

1 An overview of the Oden Arctic Technology Research Cruise 2015
2 (OATRC2015) and numerical simulations performed with SAMS
3 driven by data collected during the cruise

4 Raed Lubbad ¹ Sveinung Løset Wenjun Lu Andrei Tsarau Marnix van den Berg

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6 *Sustainable Arctic Marine and Coastal Technology (SAMCoT), Centre for Research-based Innovation (CRI)*

7 *Norwegian University of Science and Technology (NTNU), Trondheim, Norway*

8

¹ Corresponding author
E-mail address: raed.lubbad@ntnu.no

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40 **Abstract**

41 In the autumn of 2015, the Norwegian University of Science and Technology (NTNU) and the Swedish Polar
42 Research Secretariat (SPRS) performed a research cruise named the “Oden Arctic Technology Research Cruise
43 2015” (OATRC2015); it involved the two Swedish icebreakers, Oden and Frej, in the international waters north
44 of Svalbard. The ExxonMobil Upstream Research Company supported and participated in OATRC2015. The
45 overall objective of OATRC2015 was to perform a safe cruise, collect valuable and important scientific data, and
46 conduct full-scale field trials to test key technologies. The scientific scope of OATRC2015 included three major
47 fields of study, namely: 1) collection of full-scale data necessary to build, calibrate and validate numerical models
48 for floaters in ice, 2) collection of full-scale data necessary to build, calibrate and validate numerical models for
49 ice management operations, and 3) collection of data for health, safety and environmental research. This paper
50 presents OATRC2015, including the objectives of the expedition, and provides an overview of the research
51 performed and the major findings. In addition, the paper includes an extensive discussion on the use of full-scale
52 data from OATRC2015 to validate the Simulator for Arctic Marine Structures (SAMS).

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59 **Keywords:**

60 OATRC2015, Full-scale data, Ice Management, Validation, SAMS

61

62 **1 Introduction**

63 In 2012, the Norwegian University of Science and Technology (NTNU) and the Swedish Polar Research
64 Secretariat (SPRS) established a collaboration in polar research under the umbrella of the memorandum of
65 understanding, “Nordic Cooperation in Polar Research”, signed on January 29, 2010. A manifestation of the
66 collaboration between NTNU and SPRS includes a series of Arctic research cruises. In the autumn of 2015, NTNU
67 and SPRS performed the third research cruise named the “Oden Arctic Technology Research Cruise 2015”
68 (OATRC2015), which involved the two Swedish icebreakers, Oden and Frej, in the international waters north of
69 Spitsbergen. The ExxonMobil Upstream Research Company supported and participated in OATRC2015.

70 The overall objective of OATRC2015 was to perform a safe cruise, collect valuable and important scientific data,
71 and conduct full-scale field trials to test key technologies. The scientific scope of OATRC2015 included three
72 major fields of study, namely: 1) collection of full-scale data necessary to build, calibrate and validate numerical
73 models for floaters in ice, 2) collection of full-scale data necessary to build, calibrate and validate numerical models
74 for ice management operations, and 3) collection of data relevant for health, safety and environmental research.

75 OATRC2015 was successful in its objectives and generated a considerable amount of environmental data,
76 including ice, metocean, and biodiversity data, along with a unique dataset on icebreaker performance and ice
77 management operations. An overview of the research conducted, and major findings are provided below.

78 In addition, the following text introduces a newly released Simulator for Arctic Marine Structures (SAMS), which
79 is a product of NTNU’s spin-off company: Arctic Integrated Solutions AS (ArcISo). The text includes an extensive
80 discussion on the use of OATRC2015 full-scale data to validate SAMS.

81 **2 OATRC2015 Overview**

82 The Swedish icebreakers, Oden and Frej, were used in the research cruise. Fig. 1 shows a picture of the two
83 icebreakers conducting ice management trials in the Arctic Ocean during OATRC2015. Table 1 shows the
84 technical specifications of the icebreakers. An AS-355NP helicopter was also used during the expedition, and
85 flight operations were based off the Oden. During planning and preparation, both vessels and the helicopter
86 operations were thoroughly reviewed and prepared for the expedition.

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Fig. 1 Icebreakers Oden and Frej testing ice management tactics during OATRC2015.

Table 1 Technical data of Oden and Frej.

Oden	
Length	107.75 m
Beam	31.2 m
Draft	7.0-8.5 m
Total power	18 MW, 24500 hp
Speed in open water	15 knots, normal sea speed 11 knots
Crew	23 persons, up to 50 scientists
Icebreaking capability	1.9 m level ice at 3 knots
Bunker capacity	4600 m ³ , equal to 27000 nmi in open sea at 13 knots or 100 days
Displacement	11000 – 13000 tonnes
Propulsion	4 medium speed, 8-cylinder Sulzer diesel engines. 2 propellers in nozzles
Building yard	Götaverken-Arendal AB 1988 (NB953)
Owner	Swedish Maritime Administration
Frej	
Length	105.7 m
Beam	23.8 m
Draft	8.3 m
Total power generators	25 000 hp
Speed in open water	18 knots, normal sea speed 12 knots
Crew	25 persons, up to 25 scientists
Icebreaking capability	1.2 m level ice at 3 knots
Bunker capacity Heavy fuel	1400 m ³
Displacement	7800 t
Propulsion	2 front, 2 aft electric engines
Building yard	Helsinki Shipyard
Owner	Swedish Maritime Administration

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90 Sixty-two scientists and supporting personnel participated in the research cruise. A full list of participating
91 organisations is listed under the acknowledgements section in this paper. SPRS performed a medical risk
92 assessment followed by a thorough medical screening of all participants with special focus on the remote Arctic
93 operations.

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95 The cruise began on the 18th of September 2015 from Longyearbyen, and the icebreakers returned to Longyearbyen
 96 on the 2nd of October 2015. Fig. 2 shows the complete timeline of OATRC2015. Fig. 3 displays the tracks of the
 97 two vessels during the research cruise. The two icebreakers generally followed the same pathway to the ice pack
 98 north of Svalbard while conducting some preliminary communications testing. However, on the return trip, the
 99 two icebreakers adopted different pathways due to an encroaching autumn storm system.

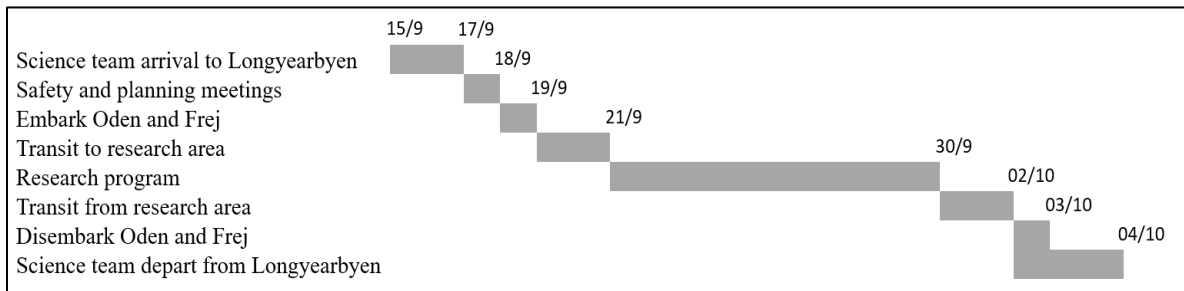


Fig. 2. OATRC2015 timeline.

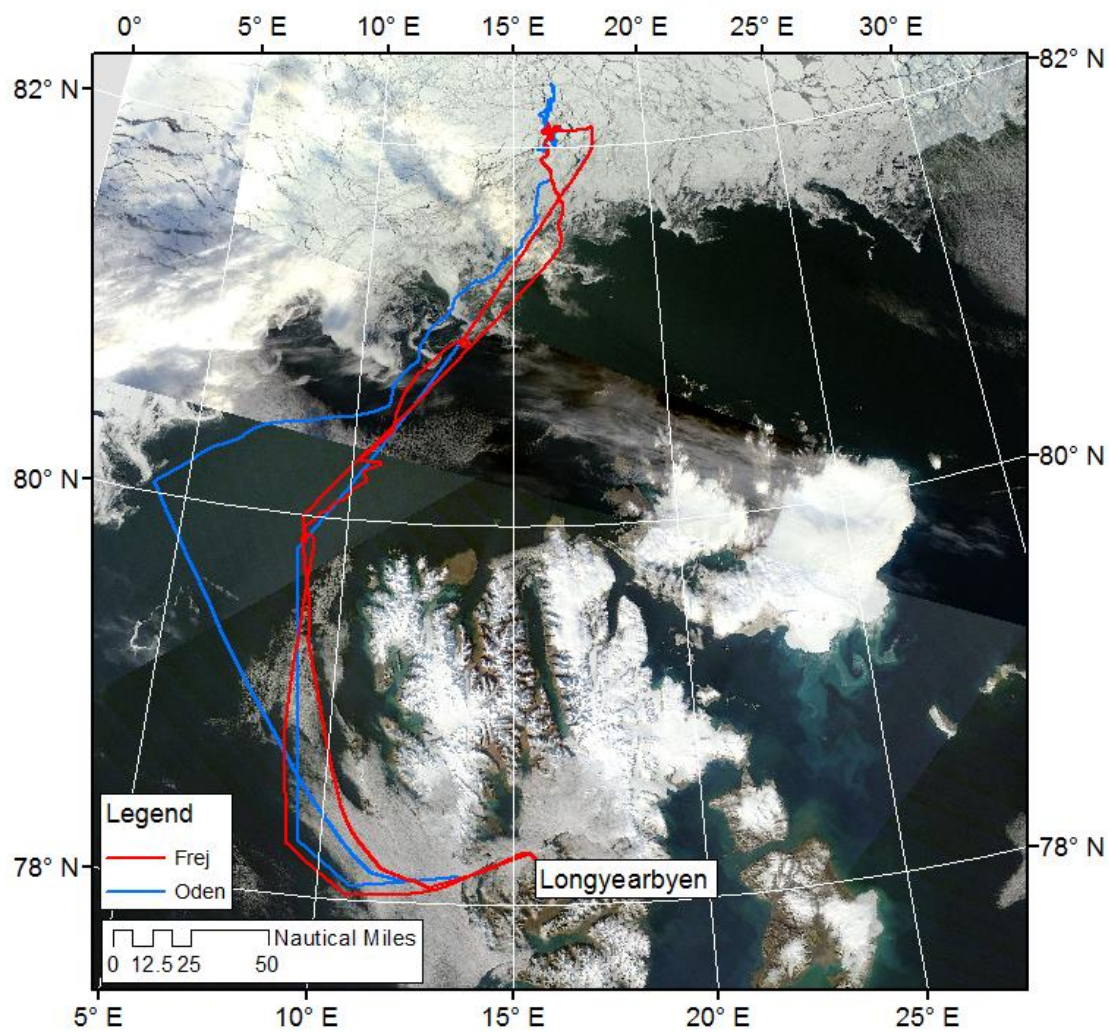


Fig. 3. Routes of the Oden and Frej: 18.09.2015 to 02.10.2015. NASA Worldview, (see Worldview).

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104 Longyearbyen was used as the shore base for the expedition. Safety and planning meetings were held at the
105 University Centre in Svalbard (UNIS) in the days prior to the expedition. UNIS provided safety oversight for
106 OATRC2015, leading risk assessments and emergency planning and training, and on-board field safety experts.
107 Loading of the equipment and vessel outfitting were conducted at Longyearbyen, Svalbard and at the vessels'
108 home ports in Sweden.

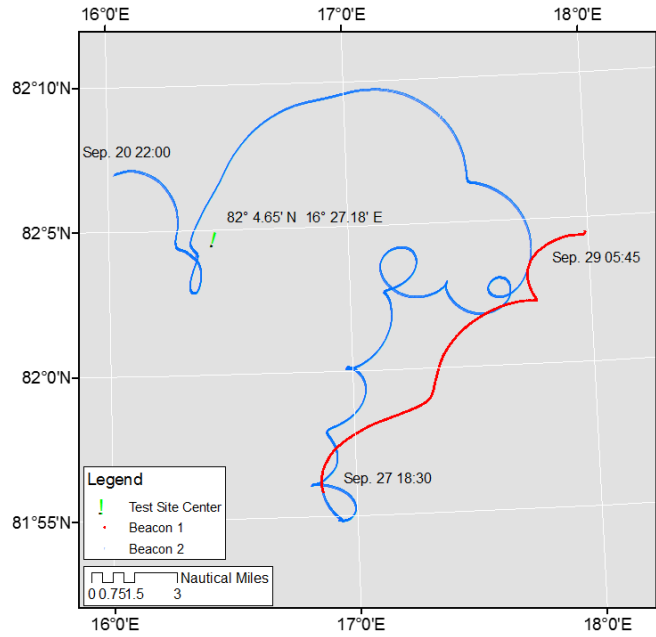
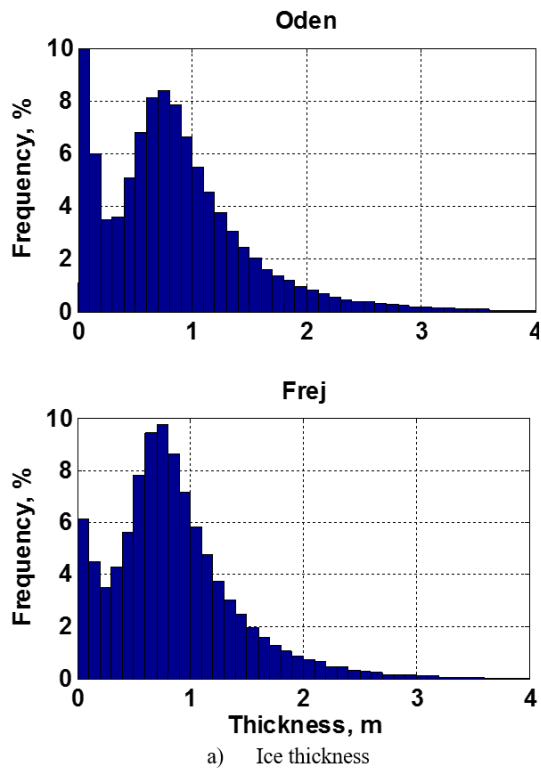
109 The ice conditions on September 18, 2015 are shown in the background image of Fig. 3. Sea ice conditions suitable
110 for the Frej to safely and effectively operate were specifically sought out for the trials. Hence, the trials were
111 conducted in predominantly medium first-year ice, with an average thickness in the range of 0.7 to 1.2 m and
112 mostly 9+ tenths ice concentration. The ice thickness was continuously measured in real time using Electro-
113 Magnetic (EM) systems hung over the bow of each icebreakers (Fig. 4a). Such methods have been used in previous
114 research expeditions (Haas et al., 2011). In addition to the EM system, a supporting ice thickness camera was also
115 installed to visually extract the ice thickness information (Lu et al., 2016a). Both thin and thick first-year ice, as
116 well as young ice and some older ice inclusions, were also occasionally encountered. Fig. 5 shows typical views
117 of the ice conditions encountered.

