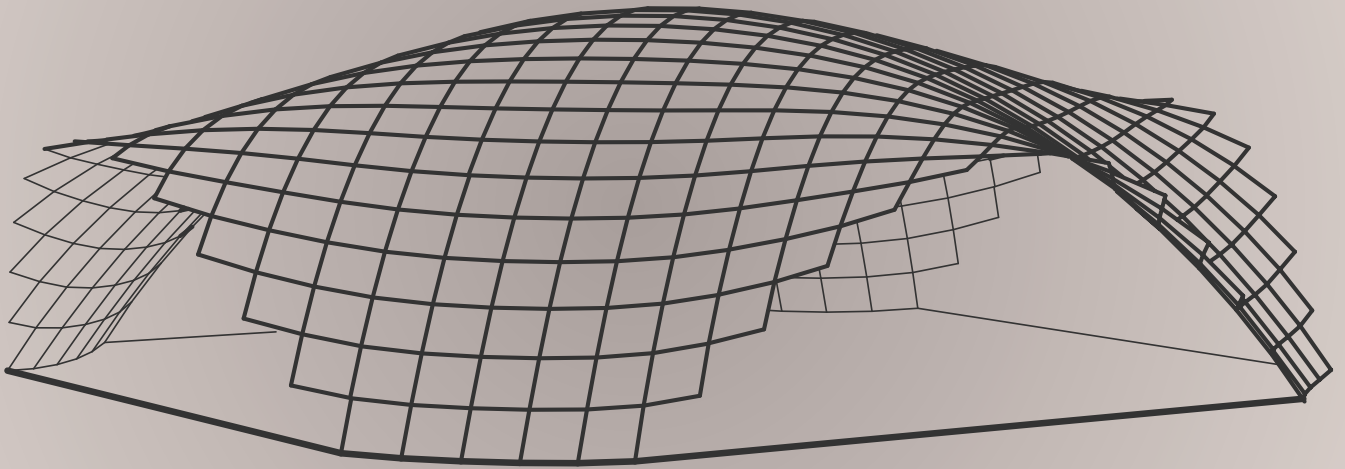


GRIDSHELL

MANUAL



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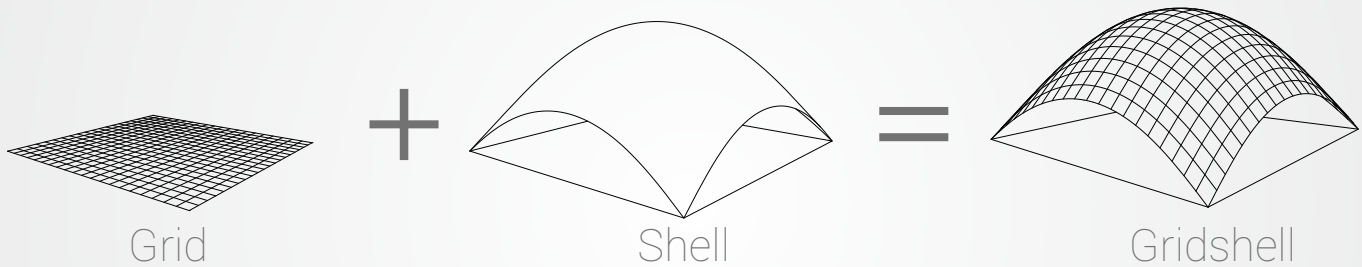
This manual is a part of a master thesis project at NTNU, Spring 2015.

This project is inspired by the work of the gridshell.it group. A special thanks to Sergio Pone, Sofia Colabella and their team!

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WHAT IS A GRIDSHELL?



EXPLANATION

A gridshell is a structure which derives its strength from its double curvature (in a similar way that a fabric structure derives strength from double curvature), but is constructed of a grid or lattice.

Wikipedia

WHAT IS A GRIDSHELL?

Shortly said, a shell is a construction type that carries loads through membrane forces, or in-plane stresses, rather than bending and shear forces. While a concrete shell is a continuous surface, a gridshell is divided in a grid of smaller elements.

A way to create gridshells are the kinematic construction process. It consists of building a rectangular or quadratic grid flat, and then deform it into shape by pulling together or lift parts of the grid. Wood is an appropriate material, because of its good bending attributes. It is fairly simple to construct a timber gridshell out of straight elements

The model and process described in this manual, is based on this construction method.

Why gridshell?

The main reason to pick a gridshell construction is not only based on performance, efficiency and cost, but on architectural shape. Based on a gridshell, one can construct spectacular shapes and characteristic buildings. In addition you have got the spatial attributes, which is important for the use of the building. A self bearing construction gives flexibility in the interior.

How gridshell?

The shape of the gridshell must be structural, which demands an understanding from the architect and collaboration with the structural engineer. One can not make decisions solely based on design ideas but have to do it in harmony with the structural shape. Also, the structure must be stable during the whole construction process.

This model and process described in this manual, describes how designing and construction could be done in such a manner.

DICTIONARY

Anchor Points is the same as foundation.

Bending strength, see Flexural strength.

Catenary is the shape of a hanging chain or cable supported at the ends. The inverted shape is ideal for compression only structures. The shape is also called funicular. (See page 12).

Compressive strength is the capacity of a material or structure to withstand loads tending to reduce size.

Curvature is a measure of how a line deviates from being flat. See Radius of curvature.

Dynamic relaxation is a numerical method that can be used for form finding for cable and fabric structures. By adding different forces, it aims to find a state, or geometry where all forces are in equilibrium.

E-module, see Young's Modulus.

An **Elastic modulus** is a number that measures an object or substance's resistance to being deformed elastically (i.e., non-permanently) when a force is applied to it. It includes Young's modulus (E), Shear Modulus (G) and Bulk Modulus (K).

Equilibrium is a state when the system (eg. a gridshell) is in balance, resulting in no internal shape change.

Flexural strength is defined as a material's ability to resist deformation under load. Flexural stress causes both compressive and tensile stresses, and is similar to tensile strength for homogeneous materials. See page 36.

DICTIONARY

Finite Element Method, or FEM is simply said an advanced method of structural analysis. It divides the structure into smaller parts, finite elements, and adds material values and loads to calculate load distribution.

Funicular, see catenary.

Grasshopper is a graphical programming plugin for Rhino. See page 50.

a **Particle spring system** is a method of formfinding, that is a collection of points collected by springs and acted on by external forces. This method is implemented in our process using Kangaroo for Rhino.

Radius of curvature is mathematically the inverse of curvature, $R=1/k$. It is on a point on a curve, defined as the radius of a circle that best approximates that curve. The maximal bending of a wood lath is defined with a 'smallest possible' radius. (See page 36).

Rhino is a NURBS based CAD software. (See page 50).

Tensile strength, or Ultimate strength is the maximum stress a material can withstand beeing stretched or pulled.

Karamba is an element analysis plugin for Grasshopper. See page 50.

Kangaroo is a physics engine plug-in for Grasshopper. See page 50.

The **segment-lath** is the "weaved" lath-principle developed during this master-thesis.

