Adhesion between rubber and glass in dry and lubricated condition

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We study the adhesion between differently processed glass and filled bromobutyl rubber in dry condition, and in water and in silicone oil. The boundary line between contact and non-contact in adhesion experiments can be considered as a mode I crack and we show that viscoelastic energy dissipation close to the opening (or closing) crack tip and surface roughness, strongly affect the work of adhesion. We observe strong adhesion hysteresis in contrast to the Johnson–Kendall–Roberts (JKR) theory prediction for elastic solids this results in a pull-off force (and work of adhesion) which depends on the loading force and contact time. In particular, for the system immersed in water and silicone oil we register very weak adhesive bonding. For glass ball with baked-on silicone oil the pull-off force is nearly independent of the contact time, but this is not observed for the unprocessed glass surface.

1 Introduction

In our everyday practice most of the contacts manifest rather weak adhesion [1, 2]. However, sometimes adhesion becomes an issue. For instance, clean smooth glass surfaces can exhibit strong adhesion against (smooth) rubber surfaces. Thus, in applications involving rubber in contact with glass it is often necessary to “passivate” the glass surface e.g. by siliconisation. One such example is syringes, where a rubber stopper must be able to slide with low stable friction against a barrel made from glass[3, 4]. The rubber-glass interface is usually lubricated with silicone oil. However, during long time of stationary contact the silicone oil is squeezed out from the rubber-glass asperity contact regions, resulting in a high breakloose friction force. In addition, when the syringe is filled with water (with additives), the silicone oil film may be unstable and break up into small droplets (spherical cups). In this case the rubber stopper can be exposed to bare glass in some contact areas, resulting in a high sliding friction. This can be avoided if silicone oil molecules are chemically attached to the glass surface, which is possible using heat treatment of the (silicone oil covered) glass barrel.

The siliconisation of the syringe barrel is an extremely important aspect of the production of sterile, prefillable glass syringes. Both inadequate and excessive siliconisation can cause problems in this connection[5]. One option for minimizing the amount of free silicone oil in a syringe is the thermal fixation of the silicone oil on the glass surface in a process called baked-on siliconisation. Usually the silicone oil is applied as an emulsion and then annealed at the temperature ≈ 300°C. This creates a permanent hydrophobic anti-friction coating due to the formation of stable covalent bonds between the glass surface and the silicone oil.

The tribology of the contact between glass and rubber have been studied in pioneering work of Roberts[6] and of McClune et al[7]. Here smooth rubber surfaces was squeezed against glass in a fluid, while being optically observed. It was shown that the flexible rubber resulted in entrapment of liquid by elastic deformation. The removal of fluid (water) between rubber and glass surfaces depends on the wetting properties of the interface, as shown by Roberts and Tabor in Ref. [8, 9]. In the work of Koenen et al[10, 11] the rubber-glass wiping problem was studied experimentally. They showed that stick-slip motion and related squeal noise occurred in a narrow range of sliding speeds and load, which is complicated by capillary adhesion effects that can induce higher friction than in the dry environment.

In this paper we study the adhesion between “clean” and siliconised glass balls (radius $R$) and a flat rubber surface. The relation between adhesion and sliding friction is not trivial, but it is clear that some phenomena such as fluid squeeze-out and interfacial aging of the contact should manifest itself in both the adhesion and friction. Thus, the increase in the breakloose friction force with the time of stationary contact depends on fluid squeeze-out, dewetting and bond-formation between the two solids, all of which also influence the adhesive interaction between the solids which can be probed in pull-off experiments. The nature of the breakloose friction has been studied in Ref. [12–14] for glass surfaces covered by silicone oil, but not for surfaces with baked-on silicone oil.

The contact between a spherical ball and a flat constitute the simplest and most well-defined contact mechanics problem. For elastically soft solids, and with large radius $R$, the Johnson–Kendall–Roberts (JKR)[15–18] theory is valid. This theory predict the pull-off force
$F_c = (3\pi/2)wR$, where $w = w_{open}(v)$ is the work of adhesion or, more accurately, the energy (per unit surface area) to propagate an opening crack at the speed $v$ (where $v$ is the crack tip speed at the point of the pull-off instability). In the adiabatic limit (i.e., infinitesimally low pull-off velocity) $w$ is equal to the change in the interfacial free energy $\Delta \gamma = \gamma_1 + \gamma_2 - \gamma_{12}$ (where $\gamma_1$, $\gamma_2$ and $\gamma_{12}$ is the solid-vapor interfacial energies of solid 1 and 2, and the interfacial energy of the contact between solid 1 and 2, respectively).

Adhesion mechanics of real objects is a complex phenomenon and is only partly understood [19–28], especially for soft materials with viscoelastic and non-linear properties [29, 30]. The work of adhesion during pull-off is strongly influenced by two competing effects: non-adiabatic effects, in particular the viscoelastic energy dissipation in the vicinity of the opening crack tip[31, 32] (which may strongly increase the work of adhesion), and the surface roughness, which usually reduce the work of adhesion[33, 34]. We note that the boundary line between contact and non-contact in JKR adhesion experiments can be considered as a mode I crack even if the material on the two sides are different (see, e.g., Ref. [35]). The non-adiabatic effects also often result in an adhesion force which is much smaller during approach than during pull-off, an effect referred to as adhesion hysteresis. The effect of surface roughness is considered separately in [33, 36–41].

In the present study we consider the adhesion between bromobutyl rubber and a smooth glass surfaces. We consider both dry condition, and in water and in silicone oil. In Sec. 2 and Appendix A, B and C we present the material properties, namely the viscoelastic modulus of the rubber, viscoelastic stress and strain relaxation, contact angles and surface energies, and the surface roughness power spectrum of the rubber surface. In Sec. 3 we present the results of contact mechanics calculations, which form the basis for the analyze of the experimental adhesion data presented in Sec. 6. Sec. 4 discuss viscoelastic crack propagation at the rubber–glass interface. In Sec. 5 we present optical pictures of the contact between a smooth glass surface and the bromobutyl rubber, which illustrate some important aspects of contact hysteresis. In Sec. 6 we consider adhesion between the rubber and glass balls in the dry state, in water, and in silicone oil. Sec. 7 contains the summary and conclusion. Appendix A–J present details related to material properties and some calculations.

2 Material properties and surface topography

2.1 Viscoelastic modulus.

The viscoelastic properties of rubber is needed for contact mechanics or adhesion calculations, and for calculating the velocity dependency of the adhesive crack propagation e.g., during pull-off. For adhesion study it is necessary to have information about the complex elastic modulus over a rather large frequency range, as well as at different strain values sometimes (on rough surfaces) including very large strain of order 100%. A standard way of measuring the viscoelastic modulus is to oscillatory deform the rubber sample with a constant strain or stress amplitude. This is done at different frequencies and then repeated at different temperatures. The results measured at different temperatures can be time-temperature shifted to form a master curve at a chosen reference temperature, covering a broad range of frequencies. In Appendix A we summarize the results obtained for the filled bromobutyl rubber compound used in the adhesion studies.

2.2 Viscoelastic stress and strain relaxation.

We have performed stress and strain relaxation experiments for the bromobutyl rubber compound. In Fig. 1 we show the time dependency of the relaxation modulus $E(t)$ in units of the relaxation modulus at time $t_0 = 10$ s. The green curve is the stress relaxation modulus $E(t) = \sigma(t) / \sigma_0$, where $\sigma_0 = 0.4$ MPa is the stress imposed at time $t = 0$ and $\sigma(t)$ the resulting stress at time $t$. The solid red curve is the strain relaxation modulus $E(t) = \sigma_0 / \epsilon(t)$, where $\sigma_0 = 0.4$ MPa is the stress imposed at time $t = 0$ and $\epsilon(t)$ the resulting strain at time $t$. The red dashed curve is the strain relaxation modulus calculated from the low-strain (0.04%) master curve $E(\omega)$ shown in Fig. 27.
same as the strain relaxation modulus (dashed red curve) and is not shown in the figure.

Note that the strain relaxation modulus obtained from the small-strain measurement (strain amplitude 0.04\%) initially decay slower with time than the one obtained for large strain (of order \(\sim 10\%\)), but for large time the opposite behaviors is observed. The drop in \(E(t)\) from the large strain measurements (solid lines) in the time interval of interest below (from \(\sim 10^2\) s to \(\sim 10^5\) s) is about \(\approx 25\%\). The implication of this result for the time dependency of the contact area and the pull-off force will be discussed below.

2.3 Contact angles and surface energies.

In order to study the adhesion in water and silicone oil we need to know the interfacial energies between the rubber and glass and the two fluids, which can be estimated from contact angle measurements. We have measured the contact angles for water and silicone oil on the glass ball surface and on the surface of the bromobutyl rubber. Using this information we have estimated the adiabatic work of adhesion between the rubber and the glass surface, in the dry state, in water and in silicone oil. Here we summarize the most important results (see Appendix B for details).

In the dry state for long contact time the adhesive JKR contact is characterized by the adiabatic work of adhesion (for perfectly smooth surfaces) \(\Delta \gamma = \gamma_1 + \gamma_2 - \gamma_{12}\). Assuming that only dispersion forces are responsible for the interaction between the glass and the bromobutyl rubber, in Appendix B we estimate the adiabatic work of adhesion \(\Delta \gamma(\text{dry}) \approx 0.08 - 0.1\ J/m^2\). However, the experimental adhesion study presented below indicates that stronger bonds form between the two surfaces and \(\Delta \gamma \approx 0.3\ J/m^2\).

In a liquid the adiabatic work of adhesion can be calculated using the Young-Dupre equation:

\[
\Delta \gamma(\text{wet}) = \Delta \gamma(\text{dry}) - \gamma(\cos \theta_{gl} + \cos \theta_{gl})
\]

where \(\gamma\) is the liquid surface tension and \(\theta_{gl}\) the contact angle of the liquid on glass and \(\theta_{rl}\) the contact angle of liquid on the rubber. Using this equation with \(\Delta \gamma(\text{dry}) \approx 0.3\ J/m^2\) gives in water \(\Delta \gamma(\text{wet}) \approx 0.2\ J/m^2\).

In Appendix B we argue that the interaction potential between a flat glass surface and a flat rubber surface in water takes the form shown in Fig. 31 with a repulsive barrier before the strong attraction due to direct rubber-glass bonds. That is, at separation of order a few nanometer the interaction is only via dispersion forces and steric repulsion and is repulsive. At short separation the interaction potential has a minimum corresponding to direct contact between the rubber and the glass surface. In this state bonding forces (of unknown nature) stronger than the dispersion forces occur between the surfaces.

When a bromobutyl rubber is squeezed in contact with glass surface in water we expect first a rapid squeeze-out (see Sec. 3) until contact occur between the rubber asperities and the glass surface. However, at short contact time we do not expect any true atomic contact between the rubber and the glass surface but a water film of nanometer thickness separate the surfaces in the asperity contact regions. However, this state is only metastable and after a long enough time we expect true atomic contact to form between the rubber and the glass surface in the asperity contact regions. This dewetting transition involves the nucleation (by thermal fluctuations) of nanometer sized contact region followed by the removal of the nanometer water film by a (mainly) surface-energy driven squeeze-out process. Thus we expect the contact area between the rubber and the glass surface to increase continuously with increasing contact time, as indeed observed (see Sec. 6).

2.4 Rubber surface roughness.

We have studied the rubber surface topography using an optical method and atomic force microscopy (AFM). As shown in Appendix C the height probability distribution is nearly Gaussian, with the root-mean-square (rms) roughness, when measured over a surface area \(1\ mm \times 1.4\ mm\), of about \(h_{\text{rms}} = 2.9 \pm 0.1\ \mu m\) and with the highest point \(\sim 13\ \mu m\) above the average plane. In Appendix C we also give the surface roughness power spectrum which is needed for the adhesion and fluid squeeze-out calculations.

3 Theory: contact area and interfacial separation

As a preparation for the analysis of the adhesion data
to be presented in Sec. 5 and 6, here we present some theoretical predictions for the contact between the bromobutyl rubber and smooth glass. We first study adhesion using the theory developed in Ref. [42, 43] which accounts for the influence of the surface roughness on work of adhesion and the contact area. Next we calculate the time-dependent average interfacial separation, and the area of real contact, during fluid squeeze-out between a rubber block and the glass surface. The fluid is assumed to be Newtonian, and we neglect the influence of interfacial energies on the squeeze-out process, i.e., no dewetting transition occurs. The calculations are performed using the Reynolds equations for fluid flow, where the surface roughness enter via flow factors, which are obtained using the Persson contact mechanics theory and the Bruggeman effective medium theory (see Ref. [44]).