118 A trace of the beacon-measured ice drift over the 14-day trials period is shown in Fig. 4b. This trace is the
119 combination of two beacons deployed during OATRC2015. Most tests were conducted around a fixed waypoint
120 ($82^{\circ} 4.65'N$ $16^{\circ} 27.18'E$). Local radio and satellite ice drift beacons were used to monitor ice drift during the trials,
121 as well as long-term regional ice drifts. As shown in Fig. 4b, during the 14-day expedition, there were numerous
122 Coriolis loops and cusps at approximate 12-hour intervals, and several 180° drift reversals in response to changing
123 winds. Ice drift speeds during the period ranged from 0 to 0.4 m/s, with an overall average of approximately 0.2
124 m/s.

125 Apart from the storm event during the return transit, the general weather conditions were good, with varying
126 visibility and low to moderate wind speeds. The air temperatures ranged between $+4^{\circ}C$ and $-13^{\circ}C$. Helicopter
127 operations were limited by weather on only a few occasions; however, some fog and snowfall were encountered,
128 providing an opportunity to test the ice management operations and technology in conditions with reduced
129 visibility.

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Fig. 4. Observed ice thickness and ice drift.



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Fig. 5. Photos of typical ice conditions.

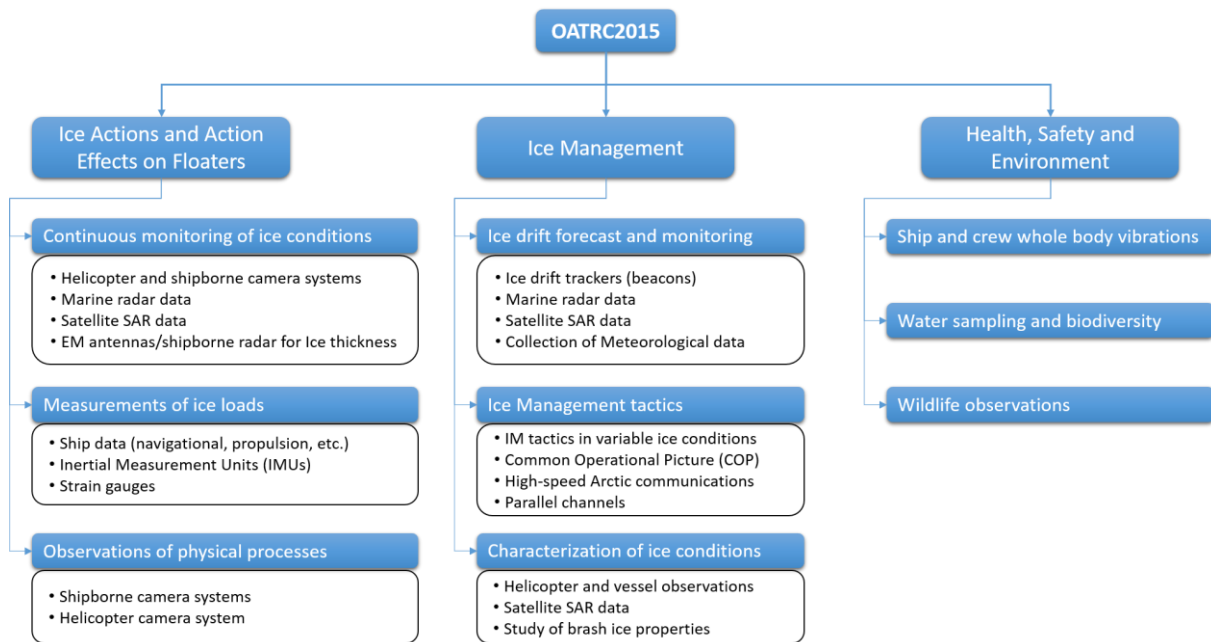
136 3 OATRC2015 Research Program

137 The scientific scope of OATRC2015 included three major fields of study:

- 138 • Collection of full-scale data necessary to build, calibrate and validate numerical models for floaters in ice,
- 139 • Collection of full-scale data necessary to build, calibrate and validate numerical models for ice management,
- 140

- 141 • Collection of data relevant to health, safety and environmental research.

142 Fig. 6 illustrates the scope of OATRC2015, and the numerous research activities that were performed during the
 143 14-day field programme. This paper provides a brief description of the performed research. A detailed description
 144 of the activities can be found in the companion papers in this special issue.



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Fig. 6. OATRC2015 research activities.

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148 3.1 Ice Actions and Action Effects on Floaters

149 One of the main objectives of OATRC2015 was to collect the necessary full-scale data to build, calibrate and
 150 validate theoretical models for estimating ice actions and action effects on floating structures. This included
 151 quantification of the sea-ice environment, observation of the ice-ship interaction processes, measurements of the
 152 local and global ice loads on the ship, and measurement of the ship response. Fig. 7 provides some example data
 153 collected under this research thrust.

154 3.1.1 Continuous monitoring of ice conditions and Observations of Physical Processes

155 Numerous cameras of three types were installed on Oden and Frej:

156 Type #1: Cameras to document the ice conditions (e.g., 360° camera, 180° camera, forward, aft);

157 Type #2: Cameras to observe ice-structure interaction zones (i.e., bow video cameras);

158 Type #3: Cameras to measure the ice thickness, wake region, parallel channel effect and floe motion.

168 Furthermore, a total of 12 helicopter flights were conducted to document ice conditions using high-resolution
169 photography. The AS-335NP helicopter was used for photographing, and it was equipped with a camera system
170 consisting of a 6-axes gyro stabilised camera support (i.e., ShotOver F1) and a Red Dragon camera with Fujinon
171 25 – 300 mm lens. All the images were enriched with real-time information, such as latitude, longitude, and the
172 camera's filming parameters (i.e., pan, tilt and roll angles). Fig. 7b provides an example of the imagery collected
173 during OATRC2015. In Fig. 7b, the Oden can be seen passing perpendicularly through an existing ice management
174 channel. A small unmanned aerial system (UAS) was also tested for the collection of aerial photography near the
175 Frej. The UAS collected limited data, as flight operations were challenged by the marine Arctic conditions.

176 Finally, ice enhanced marine radar was used on both icebreakers to monitor the local ice conditions and ice drift
177 (Shafrova et al., 2016). As noted above, EM instruments were deployed on both icebreakers to measure the ice
178 thickness. The use of a radar system to monitor ice thickness was also tested during the expedition.

179 **3.1.2 Measurement of ice loads**

180 The Oden's and the Frej's navigational and propulsion data (e.g., position, heading, speed over ground, shaft power,
181 propeller RPM and pitch, rudder angles) were continuously logged. These data in combination with the data
182 collected on ice conditions (e.g., ice thickness, floe size distribution, concentration) are very useful to analyse the
183 performance of the two vessels in different ice conditions.

184 The vibrations of the Oden and Frej due to ice actions were measured with inertial measurement units (IMUs). On
185 each icebreaker, 4 IMUs were placed close to the ice interaction zone. Each IMU contained six sensors, i.e., three
186 accelerometers and three gyros, measuring the six degrees of freedom (6DOF) motion of the ship. This enables
187 the calculation of global ice loads on the vessels, see Kjerstad and Skjetne (2016). The IMU data are also useful
188 to study the different ice failure modes and possibly to anticipate changes in ice drift direction (Heyn and Skjetne,
189 2016). Heyn and Skjetne (2018) applied the Wigner-Ville distribution on the ice-induced acceleration
190 measurements, which gives time-varying energy spectral densities and significantly improves the frequency
191 analysis of the ice-load signals. They provided examples of different ship-ice interaction events, which underline
192 that the time-frequency distribution can be used to identify different ship-ice interaction events and to evaluate the
193 severity of ice actions on the ship.

194 A system was designed and installed on the icebreaker, Frej, to measure the local ice loads on the vessel (Piercy
195 et al., 2016). The system consisted of an array of over 160 strain gauges installed over three panels on the bow and
196 shoulder of the vessel. The instrumented locations are shown in Fig. 7c. Physical calibrations onsite were

197 performed as quality checks on the gauge installation and to benchmark the finite element model (Fig. 7d) used to
198 convert the measured strain data into pressures. More than 200 hours of ice loads data were collected throughout
199 the programme, including measurements while station-keeping in managed ice conditions, actively managing ice,
200 and transiting. Fenz et al. (2018) used the up-crossing rate method to analyse the local pressure data from the Frej.
201 They concluded that the local pressures from station-keeping in managed ice are two to four times lower than the
202 transiting cases. They claimed that such a finding provides a sound basis for advocating for local design pressures
203 that are lower than the current recommendations, which can potentially extend the operating envelope of offshore
204 vessels, leading to significant savings.

205

206 **3.2 Ice Management**

207 One of the main objectives of OATRC2015 was to collect full-scale data necessary to build, calibrate and validate
208 theoretical models for ice management (IM) operations. This includes: forecasting and monitoring of ice drifts,
209 performing IM tactics in various ice conditions, and monitoring outgoing ice conditions resulting from different
210 ice management scenarios. Fig. 8 provides example data collected under this research thrust.

211 **3.2.1 Ice drift forecasting and monitoring**

212 Ice drift beacons were used to provide input to ice management field operations and to study long term regional
213 ice drift. Both locally transmitting radio and satellite Iridium beacons were used. Fig. 4b shows example drift data
214 collected during the campaign. The drift data were also used to benchmark satellite methods for monitoring ice
215 drift and to test tactical ice drift forecasts. Fig. 8a provides example regional ice drift information extracted from
216 the Sentinel-1 satellite imagery.

217 Mitchell and Shafrova (2018) describe a free drift tactical ice forecast model, developed by the ExxonMobil
218 Upstream Research Company (EMURC) and designed to forecast the drift of individual ice floes in low ice
219 concentrations. The model was applied in near real time during OATRC2015. Mitchell and Shafrova (2018)
220 compare the forecast results with the drift data collected during OATRC2015. The results show that the free drift
221 forecasting tool produces reasonably accurate and useful forecasts in the high concentration ice observed.

222 **3.2.2 Ice management tactics**

223 Various icebreaker fleet deployment tactics were tested during OATRC2015. During these tests, the Oden and
224 Frej were deployed in systematic ice management patterns around a stationary waypoint to assess the resulting
225 managed ice conditions. Approximately 150 hours of ice management tests were conducted, with the longest test

226 lasting approximately 90 hours. The systematic commands for the two icebreakers were communicated using a
227 Common Operational Picture (COP). The COP was used to analyse incoming ice conditions and generate ice
228 management commands for display on the bridge of both icebreakers. Fig. 8b shows orbital ice management tactics
229 on the icebreaker captains' view of the COP. In this test, the Oden was acting as the primary icebreaker, following
230 the largest diameter orbital path around the fixed waypoint. The Frej was acting as the secondary icebreaker,
231 further reducing the floe size in a smaller orbital pattern around the fixed waypoint. Ice management tactics and
232 COP are further discussed by Hamilton et al. (2016) and by Shafrova et al. (2016), respectively.

233 Kinematic simulations were used to design the systematic arched racetrack tactics that were implemented and
234 tested during OATRC2015. Holub et al. (2018) compared the simulation results with the data from OATRC2015.
235 They showed that the virtual drilling rig was maintained within the managed ice channel in complex ice drift
236 conditions that included multiple ice drift loops, cusps, and reversals; which confirm the fundamental simulation
237 methods.

238 Omnidirectional radio antenna units (KM Seatex MBR 179) were installed on both the Oden and Frej to ensure a
239 high bandwidth data link for IP-based video streaming, VoIP, and data communication between the vessels. In
240 addition, a customised Gb-WiFi inter-vessel network was configured and installed on both vessels. The inter-
241 vessel communication between the icebreakers was systematically tested, and the performance of the MBR link
242 and WiFi link were compared. During the 14-day programme, the MBR link worked robustly, without any fallouts,
243 giving a data rate of approximately 380 MB/s. The WiFi-link, on the other hand, had a shorter range, but gave
244 higher speeds at lower output power.

245 **3.2.3 Characterisation of ice conditions**

246 During ice management operations, a narrow parallel channel spacing can effectively reduce ice floe sizes at the
247 protected vessel/structure. However, a channel spacing that is too narrow might lead to excessive, or even
248 impractical, ice management operations. During OATRC2015, several parallel channel tests were conducted. Fig.
249 8c shows a typical snapshot of the ice conditions while carrying out parallel channel tests. An image processing
250 technique was used to extract information about the cracks that formed between the neighbouring parallel channels.
251 Crack orientation and occurrence frequency were quantified versus different channel spacing to reveal the
252 relationship between the parallel channel spacing and the size of the generated ice floes during an IM operation
253 (Lu et al., 2016b). Lu et al. (2018a) presented a theoretical model for parallel channels' fracturing mechanism

254 during ice management operations, and Lu et al. (2018b) used full-scale data from OATRC2015 to validate that
255 model.

256 Satellite data of various forms were used 1) to prepare for the expedition and site selection, 2) to monitor ice
257 conditions and experimental results during the field campaign, and 3) for ice monitoring following the trials. The
258 satellite data used at different stages of OATRC2015 cover a wide spectrum ranging from ultra-high-resolution
259 images (e.g., WorldView 3 optical satellite imagery with 30 cm resolution and CosmoSkyMed X-band radar
260 satellite imagery with 1.0 m resolution) to lower resolution images (e.g., AQUA/TERRA MODIS optical satellite
261 imagery with 250 m resolution and 40 m resolution Sentinel-1 C-band radar imagery). Matskevitch et al. (2016)
262 reports that 228 satellite images were acquired and analysed in support of OATRC2015.

263 The properties of the brash ice produced during IM were tested repeatedly. Each test took approximately 10
264 minutes, and it measured the brash ice thickness, friction at uplift and weight of ice blocks. The experimental setup
265 is shown in Fig. 8d, and it can be described as an umbrella, 2 m in diameter and 3 m in height. In total, 18 tests
266 were performed, measuring brash ice properties at 14 different locations. The measured brash ice thicknesses were
267 between 0.6 m and 1.3 m, which is in good agreement with the EM-measurements. The peak load at uplift was
268 typically twice the weight of the ice for interlocked ice blocks and very small for free-floating blocks. The data
269 from the brash ice tests will be used later to verify numerical models of brash ice.

