

# Short-term insurance versus long-term bet-hedging strategies as adaptations to variable environments

Thomas Ray Haaland, 1,2 Donathan Wright, 1 Darle Tufto, 3 and Irja Ida Ratikainen 1 D

<sup>1</sup> Department of Biology, Centre for Biodiversity Dynamics, Norwegian University of Science and Technology, Trondheim, Norway

<sup>2</sup>E-mail: thomas.r.haaland@ntnu.no

<sup>3</sup>Department of Mathematical Sciences, Centre for Biodiversity Dynamics, Norwegian University of Science and Technology, Trondheim, Norway

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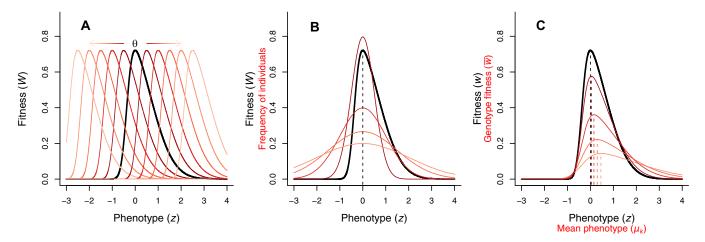
Understanding how organisms adapt to environmental variation is a key challenge of biology. Central to this are bet-hedging strategies that maximize geometric mean fitness across generations, either by being conservative or diversifying phenotypes. Theoretical models have identified environmental variation across generations with multiplicative fitness effects as driving the evolution of bet-hedging. However, behavioral ecology has revealed adaptive responses to additive fitness effects of environmental variation within lifetimes, either through insurance or risk-sensitive strategies. Here, we explore whether the effects of adaptive insurance interact with the evolution of bet-hedging by varying the position and skew of both arithmetic and geometric mean fitness functions. We find that insurance causes the optimal phenotype to shift from the peak to down the less steeply decreasing side of the fitness function, and that conservative bet-hedging produces an additional shift on top of this, which decreases as adaptive phenotypic variation from diversifying bet-hedging increases. When diversifying bet-hedging is not an option, environmental canalization to reduce phenotypic variation is almost always favored, except where the tails of the fitness function are steeply convex and produce a novel risk-sensitive increase in phenotypic variance akin to diversifying bet-hedging. Importantly, using skewed fitness functions, we provide the first model that explicitly addresses how conservative and diversifying bet-hedging strategies might coexist.

**KEY WORDS:** Cliff-edge effect, environmental canalization, environmental stochasticity, fluctuating selection, geometric mean fitness, variance-sensitivity.

How organisms adapt to unpredictable fluctuations in the environment has been an intriguing and important problem for many years in evolutionary biology, and especially recently when predicting adaptive responses to environmental change. Conditions may vary over different time scales, selecting for adaptations that maximize fitness in the face of environmental stochasticity in everything from labile behavioral traits within a lifetime (e.g., variance-sensitive foraging, Stephens 1981) to cross-generational effects of life-history traits (e.g., bet-hedging; Simons 2011; Starrfelt and Kokko 2012). Thus, the phenotypes we observe in organisms today have likely been shaped by

environmental variation experienced across longer timescales during their evolutionary history, and trait values may not necessarily appear optimal when considering just short-term current environmental conditions (Nadeau et al. 2017). Environmental variation itself is expected to be a strong selective agent, since genotypic rather than individual fitness determines optimal strategies that are produced over evolutionary time in stochastic environments (Lewontin and Cohen 1969; McNamara 1998).

Asymmetric fitness functions pose an additional challenge to evolutionary biologists seeking to understand genotypic adaptations in variable environments (Yoshimura and Shields 1987;



**Figure 1.** Asymmetric fitness functions and uncertainty in fitness returns produces insurance. Both (A), environmental variation  $\theta$  (arrows) moving the fitness function around (darker to lighter colors indicate increasing fluctuations in location parameter  $\theta$ ), and/or (B) phenotypic variation among individuals of a genotype (darker to lighter colored lines represent normal distributions of individuals with increasing standard deviations), can cause variation in the fitness returns. Insurance therefore takes the form of an adjustment of the mean phenotypic value  $\mu_k$  away from the peak of the deterministic fitness function (0, indicated by black dotted line) toward the less steeply decreasing side, to avoid accidentally falling off the cliff-edge (C). Colored lines in C depict arithmetic mean fitness of a genotype experiencing environmental or phenotypic variation with standard deviation corresponding to the colored curves in A and B (from darker to lighter, 0.5, 1, 1.5, and 2). Dotted lines indicate the peak of these curves, which moves farther away from 0 the more variation there is. See Methods text for more details.

Urban et al. 2013). Skew in the function relating a single, continuous phenotypic trait to fitness is commonly seen in nature, occurring whenever costs and benefits differ in how they relate to increasing versus decreasing values of the phenotype, or when the strength of selection acting on the two sides of the phenotypic distribution differs. Common examples are thermal performance curves (Angilletta 2009), optimal clutch or litter sizes (Mountford 1968; Boyce and Perrins 1987; Gamelon et al. 2018), and reproductive benefits versus viability costs of sexually selected ornaments (Andersson and Iwasa 1996). In these types of scenarios, uncertainty across instances in any component determining individual fitness will cause the optimal trait value to differ from the trait value at the peak of the fitness function (Yoshimura and Shields 1987; Parker and Smith 1990). Such uncertainty in fitness pay-offs across instances is also almost ubiquitous in biological systems. Across lifetimes, phenotypic differences among individuals (as instances) of the same genotype may arise due to developmental instability creating random (uncanalized) variation in phenotypes and thus also in their fitness, and strong environmental canalization to avoid such variation may itself incur costs (DeWitt et al. 1998; Zhang and Hill 2005). Within lifetimes, uncertainty may occur in individual energetic state on short (e.g., behavioral) timescales, due to stochastic variation in resource acquisition, such as prey captures. In addition, the fitness effects of the phenotype itself (i.e., the shape or position of the fitness function) may be uncertain, for example due to micro-environmental

variability, or variation occurring over short-time scales, such as in social environments.

