

1 **Functional electronic inversion layers at ferroelectric domain**  
2 **walls**

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28 Ferroelectric domain walls hold great promise as functional 2D-materials because of  
29 their unusual electronic properties. Particularly intriguing are the so-called charged  
30 walls where a polarity mismatch causes local, diverging electrostatic potentials  
31 requiring charge compensation and hence a change in the electronic structure. These  
32 walls can exhibit significantly enhanced conductivity and serve as a circuit path. The  
33 development of *all-domain-wall* devices, however, also requires walls with  
34 controllable output to emulate electronic nano-components such as diodes and  
35 transistors. Here we demonstrate electric-field control of the electronic transport at  
36 ferroelectric domain walls. We reversibly switch from resistive to conductive behavior  
37 at charged walls in semiconducting  $\text{ErMnO}_3$ . We relate the transition to the formation  
38 – and eventual activation – of an inversion layer that acts as the channel for the  
39 charge transport. The findings provide new insight to the domain-wall physics in  
40 ferroelectrics and foreshadow the possibility to design elementary digital devices for  
41 all-domain-wall circuitry.

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50 Recently, ferroelectric domain walls have been demonstrated to develop novel  
51 electronic ground states that differ from those of the surrounding bulk material. In  
52 addition, they can be induced, moved, and erased on demand, representing natural,  
53 flexible interfaces with novel functional properties<sup>1-3</sup>. After the seminal discovery of  
54 electrically conducting walls in the multiferroic semiconductor BiFeO<sub>3</sub><sup>4</sup>, there have been  
55 numerous reports on conducting walls in prototypical ferroelectrics including  
56 PbZr<sub>0.2</sub>Ti<sub>0.8</sub>O<sub>3</sub><sup>5</sup>, LiNbO<sub>3</sub><sup>6</sup>, and BaTiO<sub>3</sub><sup>7</sup>, as well as improper ferroelectrics such as  
57 hexagonal RMnO<sub>3</sub> (*R* = Sc, Y, In, Dy to Lu)<sup>8,9</sup> and (Ca,Sr)<sub>3</sub>Ti<sub>2</sub>O<sub>7</sub><sup>10</sup>, indicating that such  
58 conductivity is a general phenomenon<sup>2,3,11,12</sup>. Conducting domain walls are now  
59 anticipated in a wide range of otherwise insulating ferroic materials, with the  
60 observation of metallic domain walls in the magnetic insulator Nd<sub>2</sub>Ir<sub>2</sub>O<sub>7</sub> being a major  
61 new development<sup>13</sup>. Furthermore, recently established characterization methods allow  
62 to determine intrinsic domain wall properties with unprecedented completeness. Local  
63 Hall measurements, for instance, reveal the types, mobilities and densities of involved  
64 carriers<sup>14</sup>, and advanced frequency-dependent<sup>15,16</sup> and contact-free transport<sup>17,18</sup>  
65 measurements provide insight into the underlying conduction mechanisms. In order to  
66 make use of the exotic domain wall properties and ultimately design domain-wall-based  
67 devices for nanotechnology, however, additional functionality beyond just conduction is  
68 required that allows the behavior of classical electrical components to be emulated at  
69 the nanoscale. Here, we demonstrate electric-field control of the electronic transport at  
70 charged head-to-head domain walls in semiconducting ErMnO<sub>3</sub>. The electric field allows  
71 reversible switching between resistive and conductive domain wall states,

72 corresponding to a domain-wall-based binary switch. We relate this qualitative change  
73 in the transport behavior to the formation – and eventual activation – of an electronic  
74 inversion layer at the head-to-head walls that acts as the channel for the charge  
75 transport.

