

The Efficiency of a Mewis Duct in Waves

Rolf Arild Topphol

Marine Technology (2 year) Submission date: June 2013 Supervisor: Sverre Steen, IMT

Norwegian University of Science and Technology Department of Marine Technology



Title:	Delivered:
The Efficiency of a Mewis Duct in Wayes	06.06.2013
The Efficiency of a Mewis Duct in Waves	Availability:
	Open
Student:	Number of pages:
Rolf Arild Topphol	72

Abstract:

In this thesis, the efficiency of a Mewis Duct in waves has been investigated with the use of model tests in the large towing tank at MARINTEK in Trondheim. A "load-varying" self-propulsion method was used, allowing for calculations without the need for results from a resistance test. Still water, regular and irregular wave conditions have been tested. The vessel model used, M3030 A, was originally used to test the Mewis Duct in still water.

Results in still water have been compared to the original test results. Deviations from the original tests have been found, which could be due to increased resistance of the model and bias in the tow force and thrust measurements.

Results in regular waves show a consistent increase in the effective wake with the Mewis Duct fitted, but the thrust deduction contains a high amount of scatter. This results in scatter in the hull efficiency, and further in the propulsive efficiency.

Uncertainty analysis has been carried out and shows that scatter in the tow force are probably the reason for inaccurate results. It indicates the necessity of accurate measurements of the tow force with the loadvarying self-propulsion method.

Keyword:

Mewis-Duct

Efficiency

Wake

Address: NTNU Department of Marine Technology N-7491 Trondheim Location Marinteknisk Senter O. Nielsens vei 10

Advisor:

Sverre Steen

Tel. +47 73 595501 Fax +47 73 595697

Sammendrag

I denne avhandlingen, har effekten av en "Mewis Duct" i bølger blitt undersøkt ved hjelp av modellforsøk i den store modelltanken ved MARINTEK i Trondheim. En "last-varierende" propulsjonsmetode ble tatt i bruk, som gjør at beregninger kan bli foretatt uten behovet for data fra motstandstester. Propulsjon i stille vann, regelmessige og uregelmessige bølgeforhold har blitt foretatt. Modellen benyttet, M3030 A, ble opprinnelig brukt til modellforsøk av "Mewis Duct" i stille vann.

Resultater fra stille vann har blitt sammenlignet med de opprinnelige testresultatene. Avvik fra de originale testene har blitt funnet, noe som kan skyldes økt motstand av modellen og bias i thrust- og momentmålinger.

Resultater i regulære bølger viser en konsekvent økning i medstrøm med "Mewis Duct" montert, mens thrustreduksjonen inneholder høy spredning. Dette resulterer i spredning i skrogvirkningsgraden, og videre i propulsjonsvirkningsgraden.

En usikkerhetsanalyse er gjennomført og viser at spredning i slepekraften trolig er årsaken til unøyaktige resultater. Det indikerer nødvendigheten av nøyaktige målinger av slepekraft med den last-varierende testmetoden.

MASTER THESIS IN MARINE TECHNOLOGY

SPRING 2013

FOR

Rolf Arild Topphol

The efficiency of a Mewis duct in waves

Both due to environmental concerns and increasing fuel prices there is an increasing demand for energy saving in the international shipping fleet. Thus, there is a renewed interest in so-called energy saving devices. There is a large sub-group of these devices which are related to the propeller and the area around the propeller, and the current project focus on this sub-group. An example of such a device, which has gotten quite a lot of attention and some popularity in the market recently, is the socalled Mewis duct, which is a combination of a wake-equalizing duct and pre-swirl fins. Power-saving in the order of 5% is reported, but mainly in calm water. The most reliable estimates of power saving are obtained in very carefully executed model tests, and so far these have been performed only in calm water. However, it is known that when the ship operates in waves the flow into the propeller changes quite significantly. Thus, it is expected that waves might influence the efficiency of the Mewis duct. Therefore, the objective of the master thesis is to investigate and document through model testing how the efficiency of a Mewis duct change when subject to waves. The primary activity will be a model test of one particular vessel, belonging to Solstad Shipping. The model test will be carried out in the spring term, as part of the master thesis. The master thesis is a part of the research project Energy Management in Practice II (EMIP II).

The master thesis should address the following issues:

- Give a short introduction to the Mewis duct, and how it compares to other energy devices. Document what is known about efficiency gain with use of Mewis duct.
- Discuss how speed loss and change of propulsive factors due to waves can be assessed, in general and in particular by using model tests.
- Make a detailed plan for the model tests
- Co-operate with the workshop and laboratories at MARINTEK in the preparations for the tests.
- Perform the model tests with assistance from technicians from MARINTEK and/or NTNU.
- Analyze the model test results to determine the influence of waves on the efficiency of the Mewis duct. Also determine the efficiency of the duct in calm water with the current set-up as a necessary reference.
- Discuss and conclude regarding how waves influence the efficiency of a Mewis duct.

In the thesis the candidate shall present his personal contribution to the resolution of problem within the scope of the thesis work.

Theories and conclusions should be based on mathematical derivations and/or logic reasoning identifying the various steps in the deduction.

The candidate should utilize the existing possibilities for obtaining relevant literature.

The thesis should be organized in a rational manner to give a clear exposition of results, assessments, and conclusions. The text should be brief and to the point, with a clear language. Telegraphic language should be avoided.

The thesis shall contain the following elements: A text defining the scope, preface, list of contents, summary, main body of thesis, conclusions with recommendations for further work, list of symbols and acronyms, reference and (optional) appendices. All figures, tables and equations shall be numerated.

The supervisor may require that the candidate, in an early stage of the work, present a written plan for the completion of the work. The plan should include a budget for the use of computer and laboratory resources that will be charged to the department. Overruns shall be reported to the supervisor.

The original contribution of the candidate and material taken from other sources shall be clearly defined. Work from other sources shall be properly referenced using an acknowledged referencing system.

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Supervisor: Professor Sverre SteenStart: 14.01.2013Deadline: 10.06.2013

Trondheim, 18.01.2013

Sverre Steen Supervisor

Preface

This master thesis is a part of the fulfillment requirements to obtain the degree of Master of Science in Marine Technology from the Norwegian University of Science and Technology (NTNU). The work was carried out in the spring semester in 2013.

The thesis is alloo part of the research program Energy Management in Practice II (EMIP II) which seeks to reduce fuel consumption and thus CO2 emission through improving energy efficient ships in a practical and cost efficient way. I would like to thank the participants for providing information regarding the Mewis Duct and for the constructive feedback in the session in the middle of the semester.

I would like to thank the students who I share office space with, who are all in the same situation and responsible for a positive work environment. They have also helped with technical insight of the softwares used in the thesis, MATLAB, Excell and Word.

The technicians I worked with for the model tests in the MARINTEK towing tank have been helpful, and I want to thank them for an interesting, educational and pleasant stay.

Last I would like to thank my supervisor Prof. Sverre Steen for all the help and constructive feedback he have given me during the semester.

Trondheim, June 6th, 2013

Rolf Arild Spolar

Rolf Arild Topphol

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Nomenclature

Symbols

$\eta_{\scriptscriptstyle D}$	Propulsive efficiency	V	Velocity in general
η_0	Open water efficiency	U	Velocity in general
$\eta_{\scriptscriptstyle H}$	Hull efficiency	F_D, F	Tow-rope force
$\eta_{\scriptscriptstyle R}$	Polotivo rotativo officionav	R_{T}	Resistance
n	Relative lotative efficiency	L	Length unit
η_i	Ideal efficiency	λ	Scaling factor
η_r	Efficiency accounting for	Δp	Pressure gradient
	fluid rotation	η_i	Motion amplitude in degree
$\eta_{_f}$	Efficiency accounting for		of freedom i
	blade friction	$C_{\scriptscriptstyle B}$	Block coefficient
ζ_{mom}	Momentum loss	h	Distance between propeller
C_T	Thrust loading coefficient		shaft center and water
Т	Thrust		surface
Q	Torque	β	Thrust diminution factor
Р	Power	$\eta_{{ m R}\zeta}$	Relative vertical motion
K_{τ}			amplitude
K	I nrust coefficient	F_n	Froude number
\mathbf{R}_{Q}	Torque coefficient	R_n	Reynolds number
n	Propeller revolutions	m	Empirical constant
W	Wake fraction	r	Radius of gyration
W _p	Potential wake	ρ	Mass density
t	Thrust deduction	g	Acceleration of gravity
<i>t</i> *	"True" thrust deduction	Wave data	
k	Form factor	ζ_a	Wave amplitude
J_A, J_0, J	Advance ratio	λ	Wave length
A_{P}	Propeller disk area	ω	Circular frequency
D	Propeller diameter	ω_{0}	Wave circular frequency
R	Propeller radius		

ω_{e}	Circular frequency of	Х	True value for which
	encounter		uncertainty is sought
	ω^2	$\mathbf{Y}_{\mathbf{i}}$	Parameters which X
K	Wave number $\frac{w}{g}$		depends on
Н	Wave height	ΔY_i	Error of parameter Y _i
Т	Period	X	Resultfrom the measurement
Symbols in uncertainty analysis		κ_{i}	Influence coefficient
S	Standard deviation	е.	Elemental error
n	Number of observations	P	Combined error
q_k	Observed quantity	e Sub-indio	ces
\overline{q}	Mean value	m	Model
Р	Precision limit	S	Ship
t	Weight from Student's t		
	distribution		

1 Introduction

Considering the continuously rising fuel oil prices and the increasing awareness of the environmental conditions, energy saving is of high priority, and Energy Saving Devices (ESD) for propellers and propulsors has gained renewed attention. ESD's are flow-directing devices placed near or at the propeller. These can either be active systems, such as contra-rotating propellers and the Grim vane wheel, or passive systems such as various ducts and tunnels, fins and fin systems and rudder bulbs.

The Mewis Duct is an ESD placed in front of the propeller, and is targeting individual loss factors by combining two different principals to reduce the energy loss. The duct is built up by two components; a wake-equalizing duct for equalization of the flow created by the hull towards the propeller, and a set of pre-swirl fins to generate a swirl in the flow in the opposite direction of the propeller to reduce the rotational losses. The duct to propeller radii is also optimized to create a higher loading at the inner radii of the propeller area to reduce the hub-vortices.

The Mewis Duct have been model tested in several model tank facilities, and energy savings in the order of 5% have been reported depending on vessel type and loading condition. Former tests have only been conducted in still water conditions, and due to what is known about added resistance, speed loss and change of propulsive factors in waves it have been questioned whether such benefit is present in waves. Especially the modification of the wake field in waves is expected to be of importance as it is an important part of the Mewis Duct. Full scale trials of the Mewis Duct have also been carried out, with varying or inconclusive results, which can either come from inaccurate measurements, or that there is a cancelation of the efficiency gain in waves. In an attempt to aquire accurate data regarding the efficiency in waves, model self-propulsion tests is conducted, with and without the Mewis Duct fitted, in the large towing tank at MARINTEK in Trondheim, Norway.

Since the expected energy saving with the Mewis Duct is in the order of 5% and could be smaller or even canceled in waves, a careful execution of the model test setup is of importance. The conditions tested should be as equal as possible with and without the Mewis Duct fitted to obtain comparable results.

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This master thesis is part of the project Energy Management in Practice phace II (EMIP II), which stand for the financing of the model tests conducted at MARINTEK. The EMIP II project is controlled by the socalled WG 5 cooperation, consisting of 5 shipping companies; Klavness Ship Management AS, Wilh. Wilhelmsen AS, BW Gas AS, Grieg Star Shipping AS and Solvang ASA. The project group have also joined forces with MARINTEK. It is a User controlled Innovation Project (UIP) supported by the Research Council of Norway, with a budget of 10.5 MNOK and the period of execution started September 2011 and is planned finished September 2013. The goal of the project is to reduce fuel consumption and thus CO2 emission through improving energy efficient ships in a practical and cost efficient way as a contribution towards the NSA environmental vision "zero harmful emissions to air and sea".

2 Working Principles of Energy Saving Devices

A more comprehensive literature study of the topic in this section was carried out in the project thesis in the fall semester of 2012, Topphol (2012).

2.1 Energy Loss around a Rotating Propeller

To understand the working principles of the Mewis Duct and other energy saving devices in general, knowledge of the energy losses the devices target to improve is needed. Around a working propeller behind the stern of a ship there are many factors contributing to energy loss, and hence a loss of propulsive efficiency. The losses around a rotating propeller can be divided in axial losses considering the ideal efficiency, rotational losses in the slip-stream rotation, hub vortices and tip vortices, frictional losses due to the roughness of the propeller blades and other propulsor parts and appendages and the losses related to the propeller to hull interaction effects.

According to Molland et al. (2011) the effects on the various components of the quasipropulsive coefficient η_D need to be considered:

$$\eta_D = \eta_0 \eta_H \eta_R \tag{2.1}$$

where η_0 is the open water efficiency, η_H is the hull efficiency and η_R is the relative rotative efficiency.

 η_0 can be considered made up of:

$$\eta_0 = \eta_i \eta_r \eta_f \tag{2.2}$$

Here η_r accounts for losses due to fluid rotation induced by the propeller, and η_f accounts for losses due to blade friction drag. The breakdown of the components will indicate where savings can be made.

2.1.1 Axial Loss

For high propeller loadings, the axial loss is the largest factor, and is due to the axial velocity increase required for thrust generation. The axial loss is calculated according to Steen (2012):

$$\zeta_{mom} = 1 - \eta_i \tag{2.3}$$

Based on axial momentum theory the loss expressed through the ideal efficiency is derived as:

$$\eta_i = \frac{2}{1 + \sqrt{1 + C_T}} \tag{2.4}$$

where the thrust loading coefficient C_T is defined as:

$$C_T = \frac{T}{\frac{1}{2}\rho A_P V^2}$$
(2.5)

where A_p is the propeller disk area and T is the thrust.

2.1.2 Rotational Loss

Rotational losses are due to the induced tangential and swirling velocities in the slip-stream of the propeller which leads to lost kinetic energy. These losses can be reduced by reducing the swirl, either by pre-swirling the flow in the opposite direction towards the propeller, or to convert the swirling velocities behind the propeller to axial velocities and by that generating thrust.

2.1.3 Frictional Loss

Frictional losses are due to the frictional resistance of the propeller blades and other components, like ducts or fins. The losses from frictional resistance on the blades are a significant contribution due to the high velocities involved. It is important to consider especially when the propeller loadings are low.

2.1.4 Hull Interaction Losses

Hull interactional losses are a very complex and not very precise form of loss contribution, and more or less results in the three types of losses described above. The most important contributions to this are the thrust deduction and the wake from the hull. The average wake tends to increase the propeller efficiency, but inhomogeneous wake will be a problem because it will lead to an uneven propeller loading which again can lead to cavitation and vibration. An uneven wake will also lead to losses because the acceleration of the flow through the propeller disk will be uneven, which relates to momentum losses. It also requires a larger margin against cavitation, which is typically requiring a larger blade area and hence increased frictional resistance.

2.2 Energy Saving Devices

An "Energy Saving Device" (ESD) for propulsion is a device placed at or near the propeller to increase its efficiency by targeting the energy losses explained in the previous section. There are a large variety of such devices on the market, and a brief discussion of the most common follows in this section.

2.2.1 Ducts and Tunnels

Various ducts and tunnels are a common form of ESD. The Schneekluth Wake-Equalizing Duct, Schneekluth (1986), is placed immediately in front of the propeller. It aims to reduce the amount of separation over the after body, by accelerating the flow in the upper part of the propeller disc which establish a more uniform inflow, and attempting to minimize the tangential velocity components in the wake field. The main effect on more slender ships is homogenous flow and vibration reduction. Power savings up to 4% have been registered for C_T =5, Mewis (2010). Stern tunnels, the Hitachi Zosen nozzle and integrated ducted propeller are other examples of devices developed to target improvement of the wake field, Carlton (2007). Originally, ducts were not applied to increase the efficiency, but to reduce the propeller induced vibrations by reducing the wake peak effect of pronounced V-form hulls. Ducts can also be subcategorized in axisymmetric ducts and asymmetric ducts (to compensate for uneven and inhomogeneous wake).

A propeller duct placed at the propeller increases the efficiency of highly loaded propellers, but also increases the risk of cavitation. Its frictional resistance also means that it is inefficient on low propeller loadings. Decelerating ducts are also used to reduce the risk of cavitation.

2.2.2 Fins and Fin Systems

Fins and fin systems are placed either in front of the propeller or on the rudder. They aim to convert vertical velocity to thrust, reducing the rotational losses. placed immediately in front of the propeller. Fins placed behind the propeller on the rudder, the boss cap or a rudder bulb aim to reduce the hub vortex losses. Thrusting fins placed on the rudder, such as the Hyundai Thrust Fin system, reduces the hub vortex losses, but can also reduce the overall tangential velocities. Fins and fin systems in front reduces the rotational losses by pre-swirling the flow into the propeller. The SVA-Pre Swirl Fin, the DSME-Pre Swirl System and reaction fins are such devices. Reaction fins is a system normally built up of six radially located fins reinforced by a slim ring nozzle. Propeller tip end-plates, Carlton (2007), suppress the tip vortices, but at

the cost of high drag due to the high tip-velocity of propellers, and it are not certain that the concept will increase the efficiency. The Kappel propeller utilizes this concept, Mewis (2009).

2.2.3 Rudder Bulbs

Rudder bulbs behind the propeller aim to reduce the hub vortex losses and also increase the thrust due to the displacement effect of the bulb, which eliminates the drag force on the hub and gives increased velocity in the slip-stream. Examples of rudder bulbs are the Costa-bulb, Mewis (2010), the Propac rudder with bulb from Värtsilä and the Promas system, Rolls Royce (2009), from Rolls-Royce Marine. The Promas system is also integrated with a twisted rudder to reduce the rotational losses. Efficiency gains up to 10% have been registered for such devices.