With a skewed fitness function, any stochastic environmentally induced variation in fitness pay-offs will select for apparently suboptimal phenotypes with trait values away from the peak of the deterministic fitness function when selection maximizes arithmetic mean fitness (Fig. 1). Finding the (arithmetic) mean fitness in such cases involves multiplying the phenotype-specific fitnesses with the frequencies of the different phenotypes (Mountford 1968). This phenomenon is sometimes described as the cliffedge effect (Vercken et al. 2012; Mitteroecker et al. 2016), and is commonly encountered as "insurance" strategies in fields such as behavioral ecology (Dall 2010). A well-known example is the small bird in winter (Brodin 2007). Facing a starvation-predation trade-off, the small passerine bird benefits from being as light as possible to nimbly avoid predators during the day, but needs to store fat before nightfall, which it metabolizes to stay warm during the night. Small birds in winter will therefore adaptively store more fat as insurance when temperatures are more variable (Bednekoff et al. 1994), and/or when food supply is more uncertain (Krams et al. 2010; Ratikainen and Wright 2013). This same logic of insurance maximizing arithmetic mean fitness over repeated trials for a single individual, also applies among individuals sharing a genotype. If members of the same genotype differ in their expected fitness payoffs due to different individuals inhabiting different microenvironments (Fig. 1A), and/or due to developmental instability creating individual environmentally induced phenotypic variation (Fig. 1B), maximizing genotype fitness requires insurance in the mean phenotype of its bearers (Fig. 1C).

Across generations, however, the fitness of a lineage is determined by its geometric mean fitness rather than the arithmetic mean, due to reproduction being an inherently multiplicative process (Lewontin and Cohen 1969; Simons 2002). When environmental conditions are constant between generations (i.e., the function relating the trait in question to fitness is exactly the same each generation), arithmetic and geometric mean fitness are equal. However, once some aspect of the fitness function differs between generations, creating variation in realized fitness between individuals of the same genotype, then the geometric mean will be lower than arithmetic mean. Crucially, a change in strategy that lowers variance in realized fitness at the genotype level may increase geometric mean fitness, and thus be selectively favored. If such a strategy that increases geometric mean fitness at the genotype level also involves a simultaneous decrease in arithmetic mean fitness, it is defined as bet-hedging (Philippi and Seger 1989). Two main types of bet-hedging are usually considered, diversifying bet-hedging (DBH) and conservative bethedging (CBH) (Philippi and Seger 1989; Simons 2011; Starrfelt and Kokko 2012). DBH increases phenotypic variance and thus reduces the correlations in fitness between individuals of the same genotype, such that not all individuals are affected by the environment in the same correlated way. DBH strategies can include both producing two discrete "types" of individuals, such as dry and wet-year specialists, or dormant and active life stages in response to good and bad years (Lewontin and Cohen 1969; Venable 2007; Graham et al. 2014), and continuous variation in a trait among individuals, such as size of offspring, or timing of reproduction and entering or exiting dormancy (Simons 2009; Devaux and Lande 2010; Lof et al. 2012). In contrast, CBH reduces variance in realized fitness at the individual level, such that each individual within a genotype will perform moderately well across a range of environments. However, there is nothing stopping a strategy from combining the two types, and Starrfelt and Kokko (2012) argue that DBH, reducing only among-individual fitness variance, and CBH, reducing only each individual's fitness variance, are actually two ends of a continuum with strategic combination of DBH and CBH possible in between. Despite this, neither Starrfelt and Kokko (2012) nor later authors exploring similar models (e.g., Crowley et al. 2016) explain how such a combination of DBH and CBH would work. These papers examine models with two discrete environments, and a suggested conservative bet-hedger (acting as a generalist coping moderately well with both environments) is never able to outperform a diversified bet-hedger (producing specialists to each environment in the proportions that they occur).

We present a different interpretation of CBH, which potentially allows for both CBH and DBH to coexist within the same model. Considering a continuous trait with an asymmetric fitness function that fluctuates between generations, CBH can be envisioned as having a cliff-edge effect in the same way as insurance (see above). Organisms would thus be "playing it safe" by shifting the mean trait value away from the fitness function maximum, toward the less steeply decreasing side (analogous to that in Fig. 1). In such a scenario, we expect insurance to maximize arithmetic mean fitness within each generation. An additional shift in the optimal trait value even further away from the cliff edge might then be selected for if it lowers fitness variance between generations (despite lowering arithmetic mean fitness in a single generation). Such an effect would essentially constitute a CBH strategy. Phenological features such as breeding date, migration date or egg laying date for temperate birds are examples of traits with such asymmetric fitness functions. The strength of selection may differ for the underlying selection pressures, for example if being too late leads to lower offspring competitive ability, but being too early leads to a much more severe mismatch with the food peak resulting in complete reproductive failure (Gienapp 2012). Whether breeding after the peak in the fitness function represents insurance or CBH depends upon whether the mismatch between the mean trait value and the peak of the asymmetric fitness function is the result of individuals maximizing arithmetic mean fitness within their lifetime versus lineages being favored that maximize geometric mean fitness over long time periods (see Lof et al. 2012). Despite having much in common and some confusion between the terms in the literature, CBH has rarely been placed in the same theoretical framework as insurance, and insurance has been all but absent as part of the bet-hedging literature.

Here, we investigate the relative importance of insurance and CBH in coping with stochastically fluctuating environments within and between generations when the fitness function is skewed. We use a single, continuous trait and calculate the means and variances in phenotype that maximize arithmetic or geometric mean fitness under different magnitudes of fluctuations in the optimal trait value. Mechanisms regulating the phenotypic variance expressed within a genotype, such as DBH increasing such variance or environmental canalization decreasing it, are expected to interact with insurance and/or CBH. Previous theoretical work has shown that DBH will adaptively increase variance in trait values once the variance in the phenotypic optimum exceeds the squared width of the fitness function, whereas smaller environmental variance favors the opposite mechanism, canalization of the trait toward the value that maximizes fitness in the mean environment (Bull 1987; Slatkin and Lande 1976). Intuitively, greater stochastic variation in trait values should require there to be more insurance or CBH modifying the mean trait value, but these different components have not previously been placed in a

common framework. By using a skewed fitness function to illustrate the effects of insurance versus CBH, we are able to examine these interactions, while modeling DBH alongside CBH in such a way allows us to formally explore Starrfelt and Kokko's (2012) suggestion regarding an adaptive continuum between these two potentially coexisting forms of bet-hedging.