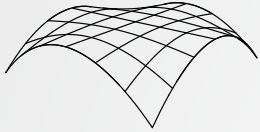
Shear modulus describes a material's response to shear stress and is defined as the ratio of shear stress to the shear strain.

Young's modulus is a measure of stiffness of a material, along an axis to the strain. For material properties of wood see page 36.

Definitions from wikipedia



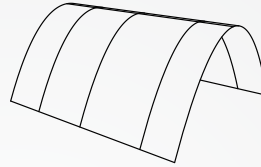
Good and bad shape



1: Bad shape



2: Good shape



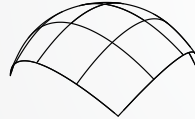
3: OK shape



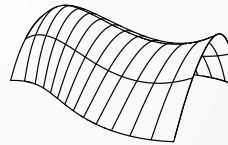
4: Good shape



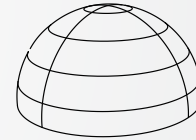
5: Bad shape



6: OK shape



7: Good shape



8: OK shape

EXPLANATION

There are many different parameters that decides if it is a good shape or a bad shape. Generally, form follow function, but when it comes to gridshells, forms mostly follows forces.

1. Bad because it is too flat on the top.
2. Good because it is doubled curved.
3. OK because it is very curved in one direction, but is straight in the other.

4. A good, doubled curved shape. A good shape doesn't have to be symmetrical.

5. Only singled curved and has kinks in it's curvature.

6. OK shape, but not good because the edges are cantelivering too much.

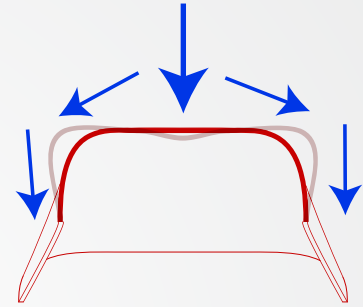
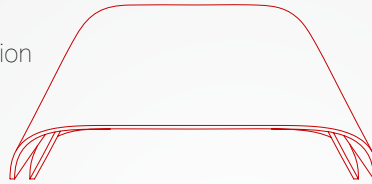
7. Good. Curved in two directions.

8. Conidering only shape, it is perfect, but it is not possible to create a gridshell like that from a flat grid.

Why good shape, why bad shape

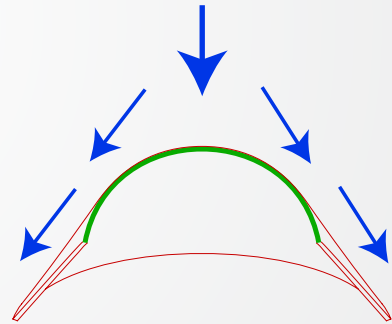
Flat top

Is unfavourable and can lead to deformation



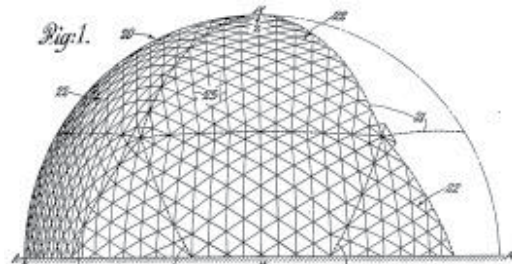
Tall arc

A clear shape distributes the forces correctly



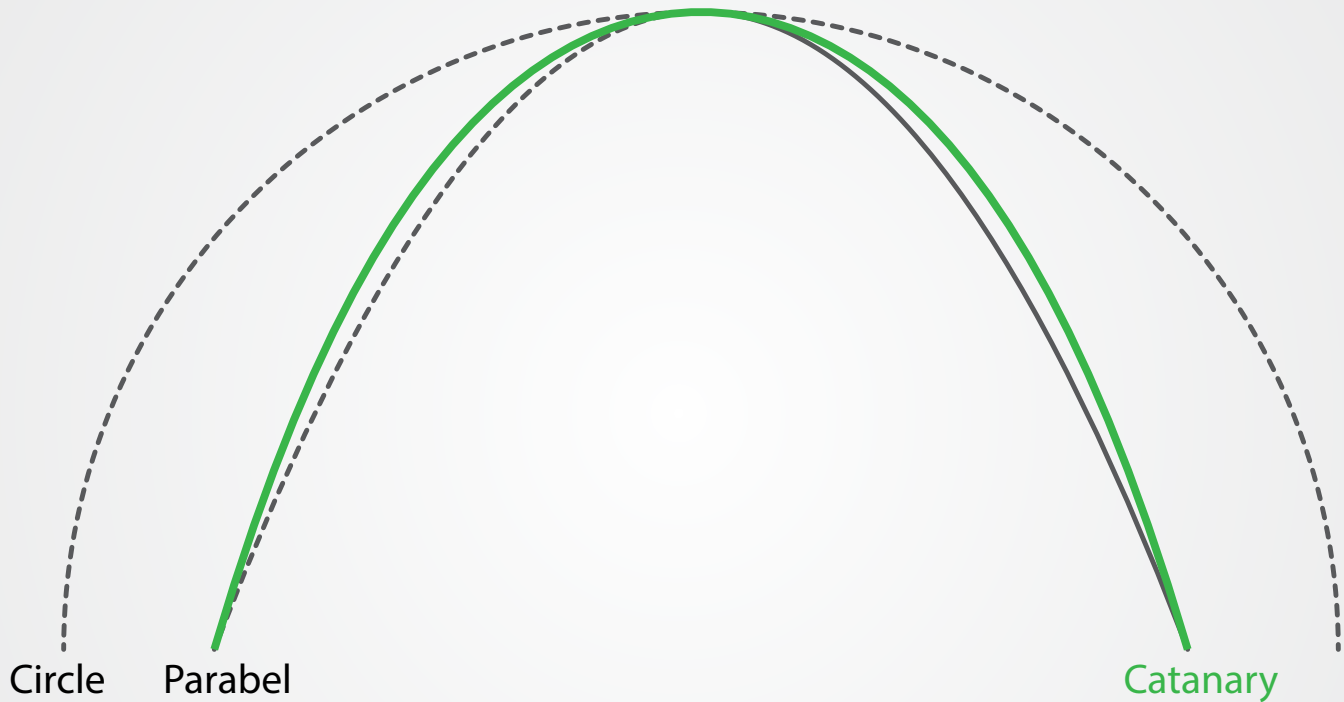
EXPLANATION

The most important check to do on your shape is controlling top area. If it gets too flat, it will function more like a beam than a shell, and will more easily deform.



The optimal shape would be a spherical dome, but this shape is impossible to deform from a flat grid. Drawing: Buckminster Fuller

Curve Principles



EXPLANATION

The circle and the parabel are easy to draw, but the catenary curve is the perfect curve for even load distribution.

Wikipedias definition:

In physics and geometry, a catenary is the curve that an idealized hanging chain or cable assumes under its own weight when supported only at its ends.

Catanary curves works only in tension. When flipped the curve will be in compression. Since the shell is very thin, it doesn't have any bending capacity and has to absorb most forces through compression.

Taking into account material parameters, such as bending capacity, we also know that this shape is not optimal for gridshell.

