Fig. 4 shows the main phase for Band I-Slag is C₂AS and CAS, respectively. The result is supported by XRF analysis of the products which shows different composition in slag and pig iron produced from B- and I-Bauxite, regardless the similar phase and C/A ratio of the bauxites mixture have before. This gives indication that during smelting-reduction and solidification of the melt the elemental distribution may act as a decisive factor on the final phases in slag.

478

Fig. 15 shows the distribution of phases in calcined bauxite ores and the corresponding slags after smelting-reduction according to the XRF results. The weight fraction of Al₂O₃ and SiO₂ phases remain the same before and after the treatment, which indicates the two phases are not easily reduced during the smelting-reduction treatment. The significant decreasing quantity of SiO₂ phase in B-Slag has already discussed in section IV.4. The CaO wt pct in G-Slag is higher than in other slags because

of the high amount of lime used to maintain the required C/A ratio to get the leachable calcium

aluminate phase.



The reduction extent of each phase can be calculated by simple mathematical expression:

Reduction extent (pct)=
$$\left[\frac{W}{W^{\circ}}\right] \times 100 \text{ pct}$$

Where W° is mass of the amount of metal based on the stoichiometry, as if 100 pct reduced from an oxide and W is the actual amount of that metal present in the metal phase based on the XRF result of the pig iron. To make the mass loss based on the stoichiometry simple, we consider the iron reduction is 100 pct as the average WDS results of FeO content in all slags are low (see Table 7). Therefore, the SiO₂ reduction extent in B-, G-, and I-slag is 2.8, 1.3, and 1.6 pct, respectively. Higher SiO₂ reduction

(24)

499	in B-Bauxite might be resulted from higher smelting temperature of this trial compare to G- and I-		
500	Bauxite as discussed above. According to HSC data, reaction (8) goes to the right side at temperature		
501	more than 1938 K (1665 °C), and based on the smelting temperature setup in Fig. 2 thein section II.2.,		
502	B-Bauxite was exposed in this temperature relatively longer than others were. From kinetics point of		
503	view, carbothermic reduction of SiO_2 from slag is much slower than that FeO. The other partially		
504	reduced phase was TiO ₂ . The TiO ₂ reduction extent is 2.8, 8.4, 1.5 pct for B-, G-, and I-Bauxite,		
505	respectively. This calculation is in agreement with the amount of TiC that is observed in BSE image		
506	of the pig iron in Fig. 121. The reduction of TiO2 in reaction (11) proceeds at around 2023 K (1750	 Formatted: Subscript	
507	°C) when pure substances are involved. However, as the activity of titanium in the molten iron is low,		
508	the reduction of TiQe may occur at the lower process temperature to some extent, yielding dissolved	 Formatted: Subscript	
509	titanium in iron. Under carbon-saturated condition, the dissolved titanium has high possibility to make		
510	bond with the existing carbon and forms TiC during solidification of pig iron (reaction (25)). This is		
511	enhanced due to the low solubility of titanium in Fe-C _{enturated} -Ti system The reduction of TiO ₂ -in	 Formatted: Subscript	
512	reaction (11) proceeds at around 2023 K (1750 °C) when pure substances are involved. However, as		
513	the amount and activity of Ti in the molten iron is low, the reduction of TiO_2 may occur at the lower		
514	process temperature to some extent. Under carbon saturated condition, the dissolved titanium has high		
515	possibility to make bond with the existing carbon and forms TiC during solidification of pig iron		
516	(reaction (25)). This is enhanced due to the low solubility of titanium in Fe-C _{saturated} -Ti system		
517	[29] [29].		
518			
519	<u>Ti</u> + C = TiC $\Delta G^{\circ}_{\frac{25^{\circ}C^{298}K}{2}} = -180.8 \text{ kJ/mole Ti} (25)$		
520			
521	Another mechanism for the formation of TiC particles can be the direct reaction of the dissolved		
522	carbon in the melt with TiO2 in the slag at slag/metal interface, as in reaction (26).		
523			
524	$3C + (TiO_2) = TiC + 2CO_{(g)}$ $\Delta G^{\circ}_{1873 K} = -104.0 \text{ kJ/mole Ti}$ (26)	 Formatted: English (U.S.)	
525		Formatted: English (U.S.)	

