Defect chemistry as a crystal structure design parameter:

Intrinsic point defects and Ga substitution in $InMnO_3$.

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Abstract

The effect of defect chemistry on the polar and non-polar phases of hexagonal $InMnO_3$ is investigated using first principles density functional calculations. Our motivation is to show how point defects and substitutional atoms can modify the delicate balance between ferroelectric and non-ferroelectric phases in a complex multiferroic oxide. By analyzing the distinct In corrugation patterns of the competing phases, we find that oxygen interstitials and indium-oxygen vacancy pairs favor the polar $P6_3cm$ phase, which is also the ground state of stoichiometric $InMnO_3$. The polar P3c1 phase is stabilized by oxygen vacancies, while In vacancies and Ga substitution on the Mn site

destabilize the ferroelectric phases and favor instead the non-polar $P\bar{3}c$ or $P6_3/mmc$ structures. In addition to the structure, the electrical properties are also strongly dependent on the defect chemistry, ranging from metallic to large band-gap insulating. The implications of the strong influence of vacancies, interstitials and substitutions on the ferroelectric and electronic properties are discussed with respect to synthesis and applications.

Introduction

The search for multiferroic materials, with their multiple coexisting ferroic orders, has been a hotbed of research activity in recent decades ^{1–5} and has led to the identification of new mechanisms for ferroelectricity that are compatible with the coexistence of magnetism. ⁶ The so-called *improper geometric ferroelectricity* identified in the rare-earth hexagonal manganites, RMnO₃ (R=Sc, Y, Dy, Ho, Er, Tm, Yb, Lu, In), is of particular interest and has stimulated research in topics as diverse as high-temperature multiferroism, ⁷ nanodevices ^{8,9} and testing of early-universe theories. ¹⁰

The high-symmetry $P6_3/mmc$ prototype structure of the hexagonal manganites consists of layers of corner-sharing Mn-O trigonal bipyramids separated by layers of Y, In or small rare-earth ions (Fig. 1(a)). The $P6_3cm$ ferroelectric structure has a tripled unit cell which is reached through a trimerizing tilting of the trigonal bipyramids at one of six equivalent angles around the z axis (labeled $\phi = 0^{\circ}, 60^{\circ}$ etc.) (Fig. 1(b)). ^{11–14} The tilting is accompanied by staggered 'up-up-down' z displacements of the R cations that cause the non-zero polarization. Analysis of the structure and symmetry indicates that an equivalent trimerizing tilting at the exactly intermediate angles of $\phi = 30^{\circ}, 90^{\circ}$ etc., accompanied by 'up-none-down' rare-earth z displacements yields the non-polar $P\bar{3}c$ structure shown in Fig. 1(d). ¹³ Trimerization tiltings at arbitrary ($\phi \neq 0$ or 30°) angles are accompanied by non-cancelling z displacements, and result in the lower-symmetry ferroelectric P3c1 space group (Fig. 1(c)), which is a subgroup of both $P6_3cm$ and $P\bar{3}c$. ¹⁵

While the ferroelectric $P6_3cm$ structure is well established to be the ground state for most members of the series, the behavior of InMnO₃ has been controversial. The first fluxgrown samples were reported from x-ray diffraction measurements to have the high-symmetry $P6_3/mmc$ structure, ¹⁶ whereas polycrystalline samples annealed at 1000 °C in an evacuated sealed quartz tube indicated a unit-cell tripling that was interpreted in terms of the polar P6₃cm structure. ¹⁷ The polar state was supported by measurements of polarization-electric field hysteresis loops that were interpreted in terms of a ferroelectric polarization; ¹⁸ subsequent dielectric measurements on high quality ceramics interpreted similar loops as dielectric loss behavior and concluded an absence of polarization. ¹⁹ A study of Ga-substituted $In(Mn,Ga)O_3^{20}$ obtained a good refinement of the x-ray data within the $P6_3cm$ symmetry group, and obtained refined atomic positions consistent with a substantial ferroelectric polarization, but failed to observe signatures of ferroelectricity in dielectric, phonon, secondharmonic-generation and differential scanning calorimetry measurements. This inconsistency was somewhat resolved by a subsequent analysis of x-ray data for InMnO₃, which found equally good refinements using either $P6_3cm$ or $P\bar{3}c$ symmetries. ¹⁴ Their comprehensive study combining piezoresponse force microscopy (PFM) and second harmonic generation (SHG) also failed to find evidence of polarization; accompanying first-principles calculations based on density functional theory found a very small energy difference between the centrosymmetric $P\bar{3}c$ and ferroelectric $P6_3cm$ structures. ¹⁴ Recently, Bekheet et al. ²¹ prepared single crystals of $InMnO_3$ with PbF_2 flux to avoid the Bi impurities reported for single crystals grown in a Bi_2O_3 flux, 22,23 and concluded that the ambient structure is $P6_3cm$ based on single crystal x-ray diffraction, SHG and PFM.