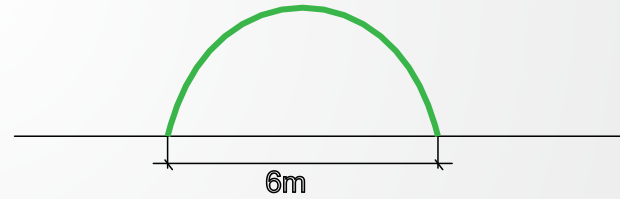
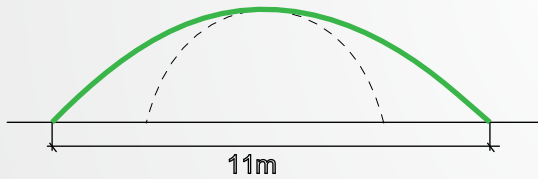
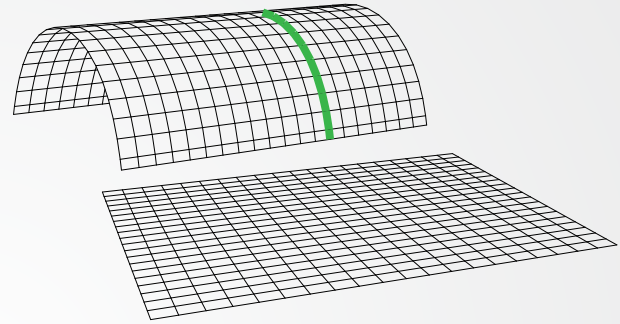
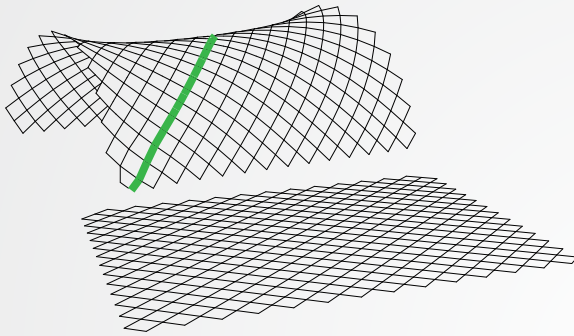
Curve principles



P: Kamel 15, wikipedia



Diagonal vs orthogonal grid

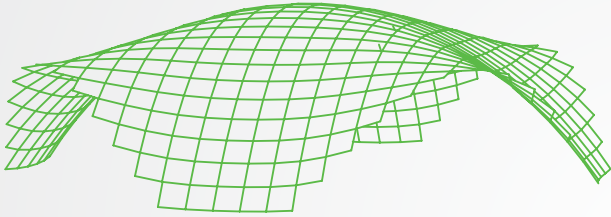


EXPLANATION

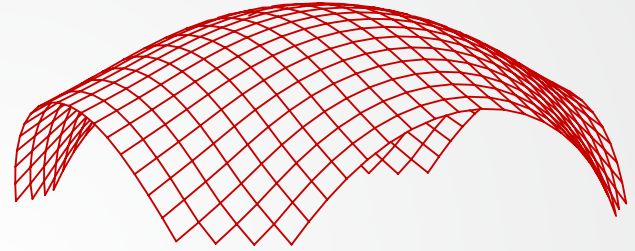
An important design parameter is to choose either an orthogonal or a diagonal grid-layout. The same geometry can have totally different results. As the example shows, the orthogonal grid has laths that has the same curvature as the shape it self. But the diagonal laths are much less curved.

The diagonal pattern can be useful when designing small gridshells. This because the bending capacity often is the biggest challenge.

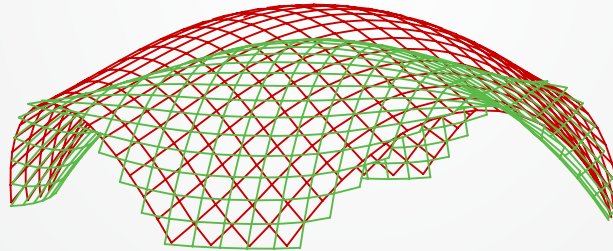
Diagonal vs orthogonal grid



Diagonal



Orthogonal



EXPLANATION

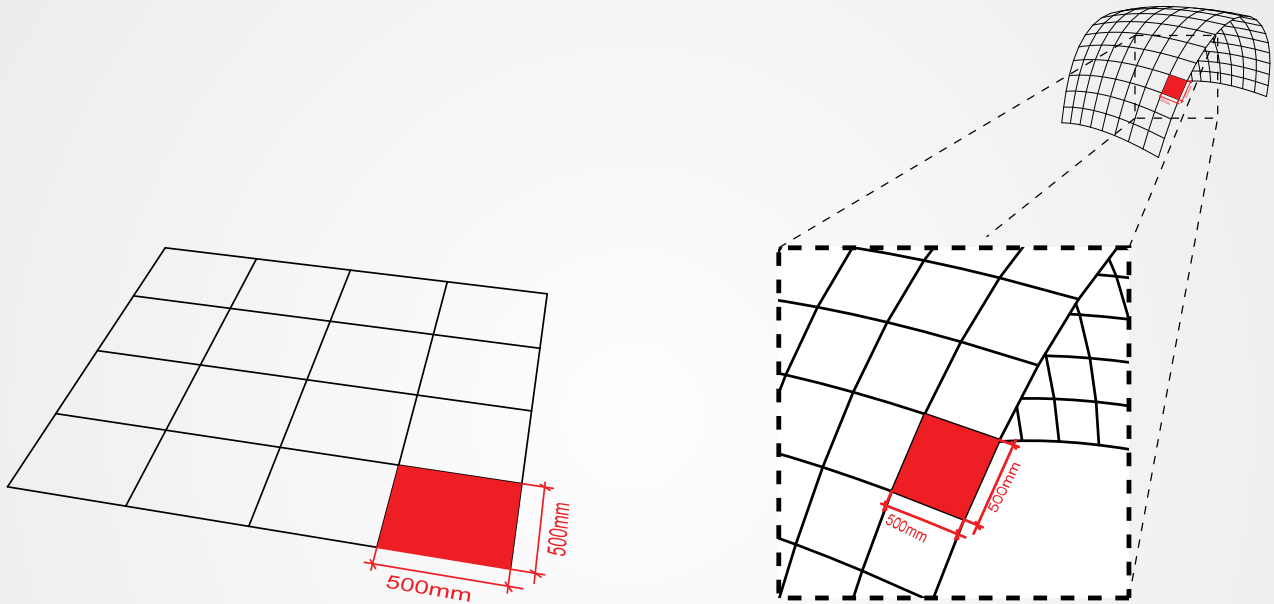
Both examples above have the same anchorpoints and the same original grid properties.

The grid-direction determines how the forces are being distributed through the laths, and

this affects the form-finding of the shape.

The orthogonal grid is pushed to the limits of its curvature, while the diagonal grid still can handle a taller top and smaller distance between anchors.