76 For our study we choose the narrow band gap, p-type semiconductor  $\text{ErMnO}_3$  ( $E_g$   
77 = 1.6 eV<sup>19</sup>) as it naturally develops all fundamental types of ferroelectric domain walls at  
78 room temperature ( $T_c = 1470 \text{ K}^{20}$ ), including neutral (side-by-side) as well as negatively  
79 (tail-to-tail) and positively charged (head-to-head) wall configurations<sup>8</sup>. Moreover, the  
80 atomic structure and basic transport properties of these walls are particularly well-  
81 understood<sup>8,21,22</sup>. While the main interest in neutral domain walls is associated with  
82 their functionality as insulating barriers<sup>23</sup>, charged domain walls are intriguing because  
83 of their unique electrostatics, giving rise to diverse and tunable electronic transport  
84 properties<sup>8</sup>. Enhanced electronic conductance has been reported for tail-to-tail walls in  
85  $\text{ErMnO}_3$  and explained based on the accumulation of mobile holes<sup>3,14</sup>. The holes  
86 originate from interstitial oxygen anions<sup>24</sup> and represent the majority carriers. These  
87 carriers accumulate at tail-to-tail walls to screen the local, divergent electric field.  
88 Likewise, head-to-head walls in the same sample exhibit suppressed conductance, which  
89 has been explained by the depletion of majority carriers, with possible additional  
90 contributions from minority carriers (electrons)<sup>8,11</sup>. The latter are particularly interesting,  
91 as the involvement of both majority and minority carriers may give rise to novel,  
92 functional domain-wall behavior.

93 In order to study emergent domain-wall properties at head-to-head walls in  
94  $\text{ErMnO}_3$ , we measure the local electronic transport over an extended voltage range.  
95 Crystals of  $\text{ErMnO}_3$  were grown by the pressurized floating-zone method<sup>25</sup> and  
96 specimens with in-plane polarization and a thickness of  $\approx 1$  mm were prepared and  
97 chemo-mechanically polished with silica slurry. In Fig. 1a–c we present conductive  
98 atomic force microscopy (cAFM) data obtained with a conductive diamond-coated tip  
99 (DCP12, NT-MDT) under sample bias voltages of up to 6 V. Test measurements on  
100 different walls and with different tip-coatings reveal bulk-dominated transport behavior,  
101 ensuring that intrinsic domain wall properties are probed (see Supplementary Notes and  
102 Supplementary Fig. 1 and 2). At low bias voltage ( $V_{\text{bias}} = 2.5$  V) we observe the  
103 established transport behavior<sup>8,9</sup> with conducting tail-to-tail (bright) and insulating  
104 head-to-head (dark) domain walls (Fig. 1a). A qualitatively different transport  
105 phenomenon, however, arises at higher voltage as shown by the scan in Fig. 1b, taken at  
106  $V_{\text{bias}} = 6$  V. The spatially resolved data highlights that both tail-to-tail and head-to-head  
107 walls can exhibit a higher electronic conductance than the surrounding domains. A more  
108 detailed study is shown in Fig. 1c, which is conducted in an area with well-separated  
109 walls to exclude crosstalk effects (see Supplementary Figure 3). Figure 1c shows the  
110 relative domain-wall conductance,  $\Delta I$ , after subtracting the bulk current, which for  
111 reference, is shown in the inset to Fig. 1c ( $\Delta I = I_{\text{wall}} - I_{\text{bulk}}$ ). The comparison with respect  
112 to the bulk (black dotted line in Fig. 1c) reveals that the head-to-head domain walls  
113 become more conducting than the bulk above  $V_c \approx 4.8$  V, approaching the conductance  
114 measured at the tail-to-tail walls for  $V > V_c$ . The transition from resistive ( $I_{\text{wall}} < I_{\text{bulk}}$ ) to

115 conductive ( $I_{\text{wall}} > I_{\text{bulk}}$ ) behavior occurs gradually and for moderate electric fields (see  
116 also Supplementary Fig. 2). For comparison, more than one order of magnitude higher  
117 electric fields are used to induce domain wall currents in BiFeO<sub>3</sub> or PbZr<sub>0.2</sub>Ti<sub>0.8</sub>O<sub>3</sub> thin  
118 films<sup>4,5</sup>. The low electric field energy suggests a *qualitative* change in the electronic  
119 transport at head-to-head walls rather than a breakdown of the insulating domain wall  
120 state. This qualitative change, however, cannot be explained based on the depletion of  
121 majority carriers (holes) alone.