2.2.4 Rotating Devices

The contra-rotating propeller, Mewis (2010), developed in 1836 is a very efficient device to regain the tangential velocities in the slipstream. The downside of it is that it is very costly. Power savings up to 14% for C_T =5 have been registered.

The Grim vane wheel, Carlton (2007), from 1966 uses the rotational velocity in the slipstream to run a "turbine", which also has a propeller portion on the tips of the turbine wheel for generation of extra thrust. The device increases the total diameter of the propeller, and the turbine wheels are easily damaged due to the long and slender form.

2.2.5 Combination of Principles

Often the various energy-loss sources can be handled independent by combining different principles to develop new devices. Some of the above mentioned devices are such combinations. Examples are boss cap fins, the Grim vane wheel, the counter rotating propeller and the Promas system. The Mewis Duct tested in this thesis is also a combination of principles.

3 The Mewis-Duct

The Pre-Swirl Duct (PSD) marketed under the trademark "Mewis Duct" is named after the developer Friedrich Mewis, and developed in cooperation with Becker Marine Systems in Hamburg. It is an energy-saving device placed in front of the propeller, and a combination of a wake equalizing duct and a pre-swirl fin system. It is suited to single-screw vessels with high block coefficient and speeds up to 20 knots, such as tankers and bulk carriers of all sizes, and multi-purpose carriers and container-feeder vessels. A principle sketch of the PSD is shown in Figure 1 below.



Figure 1 Principle sketch of the Mewis-Duct, Mewis and Guiard (2011)

3.1 Design

The purpose of the PSD is to target and improve three components of the propeller flow:

- 1. Equalization of the wake inflow
- 2. Reduction of rotational losses in the slipstream
- 3. Higher load at the inner radii of the propeller for reduction of the hub-vortices

The duct component equalizes the wake created by the ship hull. It is vertically offset, above the propeller shaft axis to distribute the wake equally in the upper region of the propeller area, and to distribute the wake race of the duct through a wider range towards the propeller. The duct component works as an endplate for the fins, suppressing tip-vortices from them. The effect from the increased loading on the inner radii of the propeller increases with the hub to propeller diameter ratio. The pre-swirl fin system reduces the rotational losses. It is set up with asymmetrical arranged fins to consider the shape of the ships wake. An upward turning blade will mainly work with the wake flow, and downward turning blades are working against it, hence to get the desired pre-swirl it is required more blades turning upwards than downwards.

3.2 Power Saving

The best possibilities for improvement are present when the thrust coefficient C_T is high and the velocity of the ship is relatively low, as can be seen from in Figure 2 taken from Mewis (2009).

The thrust coefficient is defined as:

$$C_T = \frac{T}{\frac{1}{2}\rho A_P V^2} \tag{3.1}$$

where T is the thrust, ρ is the water density, A_p is the propeller disk area and V is the velocity of the vessel.

Because of that, the PSD is best suited for smaller container vessels, small vessels with high block coefficient, such as multi-purpose carriers, and bulk carriers and tankers of all sizes. At the present stage of development the PSD is not well suited for high speed vessels, including large container vessels.



Figure 2: Possible power reductions by the PSD, Mewis (2009)

3.3 Model Test Results

Up until May 2012, as many as 48 projects in 8 model tanks was conducted with and without the Mewis Duct, with an average power-saving of 6.3%, Mewis (2012). Figure 3 below presents the power savings obtained from these propulsion tests, including design draught and ballast draught. The tabulated results can be found in appendix E.



Power reduction by Mewis Duct® - Model test results

Figure 3: Power savings with Mewis Duct from propulsion tests, Mewis (2012)

3.4 Full Scale Trial Results

Full scale trials has also been conducted with the Mewis Duct. These have not all shown conclusive results. It has been discussed if this could be due to cancelation of the effect in waves, but might be a result of high uncertainty in the measurements.

Full scale trial results without and with the Mewis Duct was conducted in October 2010 for a bulk carrier new building, AS VINCENTIA, within 5 days of each other and under ideal comparable conditions, Mewis and Guiard (2011). 6.5% power reduction, or 0.25 [knots] higher speed at constant power was observed in this case.

In January/February 2013, results from speed trials for the sister vessels Star Istind, fitted with the Mewis Duct, and Star Ismeme, without the Mewis Duct, was executed. The two vessels was tested at near optimum comparable conditions. The conclusion was that Star Istind with the Mewis Duct fitted had a power saving in the magnitude of 6% compared to Star Ismeme in weather condition Beufort 3 or lower, Langeland (2013).

4 Speed Loss and Propulsive Factors due to Waves

A more comprehensive literature study of the topic in this section was carried out in the project thesis in the fall semester of 2012, Topphol (2012).

4.1 Change of Open Water Characteristics

When analyzing propulsion factors based on resistance and propulsion tests in waves, it is common to fit data into open water propeller diagram derived from tests with deeply immersed propeller. But the open water propeller diagram is a function of submergence, especially for h/R < 1.5, where h is the distance between the propeller shaft center and the water surface and R is the propeller radius. When the propeller is oscillating in waves it might be in instantaneous positions where h/R < 1.5, in particular for a ship in ballast condition, which indicates that it might be physically wrong to use an open water propeller diagram for deeply immersed propeller. It may lead to wrong conclusions about effective wake, relative rotatory efficiency and propeller efficiency. Faltinsen et al. (1980)

According to Faltinsen et al. (1980), when the propeller is working close to the free surface, it will set up a steady wave motion, which leads to a reduction in the propeller thrust. This reduction is a function of the propeller loading, and the Froude number.

Thrust and torque coefficients can be corrected for reductions in propeller submergence due to waves and ship motions with to the approximations according to Faltinsen et al. (1980):

$$K_T = \beta \cdot K_{T0} \tag{4.1}$$

$$K_o = \beta^m \cdot K_{o0} \tag{4.2}$$

where K_{T0} and K_{Q0} are thrust and torque coefficients for deeply submerged propeller, m is a factor between 0.8 and 0.85 and β is the thrust diminution factor which can be approximated according to ITTC (2008) by

$$\beta = \begin{cases} 1 - 0.675 \cdot (1 - 0.769 \cdot h/R)^{1.258}, h/R < 1.3 \\ 1, h/R \ge 1.3 \end{cases}$$
(4.3)

With the submergence in still water h_0 and the relative vertical motion amplitude between the shaft and the water surface $\eta_{R\zeta}$ the instantaneous value of the submergence ratio can be approximated, disregarding the wave diffraction:

$$h/R = h_0 / R + (\eta_{R\zeta} \sin(\omega_e t + \varepsilon)) / R$$
(4.4)

Averaging β and β^m over one wave cycle the averaged values of thrust and torque coefficients can be written, according to Faltinsen et al. (1980), as:

$$K_T = \overline{\beta} \cdot K_{T0} \tag{4.5}$$

$$K_{Q} = \overline{\beta^{m}} \cdot K_{Q0} \tag{4.6}$$

The relative motion amplitude $\eta_{R\zeta}$ can be found both from calculation and model tests in waves.

4.2 Change of the Wake

Nakamura and Naito (1975), have shown that the wave induced motions of the ship is increasing the velocities of the wake. They showed in regular waves that the wake velocities increased with the wave height and that the change was more noticeable around the natural period of pitch. They also performed tests of forced motion in pitch, and could show that the velocities increased with pitch angle and frequency. Faltinsen et al. (1980) has shown a theoretical approach to help understanding this qualitatively by examining the influence of the wave induced motions on the mean pressure along the ship. Considering a flat plate as a rough model of the ship bottom and the plate is pitching harmonically. It is then possible to make a rough approximation of the mean pressure at a fixed point in the fluid due to oscillatory fluid motion

$$\Delta \bar{p} \sim -\frac{\rho}{4} \omega_e^2 |\eta_5|^2 x^2 \tag{4.7}$$

where ω_e is the circular frequency of encounter and η_5 is motion in pitch. This indicates a pressure drop from the middle of the ship towards the stern because of the pitching motion. This will cause the flow to get sucked towards the stern of the ship and hence increase the flow velocities to the propeller. Some of the consequences of this velocity increase are that the boundary layer thickness is reduced, the shear forces on the ship are changed and the separation point is delayed.

4.3 Change of Thrust Deduction

Nakamura and Naito (1975) made observations that the thrust deduction decreases in waves compared to still water, with a minimum around the pitch natural period. They also found that

for increasing wave height the thrust deduction decreases, but this was relatively a small change. According to Faltinsen et al. (1980), Nowacki and Sharma came to a simplified equation for the potential thrust deduction fraction in still water, by neglecting the wave induced wake and assuming uniform source distribution over the propeller disc area.

$$t = \frac{2}{1 + \sqrt{1 + C_T}} \frac{w_p}{1 - w}$$
(4.8)

where

$$C_T = \frac{T_p}{\frac{\rho}{2} V_a^2 \pi R^2} \tag{4.9}$$

w is the effective wake, w_p is the potential wake, R is the propeller radius and V_a is the advance velocity

$$V_a = U\left(1 - w\right) \tag{4.10}$$

If this equation is used in waves, and use the information about propeller loading in waves compared with calm water, a decrease in the thrust deduction can be found of the same order which has been measured by model testing.

4.4 Change of Relative Rotative Efficiency

It have been shown by Nakamura and Naito (1975), that the relative rotative efficiency η_R sometimes may change in severe sea conditions compared to still water, with both increasing and decreasing values reported. According to Faltinsen et al. (1980), the change can sometimes be a false change because of use of open water diagram for deeply submerged propeller, but it might be real changes due to change in the wake field and propeller loading. This has been showed both theoretically and experimentally.

4.5 Speed Loss and Propulsive Factors in Waves using Model Test Results

In order to assess the differences in speed and propulsive coefficients in waves by model testing, propulsion tests in waves can be carried out for the same speeds as for calm water and for several wave conditions. Procedures for conducting model tests are explained in section 5.

According to ITTC (2011_1), the measurements to find the difference in the propulsive characteristics can be done by conducting self-propulsion tests in two runs with constant carriage speed:

- Estimation of the self-propulsion point in still water at a certain speed.
- Estimation of the corresponding SPP in waves.

The differences in the propulsive characteristics required to maintain the constant speed is obtained as the difference in averaged values from still water and in regular waves. Speed loss by this method can be assessed by interpolation in the results at different test conditions.

5 Model Test Procedure

Propulsion in still water, regular waves and irregular waves was conducted for the model M3030 A, see details of the model in section 6.1.2. Open water test results from previous model tests by MARINTEK, Alterskjær (2012), with the same stock propeller, P-1099, was used in the analysis in this thesis.

5.1 Open Water Test

To measure the performance of the propeller alone an open water test needs to be carried out. Propeller open water characteristics are required for use in the analysis of propulsion tests and the estimation of required power.

5.1.1 Data Reduction Equations

The results of the open water test are presented as dimensionless data reduction equations and presented in an open water diagram as shown in Figure 4. This is the diagram for the stock propeller P-1099, produced based on the data from the previous tests by MARINTEK, Alterskjær (2012). The reduction equations is defined according to Steen and Minsaas (2012):

$K_T = \frac{T}{\rho n^2 D^4}$	Thrust coefficient	(5.1)
$K_{\underline{Q}} = \frac{Q}{\rho n^2 D^5}$	Torque coefficient	(5.2)
$J_A = \frac{V_A}{nD}$	Advance coefficient	(5.3)
$\eta_0 = \frac{JK_T}{2\pi K_0} = \frac{TV_A}{2\pi nQ}$	Open water efficiency	(5.4)



Figure 4: Open Water Diagram for P-1099, reproduction from Alterskjær (2012).

5.2 **Propulsion Tests**

A geometrically scaled propeller model is fitted and driven by an electric motor mounted inside the hull. Dynamometers are fitted inboard for measurements of thrust T, torque Q and rate of revolutions n of the propeller.

5.2.1 Load Varying Self-Propulsion Test

The procedure used for testing the Mewis Duct was a load varying self-propulsion procedure (constant speed). The load varying self-propulsion extrapolation procedure, proposed by Holtrop (2001), seeks to predict delivered power and propulsion factors without the need to conduct resistance tests for the model. For each constant speed at least two different constant propeller revolution settings are tested and hence two values for thrust T, torque Q and towing force F_D are measured allowing for a minimum for interpolation in the results. The values at the tow force that gives the self propulsion point (SPP) corresponding to the full scale SPP is found by interpolation in the results. The rates of revolutions are chosen so that one value of the tow force are below the self propulsion point and the other is above.

5.2.2 Thrust and Torque Correction

Since the propeller dynamometer is fitted inside the hull for conventional shafted propellers, the friction of bearings and seals will influence the measurement of torque. This can be corrected for by measurements of idle torque for several propeller speeds, which is the measured torque with a dummy boss with identical weight as the model propeller, and then later on make corrections to the measured propeller torque by interpolation. A plot of the torque polynomial used is presented in Figure 5 below:



Figure 5: Plotted polynomial for torque correction

Thrust correction considers the effect the weight of the shaft and drag on the propeller hub. As with the torque correction, a dummy boss cap is placed instead of the propeller. The tests are performed at constant propeller speed and the vessel speed is varied. Torque and thrust correction has been applied in all calculations. A plot of the thrust polynomial is presented in Figure 6 below:



Figure 6: Plotted polynomial for thrust correction

5.2.3 External Tow Force

The frictional resistance coefficient is larger in model scale than in full scale. Hence a correction for this must be applied in the set-up to obtain the correct loading condition for the propeller. An external tow force F_D has to be applied. Depending on the experimental

procedure adopted, the model can either be towed by a resistance dynamometer to measure the unknown external towing force during each run, "British method", or a preselected tow force can be directly applied as a constant load, "Continental method". In the model tests conducted for this analysis, a method alike the "British Method" was used in the way explained in section 5.2.1. The basis for the interpolasion was the calculated tow force F_D from the previous tests by MARINTEK, Alterskjær (2012).

The tow force was calculated as:

$$F_D = C_s \cdot \frac{\rho_M}{2} \cdot {V_M}^2 \cdot S_M \tag{5.5}$$

where

$$C_{S} = (C_{Fm} - C_{Fs} - \Delta C_{F}) \cdot (1 + k) - C_{A} + (C_{BDm} - C_{BDs}) + (C_{Appm} - C_{Apps})$$
(5.6)

and the frictional resistance coefficients C_{Fm} and C_{Fs} are calculated according to the ITTC57 correlation line:

$$C_{F-ITTC57} = \frac{0.075}{(\log(R_N) - 2)^2}$$
(5.7)

 $C_{\rm BD}$ are the transom stern resistance coefficients and $C_{\rm App}$ are appendage resistance coefficients.

The roughness allowance ΔC_F was calculated as:

$$\Delta C_F = (110.31 \cdot (HV_s)^{0.21} - 403.33) \cdot C_{Fs}^2$$
(5.8)

where *H* is the hull surface roughness in $\mu(10^{-3}$ mm).

The value of the correlation factor C_A is the standard for the ship based on previous model tests performed in the specific facility.

The tow force should where possible be applied at X_{CB} and Z_{CB} to avoid artificial trim due to the force.

5.2.4 Propeller Hull Interaction

The interaction effects between the propeller and hull, except the thrust deduction t, is found by using the propeller open water test results in combination with the propulsion test and the resistance test if conducted. In this particular case only propulsion tests were conducted, and as mentioned in the previous section, earlier open water test results were used in the analysis. w, t, η_R and η_H are calculated as following:

The effective wake is the difference between the ship velocity and the apparent velocity and is defined as:

$$w = 1 - \frac{V_A}{V} = 1 - \frac{J_0}{J} \tag{5.9}$$

where V_A is the apparent velocity, V is the ships velocity, J_0 is the advance coefficient found by using "thrust identity" in the open water diagram. K_Q , K_T and $J = \frac{V}{nD}$ values are calculated for the propulsion test. K_T is entered in the open water diagram to obtain corresponding J_0 and K_{Q0} values. The effective wake can now be rewritten as:

$$w = 1 - \frac{J_0 nD}{V} \tag{5.10}$$

Below follows plots of J and K_Q polynomials used to find J_0 and K_{Q0} from the propulsion test using thrust identity, Figure 7 and Figure 8:



Figure 7: Plotted polynomial for J versus Kt



Figure 8: Plotted polynomial for Kq versus J

The thrust deduction represents a difference between the thrust and the resistance of the ship due to the fact that the propeller creates suction behind the hull, and as a consequence increases the velocities in the after body. It is defined in model scale as:

$$t = 1 - \frac{R_{Tm} - F_D}{T_m}$$
(5.11)

where R_{Tm} is the model resistance found from a resistance test or calculated from the zero thrust condition, $F_{T=0}$, from the load-varying propulsion test which was the method adopted in this thesis. From the load-varying propulsion test the tow force F can be plotted against the total thrust. According to Holtrop (2001), the linearity between T and F is nearly always preserved as long as the towing force is in the forward direction, and applies to all kinds of hull forms and propulsors. This is shown in Figure 9 below for different ship speeds and in bollard pull condition (V=0). The plot also includes the condition of severe overloading.