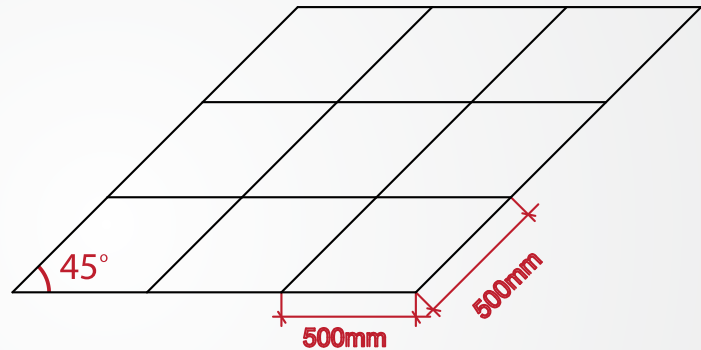
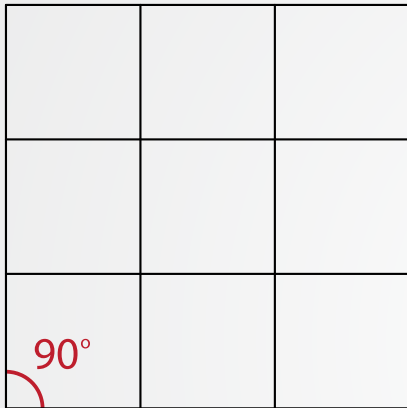
Fixed grid dimension



EXPLANATION

An important precondition is that every member in the gridshell has a fixed length. This counts for both the flat grid, during the shaping and for the final shape.

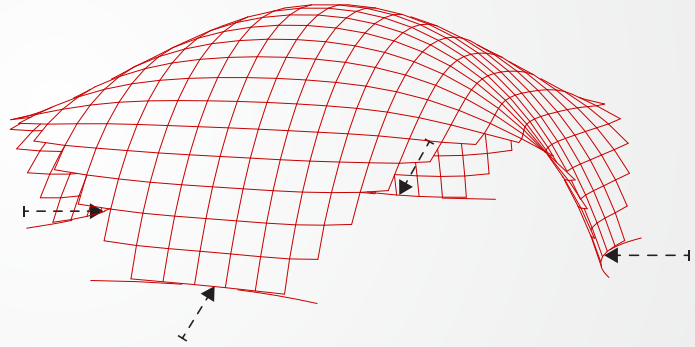
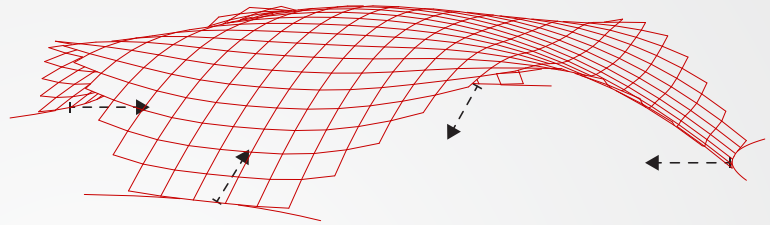
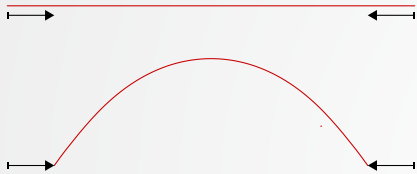
Fixed grid dimension



EXPLANATION

Every joint in the gridshell should allow normal rotation. This is important to be able to form the shape from a flat grid. When the shape is set, diagonals can be attached to lock the shape.

Anchor point controlled



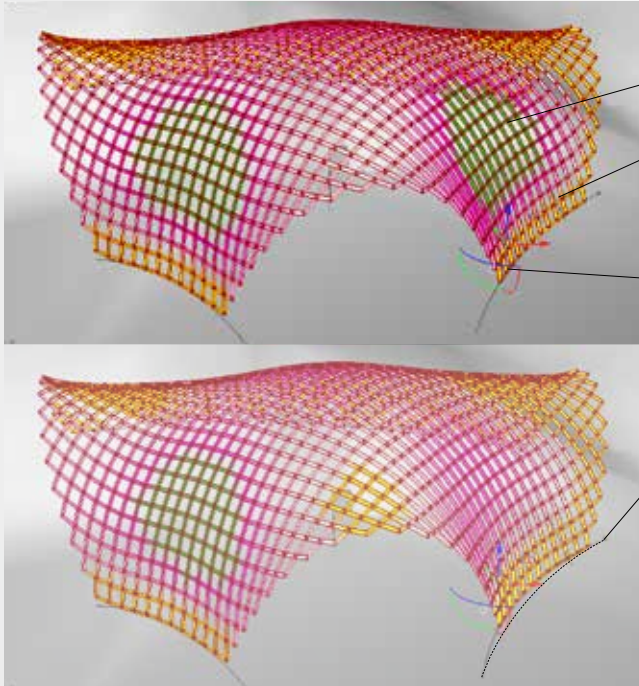
EXPLANATION

The kinematic construction process is done by forcing a flat grid into its shape.

A key element in this process is placing the anchor points. In addition to the material characteristics of the wood, this is what shapes the structure.

In the same way a line (straight beam) takes the shape of a curve when pushing the ends together, the flat grid takes the shape of a shell when the anchorpoints is moved. See more at page 63.

Small changes - big impact



Green indicates high (relative) deformation.

Yellow indicates no (relative) deformation

Moving the center of the anchor line 30 cm changes the load distribution dramatically

Knowing what a good shape looks like, and how to control it is very important

EXPLANATION

These screenshots from Karamba shows that small anchor-point transformations, leads to big deformation changes.

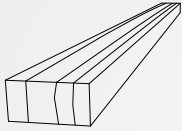
Moving the center of the anchor-line 30 cm, removes the large deformations (green color).

This is why it is very important to replicate the digital shape as good as possible. Small differences changes the load distribution totally.