In the following we will present results for the work of adhesion and we will use the following notation. The adiabatic work of adhesion (for perfectly flat surfaces) is denoted by \( \gamma_0 \). We also refer to this as the interfacial binding energy per unit surface area. For an opening crack we denote the work of adhesion (for perfectly smooth surfaces) by \( \gamma_{\text{open}}(v) \) which depend on the crack tip velocity \( v \). Similarly, \( \gamma_{\text{close}}(v) \) denote the work of adhesion for a closing crack. Note that \( \gamma_{\text{close}}(v) < \Delta \gamma < \gamma_{\text{open}}(v) \) and that as \( v \to 0 \) we have \( \gamma_{\text{open}}(v) \to \Delta \gamma \) and \( \gamma_{\text{close}}(v) \to \Delta \gamma \).

3.1 Influence of surface roughness on the adhesion.

In this section we study the influence of surface roughness on the contact between rubber and glass balls in the dry state, and in water and in silicone oil. We assume infinite long contact time so that viscoelastic effects, and other non-adiabatic processes, are unimportant. In this limit, in the dry state the adhesive contact is characterized by the adiabatic work of adhesion (for perfectly flat surfaces) \( \Delta \gamma = \gamma_1 + \gamma_2 - \gamma_{12} \). In the case of adhesion in a liquid (here water or silicone oil) we assume that the liquid pressure is everywhere equal to the external pressure so the total load is carried by the area of real contact. In a liquid the adiabatic work of adhesion can be calculated using the Young-Dupre equation (1).

We will now present calculated results for the adhesive contact between the glass ball and the surface of the bromobutyl rubber. Fig. 3(a) shows the normalized area of real contact, \( A/A_0 \) (where \( A_0 \) is the nominal contact area), as a function of the nominal contact pressure (in MPa), without adhesion (green curve) and with adhesion (red and blue curves). The rubber surface is assumed to have surface roughness with the power spectrum shown in Fig. 33 (dashed line) and the Young’s modulus \( E = 2.5 \) MPa and Poisson ratio \( \nu = 0.5 \). The work of adhesion used for obtaining the red curve is \( \Delta \gamma = 0.1 \) J/m\(^2\) and for the blue curve \( \Delta \gamma = 0.025 \) J/m\(^2\). Fig. 3(b) shows the average surface separation, as a function of the nominal contact pressure (in MPa), without adhesion (green curve) and with adhesion (red and blue curves). The rubber surface is assumed to have surface roughness with the power spectrum shown in Fig. 33 (dashed line) and the Young’s modulus \( E = 2.5 \) MPa and Poisson ratio \( \nu = 0.5 \). The work of adhesion used for obtaining the red curve is \( \Delta \gamma = 0.1 \) J/m\(^2\) and for the blue curve \( \Delta \gamma = 0.025 \) J/m\(^2\). These values for the work of adhesion is smaller than the adiabatic value (which may be \( \approx 0.3 \) J/m\(^2\), but during contact formation the work of adhesion is reduced. Results for \( \Delta \gamma = 0.3 \) J/m\(^2\) will be shown below.

Fig. 3(b) shows the average surface separation as a function of the nominal contact pressure with adhesion (\( \Delta \gamma = 0.1 \) J/m\(^2\), red curve) and without adhesion (green curve).

In contact mechanics for rough surface with roughness over many decades in length scales, the concept of magnification is very important [43]. When we study the interface at the magnification \( \zeta \) we only observe the surface roughness with wavenumber \( q < \zeta q_0 \), where \( q_0 \) is a
reference wavenumber, here chosen as \( q_0 = 10^4 \text{ m}^{-1} \), corresponding to the reference length \( \lambda_0 = 2\pi/q_0 \approx 0.6 \text{ mm} \). Physical quantities, like the contact area, depend on the magnification used when studying the contact. For example, if \( \zeta \) is small (of order 1) we do not observe any surface roughness and it appears as if the contact is complete i.e. \( A/A_0 \approx 1 \). Fig. 4 shows the interfacial binding energy (or work of adhesion) (a), and the normalized area of real contact (b), as a function of the logarithm of the magnification \( \zeta \). Note that the work of adhesion \( w_0 \) vanishes when \( \Delta \gamma = 0.1 \text{ J/m}^2 \). In fact, the surface roughness result in a vanishing work of adhesion for \( \Delta \gamma < 0.25 \text{ J/m}^2 \) (not shown).

Fig. 5 shows the (a) normalized area of real contact and (b) the work of adhesion, as a function of the logarithm of the magnification \( \zeta \) when \( \Delta \gamma = 0.3 \text{ J/m}^2 \) found from Persson’s theory. Note that \( w_0(\zeta = 1) \approx 0.03 \text{ J/m}^2 \) which imply that there is a non-vanishing pull-off force. For the same parameters as in Fig. 3.

Another very important implication of adhesion hysteresis is the following: during removal of the loading force the contact area will not drop to zero but will stay nearly unchanged. The reason is that for the opening crack (crack tip velocity \( v \)) the interfacial binding energy \( \gamma_{\text{open}}(v) >> \Delta \gamma \) unless \( v \) is extremely small, so that the decrease in the contact area with increasing time after removing the load is so slow that it can be neglected on the time-scale of practical importance. If the contact area is unchanged we also expect only a relative small increase in more detail in Sec. 5. Thus during contact formation, for short contact time the interfacial binding energy nearly vanishes while it is strongly enhanced during pull-off. Fig. 3 shows that if the nominal contact pressure \( p_0 \approx 0.1 \text{ MPa} \), for relatively short times where adhesion can be neglected, \( A/A_0 \approx 0.1 \). However, after very long time the interfacial binding energy will approach the adiabatic interfacial binding energy, \( \gamma \approx 0.3 \text{ J/m}^2 \), and in this case from Fig. 5 for \( p_0 \approx 0.1 \text{ MPa} \) we expect \( A/A_0 \approx 0.9 \). Thus we expect the contact area to increase slowly with time from a relative small value, of order \( A/A_0 \approx 0.1 \), to a value close to complete contact for very long contact times.

**FIG. 4:** The (a) interfacial binding energy (or work of adhesion), and (b) the normalized area of real contact, as a function of the logarithm of the magnification \( \zeta \) found from Persson’s theory. Note that for both \( \Delta \gamma = 0.1 \text{ J/m}^2 \) (red curve) and \( \Delta \gamma = 0.025 \text{ J/m}^2 \) (blue curve) \( w_0(\zeta = 1) = 0 \) which imply that there is vanishing pull-off force in the adiabatic limit (infinitely small pull-off velocity). For the same parameters as in Fig. 3.

**FIG. 5:** The (a) normalized area of real contact and (b) the interfacial binding energy (or work of adhesion), as a function of the logarithm of the magnification \( \zeta \) when \( \Delta \gamma = 0.3 \text{ J/m}^2 \).
in the average interfacial separation when the load is removed. For contact in fluids (water and silicone oil) we also observe (a weak) adhesion and the results presented in Sec. 6 indicate that in these cases too the contact area and the average interfacial separation change rather little when the load is reduced from the maximum (where the nominal contact pressure is about 0.1 MPa) to zero. Optical pictures of the contact in water (see Sec. 6) support this claim.

3.2 Fluid squeeze-out.
We will show that the viscous forces in silicone oil (and hence also in water) have a negligible influence on the adhesion except in a short time period around detachment. Let us first estimate the typical contact pressures in the applications below. The maximum applied normal forces used below are of order $F = 0.1 - 0.2$ N. At these loads we can neglect the adhesion when estimating the nominal contact pressures. When a spherical ball with radius $R$ is squeezed against a flat surface with the normal force $F$, according to the Hertz theory the radius of the circular contact region is

$$r_0 = \left(\frac{3FR}{4E^*}\right)^{1/3},$$

where $E^* = E/(1 - \nu^2)$. The maximum nominal contact pressure

$$p_0 = \frac{3F}{2\pi r_0^2}.$$

Note that the contact pressure scale with the loading force as $p_0 \sim F^{1/3}$. Using $E = 2.5$ MPa, $\nu = 0.5$, $R = 1.5$ cm and $F = 0.1$ N gives $r_0 \approx 0.7$ mm and $p_0 \approx 0.1$ MPa.

Consider the squeezing of the glass ball against the rubber surface in silicone oil. The glass ball is assumed to be perfectly smooth, while the rubber surface has surface roughness with a power spectrum shown in Fig. 33. As shown elsewhere[45], the separation between the glass ball and the substrate as a function of time can be accurately described by a simpler model where the glass ball is replaced with a circular disc with the same radius $r_0$ as the radius of the Hertz contact region when the ball is squeezed against the rubber (with the same normal force) without a liquid. On the circular disc act the same load as on the glass ball. We will now present results for the interfacial separation and the area of real contact using this mapping of a ball on a disc.

Let us consider a circular disc with radius $r_0 = 0.7$ mm being squeezed against a nominal flat surface in a Newtonian fluid with the viscosity $\eta = 0.35$ Pas. The substrate surface has the surface roughness power spectrum shown in Fig. 33 (dashed line), and the Young’s elastic modulus $E = 2.5$ MPa and Poisson ratio $\nu = 0.5$. We show results for the squeezing pressures $p = 0.07$ MPa (green lines) (as relevant for the experiments presented in this paper), and for a much higher pressure $p = 1.5$ MPa (red lines), as typical for rubber seals or syringe applications. In (a) the lower red and green lines show the interfacial separation for perfectly flat surfaces (no surface roughness), while the other two lines is with the surface roughness included.

FIG. 6: The (a) logarithm of the interfacial separation and (b) the relative area of real contact, as a function of the logarithm of time, as a circular disc with radius $r_0 = 0.7$ mm is squeezed against a nominal flat surface in a Newtonian fluid with the viscosity $\eta = 0.35$ Pas. The substrate surface has the surface roughness power spectrum shown in Fig. 33 (dashed line), and the Young’s elastic modulus $E = 2.5$ MPa and Poisson ratio $\nu = 0.5$. We show results for the squeezing pressures $p = 0.07$ MPa (green lines) (as relevant for the experiments presented in this paper), and for a much higher pressure $p = 1.5$ MPa (red lines), as typical for rubber seals or syringe applications. In (a) the lower red and green lines show the interfacial separation for perfectly flat surfaces (no surface roughness), while the other two lines is with the surface roughness included.
be resolved in the experiments presented below, where the
time resolution is 1 s), but in the silicon oil (which
has 350 times higher viscosity than water), the snap-off
extend over ~ 100 s in agreement with theory predictions
(see Appendix I and J). Since the squeeze-out time
is proportional to the fluid viscosity, for water we expect
that it takes less than 1 s for the disc (or the ball) to
reached its final state.

For the higher nominal contact pressure \( p = 1.5 \) MPa
(red lines) the situation is completely different. Although
this case is not of relevance for the experiments presented
below, we will discuss this case in some detail as this is
the typical contact pressure prevailing in most engineer-
ing applications, e.g., for rubber seals or in the contact
regions between the ribs of a rubber stopper and the
barrel in syringe applications. At the contact pressure
\( p = 1.5 \) MPa, in the absence of the fluid, nearly complete
contact occurs between the solids in the nominal con-
tact area, i.e. \( A/A_0 \approx 1 \). However, in a fluid, when
the relative contact area reach \( A/A_0 \approx 0.4 \) the area of real
contact percolate, and no fluid can flow at the interface;
this result in trapped islands of pressurized fluid at the
interface. Hence, in a fluid, at least in the absence of
adhesion (dewetting), when during squeezing the relative
contact area approach \( A/A_0 \approx 0.4 \) the fluid flow at the
interface (squeeze-out) will slow down. This will result
in almost infinitely long squeeze-out times when the ex-
ternal load is large enough to give \( A/A_0 > 0.4 \) for dry
surfaces. This is the origin of the long-time dependency
of \( u(t) \) and \( A(t) \) shown in Fig. 6 for \( p = 1.5 \) MPa. We
note that this effect is of great importance in applica-
tions, e.g., to seals or syringes.