Figure 9: T-F diagram including severe overloading, Holtrop (2001)

Knowing this a coefficient t* can be defined as:

$$t^{*} = 1 - \frac{(F_{T=0} - F)}{T} = 1 - \frac{\delta F}{\delta T}$$
(5.12)

This assumes that the thrust deduction fraction is not influenced by the loading contrary to the classical thrust deduction. Applying t*, the $F_{T=0}$ can be found for each velocity:

$$F_{T=0} = F + T(1 - t^*) \tag{5.13}$$

Examination of many model test results show that the resistance R found from conventional resistance tests is in almost all cases 1-4% lower than $F_{T=0}$, Holtrop (2001). If $F_{T=0}/R$ is larger than 1, t will always be larger than t*, and also implies a dependency of the propeller loading where t decreases for increasing loading.
The relative rotative efficiency η_R is an expression for the fact that the propeller operates in a non-homogenous wake field in front of a rudder. This gives variable propeller blade forces and may decrease or increase the lift/drag ratio of the propeller blades compared to the open water test. The relative rotative efficiency is expressed as:

$$\eta_R = \frac{Q_0}{Q_m} = \frac{K_{Q0}}{K_{Qm}}$$
(5.14)

The hull efficiency η_H is determined from the thrust deduction and the effective wake according to:

$$\eta_H = \frac{1-t}{1-w} \tag{5.15}$$

The open water efficiency of the propeller η_0 is found with use of the data from a propulsion test according to:

$$\eta_0 = T_m (1 - w) \cdot \frac{V}{2\pi Q_0 n}$$
(5.16)

Finally the quasi-propulsive efficiency η_D is determined as:

$$\eta_D = \eta_H \eta_0 \eta_R \tag{5.17}$$

This is an expression for the relationship between the effective power and power developed by the propeller.

5.3 Seakeeping Tests

Seakeeping are the general term used for model testing in wave conditions. It can be carried out in a towing tank equipped with a wave maker, limiting it to head and following sea, or in a seakeeping basin/ocean laboratory, where arbitrary wave headings can be covered. A towing tank procedure was used in this case.

5.3.1 Test Requirements

In wave conditions, gravity forces are the governing force contribution, hence Froude scaling must be applied, Steen (2012). This implies that the scaling of wave height follows the geometrical scaling ratio and the period follows the square root of the scale ratio.

The dynamic motions of the model are the key to the obtained results and hence the inertia forces will be important. This implies that the mass distribution of the model needs to be scaled correctly. The following requirements need to be satisfied:

- Total mass
- Moment of inertia expressed in terms of the gyration radii r_{xx} , r_{yy} and r_{zz}
- Longitudinal and vertical center of gravity

To determine the position of the center of gravity and momentum of inertia it is common to perform a pendulum test. The model is arranged in a pendulum, free to rotate around a fixed point. In the set-up for the tests with the Mewis Duct, only pendulum test in pitch was of relevance. The results from the test can be found in appendix A.

5.3.2 Test Procedure

Self-propelled model tests in both regular and irregular waves were conducted for the M3030 A. Propulsion tests in waves are usually performed by applying one of the following procedures according to Steen (2012):

- At constant propulsion power, adjusting the carriage speed to follow the model
- At constant carriage speed, adjusting the propulsion power to follow the carriage

For the M3030 A, the load-varying propulsion procedure explained in section 5.2.1 was used, following the same calculation procedures for the hull-propeller interaction. The runs was initiated after the waves was fully developed and the model was accelerated after the wave front had passed the model.

In irregular waves the model was accelerated with the spectra fully developed, and run three times through the tank distance with a constant time interval between each run. To get long measurements only one rate of revolution was applied attempting to get a tow rope force as close as possible to the one required for the SPP. As no resistance test was conducted the thrust deduction t cannot be calculated directly, hence a mean value of t from either the regular waves with approximately the same wave length λ , or values from still water is used in the analysis.

5.4 Resistance Test

Model resistance tests are conducted to provide data from which the model resistance can be determined for any desired speed. The results from a resistance test may be used as part of performance predictions. The original tests of M3030 A and the Mewis Duct performed by MARINTEK used the MARINTEK standard procedure for the extrapolation from model scale to full scale values, and hence resistance tests was performed on the hull, Alterskjær (2012). Resistance tests was not concucted for the current setup, and is therefore not further discussed.

6 Model Test of Becker Mewis Duct

Model testing regarding the efficiency of the Mewis Duct in waves was carried out in the large towing tank at MARINTEK, Trondheim, Norway in February/March of 2013.

6.1 Test Set-Up

6.1.1 Test Arrangement

The seakeeping carriage in the towing tank was used to tow the model. The model was fastened to the carriage in a system of springs and pre-tensioned wires as can be seen in Figure 10 below taken from Steen (2012). The springs were located between the connections to the carriage and the wires. A beam located amidships connected the model to the wires, with force transducers in each end for measurements of the towrope force, shown in Figure 11 below.



Figure 10: Schematic of model test set-up, Steen (2012).



Figure 11: Force transducers located at each beam end

6.1.2 Hull Model

The hull model used in the test was M3030 A, seen in Figure 12, which is a model representing the 84 k LPG carrier, and is in scale 1:31.005. The hull model is made from Divinycell and reinforced with wood and coated with paint for a hydro dynamically smooth finish. The test was performed at the Design Waterline (DWL) 11.6/11.6 [m] in full scale.

The model went through its original model tests in 2012, conducted by the MARINTEK staff, which included resistance tests and propulsion tests in calm water with and without the Mewis Duct model fitted, for DWL and Ballast Waterline (WL1) 7.8/5.8 [m]. The MARINTEK report from these tests, Alterskjær (2012) was available and has been used both for comparison and directly for calculations in this report.

Since these tests the hull model has been through repairing of some cracks on the surface which may influence the resistance of the model. It is known that due to ageing the resistance of models tend to increase with time, mainly due to detoriation of surface finish. An increase in the order of 2% could be observed, but this is clearly not known exactly.

The model was first prepared for testing at the ballast waterline, where the largest difference of brake power was calculated from the original tests in still water. A decision to first conduct the regular wave tests was made to observe if the propeller ventilated during the runs, which would have had a large influence on the measured data. Both visible and audible indications of air suction from the surface were observed, and the model was hence prepared for the design waterline by the technicians at MARINTEK. This was done by adding weight without taking the model out of the tank, to physically reach the waterline, and a pendulum test to determine the location of vertical center of gravity and longitudinal radius of gyration was performed after the propulsion tests due to the time schedule.

Due to confidentiality agreements drawings are not included in the report.



Figure 12: Model M3030 A, aft view

Hull main dimensions and characteristics, obtained from Alterskjær (2012), are presented in Table 1 below:

	Symbol	Unit	Full scale	Model scale
Length overall	L _{OA}	[m]	225.001	7.257
Length on designed waterline	L _{WL}	[m]	212.198	6.844
Length between perp.	L _{PP}	[m]	220.000	7.096
Breadth molded	В	[m]	36.615	1.181
Breadth waterline	B _{WL}	[m]	36.608	1.181
Depth to 1st deck	D	[m]	24.212	0.781
Draught at LPP/2	Т	[m]	11.600	0.374
Draught at FP	T _{FP}	[m]	11.600	0.374
Draught at AP	T _{AP}	[m]	11.600	0.374
Trim (pos. aft)	t	[m]	0	0
Volume Displacement	∇	m ³	69033.9	2.316
Displacement	Δ	t	71173.8	2.314
Block Coefficient	C _B	-	0.7388	0.7388
Wetted Surface	S	m ²	10963.05	11.404
Wetted Surf. of Transom Stern	A _T	m^2	2.59	0.003

Table 1: M3030 A hull main dimensions and properties

6.1.3 Becker Mewis Duct Model

The Becker Mewis Duct model, shown in Figure 13 and Figure 14, is made of a plastic material using a 3D printer. The accuracy of the printer is 16 µm, Alterskjær (2012).





Figure 13: Becker Mewis Duct model

Figure 14: Becker Mewis Duct model fitted to M3030 A



Figure 15: Stock propeller P-1099

6.1.4 Propeller Model

The propeller model used in the test was the stock propeller P-1099, seen in Figure 15, which has the characteristics, obtained from Alterskjær (2012), presented in Table 2 below:

	Symbol	Unit	Model
Diameter	D	[mm]	238,67
Pitch ratio	P/D _{mean}	[-]	0,833
EAR	A_E/A_0	[-]	0,555
Number of blades	Z	[-]	4
Hub diameter ratio	d/D	[-]	0,163

Table 2: P-1099 main characteristics

6.2 Instrumentation

The following instrumentation was mounted:

- Ocus mast (6 DoF optical position measurement)
- Vertical acceleration at FP, CoG, AP.
- Longitudinal acceleration at CoG
- Tow force measurements (one transducer at each beam end)
- Wave probe on the carriage, at the longitudinal position of FP
- Relative wave probe at the propeller position
- Propeller torque, thrust and rate of revolution (conventional propeller dynamometer)

Details of the calibration can be found in appendix B.

6.3 Environmental Conditions

The tests were performed for calm water, regular waves and irregular waves. No wind or current was present. A water density of $\rho_m = 999.14 \text{ [kg/m}^3\text{]}$ was assumed in the calculations. Dimensions of the towing tank, obtained from Steen (2012), are shown in Table 3 below:

	Symbol	Unit	Tank
Width	В	[m]	10.5
Length	L	[m]	175
Depth	D	[m]	5.6

Table 3: Dimensions of the towing tank

6.3.1 Wave Calibration

For the test, 7 regular waves and 2 irregular spectra was calibrated. The calibration was done without the model present in the tank to avoid disturbance from reflections. Wave 8999 was a standard test wave for the calibration. Waves 8200-8260 are regular waves with length λ ranging from 0.6-1.5 of the ship length L_{OA}. Waves 8000 and 8010 are irregular spectra of the Pierson-Moskowitz type. Details of the calibration of the irregular spectra can be found in appendix C. A numerical spectra was first simulated and used to create the physical wave spectra in model scale. The approximation as given in DNV (2010) is fulfilled for both spectra:

$$5 \le T_P / \sqrt{H_S} \tag{6.1}$$

Data from the wave calibration is presented in Table 4 below:

Wave	1/L	Wave data M	Wave data F	Meas. H	ΔH [%]	Meas. T	ΔT [%]
				[m]		[s]	
8999		H0.25-T2					
8200	0.6	H0.13-T1.670	H4.03-T9.3	0.13831	6	1.666	-0.24
8210	0.8	H0.13-T1.928	H4.03-T10.7	0.12841	-1.23	1.932	0.21
8220	1	H0.13-T2.156	H4.03-T12.0	0.12586	-3.18	2.152	-0.19
8230	1	H0.17-T2.156	H5.27-T12.0	0.16631	-2.17	2.158	0.09
8240	1.1	H0.13-T2.261	H4.03-T12.6	0.12529	-3.62	2.270	0.4
8250	1.3	H0.13-T2.458	H4.03-T13.7	0.1308	0.61	2.453	-0.2
8260	1.5	H0.13-T2.640	H4.03-T14.7	0.1345	3.34	2.645	0.2
8000		Hs0.113-	Hs3.5-				
		Tp2.156	Tp12.0				
8010		Hs0.161-	Hs5.0-				
		Tp2.156	Tp12.0				

Table 4: Data from wave calibration

6.4 Test Program

6.4.1 Decay Tests

Decay tests was performed for surge and roll motion. This was done by physically setting motion to the model in the respective degree of freedom. The test program is presented in Table 5 below.

TEST NO.	INFORMATION	Tn [s]
9007	Surge	13,6
9008	Roll	1,95

Table 5: Decay tests

6.4.2 Calm Water Propulsion

The calm water propulsion was performed for 3 speeds and 2 different propeller revolution settings at each speed with and without the Mewis Duct fitted. The test program is presented in Table 6 below. The propeller revs. in the table are the measured mean values, so there are slight differences with and without the duct fitted.

Table 6: Test program in still water

With Mewis Duct Fitted							
TEST NO.	Vs [knots]	Vm [m/s]	n1	n2			
6100	15	1,386	6,658	7,992			
6110	16	1,478	7,154	10,013			
6120	17	1,571	7,651	9,038			
6111	16	1,478	7,154	8,487			
	Without Me	ewis Duct Fit	ted				
6200	15	1,386	6,660	7,995			
6210	16	1,478	7,156	8,490			
6220	17	1,571	7,653	9,027			

6.4.3 Propulsion in Regular Waves

Propulsion in regular waves was performed for 2 speeds with 2 different propeller revolution settings for the 7 waves presented in section 6.3.1 with and without the Mewis Duct fitted. The test program is presented in Table 7 for the Mewis Duct fitted and Table 8 without the Mewis Duct fitted below.

With Mewis Duct Fitted					
TEST NO.	WAVE NO.	Vs [knots]	Vm [m/s]	n1	n2
2200	8200	15	1,386	6,66	8,19
2210	8200	17	1,571	7,652	8,934
2220	8210	15	1,386	6,66	9,023
2230	8210	17	1,571	7,652	9,38
2240	8220	15	1,386	6,659	9,375
2250	8220	17	1,571	7,652	10,01
2260	8230	15	1,386	6,659	10,6972
2270	8230	17	1,571	7,651	10,8
2280	8240	15	1,386	6,658	10,0096
2290	8240	17	1,571	7,6514	10,9957
2300	8250	15	1,386	6,6585	9,5024
2310	8250	17	1,571	7,6517	10,0146
2320	8260	15	1,386	6,7083	7,993
2330	8260	17	1,571	7,6518	8,8346
2251	8220	17	1,571	9,0201	10,3103
2271	8230	17	1,571	9,0247	11,4873

Table 7: Test program in regular waves with Becker Mewis Duct fitted

	Without Mewis Duct Fitted						
TEST NO.	WAVE NO.	Vs [knots]	Vm [m/s]	n1	n2		
2400	8200	15	1,386	6,660	8,226		
2410	8200	17	1,571	7,654	8,894		
2420	8210	15	1,386	6,660	9,025		
2430	8210	17	1,571	7,654	9,386		
2440	8220	15	1,386	6,660	9,380		
2450	8220	17	1,571	7,653	10,313		
2460	8230	15	1,386	6,660	10,700		
2470	8230	17	1,571	7,654			
2480	8240	15	1,386	6,660	10,013		
2490	8240	17	1,571	7,653	11,000		
2500	8250	15	1,386	6,660	9,508		
2510	8250	17	1,571	7,654	10,020		
2520	8260	15	1,386	6,660	7,995		
2530	8260	17	1,571	7,654	8,837		
2471	8230	17	1,571	7,653	11,491		
2531	8260	17	1,571	7,654	8,837		
2532	8260	17	1,571	7,654	8,837		
2533	8260	17	1,571	7,654	8,838		
2534	8260	17	1,571	7,654			
2501	8250	15	1,386	6,660	9,509		
2535	8260	17	1,571	7,654	8,837		

Table 8: Test program in regular waves without Becker Mewis Duct fitted

6.4.4 Propulsion in Irregular Waves

Propulsion in irregular waves was performed for 1 speed and 1 propeller revolution setting trying to get as close as possible to the calculated tow force F_D for the 2 wave spectra presented in section 6.3.1. The test program is presented in Table 9 below.

With Mewis Duct Fitted								
TEST NO.	WAVE NO.	Vs [knots]	Vm [m/s]	n				
3000	8000	15	1,385841	7,9912				
3010	8010	15	1,385841	7,9919				
	Without Mewis Duct Fitted							
3100	8000	15	1,385841	7,9947				
3110	8010	15	1,385841	7,9946				

Table 9: Test	program	in	irregular	waves
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7 Results and Analysis

7.1 Surge Decay Test

To ensure the spring setup did not affect the surge motion due to encounter period in head waves with period T_0 and frequency ω_0 , the natural period T_N in surge was compared to the encounter periods T_e from the runs in waves. The natural period in surge was found to be $T_N = 13.6$ [s], see section 6.4.1. The calculated encounter frequency in each condition is presented in Table 10. The encounter period is calculated in head waves according to Faltinsen (1990):

$$T_e = 2\pi / \omega_e \tag{7.1}$$

where the encounter frequency is calculated as

$$\omega_e = \omega_0 + \omega_0^2 \cdot \frac{V}{g} \tag{7.2}$$

The results show that the periods do not coincide and should therefore not be a problem.

Vm = 1,386 [m/s]						
Run	T ₀	ω_0	ω _e	T _e		
2210	1,666	3,771	6,049	1,039		
2230	1,932	3,252	4,946	1,270		
2250	2,152	2,920	4,285	1,466		
2270	2,158	2,912	4,269	1,472		
2290	2,270	2,768	3,995	1,573		
2310	2,453	2,561	3,612	1,740		
2330	2,645	2,375	3,279	1,916		
2251	2,152	2,920	4,285	1,466		
2271	2,158	2,912	4,269	1,472		
	Vm	= 1,571 [m	n/s]			
2200	1,666	3,771	5,781	1,087		
2220	1,932	3,252	4,746	1,324		
2240	2,152	2,920	4,124	1,524		
2260	2,158	2,912	4,109	1,529		
2280	2,270	2,768	3,850	1,632		
2300	2,453	2,561	3,488	1,801		
2320	2,645	2,375	3,173	1,980		

Table 10: Calculated encounter period in regular waves

7.2 Calm Water Propulsion

The main purpose of the analysis of the calm water measurements are to make a basis for comparison with the further results for propulsion in waves. The results are also compared to the original results by MARINTEK, Alterskjær (2012), to indicate the reliability of the measurements.

7.2.1 Initial Results

Interpolated results in model scale at the self-propulsion point in still water are presented in Table 11 below. The tow force F_D used is the calculated tow force from MARINTEK's results in 2012, Alterskjær (2012). Model resistance R_{Tm} is an estimated value using $F_{T=0} / R_{Tm} = 1.04$. The value is an assumption based on that $F_{T=0} / R_{Tm}$ is known to be a value between 1.01-1.04, Holtrop (2001), and is calculated for camparison with the original results from MARINTEK, Alterskjær (2012) and in order to obtain reasonable values for the thrust deduction t. It should be noted that this do not affect the relative difference of t with and without the duct remarkably. The measured values are available in appendix D. Three different revolutions were measured for $V_S = 16$ and 17 [knots] with the duct fitted and Figure 16 shows that linearity of thrust with the loading is a reasonable assumption. Only two points was measured for 15 [knots] but the results seems to correspond to the assumption as well.