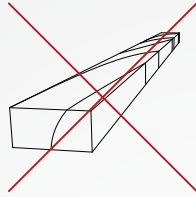


SCALE MODELING

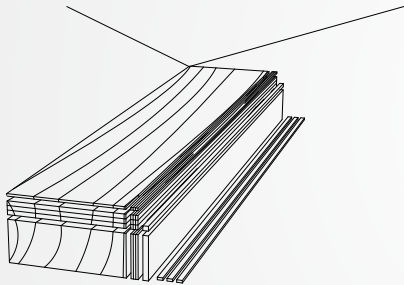
Scale model materials



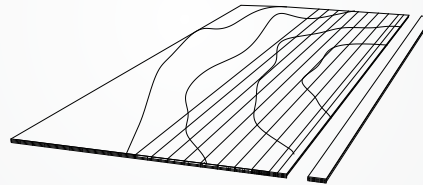
Straight wood grains



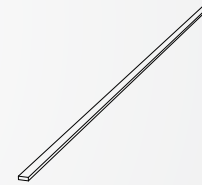
Curved wood grains



Wood laths



Plywood laths



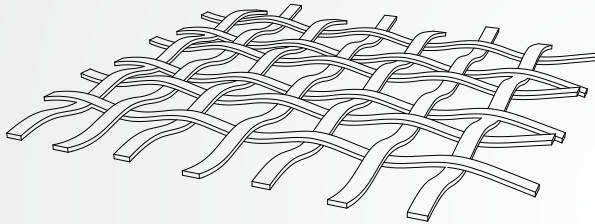
Plastic

EXPLANATION

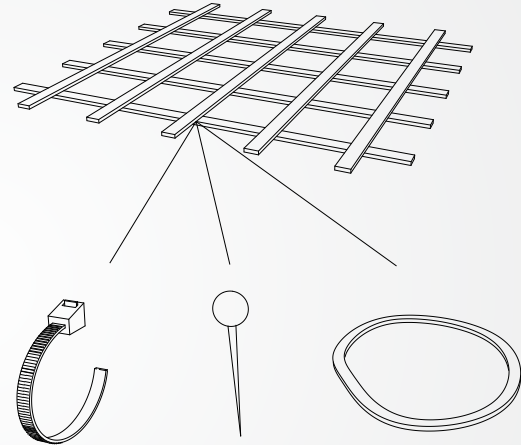
To get a feeling on how forces apply to the grid, scale modeling is recommended.

The best material for building is wooden laths. It is then important to avoid wood blanks with curved grains or knots.

Scale model techniques



Weaving
Fast and flexible



Strips
Slow and stiff

Needles
Slow and stiff

Rubber bands
Slow but flexible

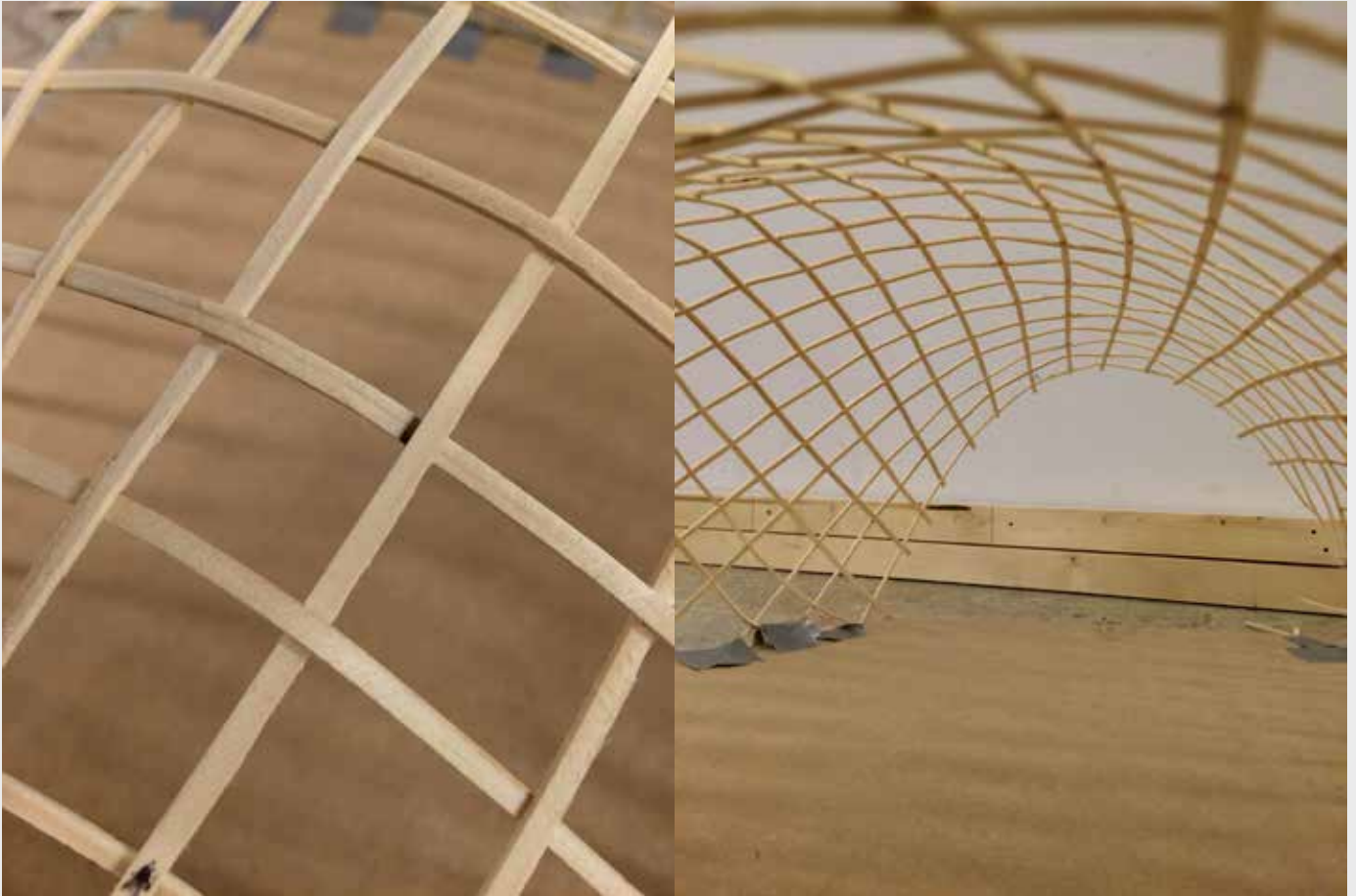
EXPLANATION

The far best modeling method is weaving. This is only possible with materials with some friction, such as wood or plywood. This technique is the fastest, and it also allows rotation and some movement.

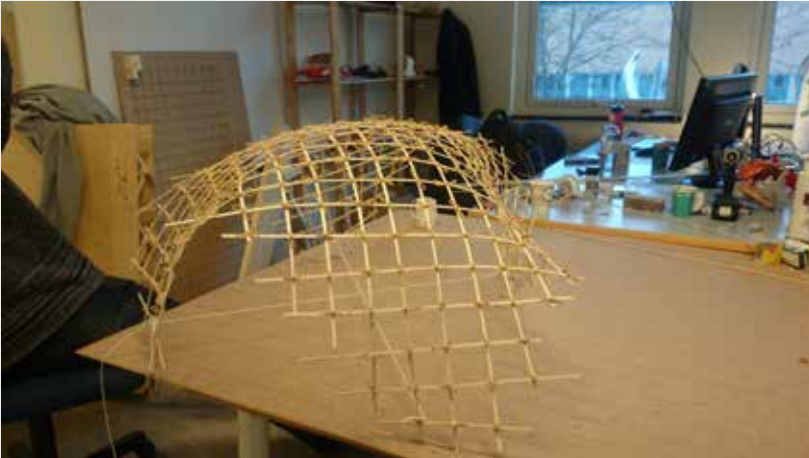
We learned this method from gridshell guru and leader of the research group gridshell.it, Sergio Pone.

Other techniques are not recommended, but the best alternative is to use rubberbands and tie a knot around every joint.