4 Viscoelastic crack propagation
It is well known that the boundary line between con-
tact and non-contact in JKR adhesion experiments can
be considered as a mode I crack even if the material
on the two sides are different (see, e.g., Ref. [35]).
For viscoelastic material the (opening) crack propaga-
tion energy (per unit surface area) can be written as
\( \gamma_{\text{open}}(v,T) = \Delta \gamma [1 + f(v,T)] \), where \( \Delta \gamma \) is the crack
propagation energy as the crack tip velocity \( v \to 0 \). From
the measured viscoelastic modulus we can calculate the
enhancement factor \( [1 + f(v,T)] \) to interfacial crack propa-
gation (see Appendix D), which is important for under-
standing the adhesion data to be presented later.

Using the theory developed in Ref. [31], in Fig. 7
we show the viscoelastic crack propagation factor \( [1 + f(v,T)] \) as a function of the logarithm of the crack tip
velocity \( v \). The results are for the bromobutyl rubber
compound at \( T = 20^\circ C \). The red line use the low-strain
(0.04% strain) modulus and the green line the large-
strain (≈ 15% strain) modulus. The vertical dashed line
indicate a typical crack tip velocity in the experiments
reported on in Sec. 6.

For the higher nominal contact pressure \( p = 1.5 \) MPa
(red lines) the situation is completely different. Although
this case is not of relevance for the experiments presented
below, we will discuss this case in some detail as this is
the typical contact pressure prevailing in most engineer-
ing applications, e.g., to seals or syringes.

5. Adhesion hysteresis
The discussion in Sec. 3 was assuming no adhesion
hysteresis. Let us now include the adhesion hysteresis.
We will use the argument first presented in Ref. [46,
47] to show that the pull-off force is always finite when
adhesion hysteresis prevail, assuming it is big enough.

Assume that at the end of the loading cycle the as-
perity contact regions appear as shown in Fig. 8(a). In
the absence of adhesion hysteresis (Fig. 8(b)), during
unloading the asperity contact regions would disappear
in a similar way as they were formed, and asperity con-
tact regions even at the center of the macroscopic contact
area will decrease in size even at the start of unloading,
where the radius \( r(t) \) of the the macroscopic separation
line (dashed lines in Fig. 8) is far from the center of
the contact region. However, if the adhesion hysteresis
is large enough so that the energy per unit area for the
opening crack \( \gamma_{\text{open}}(v) > > \Delta \gamma \), then the asperity contact
regions will only start to shrink when they are very close
to the macroscopic opening crack (in the crack-tip pro-
cess zone) (Fig. 8(c)). In this case the pull-off force will
be non-vanishing, and to a good approximation given by
the JKR theory with \( u \approx \gamma_{\text{open}}(v)A_1/A_0 \), where \( \gamma_{\text{open}}(v) \)
that the nominal contact pressure depends on the load approach we expect from the Hertz contact theory will be close to the relative contact area when the load occurs the work of adhesion during separation will be

As pointed out above, when strong adhesion hysteresis hysteresis, and (c) when strong adhesion hysteresis occurs so that \( \gamma_{\text{open}} \gg \Delta \gamma \). The black regions indicate asperity contact regions. Because of the adhesive interaction, complete contact occurs within the black regions. During pull-off in case (b) the asperity contact regions decrease in size everywhere. During pull-off in case (c) the size of the asperity contact regions remain unchanged (in spite of the reduction in the contact pressure) except close to the macroscopic (apparent) opening crack tip (dashed circle), where the asperity contact regions are broken by the propagation of microscopic opening cracks at each asperity contact region.

is the work of adhesion (for opening crack) obtained from the contact between smooth surfaces, and \( A_1/A_0 \) the normalized area of real contact. This is illustrated in Fig. 8(c) where the size of the asperity contact regions outside of the crack-tip process zone, remain unchanged (in spite of the reduction in the contact pressure). Very close to the tip of the macroscopic (apparent) opening crack (dashed circle) the asperity contact regions are broken by the propagation of microscopic opening cracks at each asperity contact region.

We now present results for how the adhesion force depend on the applied (maximum) load or normal force. As pointed out above, when strong adhesion hysteresis occur the work of adhesion during separation will be

where \( A_1/A_0 \) will be close to the relative contact area when the load is maximal. Assuming that the adhesion is weak during approach we expect from the Hertz contact theory that the nominal contact pressure depends on the load as \( F_1^{1/3} \).

If we assume that \( A_1/A_0 \) depends linearly on the nominal contact pressure (as is the case as long as adhesion is not important during approach, and \( A_1/A_0 \) smaller than \(-0.3\) then it follows that the pull-off force should be proportional to \( F_1^{1/3} \). We now present adhesion experiments to test this hypotheses (see also Ref. [47]).

Fig. 9(a) shows the interaction force as a function of time when a glass ball (diameter \( 2R = 5 \text{ cm} \)) approach and retract (speed \( v_z = \pm 25 \text{ \mu m/s} \)) from the bromobutyl rubber sheet. We show results for three different loading regimes, where the maximum loading forces are \( F_1 = 0.126 \) (red curve), \( 0.407 \) (green curve) and \( 0.747 \) N (blue curve). Assuming the rubber elastic modulus \( E_{\text{eff}} = 2.5 \text{ MPa} \) gives the Hertz maximum contact pressures \( P_0 = 0.072, 0.106 \) and \( 0.130 \) MPa. These are all in the region where, in the absence of adhesion, we expect the contact area to depend linearly on the contact pressure (see Fig. 3). Thus, since the Hertz contact pressure scales as \( F_1^{1/3} \) we expect the pull-off force to be proportional to \( F_1^{1/3} \). Fig. 9(b) shows that this is indeed the
case. Note that for smooth surfaces, where the contact is complete, we do not expect any dependency of the pull-off force on the maximum loading force. This was indeed shown to be the case in Ref. [47] for Polydimethylsiloxan (PDMS) rubber with very smooth surface.

We have performed optical studies of the contact between the bromobutyl rubber and a smooth glass surface. The glass plate was first loaded against the rubber surface with a large force (of order ~ 50 N) for ~ 5 s and after the load was removed. We observed that the rubber continue to adhere to the glass surface and the contact area was unchanged. (a) The contact after ~ 200 s contact time, prior to which we removed (by peeling) the contact between the rubber and the glass surface over the upper half of the nominal contact region. Note the boundary line (opening crack tip) between the non-contact area and the (partial) contact. (b) After waiting 48 hours the contact is virtually the same as after ~ 200 s contact time. This is the result of the huge contact hysteresis: the elastic deformation energy stored in the compressed asperity contact regions is not large enough to propagate opening cracks around the contact spots, resulting in a time-independent contact area.

From the optical pictures in Fig. 11 it is possible to estimate the relative contact area, but the result depends on the black/white intensity threshold used: threshold = 0.15 gives \( A/A_0 = 0.14 \) after 200 s and 0.28 after 64800 s. If we instead use threshold = 0.2 we get 0.18 and 0.35, respectively, and with the threshold = 0.1 we get 0.085 and 0.20, respectively. In all cases the contact area increases with increasing contact time.

There are two effects which result in an increase in the contact area with increasing time. Assume first that adhesion can be neglected. In this case the contact area will increase only due to the bulk viscoelasticity. Assuming that the contact area is inversely proportional to the relaxation modulus[48, 49] \( E(t) \) (as expected when \( A/A_0 \ll 1 \) and without adhesion), from Fig. 1 we get an increase in the contact area with about a factor of 1.3 which is smaller than we observe in the optical experiments.

To understand the role of adhesion we note first that the asperity contact regions in Fig. 11(a) have diameters of order 30 \( \mu m \) which on the average increases by a factor of ~ 1.4 when going to Fig. 11(b). Thus the closing crack around each asperity contact region must move with the average speed \( v \approx d/t \), where \( d \approx 10 \mu m \).
The nominal contact pressure is approximate 0.097 MPa. (a) The contact after 200 s. (b) The contact after 64800 s (18 hours). The dark regions is contact area. The two bright (white) circular areas arises from two of the four light diodes used to illuminate the contact. From the optical pictures it is possible to estimate the relative contact area, but the result depends on the black/white intensity threshold used: threshold = 0.2 gives $A/A_0 = 0.18$ after 200 s and 0.35 after 64800 s. If we instead use threshold = 0.15 we get 0.14 and 0.28, respectively, and with the threshold = 0.1 we get 0.085 and 0.20, respectively. In all cases the contact area increases with a factor $\approx 2$.

and $t \approx 64800$ s i.e., $v \approx 2 \times 10^{-10}$ m/s. For this velocity, from Fig. 7 we obtain the viscoelastic crack reduction factor $1/[1 + f(v, T)] \approx 0.16$. Thus the effective work of adhesion $\gamma_{\text{close}} \approx 0.16 \Delta \gamma \approx 0.045$ J/m$^2$. Using this value from Fig. 3 we obtain $A/A_0 \approx 0.35$. This estimation is very rough since the opening crack tip does not move with a constant velocity as assumed above, but with a decreasing velocity. Still the estimation shows that the relative contact area estimated by the theory is similar to what is deduced from the optical picture (see Fig. 11).

To estimate more accurately how the contact area depends on the contact time we approximate $w_{\text{open}} = w_0(1 + (v/v_0)\alpha)$. From Fig. 7 in the relevant (low-velocity) region $\alpha \approx 10$. Thus we get $w_{\text{close}} = w_0/(1 + (v/v_0)\alpha) \approx w_0 (v/v_0)^{-\alpha}$. Assuming that each contact region can be treated as a small JKR region, one can show that for long times (or for all times when the nominal contact pressure vanish and $w_{\text{close}} \sim v^{-\alpha}$) the contact area scales with time as $A \sim t^{2/3\alpha}$. When $t$ increase from $t = 200$ s to 64800 s this gives an increase in the contact area with a factor $(64800/200)^{2/3\alpha} \approx 1.5$. Taking into account this and the increase resulting from viscoelastic relaxation (see above) gives a total increase by a factor of $1.5 \times 1.3 \approx 2$ in good agreement with observations (see Fig. 11). Note also that $t^{2/3\alpha} = \exp((2/3\alpha)\log t) \approx 1 + (2/3\alpha)\log t$ as long as $(2/3\alpha)\log t << 1$ so in some intermediate time interval the relation $A/A_0 \sim t^{2/3\alpha}$ is similar to a logarithmic time-dependency.

We have shown above that when strong contact hysteresis occur the work of adhesion and hence the JKR pull-off force is proportional to the normalized area of real contact, $A/A_0$. The contact area increases with the time of stationary contact due to viscoelastic relaxation (see Fig. 1), and (more importantly) due to strengthening of the adhesive interaction with increasing contact time.

The effect of the contact time on the pull-off force is illustrated in Fig. 12 where we show the measured work of adhesion (red squares) as a function of the logarithm of the waiting contact time (see Sec. 5 for the experi-
6 Adhesion: experiments and analysis

In this section we describe the set-up used for our adhesion studies, and present results for the contact between smooth glass and the bromobutyl rubber in dry condition, and when immersed in water and in silicone oil.

6.1 Experimental.

We study the adhesion interaction between spherical silica glass balls \([\text{diameter } 2R = 2.5 \text{ cm (in fluids), and 4 cm or 5 cm (dry state)}]\) and rubber in dry and lubricated condition. We bring the ball into contact with the substrate using a drive which can be represented by a spring (see Fig. 34(b) and Appendix H). The contact region is not observed directly but only the time dependency of the interaction force \(F(t)\), and the displacement \(s(t)\) of the upper part of the driving spring, are measured. The experimental adhesion data are analyzed using the JKR theory (see Appendix E).

The rubber substrate is positioned on a very accurate balance (analytical balance produced by Mettler...
Toledo, model MS104TS/00) which has a reproducibility of 0.1 mg (or \( \approx 1 \) \( \mu \)N) (see Fig. 13). After zeroing the scale of the instrument we can measure the force \( F(t) \) on the substrate as a function of time, which is directly transferred to a computer at a rate of 1 or 10 measurement points per second.

To move the glass ball up and down we use an electric motor coiling up a nylon cord, which is attached to the glass ball. The drive velocity as a function of time can be specified on a computer. In the experiments reported on below the glass ball is repeatedly moved up and down, sometimes for more than 10 contact cycles, involving a measurement time of sometimes more than 24 hours. The maximum loading force is typically \( \sim 0.1 \) N corresponding to the loading mass \( \sim 10 \) gram.