A breakthrough in understanding was made when it was shown that the details of the sample preparation affect the resulting ferroelectric properties. ²³ Using transmission electron microscopy (TEM) and high-angle annular dark-field scanning (HAADF) TEM, ferroelectricity was found in slowly cooled samples, whereas fast cooling in a furnace was shown to favor the centrosymmetric phase. A follow-up study combining first-principles calculations

with HAADF-TEM¹⁵ demonstrated that all three possible phases discussed in the symmetry analysis above could be obtained simultaneously in a single sample, and showed that their coexistence is due to extremely shallow energy barriers separating the states. (We note that, while distinguishing between the $P6_3cm$, $P\bar{3}c$ and P3c1 space groups is difficult using XRD, particularly when they coexist in a single sample, HAADF-TEM experiments image the In displacements and can thus detect the local structural details corresponding to the different symmetries. ¹⁵ In addition, it was shown that substitution of Ga on the Mn site could be used to tune between the various phases. It now seems likely that ideal, stoichiometric InMnO₃ has the $P6_3cm$ ferroelectric ground state, with the non-polar $P\bar{3}c$ phase, as well as the low-symmetry ferroelectric P3c1 and possibly even the high-symmetry paraelectric reference $P6_3/mmc$ structures accessible by modifying the defect concentration or overall stoichiometry.

These combined findings point to an essential role of point defects in determining the structural ground state, and hence the ferroelectric properties of InMnO₃. While the point defect chemistry of perovskite oxides has been studied extensively due to their importance in electronic and energy technology applications, and has been shown to strongly influence functionality, particularly in the context of strained thin films, $^{24-27}$ far less is known about the role of point defects in hexagonal RMnO₃. We anticipate strong effects, since RMnO₃ have already been shown to tolerate significant oxygen deficiency down to $3 - \delta = 2.75$, 28 excess oxygen up to $\delta = 0.35^{29,30}$ and R³⁺ deficiency down to 1 - x = 0.72. The possibility of In deficiency is even more likely due to the relatively high volatility of In at typical temperatures for single-crystal growth or sintering of polycrystals, with a vapor pressure over solid In at 950 ° C for example of 5.4×10^{-5} atm. 32

In this work we use first-principles electronic structure calculations based on density functional theory to perform a comprehensive study of the role of various defects in determining the ground state polar or non-polar structure of InMnO₃, as well as the resulting properties. Specifically, we calculate the influence of oxygen vacancies and interstitials, in-

dium vacancies, indium-oxygen vacancy pairs and Ga substitution on the Mn site. We find that, because of the energetic proximity of multiple competing ground states in InMnO₃, the coupling between structure, defect chemistry and functionality is even stronger than in the case of the perovskite oxides, where it is also of tremendous current interest in the context of strained thin films.^{24–27} Finally we discuss the enticing possibility of switching between the polar and non-polar phases through reversible modifications of the defect profile.

Computational Details

We performed density functional calculations using the projector augmented wave (PAW) method as implemented in the Vienna ab initio Simulation Package (VASP). ^{33,34} In(4d, 5s, 5p), Mn(3p, 3d, 4s), Ga(3d, 4s, 4p) and O(2s, 2p) electrons were treated as valence electrons, and their wavefunctions expanded in plane waves to an energy cutoff of 550 eV. The Brillouin zone was sampled using Gamma-centered k-point grids of 4x4x2 and 2x2x2 for 30- and 120- atom unit cells respectively. The magnetic ordering was initialized to be collinear with alternating planes of 'up-up-down' and 'down-up-down' ordering; ³⁵ spin-orbit coupling was not included. Since our defect concentrations are high, corresponding to typical experimental concentrations, we performed full structural relaxations of the internal coordinates and the cell shape and size until the Hellmann-Feynman forces were below 1 meV/Å and the stresses were below 0.01 kbar for each defect chemistry studied. We considered neutral defect cells since charged defect cells are unexpected for finite defect concentrations in this low band gap transition metal oxide.

Previous *ab initio* studies 14,15 found that the ground-state energetics are sensitive to the choice of exchange-correlation functional. For spin-polarized Perdew-Burke-Ernzerhof functionals (PBE), 36 for example, a non-polar ground state is slightly favored for stoichiometric InMnO₃, whereas the spin-polarized PBE plus Hubbard U (GGA+U) method yields a ferroelectric ground state, in agreement with the likely experimental situation. For our

calculations we used the PBE functional in its form that is modified for solids (PBEsol), ³⁷ as this typically gives excellent agreement with experiment for bond lengths and lattice parameters, and added an effective Hubbard U term, $U_{eff} = U - J = 4$ eV, in keeping with previous work on InMnO₃ and other hexagonal manganites. ³⁸ With these settings we found the $P6_3cm$ phase to be only 4 meV per formula unit lower in energy than the $P\bar{3}c$, consistent with the previously calculated near degeneracy of the two phases. ^{14,15} Both structures were found to be insulating with a calculated band gap of 1.21 eV for the $P\bar{3}c$ phase, and 1.16 eV for the $P6_3cm$ phase.

Table 1: Calculated lattice parameters and structure types for the lowest-energy stoichiometric and defective $InMnO_3$ materials. The reported lattice parameters are calculated for 120-atom unit cells with the in-plane lattice parameter, \mathbf{a} , divided by 2.