122         To better understand this unusual transport phenomenon, we build a DFT-based  
123 semi-classical model describing the redistribution of mobile carriers. Assuming that  
124 ErMnO<sub>3</sub> behaves like a simple band insulator we solve Poisson's equation self-  
125 consistently with the carriers treated semi-classically (see Methods for details) and  
126 obtain the band diagram presented in Fig. 1d. We see that far from the domain walls the  
127 potential is flat and the Fermi level,  $E_{\text{Fermi}}$ , lies just below the valence-band maximum  
128 (VBM) corresponding to a realistic carrier density of  $p_0 = 2 \cdot 10^{19} \text{ cm}^{-3}$ , i.e., a doping level  
129 of 0.007 holes per unit cell. At the tail-to-tail walls the VBM shifts upwards and  
130 generates more holes which screen the negative bound domain-wall charge,  $-2P_z$  ( $\mathbf{P} = (0,$   
131  $0, P_z)$ ); this is consistent with the enhanced conductance measured at the tail-to-tail  
132 domain walls<sup>8,9</sup> (see Fig. 1a). For the head-to-head domain walls, we find a significant  
133 band bending with the conduction-band minimum (CBM) dipping below the Fermi  
134 energy. This implies that the screening at head-to-head domain walls is realized by both  
135 a depletion of holes, occurring in a total range of about 22 nm, and an accumulation of  
136 electrons right at the wall where the CBM lies below  $E_{\text{Fermi}}$  (see Fig. 1d). Thus, the simple

137 model indicates that the density of electrons, i.e., the minority carriers, is considerably  
138 enhanced at the head-to-head walls. This result is in agreement with previous analytical  
139 investigations<sup>11</sup>, demonstrating the soundness of our alternative DFT-based approach. In  
140 both models, however, hole depletion needs to override the electron accumulation in  
141 order to reproduce the experimental observation of insulating walls for  $V < V_c$  (Fig. 1a).  
142 The latter is illustrated in Fig. 1e, where the density of carriers is plotted as a function of  
143 the distance from the wall. The corresponding average carrier density – which is  
144 proportional to the conductance – is shown in the inset. For  $V > V_c$  the electrons likely  
145 dominate the domain-wall conductance as they are the only mobile carriers available for  
146 charge transport at the head-to-head walls. Aside from the observed change in  
147 conductance, the pronounced band bending at head-to-head walls is appealing for the  
148 design of domain-wall-based transistors as sketched in Fig. 1f. The field effect associated  
149 with the polarization charges can, in principle<sup>8,26</sup>, be used to modulate the conductivity  
150 at the wall and, hence, serve as a natural, intrinsic gate. In the following, however, we  
151 will focus on the voltage-driven transition from resistive to conductive behavior.

152 We next use electron energy loss spectroscopy (EELS) to probe the electronic  
153 structure at the head-to-head walls at atomic resolution. Figure 2a shows a high-angle  
154 annular dark field scanning transmission electron microscopy (HAADF-STEM) image of a  
155 head-to-head domain wall imaged along the [100] zone axis of  $\text{ErMnO}_3$  (see Methods for  
156 details). The erbium ions are shifted with respect to the manganese-oxygen polyhedra,  
157 displaying either an up-down-down ( $-P$  domain) or down-up-up ( $+P$  domain)  
158 arrangement<sup>21</sup>. These displacements indicate the local spontaneous polarization and

159 thus provide a local measure for the polarization reorientation across the head-to-head  
160 wall. We find a rather abrupt discontinuity of the polarization orientation at the wall,  
161 consistent with previous work<sup>21</sup>. Using spatially resolved EELS we investigate the  
162 electrochemical wall structure by measuring the local manganese valence. Figure 2b  
163 displays the evolution of the corresponding EELS spectra, taken at the Mn L<sub>2,3</sub>-edge,  
164 across the head-to-head wall. Figure 2c shows an enlarged image of the Mn L<sub>3</sub>-edge  
165 where the experimental data points are overlaid with a manganese reference spectrum  
166 collected on the ErMnO<sub>3</sub> sample away from the domain wall. The spectra collected  
167 within the domain areas exhibit minor differences that reflect an inhomogeneity of the  
168 electrical background. In the vicinity of the head-to-head wall, we clearly note a distinct  
169 feature at ~641 eV in the spectra. Here, the data is not well described by the Mn<sup>3+</sup>  
170 reference spectrum (see also Supplementary Figure 4).