We consider the adhesion between borosilica glass balls and the (carbon black filled) bromobutyl rubber. Here we note that the rubber contains low-molecular weight components, which can migrate (diffuse) from the bulk to the surface. In the experiments we have used rectangular or circular rubber sheets with a diameter of order a few cm, and the thickness \( \approx 2 \) mm. For measurement of adhesion in the dry state the rubber sheets where attached to a flat surface using double sided adhesive tape. For measurements in liquids the rubber sheets where confined at the bottom of a cylindrical PMMA tube using an elastic spring.

We study first the dry rubber-glass contact, where the rubber surface has been cleaned using different procedures. Next we study the adhesion when the system is immersed in water or in silicone oil.

### 6.2 Adhesion for dry condition.

The adhesion experiments consist of several loading-unloading cycles. In the loading phase we lower the glass ball towards the rubber sample with a constant speed \( v_z \). After some fixed displacement, which result in the contact between the glass ball and the rubber (contact force \( \sim 0.1 \) N), we reverse the velocity, and pull-off the glass ball with the same velocity as during approach. As an example, in Fig. 14 we show the interaction force between the glass ball and the rubber compound as a function of time for 4 contact cycles with the drive speed \( v_z = \pm 0.9 \) \( \mu \)m/s. The green line is for bromobutyl cleaned by brushing the surface with soft toothbrush in boiling hot water for about 1 minute. The blue curve is the same procedure followed by lapping the rubber surface for a few second with soft tissue wet by acetone.

Note that the detachments in Fig. 14 occur rather abruptly (in about \( \sim 1 \) s). In fact, for a purely elastic solid and neglecting the detachment time would be zero, but in the present case the detachment time is determined by the velocity dependency of the crack propagation energy.

Fig. 15 shows the work of adhesion during retraction (separation) as a function of the number of contacts. The glass ball was originally cleaned with acetone and the rubber surfaces with acetone (square symbols) or brushed in hot distilled water (stars), or first cleaned in hot water and then with acetone (triangles). Note that in all cases, due to transfer of mobile molecules (e.g. stearic acid) from the rubber surface to the glass surface, the adhesion decreases with the number of contacts.

A decrease in the work of adhesion with increasing number of contact has also been observed in Ref. [50–53] for sapphire and glass balls in contact with silicone rubber. In these cases the reduction in adhesion was attributed to transfer of oligomers from the rubber to the balls.

Fig. 16 shows the result of a second adhesion study performed \( \sim 1/2 \) year after the experiments reported on in Fig. 15, and for a higher the pull-off speed (5 \( \mu \)m/s, as compared to 0.9 \( \mu \)m/s in Fig. 15). In this case the rubber surfaces was cleaned by lapping it for a few second with soft tissue wet by isopropanol. Isopropanol is a “softer” cleaning fluid than acetone, but the results are very similar.

Fig. 7 shows that for the crack tip velocity \( v_t = 5 \) \( \mu \)m/s the viscoelastic enhancement factor for the work of adhesion is \( (1 + f) = 20 \). If we assume a clean glass surface and that only dispersion forces act between the rubber and the glass surface, the adiabatic work of adhesion was estimated in Sec. 2 to be \( \Delta \gamma = 0.1 \) J/m\(^2\), and if we use the contact area \( A_1/A_0 \approx 0.3 \) (see Fig. 3 and Fig. 11) we get the work of adhesion \( w \approx \Delta \gamma (A/A_0)(1 + f) \approx 0.6 \) J/m\(^2\). This is a factor \( \sim 3 \) smaller than what is observed in Fig. 15 and 16 for the first contact with the glass ball. Hence for the clean glass ball the work of adhesion \( \Delta \gamma \approx 0.3 \) J/m\(^2\). This is larger than expected in the adiabatic limit if only dispersion forces act between the rubber and the glass surface (see Sec. 2), and shows that some other types of stronger bonds form between the clean glass and rubber surfaces. However, after the glass surface is contaminated the work of adhesion drop to \( \approx 0.6 \) J/m\(^2\) and at this point the dispersion forces may give the dominant contribution to the work of adhesion.

### 6.3 Adhesion in water.

We have performed adhesion experiments with the glass ball and rubber immersed in water and in silicone oil. Fig. 17 shows the experimental set-up. The fluid is located in a PMMA container (inner diameter 4 cm) with a PMMA cover to avoid evaporation of the fluid. The top cover has a small hole (diameter 1 mm) through which the nylon rope (diameter 0.3 mm), used for moving the glass ball, passes. The rubber sheet is located at the bottom of the container. The glass ball (diameter \( 2R = 2.5 \) cm, with a flattened top part) is fully immersed in the fluid during the contact cycling. The container is located on a sensitive laboratory balance used for measuring the pull-off force.

Fig. 18 shows the work of adhesion during retraction...
FIG. 17: Experimental set-up for adhesion studies in fluids (in this case in silicone oil). The fluid is located in a PMMA container (inner diameter 4 cm) with a PMMA's cover to avoid evaporation of the fluid. The top cover has a small hole (diameter 1 mm) through which the nylon rope (diameter 0.3 mm), used for moving the glass ball, passes. The rubber sheet (in this case a carbon filled bromobutyl rubber sheet) is located at the bottom of the container. The glass ball (diameter 2.5 cm, with a flattened top part) is fully immersed in the fluid during the contact cycling. The container is located on a sensitive laboratory balance used for measuring the pull-off force.

FIG. 18: The work of adhesion during retraction (separation) as a function of the number of contacts between the glass ball (diameter $2R = 2.5$ cm) and the bromobutyl rubber in water. The glass ball was originally and rubber cleaned with acetone and isopropanol. The rubber surface was cleaned with isopropanol.

FIG. 19: The work of adhesion during retraction (separation) as a function of the contact time between the glass ball and the bromobutyl surface in water. The glass ball was originally cleaned with acetone and isopropanol. The rubber surface was cleaned with isopropanol.

FIG. 20: Optical picture of the contact between a flat glass plate and a rectangular rubber block squeezed together in water. Note the granular structure which result from the rubber surface roughness. For the glass-rubber contact fully immersed in water we cannot detect any time-dependent changes in the optical pictures. This is due to the rapid fluid squeeze-out, and the fact that in the optical pictures the rubber-glass contact regions where the surfaces are separated by, say, 1 nm of water, looks the same as when the rubber is in direct contact with the glass.

much smaller than for the dry contact (Fig. 15 and 16). Thus there appear to be a strong reduction in the transfer of molecules from the rubber to the glass surface when the contact is in water as compared to the dry contact. Fig. 19 shows the work of adhesion during retraction (separation) as a function of the contact time between the glass ball and the rubber surface. Note the huge increase in the work of adhesion with increasing contact time. This increase is much stronger than observed for dry surfaces, where the work of adhesion increased with...
a factor of $\sim 1.5$ as time increase from $10^3$ s to $10^5$ s (see Fig. 12). In the present case the increase in the same time interval is a factor of $\sim 5$. We interpret this as resulting from (slow) thermally activated dewetting transitions in the asperity contact regions. We have seen in Sec. 3 that continuum mechanics calculations for the contact between the glass ball and the rubber in water predict that already after $\sim 1$ s the water is squeezed out from the asperity contact regions, and the contact area and the interfacial separation become time independent. This is also consistent with optical pictures of the contact in water where the contact looks the same after $\sim 10$ hours as compared to $\sim 100$ s contact time. However, we believe that there is a very thin (of order nanometer) water film between the rubber asperities and the glass surface, which only very slowly is removed by the nucleation of dry rubber-glass surface areas (dewetting transitions). Only by assuming this is it possible to explain the observed strong increase in the work of adhesion with increasing contact time (see Fig. 19).

We have argued in Sec. 2 that the interaction potential between rubber and the glass surface in water has the form shown in Fig. 31. At short separation the interaction potential has a local minimum corresponding to direct contact between the rubber and the glass surface. In this case bonding forces (of unknown nature), stronger than the dispersion forces, occur between the surfaces. When a bromobutyl rubber is squeezed in contact with glass surface in water we expect first a rapid squeeze-out (see Sec. 3) until contact occur between the rubber asperities and the glass surface. However, at short contact time we do not expect any true atomic contact between the rubber and the glass surface but a water film of nanometer thickness separate the surfaces in the asperity contact regions. However, this state is metastable and after a long enough time we expect true atomic contact to form between the rubber and the glass surface in the asperity contact regions. This dewetting process involves the nucleation (by thermal fluctuations) of nanometer sized contact region followed by the removal of the nanometer water film by a (mainly) surface-energy driven squeeze-out process. Thus we expect the contact area between the rubber and the glass surface to increase continuously with increasing contact time, which is consistent with the observed increase in the work of adhesion with increasing contact time (see Fig. 19). We note, however, that optical pictures of the glass-rubber contact in water does not show any time-dependent changes. This is due to the fast fluid squeeze-out, and to the limitation of our optical microscope. Thus, with our optical set-up, if the rubber-glass surfaces are separated by thin fluid film, say, 1 nm of water, it may appear the same as for direct rubber-glass contact.

Fig. 20 shows an optical picture of the contact between the glass and rubber surface squeezed together in water. Note the granular structure which must be caused by the rubber surface roughness. Similar pictures obtained after different contact time (not shown) looks the same.

Fig. 21 shows an optical picture of a small water droplet squeezed between the glass and rubber surface. Both dry and wet regions can be observed. When the normal load is slowly increased, the fluid covered region increases in size via small local (rapid) expansions of the wet area, followed by time periods where no change occur in the line boundary separating the water covered and the dry surface area. We interpret this as a Laplace-pressure effects, where the water pressure locally must become high enough to overcome surface-energy derived energetic barriers associated with narrow constrictions in the non-contact fluid flow channels. These energy barriers could be important for the fluid flow at the interface in leakage experiments when a small applied fluid pressure difference occur between the two sides in a seal (see Ref. [12, 54]).

Note that if the water is completely removed from some rubber-glass contact regions during the loading phase, during pull-off, because of the strong adhesion hysteresis, the effective work of adhesion may be large. When strong contact hysteresis occur we have shown in Sec. 5 that $w = \gamma_{\text{open}}(v)A/A_0$. The large magnitude of $\gamma_{\text{open}}(v) = \Delta \gamma(1 + f)$ imply that the relative contact area $A_1/A_0$ must be very small for the contact in water for short contact times. Thus using $\gamma_{\text{open}}(v) \approx 1$ J/m$^2$ and $w = 0.01$ J/m$^2$ as observed for very short contact time (about 200 s) we get $A/A_0 \approx 0.01$ as compared to $A/A_0 = 0.3$ for the dry contact case. However, the relative contact area increases monotonically due to dewetting in the asperity contact regions and for $t \approx 10^5$ s from Fig. 19 we have $w \approx 0.1$ J/m$^2$ and hence $A/A_0 \approx 0.1$.

On contact formation (approach) in water (and in silicon oil) no adhesion can be detected, while during pull-off we always observe adhesion.
6.4 Adhesion in silicone oil.

We have performed two sets of experiments involving silicone oil. In one experiment the rubber and the glass ball was covered with thin films (thickness $d$) of silicone oil. In this case we observed adhesion due to formation of a capillary bridge (see Appendix G). In the second set of experiments, which we report on here, the glass ball and the rubber sample is fully immersed in the silicone oil.

Fig. 22 shows the work of adhesion as a function of the contact number between the glass ball and the bromobutyl rubber immersed in silicone oil (viscosity 0.35 Pas). Results are shown for the pull-off speeds 0.9 $\mu$m/s (yellow squares), 0.9 $\mu$m/s (red squares), 1.75 $\mu$m/s (green squares), 6.3 $\mu$m/s (black squares) and 35 $\mu$m/s (blue squares).

![FIG. 22: The work of adhesion as a function of the contact number for the glass ball and the bromobutyl rubber immersed in silicone oil (viscosity 0.35 Pas). Results are shown for the pull-off speeds 0.7 $\mu$m/s (yellow squares), 0.9 $\mu$m/s (red squares), 1.75 $\mu$m/s (green squares), 6.3 $\mu$m/s (black squares) and 35 $\mu$m/s (blue squares).](image)

For pull-off in the dry state and in water we observed very rapid detachment transition involving a transition time of order $\sim 1$ s. For the system immersed in silicone oil the detachment transition occur over much longer time period. This is illustrated in Fig. 23 which shows the interaction force as a function of time close to a detachment for (a) dry surfaces, (b) in water and (c) in silicone oil (viscosity 0.35 Pas). The drive speed is $v_z = 0.9$ $\mu$m/s in (a) and (b) and 1.8 $\mu$m/s in (c). In (c) we have superimposed (by shifting along the time axis) 4 different pull-off events indicated by the different symbols. The green line in (c) is the theory prediction for the interaction force assuming only a viscous drag force (see Appendix J), with the initial (at $F = 0$) surface separation $u_0 = 1.4$ $\mu$m.