Type	Space group	(Å)	c (Å)
Stoichiometric	$P6_3cm$	5.94	11.49
O interstitial	$P6_3cm$	5.93	11.50
O vacancy	P3c1	5.96	11.48
In vacancy	$P6_3cm$	5.94	11.60
In-O vacancy pair	$P6_3cm$	5.94	11.56

The inclusion of interstitials, substitutions and vacancies lowers the symmetry from the ideal cases discussed above, making a direct comparison of the role of defects on the structural stability of the competing phases non-trivial. To assign our defective structures to one of the four space groups, we analyze the z displacements of the In ions in the region of the unit cell furthest from the location of the defects. In the case of the prototype paraelectric $P6_3/mmc$ structure, all In ions in the same plane have the same z value. For the lower-symmetry structures we label three consecutive In ions along the x direction as a, b and c, with z coordinates z_a , z_b and z_c . We then define $\Delta z_1 = z_a - z_b$ and $\Delta z_2 = z_b - z_c$. The ideal $P6_3cm$ structure is then indicated by one zero and one non-zero Δz value, $P\bar{3}c1$ by non-zero and equal Δz_1 and Δz_2 , and P3c1 by non-zero and unequal values. In our defective systems we refer to the corresponding structures as " $P6_3/mmc$ -type", " $P6_3cm$ -type", etc. In borderline

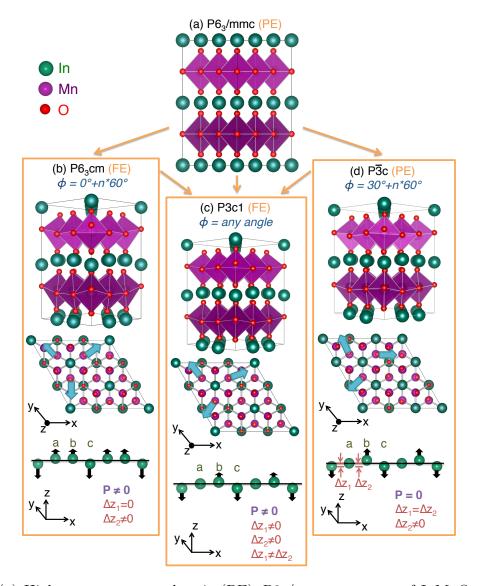


Figure 1: (a) High-symmetry paraelectric (PE) $P6_3/mmc$ structure of InMnO₃. Note the absence of trimerization. (b-d) Low symmetry structures of InMnO₃. a) shows the ferroelectric (FE) $P6_3cm$ structure with $\phi=60^\circ+n^*60^\circ$, (b) the ferroelectric P3c1 structure with a general tilt angle ϕ , and (d) the non-polar $P\bar{3}c$ structure with $\phi=30^\circ+n^*60^\circ$. In (b-d) the middle panel illustrates with blue arrows the pattern of tilting of the MnO₅ trigonal bipyramids, and the lower panel shows the In displacements along the z axis ('up-up-down', intermediate and 'up-down-none' for $P6_3cm$, P3c1 and $P\bar{3}c$ respectively).

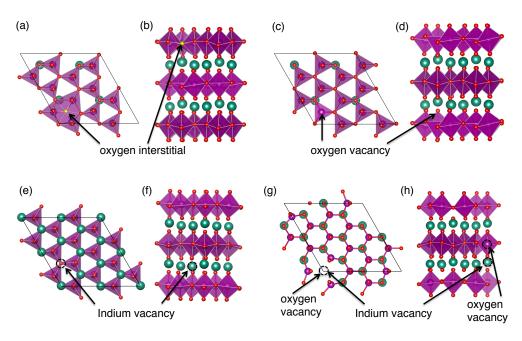


Figure 2: Calculated lowest-energy structures for interstitial and vacancy defects in $InMnO_3$. (a) and (b) show the calculated lowest-energy structure containing one oxygen interstitial per 24 formula units. The oxygen interstitial lies in the Mn-O plane and the structure retains the $P6_3cm$ -type symmetry, with 'up-down-down' In displacements, of the stoichiometric material. (c) and (d) show the calculated structure for one oxygen vacancy per 24 formula units. The oxygen vacancy is at the apex of a trigonal bipyramid and the In displacements reveal the resulting P3c1-type structure. The calculated lowest-energy structures for $InMnO_3$ containing indium vacancies are shown in (e) and (f), and for indium-oxygen vacancy complexes in (g) and (h). Both structures show an 'up-down-down' pattern of In displacements indicating $P6_3cm$ -type structures; in the vacancy complex case the In and O vacancies are directly above each other with the same x and y coordinates.

cases we take a tolerance threshold on the difference between Δ_z values of 0.002 Å.

Results

Oxygen Defects

To study the effects of oxygen vacancies and oxygen interstitials, we introduced single point defects into 2x2x1 supercells, containing 24 formula units, of the non-polar $P\bar{3}c1$ -type and polar $P\bar{6}_3cm$ -type structures. These supercells provide defect separations of ~ 12 Å which are sufficiently large for the interaction of periodic images to be neglected. ³⁹ We then relaxed the atomic positions and cell parameters. The magnetism was initialized to the collinear antiferromagnetic order described above and remained in that state. ³⁵

The formation of oxygen interstitials can be expressed by the defect reaction: 40

$$\frac{1}{2}O_2(g) + 2Mn^{3+} \to O_i^{2-} + 2Mn^{4+}$$
 (1)

where an oxygen interstitial O_i^{2-} is formally charge compensated by two holes on the Mn sublattice, such that one O_i^{2-} oxidizes two Mn³⁺ to Mn⁴⁺. Recent experimental work on oxygen-loaded hexagonal $RMnO_3$ (R = Ho, Er and Y), ³⁰ and a recent DFT study of interstitial oxygen in YMnO₃ ³⁹ indicate that oxygen interstitials occupy the Mn layer, consistent with the Mn ions' ability to change their oxidation state; we study this arrangement here. We performed two structural relaxations starting with the interstitial oxygen at two different symmetry-inequivalent positions in the Mn layer, with the coordinates $(\frac{1}{3}, \frac{1}{3}, \frac{3}{4})$ and $(\frac{2}{3}, \frac{2}{3}, \frac{1}{4})$. Both starting structures relaxed to the ferroelectric $P6_3cm$ -type structure of the stoichiometric material. Figs. 2(a) and (b) show the location of and structure with the lowest-energy oxygen interstitial, with initial location $(\frac{1}{3}, \frac{1}{3}, \frac{3}{4})$, which we found to be 0.1 meV per formula unit lower in energy than the other oxygen interstitial site; we note that both formation energies are rather low. It can be seen from Fig. 2(a) that the local environment of the oxygen