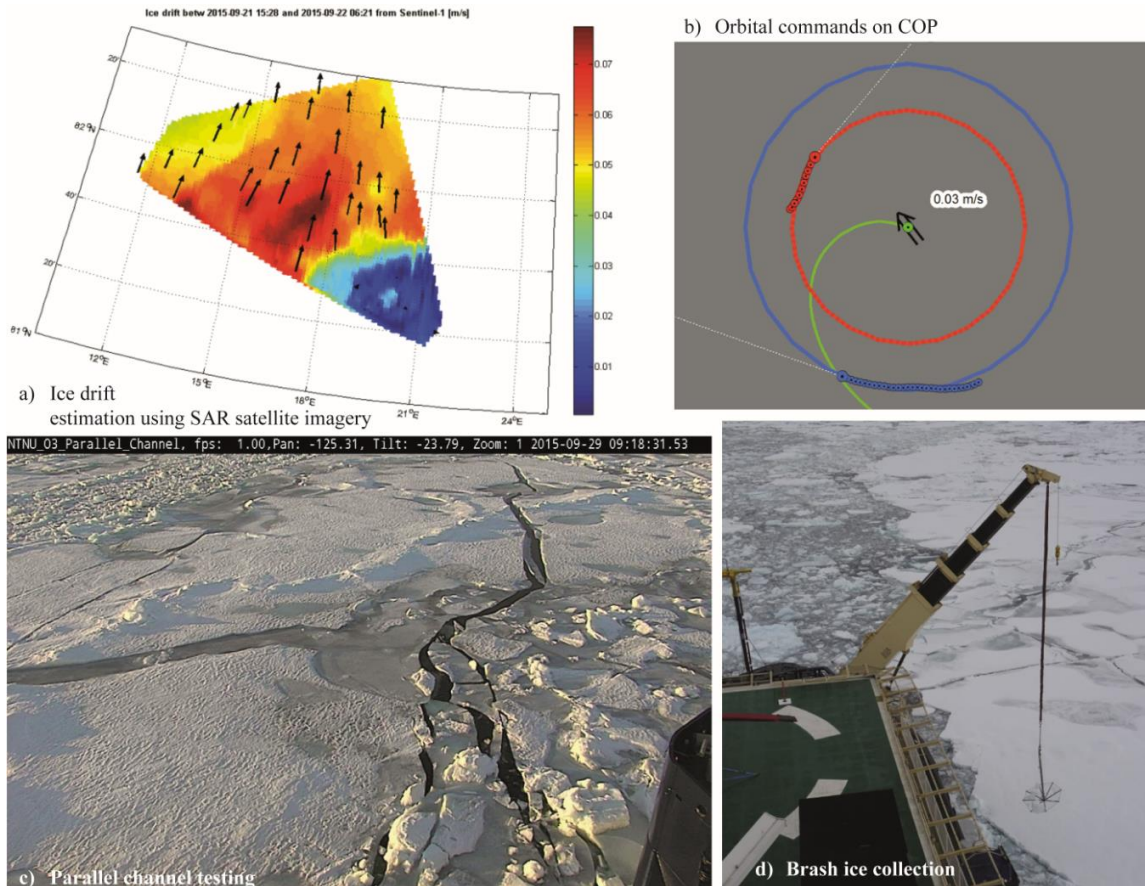


Fig. 8. Ice management.

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3.3 Health, Safety, and Environment

278 One of the main objectives of OATRC2015 was to collect data for health, safety, and environment research. This
279 included data on ship and crew vibrations during icebreaking operation, water collection and processing to
280 understand marine biodiversity, and wildlife observations.

3.3.1 Ship and crew vibrations

282 The level of exposure to whole body vibrations for the Oden and Frej crew during icebreaking conditions were
283 measured. The purpose of this measurement was to investigate whether problems with the lower back are more
284 common among icebreaker crew members. The methods used in the study include a variety of physical
285 measurements and a questionnaire (Johannesson, 2016), see Fig. 9a.

3.3.2 Water sampling and biodiversity

287 A total of 9 stations and 12 casts were performed with the Oden's CTD (Conductivity, Temperature, and Depth)
288 (see Fig. 9b) to collect hydrographic data and sample water from different depths. The system used was a SeaBird

289 911+ with 11+ deck unit CTD equipped with 23 Niskin bottles of 6 litres each. The measured parameters were:
 290 temperature (°C), salinity (psu), oxygen content (ml/L), conductivity (S/m) and sound velocity (m/s). Samples
 291 were taken for biological analyses of bacteria, chlorophyll, nutrients, and pigments. Typical depths for samples
 292 were bottom, 225, 40, 25 and 10 metres.

293 The seawater samples were also used for environmental genomics analysis. Environmental genomics is an
 294 evolving technology area that is used to characterise biodiversity in a survey region by analysing the environmental
 295 DNA in environmental media, such as seawater or sediment (N'Guessan et al., 2012; Baird and Hajibabaei, 2012).
 296 In addition to samples collected using the CTD, the samples were also collected using the Oden's underway system
 297 throughout the journey. Once the seawater samples are processed and analysed, the DNA sequence data will be
 298 compared to a genomic database and will allow for the identification of known and potentially unknown marine
 299 organisms. These data will then be validated against marine mammal observations made by the Marine Wildlife
 300 Observers (MWO) who were also present on the vessel (see Table 2).



Fig. 9. Health, Safety and Environment.

Table 2. Marine wildlife observations

Marine mammal species	Total individuals	Total observations	Bird species	Hours observed
Blue whale	3	2	Fulmar	53
Fin whale	6	5	Pomarine jaeger/skua	2
Minke whale	4	4	Arctic jaeger/skua	1
Unidentified large whale	4	3	Ivory gull	110
Orca	7	2	Glaucous gull	27
Bearded seal	2	2	Kittiwake	37
Hooded seal	8	5	Arctic tern	1
Ringed seal	4	3	Brünnich's guillemot	11

Harp seal	2	1		Puffin	4
Unidentified seal	15	12		Black guillemot	26
Polar bear	9	7		Little auk/dovekie	9
Unspecified mammal	5	3		Snow bunting	5
Total	69	49		Total	286

304 **4 Simulator for Arctic Marine Structures (SAMS)**

305 As offshore activities in the Arctic constitute a relatively new field, with only a handful of relevant operations to
306 draw experience from, and since full-scale trials are extremely expensive, there is an expressed need for much
307 more extensive, detailed and cost-efficient analysis of concepts based on numerical simulations. However, until
308 recently, simulation tools of sufficient quality to perform such numerical analysis have not existed. The only
309 verification available has been through a limited set of experiments in ice model basins. Today, this has changed,
310 partly through the efforts at NTNU hosting SAMCoT (Centre for Research-based Innovation - Sustainable Arctic
311 Marine and Coastal Technology), laying the foundation of a versatile and highly accurate high-fidelity numerical
312 simulator for offshore structures in various ice conditions, such as level ice, broken ice and ice ridges.

313 Arctic Integrated Solutions AS (ArcISo) is a spin-off company from NTNU, established in 2015 with the vision
314 of increasing the technology readiness level of SAMCoT's numerical models to become a professional software
315 package for the analysis of sea ice actions and action effects on Arctic offshore structures. This software package
316 is now called the Simulator for Arctic Marine Structures (SAMS), and it was first released in 2017. The following
317 text briefly introduces the theoretical basis of SAMS, and it discusses the potential use of OATRC2015 full-scale
318 data to validate the simulator. Recall that one of the major objectives for OATRC2015 was to collect the necessary
319 full-scale data to build, calibrate and validate numerical simulators for floaters in ice.

320 **4.1 Theoretical Basis for SAMS**

321 This section gives only a brief description of the theoretical basis for SAMS. More details can be found in
322 numerous earlier publications. An overview paper, which gives a thorough description of the theory and software
323 implementation of SAMS, is in progress and will be submitted for publication soon.

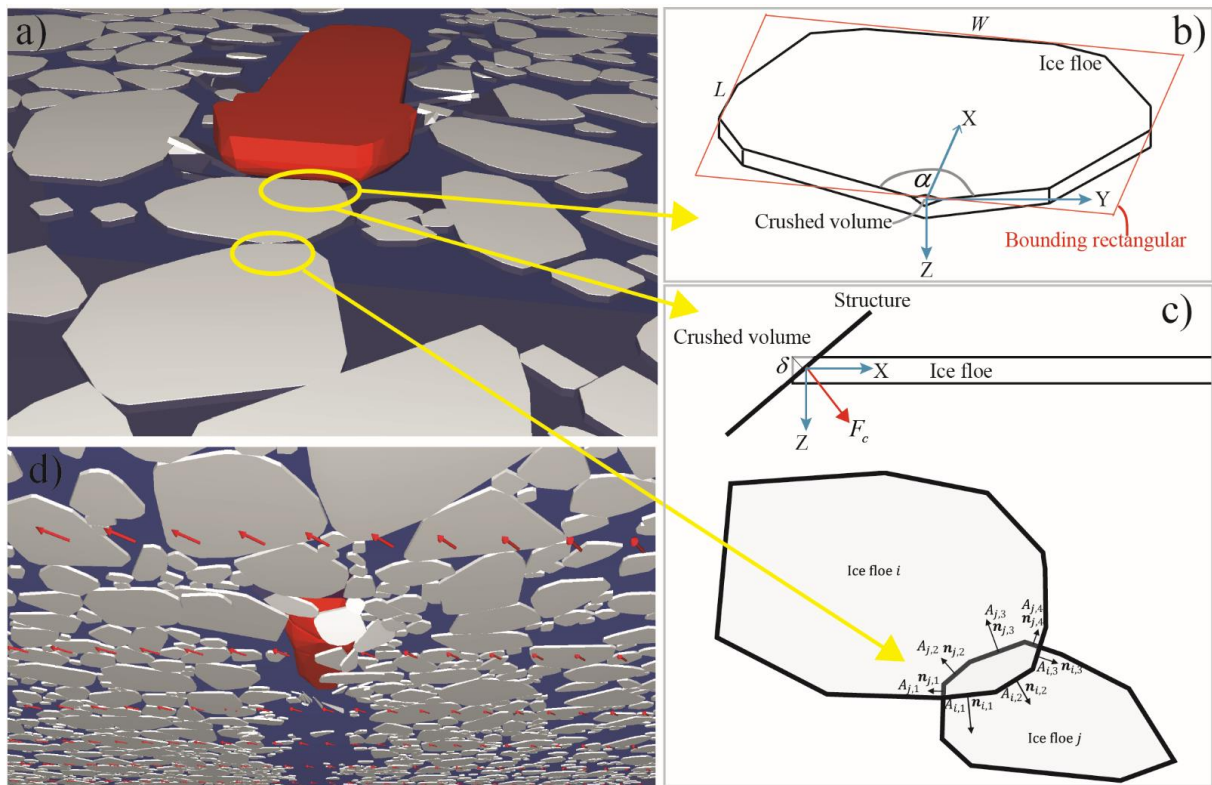
324 Depending on the confinement, ice concentration and floe size distribution, the governing mechanisms during the
325 floe ice and floaters interactions can differ considerably. The term floe ice is quite generic, and can be used to
326 describe level ice or any fragmented ice field whether it is naturally broken, e.g., by gravity waves, or artificially
327 broken, e.g., by ice management (IM) operations.

328 For the numerical modelling of a floater in floe ice, time-domain modelling is inevitable due to the considerable
329 nonlinearities in the interaction processes between ice floes and the floater. The distinct nature of ice floes in a
330 broken ice field has often promoted the use of discrete element modelling methods (DEM). The latter can broadly
331 be divided into two main categories: smooth discrete element modelling (SDEM) and non-smooth discrete element
332 modelling (NDEM). The difference between the two can be seen as the difference between implicit and explicit
333 time integration, allowing much larger time steps, while maintaining stable simulations, when using NDEM.
334 SAMS falls under the NDEM category, but it applies a novel implicit time stepping scheme and an improved
335 contact model, enabling general visco-elastic contacts. This increases the accuracy and expands the applicability
336 range of the SAMS compared to existing models, see Van den Berg et al. (2017).

337 Moreover, the current version of SAMS adopts an analytical framework that supplements the NDEM method with
338 analytical closed-form solutions to simulate the fracture of sea ice. This methodology was first presented by
339 Lubbad and Løset (2011) to model the bending failure of ice. Later, the method was expanded with a number of
340 closed-form solutions that cover other failure modes, e.g., splitting and radial cracking. These solutions are
341 published in a series of papers (Lu et al., 2015a; Lu et al., 2015b; Lu et al., 2016c).

342 In addition to the improved NDEM formulation and the comprehensive set of analytical solutions to ice fracture,
343 SAMS applies innovative numerical solutions to calculate different hydrodynamic force components on the floater
344 and every ice floe in the calculation domain. This includes, among other things, drag forces from wind, current
345 and propeller flow. These solutions are calibrated and validated against full-scale and lab-scale data, see (Tsarau
346 et al., 2014; Tsarau and Løset, 2015).

347 Fig. 10 illustrates the aforesaid building block of SAMS, namely: 1) the NDEM or multi-body dynamics module,
348 2) the fracture module, and 3) the hydrodynamic module. Additional information on these modules is given below.



349

350
351
352

Fig. 10. Illustration of different modules within SAMS: a) the simulation environment; b) the fracture module; c) the NDEM or multi-body dynamic module illustrating the non-rigid contact due to ice crushing at the contact interface; d) illustration of the fluid domain, e.g., current flow, with velocity vectors.

353

354 4.1.1 Multi-body dynamic module and contact model

355 As described in the previous section, a floe ice field is represented numerically in the simulator as a collection of
 356 discrete ice bodies. The interaction forces at ice-ice and ice-structure contacts are calculated using an implicit time-
 357 stepping scheme that falls under the category of NDEM modelling. Previously, the NDEM modelling technique
 358 was applied by several researchers to model ice-structure interactions, e.g., (Alawneh et al., 2015; Dudal et al.,
 359 2015; Konno and Mizuki, 2006; Lubbad and Løset, 2011; Metrikin, 2014; Yulmetov et al., 2016). Within the
 360 framework of NDEM modelling, one of the key challenges is obtaining a physically correct contact force. The
 361 ‘traditional’ NDEM methodology only defines contact impulses, which cannot be easily translated to equivalent
 362 contact forces. This is problematic because the contact force is needed to determine whether ice failure will occur.
 363 Earlier works partly mitigated this limitation by defining an upper limit to the contact force based on the contact
 364 geometry and material properties, as is done in Lubbad and Løset (2011) and Metrikin (2014), in which both papers
 365 used a different method to limit the contact force. Others attempted to obtain a contact force by post processing of
 366 the obtained contact impulses, as is done by Yulmetov et al. (2016) and Alawneh et al. (2015).

367 SAMS uses the novel method presented by Van den Berg et al. (2017) to remedy the abovementioned problem.
 368 This method considers the contact crushing force as well as the force-penetration gradient, leading to a more
 369 accurate contact force prediction than with previously applied methods for the majority of contact cases. The
 370 contact model in SAMS assumes constant energy absorption per unit crushed volume of ice, represented by a
 371 Crushing Specific Energy value (CSE). This is in accordance with previous research (Kim and Gagnon, 2016;
 372 Kinnunen et al., 2016), and it is equivalent to a contact model with constant crushing pressure. This contact model
 373 ensures that the energy absorbed in an ice-ice or ice-structure contact matches the change in overlap volume of the
 374 interacting bodies within each time step, where the overlap volume of interacting bodies represents crushed ice.
 375 The energy match is ensured by considering the projected area of a contact occurring, and the expected change of
 376 projected area. This is used to define a force-penetration gradient, as in Eq. (1).