526	The thermodynamic activities given in reaction (11) and (26) are in standard condition with the		
527	titanium activity is unity. Therefore, we need to evaluate the reactions in a non-standard conditions,		
528	where we have a low titanium activity in the melt. For reactions (11) and (26) the expression of Gibbs		
529	energy changes can be written as:		
530			
531	$\underline{\Delta G_{II}} = \underline{\Delta G_{II}}^{o} + RT \ln \frac{a_{Ti} \cdot pCO^2}{a_{TiO_2} \cdot aC^2} $ (27)		
532			
533	$\Delta G_{26} = \Delta G_{26}^{o} + RT \ln \frac{a_{TiC} \cdot pCO^2}{a_{TiO_2} \cdot aC^3} $ (28)		
534			
535	Where ΔG_{II}° and ΔG_{26}° are the standard Gibbs energy changes of reactions (11) and (26),		
536	respectively. The activity of C and TiO ₂ in the melt is unity and unknown, respectively. The partial		
537	pressure of CO _(g) for both reactions is the same, thus equation (27) and (28) can be rearranged to		
538			
539	$\Delta \underline{G_{II}}^{o} + RT \ln \underline{a_{II}} = \Delta \underline{G_{II}} - RT \ln \frac{pCO^{2}}{a_{IiO_{2}} \cdot aC^{2}} = \delta \underline{G_{II}} $ (29)		
540			
541	$\Delta G_{26}^{o} + RT \ln a_{TiC} = \Delta G_{26} - RT \ln \frac{pCO^2}{a_{TiO_2} \cdot aC^3} = \delta G_{26} $ (30)		
542			
543	Since activity of TiC is unity, then equation (30) becomes		
544			
545	$\Delta G_{26}^{o} = \Delta G_{26} - RT \ln \frac{pCO^2}{a_{TiO_2} \cdot aC^3} = \delta G_{26} $ (31)		
546			
547	By comparing δG_{11} and δG_{26} values, we may predict which reaction is more favorable to occur in a		
548	particular temperature. We determine the activity of titanium in Fe-C _{saturated} -Ti system at 1873 K (1600		
549	<u>°C) from FactSageTM database and calculate the δG_{11} and δG_{26} in the melt, as seen in Fig. 16.</u>		
550			

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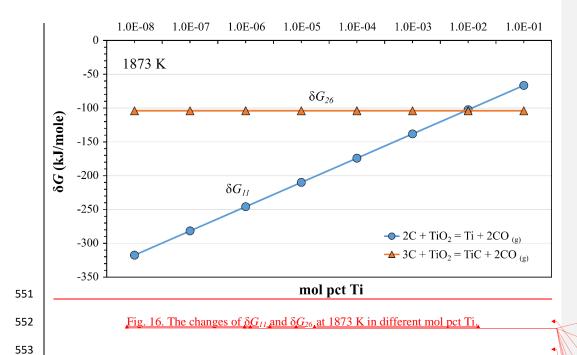


Fig. 16 shows that if the amount of titanium in the melt is less than about 0.01 mol pct, the reaction
(11) is more favorable than reaction (26), which means the TiO₂ is reduced and yields the dissolved
titanium in the metal. In the contrary, if the titanium content is larger than about 0.01 mol pct then
reaction (26) is more favorable than that of reaction (11), which means TiC formation at slag/metal
interface is likely to occur.

559

567

As seen in WDS analysis of pig iron in Table 8, silicon content on number 1 and 2 of B-Pig iron show higher amount compare to that <u>in-of silicon content in I-Pig iron (Table 6)</u>. This confirms the result in XRF analysis and demonstrate the reduction mechanism of silica in bauxite during smeltingreduction. The WDS results for Phase (2)of point number 3 and 4 show in Table 8 in both images confirmed the formation of (Ti,V)C in metal as was reported from literature [7][7]. As the solidus temperature of metal is lower than slag, the solute titanium in pig iron <u>may</u> segregates to the boundaries of metal and slag and forms carbide.