With Mewis Duct Fitted								
Vs	V _m	t*	$F_{T=0}$	R _{Tm}	F _D	n	Т	Q
[kn]	[m/s]	[-]	[N]	[N]	[N]	[Hz]	[N]	[Nm]
15	1,3858	0,1113	44,5457	42,8324	19,2127	6,7330	28,5061	0,9048
16	1,4782	0,1314	49,7215	47,8092	21,3632	7,2161	32,6502	1,0383
17	1,5706	0,1172	56,9474	54,7571	23,5970	7,7398	37,7789	1,2044
			With	out Mewis Du	ict Fitted			
Vs	V _m	t*	$F_{T=0}$	R _{Tm}	F _D	n	Т	Q
[kn]	[m/s]	[-]	[N]	[N]	[N]	[Hz]	[N]	[Nm]
15	1,3858	0,1055	43,3462	41,6790	18,7967	6,8633	27,4463	0,9055
16	1,4782	0,0789	50,0173	48,0935	20,9017	7,3705	31,6087	1,0443
17	1,5706	0,0974	55,8450	53,6972	23,0882	7,8729	36,2898	1,1977

Table 11. Interpolated results in still water



Figure 16: T-F diagram illustrating the linearity between thrust and tow force

The plots in Figure 17 and Figure 18 below present the estimated model resistance R_{Tm} from the current setup and the R_{Tm} calculated in MARINTEK's model tests, Alterskjær (2012), at the same model speeds. It show that the R_{Tm} are still higher for the curren setup with the $F_{T=0} / R_{Tm} = 1.04$ used. There may be several reasons for this, and some of them are discussed in a later section.



Figure 17: Model resistance calculated with Becker Mewis Duct in calm water



Figure 18: Model resistance calculated without Becker Mewis Duct in calm water

7.2.2 Propulsive Factors

Table 12 presents results of propulsive factors used in the calculations. Thrust deduction t is calculated using the estimated R_{Tm} as input. From the table and Figure 19 it is clear that the wake fraction follows a slightly decreasing trend with increasing ship velocity, reflecting the increasing Reynolds number, which corresponds to the statement in Holtrop (2001). It also show a clear consistent increase over the different speeds with the Mewis Duct fitted. The calculated wake fraction from Alterskjær (2012) is also included in the figure. The data for the current setup are higher and has a larger increase for the tests with the Mewis Duct.

The thrust deduction can be seen in Figure 20. The figure also presents the thrust deduction for the same speeds from Alterskjær (2012). It shows an increase with the duct fitted, but seems to be very scattered. This will be investigated and explained further in a later section. Large difference in the thrust deduction with the duct fitted result in a decrease in the difference of the hull efficiency, following the formula for hull efficiency in section 5.2.4, and further to the propulsive efficiency.

			With N	Mewis Duct	Fitted			
V _m	t	Κ _T	J	JO	W	K _{Q0}	Q ₀	Kq
[m/s]	[-]	[-]	[-]	[-]	[-]	[-]	[Nm]	[-]
1,3858	0,1714	0,1940	0,8624	0,5140	0,4040	0,0269	0,9449	0,0258
1,4782	0,1900	0,1934	0,8583	0,5152	0,3997	0,0269	1,0829	0,0258
1,5706	0,1752	0,1945	0,8502	0,5128	0,3968	0,0270	1,2514	0,0260
			Without	t Mewis Du	ct Fitted			
V _m	t	Κ _T	J	JO	W	K _{Q0}	Q ₀	Kq
[m/s]	[-]	[-]	[-]	[-]	[-]	[-]	[Nm]	[-]
1,3858	0,1663	0,1797	0,8460	0,5440	0,3570	0,0254	0,9250	0,0248
1,4782	0,1397	0,1795	0,8403	0,5445	0,3521	0,0254	1,0656	0,0248
1 5706	0 1 5 6 5	0 1 9 0 6	0 0250	0 5 4 2 1	0 2514	0.0255	1 2210	0.0250

Table 12: Calculated propulsive factors in still water



Figure 19: Wake fraction versus model velocity in calm water



Figure 20: Thrust deduction versus model velocity in calm water

7.2.3 Propulsive Efficiency

Table 13 presents the calculated propulsive efficiency and its components. The relative rotative efficiency η_R and the open water efficiency η_0 follow roughly the expected values, and η_0 corresponds with the usual range of 0.6-0.8 for conventional propellers in design condition and 0.5-0.6 for ducted propellers as stated in Steen and Minsaas (2012).

The hull efficiency η_H reflects the inaccurate results for the thrust deduction t, and are uncharacteristically high compared to results in Alterskjær (2012) where η_H was calculated to be around 1.25-1.26 with the Mewis Duct fitted and around 1.22-1.23 without. This can also be influenced by bias errors in the thrust and tow force measurements. Further this results in the propulsive efficiency η_D being higher than the expected values and does not follow a clear trend with the velocity as can be seen from Figure 21. The efficiency still seems to be higher with the Mewis Duct fitted. Results from Alterskjær (2012) are also included in the plot.

		With Me	wis Duct F	itted	
V _m	η _R	η _н	η_0	η_{D}	
[m/s]	[-]	[-]	[-]	[-]	
1,3858	1,0443	1,3901	0,5891	0,8551	
1,4782	1,0430	1,3494	0,5901	0,8304	
1,5706	1,0391	1,3675	0,5881	0,8356	
Mean				84,04 %	
	١	Nithout N	lewis Duct	Fitted	
V _m	η _R	η _H	η_0	η_{D}	Diff. η _D
[m/s]	[-]	[-]	[-]	[-]	[%]
1,3858	1,0215	1,2966	0,6131	0,8121	5,033 %
1,4782	1,0204	1,3277	0,6135	0,8312	-0,093 %
1,5706	1,0201	1,3004	0,6117	0,8114	2,892 %
Mean				81,82 %	
Diff.				2,64 %	

Table	13:	Propul	lsive	efficienc	y in	still	water
		• r •••			· · · · ·		



Figure 21: Propulsive efficiency versus model velocity in calm water

7.2.4 Powering Prediction

From the previous measurements by MARINTEK, the brake power P_B was used as the main reference to determine the gain with the Mewis Duct fitted. The brake power at the design waterline was found to be 4.1% lower with the duct fitted at 16.8 [knots], Alterskjær (2012). A power difference around 3-5% was predicted for different speeds. For comparison the brake power was calculated and scaled to ship scale for the current setup, and the results are presented in Table 14 and Figure 22. The brake power was calculated for the tow force corresponding to the self-propulsion point. The calculation method differs from the original tests where the delivered power was calculated according to Alterskjær (2012) following the MARINTEK extrapolation method, and the final delivered power was calculated as:

$$P_D = \frac{2\pi}{1000} \cdot \rho \cdot D^5 \cdot \left(\frac{RPM}{60}\right)^3 \cdot \frac{K_Q}{\eta_R}$$
(7.3)

The delivered power was calculated for the current setup according to ITTC (2011_2):

$$P_D = \frac{\rho_S}{\rho_M} \cdot \lambda^{3.5} \cdot 2\pi \cdot n_M \cdot Q / 1000 \tag{7.4}$$

The brake power was calculated using the same mechanical efficiency $\eta_M = 0.98$ as in the previous tests, Alterskjær (2012).

$$P_B = \frac{P_D}{\eta_M} \tag{7.5}$$

The table and the figure show a decrease in the brake power with the Mewis Duct fitted and in an order of around 2%.

		With N	lewis Duct l	itted	
Vs [knot	s]	Vm [m/s]	Pd	Pb	Diff.
1	15	1,385831	6522,682	6655,798	
1	16	1,478219	8021,921	8185,634	
1	17	1,570608	9980,4	10184,08	
		Without	Mewis Duc	t Fitted	
1	15	1,385831	6653,966	6789,761	1,97 %
1	16	1,478219	8240,457	8408,629	2,65 %
1	17	1,570608	10095,87	10301,91	1,14 %
Mean					1,92 %

Table 14: Powering prediction results in still water



Figure 22: Difference in brake power in still water with and without Becker Mewis Duct fitted

7.3 Propulsion in Regular Waves

7.3.1 Pitch and Heave Motion in Regular Waves

To present the relative pitch and heave motions in regular waves, the response amplitude operators (RAO) have been calculated and plotted versus the wave length to ship lengt ratio λ/L . Figure 23 show RAO for heave for $V_S = 15$ [knots] and $V_S = 17$ [knots]. Large motions can be observed for λ/L around 1-1.5, peaking around $\lambda/L = 1.1$ and 1.3 for $V_S = 15$ and 17 [knots] respectively.



Figure 23: RAO for heave

Figure 24 show RAO for pitch for $V_s = 15$ [knots] and $V_s 17$ [knots]. A peak can be observed around $\lambda/L = 1.3$.



Figure 24: RAO for pitch

7.3.2 Initial Results

Interpolated results in model scale for propulsion in regular waves at the self-propulsion point are presented in Table 15 for 15 [knots] and Table 16 for 17 [knots] below. The tow force F_D used is the calculated tow force from MARINTEK's results in 2012, Alterskjær (2012). Model resistance R_{Tm} is estimated using $F_{T=0} / R_{Tm} = 1.04$. The measured values are available in appendix D.

			With N	/lewis Duct Fi	tted, 1.386	[m/s] (15 [k	n] full scale)	
Н	λ/L		t*	$F_{T=0}$	R _{Tm}	F _D	n	Т	Q
[m]	[-]		[-]	[N]	[N]	[N]	[Hz]	[N]	[Nm]
0,13		0,6	0,1187	59,6377	58,4684	19,2127	7,9533	45,8700	1,4225
0,13		0,8	0,1883	66,0864	64,7906	19,2127	8,6051	57,7507	1,7815
0,13		1	0,1867	79,8652	78,2992	19,2127	9,5442	74,5716	2,2974
0,17		1	0,2385	101,4654	99,4759	19,2127	11,0857	108,0193	3,2842
0,13		1,1	0,2102	77,4419	75,9235	19,2127	9,3545	73,7223	2,2660
0,13		1,3	0,1851	65,3899	64,1077	19,2127	8,4379	56,6651	1,7574
0,13		1,5	0,1157	57,8937	56,7586	19,2127	7,7918	43,7440	1,3725
			Without	Mewis Duct	Fitted, 1.38	6 [m/s] (15	[kn] full sca	le)	
Н	λ/L		t*	F _{T=0}	R _{Tm}	F _D	n	Т	Q
[m]	[-]		[-]	[N]	[N]	[N]	[Hz]	[N]	[Nm]
0,13		0,6	0,1602	55,5965	54,5064	18,7967	8,0725	43,8211	1,4152
0,13		0,8	0,1944	63,8563	62,6042	18,7967	8,7630	55,9336	1,7883
0,13		1	0,1284	80,5654	78 <i>,</i> 9857	18,7967	9,6303	70,8708	2,2457
0,17		1	0,2183	101,2084	99,2239	18,7967	11,2753	105,4270	3,2742
0,13		1,1	0,1423	81,8498	80,2449	18,7967	9,6195	73,5182	2,3106
0,13		1,3	0,1069	67,9572	66,6247	18,7967	8,6029	55,0462	1,7514
0,13		1,5	0,1223	56,7476	55,6349	18,7967	8,0149	43,2409	1,3932

Table 15: Interpolated results in regular waves at Vs = 15 [knots]

Table 16: Interpolated results in regular waves at Vs = 17 [knots]

Н	λ/L		t*	F _{T=0}	R _{Tm}	F _D	n	Т	Q
[m]	[-]		[-]	[N]	[N]	[N]	[Hz]	[N]	[Nm]
0,13		0,6	0,1678	69,6203	68,2552	23,5970	8,8616	55,3010	1,7278
0,13		0,8	0,2286	74,7578	73,2920	23,5970	9,4470	66,3253	2,0680
0,13		1	0,1546	96,4129	94,5225	23,5970	10,3846	86,1271	2,6712
0,17		1	0,2083	114,3303	112,0886	23,5970	11,5842	114,6110	3,5131
0,13		1,1	0,1612	99,4685	97,5182	23,5970	10,4791	90,4500	2,7901
0,13		1,3	0,1573	87,2347	85,5242	23,5970	9,8521	75,5194	2,3487
0,13		1,5	0,2115	70,0579	68,6843	23,5970	9,0504	58,9232	1,8525
			Without	t Mewis Duct	Fitted, 1.571	[m/s] (17 [kn] full scal	e)	
Н	λ/ι		±*	F	D	-		T	<u> </u>
	/y∟		τ	F _{T=0}	ĸ _{Tm}	FD	n	I	Q
[m]	[-]		t* [-]	F _{T=0} [N]	R _{Tm} [N]	F _D [N]	n [Hz]	I [N]	Q [Nm]
[m] 0,13	[-]	0,6	[-] 0,1369	F _{T=0} [N] 68,5430	κ _{τm} [N] 67,1990	F _D [N] 23,0882	n [Hz] 8,9891	I [N] 52,6659	Q [Nm] 1,7116
[m] 0,13 0,13	[-]	0,6 0,8	[-] 0,1369 0,1667	F _{T=0} [N] 68,5430 75,8627	κ _{τm} [N] 67,1990 74,3752	F _D [N] 23,0882 23,0882	n [Hz] 8,9891 9,5779	I [N] 52,6659 63,3306	Q [Nm] 1,7116 2,0424
[m] 0,13 0,13 0,13	[-]	0,6 0,8 1	[-] 0,1369 0,1667 0,1555	F _{T=0} [N] 68,5430 75,8627 92,9878	N [N] 67,1990 74,3752 91,1645	F _D [N] 23,0882 23,0882 23,0882	n [Hz] 8,9891 9,5779 10,5490	[N] 52,6659 63,3306 82,7702	Q [Nm] 1,7116 2,0424 2,6370
[m] 0,13 0,13 0,13 0,13	[-]	0,6 0,8 1 1	[-] 0,1369 0,1667 0,1555 0,2287	F _{T=0} [N] 68,5430 75,8627 92,9878 118,9292	к _{тм} [N] 67,1990 74,3752 91,1645 116,5973	F _D [N] 23,0882 23,0882 23,0882 23,0882 23,0882	n [Hz] 8,9891 9,5779 10,5490 12,4294	I [N] 52,6659 63,3306 82,7702 124,2579	Q [Nm] 1,7116 2,0424 2,6370 3,8704
[m] 0,13 0,13 0,13 0,17 0,13	[-]	0,6 0,8 1 1,1	[-] 0,1369 0,1667 0,1555 0,2287 0,1530	FT=0 [N] 68,5430 75,8627 92,9878 118,9292 99,2907	N [N] 67,1990 74,3752 91,1645 116,5973 97,3438	F _D [N] 23,0882 23,0882 23,0882 23,0882 23,0882 23,0882	n [Hz] 8,9891 9,5779 10,5490 12,4294 10,7582	[N] 52,6659 63,3306 82,7702 124,2579 89,9718	Q [Nm] 1,7116 2,0424 2,6370 3,8704 2,8362
[m] 0,13 0,13 0,13 0,17 0,13 0,13	[-]	0,6 0,8 1 1,1 1,1	[-] 0,1369 0,1667 0,1555 0,2287 0,1530 0,0602	FT=0 [N] 68,5430 75,8627 92,9878 118,9292 99,2907 91,8148	к _{тм} [N] 67,1990 74,3752 91,1645 116,5973 97,3438 90,0145	F _D [N] 23,0882 23,0882 23,0882 23,0882 23,0882 23,0882 23,0882	n [Hz] 8,9891 9,5779 10,5490 12,4294 10,7582 10,0342	I [N] 52,6659 63,3306 82,7702 124,2579 89,9718 73,1327	Q [Nm] 1,7116 2,0424 2,6370 3,8704 2,8362 2,3341

With Mewis Duct Fitted, 1.571 [m/s] (17 [kn] full scale)

7.3.3 Propulsive Factors

Table 17 presents results of calculated propulsive factors in regular waves at 15 [knots]. Thrust deduction t is calculated using the estimated R_{Tm} as input.