Weaving model technique



Other modelling techniques



Rubberbands

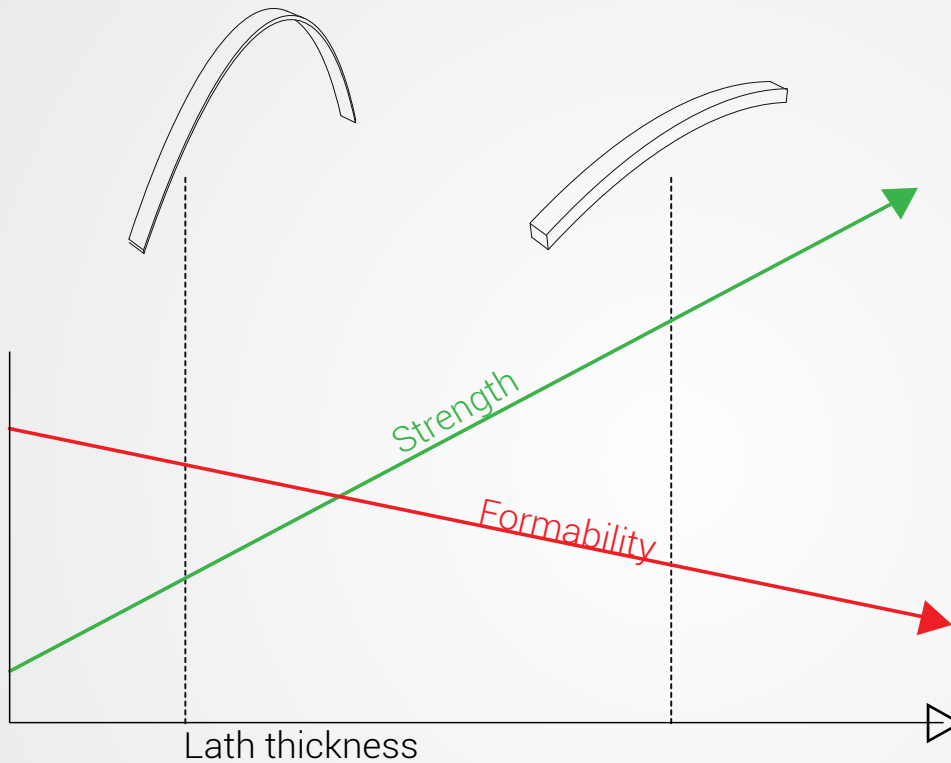


Needles and screws



DEFINING
MATERIAL
PROPERTIES

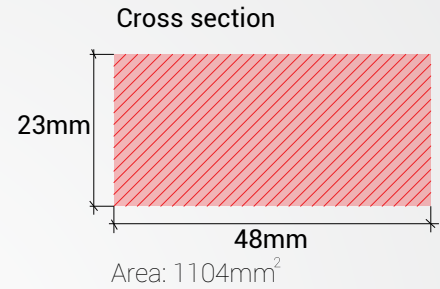
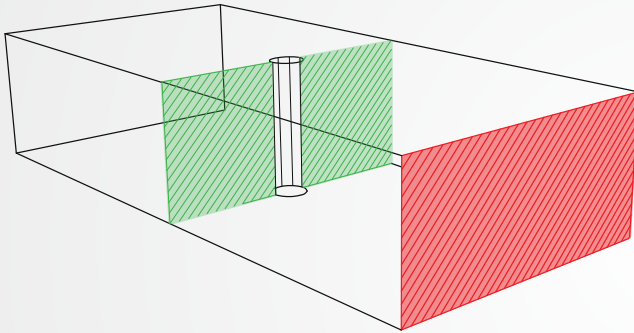
The important balance



EXPLANATION

A key element is to find the correct cross-section. Larger cross-section (height) increases the strength, but decreases the formability.

Dimensioning cross section



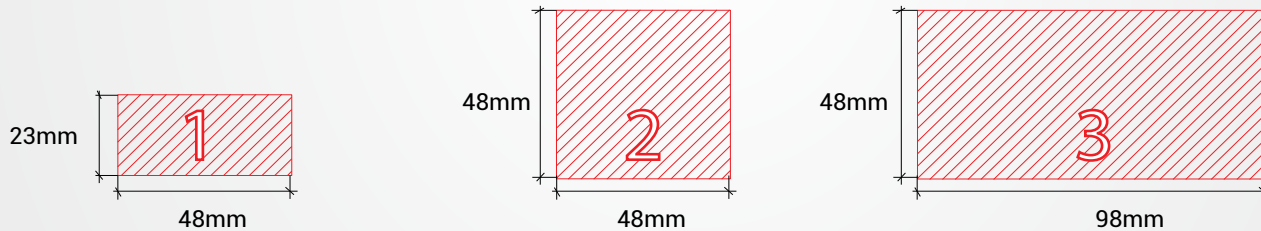
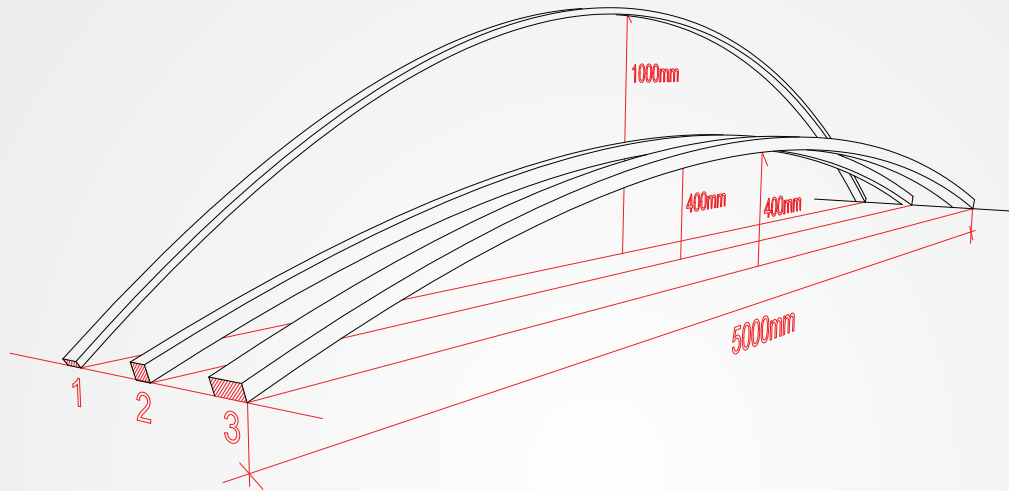
EXPLANATION

It is important to keep in mind that you remove parts of the cross-section when making holes for the bolts.

Other girdshell projects uses clamps that removes this issue..



Cross-section



EXPLANATION

As mentioned, the cross-section affects the formability. The relationship between the cross-section height and the minimum radius are proportional.

As a practical example: double cross-section height, results in a doubled radius.

The relationship are determined by a species/quality dependent constant.

Smallest curvature radius

Different material constants

Strength class	Constant	Cross-section (h)	Smallest radius
C16	250	23	5750
C24	229	23	5267
C30	200	23	4600
D30	167	23	3841
D70	143	23	3289
Segment-lath	152	23	3496

Different cross-sections

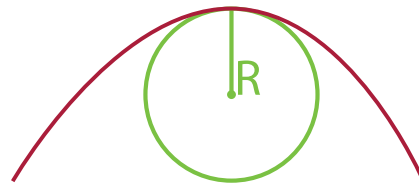
Strength class	Constant	Cross-section (h)	Smallest radius
Segment-lath	152	12	1824
Segment-lath	152	24	3648
Segment-lath	152	48	7296

EXPLANATION

The first table exemplifies that similar cross-sections with different **timber-qualities** results in different **radiuses**.