interstitial is perovskite-like with the Mn ions surrounding the vacancy now 6-coordinated with oxygen. The octahedra are strongly distorted, however, with Mn-O bond lengths in the three octahedra containing the interstitial varying between 1.90Å - 2.68Å, 1.87Å - 2.02Å and 1.85Å - 2.00Å. Here the smallest bond length in each octahedron is that of the Mn-interstitial. The 'up-up-down' pattern of In displacements can be seen in Fig. 2(b); we obtain $\Delta z_1 = 0.001$ and $\Delta z_2 = 0.036$.

The total- and orbital-resolved densities of states for stoichiometric $InMnO_3$ are plotted in Fig. 3 (a), and for the lowest-energy structure containing an oxygen interstitial in Fig. 3(b). We see that the insulating nature is maintained in the oxygen-interstitial containing structure, although the band gap is reduced to ~ 0.9 eV. As in the stoichiometric case, the valence band is mainly comprised of Mn d and oxygen p states, and we expect that oxidized $InMnO_{3+\delta}$ will show the same p-type semiconducting behavior observed in Seebeck measurements for the related hexagonal manganite $YMnO_3$. The formal oxidation of Mn to charge compensate oxygen interstitials lifts a fraction of the Mn d-states from below to above the Fermi energy.

Oxygen vacancy formation can formally be expressed by the defect reaction: 40

$$O_O^{2-} + 2Mn^{3+} \to V_O^{2+} + 2Mn^{2+} + \frac{1}{2}O_2(g)$$
 (2)

in which an oxygen vacancy V_O^{2+} is formally charge compensated by two electrons donated to the Mn sublattice, with each V_O^{2+} providing two electrons and reducing two Mn³⁺ ions to Mn²⁺. We calculated the structures and energetics of supercells containing in turn the three symmetry-inequivalent oxygen vacancies – two planar and one apical – for the $P\bar{3}c$ -type structure, and the four symmetry-inequivalent oxygen vacancies – two planar and two apical – for the $P6_3cm$ -type structure. We find that the lowest energy arrangement has an apical oxygen vacancy and is P3c1-type, as shown in Fig. 2(c), (d). This structure was calculated to be 1 meV/f.u. lower in energy than the lowest-energy $P6_3cm$ -type structure. Note that

the P3c1 structure has not been observed as a bulk phase in stoichiometric InMnO₃, but was recently reported at the walls separating the partially undistorted antipolar domains in the Ga-doped material. ¹⁵ Interestingly, in YMnO₃ planar oxygen vacancies are favored compared to apical. ²⁸ This difference may stem from the fact that In is significantly less electropositive than Y (1.78 vs 1.22 on the Pauling scale), resulting in weaker In-apical oxygen than Y-apical oxygen bonds.

The presence of an oxygen vacancy causes significant changes in the density of states, particularly near the Fermi level, as shown in Fig. 3(c). In particular, an impurity state derived primarily from O p states is formed in the gap, reducing the overall charge gap between the top of the valence band and the bottom of the impurity states to ~ 0.2 eV. Compared to stoichiometric InMnO₃, the Fermi level shifts to above the narrow d_z orbitals suggesting that InMnO_{3- δ} would be more likely to show n-type than p-type semiconducting behavior. Similar changes to the electronic structure have been observed experimentally for donor-doped YMnO₃. 41

Indium Vacancies

Indium vacancies can arise from evaporation of In during high-temperature growth or postprocessing, or through non-stoichiometry unintentionally introduced during the synthesis process. The corresponding defect reaction depends on whether $InMnO_3$ is present in an oxygen-rich or oxygen-poor environment, with distinctly different charge compensation. In oxygen-rich conditions the formation of one In vacancy is formally charge compensated by oxidation of three Mn ions. This can be expressed as the evaporation of gaseous (g) In from $InMnO_3$:

$$InMnO_3 \to In_{1-\delta}^{3+}Mn_{1-3\delta}^{3+}Mn_{3\delta}^{4+}O_3 + \delta In(g),$$
 (3)

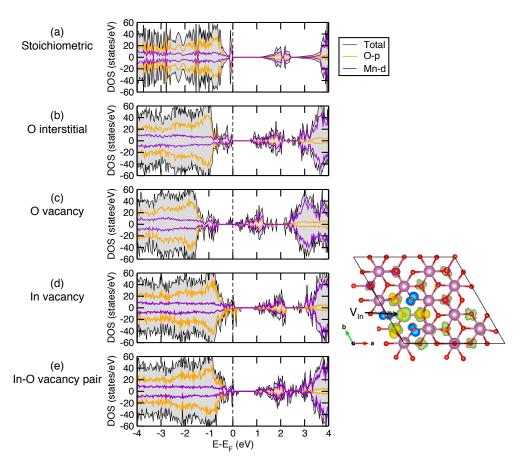


Figure 3: Calculated densities of states for (a) stoichiometric InMnO₃ and (b) - (e) the lowest-energy structures shown in Fig. 2 containing the following defects (each per 24 unit cells of InMnO₃): (b) one oxygen interstitial (c) one oxygen vacancy (d) one indium vacancy, and (e) one In-O vacancy pair. The grey shading shows the total density of states, the purple and orange lines the Mn-d and O-p states. The Fermi energy is set to 0 eV and marked by the dashed line. Alongside (d), the In vacancy density of states, we show the partial charge density in a region around the Fermi energy, which is localized in the Mn-d and O-p orbitals adjacent to the vacancy site.