			With i	Mewis Duc	t Fitted, 1.	386 [m/s] (15 [kn] full	scale)		
Н	λ/L		t	K _T	J	10	W	K _{Q0}	Q ₀	Kq
[m]	[-]		[-]	[-]	[-]	[-]	[-]	[-]	[Nm]	[-]
0,13		0,6	0,1442	0,2237	0,7301	0,4503	0,3833	0,0301	1,4734	0,0291
0,13		0,8	0,2108	0,2406	0,6748	0,4132	0,3876	0,0319	1,8254	0,0311
0,13		1	0,2077	0,2525	0,6084	0,3867	0,3643	0,0331	2,3321	0,0326
0,17		1	0,2570	0,2711	0,5238	0,3449	0,3416	0,0350	3,3266	0,0345
0,13		1,1	0,2308	0,2599	0,6207	0,3703	0,4035	0,0338	2,2912	0,0335
0,13		1,3	0,2077	0,2455	0,6882	0,4023	0,4153	0,0324	1,7831	0,0319
0,13		1,5	0,1417	0,2222	0,7452	0,4534	0,3916	0,0300	1,4071	0,0292
			Withou	t Mewis Du	uct Fitted, 2	1.386 [m/s]	(15 [kn] fu	Ill scale)		
H	λ/L		Withou t	t Mewis Du K _T	uct Fitted, 1 J	1.386 [m/s] J0	(15 [kn] fu w	Ill scale) K _{Q0}	Q ₀	K _Q
H [m]	λ/L [-]		Withou t [-]	t Mewis Dι K _τ [-]	uct Fitted, : J [-]	1.386 [m/s] J0 [-]	(15 [kn] fu w [-]	Ill scale) K _{qo} [-]	Q ₀ [Nm]	К _Q [-]
H [m] 0,13	λ/L [-]	0,6	Withou t [-] 0,1851	t Mewis Du K _T [-] 0,2074	uct Fitted, : J [-] 0,7193	1.386 [m/s] J0 [-] 0,4853	(15 [kn] fu w [-] 0,3252	Ill scale) K _{Q0} [-] 0,0284	Q ₀ [Nm] 1,4312	K _Q [-] 0,0281
H [m] 0,13 0,13	λ/L [-]	0,6 0,8	Withou t [-] 0,1851 0,2168	t Mewis Du K _T [-] 0,2074 0,2247	uct Fitted, 2 J [-] 0,7193 0,6626	1.386 [m/s] J0 [-] 0,4853 0,4481	(15 [kn] fu w [-] 0,3252 0,3238	III scale) K _{Q0} [-] 0,0284 0,0302	Q ₀ [Nm] 1,4312 1,7949	K _Q [-] 0,0281 0,0301
H [m] 0,13 0,13 0,13	λ/L [-]	0,6 0,8 1	Withou t [-] 0,1851 0,2168 0,1507	t Mewis Du K _T [-] 0,2074 0,2247 0,2357	uct Fitted, 2 J [-] 0,7193 0,6626 0,6029	1.386 [m/s] J0 [-] 0,4853 0,4481 0,4239	(15 [kn] fu w [-] 0,3252 0,3238 0,2969	III scale) K _{Q0} [-] 0,0284 0,0302 0,0314	Q ₀ [Nm] 1,4312 1,7949 2,2502	K _Q [-] 0,0281 0,0301 0,0313
H [m] 0,13 0,13 0,13 0,13 0,17	λ/L [-]	0,6 0,8 1 1	Withou t [-] 0,1851 0,2168 0,1507 0,2371	t Mewis Du K _T [-] 0,2074 0,2247 0,2357 0,2558	uct Fitted, 2 J [-] 0,7193 0,6626 0,6029 0,5150	1.386 [m/s] J0 [-] 0,4853 0,4481 0,4239 0,3794	(15 [kn] fu w [-] 0,3252 0,3238 0,2969 0,2633	III scale) K _{Q0} [-] 0,0284 0,0302 0,0314 0,0334	Q ₀ [Nm] 1,4312 1,7949 2,2502 3,2878	K _Q [-] 0,0281 0,0301 0,0313 0,0333
H [m] 0,13 0,13 0,13 0,13 0,17 0,13	λ/L [-]	0,6 0,8 1 1,1	Withou t [-] 0,1851 0,2168 0,1507 0,2371 0,1642	t Mewis Du K _T [-] 0,2074 0,2247 0,2357 0,2558 0,2451	uct Fitted, 2 J [-] 0,7193 0,6626 0,6029 0,5150 0,6036	1.386 [m/s] J0 [-] 0,4853 0,4481 0,4239 0,3794 0,4033	(15 [kn] fu w [-] 0,3252 0,3238 0,2969 0,2633 0,3319	III scale) K _{Q0} [-] 0,0284 0,0302 0,0314 0,0334 0,0323	Q ₀ [Nm] 1,4312 1,7949 2,2502 3,2878 2,3143	K _Q [-] 0,0281 0,0301 0,0313 0,0333 0,0323
H [m] 0,13 0,13 0,13 0,13 0,13 0,13	λ/L [-]	0,6 0,8 1 1,1 1,3	Withou t [-] 0,1851 0,2168 0,1507 0,2371 0,1642 0,1311	t Mewis Du K _T [-] 0,2074 0,2247 0,2357 0,2558 0,2451 0,2294	uct Fitted, 2 J [-] 0,7193 0,6626 0,6029 0,5150 0,6036 0,6749	1.386 [m/s] J0 [-] 0,4853 0,4481 0,4239 0,3794 0,4033 0,4377	(15 [kn] fu w [-] 0,3252 0,3238 0,2969 0,2633 0,3319 0,3514	III scale) K _{Q0} [-] 0,0284 0,0302 0,0314 0,0334 0,0323 0,0307	Q ₀ [Nm] 1,4312 1,7949 2,2502 3,2878 2,3143 1,7583	K _Q [-] 0,0281 0,0301 0,0313 0,0333 0,0323 0,0306

Table 17: Calculated propulsive factors in regular waves at Vs = 15 [knots]

Figure 25 show the thrust deduction plotted against the wave length/ship length ratio λ/L at $V_S = 15$ [knots] in full scale and wave height H = 4.03 [m], (0.13 [m] model scale). The plot indicates no clear trend; hence no conclusion can be drawn from it. According to Faltinsen et al. (1980) it has been found that for increasing wave height the thrust deduction decreases, while from Table 17 it rather show the opposite trend, with increased values of t for H=0.17 [m] for both with and without the Mewis Duct fitted.



Figure 25: Thrust deduction versus wave length for V_S =15 [knots]

Figure 26 show the effective wake plotted against the wave length/ship length ratio at $V_S = 15$ [knots] in full scale and wave height H = 4.03 [m] (0.13 [m] model scale). There is a dump in the values at approximately $\lambda/L = 1$. The results corresponds roughly with analysis by Nakamura and Naito (1975), where they showed that wave induced motions increases the velocities of the wake, and is more noticeable around the pitch natural period. From the pitch RAO in section 7.3.1 one can see there is a peak around $\lambda/L = 1.3$. It also show a consistent increase of the wake fraction for the tests with the Mewis Duct fitted, as in the still water results.



Figure 26: Effective wake versus wave length for Vs=15 [knots]

Table 18 presents results of calculated propulsive factors in waves regular at 17 [knots]. Thrust deduction t is calculated using the estimated R_{Tm} as input.

			With	Mewis Duc	t Fitted, 1.	571 [m/s] (17 [kn] full	scale)		
Н	λ/L	ł	t	Κ _T	J	JO	W	K _{Q0}	Q_0	Kq
[m]	[-]		[-]	[-]	[-]	[-]	[-]	[-]	[Nm]	[-]
0,13		0,6	0,1925	0,2172	0,7426	0,4643	0,3748	0,0294	1,7879	0,0284
0,13		0,8	0,2507	0,2292	0,6966	0,4381	0,3710	0,0307	2,1189	0,0299
0,13		1	0,1765	0,2463	0,6337	0,4004	0,3681	0,0325	2,7081	0,0320
0,17		1	0,2279	0,2634	0,5681	0,3622	0,3624	0,0342	3,5514	0,0338
0,13		1,1	0,1827	0,2541	0,6280	0,3832	0,3897	0,0332	2,8249	0,0328
0,13		1,3	0,1800	0,2400	0,6680	0,4145	0,3794	0,0318	2,3883	0,0313
0,13		1,5	0,2348	0,2219	0,7271	0,4541	0,3754	0,0299	1,8960	0,0292
			Withou	t Mewis Di	ict Fitted	1 571 [m/s]	l (17 [kn] fi	ill scale)		
						, I [III, 5]		in searcy		
Н	λ/L	i	t	K _T	J	JO	W	K _{Q0}	Q ₀	Kq
H [m]	λ/L [-]		t [-]	K _T [-]	J [-]	JO [-]	w [-]	K _{Q0} [-]	Q₀ [Nm]	К _Q [-]
H [m] 0,13	λ/L [-]	0,6	t [-] 0,1624	K _T [-] 0,2010	J [-] 0,7321	J0 [-] 0,4990	w [-] 0,3184	K _{Q0} [-] 0,0277	Q ₀ [Nm] 1,7320	K _Q [-] 0,0274
H [m] 0,13 0,13	λ/L [-]	0,6 0,8	t t 0,1624 0,1902	K _T [-] 0,2010 0,2129	J [-] 0,7321 0,6871	J0 [-] 0,4990 0,4735	w [-] 0,3184 0,3109	K _{Q0} [-] 0,0277 0,0290	Q ₀ [Nm] 1,7320 2,0565	K _Q [-] 0,0274 0,0288
H [m] 0,13 0,13 0,13	λ/L [-]	0,6 0,8 1	t t [-] 0,1624 0,1902 0,1775	K _T [-] 0,2010 0,2129 0,2294	J [-] 0,7321 0,6871 0,6238	J0 [-] 0,4990 0,4735 0,4377	w [-] 0,3184 0,3109 0,2983	K _{Q0} [-] 0,0277 0,0290 0,0307	Q ₀ [Nm] 1,7320 2,0565 2,6438	K _Q [-] 0,0274 0,0288 0,0306
H [m] 0,13 0,13 0,13 0,13 0,17	λ/L [-]	0,6 0,8 1 1	t [-] 0,1624 0,1902 0,1775 0,2475	K _τ [-] 0,2010 0,2129 0,2294 0,2481	J [-] 0,7321 0,6871 0,6238 0,5294	J0 [-] 0,4990 0,4735 0,4377 0,3966	w [-] 0,3184 0,3109 0,2983 0,2510	K _{Q0} [-] 0,0277 0,0290 0,0307 0,0326	Q ₀ [Nm] 1,7320 2,0565 2,6438 3,9010	K _Q [-] 0,0274 0,0288 0,0306 0,0324
H [m] 0,13 0,13 0,13 0,13 0,17 0,13	λ/L [-]	0,6 0,8 1 1 1,1	t [-] 0,1624 0,1902 0,1775 0,2475 0,1747	K _T [-] 0,2010 0,2129 0,2294 0,2481 0,2398	J [-] 0,7321 0,6871 0,6238 0,5294 0,6117	J0 [-] 0,4990 0,4735 0,4377 0,3966 0,4150	w [-] 0,3184 0,3109 0,2983 0,2510 0,3216	K _{Q0} [-] 0,0277 0,0290 0,0307 0,0326 0,0318	Q ₀ [Nm] 1,7320 2,0565 2,6438 3,9010 2,8459	K _Q [-] 0,0274 0,0288 0,0306 0,0324 0,0317
H [m] 0,13 0,13 0,13 0,13 0,17 0,13 0,13	λ/L [-]	0,6 0,8 1 1,1 1,1	t [-] 0,1624 0,1902 0,1775 0,2475 0,1747 0,0849	K _T [-] 0,2010 0,2129 0,2294 0,2481 0,2398 0,2240	J [-] 0,7321 0,6871 0,6238 0,5294 0,6117 0,6558	J0 [-] 0,4990 0,4735 0,4377 0,3966 0,4150 0,4495	w [-] 0,3184 0,3109 0,2983 0,2510 0,3216 0,3147	K _{Q0} [-] 0,0277 0,0290 0,0307 0,0326 0,0318 0,0301	Q ₀ [Nm] 1,7320 2,0565 2,6438 3,9010 2,8459 2,3482	K _Q [-] 0,0274 0,0288 0,0306 0,0324 0,0317 0,0300

Table 18: Calculated propulsive factors in regular waves at Vs = 17 [knots]

Figure 27 show the thrust deduction plotted against the wave length/ship length ratio λ/L at $V_S = 17$ [knots] in full scale and wave height H = 4.03 [m], (0.13 [m] model scale). Same as the results for $V_S = 15$ [knots], even though thrust deduction seems higher for the Mewis Duct fitted, the plotted results are too scattered and no certain conclusion can be drawn. From the table and the figure one can see that some of the thrust deduction values are remarkable smaller than the others both for $V_S = 15$ [knots] and $V_S = 17$ [knots]. This is discussed further in a later section.

Figure 28 show the effective wake plotted against the wave length/ship length ratio at $V_S = 17$ [knots] and wave height H = 4.03 [m] (0.13 [m] model scale). The effective wake follows roughly the same trend as discussed for $V_S = 15$ [knots] and clearly show a consistent increase with the Mewis Duct fitted.



Figure 27: Thrust deduction versus wave length for Vs=17 [knots]



Figure 28: Effective wake versus wave length for Vs=17 [knots]

7.3.4 Propulsive Efficiency

Table 19 presents the calculated propulsive efficiency and its components in regular waves at $V_S = 15$ [knots]. The relative rotative efficiency η_R and the open water efficiency η_0 follows reasonable values with a clear reduction of η_0 around $\lambda/L = 1$, and most noticeable for the highest wave H = 0.17 [m] in model scale. The hull efficiency η_H also follows a decreasing trend towards $\lambda/L = 1$ for the tests performed with the Mewis Duct fitted, but are more scattered without and no trend is clear. No relative difference of the propulsive efficiency η_D with and without the duct fitted can be concluded with, which can be seen from Figure 29.

	With M	ewis [Duct Fitte	ed, 1.386 [I	m/s] (15 [k	n] full scale	e)
Н	λ/L	η	R	η _H	η_0	η_{D}	
[m]	[-]	[-]	[-]	[-]	[-]	
0,13	(D,6	1,0358	1,3877	0,5325	0,7653	
0,13	() <i>,</i> 8	1,0247	1,2887	0,4966	0,6558	
0,13		1	1,0151	1,2465	0,4697	0,5944	
0,17		1	1,0129	1,1286	0,4254	0,4863	
0,13	1	1,1	1,0111	1,2896	0,4526	0,5901	
0,13	1	1,3	1,0146	1,3551	0,4857	0,6678	
0,13	1	1,5	1,0252	1,4108	0,5354	0,7743	
	Without N	Mewis	5 Duct Fi	tted, 1.386	[m/s] (15	[kn] full sca	ale)
Н	Without Ν λ/L	Mewis ካ	S Duct Fi	tted, 1.386 ղ _н	[m/s] (15 η ₀	[kn] full sca η _D	ale) Diff. η _D
H [m]	Without Ν λ/L [-]	Mewis ղ [-	s Duct Fit R]	tted, 1.386 ղ _н [-]	[m/s] (15 η ₀ [-]	[kn] full sca Ŋ⊳ [-]	ale) Diff. η _D [%]
H [m] 0,13	Without Ν λ/L [-]	<u>Newis</u> مر [-] ک,6	5 Duct Fit R] 1,0113	tted, 1.386 դ _н [-] 1,2077	0 [m/s] (15 η ₀ [-] 0,5645	[kn] full sca η _D [-] 0,6894	ale) Diff. η _D [%] 9,92 %
H [m] 0,13 0,13	Without Ν λ/L [-] (<u>Mewis</u> ۹۱ [-] ۵,6 ۵,8	5 Duct Fit 7 1,0113 1,0037	tted, 1.386 Ŋ _H [-] 1,2077 1,1582	[m/s] (15 η ₀ [-] 0,5645 0,5304	[kn] full sca η _D [-] 0,6894 0,6166	ale) Diff. η _D [%] 9,92 % 5,98 %
H [m] 0,13 0,13 0,13	Without Ν λ/L [-] (<u>Mewis</u> η _ι [- 0,6 0,8 1	5 Duct Fit 7 1,0113 1,0037 1,0020	tted, 1.386 η _H [-] 1,2077 1,1582 1,2079	[m/s] (15 η ₀ [-] 0,5645 0,5304 0,5072	[kn] full sca η _D [-] 0,6894 0,6166 0,6139	ale) Diff. η _D [%] 9,92 % 5,98 % -3,28 %
H [m] 0,13 0,13 0,13 0,13	Without Ν λ/L [-] (Mewis n [- 0,6 0,8 1 1	5 Duct Fit 7 1,0113 1,0037 1,0020 1,0042	tted, 1.386 η _H [-] 1,2077 1,1582 1,2079 1,0355	[m/s] (15 η₀ [-] 0,5645 0,5304 0,5072 0,4621	[kn] full sca η _D [-] 0,6894 0,6166 0,6139 0,4805	hle) Diff. η _D [%] 9,92 % 5,98 % -3,28 % 1,18 %
H [m] 0,13 0,13 0,13 0,17 0,13	Without Ν λ/L [-] () () () () () () ()	Mewis ni [- 0,6 0,8 1 1,1	B Duct Fit R 1,0113 1,0037 1,0020 1,0042 1,0016	tted, 1.386 η _H [-] 1,2077 1,1582 1,2079 1,0355 1,2510	 [m/s] (15 η₀ [-] 0,5645 0,5304 0,5072 0,4621 0,4866 	[kn] full sca η _D [-] 0,6894 0,6166 0,6139 0,4805 0,6098	hle) Diff. η _D [%] 9,92 % 5,98 % -3,28 % 1,18 % -3,34 %
H [m] 0,13 0,13 0,13 0,13 0,13 0,13	Without Γ λ/L [-] () () () () () () () () () ()	Mewis ni [- 0,6 0,8 1 1,1 1,3	5 Duct Fit R 1,0113 1,0037 1,0020 1,0042 1,0016 1,0039	tted, 1.386 η _H [-] 1,2077 1,1582 1,2079 1,0355 1,2510 1,3397	[m/s] (15 η₀ [-] 0,5645 0,5304 0,5072 0,4621 0,4866 0,5206	[kn] full sca η _D [-] 0,6894 0,6166 0,6139 0,4805 0,6098 0,7001	hle) Diff. η _D [%] 9,92 % 5,98 % -3,28 % 1,18 % -3,34 % -4,85 %

Table 19: Propulsive efficiency in regular waves at Vs = 15 [knots]



Figure 29: Propulsive efficiency versus wave length to ship length ratio in regular waves at Vs = 15 [knots]

Table 20 presents the calculated propulsive efficiency and its components in regular waves at $V_S = 17$ [knots]. As for $V_S = 15$ [knots], no conclusion can be drawn from the values in the table and Figure 30 showing the propulsive efficiency η_D with and without the Mewis Duct.