# Model Description

### THE SKEW NORMAL FITNESS FUNCTION

A wide variety of fitness functions have been used to characterize asymmetrical relationships between phenotype and fitness (Martin and Huey 2008; Vasseur et al. 2014), and the results we demonstrate here can also arise from other functions with nonzero skew. We base our skewed fitness function on the density function of the skew normal distribution (O'Hagan and Leonard 1976), omitting the normalizing constant such that individual fitness takes a value of one for  $z = \theta$ . Fitness as a function of the phenotype z is then given by

$$w(z; \theta, \omega, \alpha) = 2e^{-\frac{(z-\theta)^2}{2\omega^2}} \Phi\left(\alpha \frac{z-\theta}{\omega}\right),$$
 (1)

which is a Gaussian function multiplied by a term involving the cumulative distribution function Φ of the standard normal distribution. The parameter  $\theta$  specifies the location,  $\omega$  the width, and  $\alpha$ the skew of the fitness function.  $\alpha > 0$  gives a right-skewed function (positive skewness),  $\alpha < 0$  a left-skewed function, and  $\alpha = 0$  a symmetric Gaussian fitness function. Importantly,  $\alpha$  also changes the position of the maximum value of w (despite location parameter  $\theta$  being kept constant), so we will write  $\theta_0$  as the value of  $\theta$  that provides maximum fitness for a trait value of zero. To examine the effects of skewed fitness functions on trait values we will use α > 0 and  $\theta = \theta_0$ , so that adaptations in terms of phenotypic values shifted away from the fitness function maximum (due to insurance or CBH) become positive and easily interpretable relative to zero (i.e., the value of z simply becomes the distance from the peak, or the "amount" of insurance or CBH). The fitness function in Fig. 1 (black) has  $\theta = \theta_0$ ,  $\omega = 1$ , and  $\alpha = 5$ .

## **GENOTYPIC FITNESS WHEN PHENOTYPES VARY** WITHIN GENOTYPE

There may be uncertainty in the fitness returns of individuals of genotype k. This can be due either to different individuals experiencing different microenvironments (Fig. 1A), or due to some (adaptive or nonadaptive) environmentally induced instability in individual development, leading to individuals expressing stochastically different phenotypes z despite having the same gene for the mean phenotype (Fig. 1B). Whichever the mechanism, we assume there is a genetic basis that can modulate this uncertainty. If the variation in fitness returns arises from

environmental variation (Fig. 1A), a gene affecting this variation at the genotype level is envisioned as controlling some trait that affects the degree of similarity between microenvironments that offspring experience. For example, dispersal can place offspring in more different microenvironments, whereas other traits such as building well-insulated nests that lower the effect of temperature variation, or habitat choice or seeking out habitats with less variable food availability, can provide offspring of the same genotype with more similar microenvironments. The variation in fitness returns due to phenotypic differences arising from intrinsic factors, such as susceptibility to developmental instability or environmental canalization (Fig. 1B), are known to have a genetic basis (e.g., Shen et al. 2012). The evolution of such genes under fluctuating selection has previously been modeled in detail (Bull 1987; Tufto 2015), and this is the mechanism modulating individual variation in fitness typically considered in the context of bet-hedging.

Whichever the mechanism, we follow Bull (1987), and assume this phenotypic variation to exhibit a normal distribution  $f_k(z)$ , with a mean  $\mu_k$  and a variance  $\sigma^2_k$ . We are interested in the joint evolution of the two underlying genotypic values  $\mu_k$  and  $\sigma_k$ , and assume no genetic linkage or pleiotropic effects between

The mean fitness of all individuals with the genotype k (with genotypic values  $\mu_k$  and  $\sigma_k^2$ ) in any given environment  $\theta$  (or a constant environment over time) then becomes:

$$\bar{w} (\mu_{k}, \sigma_{k} | \theta, \omega, \alpha) = \int_{z = -\infty}^{\infty} w(z; \theta, \omega, \alpha) f_{k}(z) dz$$

$$= \frac{2\omega}{\sqrt{\omega^{2} + \sigma^{2}_{k}}} e^{\left(-\frac{(\mu_{k} - \theta)^{2}}{2(\omega^{2} + \sigma^{2}_{k})}\right)} \Phi\left(\frac{\omega\alpha}{\sqrt{\omega^{2} + \sigma^{2}_{k}} (1 + \alpha^{2})} \frac{\mu_{k} - \theta}{\sqrt{\omega^{2} + \sigma^{2}_{k}}}\right),$$
(2)

which is akin to equation (3) in Bull (1987). The resulting function  $\bar{w}$  has the same form as (1), but with a larger width parameter and a smaller skew parameter. When  $\sigma_k^2 = 0$ , the functions are identical. Choosing a constant phenotypic variance  $\sigma^2_k > 0$ , we can use numerical optimization over  $\mu_k$  and compare the difference in maxima of w and  $\bar{w}$ , to find the amount of insurance needed to maximize arithmetic mean fitness across all individuals of the genotype (i.e., the optimal shift in the mean phenotype away from the fitness function maximum). Figure 1C shows w (in black) together with  $\bar{w}(k;\theta_0,1,5)|\sigma_k$  (in reds) for increasing values of  $\sigma_k$  (darker to lighter colors represent  $\sigma_k = \{0.5, 1, 1.5,$ 2)). In this case, since the maximum of the fitness function is at zero, the optimal amount of insurance is simply the value of the phenotype that gives the highest fitness,  $\operatorname{argmax}_{\mu}(\bar{w})$ . These approximate to 0.044, 0.153, 0.297, and 0.458, respectively. The larger the phenotypic variance  $\sigma^2_k$ , the more insurance is needed to maximize genotype fitness. We also note that genotype fitness strongly declines with increasing phenotypic variance - except when the mean phenotype is far away from the fitness function peak.