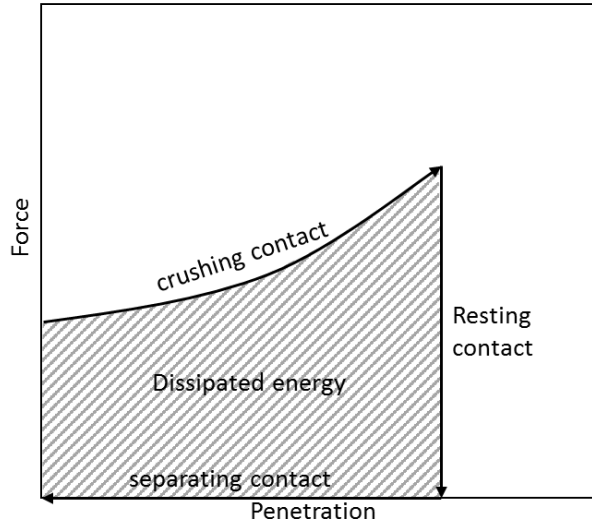
$$377 \quad \frac{\Delta F}{\Delta \delta} = \left(\frac{(A_{\text{proj}}^{\text{prop}} - A_{\text{proj}}) \text{CSE}}{\Delta \delta} \right) \quad (1)$$

378 where $A_{\text{proj}}^{\text{prop}}$ stands for the projected area when the interacting bodies are propagated with their current velocity,
 379 A_{proj} is the contact projected area at the beginning of the time step, $\Delta \delta$ is the change of contact penetration, and
 380 $\Delta F / \Delta \delta$ is the force-penetration gradient. This force-penetration gradient is used together with the projected area
 381 at the beginning of the time step to define the compliance parameters that represent local ice crushing.

382 Three types of contact behaviour can be distinguished as follows:

- 383 1. **Crushing contact.** The increase in overlap volume of interacting bodies is matched by the energy
 384 dissipated during the contact.
- 385 2. **Resting contact.** The relative velocity between the interacting bodies is zero. The contact force is
 386 determined such that the resting contact is maintained, provided that the crushing force is not exceeded,
 387 and the force needed to maintain the zero velocity is not negative (no adhesive force).
- 388 3. **Separating contact.** The contact penetration decreases, and the contact force drops to zero.

389 This contact behaviour can be considered as hysteretic damping, in which the loading/unloading curve will be
 390 similar to Fig. 11. A more detailed description of the contact model can be found in Van den Berg et al. (2017).



391

392

Fig. 11 Crushing contact implementation as hysteretic damping.

393 4.1.2 Floe ice's fracture module

394 The ice fracture module aims to simulate the fracturing of ice floes during the interaction with the floater.
 395 Previously, we investigated two different approaches to simulate ice fracture, i.e., a pure computational mechanics
 396 approach suitable for detailed design simulation, and a pure analytical approach targeting efficient simulations
 397 related to large scale Arctic marine operations.

398 The current version of SAMS implements the analytical fracture approach. The implemented algorithms can
 399 simulate local bending and global splitting failures of an ice floe interacting with the floater. The theoretical basis
 400 of these algorithms can be found at (Lubbad and Løset 201, Lu et al., 2015a; Lu et al., 2015b; Lu et al., 2016c).

401 Fig. 10a shows an illustration of an ice floe in contact with the floater. Basically, we employ Eq. (2) to calculate
 402 the contact force component F_z that is needed to initiate the local out-of-plane bending failure (Note the
 403 coordinate system in the figure).

$$404 \quad F_z = \begin{cases} \frac{\sigma_f h^2}{3} \tan\left(\frac{\alpha}{2}\right) \left[1.05 + 2\frac{\delta}{\ell} + 0.5\left(\frac{\delta}{\ell}\right)^2\right] & (\alpha \leq 90) \\ \frac{m\sigma_f h^2}{3} \tan\left(\frac{\alpha}{2m}\right) \left[1.05 + 2\frac{\delta}{\ell} + 0.5\left(\frac{\delta}{\ell}\right)^2\right] & (90 < \alpha \leq 180) \end{cases} \quad (2)$$

405 in which,

σ_f is the flexural strength of sea ice, [kPa];

h is the thickness of sea ice, [m];

α is the angle of the wedge where the local bending failure occurs, also see

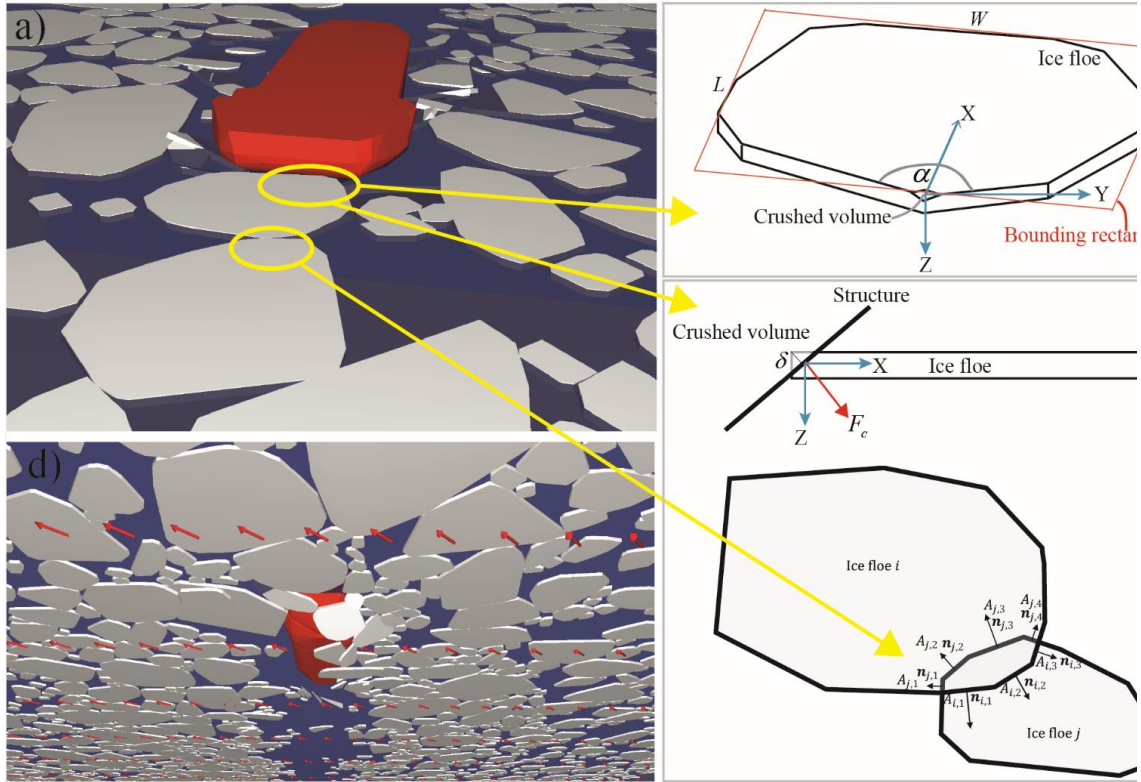


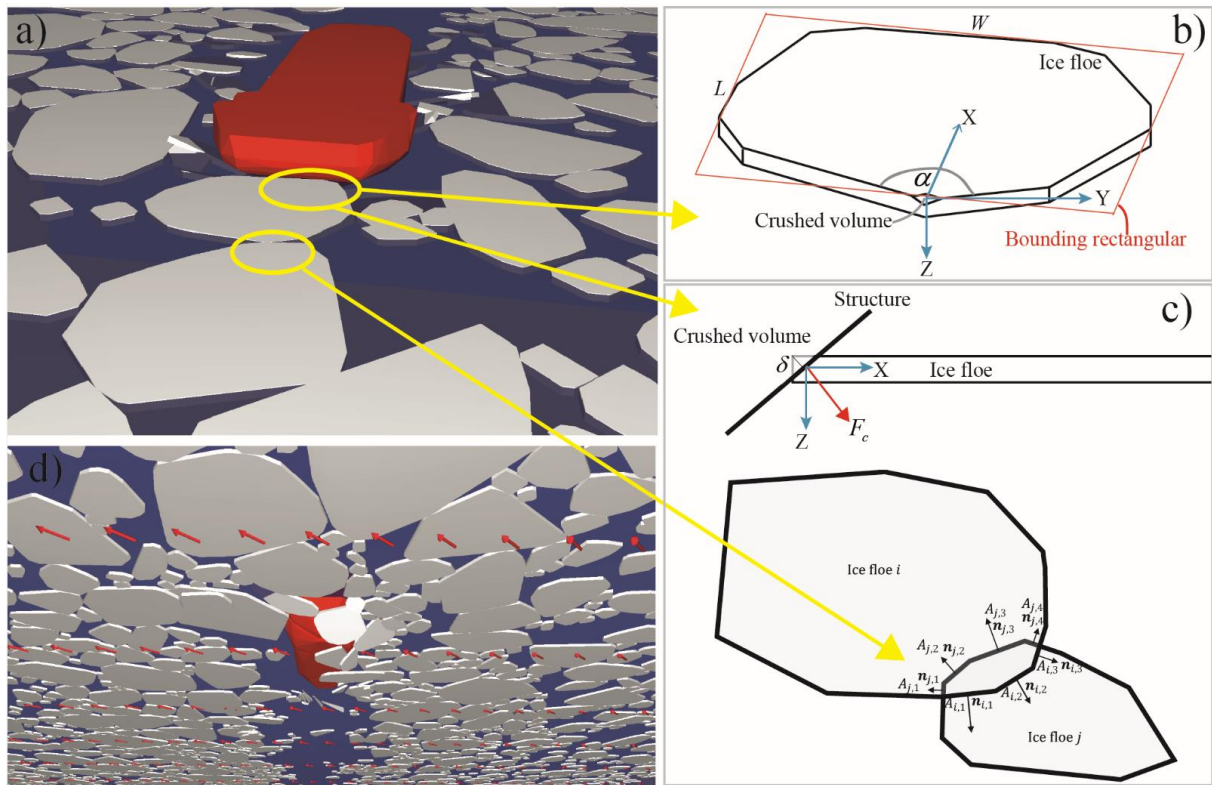
Fig. 10b, in [deg];

δ is the penetration depth and is considered equivalent to the loading area size at the wedge tip, [m];

m is the number of wedges that are bent off from the original ice sheet and is set as a random number between 2 and 3.

ℓ is the characteristic length [m] of sea ice and is calculated by $\ell = [Eh^3 / (12\rho_w g)]^{1/4}$, and E , ρ_w and g are the Young's modulus [kPa], water density [kg/m³] and gravitational acceleration [m/s²], respectively.

406 For the in-plane splitting failure mode, we have two cases: 1) centric or almost centric contacts, 2) and off-centre
 407 contacts. For the former, the fracture module employs Eq. (3) to calculate the contact force component F_y that
 408 is needed to initiate the splitting failure. The ice floe is idealised by its bounding box with a length L and width



410

411 Fig. 10b.

412

$$F_Y(a) = \frac{hK_{IC}\sqrt{L}}{H(a,0)} \quad (3)$$

413 in which,

h is the thickness of sea ice, [m];

K_{IC} is the fracture toughness of sea ice, [$\text{kPa}\sqrt{\text{m}}$];

$H(a,0)$ is the weight function of a rectangular ice floe with a centred edge crack. Its formulation can be found in Dempsey and Mu (2014)

a is the non-dimension crack length given by $a = A/L$, whereas A is the crack length and L is the length of the ice floe, as shown in Fig. 10b.

414

415 For off-centre collision cases, Eq. (4) is applied to calculate the F_Y that is needed to initiate the splitting failure.

416 These equations are derived by Lu et al. (2018a), and they take into account the crack's kink behaviour.

417
$$F_Y = \frac{f(A_0 / W_1)}{hK_{IC}\sqrt{W_1}} \quad (4)$$

418
$$f(A_0 / W_1) = \sqrt{\frac{\pi}{\pi^2 - 4}} \left(\frac{A_0}{W_1}\right)^{-1/2} + \sqrt{6} \left[1 + \frac{0.3532}{(A_0 / W_1)^{1/2}} + \frac{0.0116}{(A_0 / W_1)^1} \right] \left(\frac{A_0}{W_1}\right)$$

418 In Eq. (4),

h is the thickness of sea ice, [m];

A_0 is the length of the initial radial crack due to local bending failure, in [m]; it can be calculated as $A_0 = 2(D/k)^{0.25}$ with flexural rigidity D and the elastic foundation k of a floating ice floe, which can further calculated as $D = Eh^3 / [12(1-\nu^2)]$ and $k = \rho_w g$ with Young's modulus E , Poisson's ratio ν , water density ρ_w and gravitational acceleration g .

W_1 is the distance from the contact point to the closest free edge. As shown in Fig. 10b, the width of the bounding box $W = W_1 + W_2$ and $W_1 < W_2$. In general, it is required that $W_2 \geq 1.5 \cdot W_1$ for Eq. (4) to be valid. Otherwise, Eq. (3) is a better approximation.

419

420 For every time step, the multi-body dynamic (MBD) module detects the contacts, creates contact manifolds and
 421 calculates contact forces F_c . The fracture module calculates the failure criteria, as explained above, i.e., F_z and
 422 F_y . With this information available, the failure mode for each ice floe at each time step can be estimated according
 423 to Eq. (5),

424
$$\left\{ \begin{array}{ll} F_c \cdot \mathbf{z} \geq F_z \text{ and } F_c \cdot \mathbf{y} < F_y & \rightarrow \text{bending failure} \\ (F_c \cdot \mathbf{z} / F_z) > (F_c \cdot \mathbf{y} / F_y) \geq 1 & \rightarrow \text{bending failure} \\ (F_c \cdot \mathbf{y} / F_y) \geq (F_c \cdot \mathbf{z} / F_z) \geq 1 & \rightarrow \text{splitting failure} \\ F_c \cdot \mathbf{z} < F_z \text{ and } F_c \cdot \mathbf{y} \geq F_y & \rightarrow \text{splitting failure} \\ F_c \cdot \mathbf{z} < F_z \text{ and } F_c \cdot \mathbf{y} < F_y & \rightarrow \text{No failure} \end{array} \right. \quad (5)$$

425 in which, \mathbf{z} and \mathbf{y} are directional cosine in the vertical (z) and horizontal (y) directions, respectively. With this
 426 formulation, multiple failure modes can be achieved in the simulation, which gives more physically sound and
 427 realistic results. Fig. 12 demonstrates such coupling between local bending and global splitting failure modes in
 428 an off-centre collision scenario.