or as In sub-stoichiometry introduced during synthesis, equivalent to Mn excess, which in Kröger-Vink notation corresponds to the following reaction:

$$\frac{1}{2}Mn_{2}O_{3} + 2Mn_{Mn}^{x} + \frac{3}{4}O_{2}(g) \xrightarrow{InMnO_{3}} V_{In}^{"''} + 3Mn_{Mn}^{\bullet} + 3O_{O}^{\times}$$
(4)

where $V_{In}^{""}$ is an In vacancy with a relative charge of -3, and Mn_{Mn}^{\bullet} indicates Mn oxidized to Mn^{4+} . In oxygen-poor conditions, In vacancies are charge compensated by oxygen vacancies:

$$InMnO_3 \to In_{1-\delta}^{3+}Mn^{3+}O_{3-\frac{3\delta}{2}} + \delta In(g) + \frac{3\delta}{4}O_2(g)$$
 (5)

which in Kröger-Vink notation becomes:

$$\frac{1}{2}\mathrm{Mn_2O_3} \xrightarrow{\mathrm{InMnO_3}} V_{\mathrm{In}}^{\prime\prime\prime} + \mathrm{Mn_{Mn}^{\times}} + \frac{3}{2}V_{\mathrm{O}}^{\bullet\bullet} + \frac{3}{2}\mathrm{O_2(g)}$$
 (6)

As constructing a cell for DFT calculations of In vacancies under oxygen-poor conditions would involve 5 vacancies – 2 V_{In} and 3 V_{O} – we choose instead to model an intermediate situation where one V_{In} is charge compensated by one V_{O} and the oxidation of one Mn ion, which is equivalent to mild hole doping. This situation corresponds to the following reaction:

$$InMnO_3 \to In_{1-\delta}^{3+}Mn_{1-\delta}^{3+}Mn_{\delta}^{4+}O_{3-\delta} + \delta In(g) + \frac{3\delta}{2}O_2(g)$$
 (7)

which is expressed in Kröger-Vink notation as:

$$\frac{1}{2}\mathrm{Mn_2O_3} + \frac{1}{4}\mathrm{O_2(g)} \xrightarrow{\mathrm{InMnO_3}} V_{\mathrm{In}}^{\prime\prime\prime} + \mathrm{Mn_{Mn}^{\bullet}} + \mathrm{O_O^x} + V_{\mathrm{O}}^{\bullet\bullet}. \tag{8}$$

To assess the structural stability upon introduction of In vacancies we perform calculations for both symmetry inequivalent In vacancies and a range of In-O vacancy pairs. As before we construct 2x2x1 supercells of the trimerized primitive unit cell, giving a sto-

ichiometry of $In_{0.958}MnO_3$ with one In vacancy, and $In_{0.958}MnO_{2.986}$ with an In-O vacancy complex.

For the In-vacancy-only case, we find that the lowest-energy position for an In vacancy is the site around which the trigonal bipyramids tilt away, as shown in Fig. 2. The lowest energy structure is polar $P6_3cm$ -type. We show the calculated density of states for this structure in Fig. 3(d) as well as the partial charge density plotted in an energy range of 0.3 eV on either side of the Fermi level. Interestingly for a polar structure, the indium vacancy causes the system to become metallic. From the partial charge density we see that the states at the Fermi level consist primarily of oxygen 2p states from the in-plane oxygen atoms directly above and below the In vacancy and the nearest Mn 3d orbitals. This suggests that the charge redistribution caused by the removal of the In atom is confined mostly to the region immediately surrounding the vacancy. Formally, a single In vacancy is charge compensated by three Mn⁴⁺, which is equivalent to strong hole doping of InMnO₃, resulting in a p-type metal.

To study the In-O vacancy pairs expected to from in less oxygen-rich conditions, we combine the two inequivalent In sites with three different oxygen sites, and calculate the structure and total energy of all six combinations. We find that the lowest-energy structure, shown in Figs. 2(g) and (h), is $P6_3cm$ -type, although close to the P3c1 phase, with the In z coordinates $\Delta z_1 = 0.002$ and $\Delta z_2 = 0.029$. The polar structure is ~ 6 meV/f.u. lower in energy than the non-polar $P\overline{3}c$ case. The O vacancy is in the plane, with the In vacancy directly below it; combinations with other O vacancies were all higher in energy. The corresponding density of states is shown in Fig. 3(e). We see that, as in the case of the In-only vacancy, the In-O vacancy pair induces metallicity. In this case, the states nearest to the Fermi level are mainly of in-plane oxygen character, with additional oxygen and manganese contributions. Since the vacant oxygen is an apical atom, the charge mainly redistributes to the in-plane oxygen states.

In Table 1 we summarize our calculations of the structure types so far. We see that

in each of the defect cases considered, the lowest energy state is polar, suggesting that the presence of In or O point defects is not detrimental to the formation of a polar state. In the case of In vacancies and In-O vacancy complexes, however, the ground state is metallic which will disfavor ferroelectric switching of the polarization due to the associated screening of any applied electric field.