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Another important parameter in studying the slag-metal systems is the distribution of the dissolved elements between the slag and metal phases and a distribution coefficient as L_i is defined, which is expressed as:

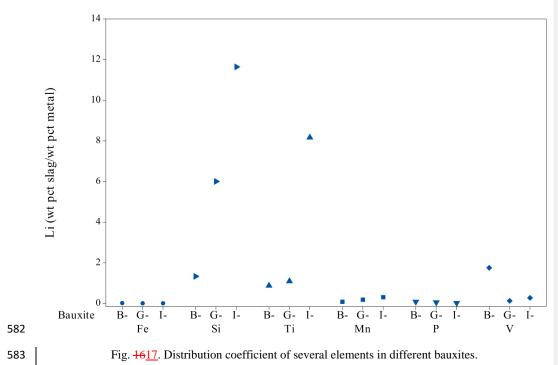
572

$$L_i = \frac{(\text{wt pct } i)}{[\text{wt pct } i]}$$

573

Where (wt pct *i*) and [wt pct *i*] are representing the mass pct of element *i* in the slag and metal phases, respectively. The distribution coefficient of Fe, Si, Ti, Mn, P, and V in current work is shown in Fig. 176. Fe, Mn, P, and V have relatively low L_{Fe} , L_{Mn} , L_{P} , and L_{V} values (0 - 1.7), which gives indication that these elements stable in pig iron and shows that iron was 99.9 pct reduced. While the L_{Si} and L_{Ti} values vary depending on the type of bauxite and so the slag composition, which is 1.3 - 11.6 and 0.8 - 8.2 for L_{Si} and L_{Ti} , respectively. More experiments are necessary to have better understanding on the elements distribution in slag and pig iron produced from smelted bauxite.

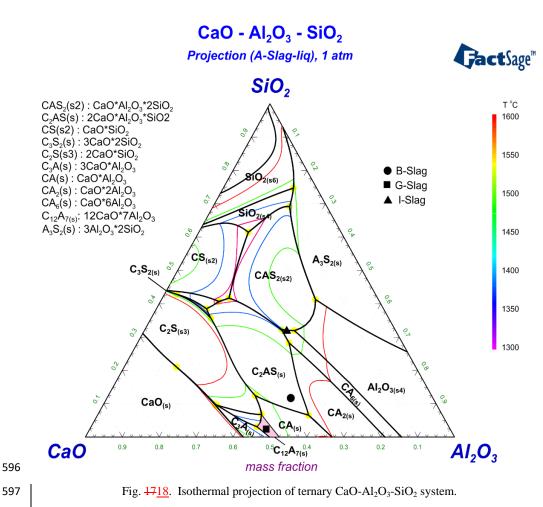




(<u>232</u>5)

585 IV.6. Stable phases in the slag system

586 Even though the mixtures was set-up with particular ratio of C/A, the other compound, i.e. SiO₂ and 587 TiO2 affect the construction of phases in the slag system. As seen in Table 5, the main slag 588 compounds are CaO, Al₂O₃, and SiO₂. While TiO₂ content is negligible (< 3 wt pct) and is not 589 constructing of any new phase in the system [24]. Therefore, the slag is regarded here as a ternary 590 CaO-Al₂O₃-SiO₂ system. Employing FactSageTM phase diagram module, the projection of isothermal 591 sections from 1573 - 1873 K (1300 - 1600 °C) in CaO-Al₂O₃-SiO₂ system can be made as seen in Fig. 592 1718. Due to the limitation of compound database in FactSage, C12A7 phase is not shown in the 593 projection. However, we draw the area of C12A7 phase manually into the ternary system (colored in 594 pink) based on provided information in literature [17] [30].