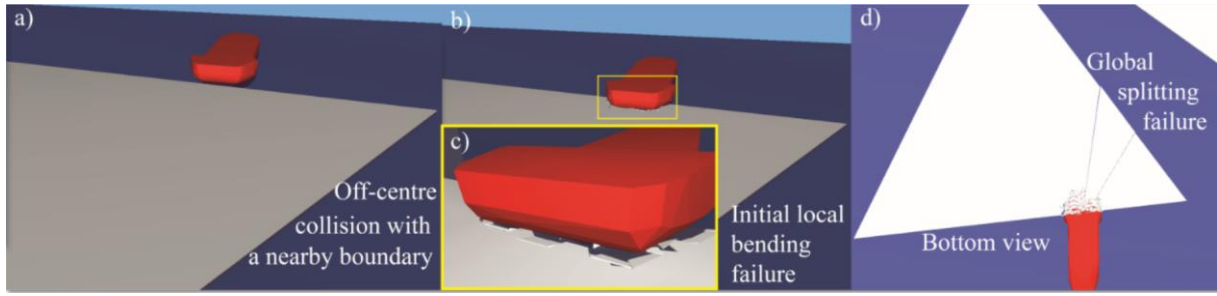


Fig. 12. Coupled local bending and global splitting failure modes in an off-centre collision case.

After ice breakings, the broken ice pieces are transported around the ship's hull (see Fig. 12d) and further interaction with the hull (structure) occurs. This is handled by the contact model described previously. In terms of simulation efficiency, built upon the MBD module, the current fracture module's analytical nature enables us to simulate unprecedentedly large temporal and spatial scales with satisfactory efficiency and accuracy.

4.1.3 Hydrodynamics module

Because all the interaction processes between the ice and structure occur within a fluid domain, the effect of hydrodynamics are present. For the current SAMS implementation, aside from the basic buoyancy of all bodies, the hydrodynamic forces, including the force due to the propeller flow, upon each individual ice floe and the structure are assigned explicitly, and ice drift simulations are possible given wind and/or current conditions. The total hydrodynamic force on a rigid body is considered here as a combination of the so-called form drag and skin-friction drag. The form drag arises because of the shape of the body, and follows the quadratic drag equation. It is higher for bodies with a larger presented cross section, and increases with the square of the flow velocity. The skin friction is caused by the viscous forces in the boundary layer at the body/fluid interface, and it is directly related to the wetted surface of the body, and rises with the square of the velocity component parallel to the wetted surface.

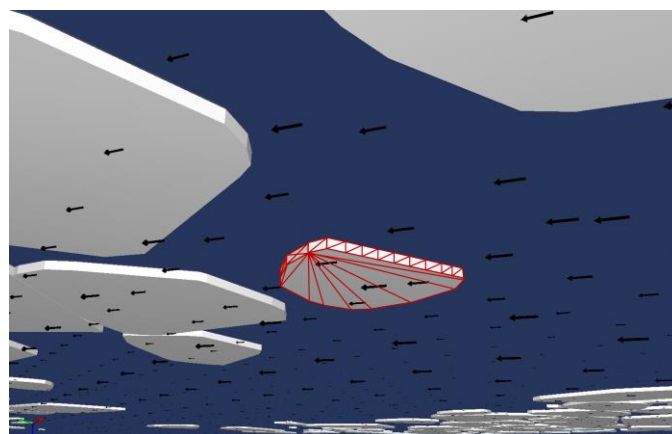
For an arbitrary rigid body in the presented simulator, the total hydrodynamic force is obtained by integrating the two drag components over the body's surface. A triangular mesh, as shown in Fig. 13, may be used to discretise the body's surface, which is useful for both the representation of the body's geometry and the calculation of the hydrodynamic forces. For the latter, the sum of the drag forces on the wholly immersed triangles is obtained as follows:

$$\mathbf{F}_h = \sum_{k=1}^M \left[\rho_w C_f S^k |\mathbf{U}_{\parallel}^k| \mathbf{U}_{\parallel}^k - \left(\frac{1}{2} \rho_w C_d S^k [(\mathbf{U}^k \cdot \mathbf{n}^k)]^2 \mathbf{n}^k \right) \right]_{(\mathbf{U}^k \cdot \mathbf{n}^k) < 0} \quad (6)$$

451 where \mathbf{F}_h is the total hydrodynamic drag force on the rigid body; M is the number of the wholly immersed
 452 triangles on the body's surface; ρ_w is water density; S^k is the surface area of the k -th triangle; \mathbf{U}^k is the
 453 relative fluid velocity at the geometrical centre of the triangle; \mathbf{n}^k is a unit vector normal to the triangle and
 454 pointing outwards from the body's interior; \mathbf{U}_{\parallel}^k is the tangential velocity calculated as
 455 $\mathbf{U}_{\parallel}^k = \mathbf{U}^k - (\mathbf{U}^k \cdot \mathbf{n}^k)\mathbf{n}^k$; and, finally, C_f and C_d are the drag coefficients due to skin friction and pressure,
 456 respectively. The expression in parentheses in Eq. (6) is calculated only if \mathbf{U}^k points towards the body's interior;
 457 otherwise it is 0. The moment due to the force \mathbf{F}_h can be obtained as follows:

$$458 \quad \mathbf{T}_h = \sum_{k=1}^M \mathbf{r}^k \times \left[\rho_w C_f S^k |\mathbf{U}_{\parallel}^k| \mathbf{U}_{\parallel}^k - \left(\frac{1}{2} \rho_w C_d S^k [(\mathbf{U}^k \cdot \mathbf{n}^k)]^2 \mathbf{n}^k \right) \right]_{(\mathbf{U}^k \cdot \mathbf{n}^k) < 0} \quad (7)$$

459 where \mathbf{r}^k is the radius vector directed from the body's centre of mass to the geometrical centre of the k -th triangle.
 460 As shown below, Eqs. (6) and (7) provide an effective way to parameterise the fluid drag on ice features, and
 461 allows the consideration of different ice shapes and various flow regimes, e.g., propeller jets. Further details on
 462 the inclusion of propeller flow within SAMS' hydrodynamic module are given in another paper within this special
 463 issue, Tsarau et al. (2018), which also presents the OATRC2015 experimental data to calibrate the presented model.



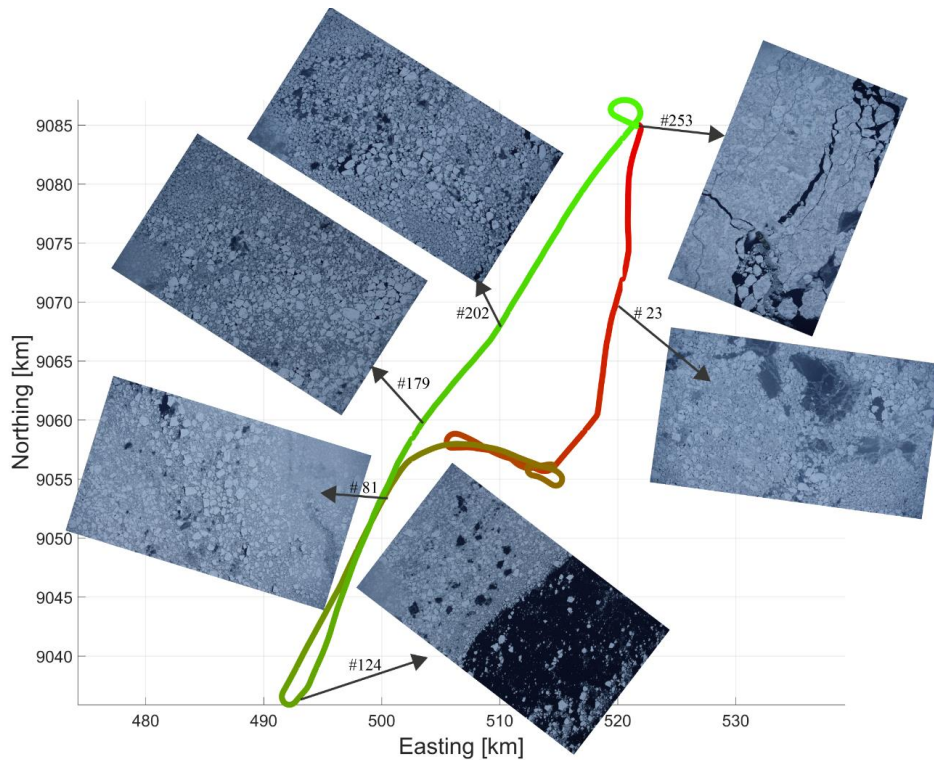
464
 465 Fig. 13. Ice floes represented by triangular meshes. The mesh is automatically refined by SAMS if the flow is not uniform.
 466

467 4.2 Validation of SAMS using OATRC2015 full-scale data

468 The different modules described above were developed over many years by a number of researchers at NTNU.
469 Despite the common vision of creating a numerical simulator for floaters in ice, the development of each module
470 was carried out almost independently from the other modules. At that stage, many attempts were also made to
471 validate each module against available full-scale and lab-scale data (Lu et al., 2015a; Lu et al., 2015b; Lu et al.,
472 2016c, Tsarau and Løset, 2015; Tsarau et al., 2014). In 2016, ArcISO was established to refactor and integrate the
473 different modules to build SAMS as a versatile and highly accurate high-fidelity numerical simulator of offshore
474 structures in floe-ice conditions. To achieve this, a firm quality control system was implemented to ensure clean,
475 readable, maintainable code that is tested and verified. In addition, great attention is given to the validation and
476 documentation of SAMS.

477 In regard to the validation of SAMS, the OATRC2015 expedition provides ample cases and data sets to validate
478 each module separately and collectively. For example, within this special issue, Tsarau et al. (2018) utilised the
479 OATRC2015 data to validate the developed propeller wash model within the hydrodynamic module, and Lu et al.
480 (2018a; 2018b) developed and validated analytical formulas to account for the kinking behaviour of long splitting
481 cracks, and these analytical formulae became a further enrichment to the existing fracture module. The following
482 text, on the other hand, focus on the overall validation of SAMS using OATRC2015 full-scale data.

483 We present a case during Oden's transit in the Marginal Ice Zone (MIZ). On September 30th, 2015, after completing
484 all the research activities, the fleet began the returning voyage. Oden began her return journey at 06:00:00.
485 Approximately 6 hours before that, the helicopter on-board of Oden was on a mission to map the ice conditions in
486 the MIZ ahead of Oden. The helicopter's flying route above ground is depicted in Fig. 14, together with sample
487 images taken by the helicopter camera system illustrating the corresponding ice conditions. The purpose of the
488 flight was to characterise the ice across the ice edge and partly along it. The flight headed south towards the ice
489 edge, then turned west at the edge before returning up north to Oden.



490

491

Fig. 14. Helicopter's flying route (starting from red and gradually changing into green) with sampled images of the ice conditions.

492

493

Oden was drifting at 0.5 m/s in the southwest direction from 00:00:05 September 30th until she began the transit

494

on 06:00:00 September 30th. The track of Oden and the helicopter route above ground are illustrated in Fig. 15. In

495

addition, if the sea-ice follows a similar drift path as Oden, we can also plot the estimated 'helicopter's flying route'

496

above the ice after considering the ice drift correction. We can see that for the time window from 06:49:00 till

497

07:05:00, there is a good overlap between Oden's track and the filmed ice condition along the helicopter route.

498

Ideally, it is possible to utilise all the collected images (e.g., from Images #179 to #253 in Fig. 14) along the route

499

to build a large mosaic image characterising the detailed ice conditions Oden has transited through. Such

500

information can be utilised to initialise the ice condition in SAMS, and we can explicitly simulate the transiting

501

process of Oden within the given ice field. The simulation output would be a time history of the resistance

502

encountered by Oden. These simulated results can, in turn, be compared with the ice resistance calculated based

503

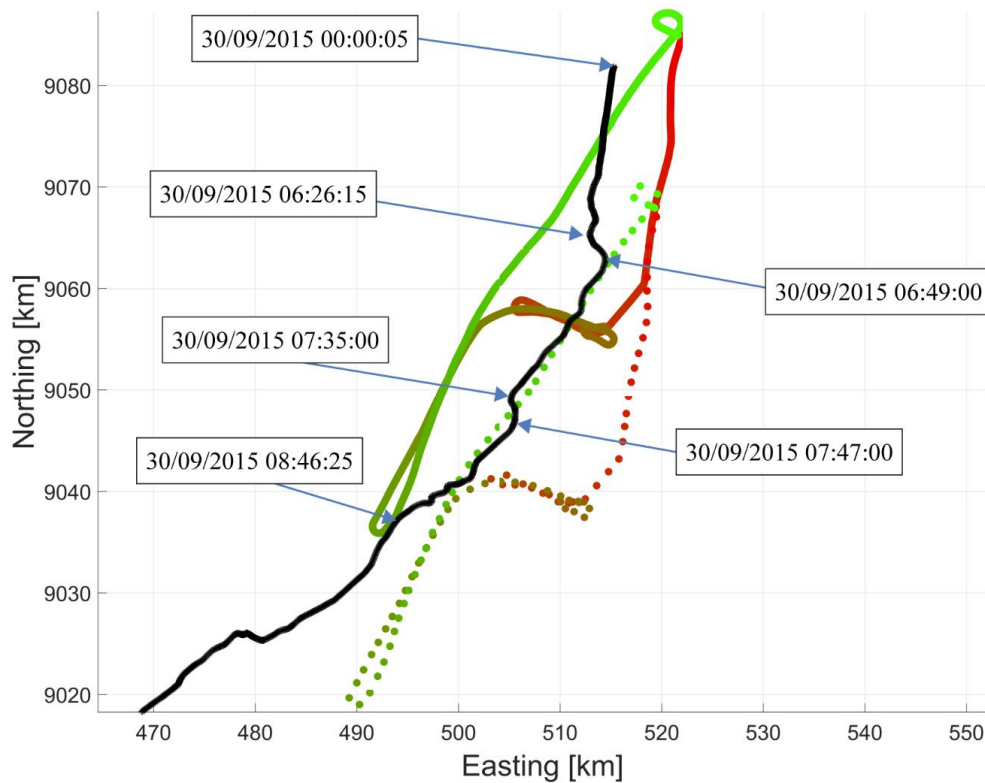
on the on-board IMUs' measurements (Kjerstad and Skjetne, 2016; Kjerstad and Lu, 2018). This gives us an

504

opportunity to utilise the OATRC2015's data to validate the capabilities of SAMS to model Oden's transit in the

505

MIZ.



506

507 Fig. 15. Oden's transit track (in dash line from north to south); the in-advance helicopter's flying route (solid line in colour, from red to green);
 508 and the estimated flying route after ice drifting correction (dotted line in colour, from red to green).