![FIG. 23: The interaction force between the glass ball and the rubber as a function of time close to a detachment for (a) dry surfaces, (b) in water and (c) in silicone oil (viscosity 0.35 Pas). The drive speed is $v_z = 0.9$ $\mu$m/s in (a) and (b) and 1.8 $\mu$m/s in (c). In (c) we have superimposed (by shifting along the time axis) 4 different pull-off events indicated by the different symbols. The green line in (c) is the theory prediction for the interaction force assuming only a viscous drag force (see Appendix J).](image)
the contact. In this case we found that using ball in contact with the rubber for 7200 s before removing this is considerably smaller than 1

the rubber, and hence to a smaller stronger adhesive interaction between the glass ball and the clean glass ball the longer contact time result in a

out the waiting time period. This is in accordance with the results obtained in Sec. 6.5, where we found that for a glass ball with baked-on silicone oil obtained using procedure 1 (pink filled circles). For contact between glass balls with diameter 2R = 2.5 cm and the bromobutyl rubber in silicone oil (viscosity 0.35 Pas). The pull-off velocity v = 6.28 µm/s. The numbers 1-3 for the “clean” glass balls indicate the time-order of the measurements where increasing number correspond to later measurement during a total time interval of ~ 5 month. During the waiting time the glass balls was immersed in silicone oil.

In Appendix J we show that the average surface separation u when F = 0 decreases as the pull-off speed decreases. Thus we find u = 1.8, 1.65 and 1.4 µm for v = 35, 6.3 and 1.75 µm/s, respectively. We interpret this as resulting from the longer glass-rubber contact time at the lower approach and pull-off speed (the contact time is proportional to 1/v).

As a further test we performed another experiment with the pull-off velocity 6.3 µm/s where we kept the ball in contact with the rubber for 7200 s before removing the contact. In this case we found that using u = 1.3 µm gives good agreement with the experiment, see Fig. 42. This is considerably smaller than 1.65 µm found without the waiting time period. This is in accordance with the results obtained in Sec. 6.5, where we found that for the clean glass ball the longer contact time result in a stronger adhesive interaction between the glass ball and the rubber, and hence to a smaller u.

Here we also note that for the rubber-ball contact in water, which exhibit a similar work of adhesion as in silicone oil, optical microscope pictures of the rubber-ball contact does not show any change when the loading force change from its maximum to zero. This again indicate that the energy to propagate the opening crack (at relevant speeds) is so large that the compressed asperities cannot reduce the contact area during unloading.

6.5 On the dependency of the pull-off force on the contact time in silicone oil.

In Sec. 6.4 we showed that the pull-off force for the contact of the glass ball and the rubber in water increases strongly with increasing time of contact. We interpreted this as resulting from a slow (thermally activated) dewetting process, where a nanometer water film is removed from the asperity contact regions. Here we study the same for the contact in silicone oil for bare glass and for glass passivated by baked-on silicone oil.
Glass surfaces with baked-on silicone oil exhibit low friction and low adhesion against rubber. In our case the glass balls was first cleaned by ultrasonic in purified water. Baked-on siliconisation involves the application of silicone oil (usually as an emulsion) on a glass surface, which then is baked on to the glass surface at a specific temperature and for a specific time period. We use an aqueous siliconization emulsion that contain 35% Dow Corning 360 Medical Fluid, 350 sSt (see Ref. [55]). The silicone oil emulsion is sprayed on the glass ball.

In the baked-on process, hydrogen and covalent bonds form between the glass surface and the polydimethylsiloxane chains (see Fig. 24). This result in a very inert and hydrophobic coating, where the bonds are so strong that the attached polydimethylsiloxane chains cannot be removed with solvent.

One set of balls was baked at $T = 300^\circ$C for 20 minutes (procedure 1) according to the standard industrial procedure for siliconisation of glass surfaces. Another set of balls was baked at $T = 150^\circ$C for 1 hour (procedure 2). In this latter case the balls where cleaned prior to the baking by exposing the glass balls to oxygen plasma.

Fig. 25 show the work of adhesion as a function of the logarithm of the waiting time for a “clean” glass ball (red stars), and for glass balls baked in silicone oil using procedure 1 (filled circles), and procedure 2 (open circles). The glass balls was removed with the speed $v_z = 6.28 \mu$m/s.

For short times all the glass balls give similar effective work of adhesion. We interpret this (see also above and Appendix H) as due mainly to the viscous drag which is the same in all cases. Thus, we expect the surfaces in most of the asperity contact regions to be separated by one or several monolayers of silicone oil molecules. We note, however, that the adhesion must be present since otherwise the (average) interfacial separation when the force is reduced to zero, $F = 0$, would be so large as to give much smaller viscous pull-off forces than observed (see Appendix F).

In some cases the work of adhesion for times $t > 10^4$ s increases very rapidly. This may involve dewetting transitions where the silicone oil is completely removed from some asperity contact regions. This is most likely a thermally activated process and needs long times to occur.

The numbers 1-3 for the “clean” glass balls indicates the time-order of the measurements, where increasing number corresponds to the later measurement during a total time interval of $\sim 5$ month. During the waiting time the glass balls was immersed in silicone oil. Clearly some type of (thermally activated) aging has occurred, which has resulted in a decrease in the adhesive force with increasing time in contact with the oil. We attribute this to an increasing passivisation of the glass surface involving processes similar to what is shown in Fig. 24. Experiments performed with new rubber and new silicone oil after long waiting time gives very low work of adhesion indicate that the “aging” probably relates to passivisation of the glass ball.

Note in Fig. 25 the strong increase in $w$ for waiting times $t > 10^4$ s for the (original) clean glass ball during the first test (denoted 1). This agrees with the time dependency of the breakloose friction force for syringes with glass barrel, where the contact between the rubber stopper and the glass is lubricated with silicone oil with similar viscosity as used above (see Ref. [13]). In Ref. [13] it was suggested that the increase in the breakloose friction force is associated with a dewetting transition.

Fig. 26 shows the work of adhesion as a function of the logarithm of the waiting time for $v_z = 0.87 \mu$m/s. Again the work of adhesion does not depend on the contact time and is roughly a factor of 2 smaller than for the higher pull-off speed used in Fig. 25. This reduction in the work of adhesion (or rather the pull-off force) is however much smaller than what would be expected if the pull-off force would be determined by the viscosity of the fluid since the velocity is reduced by a factor 0.87/6.28 = 0.14. We attribute this to an adhesion-induced reduction in the average interfacial separation $u_0$ (at the time when $F = 0$) due to the longer contact time at the lower pull-off speed.

7 Summary and conclusion

Adhesive systems of glass in contact with filled brombutyl rubber in dry condition, in water and in silicone oil have been experimentally investigated. The experimental results have been analyzed taking into consideration the interplay between the viscoelastic energy dissipation at the contact crack tip and surface roughness, and capillary effects and viscous drag in case of liquid environments. Adhesion hysteresis has been found both in pull-off force tests and supported by optical contact observation, which manifests itself as a strong dependence of the pull-off force (and effective work of adhesion) on the maximum loading force and contact time. For the systems with liquid environment much weaker adhesion has been observed compared to the dry case. However, the adhesion in liquid is significantly increased with contact time (contact aging) which can be explained by expelling the liquid from the contact region (dewetting transition). Since the latter can be practically important adverse effect for the silicone-oil lubricated devices, it has been here shown that glass surface can be protected against the contact aging by siliconisation process prior to the adhesive contact.

To summarize, the most important results of our study are:

(a) For the brombutyl rubber in contact with a clean glass surface we observe huge contact hysteresis, where the contact area remains unchanged as the external loading force (or squeezing pressure) is removed. We have shown that the contact hysteresis is mainly due to the rubber viscoelasticity, which result in an interfacial crack...
propagation energy which is much larger for an opening crack than for a closing crack.

(b) For dry rubber–glass contact we have shown that the contact area increases slowly with time due to viscoelastic creep and, more importantly, due to the time-dependency of adhesion (which is due to the velocity dependency of closing crack propagation). We have shown that the increase in the contact area manifest itself as an increase in the work of adhesion during pull-off.

(c) For rubber in contact with glass in water we observe a very strong increase in the adhesion with increasing contact time which we interpret as due to (thermally activated) dewetting transitions in the rubber–glass asperity contact regions. We have shown that the increase in the contact area manifest itself as an increase in the work of adhesion during pull-off.

(d) For the adhesion between the rubber and siliconised glass in silicone oil we observe a very small work of adhesion, which is nearly independent of the contact time. This shows the stable and inert nature of the layer of silicone oil molecules chemically attached to the glass surface.

(e) For the pull-off force depend on the oil viscosity, while for water this viscous contribution to the pull-off force is negligible for the pull-off velocities used in our study. (f) We find that in silicone oil the pull-off force depend on the oil viscosity, while for water this viscous contribution to the pull-off force is negligible for the pull-off velocities used in our study. We have developed a simple theory which describe the influence of the fluid viscosity on the pull-off force.

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Appendix A: Viscoelastic modulus

In this section we present the results for the viscoelastic properties for the filled bromobutyl rubber compound used in the adhesion studies. We used a Q800 Dynamic Mechanical Analysis (DMA) instrument produced by TA Instruments. The machine is run in tension mode, meaning that a rectangular strip of rubber clamped on both sides, is elongated in an oscillatory manner. The complex viscoelastic modulus is first measured in constant strain mode with a strain amplitude of 0.04% strain and at different frequencies. The results are shown in Fig. 27, where the real part ReE and the imaginary part ImE of the rubber viscoelastic modulus, and the ratio ImE/ReE as a function of the frequency ω experimentally measured at 0.04% strain amplitude and combined as master curves refer for the reference temperature $T_{ref} = 20^\circ C$.

FIG. 27: The (a) real part ReE and (b) the imaginary part ImE of the rubber viscoelastic modulus, and the ratio ImE/ReE as a function of the frequency ω experimentally measured at 0.04% strain amplitude and combined as master curves refer for the reference temperature $T_{ref} = 20^\circ C$.

FIG. 28: The horizontal shift factors, $a_T$, as a function of the temperature after the measurements performed at 0.04% strain amplitude and the shift factors for the reference temperature $T_{ref} = 20^\circ C$. 

$\log_{10} a_T$ temperature (°C)

$\log_{10} a_T$ temperature (°C)
different frequencies starting from 28 Hz and changed in steps until 0.25 Hz is reached (10 frequency points: 28.0, 25.0, 14.0, 7.9, 4.4, 2.5, 1.4, 0.79, 0.44, and 0.25 Hz). The rather small strain amplitude is chosen in order to avoid strain softening effects, e.g., the Mullins effect [56] or the Payne effect [57], which can strongly change the viscoelastic response of the rubber specimen. It is not clear how these nonlinear effects would affect the results at different temperatures, and one therefore usually measure the low strain master curve in the linear response region. From our previous experience we have found that a strain amplitude of 0.04% is reasonable good for most rubber compounds. Measuring the rubber sample in tension mode also requires to prestrain the rubber with a static strain that has to be larger then the dynamic strain during oscillation. The prestrain in the experiments has been set to 0.06% to avoid compressing the rubber during the DMA measurement.

The experiment started at −80°C and after measuring the modulus at all frequencies mentioned above, the temperature was increased in steps by 5°C, and the procedure was repeated until 120°C is reached. Note that it might be necessary to choose smaller temperature steps when reaching the glass transition temperature $T_g$ where the viscoelastic response of the rubber material changes strongly with frequency (and temperature). This makes sure that the curves measured at different temperatures overlap with each other, which is necessary for the shift procedure to be accurate. The results are then shifted in order to form a smooth $ReE$ master curve.

Fig. 27 shows the (a) real part $ReE$ and the imaginary part $ImE$ of the rubber viscoelastic modulus, and (b) the ratio $ImE/ReE$ as a function of the frequency $\omega$. The measurements were performed at 0.04% strain amplitude and the master curves refer to the temperature $T_{ref} = 20°C$. Fig. 28 shows the horizontal shift factors, $a_T$, as a function of the temperature.