## LONG-TERM FITNESS IN A FLUCTUATING **ENVIRONMENT**

In a fluctuating environment it is not just individual fitness but the fitness of a genotype that will differ in different environments, and long-term fitness in such cases is determined by geometric mean rather than arithmetic mean fitness (Lewontin and Cohen 1969; Simons 2011). In the case of no fluctuations, the geometric mean is simply equal to the arithmetic mean, and equation (2) is valid. If we let the optimum position  $\theta$  follow a normal distribution fwith a mean of  $\theta_0$  and a variance  $\sigma_\theta$  across generations, long-term arithmetic mean fitness can be found by taking the expectation of equation (2) across the environmental fluctuations,

$$W_{arit} = \int_{0-\infty}^{\infty} \bar{w} (\mu_k, \sigma_k | \theta, \omega, \alpha) f(\theta | \theta_0, \sigma_\theta) d\theta, \qquad (3a)$$

and for geometric mean fitness we can take the exponential of log fitnesses integrated across all different environmental conditions,

$$W_{geom} = \exp \left\{ \int_{\theta = -\infty}^{\infty} \ln \left[ \bar{w} \left( \mu_k, \sigma_k | \theta, \omega, \alpha \right) \right] f \left( \theta | \theta_0, \sigma_\theta \right) d\theta \right\}.$$
 (3b)

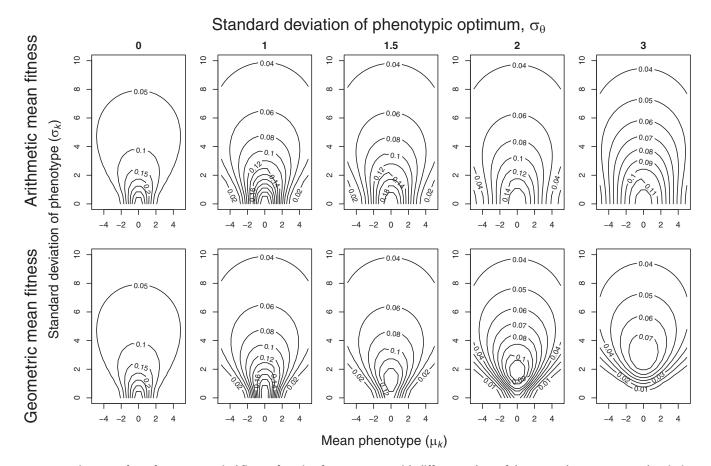
These are shown as fitness surfaces in Figs. 2 and 3. Maximizing both equations (3a) and (3b) with respect to  $\mu_k$  and  $\sigma_k$ gives the strategy that provides the highest long-term arithmetic or geometric mean fitness, respectively, for genotype k. Comparing them allows us to tease apart bet-hedging effects (those maximizing geometric mean fitness at the expense of arithmetic mean fitness) from non-bet-hedging effects (those maximizing only arithmetic mean fitness). Maximizing 3a for a fixed  $\sigma_k$  gives the optimal amount of insurance (since the peak of the individual fitness function is at zero), equal to  $\operatorname{argmax}_{\mu} [W_{arit} | \sigma_k]$ . Maximizing 3b for the same  $\sigma_k$  then reveals whether any additional shift in mean phenotype can be attributed to bet-hedging rather than just insurance, with the optimal amount of CBH then being equal to  $\operatorname{argmax}_{\mu} [W_{geom} | \sigma_k] - \operatorname{argmax}_{\mu} [W_{arit} | \sigma_k]$ . This result is plotted in Fig. 4.

Numerical integration was carried out in R version 3.3.1 (R Core Team 2016) and the code is provided in the online Supporting Information (Appendix S1).

## Results

Figures 2 and 3 show the long-term fitness of genotype k (consisting of the gene for mean phenotype,  $\mu_k$ , and for variance in the phenotype,  $\sigma^2_k$ ) measured in either arithmetic or geometric mean fitness in an environment with increasing fluctuations in the position parameter  $\theta$  of the individual fitness function (increasing  $\sigma_{\theta}$ ). In Fig. 2 the individual fitness function is symmetrical and in Fig. 3 it is skewed. With a stable environment across generations  $(\sigma_{\theta} = 0)$  the arithmetic and geometric mean fitness are equal (top and bottom panels the same). The fitness surface in these cases peaks at  $\mu_k = 0$  and  $\sigma_k^2 = 0$ , that is, the optimal genotype is a trait value phenotypically canalized (i.e., with as little variation as possible) at the peak of the individual fitness function. As environmental fluctuations increase ( $\sigma_{\theta} > 0$ ), the differences between arithmetic and geometric mean fitness increase. Notably, in Fig. 2 the peak moves upwards in the bottom panels as the environmental fluctuations increase. This adaptive increase in phenotypic variation  $(\sigma_k)$  within the genotype represents DBH, and since arithmetic mean fitness strictly declines with increasing  $\sigma_k$ (top panels), the necessary requirement that bet-hedging involves a lowering of arithmetic mean fitness is fulfilled. In accordance with Bull's (1987) result, this selection for increased phenotypic variation only appears once the environmental variance  $\sigma^2_{\theta}$  is larger than the squared width of the fitness function, and the optimal  $\sigma_k^2$  is then equal to  $\sigma_\theta^2 - \omega^2$ . For the symmetric Gaussian distribution (Fig. 2) this threshold is simply  $\omega^2 = 1$ , and DBH appears when  $\sigma^2_{\theta} > 1$ . In Fig. 3 asymmetry is introduced into the fitness function (results are shown for  $\alpha = 5$ , which matches the fitness function in Fig. 1), but all other parameters remain as in Fig. 2. The width of the fitness function decreases as the skew increases, so this scenario also produces DBH (fitness surface peak with  $\sigma_k^2 > 0$  under lower levels of environmental variance. The skew also leads to the fitness surface peaks shifting to positive values of  $\mu_k$ , away from the steeply decreasing side of the individual fitness function. This shift is seen both in the top and bottom rows of Fig. 3. The shift produced when maximizing arithmetic mean fitness represents insurance, but in each case there is a small additional shift when maximizing geometric mean fitness that can be attributed to CBH, amounting to between 27% for  $\sigma_{\theta}$ = 0.5 ( $\mu_k$  = 0.77 vs. 0.60) and 1.6% for  $\sigma_{\theta}$  = 3 ( $\mu_k$  = 0.783 vs. 0.771). The amount of CBH on top of insurance decreases as  $\sigma_{\theta}$ increases, due to the large amounts of DBH at these scenarios that lowers the skew parameter of the mean fitness function  $\bar{w}$ (eq. (2)).