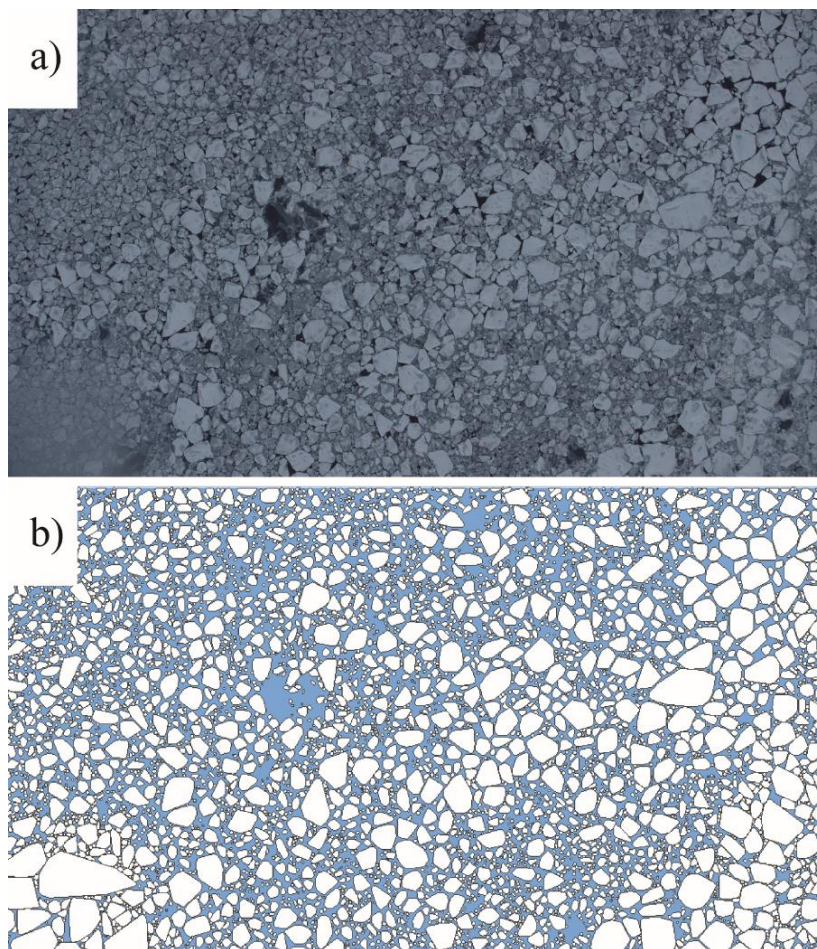
509

510 4.3 A Validation Sample

511 In this paper, instead of attempting a full validation scenario along the entire transit route, we selected one
 512 representative image (i.e., #179) from which ice conditions (i.e., ice concentration, floe size distribution, and floe
 513 geometries) are extracted based on image processing techniques (Zhang and Skjetne, 2015). The digitalised ice
 514 field, after resolving the overlap between the digitised floes, is imported into SAMS for further simulation. Fig.
 515 16 illustrates the original ice field Image #179, and its final digitalisation composed of discrete ice floes.

516 The geometrical model for a floater in SAMS is stored in the Wavefront OBJ format (.obj file), which can be
 517 generated by using 3D graphics software, and may comprise multiple triangle meshes. Each of the meshes is
 518 assumed to represent a convex hull. For the simulations presented in this paper, Oden's geometry was accurately
 519 digitalised using readily available software packages, such as *Blender* and *FreeCAD*. The input model of Oden
 520 contained 35 convex bodies, which in total contained 2240 vertices, 6510 edges and 4338 faces. The large number
 521 of mesh elements allow a very detailed approximation of Oden's hull, as seen in Fig. 17.

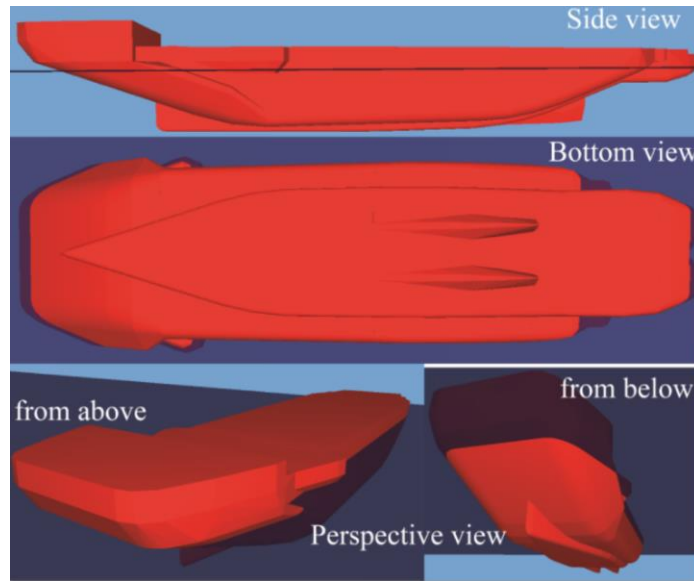
522 Furthermore, the input mechanical parameters of sea-ice in all the simulations presented in this paper are
523 summarised in Table 2. Most of the values are chosen with reference to Timco and Weeks (2010), with a preference
524 for engineering applications. For the fracture toughness of sea ice, the chosen value is based on the work of
525 Dempsey et al. (1999). Note that the form drag coefficient is set to zero. As the thickness of the ice floes compared
526 to their typical sizes is small, and no significant broken-ice accumulation was observed for the entire run, the form
527 drag coefficient is set to zero, i.e., only the frictional component of the drag is simulated.



528

529

Fig. 16. a) Initial helicopter camera image; and b) Digitalised ice field for simulation input.



530

531

532

Fig. 17. Geometric representation of Oden.

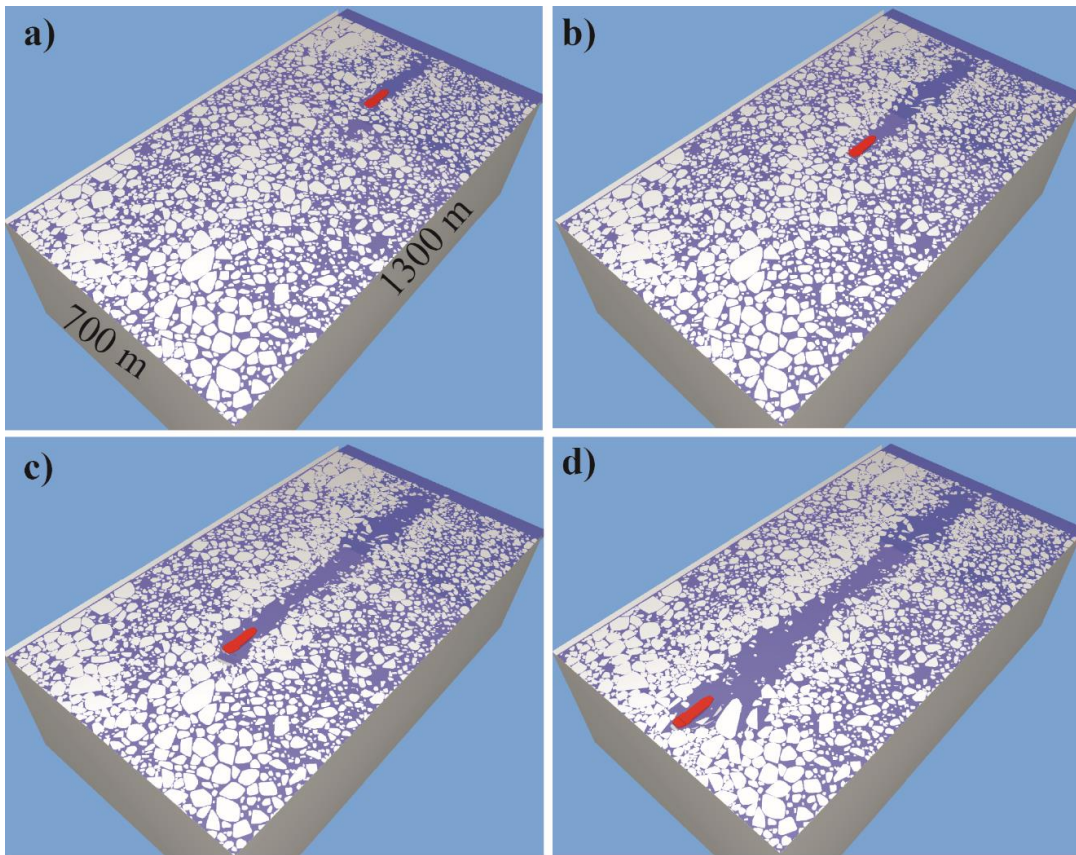
533 Table 2. Inputs for the simulations.

$\Delta t = 0.1s$	Simulation time step;
$\rho_i = 900 \text{ kg/m}^3$	Ice density;
$\rho_w = 1025 \text{ kg/m}^3$	Water density;
$C_f = 0.005 [-]$	Skin friction coefficient;
$C_d = 0.000 [-]$	Form drag coefficient;
$h = 1\text{m}$	Ice thickness;
$E = 5 \text{ GPa}$	Young's modulus;
$\nu = 0.3 [-]$	Poisson ratio;
$K_{IC} = 150 \text{ kPa}\sqrt{\text{m}}$	Fracture toughness;
$\sigma_c = 2 \text{ MPa}$	Compressive strength;
$\sigma_f = 500 \text{ kPa}$	Flexural strength;
$\mu_{ii} = \mu_{is} = \mu_{iw} = 0.1 [-]$	Ice-ice, ice-structure, and ice-boundary friction coefficient.

534

535 **4.3.1 Simulation of the Oden transit in the MIZ by SAMS**

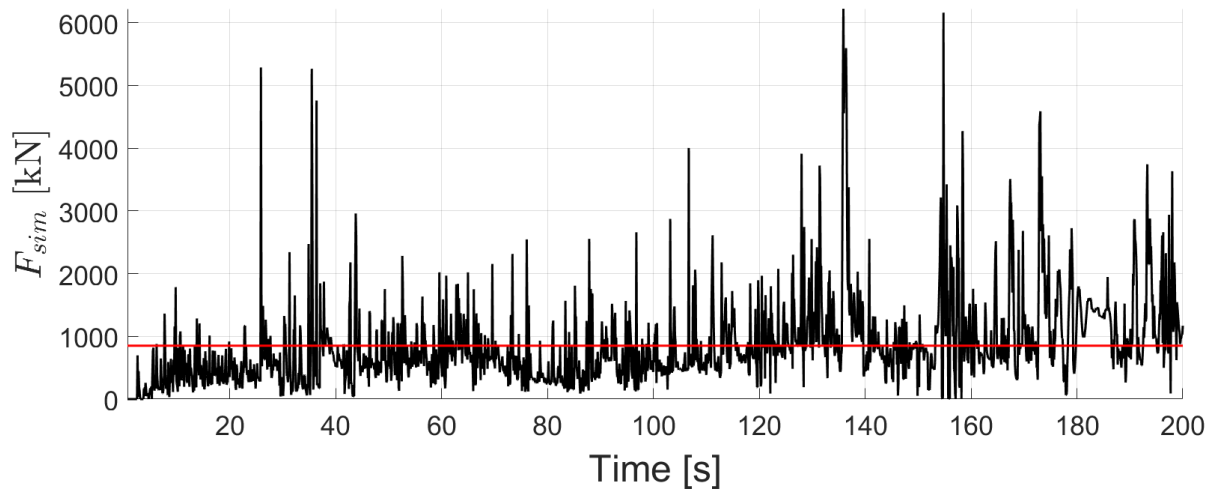
536 At first, we use the representative ice field in Fig. 16 for Oden’s transit simulation. A visual illustration of the
537 simulated transit is illustrated in Fig. 18. Given the almost linear motion of Oden illustrated in Fig. 15, the
538 simulation was performed with only one degree of freedom (1 DoF), i.e., with a constant speed of 6 m/s in the
539 surge direction. The simulated ice load history in the surge direction F_{sim} together with its averaged ice resistance,
540 $\bar{F}_{sim} = 851\text{kN}$, are shown in Fig. 19. These simulated results shall be compared with ice load estimated from the
541 field measurements.



542

543

Fig. 18. Visualisation of the simulated ship transit directly in the ice field captured in Fig. 16.



544

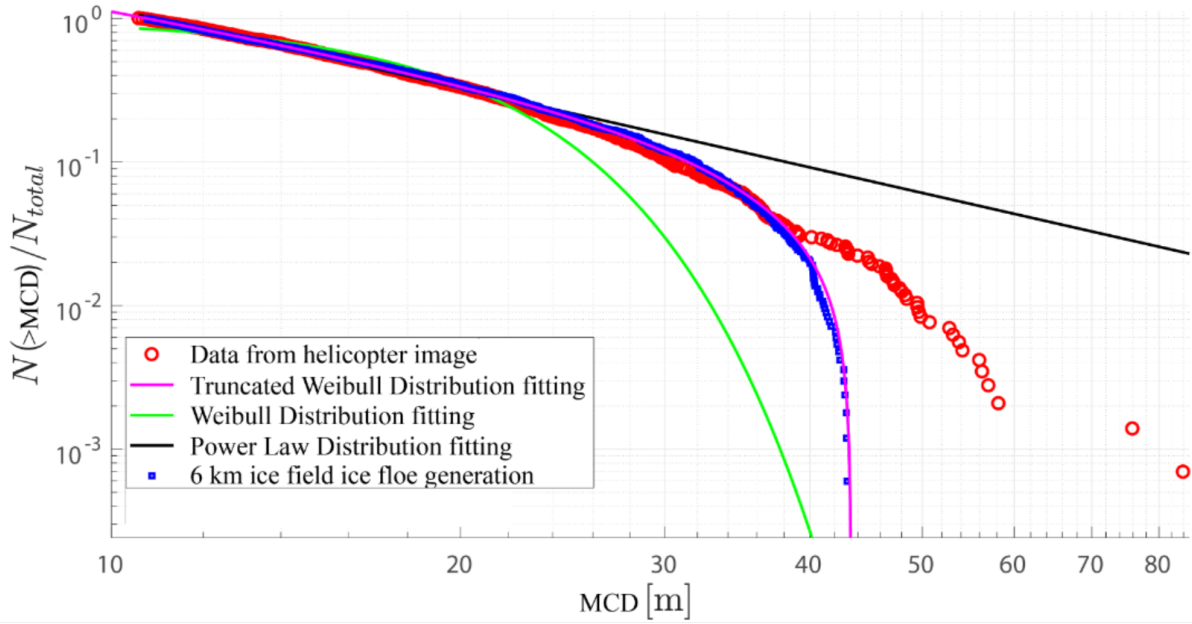
545 Fig. 19. Simulated ice load history (in black) in the surge direction (unfiltered) and its averaged ice resistance (in red solid line).

546 **4.3.2 Extended simulation of the Oden transit in the MIZ by SAMS**

547 We see from the simulation in Fig. 18 that the majority of ice floes in the width direction are not mobilised during
 548 the simulation. Moreover, the simulated transit distance is relatively short to demonstrate SAMS' capacity to
 549 efficiently perform large scale simulations. Therefore, in this section, we extend the ice field based on ice
 550 information extracted from Fig. 16. Given the identified ice floe geometry, we can characterise each ice floe's size
 551 with the Mean Clipper Diameter (MCD), as shown in Eq. (8).