171 To quantify the change observed at the Mn L<sub>2,3</sub>-edge at the head-to-head wall,  
172 the full Mn L<sub>2,3</sub>-edge is fitted with two spectra corresponding to the Mn<sup>3+</sup> and Mn<sup>2.8+</sup>  
173 valence states. The Mn<sup>2.8+</sup> spectrum is calculated as a linear combination of Mn<sup>3+</sup> and  
174 Mn<sup>2+</sup> spectra as described in the Supplementary Notes and Supplementary Fig. 5 (we  
175 note that the spectrum of six-fold coordinated Mn<sup>2+</sup> is used for reference as the current  
176 work represents the first spectroscopic study of the Mn<sup>2+</sup> electronic state in trigonal  
177 bipyramidal coordination). The analysis reveals a statistically significant concentration of  
178 the lower valence state spatially localized over 2 - 3 unit cells near the head-to-head  
179 domain wall. Based on the valence concentration, we calculate the excess charge per  
180 manganese atom at the domain wall relative to the Mn<sup>3+</sup> state in the bulk<sup>27</sup>. This charge



181 as a function of position is plotted in Fig. 2d. Aggregating over several such walls at  
182 distinct locations in the material, we find that the local valence change is equivalent to  
183 the accumulation of a negative charge of  $0.09 \pm 0.04$  electrons per manganese atom at  
184 the head-to-head wall position. Since the bulk polarization<sup>28</sup> of  $\text{ErMnO}_3$  is  $\approx 6 \mu\text{C}/\text{cm}^2$ ,  
185 the amount of negative charge density needed to screen the polar discontinuity at the  
186 head-to-head walls is  $\approx 12 \mu\text{C}/\text{cm}^2$ . This value converts into a carrier density in the order  
187 of  $\approx 0.1$  (0.3) electrons per manganese ion (unit cell, u.c.), which is in the range of our  
188 experimental uncertainty. Complementary EELS measurements at the oxygen K-edge  
189 show no statistically relevant anomaly (Supplementary Fig. 5c), excluding that oxygen  
190 vacancy formation is responsible for the local manganese valence change. EELS studies  
191 at tail-to-tail walls and X-ray photoemission electron microscopy further confirm that  
192 the lower valence state is a feature that is unique to the 2 – 3 unit cell wide area around  
193 the head-to-head walls (see Supplementary Notes and Supplementary Fig. 6-8). In  
194 agreement with our semi-classical model, the EELS results corroborate that electron  
195 accumulation, in addition to hole depletion, plays an important role for the  
196 compensation of the polarity mismatch at head-to-head domain walls in  $\text{ErMnO}_3$ .

197 To determine the orbital character of the electrons and elucidate the relation  
198 between their accumulation and the local manganese valence state, we perform first-  
199 principles calculations based on density functional theory (DFT) within the local density  
200 approximation (LDA)  $+U$  method using  $\text{YMnO}_3$  as our model hexagonal manganite  
201 ( $\text{YMnO}_3$  is structurally and electronically similar to  $\text{ErMnO}_3$ , and the absence of  $f$ -  
202 electrons simplifies the DFT description). In Fig. 3a we show the calculated orbital-

203 resolved density of states for the valence and conduction bands. We see that, consistent  
204 with literature calculations<sup>29,30</sup>, the conduction band is narrow because it is formed from  
205 localized  $d_{z^2}$ -orbitals, with only minimal hybridization with neighboring axial oxygen  $p_z$ -  
206 orbitals, whereas the valence band is broad, consisting of strongly hybridized and  
207 delocalized manganese  $d$ - and oxygen  $2p$ -states. At the head-to-head walls, where the  
208 CBM dips below the Fermi level (Fig. 1d), we therefore expect localized electrons,  
209 whereas holes at the VBM are delocalized in nature. This expectation is consistent with  
210 our spectroscopy data, indicating a manganese valence change associated with the  
211 accumulation of electrons.