The amount of CBH needed is larger when phenotypic variation  $\sigma_k$  is constrained at low values—see Figs. 4 and 5A. Figure 4 shows this difference in mean phenotype (argmax<sub>u</sub>  $[W_{geom}]$  – argmax<sub> $\mu$ </sub>  $[W_{arit}]$ ), which is attributable to CBH (y-axis), for different amounts of phenotypic variation  $\sigma_k$  (x-axis) and environmental variation  $\sigma_{\theta}$  (line color). Note that this CBH effect is largest when phenotypic variation  $\sigma_k$  is small, and environmental fluctuations  $\sigma_{\theta}$  are large enough that DBH would provide a much greater fitness gain (the steepest incline on the fitness surface comes by moving upwards along the  $\sigma_k$  axis). The



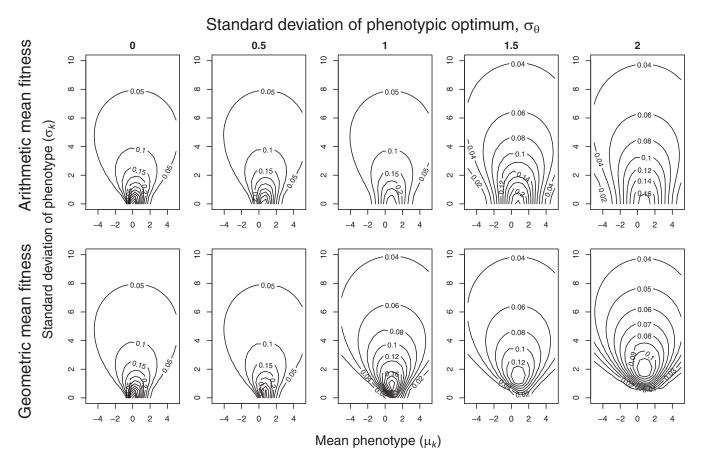
**Figure 2.** Fitness surfaces for a symmetrical fitness function for genotypes with different values of the mean phenotype  $\mu_k$  and variation in phenotype  $\sigma_k$ . Contour lines show long-term arithmetic mean fitness (top row) and geometric mean fitness (bottom row). The position  $\theta$  of the fitness function fluctuates stochastically between generations,  $\theta \sim N$  (0,  $\sigma_{\theta}$ ), the magnitude  $\sigma_{\theta}$  of environmental fluctuations increases successively (from 0 to 3) in the different columns from left to right. Irrespective of the scale of these fluctuations and the phenotypic variation ( $\sigma_k$ ), fitness is always maximized by a peak in the contours in the middle of the x-axis, corresponding to a mean phenotypic value ( $\mu_k$ ) of zero, because the individual fitness function is a symmetrical normal distribution with a mean of 0 and width of  $\omega = 1$ .

selection gradient will thus adaptively increase the phenotypic variance, and not the mean phenotype *per se*.

For phenotypically canalized traits (i.e., traits that have experienced selection in  $\sigma_k$  toward zero), we can infer that the fitness functions of these traits have fluctuated less across generations (smaller  $\sigma_\theta$ ), as we otherwise would not have seen this environmental canalization. For these values of  $\sigma_\theta$ , geometric and arithmetic mean fitness peaks at more similar  $\mu_k$  values when  $\sigma_k$  is low (Fig. 4, darker lines). As  $\sigma_k$  increases, mean fitness  $\bar{w}(k)$  becomes less skewed (see eq. (2), skew parameter  $\alpha$  decreases with increasing  $\sigma_k$ ) and therefore CBH will to a smaller extent shift  $\mu_k$  on top of any insurance already occurring. We note that if  $\sigma_k$  is constrained to only exhibit a limited amount of DBH, then considerable CBH and DBH will co-occur (e.g., the dependence of optimal  $\mu_k$  on  $\sigma_k$  in the lower right panel of Fig. 3; lighter lines showing large CBH at low  $\sigma_k$  in Fig. 4), but only limited amounts of CBH (a shift of up to 10% in  $\mu_k$  for  $\sigma_\theta = 1$ , Fig. 3) can co-occur with optimal

amounts of DBH. However, we note that there is a consistent difference in that geometric mean fitness is much more sensitive than is arithmetic mean fitness to slight changes in  $\mu_k$  away from the optimum, i.e. the geometric mean fitness surfaces are much more "peaked" than the arithmetic mean fitness surfaces, and a horizontal displacement from the peak would cause much greater fitness decline. This effect is due to the higher fitness variance at these  $\mu_k$  values, and this stronger stabilizing selection towards the optimum can thus represent an underappreciated bet-hedging mechanism.

Figure 5B illustrates a similar case of an apparent bet-hedging effect being instead attributable to simply maximizing arithmetic mean fitness, and thus not necessarily representing bet-hedging at all. In this case, if the mean phenotype is constrained at a suboptimal value, such as may be the case in a climate change scenario shifting the position of the fitness function, a positive amount of phenotypic variance is adaptive (i.e., a risk-prone strategy due to

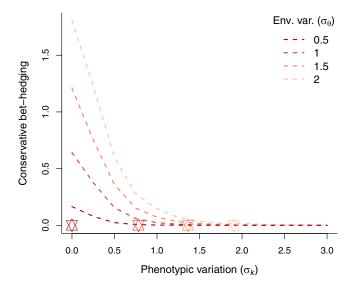


**Figure 3.** Fitness surfaces for an asymmetrical fitness function for genotypes with different values of the mean phenotype  $\mu_k$  and phenotypic variation  $\sigma_k$ . Contour lines show long-term arithmetic mean fitness (top row) and geometric mean fitness (bottom row). The position θ of the fitness function fluctuates stochastically between generations,  $\theta \sim N$  (0,  $\sigma_\theta$ ), the magnitude  $\sigma_\theta$  of the fluctuations increasing from left to right. In contrast to Fig. 2, as soon as  $\sigma_\theta > 0$  fitness is always maximized here by a peak in the contours to the right of the middle of the *x*-axis (where  $\mu_k$ =0), because the individual fitness function is a skew normal distribution with a mode of 0, width of  $\omega$ =1 and skew of  $\alpha$ =5.