552
$$\text{MCD} = 2\left(\frac{\text{Floe Area}}{\pi}\right)^{1/2} \quad (8)$$

553 The floe size distribution for the ice field shown in Fig. 16 is fitted by three proposed distribution functions (Lu et
 554 al., 2008) and is presented in Fig. 20. Among these three distributions, we see that the truncated Weibull
 555 distribution gives the best fitting to the helicopter image data. The truncated Weibull distribution's formulation
 556 together with the fitted parameters are presented in Eq. (9).



557

558 Fig. 20. Fitting floe size data from Fig. 16 with three different distribution functions and generating ice floes filling a 6 km long ice field.

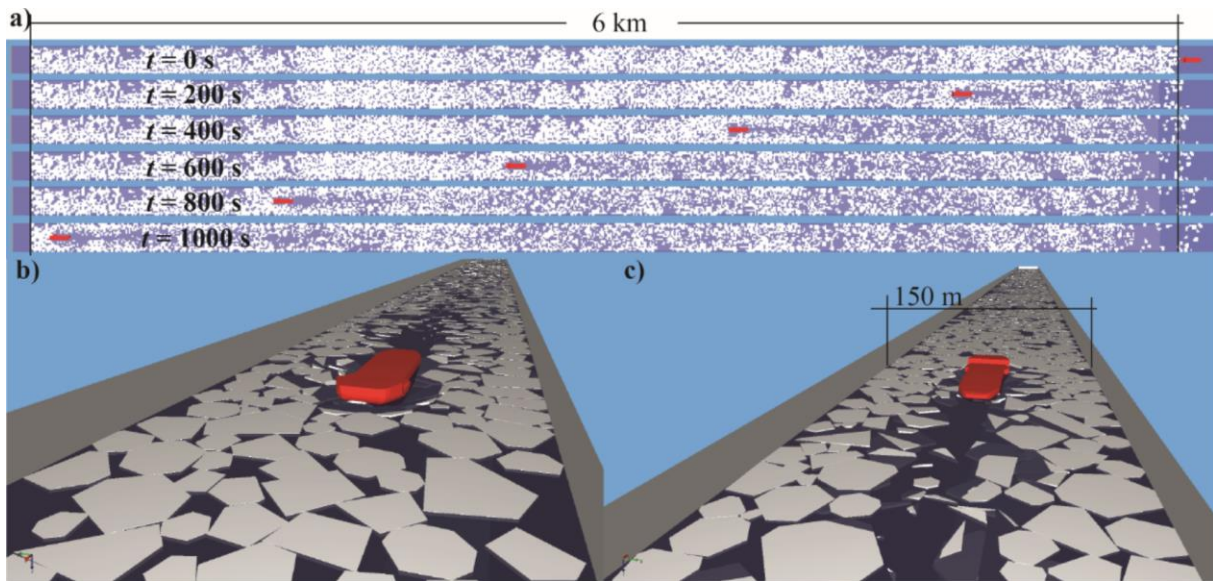
559

560

$$\frac{N(> \text{MCD})}{N_{total}} = C_0(\text{MCD}^{-D} - L_r^{-D}) = 27.25(\text{MCD}^{-1.32} - 43.41^{-1.32}) \quad (9)$$

561 where N_{total} is the total number of the generated ice floes.

562 Using the truncated Weibull distribution above, we generated an ice field that is 150 m wide and 6 km long. The
 563 150-m width leaves a space which is about twice the ship's beam width. Based on previous simulation experiences,
 564 and the transit simulation results shown in Fig. 18, this leaves a reasonable margin between the structure and the
 565 wall, with negligible boundary effects. The visual illustration of the extended simulation is presented in Fig. 21
 566 with: a) an overview at different simulation times; b) and c) nearby interaction zones near the ship bow and the
 567 wake region.



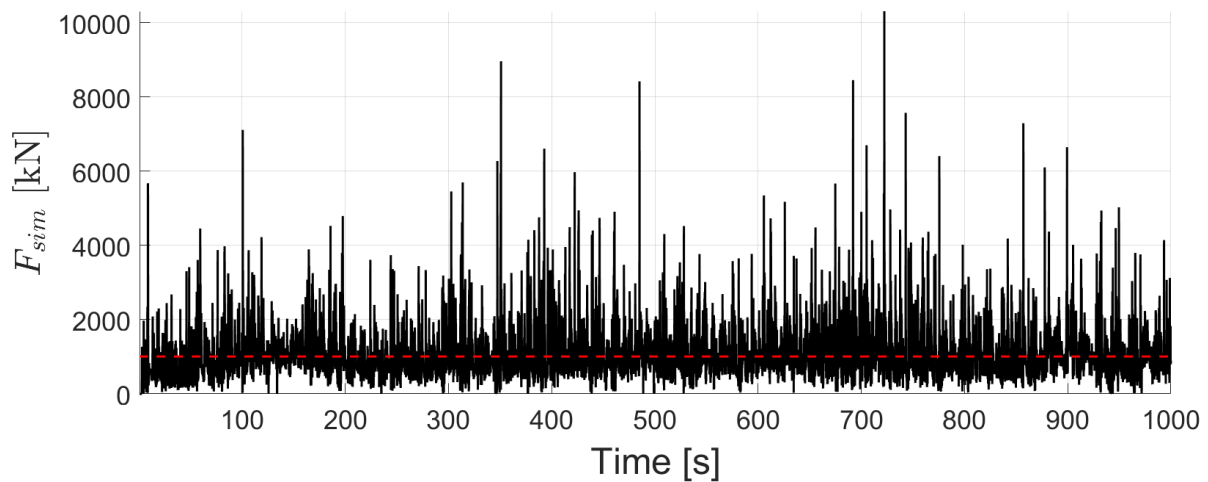
568

569

Fig. 21. Visualisation of the simulated ship transit in a 6-km ice field extended from Fig. 16.

570 Similarly, the simulated ice load time history F_{sim} and its averaged ice resistance $\bar{F}_{sim} = 1006 \text{ kN}$ are illustrated

571 in Fig. 22. These simulated results shall be compared with the ice load estimated through the field measurements.



572

573 Fig. 22. Simulated ice load history (black) from an extended ice field in the surge direction (unfiltered) and its averaged ice resistance (red
574 dashed line).

575

576 4.3.3 Full-scale ice load identification/calculation

577 To verify the simulation results in the previous sections, it is necessary for us to obtain the ice load history

578 encountered by Oden during the transit. However, direct measurement of global ice load acting on an icebreaker

579 is rather challenging, if it is at all possible. Instead, we shall utilise several indirect measurements to back-calculate

580 the global ice load history. These measurements include: 1) four Inertia Motion Units (IMUs) to obtain the ship's

581 acceleration history \dot{v} ; 2) the ship's propulsion data; and 3) ship data (including the ship's position and heading,
 582 wind direction and speed, and geometry of the ship). The identification model follows the formulations by Fossen
 583 (2011) and is written in Eq. (10).

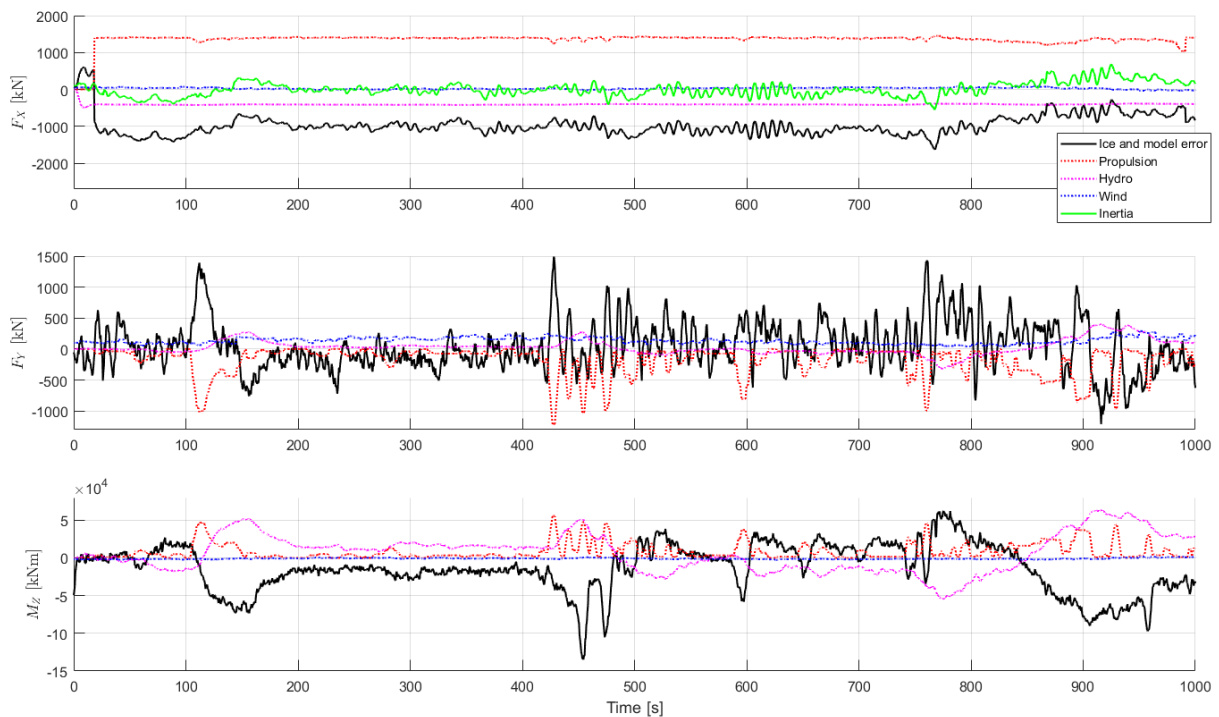
$$584 \quad M\dot{v} = \tau_a + \tau_h + \tau_w + \tau_i \quad (10)$$

585 in which,

M is Oden's mass matrix in the surge heave and yaw directions; and it is estimated in accordance with
 Table 1, i.e., $M = \text{diag}[m, m, 0.7m / 12 \cdot (L_{ship}^2 + B_{ship}^2)] = 10^6 \text{diag}[13 \text{kg}, 13 \text{kg}, 9286.4 \text{kg} \cdot \text{m}^2]$;

\dot{v} is Oden's accelerations in the surge heave and yaw directions measured by the IMUs.

586 τ_a , τ_h , τ_w , and τ_i are ship propulsion, hydrodynamic resistance, wind resistance and global ice load respectively.
 587 Their detailed formulation and calculations are presented in the companion paper (Kjerstad and Lu, 2018). In this
 588 paper, the results of the ice load identifications/calculations are presented in Fig. 23. Note the positive ice load at
 589 the start of the time series in the surge direction. This is due to the sensitivity of the identification model to the
 590 initial conditions.



591

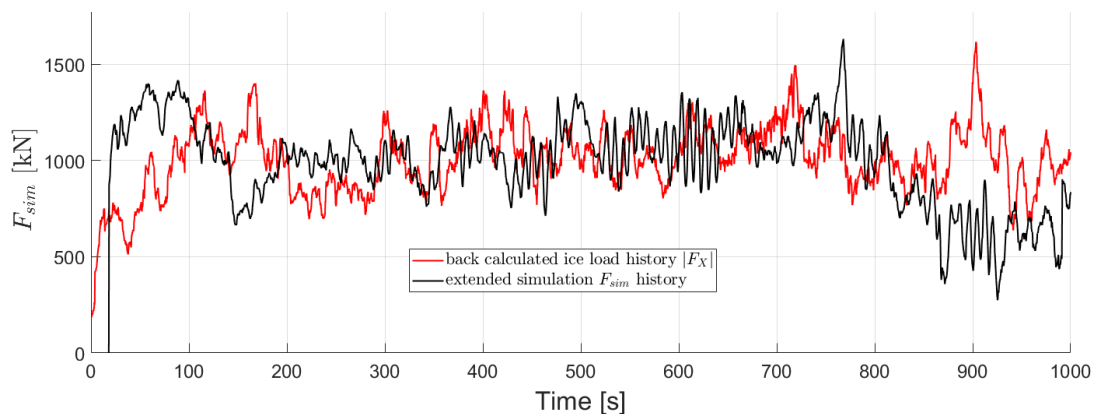
592

Fig. 23. Different load components' history during Oden's transit within the selected time window.

593

594 **4.3.4 Comparison between simulation results and measurement-based calculations**

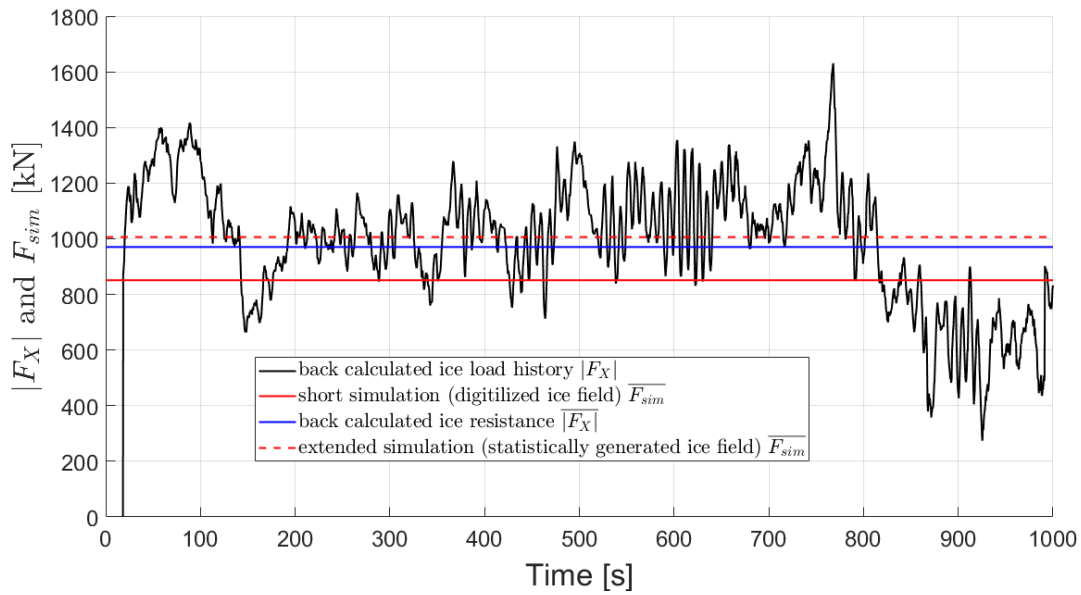
595 Fig. 24 compares the simulation results with the ice loads back-calculated from the full-scale measurements. The
596 raw simulation results are shown in Fig. 22, while those in Fig. 24 are smoothed using a moving average over a
597 window of 10 s.



598

599 Fig. 24. Time history comparison between back calculated ice load and by extended simulation.

600 Even when the ice field for the short simulation (200 s) is digitised directly from the available image, it is highly
601 unlikely that Oden transited through the exact same ice field (i.e., the initial conditions change due to wind and
602 currents). For the extended simulation (1000 s), the ice field is generated based on a statistical distribution. All this
603 suggests that we can compare the simulation results and the measurements only in a statistical sense. The statistical
604 parameters, e.g., the mean, of both the simulations and the measurements are shown in Fig. 25. The comparison
605 shows a favourable agreement between the simulation results and the full-scale data and, especially, as is to be
606 expected, for the extended simulations.