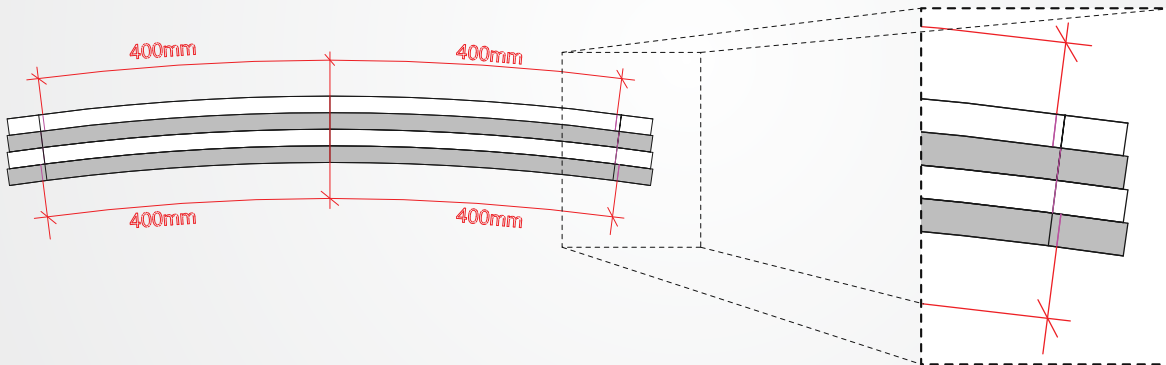
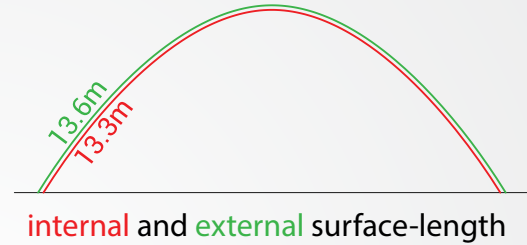
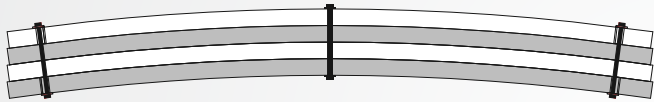
The second table exemplifies that increasingly **cross-section** heights results in larger **radiuses**.

The data (except the segment-lath) are extracted from Thomas Schiøtz Master Thesis, 2013. Data for the segment-lath was measured in a lab-test.



$$\text{minRadius} = \text{Cross-section}(h) * \text{Con-}$$

Increasing radius, increasing length



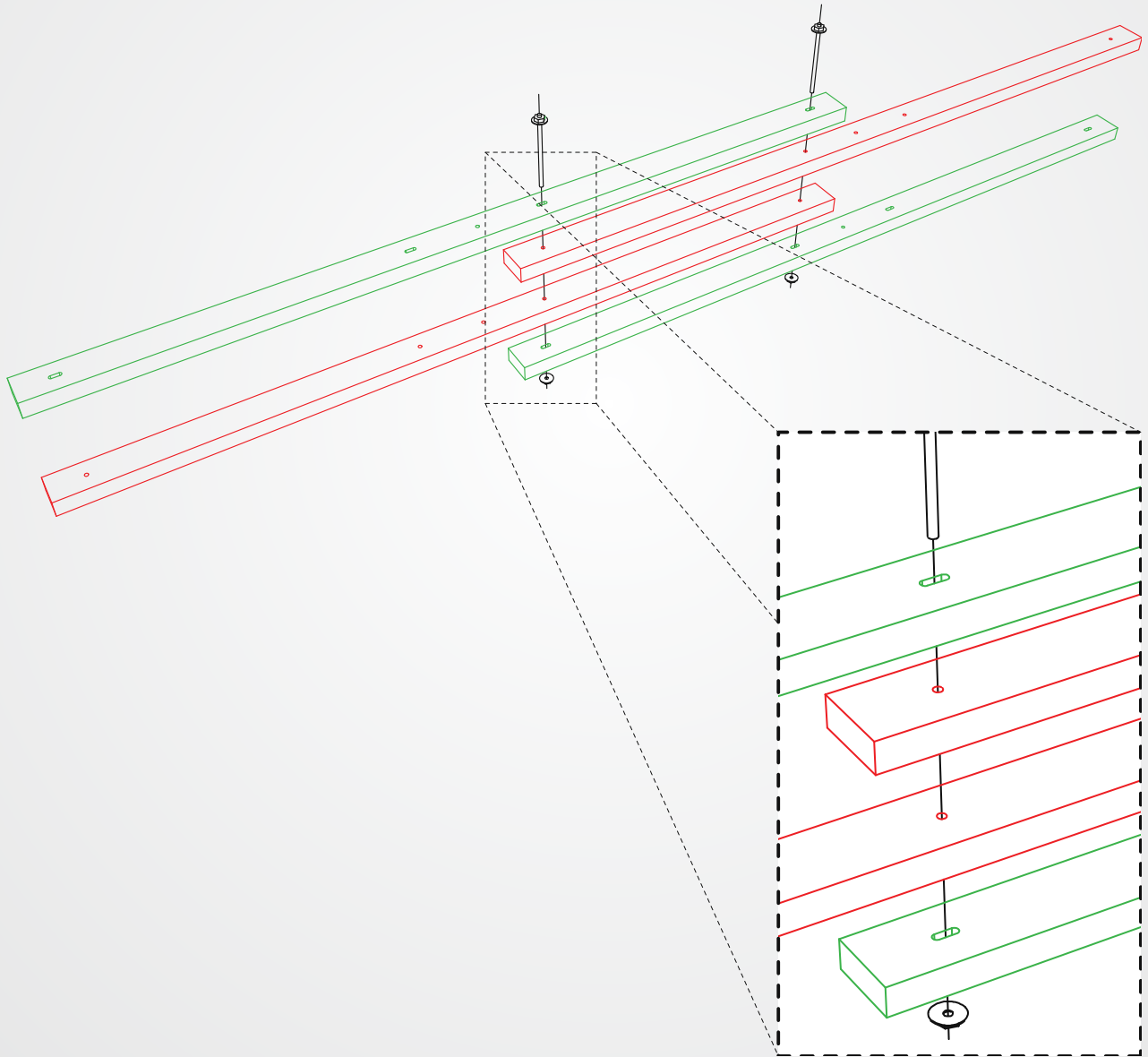
EXPLANATION

Look at the section of the shell (upper right). The thickness is only 23 mm, but the result is that the inside length of the shell is 0.3m shorter than the outside length.

This problem has to be solved in the detail as well. When the grid is flat, the distance between the bolts are the same, but when curved, there is a longer distance on the outside than the inside.