It was established in earlier work 10,15 that the nature of domain formation in hexagonal manganites, in particular the width of domain walls and the concentration of domain wall intersections, is dependent on the details of the energy barrier connecting polar and non-polar states. In particular, the different polar domains in the $P6_3cm$ ground state are separated by non-polar $(P\bar{3}c)$ domain walls. Conversely, the non-polar domains in the $P\bar{3}c$ structure have polar domain walls. The pathway between the polar and non-polar states corresponds to the variation of tilt angle, ϕ , from 0 to 30°, around the 'brim' of the Mexican-hat-shaped potential energy surface that characterizes the symmetry-lowering phase transition. ¹³ To estimate the effect of point defects on this energy path in InMnO₃, we calculated the energy difference between the polar $P6_3cm$ -type ($\phi = 60^{\circ}$) and the centrosymmetric $P\bar{3}c$ -type ($\phi = 30^{\circ}$) structures first for the stoichiometric compound and then for the various defect combinations. Consistent with Ref., 15 for our choice of exchange-correlation functional the $P\bar{3}c$ structure is highest energy and the polar $P6_3cm$ structure lowest in energy for the stoichiometric compound, with an energy difference of $\sim 4 \text{ meV/f.u.}$. This energy difference increases to ~ 6 meV/f.u. with the inclusion of In-O vacancy pairs. For the other three cases – O interstitials, O vacancies and In vacancies – both the nonpolar and polar initialized structures relaxed to polar space groups. This suggests that the inclusion of any defect will tend to stabilize a polar structure adopting either the $P6_3cm$ or P3c1 symmetry.

Ga Substitution

For studies of Ga-Mn alloying we used a supercell containing 6 formula units (30 atoms) and replaced between zero and 6 Mn atoms with Ga, resulting in Ga concentrations of 0%,

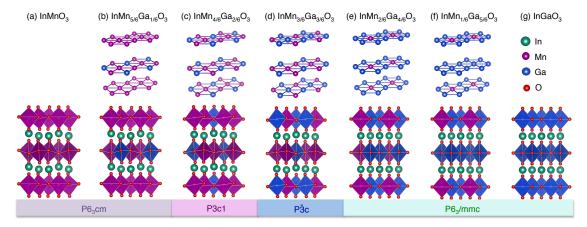


Figure 4: Calculated lowest-energy Mn-Ga orderings (top panel) and structures (lower panel) for $InMn_xGa_{1-x}O_3$. We see an evolution from the polar $P6_3cm$ symmetry of stoichiometric $InMnO_3$ to the paraelectric $P6_3/mmc$ symmetry of $InGaO_3$ via polar $P6_3cm$ - and P3c1-type to non-polar $P\bar{3}c$ -type and non-polar $P6_3/mmc$ -type as a function of increasing Ga concentration.

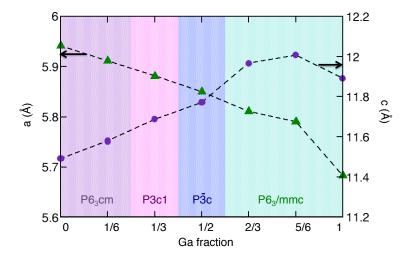


Figure 5: Calculated lattice parameters as a function of Ga concentration for the lowest-energy $In(Mn,Ga)O_3$ alloy structures. The left y-axis shows the in-plane lattice parameter, a, and the right y-axis the out-of-plane lattice parameter, c, both for 30 atom unit cells. The different structure types are indicated.

16.67%, 33%, 50%, 66.67%, 83.33% and 100%. For each concentration of Ga, all symmetry-inequivalent combinations of sites for substitution allowed by the choice of supercell were calculated. We note that the nearest-neighbor in-plane interactions between the Mn spins remain antiferromagnetic, but we expect the overall ordering magnetic ordering temperature to decrease with increasing Ga concentration due to the dilution of the magnetic ions.

Structure

Table 2: Calculated total energies relative to that of the $P6_3cm$ -type structure for the lowest-energy (Mn,Ga) arrangements of In(Mn,Ga)O₃. The energies shown are per 5 atoms. Note that for 1/3 Ga, both $P6_3cm$ - and $P\bar{3}c$ -type starting points relaxed to P3c1-type symmetry.

Ga fraction		Energy (meV/f.u.)	
	$P6_3cm$	$P\bar{3}c$	$P6_3/mmc$
0	0	4.30	45.88
1/6	0	1.45	30.13
1/3	_	_	15.01
1/2	0	-0.07	5.49
2/3	0	0.02	-0.43
5/6	0	0.37	-0.02
1	0	-0.07	-0.11

The calculated lowest-energy arrangements of the Mn and Ga ions for each alloy concentration are shown in the top panel of Fig. 4 with the relaxed structures shown below. We see an evolution from the $P6_3cm$ structure of InMnO₃ through polar P3c1- and non-polar $P\bar{3}c$ -types to the high symmetry paraelectric P63/mmc structure of InGaO₃. The calculated energy differences between the $P6_3cm$ -, $P\bar{3}c$ - and $P6_3/mmc$ -type structures are given in Table 2.