607

608

Fig. 25. Comparison between simulation and back calculations based on measurements.

609

4.3.5 Discussion of the validation sample

610

Fig. 25 presents a comparison between the simulation results and the ice loads back-calculated from the full-scale measurements. Even though several simplifications were made in the simulation set-up, the averaged ice resistance from the simulations appears to be rather consistent. As will be discussed in detail in the following text, these simplifications are reasonable given the current ship transit scenario. In this validation task, we utilised a representative ice field and conducted a direct simulation. Furthermore, we generated an extended ice field from this representative ice field, and an extended simulation was conducted. Although the ice field is not exactly the ice field Oden has transited through, from a statistical sense, the averaged ice resistance from both the simulation and measurement are not expected to differ greatly. This is presented in Fig. 25, signifying the high fidelity of the simulations that were conducted.

619

In addition, Fig. 24 takes a further step, and compares the ice load histories from the simulations and the measurements. The simulated time history was smoothed by a moving average with a 10-s time window before it was overlaid upon the measurement-based time history. The chosen 10-s time window is in accordance with the criteria adopted when processing the full-scale measurements to back calculate the ice load, i.e., down sampling all the measured data and filtering the high frequency part of the measurement (Kjerstad and Lu. 2018). After some trial and errors, the 10-s time window gives a visually comparable variation frequency against the measurement-based ice load history. However, the magnitude of variation from the measurement-based ice load history is much smaller than the raw data that was simulated in Fig. 22. For one reason, this is because of the back-calculated data is, by itself, down sampled and filtered along the processing procedures (Kjerstad and Lu, 2018). For another

627

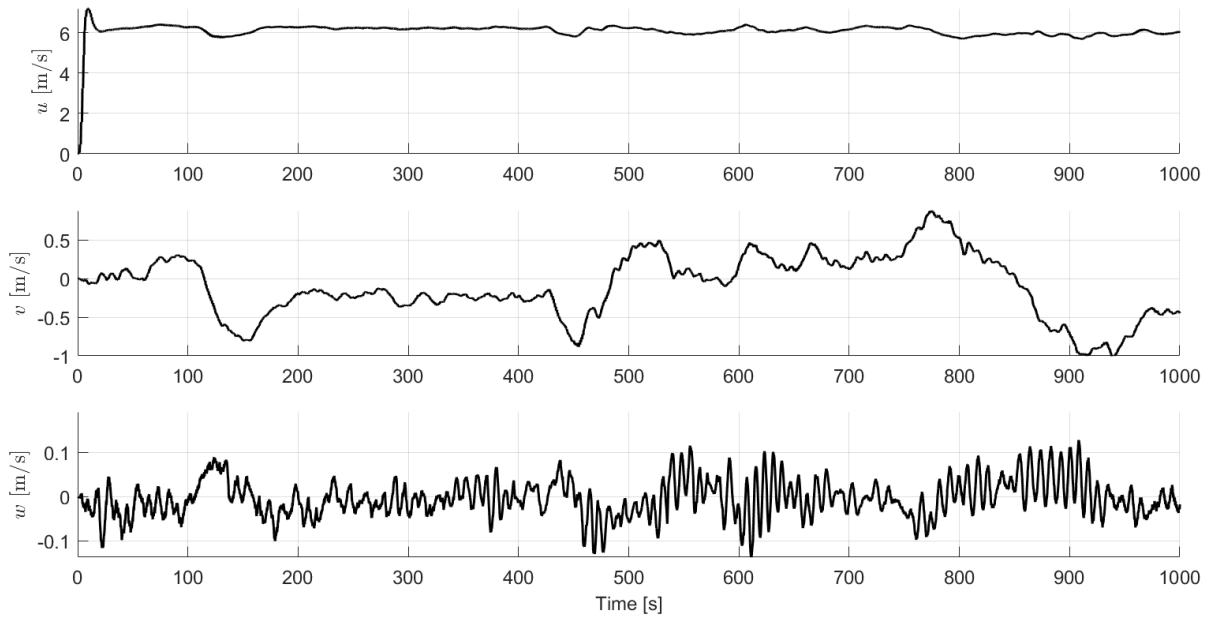
628 reason, this is attributed to our simplification of a displacement controlled simulation, i.e., Oden was travelling
629 with a constant speed of 6 m/s in the surge direction in the simulation, whereas in reality, the surge acceleration
630 varies continuously throughout the transit. Therefore, the magnitude of the simulated ice load can easily build up
631 while encountering difficult ice features, whereas in reality, the free floating structure can give away in form of,
632 e.g., deceleration, and thereby milder the ice load. An improvement to this would be to feed Oden with the
633 available propulsion during the simulation and let the behaviour of the structure (i.e., transit speed and
634 displacement) and the overall ice resistance depend entirely on the ice condition that is encountered. Thereafter, it
635 is expected that we can achieve a better comparison in the ice load history's variations in terms of both its frequency
636 and magnitude.

637 • A sample validation instead of full simulation

638 In this validation sample, the entire ship transit over 20 km from 06:49:00 to 07:35:00 was not simulated. Instead,
639 we only digitalised one ice field image covering 1.3 km by 700 m. Given the ice field images taken from the
640 helicopter illustrated in Fig. 14 together with the ship route above the ice shown in Fig. 15, we believe the selected
641 ice field is general enough to yield comparable ice resistance data. Therefore, for both the short and extended
642 simulation, all the ice information used was derived from this representative image. Generally, we can see that a
643 rather favourable comparison is achieved in Fig. 255, signifying the simulation capability of SAMS in terms of
644 ship transit in a broken ice field.

645 • 1-DoF simulation

646 For the conducted simulation, another point worth mentioning is that only a 1-DoF simulation was conducted for
647 simplicity and practical reasons. This is reasonable considering Oden's velocity in the surge, sway and heave
648 direction during the transit (see Fig. 26). A dominant velocity in the surge direction can be found in Fig. 26.
649 Comparatively, less motion is detected in the sway and heave direction. Particularly, the heave is so small such
650 that its negligence in Eq. (10) is justified.



651

652

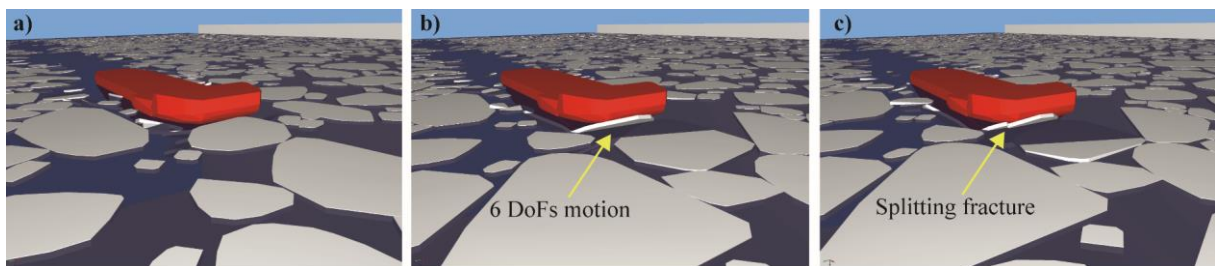
Fig. 26. The velocities in surge u , sway v and heave w during Oden's transit.

653

- Simulation features

655 Aside from the global ice resistance's simulation, it is also important to stress the detailed physical processes that
 656 SAMS has captured during the simulation. Fig. 27a and b illustrate SAMS' multi-body dynamics' capability to
 657 capture the 6 DoFs motion of an ice floe. In the consecutive image of Fig. 27c, the ice floe's splitting fracture is
 658 demonstrated. Most ice floes that interacted with Oden within the simulated ice field (i.e., Fig. 18 and Fig. 21) are
 659 relatively small ice floes, with $MCD \leq 40$ m . According to previous studies, local bending failure is less likely to
 660 occur. This is in accordance with the current simulations.

661

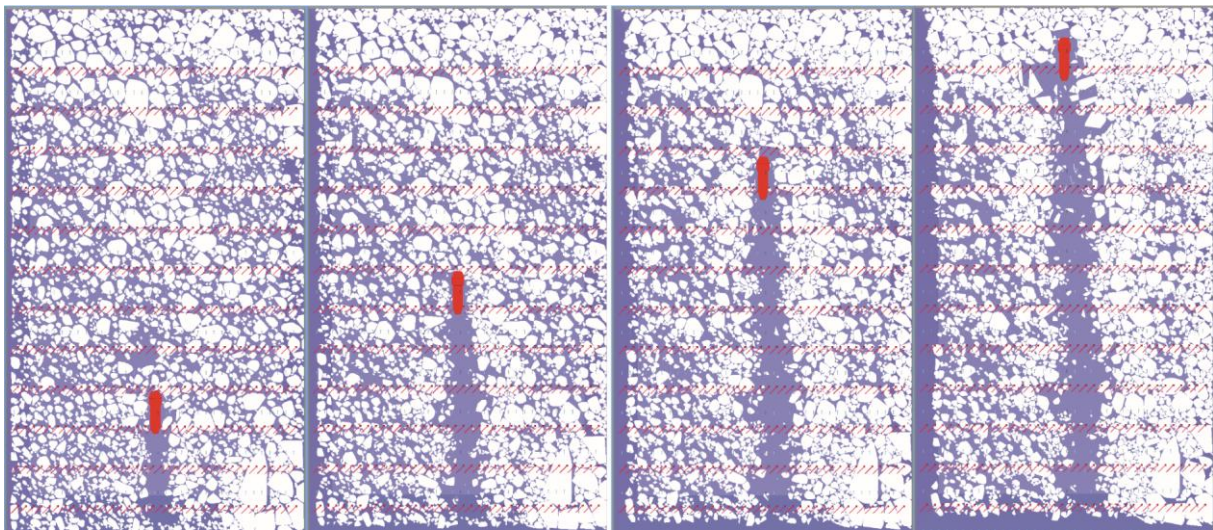


662

Fig. 27. Detailed physical processes simulated within SAMS.

663 In addition to the multi-body interactions and the ice floe's failure mode demonstrations, a different scenario with
 664 a constant 0.5 m/s current flowing with 45° to Oden's surge direction is simulated with SAMS and is illustrated in

665 Fig. 28. With the presence of current drag, ice floes within the ice field are packing to the upper right corner of the
666 simulation domain. This visually demonstrated the effectiveness of the hydrodynamic module within SAMS.



667

668 Fig. 28. Illustration of the hydrodynamic module introducing the influence of current force (0.5 m/s and with 45 deg. with reference to the
669 surge direction) in the entire simulated ice field.

670

671 5 Conclusions

672 OATRC2015 is a good example for the cooperation between academia, industry and governmental research sectors.
673 The scientific scope of OATRC2015 included three major fields of studies, namely: 1) collection of full-scale data
674 necessary to build, calibrate and validate numerical models for floaters in ice, 2) collection of full-scale data
675 necessary to build, calibrate and validate numerical models for Ice Management operations, and 3) collection of
676 data for health, safety and environmental research. Safety and the environment were considered seriously in the
677 different phases of the project, and OATRC2015 ended without a single accident. In summary, OATRC2015
678 succeeded in the overall cruise objective “to perform a safe cruise collecting valuable and important scientific data
679 and to perform full-scale field trials for testing of key technologies.” During the 14-day field programme, many
680 research activities were carried out and the research cruise produced a considerable amount of valuable data in the
681 following areas:

- 682 • Monitoring of ice conditions using different camera systems
- 683 • Characterisation of ice using helicopter and vessel observations
- 684 • Monitoring of ice with satellite data

- 685 • Collection of marine radar data
- 686 • Collection of ice drift data using beacons
- 687 • Study of ice management tactics using the Oden and Frej
- 688 • Collection of local ice loads data on the Frej
- 689 • Collection of ship motion measurements using Inertial Measurement Units (IMU)
- 690 • Collection of vessel performance data
- 691 • Measurement of ice thickness with EM and shipborne radar
- 692 • Study of brash ice
- 693 • Testing of high-speed Arctic communications
- 694 • Investigations of vibrations on the icebreaker crew
- 695 • Water sampling and biodiversity
- 696 • Collection of marine mammal observations

697
698 The data and results from the programme will continue to be used to promote safe and sustainable maritime
699 operations in the Arctic. In the second part of this paper, we used Oden's transit data (from 06:49:00 to 07:05:00
700 on September 30th) to validate the simulator for Arctic Marine Structures (SAMS). In the validation task, one
701 representative ice field image taken by the helicopter along Oden's transit route was chosen to digitalise the ice
702 field to extract information, such as ice floe size, geometry and locations. Given such real field ice information,
703 we reconstructed this ice field (1.6 km by 0.7 km) within SAMS, and directly simulated Oden's transit within it.
704 Furthermore, we further extended this ice field into a much longer ice field (i.e., 6 km by 150 m) by generating ice
705 floes, whose sizes follow a truncated Weibull distribution. Thereafter, a much longer simulation (1000 s) is
706 simulated within this extended ice field.

- 707 • Statistically, SAMS yields rather satisfactory ice resistance values for both the short and extended
708 simulations, which have -13.1% and 2.7% errors compared to the value calculated based on measurements;
- 709 • Through the validation process, different modulus within SAMS are collectively verified. Individually,
710 the functionalities of different modulus are visually demonstrated. This includes: the multi-body
711 dynamics accounting for each individual ice floe's motion and their interactions with themselves and the
712 structure; the multi-failure modes of each ice floe according to previous theoretical development; and the
713 hydrodynamic module's capability to consider the effect from the ambient fluid (both air and water).

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716 Research Company and was performed by the Norwegian University of Science and Technology (NTNU) in
717 cooperation with the Swedish Polar Research Secretariat (SPRS) and the Swedish Maritime Administration (SMA).
718 OATRC2015 was successful due to the contributions from many individuals from the organisations listed in Table
719 3. Special thanks are given to the crews of the icebreakers, Oden and Frej.

720
721 Table 3. Alphabetical listing of participating organisations

Avron Ritch Consulting Ltd.	ExxonMobil Upstream Research Company	Red Rental
Canatec Associates International Ltd.	Kallax Flyg	Swedish Maritime Administration
C-Core	Lulea University of Technology	Swedish Polar Research Secretariat
Chalmers University of Technology	Nordic Unmanned	Trumbull Unmanned
Dansk Bioconsult - Marine Observers	Norwegian University of Science and Technology	University Centre in Svalbard
European Helicopter CenterCentre	Oceaneering	University of Gothenburg

722
723 We acknowledge the use of Rapid Response imagery from the Land, Atmosphere Near real-time Capability for
724 EOS (LANCE) system, operated by the NASA/GSFC/Earth Science Data and Information System (ESDIS) with
725 funding provided by NASA/HQ.

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