				-		_	
Н	λ/L		η _R	η _H	η_0	η_{D}	
[m]	[-]		[-]	[-]	[-]	[-]	
0,13		0,6	1,0348	1,2917	0,5455	0,7291	
0,13		0,8	1,0246	1,1912	0,5210	0,6359	
0,13		1	1,0138	1,3032	0,4838	0,6391	
0,17		1	1,0109	1,2109	0,4440	0,5435	
0,13		1,1	1,0125	1,3392	0,4661	0,6320	
0,13		1,3	1,0169	1,3214	0,4979	0,6690	
0,13		1,5	1,0235	1,2252	0,5361	0,6722	
	Withou	t Mev	vis Duct F	itted, 1.57	1 [m/s] (17	7 [kn] full s	cale)
Н	λ/L		η _R	ղ _н	no	n _D	Diff. n _p
[m]							
	[-]		[-]	[-]	[-]	[-]	[%]
0,13	[-]	0,6	[-] 1,0119	[-] 1,2288	[-] 0,5764	[-] 0,7166	[%] 1,71 %
0,13 0,13	[-]	0,6 0,8	[-] 1,0119 1,0069	[-] 1,2288 1,1751	[-] 0,5764 0,5539	[-] 0,7166 0,6554	[%] 1,71 % -3,07 %
0,13 0,13 0,13	<u>[-]</u>	0,6 0,8 1	[-] 1,0119 1,0069 1,0026	[-] 1,2288 1,1751 1,1721	[-] 0,5764 0,5539 0,5206	[-] 0,7166 0,6554 0,6117	[%] 1,71 % -3,07 % 4,29 %
0,13 0,13 0,13 0,17	[-]	0,6 0,8 1 1	[-] 1,0119 1,0069 1,0026 1,0079	[-] 1,2288 1,1751 1,1721 1,0047	[-] 0,5764 0,5539 0,5206 0,4798	[-] 0,7166 0,6554 0,6117 0,4859	[%] 1,71 % -3,07 % 4,29 % 10,61 %
0,13 0,13 0,13 0,17 0,13	<u>[-]</u>	0,6 0,8 1 1,1	[-] 1,0119 1,0069 1,0026 1,0079 1,0034	[-] 1,2288 1,1751 1,1721 1,0047 1,2166	[-] 0,5764 0,5539 0,5206 0,4798 0,4983	[-] 0,7166 0,6554 0,6117 0,4859 0,6083	[%] 1,71 % -3,07 % 4,29 % 10,61 % 3,74 %
0,13 0,13 0,13 0,17 0,13 0,13	[-]	0,6 0,8 1 1,1 1,1	[-] 1,0119 1,0069 1,0026 1,0079 1,0034 1,0061	[-] 1,2288 1,1751 1,1721 1,0047 1,2166 1,3353	[-] 0,5764 0,5539 0,5206 0,4798 0,4983 0,5317	[-] 0,7166 0,6554 0,6117 0,4859 0,6083 0,7143	[%] 1,71 % -3,07 % 4,29 % 10,61 % 3,74 % -6,77 %

Table 20: Propulsive efficiency in regular waves at Vs = 17 [knots]

[m]	[-]		[-]	[-]	[-]	[-]	
0,13		0,6	1,0348	1,2917	0,5455	0,7291	
0,13		0,8	1,0246	1,1912	0,5210	0,6359	
0,13		1	1,0138	1,3032	0,4838	0,6391	
0,17		1	1,0109	1,2109	0,4440	0,5435	
0,13		1,1	1,0125	1,3392	0,4661	0,6320	
0,13		1,3	1,0169	1,3214	0,4979	0,6690	
0,13		1,5	1,0235	1,2252	0,5361	0,6722	
	Without	t Me	wis Duct F	itted, 1.57	1 [m/s] (17	7 [kn] full s	cale)
	2.1						
Н	λ/L		η _R	η _H	η_0	η_{D}	Diff. η _D
н [m]	λ/L [-]		η _R [-]	ղ _н [-]	η ₀ [-]	η _⊳ [-]	Diff. η _D [%]
H [m] 0,13	λ/L [-]	0,6	η _R [-] 1,0119	η _н [-] 1,2288	η ₀ [-] 0,5764	η _⊳ [-] 0,7166	Diff. η _D [%] 1,71 %
H [m] 0,13 0,13	λ/L [-]	0,6 0,8	η _R [-] 1,0119 1,0069	η _H [-] 1,2288 1,1751	η ₀ [-] 0,5764 0,5539	η _D [-] 0,7166 0,6554	Diff. η _D [%] 1,71 % -3,07 %
H [m] 0,13 0,13 0,13	л/L [-]	0,6 0,8 1	η _R [-] 1,0119 1,0069 1,0026	η _Η [-] 1,2288 1,1751 1,1721	n₀ [-] 0,5764 0,5539 0,5206	η _D [-] 0,7166 0,6554 0,6117	Diff. η _D [%] 1,71 % -3,07 % 4,29 %
H [m] 0,13 0,13 0,13 0,13 0,17	л/L [-]	0,6 0,8 1 1	η _R [-] 1,0119 1,0069 1,0026 1,0079	η _H [-] 1,2288 1,1751 1,1721 1,0047	η₀ [-] 0,5764 0,5539 0,5206 0,4798	η _D [-] 0,7166 0,6554 0,6117 0,4859	Diff. η _D [%] 1,71 % -3,07 % 4,29 % 10,61 %
H [m] 0,13 0,13 0,13 0,13 0,17 0,13	л/L [-]	0,6 0,8 1 1,1	η _R [-] 1,0119 1,0069 1,0026 1,0079 1,0034	η _H [-] 1,2288 1,1751 1,1721 1,0047 1,2166	n₀ [-] 0,5764 0,5539 0,5206 0,4798 0,4983	η _D [-] 0,7166 0,6554 0,6117 0,4859 0,6083	Diff. η _D [%] 1,71 % -3,07 % 4,29 % 10,61 % 3,74 %
H [m] 0,13 0,13 0,13 0,13 0,17 0,13 0,13	л/L [-]	0,6 0,8 1 1,1 1,1	η _R [-] 1,0119 1,0069 1,0026 1,0079 1,0034 1,0061	η _H [-] 1,2288 1,1751 1,1721 1,0047 1,2166 1,3353	η ₀ [-] 0,5764 0,5539 0,5206 0,4798 0,4983 0,5317	η _D [-] 0,7166 0,6554 0,6117 0,4859 0,6083 0,7143	Diff. η _D [%] 1,71 % -3,07 % 4,29 % 10,61 % 3,74 % -6,77 %
H [m] 0,13 0,13 0,13 0,13 0,13 0,13 0,13	л/L [-]	0,6 0,8 1 1,1 1,3 1,5	η _R [-] 1,0119 1,0069 1,0026 1,0079 1,0034 1,0061 1,0131	η_{H} [-] 1,2288 1,1751 1,1721 1,0047 1,2166 1,3353 1,3254	n₀ [-] 0,5764 0,5539 0,5206 0,4798 0,4983 0,5317 0,5694	η _D [-] 0,7166 0,6554 0,6117 0,4859 0,6083 0,7143 0,7645	Diff. η _D [%] 1,71 % -3,07 % 4,29 % 10,61 % 3,74 % -6,77 % -13,73 %

With Mewis Duct Fitted, 1.571 [m/s] (17 [kn] full scale)



Figure 30: Propulsive efficiency versus wave length to ship length ratio in regular waves at Vs = 17 [knots]

7.3.5 Powering Prediction

Table 21 below presents the calculated and scaled delivered power P_D and brake power P_B in waves at $V_S = 15$ [knots] with and without the Mewis Duct fitted. The results are calculated at the tow force corresponding to the self-propulsion point. The results show a mean decrease in the brake power with the Mewis Duct fitted of 1.94%. The table show somewhat scattered results, and no trend in the difference can be seen regarding wavelength or height. Results of the brake power with and without the Mewis Duct fitted are also presented in Figure 31 disregarding the run with H = 5.27 [m]. The brake power follows a clear trend with the wave length, and peak around $\lambda/L = 1$ can be observed.

With Mewis Duct Fitted, V _s = 15 [knots]							
H [m]	λ/L [-]	P _D [kW]	Pb [kW]				
4,03	0,6	12112,87	12360,07				
4,03	0,8	16413,16	16748,12				
4,03	1	23476,4	23955,51				
5,27	1	38979,87	39775,38				
4,03	1,1	22695,46	23158,63				
4,03	1,3	15876,8	16200,82				
4,03	1,5	11450,34	11684,02				
Without Mewis Duct Fitted, 15 [knots]							
H [m]	λ/L [-]	P _D [kW]	Pb [kW]	Diff.			
4,03	0,6	12231,52	12481,14	0,97 %			
4,03	0,8	16778,32	17120,74	2,18 %			
4,03	1	23154,49	23627,03	-1,39 %			
5,27	1	39525,91	40332,56	1,38 %			
4,03	1,1	23797,26	24282,92	4,63 %			
4,03	1,3	16131,98	16461,2	1,58 %			
4,03	1,5	11955,48	12199,47	4,23 %			
Mean				1,94 %			

Table 21: Powering prediction in waves at Vs = 15 [knots]



Figure 31: Brake power versus wave length to ship length ratio for H = 4.03 [m] at VS = 15 [knots]

Table 22 below presents the calculated and scaled delivered power P_D and brake power P_B in waves at $V_S = 17$ [knots] with and without the Mewis Duct fitted. The results show a mean decrease in the brake power with the Mewis Duct fitted of 3%, but the run in wave height 5.27 [m] influences the result significantly and should probably be disregarded. Without that run a mean of less than 1% is observed. From this, it seems that the gain that can be obtained with the use of a Mewis Duct in waves is better pronounced for the lower vessel speed. Figure 32 presents the brake power with and without the Mewis Duct fitted plotted against the wave length to ship length ratio at $V_S = 17$ [knots] disregarding the run in wave height 5.27 [m].

With Mewis Duct Fitted, V _s = 17 [knots]							
H [m]	λ/L [-]		P _D [kW]	Pb [kW]			
4,03		0,6	16393,02	16727,57			
4,03		0,8	20917,09	21343,97			
4,03		1	29699,88	30306,00			
5,27		1	43572,24	44461,47			
4,03		1,1	31303,42	31942,27			
4,03		1,3	24774,12	25279,71			
4,03		1,5	17950,16	18316,49			
Without Mewis Duct Fitted, 17 [knots]							
H [m]	λ/L [-]		P _D [kW]	Pb [kW]	Diff.		
4,03		0,6	16473,39	16809,59	0,49 %		
4,03		0,8	20944,52	21371,96	0,13 %		
4,03		1	29784,03	30391,87	0,28 %		
5,27		1	51506,42	52557,57	15,40 %		
4,03		1,1	32668,21	33334,91	4,18 %		
4,03		1,3	25076,02	25587,78	1,20 %		
4,03		1,5	17829,3	18193,16	-0,68 %		
Mean					3,00 %		

Table 22: Powering prediction in waves at Vs = 17 [knots]



Figure 32: Brake power versus wave length to ship length ratio for H = 4.03 [m] at VS = 17 [knots]
7.4 Propulsion in Irregular Waves

For the irregular wave tests one carriage speed was used in all runs, V_M =1.386 [m/s] corresponding to 15 [knots] in full scale. As stated earlier, the irregular wave tests was performed at one propeller revolution setting trying to hit as close as possible to the calculated tow force F_D . As no resistance tests was conducted, the thrust deduction t had to be taken as a mean from previous results. A sensitivity study regarding the influence of minor changes in the thrust deduction t on the propulsive efficiency η_D has been followed through.

7.4.1 Initial Results

Table 23 below presents the measured values from the propulsion in the irregular spectra 8000, $H_s=0.113$ [m] and $T_P=2.156$ [m] in model scale. The table show that the tow force are somewhat scattered, and does not correspond directly to the correct propulsion point, but results show that the thrust and torque are considerable higher at the given propeller revolution for the tests with the Mewis Duct.

Table 23: Measured values in the irregular wave spectrum Hs = 0.113 [m], Tp = 2.156 [m]

With Mewis Duct Fitted, Hs=0.113						
n	Q	Т	F			
7,9912	1,460608	46,69511	10,5191			
7,9917	1,459707	46,66101	13,1586			
7,992	1,462307	46,83921	11,9425			
Witho	out Mewis D	Ouct Fitted,	Hs=0.113			
Withc n	p ut Mewis D Q	Duct Fitted, T	Hs=0.113 F			
Witho n 7,9947	out Mewis D Q 1,381905	Duct Fitted, T 43,00921	Hs=0.113 F 12,051			
Withc n 7,9947 7,9949	out Mewis D Q 1,381905 1,382105	Duct Fitted, T 43,00921 43,02761	Hs=0.113 F 12,051 14,9117			

Table 24 below presents the measured values from the propulsion in the irregular spectra 8010, $H_s=0.161$ [m] and $T_P=2.156$ [m] in model scale. The tow force corresponds better with the calculated tow force, but still has some scatter. The results show the same indication of increase of thrust and torque with the Mewis Duct fitted.

With Mewis Duct Fitted, Hs=0.161							
n	Q	Т	F				
7,9919	1,455007	46,56531	17,3322				
7,992	1,456507	46,62281	21,3575				
7,992	1,458507	46,70441	20,7463				
Witho	out Mewis D	ouct Fitted,	Hs=0.161				
n	Q	Т	F				
7,9946	1,376805	42,76601	19,1919				
7,9947	1,381405	42,92351	23,5745				
7,9949	1,379405	42,85921	22,5598				

Table 24: Measured values in the irregular wave spectrum Hs = 0.161 [m], Tp = 2.156 [m]

7.4.2 Propulsive Efficiency

Table 25 and Table 26 below present results of thrust deduction t, effective wake w and the propulsive efficiency η_D and its components for H_S =0.113 [m] and H_S =0.161 [m] respectively. The t values used is averaged values from the previous results by MARINTEK, Alterskjær (2012). Using those values in the calculation result in approximately 2% higher propulsive efficiency with the Mewis Duct for H_S =0.113 and 2.4% for H_S =0.161. This does not mean a conclusion can be drawn from the results, as the thrust deduction used are from still water results. However it indicates the efficiency gain if the thrust deduction keeps the same relative difference in waves with and without the Mewis Duct as in still water. A simplification is made and the thrust deduction is assumed equal for both wave heights in these calculations, and reference is made to Nakamura and Naito (1975) where they showed that the thrust deduction had a relatively small change and only increased slightly with the wave height.

	With Mewis Duct Fitted, Hs=0.113							
t	w	η_{R}	η _H	η_0	η_{D}	diff.		
0,2	0,38594	1,02501	1,302804	0,528618	0,70591	2,08 %		
0,2	0,385323	1,025087	1,301496	0,529016	0,705786	2,04 %		
0,2	0,38783	1,026324	1,306827	0,527274	0,707195	2,18 %		
	I	Without Me	wis Duct Fit	ted, Hs=0.12	13			
t	W	η_{R}	η _H	η ₀	η_{D}			
0,195	0,332153	1,016368	1,205365	0,56421	0,691211			
0,195	0,332367	1,016571	1,205753	0,564062	0,69139			
0,195	0,333304	1,016789	1,207447	0,563466	0,691778			

Table 25: Propulsive efficiency in the irregular wave spectrum Hs = 0.113 [m], Tp = 2.156 [m]

With Mewis Duct Fitted, Hs=0.161								
t	w	η_{R}	η _H	η_0	η_{D}	diff.		
0,2	0,383888	1,026767	1,298466	0,529991	0,706596	2,37 %		
0,2	0,384696	1,026702	1,30017	0,529431	0,706731	2,36 %		
0,2	0,385878	1,026691	1,302672	0,528619	0,706997	2,40 %		
	١	Without Me	wis Duct Fit	ted, Hs=0.16	51			
t	W	η_{R}	η _H	η_0	η_{D}			
0,195	0,328714	1,015627	1,199191	0,566417	0,689857			
0,195	0,330932	1,015156	1,203166	0,564993	0,690084			
0,195	0,329969	1,015452	1,201438	0,565599	0,690032			

Table 26: Propulsive efficiency in the irregular wave spectrum Hs = 0.161 [m], Tp = 2.156 [m]

7.4.3 Influence of Thrust Deduction

A sensitivity analysis of the influence of change in the thrust deduction t on the propulsive efficiency η_D was carried out for the irregular wave data and the results are presented in Table 27 below. Different values of thrust deduction was chosen with basis in still water and regular wave data. Mean values from the runs in irregular waves with and without the Mewis Duct fitted was compared. The basis of the values chosen for t was:

- The averaged values of all the runs in regular waves with and without the Mewis Duct fitted.
- The Averaged values from regular waves with wave length to ship length ratio $\lambda/L = 0.8-1.1$ with and without the Mewis Duct fitted.
- Values obtained by curve fitting of the regular wave values at $V_s = 15$ [knots] using a polynomial of second degree. The values at $\lambda/L = 0.8$ -1.1 was used.
- Values from the still water results for $V_S = 15$ [knots] with and without the Mewis Duct fitted.
- Values from the still water results from the tests performed by MARINTEK with and without the Mewis Duct fitted, Alterskjær (2012).

The table show that values of thrust deduction with around the same difference with and without the Mewis Duct gives about the same result. Relative small changes in the propulsive efficiency is made from relative large changes in the thrust deduction, as can be seen in Figure 33, but as the values of interest are the differences with and without the Mewis Duct fitted, which is expected around 2-5 % or even smaller in waves, it show the necessity to obtain accurate values for all the parameters involved. Both positive and negative values of the

difference is obtained. The uncertainty in the measurements are discussed further in a later section.