If we define the glass transition temperature $T_g$ as the temperature where $\tan\delta = ImE/ReE$ as a function of temperature is maximal (for the frequency $\omega = 0.01$ s$^{-1}$), then we obtain $T_g = −62°C$.

In the asperity contact regions between the rubber and the glass ball the strain is usually very high, up to $\sim 1$ (where the strain $\epsilon = 1$ correspond to 100% strain). To take into account this we have performed strain sweep up to very large strain $\epsilon = 1$. Fig. 29 shows the ratio $ImE(\epsilon)/ImE(0)$ and $ReE(\epsilon)/ReE(0)$ as a function of the strain. The curves shown are polynomial fit curves to the average over measurements performed at $T = −20°C$, 0°C and 20°C.

**Appendix B: Contact angles and surface energies.**

We have measured the advancing $\theta_A$, and receding $\theta_R$ contact angles for water and silicone oil on the glass ball surface and on the surface of the bromobutyl rubber and estimated the adiabatic work of adhesion between the
rubber and the glass surface, in the dry state, in water and in silicone oil.

A small droplet of silicon oil deposited on the rubber or glass surface very quickly spread out into a pancake like structure the diameter of which increased with time. Thus, \( \theta_\text{A} = 0 \) (complete wetting) for silicon oil on both the glass and the rubber surface. It follows that the thermal equilibrium contact angle \( \theta_\text{c} = 0 \).

For water the measurements was performed by depositing a small water droplet on the rubber or glass surface (see Fig. 30). The advancing contact angle was determined after waiting \( \sim 1 \) minute at which point no movement of the contact line could be detected. The receding contact angle was determined by studying the water droplet during evaporation of the water. When enough water had evaporated the contact line started to move inwards and at this point we measured the receding contact angle. We performed 4 different experiments for (a) a glass ball cleaned with acetone, (b) the bromobutyl rubber surface cleaned with acetone, (c) a contaminated glass ball surface, which was first cleaned with acetone and then (\( \sim 10 \) times) squeezed in contact with the rubber, and (d) the same as (c) but with the rubber-glass squeezed contact in water. We give the advancing \( \theta_\text{A} \), retracting \( \theta_\text{R} \) and (calculated) thermal equilibrium contact angle \( \theta_\text{c} \).

<table>
<thead>
<tr>
<th>System</th>
<th>( \theta_\text{A} )</th>
<th>( \theta_\text{R} )</th>
<th>( \theta_\text{c} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>(a) Glass</td>
<td>26.8</td>
<td>3.0</td>
<td>15.3</td>
</tr>
<tr>
<td>(b) Rubber</td>
<td>92.5</td>
<td>26.5</td>
<td>55.9</td>
</tr>
<tr>
<td>(c) Contaminated Glass</td>
<td>56.0</td>
<td>3.5</td>
<td>28.5</td>
</tr>
<tr>
<td>(d) Contaminated Glass</td>
<td>33.0</td>
<td>4.0</td>
<td>19.0</td>
</tr>
</tbody>
</table>

The calculated thermal equilibrium contact angle \( \theta_\text{c} \) are also given in Table 1.

Note that after contact with the rubber, the water contact angle on the glass ball has increased. We interpret this as resulting from transfer of uncrosslinked molecules from the rubber to the glass ball. When the contact between the rubber and the glass surface occurred in water, the change in the water contact angle is much smaller. We conclude that less molecules are transferred to the glass surface when the rubber-glass contact occur in water as compared to in the dry state. As will be shown in Sec. 6, the transfer of molecules to the glass surface when in contact with the rubber result in an adhesion force between the two solids which decreases with increasing number of contacts cycles.

We also performed additional measurements of the water advancing contact angles on another (namely identical) glass ball. The ball were first cleaned with acetone. Next, the ball was squeezed in contact with the rubber which gave the water advancing contact angle 42°.

Let us estimate \( \Delta \gamma \) for the contact between the bromobutyl rubber and the glass surface. The surface energy (per unit surface area) for glass cleaned with acetone which results in a surface still covered by water and some (strongly bounded) organic contamination, is typically \( \gamma_1 \approx 0.06 - 0.07 \) J/m². The surface energy for bromobutyl rubber is \( \gamma_2 \approx 0.025 - 0.035 \) J/m².

In a simple approach, if only dispersion forces are responsible for the interaction between the glass and the bromobutyl rubber, the adiabatic work of adhesion is approximately given by \( \Delta \gamma \approx 2 (\gamma_1 \gamma_2)^{1/2} \), which in the present case gives \( \Delta \gamma \approx 0.08 - 0.1 \) J/m². However, the experimental adhesion study presented below indicates that stronger bonds form between the two surfaces and \( \Delta \gamma \approx 0.3 \) J/m².

In a liquid the adiabatic work of adhesion can be calculated using the Young-Dupre equation (1). The liquid surface tension \( \gamma \approx 0.072 \) J/m² for water and for silicone oil \( \gamma \approx 0.02 \) J/m².

Let us now estimate the adiabatic work of adhesion between bromobutyl rubber and the glass surface in water. As shown above, the adiabatic contact angle between water and the glass ball (cleaned by acetone) and the bromobutyl rubber (also cleaned by acetone) are \( \theta_{31} \approx 15° \) and \( \theta_{31} \approx 56° \), respectively. Assuming first only dispersion interaction \( \Delta \gamma \approx 2 (\gamma_1 \gamma_2)^{1/2} \approx 0.09 \) J/m² from (1) we get \( \Delta \gamma \approx 0.02 \) J/m². Hence in this case we obtain that \( \Delta \gamma \) is negative which imply no adhesion but a short ranged repulsion. However, as stated above, the adhesion studies presented below (see Sec. 6) shows that \( \Delta \gamma \approx 0.3 \) J/m² giving \( \Delta \gamma \approx 0.2 \) J/m².

The negative work of adhesion predicted above is due to the dispersion force (i.e., the Van der Waals interaction), which acts between the surfaces (in a modified form) also when a thin (nanometer) water film exist be-
FIG. 31: The interaction potential between a flat glass surface and a flat rubber surface in water as a function of the surface separation. At separation of order a few nanometer the interaction is only via dispersion forces and steric repulsion and is repulsive. At short separation the interaction potential has a minimum corresponding to direct contact between the rubber and the glass surface. In this case stronger bonding forces (of unknown nature) stronger than the dispersion forces occur between the surfaces. Arbitrary units and schematic.

For silicone oil the adiabatic contact angles $\theta_{gl} \approx 0^\circ$ on glass and $\theta_{rl} \approx 0^\circ$ on rubber. When one (or both) of the contact angles vanish it is not possible to use (1) to estimate the work of adhesion in the liquid, but this equation can only be used to give an upper limit for the work of adhesion. Thus, using $\Delta \gamma (\text{dry}) \approx 0.3 \text{ J/m}^2$, (1) gives $\Delta \gamma (\text{wet}) < 0.25 \text{ J/m}^2$. The adhesion measurements to be presented in Sec. 6 indicate an initially very weak adhesion in silicone oil and in water, which increases with increasing time of contact.

Appendix C: rubber surface power spectrum

We have studied the rubber surface topography using an optical method and atomic force microscopy (AFM). As shown in Fig. 32 the height probability distribution is nearly Gaussian. Fig. 33 shows the surface roughness power spectrum as a function of the wavenumber on the logarithmic scale. The green lines are from optical data and the red lines from atomic force microscopy (AFM) data. The dashed line is a fit to the data where the tilted line has a slope corresponding to the Hurst exponent $H = 0.92$ (or fractal dimension $D_f = 2.08$).

For silicone oil the adiabatic contact angles $\theta_{gl} \approx 0^\circ$ on glass and $\theta_{rl} \approx 0^\circ$ on rubber. When one (or both) of the contact angles vanish it is not possible to use (1) to estimate the work of adhesion in the liquid, but this equation can only be used to give an upper limit for the work of adhesion. Thus, using $\Delta \gamma (\text{dry}) \approx 0.3 \text{ J/m}^2$, (1) gives $\Delta \gamma (\text{wet}) < 0.25 \text{ J/m}^2$. The adhesion measurements to be presented in Sec. 6 indicate an initially very weak adhesion in silicone oil and in water, which increases with increasing time of contact.

FIG. 32: The height probability distribution for the bromobutyl rubber surface as obtained from optical measured topography. The red and green lines are from two different surface areas.

FIG. 33: The surface roughness power spectrum of the bromobutyl rubber surface as a function of the wavenumber (log-log scale). The green lines are from optical data and the red lines from atomic force microscopy (AFM) data. The dashed line is a fit to the data where the tilted line has a slope corresponding to the Hurst exponent $H = 0.92$ (or fractal dimension $D_f = 2.08$).

Appendix D: Interfacial crack propagation

The contact line between a spherical probe and a rubber substrate can be considered as a crack tip and the work of adhesion equal the crack propagation energy per unit surface area $w$. It is well known that the crack propagation energy depends on the crack tip velocity $v$ and on the temperature $T$, i.e. $w = w(v, T)$. In addition it

responding to the Hurst exponent $H = 0.92$ (or fractal dimension $D_f = 2.08$). In the calculations below we use the dashed line linearly (on the logarithmic scale) extrapolated to $q = q_1 = 10^9 \text{ m}^{-1}$. This power spectrum correspond to a surface with the rms-slope 0.55 and rms-roughness 2.9 $\mu$m.
differ for a closing crack and an opening crack.

The crack propagation energy for an opening crack is often written as\cite{31, 65–68}:

\[ \gamma_{\text{open}}(v, T) = \Delta \gamma \left[ 1 + f(v, T) \right]. \quad (A1) \]

Here we are interested in interfacial (between the glass ball and the rubber substrate) crack propagation. In this case, as the crack velocity \( v_r \to 0 \) (when viscous effects in the rubber are negligible), the measured value of \( \Delta \gamma \) can be identified as the energy \( \Delta \gamma = \gamma_1 + \gamma_2 - \gamma_{12} \) needed to break the interfacial rubber-substrate bonds, which are usually of the van der Waals type.

For simple hydrocarbon elastomers, the effect of temperature can be completely accounted for by applying a simple multiplying factor, denoted by \( \alpha_T \), to the crack velocity \( v \), i.e., \( f(v, T) = f(\alpha_T v) \). Moreover, values of \( \alpha_T \) found experimentally are equal to the Williams–Landel–Ferry (WLF)\cite{69} function determined from the temperature dependence of the bulk viscoelastic modulus. This clearly proves that the large effects of crack velocity and temperature on crack propagation in rubber materials are due to viscoelastic processes in the bulk.

In (A1) the function \( f(v, T) = f(\alpha_T v) \) describes the bulk viscoelastic energy dissipation in front of the crack tip. This term is determined by the viscoelastic modulus \( E(\omega) \) of the rubber, and can be calculated theoretically. The factor \( \Delta \gamma \) is due to the bond breaking (in our applications between the rubber and the substrate) at the crack tip (in the so called crack-tip process zone), which may involve highly non-linear processes. This term cannot be easily calculated theoretically, and must be deduced directly from experimental data.

In Ref.\cite{31, 32} we have shown that

\[ \gamma_{\text{open}}(v) = \Delta \gamma \left[ 1 + \frac{2}{\pi} E_0 \int_0^{2\pi v/a} d\omega \frac{F(\omega)}{\omega} \text{Im} \frac{1}{E(\omega)} \right]^{1/2}, \quad (A2) \]

where \( E_0 = E(0) \) and where

\[ F(\omega) = \left[ 1 - \left( \frac{\omega \nu}{2 \pi v} \right)^2 \right]^{1/2}. \quad (A3) \]

The crack tip radius \( a = a(v) \) depends on the crack-tip velocity \( v \) (and temperature), and can be determined if one assumes that the stress at the crack tip takes some critical value \( \sigma_c \). This gives

\[ \frac{a}{a_0} = \frac{\gamma_{\text{open}}}{\Delta \gamma}, \quad (A4) \]

where \( a_0 \) is the crack-tip radius for a very slowly moving crack. Note that the critical stress \( \sigma_c \) only enter in the adiabatic work of adhesion \( w_0 = 2\pi \sigma_c^2 a_0 / E(0) \), and is therefore not an independent parameter. For high crack tip velocities \( \gamma_{\text{open}}(v) \approx \Delta \gamma E(\infty) / E(0) \gg \Delta \gamma \). This is possible only if the denominator in the integral in (A2) is close to zero for high crack tip velocities which means that the term involving the integral must be close to unity. If (A2) is used directly to calculate \( \gamma_{\text{open}}(v) \) numerically this requires that \( E(\omega) \) is accurately known for all frequencies, which is usually not the case. However, it is possible to rewrite (A2) in a form convenient for numerical calculations\cite{32}. The predictions of the crack propagation theory presented above was compared to experimental data in Ref.\cite{31, 32, 70, 71}. Note that for rubber materials \( E(\infty) / E(0) \) is typically \( \sim 1000 \), so factor \( f(v, T) \) in (A1) may enhance \( w \) by a factor \( \sim 1000 \) (or more) at high crack tip velocities.