212         While our theoretical analysis gives an appealing qualitative description of our  
213 experimental data, at the quantitative level there is a discrepancy between the density  
214 of electron carriers at the domain wall predicted by the semi-classical model and that  
215 indicated by the EELS measurements. According to the cAFM measurements, hole  
216 depletion needs to override the electron accumulation in the model, while EELS points  
217 to a dominant electron-like compensation. This raises the question of whether an  
218 additional mechanism is at play in the hexagonal manganites. The semi-classical model  
219 and even our DFT band picture constitute a drastic simplification of the problem,  
220 especially in a material such as  $\text{ErMnO}_3$ , where many-body correlation effects likely play  
221 an important role. In this context, it is important to recognize that electrons in the  
222 spatially localized manganese  $d_{z^2}$ -orbitals experience a strong on-site Coulombic  
223 repulsion, which typically favors the formation of localized polaronic states rather than  
224 itinerant Bloch states<sup>31</sup>. To verify whether such a scenario might apply to our case, we

225 calculate the energies of hypothetical polaronic states for both electrons and holes by  
226 introducing a single electron or hole in a 120-atom supercell and lowering the local  
227 symmetry around a manganese site (see Methods). We find (Fig. 3b) that an isolated  
228 electron polaron has lower energy than an itinerant Bloch electron for  $U$  values of 7.5 eV  
229 and higher. (In contrast, hole polarons remain unstable relative to the Bloch state even  
230 for  $U$  values as large as 8.5 eV.) At head-to-head domain walls, we expect that polarons  
231 arrange in a two-dimensional lattice, and thereby significantly reduce their formation  
232 energy compared to the case of an isolated defect. We find that, by combining the latter  
233 effect with the data of Fig. 3b and our band-bending model (see Supplementary  
234 Information), polarons are most likely to form right at the head-to-head wall, for a  
235 realistic range of values of both the Hubbard  $U$  ( $U \approx 6-6.5$  eV) and the bulk doping level.  
236 Note that polarons should give an additional barrier to electronic conductivity at low  
237 voltage, consistent with the observations presented in Fig. 1, lifting the band-model-  
238 related condition that hole depletion dominates over electron accumulation at head-to-  
239 head walls (Fig. 1e).

240 Thus, experiment and theory identify an accumulation of electrons at the head-  
241 to-head walls, leading to the formation of an inversion layer. The electrons are in a  
242 localized polaronic state and hence do not contribute to the conductance at low voltage.  
243 For high voltage ( $V > V_c$ ) these electrons dominate the conductance as they are the only  
244 available mobile carriers. In the polaronic picture,  $V_c$  is related to the transition from  
245 localized to itinerant electrons and hence to the activation of the inversion layer as the  
246 effective channel for the domain-wall transport. This behavior is fundamentally different

247 from the majority-carrier-enabled transport at tail-to-tail domain walls, which does not  
248 involve significant lattice coupling<sup>14</sup>.

249 In Figure 4a,b we show how this behavior can be used in order to realize, e.g., a  
250 domain-wall-based binary switch. The cAFM data in Fig. 4a is collected at a head-to-  
251 head wall as a function of time with the bias voltage varying repeatedly between  $V_0 = 2$   
252 V and  $V_0 + \Delta V = 5$  V. Due to the unusual  $I$ - $V$  characteristic at the head-to-head wall, the  
253 change in electric field allows reversible switching between resistive ( $I_0 < I_{\text{bulk}}$ ) and  
254 conductive ( $I_1 > I_{\text{bulk}}$ ) behavior as reflected by the normalized domain-wall current  $I / \Delta V$   
255  $\cdot (\Delta I / I_{\text{bulk}})$  in Fig. 4a. Figure 4b shows that the related electric-field induced gain,  $\Delta I / \Delta V$ ,  
256 can be enhanced by increasing the base voltage  $V_0$ . The enhancement in gain, however,  
257 is accompanied by the flow of a larger current  $I_0$ , which causes irreversible changes in  
258 the electronic surface structure and fast degradation of the domain-wall-based binary  
259 switch after only two to three cycles (not shown). Note that the transition from resistive  
260 to conductive behavior reflects a change from hole- to electron-dominated conductance.  
261 This qualitative change in the transport behavior is a unique feature of the inversion  
262 layer formed at the head-to-head walls.