risk sensitivity (Caraco et al. 1980; Stephens 1981), later termed variance sensitivity—see Discussion). This result can be understood, like DBH, as the different individuals of the genotype being phenotypically different (so that at least some are well adapted to the current conditions) rather than everyone being somewhat maladapted. However, there is no need here to invoke a geometric mean (bet-hedging) argument because this diversification of phenotypes simply maximizes arithmetic mean fitness across the individuals of the genotype. This type of adaptive phenotypic variance is often attributed to bet-hedging without considering whether the trait specifically increases geometric mean fitness at the cost of a decrease in arithmetic mean fitness (Mountford 1968).

# Discussion

Among the various types of adaptive strategies to cope with environmental stochasticity, many have typically been considered from a within-individual perspective in the tradition of behavioral ecology. These use optimality theory to maximize some fitness proxy using the arithmetic mean across instances within a single generation, such as energy intake per time (Davies et al. 2012). An example is optimal foraging, a large body of the behavioral ecology literature that deals with such within-individual traits, including variance-sensitivity, state-dependent energy budgets, adaptive levels of energy reserves, and information sampling of foraging options (Stephens et al. 2007). Some rather different strategies have been considered to operate among individuals and over many generations. This long-term perspective has been in the tradition of evolutionary theory, which has identified key concepts such as environmental canalization and bet-hedging (Slatkin and Lande 1976; Bull 1987; Philippi and Seger 1989; Frank and Slatkin 1990). In an attempt to reconcile these contrasting views, we have calculated both long-term arithmetic and geometric mean fitnesses for combinations of trait means and variances under different levels of stochastic environmental

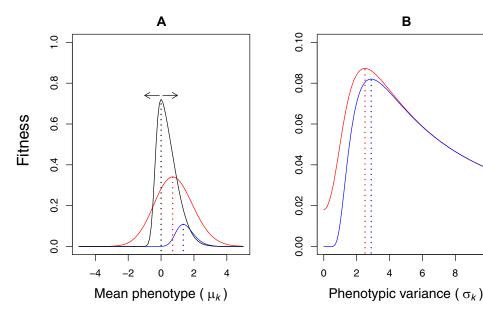


**Figure 4.** Conservative bet-hedging (CBH), defined as the difference in the mean phenotype ( $\mu_k$ ) maximizing long-term arithmetic fitness and the phenotype that maximizes geometric mean genotype fitness, for given phenotypic standard deviation ( $\sigma_k$ ). Lines represent results for different values environmental variation  $\sigma_{\theta}$ , as in Fig. 3. The individual fitness function w has a width of w = 1 and skew of w = 5, also as in Fig. 3. Colored stars along the w axis represent the optimal amount of DBH for the corresponding magnitude of environmental variation w and width of the fitness function w.

fluctuations. By comparing the results obtained when maximizing arithmetic versus geometric mean fitness, we have illustrated some possible similarities between the two approaches, and the discrepancies that arise when considering the effects of either of these two measures of fitness in isolation.

Crucially, we use skewed fitness functions to demonstrate that shifting the mean phenotype away from the steeply decreasing side of the fitness function may provide a more useful and realistic case of conservative bet-hedging (CBH). This fulfills the definition of bet-hedging, in that it increases geometric mean fitness at a cost of lower arithmetic mean fitness (i.e., it provides lower fitness in the average environment, but also a lower variance in fitness across environments). Such a type of CBH has not been formally modeled previously, rather theoretical treatments of CBH have been limited to models with two discrete environments, where CBH has been envisioned as a canalized phenotype providing a compromise between the peaks of the fitness functions for the two environments (Crowley et al. 2016; Starrfelt and Kokko 2012). This "generalist" CBH strategy always loses to a DBH strategy (producing specialists for the two environments) and is therefore not compatible with the concept of a "continuum" between CBH and DBH and thus some sort of coexistence of the two strategies.

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**Figure 5.** Cross-sections of fitness surfaces in the third column of Fig. 3 ( $\sigma_{\theta} = 1$ ). The red line is the fitness surface for arithmetic mean fitness, the blue line is the fitness surface for geometric mean fitness. Dotted vertical lines show the maxima for the respective functions. (A) A horizontal cross-section taken in the trait ( $\mu_k$ ) dimension at  $\sigma_k = 0$ , hence the individual fitness function (black line) peaks at zero, but fluctuates over time (black arrows), which causes mean fitness to be maximized at positive values of mean phenotype for both arithmetic and geometric mean. (B) A vertical cross-section taken in the phenotypic variance ( $\sigma_k$ ) dimension at  $\mu_k = -2$ , and so diversifying bet-hedging is favored by geometric mean fitness, but arithmetic mean fitness also increases with phenotypic variance, because of Jensen's inequality (the individual fitness function is strongly convex at  $\mu_k = -2$ ) and hence what is known as a variance-prone strategy – see text for details.

Various empirical studies of traits based on skewed fitness functions have invoked CBH arguments of the type we model here (e.g., Boyce and Perrins 1987; Simons and Johnston 2003). However, this shift is often also adaptive from an arithmetic mean fitness point of view in terms of an "insurance" strategy (Dall 2010). With a skewed fitness function, the cliff-edge effect entails that if individuals with the same genotype differ stochastically in their phenotypes (or the fitness value of their phenotypes, e.g., due to inhabiting different microenvironments – see Fig. 1), their average fitness is maximized if the mean phenotype is shifted away from the peak of the fitness function, toward the less steeply decreasing side (Mountford 1968; Vercken et al. 2012; Mitteroecker et al. 2016). The same is also true for a single individual experiencing uncertainty about its current state (i.e., regarding its phenotype or position on the x-axis on the fitness function) or uncertainty about its current microenvironment (i.e., the position of the fitness function on the x-axis relative to its phenotype). Its average fitness is therefore also maximized by "playing it safe" and moving its phenotype away from the peak down the shallow slope of the skewed fitness function. This shift (insurance) in the mean phenotype thus increases both arithmetic and geometric mean fitness and is not a bet-hedging strategy. Additionally, we hypothesized that CBH (lowering the variance in expected fitness for each individual) might shift the mean phenotype even more away from the peak of the fitness function than insurance alone. However, our analysis shows that maximizing geometric mean fitness only requires a moderate or small further shift in the mean phenotype of at most 27% as compared to the mean phenotype that maximizes arithmetic mean fitness, and that this effect decreases as environmental fluctuations become larger.