\textbf{Appendix E: Short review of the JKR theory}

The contact region between a spherical probe (radius \( R \)) and a flat rubber surface is circular with the radius \( r \). In the JKR theory, the interaction between the solids is described by the work of adhesion \( w \), which is the energy per unit surface area to separate two flat surfaces from their equilibrium contact position to infinite separation. According to the JKR theory the relation between the interaction force \( F \), and the radius \( r \) on the stable branch of the interaction curve is\cite{15, 16}

\[ r^3 = \frac{3RF_c}{4E^*} \left[ \frac{F}{F_c} + 2 + 2 \left( \frac{F}{F_c} + 1 \right)^{1/2} \right], \quad (B1) \]

where \( E^* = E/(1 - \nu^2) \) (where \( E \) and \( \nu \) are the rubber Young’s modulus and Poisson ratio, respectively), and where

\[ F_c = \frac{3\pi}{2} wR, \quad (B2) \]
is the pull-off force. Thus for an elastic solid, if the ball is pulled by a soft spring (and neglecting inertia effects), at \( F = -F_c \) the pull-off force abruptly drop to zero.

It is well known that the the separation line \( r = r(t) \) can be considered as a crack tip\[68, 72\]. The work of adhesion \( \gamma_{\text{open}} \) in general depends on the velocity \( v_r = \dot{r} \) of the opening (during pull-off) or closing (during contact formation) crack tip. At finite crack tip velocity, for an opening crack \( \gamma_{\text{open}} \) can be strongly enhanced (and for a closing crack \( \gamma_{\text{close}} \) strongly reduced), compared to the adiabatic (infinitely low crack tip velocity) value \( \Delta \gamma \). One contribution to the work of adhesion is derived from the viscoelastic energy dissipation in the vicinity of the crack tip (see Fig. 34(a)). For an opening crack this will enhance \( w \) with a factor \( 1 + f(v_r, T) \), which depend on the crack tip velocity \( v_r \) and the temperature \( T \). For a closing crack the corresponding reduction factor is approximately\[73\] \( 1/\left[1 + f(v_r, T)\right] \).

Since the work of adhesion depends on the crack tip velocity \( v_r = \dot{r}(t) \) we need to determine this quantity. In the experiments we calculate \( v_r \) from the time dependency of \( F(t) \) assuming that the JKR theory is valid. Thus using (B1) we can obtain \( r(t) \) from the measured \( F(t) \). During pull-off the velocity \( v_r \) varies with time, but what is most important is the velocity at the point when the pull-off force is maximal; this is the crack tip velocity quoted below.

In two earlier publications\[46, 50\] we have, for rubber materials, tested the JKR theory predictions above using another set-up where \( r(t) \) was measured directly using an optical microscopy. We found good agreement between the experiments and the JKR theory prediction. Thus, in analyzing the experiments presented below we have obtained \( v_r \) from the time dependency of the interaction force \( F(t) \) using (B1).

### Appendix F: Interfacial separation without adhesion

Contact mechanics in presence of interfacial fluid is a complex problem \[45\], and here we only employ a simple model for how the interfacial separation vary with time when the loading force is reduced from its maximum value to zero for the ball-rubber contact in silicone oil. The pull-off during the time period when \( F(t) < 0 \) will be studied in Appendix II and I. We assume first that there is no adhesion at the interface. Let \( t = 0 \) correspond to the time when we start to pull-off the ball and assume the interaction force \( F(t) = (1 - t/t_0) F_0 \) where \( F_0 \) is the maximum of the loading force, usually on order 0.1 N, and \( t_0 \) the time necessary to reduce the force to zero which depend on the pull-off velocity \( v_r \), but which is typically 100 - 1000 s. As shown in Sec. 3 during the loading phase (see green curve in Fig. 6(a)) for loading times larger than 10 s the average interfacial separation is not influenced by the fluid but is determined by the interaction between the glass surface and the rubber asperities. Thus we will assume that at \( t = 0 \) (start of pull-off) the (average) interfacial separation \( u = u_0 \) takes the value expected for static loading without the fluid. We will now study how \( u(t) \) increases as the force \( F(t) \) decreases linearly towards zero assuming that \( u(t = 0) = u_0 \).

When the loading force is maximal the Hertz contact between the glass ball and the rubber surface is circular with radius \( r_0 \) and the average contact pressure \( p_0 = F_0/(\pi r_0^2) \). We now consider a simplified situation where instead of removing a ball we remove a circular disc with radius \( r_0 \) from the rubber surface. We will also neglect the influence of the surface roughness on the fluid flow dynamics. In the present case the average contact pressure is below 0.1 MPa and the fluid pressure flow factor, which determines the influence of the surface roughness on the fluid flow, is close to unity so neglecting the influence of the surface roughness on the fluid flow is a good approximation.

The initial contact pressure \( p_0 \) is so small that we can use the asymptotic relation \( p(u) \) for the rubber-glass interaction:

\[
p = \beta E^* e^{-u/u_0}.
\]

Thus the initial separation

\[
 u_0 = -u_0 \log \left( \frac{p_0}{\beta E^*} \right).
\]

The parameters \( u_0 \) and \( \beta \) can be calculated from the surface roughness power spectrum and we get \( \beta = 0.069 \)
and \( u_0 = 1.45 \mu m \). Neglecting adhesion the loading force \( F(t) \) must equal the asperity contact force \( \pi r^2 p \) plus the viscous force i.e.

\[
F(t) = -\frac{3\pi}{2} \eta \frac{\dot{u}}{u^3} + \pi r^2 \beta E^* e^{-u/u_0}.
\] (C1)

Assuming \( F(t) = F_0(1 - t/t_0) \) one can solve (C1) numerically for \( u(t) \). In Fig. 35 we show the results for the disc removed from the elastic substrate (with Young’s modulus \( E = 2.5 \) MPa) in a fluid with the viscosity \( \eta = 0.35 \) Pas. The disc has the radius \( r_0 = 0.655 \) mm and the substrate has random roughness with the power spectrum given in Fig. 33. The squeezing force on the disc decreases linearly with time from \( F = F_0 = 0.1 \) N at time \( t = 0 \) to \( F = 0 \) at time \( t = t_0 \). The average surface separation \( u(t) \) is shown as a function of time for the case \( t_0 = 100 \) s (green line) and \( t_0 = 1000 \) s (red line). Note that the average surface separation at \( t = t_0 \) are \( u(t_0) \approx 8.8 \) and 11.0 \( \mu m \), respectively. However, in order to explain the observed pull-off forces one need to assume \( u(t_0) \approx 1.3 - 1.8 \mu m \) (see Sec. 6 and Appendix H). This indicate that due to adhesion the average surface separation at \( t = t_0 \) is almost the same as when the loading force is maximal \( u(t = 0) \approx 1.65 \mu m \) according to Fig. 35). We attribute this to strong adhesive contact hysteresis.

For water the increase in the interfacial separation during the unloading process, when \( F \) change from its maximum to zero, will be even larger than for the silicone oil due to its smaller viscosity. However, for water optical microscope pictures of the rubber-glass contact does not show any change when the loading force change from its maximum to zero. This again indicate that the energy to propagate the opening crack (at relevant speeds) is so large that the compressed asperities cannot reduce the contact area during unloading. For contact in silicone oil it is not possible to directly observe the contact area with our optical microscope because the contrast between contact and not contact is too low.

**Appendix G: Adhesion with silicone oil films on the rubber and glass surfaces.**

We have studied adhesion when both the rubber and the glass ball was covered with thin films (thickness \( d \)) of silicone oil. The adhesion data are analyzed using the JKR theory although this theory may not be strictly valid in the present case. Hence, the “work of adhesion” quoted below must be interpreted simply as \( w = 2F_c/(3\pi R) \). We note that a fluid capillary bridge (with fixed fluid volume) between a rigid sphere and a flat rigid surface gives rise to a (adiabatic) pull-off force \( F_c = 4\pi R\gamma \), where we have assumed that the fluid wet the two solids[63]. Thus in this limit the “work of adhesion” must be interpreted as \( w = 8\gamma/3 \approx 2.67\gamma \). We believe this result holds accurately also when a fluid film exist at the interface if the fluid film thickness is large compared to the root-mean-square roughness amplitude.

In fact we have recently performed experiments where the substrate was a thick \( (d = 1 \) cm) silicone oil slab (the same oil as used here), and where \( F_c = 4\pi R\gamma \) was found to hold accurately[74].

In the opposite limit where the surface roughness amplitude is much larger than the oil film thickness the JKR theory is approximately valid with \( w = 2\gamma \) (see Ref. [75]). For finite pull-off speeds the pull-off force is also influenced by the fluid viscosity.

Fig. 36 shows the “work of adhesion” during retraction (separation) (filled circles) and during approach (open circles), as a function of the number of contacts for the rubber surface. The glass ball and rubber surface was originally cleaned with acetone and after covered with a thin film of silicone oil (viscosity \( \approx 0.65 \) Pas). The red and blue circles are the work of adhesion for the pull-off or approach velocities 0.9 \( \mu m/s \) and 35 \( \mu m/s \), respectively.

Fig. 37: The interaction force between the glass ball and the bromobutyl rubber as a function of time close to a detachment for surfaces covered by a thin film of silicone oil (viscosity 0.35 Pas). The drive speed is \( v_s = 0.9 \mu m/s \).
rubber surface are covered by ~ 10 µm film of silicone oil (viscosity ≈ 0.35 Pas). The red and blue circles are the work of adhesion for the pull-off (and approach) velocities 0.9 µm/s and 35 µm/s, respectively.

In this case the work of adhesion is determined by the silicone oil capillary bridge formed between the glass ball and the rubber surface. This result in an adhesiive interaction force which extend over much larger separation distance (or time) then for the dry state. This is illustrated in Fig. 37 which shows the interaction force as a function of time close to a detachment for the drive (pull-off) speed \( v_z = 0.9 \) µm/s. Note that ~ 100 s (or the distance ~ 100 µm) is necessary in order to break the junction, in contrast to the ~ 1 s (or the distance ~ 1 µm) for the dry surface (see Fig. 23(a) below).

In this study we do not know the exact oil thickness but if the fluid film is thinner than the root-mean-square roughness amplitude, the adiabatic work of adhesion \( w_0 \) resulting from a capillary bridge is just twice the surface tension \( \gamma \) of the liquid, \( w_0 = 2\gamma \) (see Ref. [75]). The actual work of adhesion is affected by viscous dissipation in the liquid bridge and, to a much less extent, in the rubber, which will enhance \( w \) during pull-off (say from \( w_0 \) to \( w_b \)) and reduce \( w \) during approach (say from \( w_0 \) to \( w_a \)). Here we assume, as found to hold to a good approximation for the viscoelastic crack propagation case, that the enhancement factor \( w_0 \approx (1 + f) \) during pull-off is also determining (approximately) the reduction factor \( w_a \approx (1/f) \) during approach. In this case

\[
\frac{w_a}{w_0} = (w_a/w_b)_{1/2}.
\]

The silicone oil we use has the surface tension \( \gamma \approx 0.02 \) J/m² so we get \( w_0 = 2\gamma = 0.04 \) J/m². From Fig. 36 the work of adhesion at the lowest pull-off speed 0.9 µm/s is \( w_a = 0.05 \) J/m² during pull-off and \( w_b = 0.03 \) J/m² during approach. Assuming \( w_0 = (w_a/w_b)_{1/2} \) we get the adiabatic work of adhesion \( \approx 0.04 \) J/m² in good agreement with the expected adiabatic work of adhesion.