With one Ga atom in the unit cell (1/6 Ga), Fig 4(b), the structure retains the polar $P6_3cm$ -type structure of stoichiometric InMnO₃. The energy difference between the ferroelectric $P6_3cm$ -type and non-polar $P\bar{3}c$ -type symmetries is reduced, however, from ~ 4 meV/f.u. for stoichiometric InMnO₃ to ~ 1 meV/f.u. with 1/6 Ga. With two Ga atoms per

unit cell (1/3 Ga), we find that the Ga atoms separate as far as possible spatially, and both the $P6_3cm$ -type and $P\bar{3}c$ -type initialized structures relax to the polar P3c1-type structure (Fig 4(c)). When half of the Mn ions are replaced by Ga, it is lowest energy for two Ga ions to occupy one layer with the third in the second layer (Fig 4(d)). The resulting structure is non-polar $P\bar{3}c$ -type with the In ions displacing in the 'up-none-down' pattern; the $P\bar{3}c$ structure is ~ 0.1 meV/f.u. lower in energy than the $P6_3cm$ -type. With four Ga atoms in the unit cell, (2/3 Ga), the lowest-energy structure has two Ga atoms in each layer and adopts the high-symmetry $P6_3/mmc$ -type structure of the 5/6 substituted composition and of InGaO₃ (Fig. 4(e, f and g)).

Fig. 5 shows our calculated lattice parameters for the different Ga fractions. As the percentage of Ga increases, we find that the a lattice parameter decreases from ~ 5.89 Å to ~ 5.71 Å while the c lattice parameter increases, as expected from the lattice parameters of stoichiometric InMnO₃ and InGaO₃. This is consistent with experiments on solid solutions of InMn_{1-x}Ga_xO₃, ⁴² which report the in-plane lattice parameter decreasing with x from ~ 5.88 Å to ~ 5.73 Å and the out-of-plane lattice parameter increasing from ~ 11.50 Å to ~ 12.05 Å. The decrease in a lattice parameter is explained by the larger Shannon-Prewitt radius of five-coordinated Mn³⁺ (0.58 Å) than Ga³⁺ (0.55 Å). ⁴³ The increase in the out-of-plane lattice parameter is likely due to filling of the d_{z^2} antibonding states with increased Ga content, causing an increase in the apical Mn-O bond length and a reduction in tilting. This effect also contributes to the stabilization of the untilted $P6_3/mmc$ structure for $x \geq 0.6$.

Electronic Structure

The calculated band gaps for the lowest energy structures as a function of Ga content are shown in Fig. 6. We see that the materials are insulating for all Ga concentrations, with the band gap increasing from ~ 1.1 eV for stoichiometric InMnO₃ to 2 eV for stoichiometric InGaO₃. In between the end-point compounds the behavior is not monotonic, likely due to the ordered supercells used in our calculations.

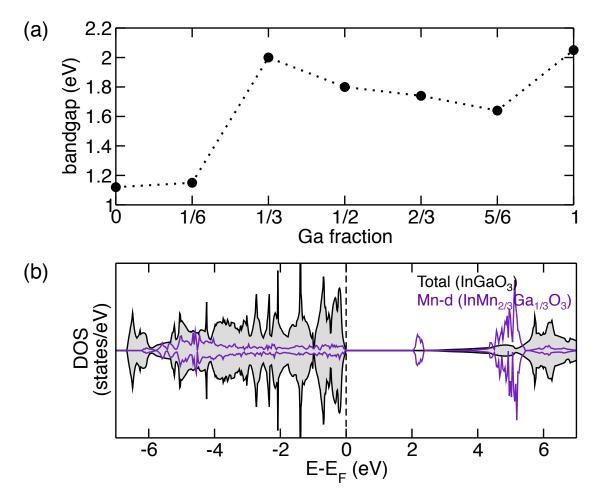


Figure 6: (a) Calculated band gap for the $In(Mn,Ga)O_3$ series as a function of Ga content. The end points (0 and 1 Ga fraction) correspond to the stoichiometric $InMnO_3$ and $InGaO_3$ compounds respectively. (b) Electronic densities of states calculated for stoichiometric $InGaO_3$ (black line, grey shading) with the Mn-d states of $InMn_{2/3}Ga_{1/3}O_3$ superimposed in purple.

The effect of Mn-site alloying on the electronic structure was studied previously for $Y(In,Mn)O_3$, ⁴⁴ where it was found that materials with substantial In content were a vibrant blue color. This was explained by the combination of the wide band gap of YInO₃, and the narrow Mn d_{z^2} crystal field level within the gap, which absorbs with a symmetry-allowed transition in the red region of the spectrum. In Fig. 6(b) we show the calculated density of states of InGaO₃ (black line, shaded) with its large 2eV gap, with the Mn-d states of InMn_{2/3}Ga_{1/3}O₃ superimposed in purple. The narrow mid-gap d band is clearly visible. A previous correlation ⁴⁴ was noted between the energy of the d_{z^2} states with respect to the top of the valence band and the Mn-O apical bond length, with an optimal value of 1.89 Å for the most intense blue color. In our system, Ga-doping varies this apical bond length between 1.91 Å for InMnO₃, to a maximum of 1.97 Å for 1/2 Ga doping, dropping back to 1.90 Å in InGaO₃. These similiarities suggest the In(Mn,Ga)O₃ series as a potential system for exploring new blue chromophores.