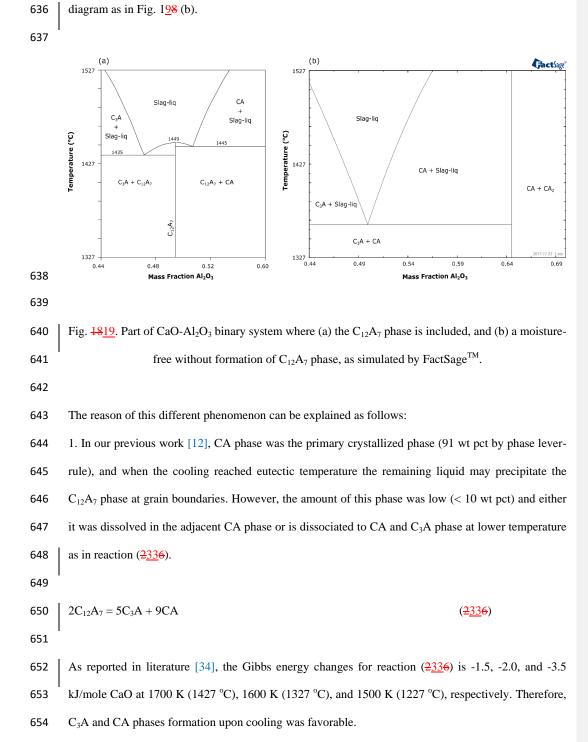
597

The calculated ternary phase diagram corresponds with the XRD result of B-Slag in Fig. 4. The 599 600 direction of crystallization path goes toward the peritectic temperature and shows that C₂AS, CA, and 601 β -C₂S phase are in equilibrium as condensed phases after solidification. However, neither β -C₂S nor γ -C₂S phases are traced in it. No existence of C₂S may be the reason why self-disintegration did not 602 happen during cooling, as we observed. The self-disintegration of slag occurs due to the volume 603 expansion by 12 pct as the crystalline phase transforms from β -C₂S to γ -C₂S [24] [31]. In a calcium 604 aluminate containing-slag produced from blast furnace, it is reported that when the cooling rate is 605 lower than 4.8 K.s⁻¹ then the major phases of the slag are $C_{12}A_7$, γ - C_2S , and CA [32]. On the other 606 hand, if the cooling rate is considerably high, 4.8 - 5.4 K·s⁻¹, the formation of C₂AS occurs. In present 607

608 work, the cooling rate averages were above 4.8 K·s⁻¹. Another possible explanation would be related 609 to low presence of β -C₂S in B-Slag (< 5 pct), as calculated in section IV.7, which is confirmed by no 610 observation of the corresponding peaks in XRD spectrums (Fig. 4).

611

612 Based on the XRD result, G-Slag has $C_{12}A_7$, CA, and low fraction of C_5A_3 phase. The $C_{12}A_7$ phase 613 was first observed by Rankin and Wright [33] in 1915 and has been in several discussions ever since. 614 In 1965, Nurse et al. [34] observed that $C_{12}A_7$ phase is unstable in anhydrous or moist-free CaO-Al₂O₃ 615 system, as it is in equilibria with H₂O above 1223 K (950 °C) and forms Ca₁₂Al₁₄O₃₂(OH)₂ when is 616 fully saturated; the water present as hydroxyl ions in crystal structure. Later on, Haccuria et al. [35] 617 showed that in a dry and high-purity (99.999 pct) argon atmosphere the formation of $C_{12}A_7$ phase 618 does not occur. Here in G-Slag, C12A7 phase is observed in its anhydrous form where the data given as 619 follows: a = 11.99856 Å, V = 1727.38 Å³, density $= 3.10^{-3}$ kg m⁻³, in cubic I-43d (220) space group. 620 The phase in the slag samples have been formed in an open furnace and oxidizing atmosphere, which 621 subsequently is cooled to room temperature. The result is in agreement with Imlach et al. [36], who 622 said the $C_{12}A_7$ phase might be stable at high temperatures as it absorbs excess of oxygen from any oxidizing atmosphere, even where pO_2 is as low as 10^{-3} Pa (10^{-8} bar). This finding is important to the 623 study of calcium-aluminate slag making, as C₁₂A7 phase is known as one of the leachable phase in 624 625 CaO-Al₂O₃ system [8] [11] [8] [17] [37] and is, therefore, crucial to Pedersen process. Hallstedt [16] 626 optimized the thermodynamic data of $C_{12}A_7$ phase and said that it melts congruently at 1449 °C. It has 627 a eutectic with other phases C₃A and CA on each side, as seen in Fig. 18-19 (a). In our results, G-Slag 628 consists mainly of 46.1 wt pct Al₂O₃ and 48.1 wt pct CaO, which means according to Fig. $\frac{18-19}{12}$ (a) it may rather have C₃A and C₁₂A₇ than C₁₂A₇ and CA phase. However, Hallstedt considers only the 629 630 binary system of CaO-Al₂O₃ and not the role of other constituents as if any involved; silica, titania, 631 etc . Moreover, C3A phase is relatively unstable as it can be reacted with free-Al2O3 in the system to form $C_{12}A_7$ (see reaction (18)). In our previous work [12] we did not observe the presence of $C_{12}A_7$ 632 633 phase in a slag that was synthesized at high temperature and oxidizing atmosphere. The composition 634 was 38 wt pct and 62 wt pct of CaO and Al₂O₃, respectively. Instead of the occurrence of CA and



 $C_{12}A_7$ phase, the encountered phases were CA and C_3A that agrees with a moisture-free binary

2. In the present work, as indicated by the strongest intensity in XRD in Fig. 4, the primary crystallized phase from G-Slag is $C_{12}A_7$. As it has significant amount, it may absorb the required oxygen during precipitation and eventually become more stable. From this reason, we may say that unless the composition of the binary slag is on the range of its primary crystallization (about 46 - 51 wt pct Al₂O₃) or as the majority phase in the system, the $C_{12}A_7$ phase is likely unstable even in oxidizing atmosphere.