The work of adhesion at the higher pull-off speed (35 µm/s) is larger than for the lower speed due to the increased viscous dissipation. For 35 µm/s from Fig. 36 we get \( w_a = 0.13 \) J/m² and \( w_b = 0.015 \) J/m². Thus we get \( (w_a/w_b)_{1/2} \approx 0.04 \) J/m² again in agreement with the expected adiabatic work of adhesion. In Ref. [74], where we studied adhesion during (slow) cross-linking of silicone oil, we did not observe any effect of the silicone oil viscosity on the pull-off force until very close to the gel point of the silicone oil (where the viscosity becomes huge), but we attribute this to the different experimental conditions: In Ref. [74] the glass ball interacted with a bulk oil sample while in the present study the silicone oil film is very thin, and the viscous energy dissipation is much larger in a thin fluid film (assuming similar flow velocities) than in a bulk sample.

Appendix H: Rope spring constant

![FIG. 38: The relation between the force and the displacement of the drive during a contact cycle of the glass ball against an approximately rigid (in the case PMMA) plate. The effective spring constant during retraction depends slightly on the retraction velocity but is of order \( k \approx 200 \) N/m.]

![FIG. 39: The rate of fluid squeeze-out for the sphere with radius \( R \) is the same as for a circular disc with radius \( r = (2RU)_{1/2} \).]

The nylon rope connecting the glass ball to the pulley can be considered as an effective spring with the spring constant \( k \). We can measure \( k \) by moving the glass ball towards and away from a hard substrate. Fig. 38 shows the the relation between the force and the displacement of the drive during a contact cycle of the glass ball against an approximately rigid (in the case PMMA) plate. The effective spring constant during retraction depends slightly on the retraction velocity but is of order \( k \approx 170 - 190 \) N/m.

Appendix I: Fluid squeeze-in, numerical results

For adhesion in the silicone oil, the interaction force during retraction is strongly influenced by the fluid viscosity, which result in a much slower time variation of in the interaction force at pull-off then the very fast (abrupt) (within 1 second) variation observed in water. Here we present a very simple approximate theory for the influence of the silicone oil on the interaction force during pull-off.

Consider a glass ball squeezed against the rubber sur-
face in a fluid. Let $t = 0$ denote the time during pull-off when the force on the substrate vanishes (which was denoted by $t_0$ in Appendix F). Let $u_0$ be the average separation between the surfaces in the nominal contact area at time $t = 0$. When (during unloading) the interacting force vanish, there is a fluid pressure force at the interface and an equal (but of opposite sign) asperity contact pressure force. Here we will make the assumption that when $F = 0$ the fluid pressure force vanish (which imply that the repulsive and attractive rubber-glass asperity forces balance each other). To calculate the dependency of the interaction force $F(t)$ on time, we assume that for $t > 0$ the only force acting on the ball is the viscous force from the fluid. Thus we assume that the attractive glassrubber interaction matters only in that it determined the initial (average) surface separation $u(0) = u_0$ when $F = 0$.

When a rigid ball (radius $R$) is squeezed against a flat rigid surface in a fluid with the viscosity $\eta$, the relation between the force $F$ and the (minimum) surface separation $u$ is given by\cite{76, 77}

$$F = -6\pi R^{2}\frac{\dot{u}}{u}$$  \hspace{1cm} (E1)

As shown in Appendix J, this equation can also be derived by considering the fluid squeeze-out for a circular plate with radius $r = (2Ru)^{1/2}$ (see Fig. 39).

The interfacial separation velocity $\dot{u}(t)$ is not the same as the drive velocity $v_z$ because of the elasticity in the system. Thus the nylon rope has an effective spring constant $k = 100–200$ N/m (see Appendix H), and the rubber substrate too will deform elastically in response to the viscous force $F$ acting on it. As a result $F = k^*(s-u)$, where $s = s_0 + vt$ is the drive displacement and $k^* < k$ an effective (combined) spring constant (see Appendix J). Combining this equation with (E1) gives the equation of motion for $u(t)$ (here we have neglected inertia effects):

$$6\pi \eta R^2 \frac{\dot{u}}{u} = k^*(s-u)$$  \hspace{1cm} (E2)

Let $t = 0$ correspond to the point during retraction where the force on the substrate from the ball vanish ($F = 0$). We assume that when $F \leq 0$ only the viscous force act on the ball (and the substrate). Since $F = 0$ at $t = 0$ from (E1) we get that $\dot{u} = 0$ for $t = 0$. The second boundary condition $u(0) = u_0$ is determined by the separation between the glass ball and the rubber substrate at $t = 0$, and will be used as a fitting parameter (the only fitting parameter) in the following study.

We have solved (E2) using numerical integration (see Appendix J). In Fig. 40, 41 and 23(c) we compare the theory predictions with the measured data for the pull-off speeds $v_z = 35, 6.3$ and 1.75 $\mu$m/s. The results are for the bromobutyl rubber in silicone oil with the viscosity $\eta = 0.35$ Pas. The figures show the force $F(t)$ acting on the substrate during pull-off of a glass ball (diameter $2R = 3$ cm) in silicone oil. The different symbols are from different pull-off cycles, shifted along the time axis so that the minimum of the pull-off force occur at the same time point. The green line is the theory prediction assuming that only a viscous drag force act on the rubber substrate. For the bromobutyl rubber in silicone oil with the viscosity $\eta = 0.35$ Pas. For the theory curve we have assumed that the initial separation (at $F = 0$) between the glass ball and the substrate is $u_0 = 1.8 \mu$m.

FIG. 40: The force $F(t)$ acting on the substrate during pull-off of a glass ball (diameter $2R = 3$ cm) in silicone oil. The pull-off speed $v_z = 35 \mu$m/s. The different symbols are from different pull-off cycles, shifted along the time axis so that the minimum of the pull-off force occur at the same time point. The green line is the theory prediction assuming that only a viscous drag force act on the rubber substrate. For the bromobutyl rubber in silicone oil with the viscosity $\eta = 0.35$ Pas. The theory curve we have assumed that the initial separation (at $F = 0$) between the glass ball and the substrate is $u_0 = 1.8 \mu$m.

Appendix J: Fluid squeeze-in, theory

Consider the fluid squeeze flow between a rigid sphere and a flat rigid surface. Let $u(t)$ denote the minimum separation between the surfaces. Most of the resistance towards fluid squeeze-out occur in the region where the separation between the surfaces arises from the area where the separation between the surfaces is of order a few times $u(t)$, say when the separation varies from $u(t)$ to $2u(t)$. When $u << R$ the radius of this circular region
is \( r \approx (2Ru)^{1/2} \) (see Fig. 39). In a first approximation we can replace the sphere with a circular disc with radius \( r \) separated from the flat substrate with the distance \( u \). For a circular disk the relation between the applied force \( F \) and the separation \( u \) are given by the well-known relation (see, e.g., [1, 2])

\[
F = -\frac{3\pi \eta R^2}{2} \frac{\dot{u}}{u^3}
\]

Substituting \( r \approx (2Ru)^{1/2} \) in this equation gives

\[
F = -6\pi \eta R^2 \frac{\dot{u}}{u}
\]  

(F1)

which agree with the exact result (E1).

Let us now study the fluid squeeze flow when the drive is moved away (pull-off) from the substrate with the speed \( v \). We will neglect inertia effects. Thus, the same force \( F \) which act on the sphere from the driving spring also act on the substrate. This will result in some elastic deformation of the substrate. Let \( q \) denote the displacement of the substrate at the center of the contact. If a uniform stress act on a semi-infinite solid within a circular region with radius \( r \), the displacement \( q \) is related to the force \( F \) via \( F = k'q \) where \( k' = (\pi/2)rE^* \) (where \( E^* = E/(1-\nu^2) \), where \( E \) and \( \nu \) are the Young’s modulus and the Poisson ratio of the rubber). Using this equation and \( F = k(s-w) \), where \( s = s_0 + vt \) is the displacement of the drive and \( w \) the displacement of the sphere, and \( k \) the spring constant of the driving spring (see Appendix H) we get the separation at the interface

\[
u = w - q = s - \frac{1}{k} \left( \frac{1}{k} + \frac{1}{k'} \right) F = s - \frac{1}{k^*} F
\]

In the present study \( k \ll k' \) and the effective substrate (rubber) spring constant \( k^* \) is not very important for the results presented below.

Using (F1) this gives

\[
6\pi \eta R^2 \frac{\dot{u}}{u} = k^* (s - u)
\]

or

\[
\dot{u} = (s - u)u_0 \alpha
\]  

(F2)

where

\[
\alpha = \frac{k^*}{6\pi \eta R^2}
\]  

(F3)

Note that since \( k' = (\pi/2)rE^* = (\pi/2)(2Ru)^{1/2}E^* \) depends on \( u \) so will \( \alpha = \alpha(u) \). The solution of (F2) depends on the initial condition for \( u(t) \) for \( t = 0 \) and on \( s_0 \). These values depends on the history of the contact prior to the time \( t = 0 \) which depends on the influence of the surface roughness on the contact between the ball and the rubber substrate.

Let us first consider a general case where \( u(0) = u_0 \) and \( \dot{u}(0) = \dot{v}_0 \). Writing

\[
u = \nu_0 + u_0 + v \xi
\]  

(F4)

this gives \( \xi = \dot{\xi} = 0 \) for \( t = 0 \). Substituting (F4) in (F2) gives

\[
v_0 + v \dot{\xi} = (s_0 + vt - \nu_0 - \nu_0 - v \xi)u_0 \alpha
\]  

(F5)

For \( t = 0 \) from (F2) we get \( v_0 = (s_0 - u_0)u_0 \alpha_0 \), where \( \alpha_0 = \alpha(u_0) \). Thus \( s_0 - u_0 = v_0/(\alpha_0 u_0) \). Substituting this in (F5) gives

\[
\dot{v}_0 \alpha = \nu_0 \alpha_0 u_0 + \left[ \nu_0 u_0 + \left( 1 - \frac{\nu_0}{v} \right) t - \dot{\xi} \right] u_0 \alpha(u)
\]  

(F6)

where

\[
\alpha = \frac{k}{6\pi \eta R^2} \left( 1 + \frac{k}{k_0} \left( \frac{u_0}{u} \right)^{1/2} \right)^{-1}
\]  

(F7)
with \( k_0' = (\pi/2)(2RU_0)^{1/2}E^* \).

Let \( t = 0 \) correspond to the point during retraction where the force on the substrate from the ball vanishes (\( F = 0 \)). We assume that when \( F \leq 0 \) only the viscous force act on the ball (and the substrate). Since \( F = 0 \) at \( t = 0 \) from (F1) we get that \( u = 0 \) at \( t = 0 \). Thus \( v_0 = 0 \) and (F6) reduces to

\[
\dot{\xi} = (t - \xi)(u_0 + v\xi)\alpha(u_0 + v\xi)
\]

We have solved (F8) using numerical integration. In Fig. 40, 41 and 23(c) we show the force \( F(t) \) acting on the substrate during pull-off of a glass ball (diameter \( 2R = 3 \text{ cm} \)) in silicone oil (with the viscosity \( \eta = 0.35 \text{ Pa s} \)), for the pull-off speeds \( v_2 = 35, 63 \) and \( 1.8 \mu\text{m/s} \). The green lines are the theoretical predictions, assuming that only a viscous drag force act on the rubber substrate, and the different symbols the are measured data. In 23(c) we show measured data for several pull-off events, shifted along the time axis so the minimum interaction force coincides. In the calculations we have assumed the initial ball-substrate separation \( u_0 = 1.8, 1.65 \) and \( 1.4 \mu\text{m} \), respectively.

In Fig. 42 we show the same as in Fig. 41 but for the waiting time 7200 s. We have assumed the initial separation (at \( F = 0 \)) \( u_0 = 1.3 \mu\text{m} \). The interfacial separations (for \( F = 0 \)) used above, \( u_0 = 1.3 - 1.8 \mu\text{m} \), are all consistent with what is expected from contact mechanics calculations (see Sec. 3.1).

For water the fluid flow has a negligible effect on the observed pull-off force. This is illustrated in Fig. 43, which show the theoretically estimated time dependence of interaction force between the glass ball (diameter \( 2R = 2.5 \text{ cm} \)) and a flat substrate in water (viscosity \( \eta = 0.001 \text{ Pa s} \)). The drive speed is \( v_2 = 0.9 \mu\text{m/s} \) and the initial separation between the ball and the substrate is \( u_0 = 1 \mu\text{m} \). Note that the interaction force is \( \sim 100 \) times smaller than the measured one, and the interaction force decays slower with increasing time than observed (compare Fig. 43 and 23(b)).

[77] https://ntrs.nasa.gov/archive/nasa/casi.ntrs.nasa.gov/19730001779.pdf