Discussion

Our first finding is that the presence of oxygen and indium point defects does not disfavor polar behavior in InMnO₃, with most combinations maintaining the $P6_3cm$ -type structure of the stochiometric compound, or in the case of oxygen vacancies the lower-symmetry P3c1-type. The a and c lattice parameters also change only slightly (less that \sim 0.1Å.) For the In-O vacancy pair, the energy difference between the ferroelectric and paraelectric phases even increase compared with the stoichiometric case from \sim 4 meV/f.u. to \sim 6 meV/f.u. In contrast, gallium alloying on the manganese site significantly influences the ground state crystal structure, with a polar phase ($P6_3cm$ -type and then P3c1-type) favored up to a Ga concentration of \sim 40%, followed by the low-symmetry non-polar $P\bar{3}c$ -type structure for Ga concentrations of \sim 40%-60%, with the high-symmetry, untilted paraelectric $P6_3/mmc$ phase stabilized for higher concentrations. Our calculations are consistent with recent HAADF-

TEM studies of In(Mn,Ga)O₃. ¹⁵

The evolution of the structure can be rationalized in terms of the change in the lattice parameters caused by substitution of Ga. With increasing Ga concentration, the a lattice parameter smoothly decreases, consistent with the slightly smaller ionic radius of Ga, while c increases, reflecting a reduction in the magnitude of polyhedral tilting and reducing the O 2p-In 5s covalency; this has been previously shown to favor the polar over the non-polar state. ¹⁴ In contrast, YMn_{1-x}Ga_xO₃ does not show a structural phase transition, retaining $P6_3cm$ symmetry throughout the entire Ga doping range. ^{45,46} Note that transitions from hexagonal $P6_3cm$ to perovskite structure have been reported for YMn_{1-x}Ti_xO₃ at $x = 0.2^{47,48}$ and for YMn_{1-x}Fe_xO₃ at x = 0.3. ⁴⁹

The various defects and dopants have pronounced effects on the electronic structure of the material, most notably on the band gap. The density of states with oxygen interstitials and oxygen vacancies remains gapped, however the band gap is reduced from 1.2 eV to 0.9 eV and 0.2 eV respectively. For both the indium-only vacancy and the indium-oxygen vacancy pair, the material becomes metallic, with the states at the Fermi level being of O-p character. In the latter cases, the ground state is thus both polar and metallic. Careful control of the point defect population may thus be an alternative to heteroepitaxial engineering 50 for designing polar metals. Our calculations shows that $YMn_{1-x}Ga_xO_3$ is an insulator throughout the whole doping range, with the band gap varying between 1.1 eV and 2 eV. This variation in band gap – related to the apical Mn-O bond length – could result in interesting optical properties and offers it as a potential alternative for studying new blue pigments in the hexagonal manganite class.

From an experimental point of view, In vacancies and substitutional Ga are 'irreversible defects', meaning that once introduced during synthesis or processing of the materials, they can not be eliminated or easily created. In contrast, point defects only involving oxygen ions are 'reversible defects', meaning that they can be created or removed by carefully controlling the thermal and atmospheric history of a sample. Low temperature and high p_{O_2} will favor

oxygen interstitials, 29,30,39 while high temperature and low p_{O_2} will promote oxygen vacancy formation. 40 Oxidizing or reducing ${\rm InMnO}_{3\pm\delta}$ pushes the intrinsic anti-Frenkel equilibrium $K_F = [V_O^{**}][O_i'']$ towards predominantly vacancies or interstitials. We propose that the strong coupling between defect chemistry and physical properties such as polar versus non-polar or insulating versus metallic character indicated by our calculations constitutes an avenue of opportunities for manipulating the properties of indium manganite. Studies of other hexagonal manganites show significant oxygen mobility down to 150 to 250 °C, depending on the R^{3+} cation, 29,30 while low temperature topotactic reduction of YMnO $_{3-\delta}$ has been demonstrated at 225 °C. We propose, for example, that In-deficient $In_{1-x}MnO_{3.00}$, which we find to be a polar metal, could be rendered locally insulating by lithography and local topotactic reduction of the oxygen content. A related possibility is to use $In_{1-x}MnO_{3\pm\delta}$ as a memristive material in contact with an oxygen reservoir. Additionally, since semiconducting ${\rm InMnO}_{3\pm\delta}$ can accommodate both oxygen vacancies and interstitials, the majority charge carriers can easily be tuned to be electrons or holes, respectively. Oxygen defects could therefore be used to reversibly create or remove p-n junctions, which should occur where local gradients in oxygen stoichiometry cross $\delta=0$.

Conclusions

We have shown using first-principles calculations that the relative stability of the polar and non-polar phases of $InMnO_3$ is strongly affected by the introduction of oxygen point defects, indium vacancies, indium-oxygen vacancy pairs and Ga substitution. Polar phases are favored for all investigated intrinsic point defects. The electronic properties of $InMnO_3$ can be made insulating, metallic, or close to n-type or p-type semiconducting by controlling the point defect population. The In layer corrugation indicates that the polar $P6_3cm$ -type structure of the stoichiometric material, remains the ground state with the inclusion of oxygen interstitials and with In vacancies and In-O vacancy pairs. Single oxygen vacancies

favor the polar low-symmetry P3c1-type structure, while the centrosymmetric $P\bar{3}c$ -type structure was not stabilized by any of the investigated intrinsic point defects. With increasing Ga concentration in $InMn_{1-x}Ga_xMnO_3$, the structural ground state evolves through the sequence polar $P6_3cm$ -type - polar P3c1-type - non-polar $P\bar{3}c$ -type - non-polar $P6_3/mmc$ -type. Our results point to the use of point defect chemistry as a handle for designing or modifying the structural properties of complex oxides.

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