662

According to the XRD results in Fig. 4, no CAS₂ phase in I-Slag is observed, which does not agree 663 664 with the ternary system at 101.3 kPa (1 bar) in Fig. 1718. CAS that is observed is known as Calcium 665 Tschermak's pyroxene (CATs) for geologists, which is one of the important constituent of the earth's 666 upper mantle and of the natural aluminous pyroxenes. The crystallography pattern of CAS in present 667 work matched against the measurement of Okamura et al [38] that is a = 9.609 Å, b = 8.652 Å, c =5.274 Å, $\beta = 106.06^{\circ}$, V = 421.35 Å³, in monoclinic C2/c space group. The CAS phase is formed by a 668 solid-state reaction as seen in reaction (3427) and (3528). Okamura et al. [38] synthesized a single 669 670 crystal of CAS from CAS₂, C₂AS, and Al₂O₃ after heating the mixture at 1573 K (1300 °C) within 24 671 hours in 18.10⁵ kPa (18 kbar). On the other hand, Hariya and Kennedy [39] observed that CAS₂ 672 decomposes to CAS and SiO₂ under high pressure and temperature.

673

674	$CAS_2 + C_2AS + Al_2O_3 = 3CAS$	(<u>34</u> 27)
675		
676	$CAS_2 = CAS + SiO_2$	(<u>35</u> 28)
677		

Many works concluded that CAS is a high-pressure and temperature phase [38] [40]. In addition, Hays [41] reported that pure CAS is not stable below 1433 K (1160 °C) and the pressure field of stability is relatively narrow even at higher temperature. However, Ma et al. [42] stated that although synthetic CAS is a high-pressure phase, a natural CAS could be found in low-pressure atmosphere. Fig. 9 (c) shows that I-Slag does not have lamellar structure, which indicates the phases were not

formed through a slow diffusion mechanism. Thus, in contrary to the conclusion that was given by some researchers above, we suggest that the reaction (3428) may occur during the cooling of a congruently melted CAS₂ phase on ambient pressure. The co-existing phases of CAS and SiO₂ in XRD result of I-Slag worth as the evidence of the argument. Nevertheless, this hypothesis needs further investigation.

688

689 IV.7. Phase changes upon slag solidification and cooling

690 In Table 7, the WDS analysis of B-Slag on dark and bright structure is identical with the phase of 691 C_2AS and $CaTiO_3$, respectively. The WDS result on fine lamellar phase indicates a C_2AS phase as it 692 has similar composition with the dark phase, only it has more TiO₂. This may not be precise, as the 693 lamellar is constructed with dark and less-bright phase. It is difficult to identify the composition of 694 each layer as the thickness is as much as 2 μ m. To understand the existing phases in lamellar 695 structure, a crystallization path of B-Slag becomes necessary. Based on alkemade line and phase 696 lever-rule we can describe it as follows:

697

698 1. Consider we have 100 g of slag with the composition of 50 wt pctAl₂O₃, 12 wt pctSiO₂, and 38 wt
699 pctCaO, which is a normalized XRF data of B-Slag from Table 5. At 1923 K (1650 °C), slag liquid
700 phase exists, named liquid #1.

701

702 2. From 1923 K (1650 °C) to 1783 K (1510 °C) the primary crystallization of C₂AS occurs; liquid #1
703 → C₂AS + liquid #2. The slag consists 14 g of C₂AS phase (14 pct) and 86 g of liquid #2 phase (86
704 pct).

705

3. From 1783 K (1510 °C) to 1623 K (1350 °C), following reaction occurs: liquid #2 → C₂AS + CA +
liquid (p). At this stage lamellar structure co-exists. The mass of C₂AS, CA, and liquid (p) phase is
30.1 (35 pct), 49 (57 pct), and 6.9 g (8 pct), respectively.

4. At 1623 K (1350 °C), liquid (p) + C₂AS → C₂S + CA, a peritectic reaction occurs. At current stage
the remaining liquid is consumed, as well as the partial of C₂AS phase. The mass of liquid (p), C₂AS,
C₂S, and CA phase is 6.9 g (66 pct), 3.55 (34 pct), 3.86 (37 pct), and 6.59 g (63 pct), respectively.