An exception to this is in cases where there is some constraint limiting the phenotypic variance,  $\sigma_k$ . The effect is shown in Fig. 4 and especially in Fig. 5A, where geometric mean fitness (blue line) is maximized for a higher phenotypic value (the individual fitness function peaks at zero and has its steepest decline for negative values, see Fig. 1) than arithmetic mean fitness (red line). This difference in optimum phenotypic values for such canalized traits stems solely from a fitness variance-reducing benefit and can thus be attributed to CBH. However, whenever the phenotypic variance  $(\sigma_k)$  is unconstrained and can evolve to optimum values, the diversification bet-hedging (DBH) effect of increasing phenotypic variance instead increases fitness much more effectively than does any such possible CBH effect, shifting the canalized phenotype to more positive values further down that shallow side of the fitness function. We would therefore expect selection to favor this DBH mechanism to reduce fitness variance (Lande and Arnold 1983), rather than shifting the phenotype with additional CBH beyond that already captured by the effect of adaptive insurance.

We therefore conclude that, given the opportunity for insurance, there is a limited scope for a single trait to exhibit both DBH and CBH as an additional adaptation on top of any adaptive insurance already being selected for. If any environmentally induced phenotypic variation ( $\sigma_k$ ) is allowed to evolve then DBH does appear alongside insurance, which decreases the need for CBH. Note that in our model we used as a starting point for such investigations only one phenotypic trait and a single pattern of environmental stochasticity, even if there was also independent environmentally induced effects on phenotypic variation ( $\sigma_k$ ) – see Figs. 2 and 3. Hence, any adaptive solution that maximized arithmetic mean fitness could potentially also account for the same pattern of environmental stochasticity experienced at the genotype level. This "alignment of fitness interests" maximizing both arithmetic and geometric mean fitnesses of a single trait in the face of the same regime of environmental fluctuations and skewed fitness functions at the two levels is intriguing, but it does not promise to make empirical evidence for conservative bet-hedging any less "elusive" (Childs et al. 2010; Simons 2011). While the structure of environmental variation in our model might reflect the general pattern expected of environmental stochasticity in nature, regimes of environmental stochasticity may differ between levels and timescales (e.g., seasonal variation versus El Niño events, as experienced by annual organisms) and are likely to implicate more than one trait in any evolutionary response. Therefore, understanding adaptations to environmental stochasticity at different levels, such as insurance versus CBH, requires that we appreciate how patterns of the stochasticity in question align and differ at the different levels of organismal experience.

Our result in this regard brings into focus the ecological relevance of previous work. For example, Lof et al. (2012) used a stochastic dynamic model of timing of reproduction in great tits when the timing of the food peak fluctuates between years. They assumed an asymmetric fitness function of laying date relative to the food peak and showed that maximizing expected (arithmetic mean) fitness does indeed produce an adaptive mismatch with the food peak, in the direction away from the steeply decreasing side of the fitness function (an "insurance" result). They acknowledge that "there might be additional benefits of adaptive mismatch in terms of reductions in fitness variance" - i.e., maximizing geometric rather than arithmetic mean fitness might yield a different result if fitness variance is lowest for a different laying date than the observed outcome. However, their forward simulations (using the optimal decision matrix from the dynamic model) "suggest that the variation in fitness often exhibited a minimum close to the observed optimal laying dates" (Lof et al. 2012). Hence, there is little scope for CBH to shift the optimal laying date any further away from the cliff edge. However, geometric mean fitness benefits resulting from a reduction in fitness variance across

generations can provide an added selection pressure towards the same optimum phenotypic values as insurance. This result appears in our model in that the geometric mean fitness surfaces are more peaked around the maxima than the arithmetic mean fitness surfaces (Figs. 2 and 3) - i.e., the selection pressure toward the same insurance optimum becomes stronger due to also producing lowest fitness variance (i.e., the CBH effect) across generations at this same optimum. All of which may provide reason for optimism with regards to species survival in a period when human-induced environmental change may produce sudden increases in environmental stochasticity that are too rapid for effective evolutionary responses (Barrett and Hendry 2012; Nadeau et al. 2017). This is because in the case of asymmetric fitness functions then any currently adaptive insurance strategy will already have selected for the appropriate phenotype, and little extra evolutionary conservative bet-hedging (CBH) response will be needed in terms of additional changes to the mean phenotype.

The importance of environmental stochasticity at the individual versus genotypic level is highlighted in a large body of previous work on bet-hedging (Levins 1962; Cohen 1966; Gillespie 1974). These identify the "grain" of the environmental variation as a strong determinant of whether bet-hedging strategies will evolve (Crowley et al. 2016; Starrfelt and Kokko 2012). If individuals in a population experience very different environments (i.e., the environment is "fine-grained" or "locally variable"), the fitness correlations between individuals of the same genotype will be low and the scope for DBH is reduced. Assuming a continuous distribution of environmental fluctuations, such as in our model, a very finegrained environment also implies that a larger proportion of the total environmental variation is experienced by individuals of the same genotype within each generation. The between-generation fluctuations in mean environment therefore become smaller, and a smaller proportion of the variance in fitness is experienced at the genotype level. Only when the environmental conditions are common to a large proportion of the population every generation (i.e., a "coarse-grained" environment, featuring "global variation") is there a large variance in genotype fitness between generations, which can be ameliorated by adaptive bet-hedging strategies.