	Avera reg. v	ge from waves	Averag reg. wav λ/L 0.	ge from ves with 8-1.1	Curve values f wa	e fitted rom reg. ves	Still wate = 15 [l	er for Vs ‹nots]	Still wa MAR	iter from INTEK
	t	η_{D}	t	η_{D}	t	η_{D}	t	η_{D}	t	η_{D}
w duct	0,2032	0,7037	0,218	0,6906	0,1979	0,7084	0,1714	0,7318	0,2	0,7065
w/o duct	0,1687	0,7133	0,1948	0,6909	0,147	0,7319	0,1663	0,7154	0,195	0,6907
Difference		-1,36 %		-0,03 %		-3,33 %		2,24 %		2,24 %

Table 27: Influence of changes in thrust deduction on the propulsive efficiency with and without Becker Mewis Duct



Figure 33: Influence of thrust deduction on the propulsive efficiency

7.5 Repeatability

Repeatability of the test will indicate the accuracy of the performed tests, and hence indicate if the results are reliable. The replication level of the repeated measurements indicate how large part of the set-up that is held the same. The important part in the current set-up was to ensure that as mutch as possible of the test-setup was held the same, thus moving most of the errors to bias error in the measurement.

Ideally, if time and money was of no concern, every test condition would be repeated a sufficient amount of times to ensure the accuracy. Realistically this is not possible, hence one condition is repeated and the standard deviation is assumed representative for the other conditions.

7.5.1 Precision Limit

Precision limits are calculated according to ITTC (2002). The standard deviation s is calculated as:

$$s^{2} = [1/(n-1)]\sum_{k=1}^{n} (q_{k} - \bar{q})^{2}$$
(7.6)

where q_k is the observed quantity, n is the number of observations and \overline{q} is the mean value:

$$\overline{q} = \sum_{k=1}^{n} \frac{q_k}{n} \tag{7.7}$$

Precision limits are now calculated as:

- 1

$$P(M) = \frac{s \cdot i}{\sqrt{n}}$$
 for multiple sample precision (7.8)

$$P(S) = s \cdot t$$
 for single sample precision (7.9)

where the weight t is determined following Student's t distribution for a 95% confidence interval shown in Figure 34 taken from Steen (2012):



Figure 34: The weight t for estimating confidence intervals using Student's t distribution, Steen (2012)

For the M3030 A, one of the calm wave conditions were repeated, and a total of five runs were performed (run 2530, 2531, 2532, 2533 and 2535). Wave 8260 was used (Reg H=0.13, T=2.640), and a ship velocity 17 knots (1.571 [m/s] model scale). This is a wave with a long period and hence for simplicity the results are assumed to be roughly representative for still water conditions as well, as the uncertainty in still water measurements should definitely not be higher. The results are presented in Table 28 and Table 29 below.

	n ₁	T_1	Q ₁	F_{D1}	n ₂	T_2		Q ₂	F _{D2}
	7,6537	32,3312	1,0937	45,2931	8,8372		50,6473	1,661	28,1691
	7,6536	32,1258	1,0873	43,8093	8,8371		50,6541	1,6604	27,8787
	7,6541	31,7898	1,0789	44,272	8,8372		50,7151	1,6627	28,0534
	7,6541	32,0557	1,086	44,1948	8,8376		50 <i>,</i> 583	1,6592	28,1352
	7,6541	32,2346	1,0911	44,0041	8,8371		50,6185	1,6625	29,2261
Avg	7,65392	32,10742	1,0874	44,31466	8,83724		50,6436	1,66116	28,2925
s^2	6,2E-08	0,04254	3,19E-05	0,33134	4,3E-08		0,00238	2,153E-06	0,28499
S	0,00025	0,20624	0,00565	0,57562	0,00021		0,04883	0,00147	0,53385
P(M)	0,00031	0,25609	0,00701	0,71473	0,00026		0,06063	0,00182	0,66286
%	0,004 %	0,798 %	0,645 %	1,613 %	0,003 %		0,120 %	0,110 %	2,343 %
P(S)	0,00069	0,57263	0,01568	1,59819	0,00058		0,13558	0,00407	1,48220
%	0,009 %	1,783 %	1,442 %	3,606 %	0,007 %		0,268 %	0,245 %	5,239 %

Table 28: Calculation of precision limit for multiple and single runs for the measured values

Table 28 shows that the measured quantities have a reasonable accuracy for single runs, and the tow force F_D is more uncertain than the other quantities which agree with Holtrop and Hooijmans (2002) where they stated that a higher scatter had been observed for the tow force F than the other signals. The accuracy is higher for the second thrust and torque measurements, whilst lower for the second tow force. This can be explained by the fact that higher values with difference of around the same order give a lower relative uncertainty.

	t*		w		η _R	η _H		η_0	η_{D}	
		0,0651		0,3145	1,013	1	1,3639	0,5694		0,7868
		0,1402		0,3152	1,013	5	1,2555	0,5688		0,7237
		0,1430		0,3169	1,012	9	1,2546	0,5674		0,7210
		0,1332		0,3137	1,013	1	1,2630	0,5689		0,7280
		0,1961		0,3089	1,011	3	1,1632	0,5664		0,6663
Avg		0,1355		0,3138	1,012	8	1,2600	0,5682		0,7251
s^2		0,0022		0,0000	0,000	0	0,0051	0,0000		0,0018
S		0,0467		0,0030	0,000	8	0,0711	0,0012		0,0427
P(M)		0,0580		0,0037	0,001	1	0,0883	0,0015		0,0530
%	4	2,776 %		1,183 %	0,104 %	6	7,008 %	0,272 %		7,311 %
P(S)		0,1296		0,0083	0,002	4	0,1975	0,0035		0,1185
%	9	5,650 %		2,645 %	0,233 %	6 1	15,671 %	0,609 %	1	6,348 %

Table 29: Calculation of precision limit for multiple and single runs for the calculated t*, w and propulsive efficiency

From Table 29 it can be seen that the accuracy of the effective wake w, the relative rotative efficiency η_R , and the open water efficiency η_0 is well within reasonable values for single runs. The calculated thrust deduction factor t^* show a very large precision limit of 42.776% for the multiple runs and as high as 95.65% for single runs. Two of the values are completely off in different directions from the others.

The precision limit was also calculated for the brake power P_B , and the results are presented in Table 30 below. With a precision limit of 6.2% for single runs it indicates that there are error sources in the model set-up with significant influence. With the differences with and without the Mewis Duct fitted of around 1- 3% depending on wave condition and speed, no certain conclusion can be made regarding the decrease in brake power. Further it should be noticed from the table that only one of the values of brake power are far from the others. If more repeated runs had been made one could disregard such outliers if the deviation was large enough in order to minimize the error and obtain a more certain outcome.

	-
	۲ _B
	18193,162
	18236,565
	18336,540
	18335,645
	19187,762
Avg	18457,935
s^2	170362,188
S	412,750
P(M)	512,496
%	2,777 %
P(S)	1145,976
%	6.209 %

Table 30: Calculation of precision limit for multiple and single runs for brake power

7.5.2 Error Propagation in the calculated thrust deduction

To further investigate the error in the thrust deduction t* it is useful to look at the error propagation. The thrust deduction equation is given as stated earlier:

$$t^* = 1 - \frac{\delta F_D}{\delta T} = 1 - \frac{F_1 - F_2}{T_2 - T_1}$$
(7.10)

To indicate the influence each of the input parameter have on the resulting thrust deduction t^{*}, influence coefficients have been calculated according to Steen (2012):

The reduction equation of the result for which the uncertainty is sought can be written in general as:

$$X = f_r(Y_1, Y_2, ..., Y_N)$$
(7.11)

Here f_r is the functional relation and Y_i is the parameters X depends on. Assuming a small change in parameter Y_i results in a small change in X, a Taylor expansion gives:

$$X = X + \sum_{i=1}^{N} \frac{\partial X}{\partial Y_i} \Delta Y_i + \frac{1}{2} \frac{\partial^2 X}{\partial Y_i^2} \Delta Y_i^2 + O(\Delta Y_i^3) \simeq X + \sum_{i=1}^{N} \frac{\partial X}{\partial Y_i} \Delta Y_i$$
(7.12)

Here X is the result from the measurement. The influence coefficients are from this defined as:

$$\kappa_i = \frac{\partial X}{\partial Y_i} \tag{7.13}$$

Partial differentiation of the function for t*, and with the averaged values of the measurements in the 5 repeated runs as input, gives:

$$\frac{\partial t^*}{\partial F_1} = -\frac{1}{T_2 - T_1} = -0.0466 \tag{7.14}$$

$$\frac{\partial t^*}{\partial F_2} = \frac{1}{T_2 - T_1} = 0,0466 \tag{7.15}$$

$$\frac{\partial t^*}{\partial T_1} = -\frac{F_1 - F_2}{(T_2 - T_1)^2} = -0,0539\tag{7.16}$$

$$\frac{\partial t^*}{\partial T_2} = \frac{F_1 - F_2}{(T_2 - T_1)^2} = 0,0539 \tag{7.17}$$

This indicates that changes in the thrust have slightly more influence on the end result than changes in the tow force.

From this the elemental errors can be calculated as:

$$e_i = \kappa_i \cdot \Delta Y_i \tag{7.18}$$

where for the precision elemental error ΔY_i is the precision error from the repeated measurements, and the combined effect gives:

$$e = \sqrt{\sum_{i=1}^{N} e_i^2} = 0,1208 \tag{7.19}$$

This gives a relative precision error of e/X = 89,10 %, corresponding roughly to the precision limit calculated directly from the 5 measurements in section 7.5.1. The tow force and the thrust are both relatively large quantities compared to the resulting thrust deduction. As it is calculated from dividing the difference in the values at two different conditions, even small deviations in the input values will result in large differences in the output. The scatter in the measured tow force seems to be the main reason for the variation in the thrust deduction.

This again propagates to the hull efficiency η_H with a precision limit of 15.67% for single runs:

$$\eta_H = \frac{1-t}{1-w} \tag{7.20}$$

and further to the resulting propulsive efficiency η_D with a precision limit of 16.35% for single runs:

$$\eta_D = \eta_R \eta_0 \eta_H \tag{7.21}$$

The bias error in the measurement can be investigated in a similar way, but then ΔY_i need to be estimated, which is a more complex and time consuming process.

8 Discussion of Error Sources

The main results in this thesis are based on relative differences with and without the Mewis Duct fitted during the test runs. Therefore keeping the test conditions as equal as possible for the compared runs was of high priority, thus moving most of the precision error to bias error in the measurements. After the tests were completed, some deviation from the original tests with M3030 A, and the Mewis Duct model was observed, and a discussion of possible error sources could provide useful information in that regard. Most notably the tow force in calm water was higher than the original tests with the same rate of revolution and model speed, which indicates an increase of resistance.

Before the tests were conducted the model went through reparation of some surface cracks which could have an impact on the resistance.

After the decision to change waterline, the model draught was a bit larger compared to the DWL, resulting in a larger wetted surface and increased frictional resistance. The weight measured after the test was 2342 [kg] against 2324.6 [kg] at DWL. This is a small detail and result in a minor bias.

The large size of the model resulted in the necessity of a custom setup with the wires from the mid ship beam fastened to a platform behind the model. Despite of careful mounting and test runs this still resulted in a minor yaw angle and uneven towing force SB/PB which could affect the total tow force measurement.

9 Conclusion and Recommendations

In this thesis, the efficiency of a Mewis Duct in waves has been investigated with the use of model tests in the large towing tank at MARINTEK in Trondheim. A "load-varying" self-propulsion method was used, allowing for calculations without the need for results from a resistance test, and hence saves time spent in the tank. The model used was M3030 A, which was originally used to model test the Mewis Duct in still water, and the results was made available for the work on this thesis. Still water, regular and irregular wave conditions was tested in this work.

Some of the results in still water for the current setup were compared to the original results. The model resistance was found to be higher than for the original tests, which was expected from what is known from ageing of the hull, but in a larger order than expected even with the correction applied assuming lower resistance without the propeller present. It could be affected by bias in the tow force measurements, or the execution of the model setup. The effective wake was found to be somewhat larger for the current setup and the difference with and without the duct fitted was larger. The thrust deduction was found to be lower for the current setup, and the results was scattered. The scatter is most likely due to uncertainty in the tow force measurements. This again resulted in the propulsive efficiency being scattered, but it still seems to be higher with the Mewis Duct fitted with an average difference around 2.6%. Brake power was also calculated, and was around 2% lower with the duct fitted compared to 3-5% for different speeds in the original tests.

The wake field into the propeller is an important part of the Mewis Duct, and modification of the wake field in waves is expected to be of importance. The effective wake maintained the relative difference with and without the Mewis Duct in all the wave conditions for both speeds tested. This indicates that the velocity change in the wake field does not affect the efficiency gain with the Mewis Duct compared to still water.

The thrust deduction in waves was very varying, as in the still water measurements. This resulted in both positive and negative difference in the propulsive efficiency with and without the Mewis Duct fitted. No clear trend following the wave length could be seen. The thrust deduction is not necessarily the most important parameter affecting the Mewis Duct in waves, but the scatter influenced the end result in a large degree.

The calculated brake power in waves followed a clear trend with the wave length, peaking around $\lambda/L = 1$. The relative difference with and without the Mewis Duct was in the order of

around 2% for $V_S = 15$ [knots] and below 1% for $V_S = 17$ [knots]. This indicates that the energy savings with the Mewis Duct is still preserved in waves, or at least not severely influenced by waves.

A sensitivity study of the thrust deduction on the propulsive efficiency based on these results from irregular waves was carried out. The results showed that the magnitude of the thrust deduction had relatively little influenc on the end result, but as the differences in thrust deduction with and without the Mewis Duct fitted was varying a lot, both negative and positive efficiency gain with the duct fitted was obtained. This shows the necessity of obtaining accurate values for all the parameters involved in the calculation to get certain results.

An uncertainty analysis was performed based on five repeated runs in one of the wave conditions. The precision limit for the measured quantities and the calculated quantities of interest was calculated. It showed relatively small uncertainty for rate of revolutions, thrust and torque, but the tow force contained more scatter. Influence coefficients calculated for the thrust deduction indicated a large dependency of accurate measurements of thrust and tow force. High uncertainty in the tow force measurement resulted in large scatter in the thrust deduction, and further to the resulting propulsive efficiency. This shows that no certain conclusion regarding the difference in propulsive efficiency in waves can be stated. Precision limit calculated for the brake power show a higher uncertainty than the predicted relative differences with and without the Mewis Duct. This means that a certain conclusion cannot be made from the test results. The analysis indicates that the energy savings with the Mewis Duct are very hard to measure accurate, and with the load-varying propulsion method, accurate measurements of tow force is of high importance. The inaccurate measurements also influence the interpolation to the self-propulsion point. The savings are not necessarily influenced by waves, but further study is needed to be certain.

The two different rates of revolutions for different loading conditions were measured in one run. In order to obtain more accurate measurements of the tow force, the loading conditions should be measured in separate runs to get longer time series to average. More than two loading conditions could also be used in order to verify the linearity of thrust versus tow force. Constant increments of the rate of revolutions could also provide more stable results.

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The regular MARINTEK procedure for propulsion tests could provide more accurate results, as the experience with the load-varying method is rather little for the facility. More time would be required for this, as a set of resistance tests would be needed.

A more comprehensive uncertainty analysis including investigation of the bias in the measurements can be carried out, and with several repeated conditions, and also using former test results. This is complex and time consuming.

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SHIFTIN	G WEIGH	S	Version:	~
			Last update: 20	11.02.21
Project No. Title	846002.19 M3030A-NTNU	Ettervipping etter kjøring med nytt depl VIPPING PITCH k	08.03.2013 dl.14.30	Date:
Client	Sverre Steen	F	11	Sign.:
EMPT	Y CRADLE	Mass Moment of inertia about COG	387,100 202,242	kg kg m2
		Distance from knife to COG (+ downwards) Distance from knife to base line (+ downwards)	0,496 0,450	ΕE
ADDITIONAL	L WEIGHTS	Mass per weight (2 of) Horizontal distance from knife	15,000 3,000	D E
		Vertical distance from knife to weights (+ downwards)	0'002	E
	MODEL	Mass	2342,000	kg
OSCILLATIO	IN PERIODS	Oscillation period without additional weights	8,467	o o
		Osciliation period with additional weights	8,041	Ø
	RESULTS	Moment of inertia about knife	6126,530	kg m2
		Distance from knife to COG (+ downwards) Moment of inertia about COG	0,072 6114,372	kg m2
		KG Bodii of avreation	0,378 1 616	Εß
			1,010	=

APPENDIX A: Results from pendulum test in pitch

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			Version: Last update: 2	1 2011.02.21	
^o roject No. Title	846002.19 M3030A-NTNU	Ettervipping etter kjøring med nytt depl TOMVIPPE FOR PITCH	08.03.2013 kl.10.00	Date:	
Client	Sverre Steen		T.I.	Sign.:	
EMPTY	Y CRADLE	Mass Moment of inertia about COG	000'0	kg m2	
		Distance from knife to COG (+ downwards) Distance from knife to base line (+ downwards)	0,000 0,000	EE	
ADDITIONAL	- WEIGHTS	Mass per weight (2 of) Horizontal distance from knife	15,000 3,000	<u>ð</u> E	
		Vertical distance from knife to weights (+ downwards)	0,005	ε	
	MODEL	Mass	387,100	kg	
DSCILLATIO	N PERIODS	Oscillation period without additional weights Oscillation period with additional weights	2,497 3,447	ა ა	
	RESULTS	Moment of inertia about knife Distance from knife to COG (+ downwards)	297,637 0,496	kg m2 m	
		Moment of inertia about COG KG	202,242 -0,496	kg m2 m	
		Radii of gyration	0,723	E	

dato: 8/3-2013 61 1439 sign: T. 1

M 3030A NTWU Effersipping wed myth depl.