5. From 1623 K (1350 °C) to room temperature, at the solidus line no liquid exist and impurities may
segregate and concentrated between the primary C₂AS grains. Total amount of condensed phases in
B-Slag is:

- 717 $C_2AS = 14 \text{ g} + 30.1 \text{ g} 3.55 \text{ g} = 40.55 \text{ g} (40.6 \text{ pct})$
- 718 CA = 49 g + 6.59 g = 55.59 g (55.6 pct)
- 719 $C_2S = 3.86 \text{ g} (3.8 \text{ pct})$

720 Total = 100 g (100 pct)

721

On the other hand, coarse and small grain structure in G-Slag indicates the $C_{12}A_7$ phase. Grzymek et al. [43][43] observed that $C_{12}A_7$ has polymorphic transition phase depends on the synthesizing temperature, condition of atmosphere (reducing or oxidizing), and the cooling rate when it was formed. Grzymek mentioned that when synthesize held in an oxidizing atmosphere at 1770 K (1497 °C), and then slowly cooled, the structure is isotropic and grainy-ish with an anisotropic phase formed on grain boundaries, which is similar to present result. The structure of CA phase in G-Slag is indistinguishable as the amount is considerably low.

729

730 In I-Slag, pointed WDS analysis on bright and dark structures correspond to CAS phase with 731 insignificant difference on TiO₂ amount (1-2 wt pct). No lamellar structure is shown as it was in B-732 Slag. An X-ray element mapping on I-Slag in Fig. 87 shows the dark structure has high concentration 733 in titanium and it has stronger bond to aluminum than of calcium and silicon. Interestingly, these 734 complex oxides do not behave similarly in G-Slag. The area of the phase that is rich in titanium have 735 tendency to bond with calcium and silicon than aluminum, as seen in Fig. 6, which is supported by 736 SEM and EDS results for G-Slag in Fig. 8. This gives valuable information for the leachability of the 737 slag, as the titanium that bonded to the aluminum might hinder the alumina-leaching efficacy.

738	*		Formatted: Justified
739	As we observed above the slags B, G, and I contain different Al2O3-containing phases and the	1	Formatted
740	leachability of them is important for alumina extraction. The leaching behavior of $C_{12}A_7$ and CA	//	
741	phase have been studied in literature and the main point to be mentioned here is both phases are		
742	soluble in sodium carbonate solution and therefore is favorable for the alumina recovery. Lundquist	/	
743	and Leitch [45] proposed the leaching reaction of CA phase where As we observed above the slags B , /	/	
744	\underline{G} , and I contain different $\underline{Al}_{\underline{e}}\underline{O}_{\underline{e}}$ -containing phases and the leachability of them is important for		Formatted
745	alumna extraction. The leaching behavior of,have been studied in literateure and the main		
746	points to be mention are		
747			
748	$\underline{CaO \cdot Al_2O_3 + Na_2CO_3 + 4H_2O} = \underline{CaCO_3 + 2Na_4^+ + 2Al(OH)^{4-}} $ (36)		Formatted
749			
750	While for $C_{d2}A_{7}$ phase the reaction may be described as follows [8]:		Formatted
751			
752	$12CaO \cdot 7Al_{2}O_{3} + 12Na_{2}CO_{3} + 5H_{2}O = 7Na_{2}O \cdot Al_{2}O_{3} + 12CaCO_{3} + 10NaOH $ (37)		Formatted
753			
754	-However, there is no literature no publication was found about the leachability of,CAS,		
755	C_2AS , and C_5A_3 phases. This will be the subject of study of the authors in near future. Understanding	1	Formatted
756	the leaching behavior of Al ₂ O ₂ -containing phases may pave the way to treat different metallurgical		
757	slags, which is quite important regarding the sustainable process development and circular economy.		
758			
759	As we observed above the slags B-, G-, and I contain different Al2O3-containing phases and the		
760	leachability of them is important for alumna extraction. The leaching behavior of,		
761	studied in literateure and the main points to be mention are, However, there is no literature		
762	about the leachability of,,phases. This will be the subject of study of the authors in near		
763	future. Understanding the leaching behavior of Al2O3 containing phases may pave the way to treat		
764	different metallurgical slags, which is quite important regarding the sustainable process development		
765	and circular economy.		
	38		

767 V. Conclusion

768 The characteristics of calcium aluminate-containing slags and pig iron produced from low grade 769 bauxite ores were studied. Using advance characterization techniques, the thermochemistry of oxides 770 reduction, elements distribution between the slag and metal products, and mechanisms of the 771 formation of phases in them can be explained. The main conclusions can be summarized as follows:

772

1. Iron from the ores is removed from 94.8 to 99.9 pct during smelting-reduction by carbon and yields
the alumina-containing slag containing less than 1 wt pctFe, dependent on the slag chemistry.