263 The head-to-head domain walls studied in this work thus represent a natural  
264 type of semiconducting oxide interface at which the nature of the electronic transport  
265 can be manipulated at will and in a fully reversible fashion. This new degree of freedom  
266 becomes possible as the local transport behavior is determined by the interplay  
267 between holes and electrons. Now that we have shown that functional inversion layers

268 are formed at charged domain walls, the next step is to utilize individual walls in device-  
269 like architectures. In general, an involvement of both minority and majority carries is  
270 appealing as it allows device paradigms to be extended into the realm of minority-  
271 carrier devices including bistable switches and bipolar transistors. Minority-carrier  
272 devices are typically slower, but offer better on-state performance and larger  
273 breakdown voltages<sup>32</sup>. With this, our results foreshadow conceptually new domain-wall  
274 applications that go beyond conducting 2D channels that can be written, moved, and  
275 erased on demand. This opportunity brings us an important step closer to the realization  
276 of reconfigurable *all-domain-wall* circuits for next-generation nanotechnology.

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367

## 368 **Methods:**

369 **Spectroscopy:** ErMnO<sub>3</sub> platelets were oriented by Laue diffraction diffraction such that  
370 the specimen would be imaged down the [100] zone axis of the crystal in TEM. Cross-  
371 sectional TEM samples were prepared using an FEI Strata 400 Focused Ion Beam with a  
372 final milling step of 2 keV to minimize surface damage. The TEM specimens were imaged  
373 on a 100 keV Nion UltraSTEM optimized for EELS imaging (30 mrad convergence angle,

374 130 pA of usable beam current,  $\sim 1 \text{ \AA}$  spatial resolution). The microscope was equipped  
375 with a Gatan Quantum Dual EELS spectrometer; EELS spectra were collected with a 0.1  
376 eV/pixel dispersion resulting in 0.3 eV energy resolution. Fine structure information  
377 from the O-K edge and Mn-L<sub>2,3</sub> edge was collected simultaneously with the ADF signal.  
378 Gain and dark noise were corrected using Digital Micrograph™. Four cross-sectional TEM  
379 specimens were prepared from two distinct ErMnO<sub>3</sub> platelets (within the platelets the  
380 sample locations were separated by millimeters). Multiple distinct domain walls were  
381 identified in each TEM specimen each separated by several microns. In sum, over a  
382 dozen domain walls were analyzed. Post-acquisition, an off-line drift correction was  
383 performed to correct the small sample drift ( $<0.5 \text{ \AA}/\text{min}$ ). The Mn-L<sub>2,3</sub> fine structure was  
384 analyzed following a standard power law background subtraction from approximately  
385 10 eV prior to the edge onset. No additional noise reduction algorithms were employed  
386 to avoid artifacts. Scanning was performed in rapid succession perpendicular to the wall  
387 orientation so that each scan included signal from across the wall as well as the  
388 reference regions on either side. Signals were binned perpendicular to the scan  
389 direction to produce a single line scan through the wall. Manganese positions were  
390 identified from the integrated signal intensity; the signal was then summed over each  
391 manganese position to produce a single spectrum from each row of manganese atoms  
392 in the spectrum image. Averaging over manganese positions increased the signal to  
393 noise for the EELS analysis.

394 **Model Calculations:** In our semi-classical model of the carrier redistribution at the  
395 charged domain walls, we treat the bulk material as a p-type semiconductor using the

396 calculated density of states (DOS) and values of  $P = 7.1 \mu\text{C}/\text{cm}^2$  and  $\epsilon = 13$ <sup>33</sup> extracted  
397 from DFT calculations of bulk  $\text{YMnO}_3$ . The domain walls are introduced as charged  
398 planes, with a surface charge density equal to  $\pm 2P_z$ . The equilibrium distribution of  
399 screening carriers is calculated by iteratively solving the Poisson equation of a one-  
400 dimensional system with two isolated domain walls. The local carrier density is  
401 determined at each step by integrating the bulk DOS to the trial Fermi level, and by  
402 enforcing the condition of overall charge neutrality.