Vipping i pith





Dette gir



Ballansert i vippa målt fra sp 0:

dato: 8/3-2013 Lal. 1000 sign:

millimeter

(Ettenhoring etter torode) M3030A (NTNO Tonvippe for pitch





APPENDIX B: Instrument calibration

	bjelkegiver	8671
Dato:	2012-03-01	
Tid:	10:36:00	
Operatoer:	MKo	
Gyldig til:		
Kalibreringsenhet:	20208	
MGC:	1089	
Målefrekvens [Hz]:	25	
Målelengde [s]:	3	

Slot:	5.1
ML-type:	ML801
AP-type:	AP810
Brotype:	SG full bridge
Brospenning [V]:	5
Filtertype:	Bess
Filterfrekvens [Hz]:	5
Målemetode:	Net
ML-serienummer:	040054081101
AP-serienummer:	104127001
Fysisk enhet:	kg
Skalering:	9.8066
Elektrisk enhet:	mV/V
Måleenhet:	Ν

	Sensitivity:	Span:
Kalibrering org.	1.0000 mV/V	2769.9254 N
Kalibrering mod.	1.0000 mV/V	2769.9254 N

Stigningsfaktor:	2769.925353 N/(mV/V)	+/- NaN N/(mV/V)
Nullpunkt:	0.000865 mV/V	
Største målefeil:	0.222772 N	

Beskrivelse av giver:
Notater til kalibreringen:

v. 3.8.1

	bjelkegiver	8672
Dato:	2012-03-01	
Tid:	10:50:00	
Operatoer:	MKo	
Gyldig til:		
Kalibreringsenhet:	20208	
MGC:	1089	
Målefrekvens [Hz]:	25	
Målelengde [s]:	3	

Slot:	5.1
ML-type:	ML801
AP-type:	AP810
Brotype:	SG full bridge
Brospenning [V]:	5
Filtertype:	Bess
Filterfrekvens [Hz]:	5
Målemetode:	Net
ML-serienummer:	040054081101
AP-serienummer:	104127001
Fysisk enhet:	kg
Skalering:	9.8066
Elektrisk enhet:	mV/V
Måleenhet:	Ν

	Sensitivity:	Span:
Kalibrering org.	1.0000 mV/V	2774.6565 N
Kalibrering mod.	1.0000 mV/V	2774.6565 N

Stigningsfaktor:	2774.656465 N/(mV/V)	+/- NaN N/(mV/V)
Nullpunkt:	0.004674 mV/V	
Største målefeil:	0.161343 N	

Beskrivelse av giver:
Notater til kalibreringen:

v. 3.8.1

Dynamometer	Thrust	Moment	Kalib Dato
20025 7	7 10/ 0000	6.0072	05 10 2012
20025 7	0 100 /000	5 5276	21.09.2012 Annet fortegn pa
20020 7	0 120.4920	-0.0270	31.00.2012 momentet
20027 10	8 125.3709	-0.0109	31.08.2012 dersom det er
20028 18	5 126.4874	-5.883	31.08.2012 Venstregaende
20029 18	6 130.1179	-5.585	07.08.2012 propell.
20030 1	2 292.9958	-14.3521	09.11.2012 Alle dynamometrene
20031 10	3 290.9525	-12.1305	09.11.2012 er Kalibreit med
20032 18	0 285.0361	-12.1848	07.08.2012 MOC+
20033 21	0 296.8082	-12.718	09.11.2012 1mv/v
20034 21	1 291.4244	-12.6785	15.01.2013
20035 13	6 500.0068	-18.687	14.08.2012
20324	294.8288	-12.2373	05.10.2012
20325	291.9568	-12.2352	08.08.2012
20326	493.4209	-18.4668	08.08.2012
	Span 2mv/v	,	
20046 Towrope	e 79.746		07.02.2012
20236 Rtm	492.4287		26.10.2012
Sidekraftmåler	Span 2mv/v	,	
20059 FP	-354.015		07.02.2012
20060 AP	-342.981		07.02.2012
Dysedynamometer	Span 2mv/v	,	
20039	689.6922		23.02.2012
20040 2	2 -201.3612		23.02.2012
20041 2	3 -200.402		14.02.2012
20042 2	7 -223.3325		22.02.2012
20043 1	9 -422.538		16.10.2012
20044	148,1724		14.03.2012
20045	153,4118		14.03.2012
20049	692 1631		12 03 2012
8575	637 9015		16 10 2012
0070	Thrust	Moment	10.10.2012
Frinrøvehåt	Span 2mv/v	Span 2mv/v	
20048 Frip dyn	-516.919	18.05	31.03.2011
Trimgivere	Span 80mv/	/v	
6042 Fp	-349 5458	-	mm/v vender bakover 13 03 2012
6042 Fp	323 9223		mmy vender forover 13 03 2012
6044 Ap	-337 5956		mm/v vender forover 13.03.2012
6044 Ap	317.8351		mm/v vender bakover 13.03.2012

Kalibreringsdato:11.09.2012		Kalibreringsdato:11.09.2012			Kalibreringsdato:21.09.2010		
20001	mmH2O Pa	20003	mmH2O	Pa	20004	mmH2O	Pa
CS	197.723 1939.000	CS	98.638	967.308	CS	103.007	1010.154
CP	198.486 1946.483	CP	98.982	970.682	CP	102.376	1003.966
SP	199.543 1956.848	SP	99.068	971.525	SP	100.599	986.539
СТ	200.832 1969.489	СТ	98.846	969.348	СТ	102.888	1008.987
CB	197.158 1933.460	CB	99.312	973.918	CB	93.915	920.992
TB	197.607 1937.863	TB	100.849	988.991	тв	101.804	998.356

APPENDIX C: Irregulare wave calibration





APPENDIX D: Measured values in the self-propulsion tests

	V _m	n ₁	T ₁	Q ₁	Q _{corr}	T _{corr}	F _{D1}
TEST NO.	[m/s]	[Hz]	[N]	[Nm]	[Nm]	[N]	[N]
6100	1,385831	6,6584	27,4219	0,8862	0,871507	27,41381	20,1834
6111	1,478219	7,1541	31,6941	1,0239	1,008761	31,67953	22,2062
6120	1,570608	7,6508	36,3271	1,1753	1,159714	36,30604	24,8972

Measured values in calm water propulsion with the Mewis-Duct fitted:

	V _m	n ₂	T ₂	Q ₂	Q _{corr}	T _{corr}	F _{D2}
TEST NO.	[m/s]	[Hz]	[N]	[Nm]	[Nm]	[N]	[N]
6100	1,385831	7,9921	46,9563	1,4833	1,467407	46,94821	2,8234
6111	1,478219	8,4872	52,5504	1,6597	1,643362	52,53583	4,0914
6120	1,570608	9,0383	59,2818	1,8727	1,855866	59,26074	4,6333

Measured values in calm water propulsion without the Mewis-Duct fitted:

	V _m	n ₁	T ₁	Q ₁	Q _{corr}	T _{corr}	F _{D1}
TEST NO.	[m/s]	[Hz]	[N]	[Nm]	[Nm]	[N]	[N]
6200	1,385831	6,6599	24,6051	0,8326	0,817906	24,59701	21,3452
6210	1,478219	7,1556	28,4322	0,961	0,94586	28,41763	23,8411
6220	1,570608	7,6532	32,8404	1,1056	1,090012	32,81934	26,2208

	V _m	n ₂	T ₂	Q ₂	Q _{corr}	T _{corr}	F _{D2}
TEST NO.	[m/s]	[Hz]	[N]	[Nm]	[Nm]	[N]	[N]
6200	1,385831	7,9947	43,3001	1,4086	1,392705	43,29201	4,6233
6210	1,478219	8,4896	48,2456	1,5731	1,556759	48,23103	5,5905
6220	1,570608	9,027	54,5426	1,7804	1,763576	54,52154	6,6314

	V _m	n ₁	T ₁	Q ₁	Q _{corr}	T _{corr}	F _{D1}
TEST NO.	[m/s]	[Hz]	[N]	[Nm]	[Nm]	[N]	[N]
2200	1,385841	6,66	26,58	0,8501	0,835406	26,57191	36,22
2210	1,57062	7,652	35,3	1,134	1,118413	35,27894	40,26
2220	1,385841	6,66	26,9116	0,8573	0,842606	26,90351	44,25
2230	1,57062	7,652	35,58	1,142	1,126413	35,55894	47,329
2240	1,385841	6,659	27,137	0,8657	0,851007	27,12891	57,8
2251	1,57062	9,0201	58,9247	1,8666	1,849782	58,90364	46,613
2260	1,385841	6,659	27,1942	0,8825	0,867807	27,18611	80,7642
2271	1,57062	9,0247	59,2661	1,8751	1,858278	59,24504	67,4282
2280	1,385841	6,658	27,2281	0,8826	0,867908	27,22001	55,9423
2290	1,57062	7,6514	35,84	1,1678	1,152214	35,81894	69,4228
2300	1,385841	6,6585	27,0304	0,8797	0,865007	27,02231	43,369
2310	1,57062	7,6517	35,8777	1,1684	1,152813	35,85664	57,0195
2320	1,385841	6,7083	27,8442	0,9032	0,888463	27,83611	33,2794
2330	1,57062	7,6518	35,8607	1,1666	1,151013	35,83964	41,7984

Measured values for propulsion in regular waves with the Mewis-Duct fitted:

	V _m	n ₂	T ₂	Q ₂	Q _{corr}	T _{corr}	F _{D2}
TEST NO.	[m/s]	[Hz]	[N]	[Nm]	[Nm]	[N]	[N]
2200	1,385841	8,19	49,41	1,546	1,529929	49,40191	16,1
2210	1,57062	8,934	56,52	1,781	1,764259	56,49894	22,6
2220	1,385841	9,023	64,3856	2	1,983179	64,37751	13,834
2230	1,57062	9,38	65,1976	2,05	2,032858	65,17654	24,4831
2240	1,385841	9,375	71,7968	2,2297	2,212563	71,78871	21,4761
2251	1,57062	10,3103	84,6661	2,6445	2,626521	84,64504	24,85
2260	1,385841	10,6972	100,9327	3,0904	3,072073	100,9246	24,615
2271	1,57062	11,4873	112,5361	3 <i>,</i> 4695	3,450461	112,515	25,2563
2280	1,385841	10,0096	85,0277	2,6234	2,605691	85,01961	10,2895
2290	1,57062	10,9957	100,452	3,1079	3,089304	100,4309	15,2248
2300	1,385841	9,5024	74,4078	2,3086	2,291348	74,39971	4,7605
2310	1,57062	10,0146	78,4703	2,4547	2,436987	78,44924	21,1281
2320	1,385841	7,993	46,7053	1,4783	1,462406	46,69721	16,6013
2330	1,57062	8,8346	55,3831	1,7609	1,744249	55,36204	26,405

	V _m	n ₁	T ₁	Q ₁	Q _{corr}	T _{corr}	F _{D1}
TEST NO.	[m/s]	[Hz]	[N]	[Nm]	[Nm]	[N]	[N]
2400	1,385841	6,6602	23,6961	0,8061	0,791406	23,68801	35,7039
2410	1,57062	7,6539	31,7544	1,0801	1,064511	31,73334	41,1546
2420	1,385841	6,66	24,0878	0,8159	0,801206	24,07971	44,4579
2430	1,57062	7,6535	31,9547	1,0854	1,069812	31,93364	49,2518
2440	1,385841	6,6599	24,2142	0,8214	0,806706	24,20611	59,4681
2450	1,57062	7,6533	32,0933	1,0894	1,073812	32,07224	65,9027
2460	1,385841	6,6599	24,1262	0,8202	0,805506	24,11811	82,3554
2471	1,57062	7,6534	32,1935	1,0928	1,077212	32,17244	94,1144
2480	1,385841	6,6602	24,2847	0,822	0,807306	24,27661	61,0289
2490	1,57062	7,6534	32,3169	1,0949	1,079312	32,29584	71,9374
2500	1,385841	6,6601	24,0896	0,8166	0,801906	24,08151	46,4505
2510	1,57062	7,6538	32,2843	1,0955	1,079912	32,26324	61,4953
2520	1,385841	6,6599	24,256	0,8212	0,806506	24,24791	35,4661
2530	1,57062	7,6537	32,3312	1,0937	1,078112	32,31014	45,2931

Measured values for propulsion in regular waves without the Mewis-Duct fitted:

	V_m n_2 T_2		Q ₂	Q _{corr}	T _{corr}	F_{D2}	
TEST NO.	[m/s]	[Hz]	[N]	[Nm]	[Nm]	[N]	[N]
2400	1,385841	8,2264	46,0234	1,4993	1,483196	46,01531	16,954
2410	1,57062	8,8943	51,2006	1,6824	1,665695	51,17954	24,371
2420	1,385841	9,025	59,9099	1,9281	1,911278	59,90181	15,5999
2430	1,57062	9,386	60,221	1,9626	1,945453	60,19994	25,697
2440	1,385841	9,3795	66,9388	2,1413	2,124158	66,93071	22,2307
2450	1,57062	10,313	78,6586	2,5276	2,509618	78,63754	26,5782
2460	1,385841	10,7	95,3004	2,9848	2,96647	95,29231	26,7189
2471	1,57062	11,4907	106,1806	3,3405	3,321458	106,1595	37,0476
2480	1,385841	10,013	80,0742	2,5282	2,510488	80,06611	13,1808
2490	1,57062	10,9997	94,4784	2,9914	2,9728	94,45734	19,2891
2500	1,385841	9,5082	69,4824	2,2111	2,193843	69,47431	5,9112
2510	1,57062	10,0195	72,9015	2,3441	2,326382	72,88044	23,3252
2520	1,385841	7,9946	42,9641	1,4003	1,384405	42,95601	19,0467
2530	1,57062	8,8372	50,6473	1,661	1,644347	50,62624	28,1691

APPENDIX D: Results of model tests of the Mewis Duct

No.	Towing Tank	Ship type	DWT	V [kts]	СВ	CTh	Power r Design T	eduction Ballast T
1	HSVA	BC	118k	14,5	0,847	2,27	6,9	6
2	SVA	BC	12k	15,5	0,794	1,88	8	7,4
3	HSVA	BC	45k	15,2	0,802	1,43	6	5,4
4	SSPA	BC	41k	15,2	0,795	2,1	6	11
5	SSPA	VLCC	318k	16	0,813	2,24	6,4	7,8
5a	HMRI	"	"	"	"	"	6,2	7
6	SSPA	BC	180k	15,2	0,847	1,98	5	8,5
7	HSVA	СОТ	158k	14,6	0,821	1,4	3,9	-
8	HSVA	HLC	20.5k	17,5	0,765	1,83	1,5	-
9	HSVA	BC	57k	14,4	0,848	2,05	5,4	7,2
10	HSVA	BC	163k	14,5	0,817	2,25	5,2	6,6
11	HSVA	BC	75k	16	0,879	1,86	4,5	7,1
12	SVA	RoRo	38.5k	20,2	0,687	1,1	2,7	3,4
13	MARINTEK	BC	37.5k	15	0,776	2,32	7,6	7,8
13a	MARIN	"	"	"	"	"	6,5	6,2
14	MARINTEK	BC	40k	15	0,808	2,75	9	10
15	MARIN	VLCC	306k	15,3	0,821	2,1	8,7	7,6
16	SVA	BC	45k	15,6	0,8	1,98	6,5	8,9
17	HSVA	BC	151k	15,6	0,815	2,24	5,3	-
18	MARINTEK	BC	35k	14,2	0,83	2,31	6,5	9
19	SVA	СОТ	74.7k	15	0,856	1,74	4,9	5,4
20	SVA	BC	82k	16,8	0,876	2	5,1	-
21	HSVA	BC	286k	15,4	0,85	2,14	7,6	10,2
22	HSVA	MPC	31k	18	0,755	1,16	3,6	3,3
23	HSVA	MPV	47,8	15,5	0,795	1,37	2,4	-
24	SSPA	BC	82k	14,5	0,87	1,79	5,7	10,5
25	HMRI	VLCC	318k	16	0,814	2,18	6	-
26	FORCE	BC	35k	14	0,818	1,43	1,8	4,6
26-	CCDA						inval.	inval.
208		" DC	" 205k	" 14 C	" 0 0 2 2	" 2 1 7	4,5 7 0	-
2/			205K	14,0	0,052	2,17	7,Z	- 70
20		BC	100K	15,4	0,652	2,50	4,0	0.7
29	HMRI	VICC	318k	16	0,791	2,50	5,0	5,7
21	SSPA	COT	11/1	15.2	0.83/	2,2	5 1	_
32	FORCE	BC	32k	13,2	0,004	2,37	6.8	_
32	SSPA	т	150k	14	0 774	1 74	۵,5 4 7	_
34	SV/A	BC	37 5	14 5	0.833	2.79	7.8	89
35	HSVA	BC	63.5k	14.5	0.86	1.45	0,9	2.5
36	SVA	BC	49,6k	14,5	0,795	1,74	5,6	9

The table below is reproduced from Mewis (2012).

37	SVA	BC	57k	13,9	0,861	2,86	8,1	-
38	SSPA	BC	53k	14	0,848	2,5	3,4	3,7
39	MOERI	BC	157k	15	0,819	2,11	5,6	6
40	SVA	BC	58k	13,9	0,841	2,37	10,2	-
41	HSVA	BC	40k	15	0,803	1,9	6,3	-
42	FORCE	BC	52k	15,4	0,772	1,57	4,7	6,2
43	MARINTEK	Т	74,7	14,6	0,843	2,45	4,5	-
44	HSVA	BC	36	14,1	0,82	1,63	6,1	7,2
45	SSPA	BC	105	14,2	0,817	2,37	5,6	5,7
46	SSPA	Т	316	16	0,813	1,78	7,1	7,2
47	SVA	BC	35k	14	0,805	1,35	3,2	5,2
48	FORCE	BC	113k	14,6	0,834	2,29	6,6	-
			avera	ge design/	ballast		5,8	7,1
			aver	age of all t	tests		6,3	