775

2. The partial separation of Mn, Si, Ti, V and P oxides occurs through the smelting-reduction, where low distribution coefficients of L_{Mn} , L_P , and L_V are observed, While L_{Si} and L_{Ti} values ranges are considerably wide depend on the characteristics of the produced slag.

779

3. The viscosity in calcium-aluminate slags with CaO/SiO₂ mass ratio less than three is higher
compared to other compositions at elevated temperatures. It causes less of Fe-removal and gives more
porous product.

783

4. Silicon loss from high SiO₂-containing bauxites may occur at elevated temperatures through the
SiO gas formation.

786

5. The leachable slag phases (CaO·Al₂O₃, 12CaO·7Al₂O₃), which are observed in G-Slag, are obtained after the smelting-reduction of bauxite that has $Al_2O_3/(Fe_2O_3 + SiO_2)$ mass ratio higher than two with up to 5 K·s⁻¹ of cooling rate.

790

6. The complex bonding between titanium and aluminum oxides in slag is not favorable for leaching
process and is likely to occur in CaO·Al₂O₃·SiO₂ phase.

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3	Composition	Lime (wt pct)	Coke (wt pct
4	Al ₂ O ₃	0.3	2.8
5	Fe	NA	0.6
6	Fe ₂ O ₃	NA	0.9
7	SiO ₂	1.0	5.6
8	TiO ₂	NA	0.1
Э	CaO	54.0	0.4
)	MgO	1.0	0.2
L	Mn	NA	0.03
:	MnO	NA	0.04
3	K ₂ 0	0.1	0.2
	C-Fix	NA	87.7
	CO ₂	47.5	NA
	(as carbonate)	47.5	na Na
	Р	10 ppm	0.1
	S	110 ppm	0.4
	H ₂ O	1.0	15.5
	Volatile matter	NA	1.53
	Trace elements	100 - sum	100 - sum

Table 1. Characteristics of lime and coke as received.

Table 2. XRF analysis of different bauxite ores.

Element		Bauxite Ore					
Liement	B (wt pct)	G (wt pct)	I (wt pct)				
Al	18.4	31.0	14.7				
Fe	8.3	14.2	14.3				
Si	22.2	3.4	23.9				
Ti	3.3	3.4	4.3				
Mg	0.1	0.3	0.2				
Ca	NA	5.6	0.1				
К	130 ppm	433 ppm	0.1				
Mn	0.1	323 ppm	273 ppm				
Р	0.0	91 ppm	346 ppm				
0*	100 - sum	100 - sum	100 - sum				
LOI	~16.1	~14.6	~10.9				

*oxygen presents as oxides

972	Table 3. Normalized XRF analysis of the calcined bauxites to the c	orresponding stable oxides.

Phase	Ca	lcined Baux	ite
Thuse	B (wt pct)	G (wt pct)	I (wt pct)
Al ₂ O ₃	44.2	65.4	35.7
Fe ₂ O ₃	15.2	22.7	26.2
SiO ₂	36.2	4.1	32.8
TiO ₂	4.2	3.2	4.6
MgO	0.1	0.2	0.2
CaO	NA	4.4	0.1
K ₂ O	NA	NA	0.2
MnO	0.1	NA	NA

	B-	G-	I-
Condition	Bauxite	Bauxite	Bauxite
	(kg)	(kg)	(kg)
Crucible and materials, before smelting ^(a)	8.76	9.26	7.74
Crucible and materials, after smelting ^(b)	7.34	7.84	7.27
Total mass loss: $(a) - (b)$	1.42	1.42	0.47
	(16.3 pct)	(15.4 pct)	(6.1 pct)
Materials before smelting ^(c)	2.80	3.26	1.71
Materials after smelting ^(d) :	1.64	1.98	1.24
(b) - graphite crucible mass loss*	1.07	1.70	1.27
Managurad materials mass loss: (a) (d)	1.16	1.28	0.47
Measured materials mass loss: $(c) - (d)$	(41.5 pct)	(39.4 pct)	(21.2 pct)

Table 4. Mass changes of B-, G- and I-Bauxite setup after smelting trial.