403 **Density functional theory:** First-principles calculations were performed using the  
404 projector augmented-wave method<sup>34</sup> as implemented in VASP<sup>35</sup>. PAW data sets with  
405 radial cutoffs of 1.48, 1.22 and 0.80 Å for Y, Mn and O, respectively, were employed. The  
406 exchange-correlation interactions between electrons were treated using the local  
407 density approximation with Hubbard  $U$  correction<sup>36,37</sup>. The  $U$  and  $J$  parameters on the  
408 Mn-3d orbitals were set to 5 and 0.88 eV, respectively. The  $P6_3cm$  noncollinear magnetic  
409 configuration of  $\text{YMnO}_3$ , which gives a band gap of 1.8 eV close to the experimental gap  
410 of 1.6 eV<sup>19</sup> was adopted. Lattice constants and internal positions were fully relaxed until  
411 the stress and forces acting on all atoms converged to less than 0.02 GPa and 0.005  
412 eV/Å, respectively. The cutoff energy was set to 550 eV, and a  $\Gamma$  centered  $4 \times 4 \times 2$   $k$ -  
413 point sampling for the reciprocal space integration was employed. The projected  
414 densities of states were evaluated within the spheres centered on the atomic sites with  
415 radii of 1.82, 1.32, and 0.82 Å for Y, Mn, and O, respectively. For the calculations of  
416 polarons, the lattice constants were fixed to the values of the relaxed unit cell, and a  $\Gamma$   
417 centered  $2 \times 2 \times 2$   $k$ -point sampling was adopted. The local symmetry was reduced by

418 moving the apical oxygen ions away from the Mn ion by 0.2 Å so that an electron can  
419 easily be captured to the Mn- $d_{z^2}$  orbital. Y ions were not moved in the initial structure,  
420 but they were spontaneously relaxed to the lowest energy positions via structure  
421 optimization. Relative energies between the polaronic and itinerant Bloch electrons  
422 were calculated for  $2 \times 2 \times 1$  supercells composed of 120 atoms as a function of the  $U$   
423 parameter, with  $J$  fixed at 0.88 eV. For itinerant electrons, band-filling corrections were  
424 applied. In order to remove the spurious electrostatic energy caused by the finite  
425 background charge, we adopted the scheme of ref. 38.

426 **Data availability.** The data that support the findings of this study are available from the  
427 authors on reasonable request.

428 **Supplementary Information** is linked to the online version of the paper at  
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452

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454 measurements, assisted by R.H., under supervision of D.A.M. and D.G.S. Y.K., M.S. and  
455 N.A.S. performed the semiclassical and DFT calculations. J.S. performed the cAFM  
456 measurements under supervision of D.M. The analysis in terms of X-PEEM was provided  
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464

## 465 **Figure Captions**

466 **Figure 1 | Electronic transport and band structure at tail-to-tail and head-to-head**  
467 **walls. a**, cAFM scan obtained at a bias voltage of 2.5 V on ErMnO<sub>3</sub> with in-plane  
468 polarization as indicated by the white arrows (the orientation corresponds to a y-cut  
469 with the (110)-direction normal to the sample surface). The image reveals a sixfold  
470 meeting point of conducting tail-to-tail (bright) and insulating head-to-head (dark)  
471 domain walls. **b**, cAFM image obtained with a bias voltage of 6V at the same position as  
472 shown in 1a with both tail-to-tail and head-to-head walls exhibiting enhanced  
473 conductance compared to the bulk. **c**, Relative current-voltage characteristics measured  
474 at tail-to-tail and head-to-head walls after subtraction of the bulk current (for reference,  
475 the bulk conductance is shown in the inset). See Supplementary Fig. S3 for  
476 corresponding spatially resolved data. **d**, Calculated band bending at tail-to-tail and  
477 head-to-head domain walls (vertical dashed lines) with arrows indicating the  
478 polarization orientation in adjacent domains. Black solid lines correspond to the