While environmental "grain" is not explicitly modeled here, it is interesting to consider the  $\sigma_k$  gene as any trait that interacts with the grain of the environment. DBH traits, such as offspring dispersal and variation in dormancy duration (i.e., dispersal in time and space), in effect respond to and modify the grain of the environment as it is experienced. Hence, adaptive dispersal (in time or space) leads such genotypes to experience a more fine-grained environment (Gourbière and Menu 2009; Scheiner 2014). We therefore see why our model suggests that the possibility of DBH makes additional CBH on top of insurance unnecessary – the correlation in fitness between individuals of the same genotype can always evolve to be low enough (via DBH) such

that arithmetic mean fitness is a good determinant of long-term fitness.

An early model that hinted at this point involved three distinct adaptations for "reducing risk in variable environments" in seed production in desert plants: seed size, dispersal, and dormancy (Venable and Brown 1988). Seed size increases survival in bad environments, but does not affect survival in good environments. Given the trade-off between seed number and size, small seeds are optimal in good environments, but large seeds have a lower variance in expected fitness per individual. Whether increasing seed size represents insurance or CBH depends on the proportion of the environmental variation that is experienced by the genotype within versus between each generation. With no dispersal or dormancy, the environment is coarse-grained, fitness is purely a multiplicative process and increased seed size is clearly a bethedging trait increasing geometric mean fitness at the cost of a lower arithmetic mean fitness. But increased seed size may also maximize arithmetic mean fitness across fine-grained environments, which is the appropriate fitness measure if the genotype is sufficiently spread in space (or time, in this case) to experience the full range of environmental variation in each generation (Levins 1962). Thus, dispersal and dormancy are not only diversifying bet-hedging (DBH) traits, but also determine the grain of the environment and the need for conservative bet-hedging (CBH) versus insurance. Venable and Brown (1988) show that these adaptations to reduce risk are essentially substitutable and that a decrease in the value of either of the traits away from the optimum leads to evolutionary compensation in an increased value of the other traits. However, note that the DBH traits here, dispersal and dormancy, are inherently different from a conceivable fourth risk-reducing strategy: variation in seed size itself. In discrete environments ("good" and "bad") the optimal DBH strategy maximizing geometric mean fitness is to produce seeds with optimal size for each of the environments (small and large) with the probabilities of those respective environments occurring, while in continuously varying environment seed size should vary around a mean trait value, as in our model. Here, we showed that in a continuously varying environment, this type of DBH (which Venable and Brown (1988) do not explore) generally provides a greater benefit than CBH. However, we do not rule out that with other types of environmental variation and environmentspecific fitness functions then changing the mean trait value may be a better strategy. We also point out again that both of these risk-reducing strategies are only effective once the grain of the environment causes selection to maximize geometric rather than arithmetic mean fitness (Venable and Brown 1988; Scheiner 2014).

In our current model, the only time arithmetic mean fitness would be higher with more phenotypic variance (i.e., for an individual, rather than a DBH genotype increasing among-individual variation) would be if its fitness function were strongly convex around its current phenotype (Fig. 5B), such as at the tails of a Gaussian fitness function. This is the same adaptive gambling effect that produces risk sensitivity (Caraco et al. 1980; Stephens 1981), aka variance sensitivity (Smallwood 1996; Stephens et al. 2007), which is an important concept from economics used to explain foraging decisions and other behaviors when there are more or less variable options. The fitness advantage of variance sensitivity follows directly from Jensen's inequality: if the fitness function f of some utilized resource or trait x is convex, then the mean fitness gained over a sequence of events with variable reward x will be larger than the fitness gained from the mean reward x: E[f(x)] > f(E[x]). This is an arithmetic mean fitness maximizing argument, and the benefit of increasing phenotypic variance can therefore be seen in our calculations of arithmetic mean fitness as well (top rows of Fig. 2 and 3; Fig. 5B). Essentially, for a constant  $\mu_k$  sufficiently far from the fitness function peak, arithmetic mean fitness is maximized at an intermediate value  $\sigma_k > 0$ . This similarity between variance sensitivity and DBH in producing variable phenotypes but at different adaptive timescales has not been reported before, and it is made explicit here through our comparison of trait means and variances maximizing long-term arithmetic or geometric mean fitness.

We have demonstrated several results linking theory concerning individual-level strategies from behavioral ecology with genotype-level adaptations from evolutionary biology in context of environmental uncertainty. There is still more work to be done in reconciling bet-hedging theory with other types of adaptations to variable and unpredictable environments, such as specialist versus generalist strategies (Gilchrist 1995; Buckley and Huey 2016), interactions with phenotypic plasticity (Simons 2014; Grantham et al. 2016), the evolution and maintenance of sexual reproduction (Burke and Bonduriansky 2017; Li et al. 2017; Gerber et al. 2018), and topics on human development and decision-making (McNamara et al. 2011; Fawcett et al. 2014; Higginson et al. 2016). An important next step is now to connect these theoretical studies to real world examples and quantitative studies of organisms in the lab and in the wild, for example if we are to understand how populations might respond to current human-induced rapid environmental change. Applying this genotype-level view to predictive statements concerning evolutionary responses requires extensive data on past environmental fluctuations, clear links between trait values and individual fitness, as well as detailed knowledge of the genetic mechanisms underlying the traits. While this might seem an insurmountable task, the empirical evidence for bet-hedging in the wild has shown that long-term studies on natural populations can provide answers to these types of questions (Simons 2011). We hope that our results here act as a motivation to both empirical and theoretical studies on adaptations to stochastic environments to compare and contrast individual versus genotype

perspectives and the alternative adaptive currencies of arithmetic versus geometric mean fitness.

#### **AUTHOR CONTRIBUTIONS**

I.I.R., J.W., and J.T. conceived of the ideas and all authors contributed to the development of the ideas. J.T. and T.R.H. wrote the code and did the calculations. T.R.H. wrote the manuscript with contributions from all authors. All authors gave final approval for publication.

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#### **CODE ACCESSIBILITY**

The code is available as Supporting Information.

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## Supporting Information

Additional supporting information may be found online in the Supporting Information section at the end of the article.

Appendix S1: R code