993 0.5 pct and 4 pct, respectively.

⁹⁹² **The mass loss pct of the graphite crucible and graphite rod after one hour of smelting trial are* $2.2 \pm$

Table 5. Normalized XRF analysis of the obtained slags in smelting-reduction.

Phase	Slag					
Thuse	B (wt pct)	G (wt pct)	I (wt pct)			
Al_2O_3	47.5	46.1	36.7			
SiO ₂	11.2	2.3	30.3			
TiO ₂	0.9	1.8	2.8			
MgO	0.4	0.5	0.5			
CaO	36.8	48.1	28.0			
K ₂ O	NA	NA	0.5			
MnO	NA	NA	0.1			
FeO	0.01	0.44	1.4			
Trace elements	NA	NA	NA			

Table 6. XRF analysis of pig iron samples resulted from smelting-reduction treatment.

Element	Pig Iron						
Element	B (wt pct)	G (wt pct)	I (wt pct)				
Fe	89.9	92.0	92.7				
C _{sat}	4.6	5.3	4.9				
Si	4.0	0.2	1.2				
Mn	0.5	0.2	0.4				
Ti	0.6	0.9	0.2				
V	0.1	0.2	0.1				
Cr	0.1	0.5	0.1				
Р	450 ppm	950 ppm	0.1				
S	NA	70 ppm	70 ppm				
Trace elements	100 - sum	100 - sum	100 - sum				

1036	Table	e 7. WDS	analysis	of phases	observed	l in B-, C	i-, and I-S	lags struc	tures sho	wn in Fig	. 10 9.

Point	CaO	Al ₂ O ₃	SiO ₂	TiO ₂	MgO	FeO	V_2O_3	MnO	P ₂ O ₅	K ₂ O
no.	(wt pct)	(wt pct)	(wt pct)	(wt pct)	(wt pct)	(wt pct)	(wt pct)	(wt pct)	(wt pct)	(wt pct)
(a)1-3	42.66	35.05	21.62	0.33	0.29	NA	NA	0.01	0.03	NA
(a)4-6	42.99	34.72	21.41	0.61	0.23	0.01	0.01	0.01	0.01	0.01
(a)7-9	55.29	6.00	4.20	31.12	2.93	NA	0.26	0.19	NA	0.01
(b)1-3	49.58	48.99	0.79	0.32	0.24	0.01	0.01	0.03	0.03	NA
(b)4-6	48.94	42.66	2.73	4.35	1.12	0.04	0.05	0.07	0.04	NA
(c)1-3	30.81	32.35	33.95	1.36	0.41	0.10	0.03	0.12	0.02	0.85
(c)4-6	28.43	33.86	33.50	2.87	0.67	0.04	0.03	0.10	0.01	0.49

1	n	5	6
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Table 8. WDS analysis of phases in B-Pig iron shown in Fig. <u>4410</u>.

Point	Fe	С	Mn	Si	Ti	Mg	v	Al	Р	Others
no.	(wt pct)									
1	90.5	4.9	1.1	2.9	NA	0.1	0.3	NA	0.2	NA
2	90.5	4.6	1.1	3.1	0.1	0.1	0.3	NA	0.2	NA
3	2.8	13.1	NA	0.5	80.4	0.0	2.9	0.1	NA	0.2
4	2.3	15.0	NA	0.1	79.4	0.1	2.3	0.2	NA	0.6

Table 9.	Correlation	between	starting	materials	mass	loss	with	their	causes.
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Materials Mass Loss Causes	B-Bauxite setup	G-Bauxite setup	I-Bauxite setup	
	(kg)	(kg)	(kg)	
Total materials mass loss as measured ⁽¹⁾	1.16	1.28	0.47	
LOI of Bauxite ^{<i>a</i>}	0.28	0.25	0.12	
LOI of Lime ^b	0.45	0.66	0.23	
LOI of Coke ^c	2.10-3	2.10-3	2.10-3	
Total loss due to $LOI^{(2)}$: $a + b + c$	0.74	0.92	0.36	
Mass loss due to reduction ⁽³⁾	0.16	0.21	0.16	
Theoretical mass loss/measured mass loss: $(3)/(1)$	0.77	0.87	1.10	