479 conduction band minimum (CBM) and valence band maximum (VBM) for  $p_0 = 2 \cdot 10^{19}$   
480  $\text{cm}^{-3}$  with the horizontal dashed line indicating the Fermi level,  $E_{\text{Fermi}}$ . **e**, Calculated  
481 carrier density at head-to-head walls. With increasing hole carrier density the screening  
482 by hole depletion becomes more efficient so that the density of electrons decreases.  
483 The inset presents the average carrier density. Lines are running averages based on a  
484 Gaussian convolution function ( $\propto \exp(-x^2/s^2)$ ,  $s = 30 \text{ nm}$ ), which corresponds to a  
485 realistic spatial resolution when mapping local current by cAFM. **f**, Conceptual sketch of  
486 a domain-wall-based field-effect transistor with polarization charges playing the role of  
487 the gate.

488 **Figure 2 | Manganese valence change at head-to-head domain walls.** **a**, HAADF-STEM  
489 image of a head-to-head domain wall. The image is colored to indicate the magnitude  
490 and direction of the displacement of erbium atoms with a sharp transition between  $+P$   
491 and  $-P$  domains ( $-P$  domain: up-down-down;  $+P$  domain: down-up-up as indicated by  
492 yellow circles)<sup>21</sup>. The scale bar is 1 nm. **b**, Layer-by-layer EELS spectra showing the  
493 evolution of the Mn  $L_{2,3}$ -edge across the head-to-head domain wall. **c**, Zoom-in to the  $L_3$ -  
494 edge in **b**. A comparison of the EELS spectra (blue dots) with  $\text{Mn}^{3+}$  reference data (solid  
495 line) reveals a spectral feature around 641 eV (indicated by the dashed line) that occurs  
496 in the vicinity of the head-to-head domain wall. **d**, Electron transfer (per manganese  
497 atom at the domain wall) to the wall calculated from the local manganese valence  
498 measured by EELS. Error bars are the standard error of the mean.

499 **Figure 3 | Orbital nature of electrons at head-to-head domain walls. a,** Orbital-resolved  
500 density of states (DOS). The black lines indicate the sum of the local density of states,  
501 while the blue and red lines show the contributions from the different orbitals. The  
502 black dashed line at 0 eV indicates the Fermi energy.  $O_{ap}$  and  $O_{ip}$  represent the oxygens  
503 located at the apical sites and in-plane sites, respectively, of the MnO-bipyramidal layers.  
504 **b,** Calculated relative energy between electronic Bloch and polaron states. Data points  
505 (black crosses) above the dashed line indicate that an itinerant Bloch state is stable for  
506 the respective  $U$  values, whereas data points below the line show that a polaronic state  
507 is stabilized. **c,** Illustration of the calculated electronic polaron state.

508 **Figure 4 | Electric-field control of electronic transport at head-to-head domain walls. a,**  
509 Normalized domain-wall current measured as a function of time over 20 switching  
510 cycles between resistive ( $I_0 < I_{bulk}$ ) and conducting ( $I_1 > I_{bulk}$ ) behavior. For voltages  $V_0 =$   
511 2V and  $\Delta V = 3V$  (see inset to 4a for a schematic illustration) , reversible control can be  
512 reliably realized for 20 switching cycles, which is the largest number of cycles we  
513 investigated. **b,** Enhanced gain can be achieved, e.g., by increasing  $I_0$ , yielding  $\Delta I / \Delta V \approx$   
514  $15 \text{ pA V}^{-1}$  for  $V_0 = 4V$  and  $\Delta V = 1V$ . The increase in gain, however, requires larger  
515 currents which cause degradation as described in the main text. **c,** Sketch showing the  
516 conductive domain-wall state for  $V = V_0 + \Delta V$  with itinerant electrons illustrated in blue.  
517 **d,** Resistive domain-wall state with localized electrons for  $V_0$ .