The detail on the next page shows how the problem is solved with the segment-lath. The bottom and top lath has slotted/rectangular hole. This allows the bolt to slide when shaping the shell. When the shape is satisfying, the bolt is tighten.

Increasing radius - detail example



Material characteristics

Density, wood species (kg/m³)

Balsa	200
Aspen	420
Spruce	430
Pine	490
Birch	580
Teak	630
Oak	650
<i>Pokkenholt</i>	1200

Material characteristics in construction timber

	Bending strength (N/mm ²)	E-module (GPa)
C16	16	8000
C24	24	11000
C30	30	12000
D30 (oak)	30	10000
D70	70	20000

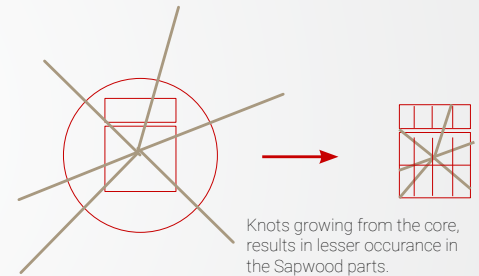
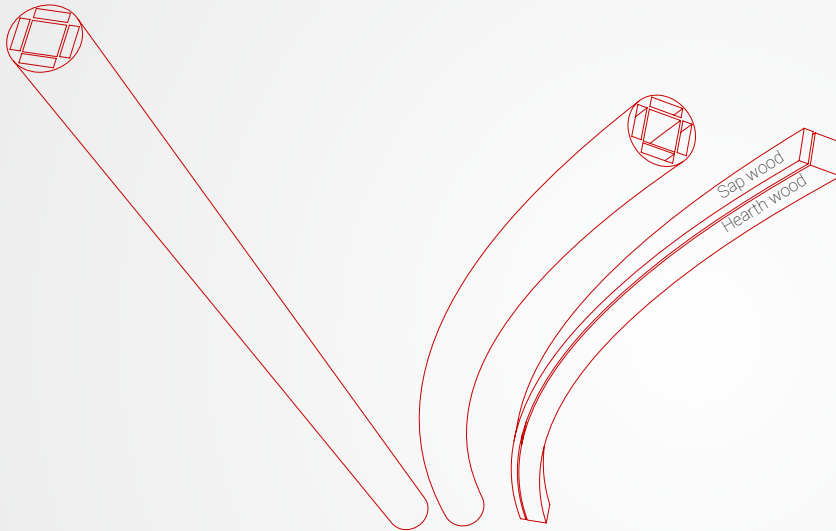
EXPLANATION

The most important characteristics to look for when choosing material is flexibility, formability and bending strength.

Table 1.
Treteknisk Håndbok, Kapittel 2,
http://www.engineeringtoolbox.com/wood-density-d_40.html

Table 2. Materialegenskaper
for konstruksjonstre, fra EN 338

Choosing the best (part of the) tree



EXPLANATION

The conditions the tree has grown in is important. If the forest is dense, it forces the tree to grow upwards instead creating many branches (knots). It is also said that slowly grown trees are stronger than fast grown.

Based on the timber mill's experience, it is best to use the Sapwood (yted):

- + More elastic due to longer fibers
- + Less knots
- Not so moisture resistant

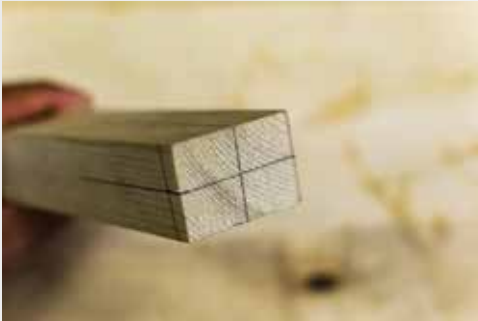


Wood species

Characteristics of some species found in Norway
Table from (Berge, 1992)

Spruce	Soft, elastic, medium strength, easy to glue and paint, hard to impregnate.
Pine	Soft, elastic, strong, durable, easy to cut and process, hard to glue and paint, can be impregnated
Birch	Ductile, elastic, low moisture resistance, easy to process,
Oak	Dense, heavy, hard, durable, elastic, semi-hard to process, moisture resistant
Aspen	Soft and loose, fluffing, moisture resistant (strongest dry), no cracking while drying

Wood species



Spruce



Aspen



Pine



Birch



Oak

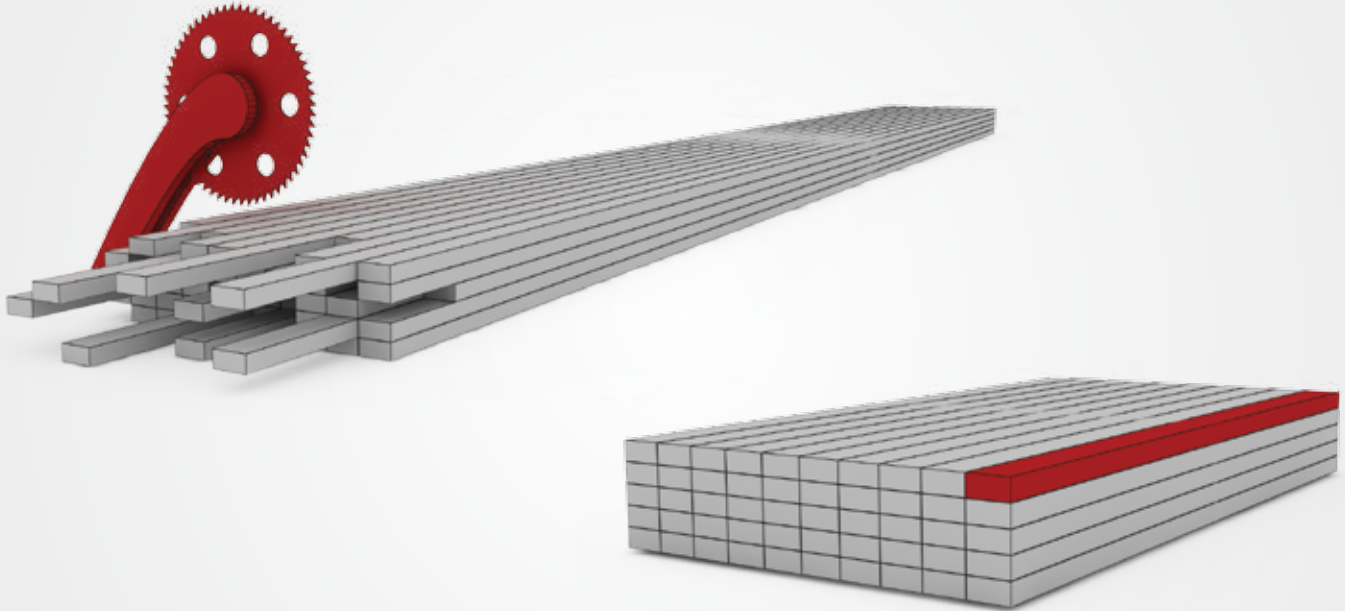


RedOak



HOW TO BUILD

01: Precut

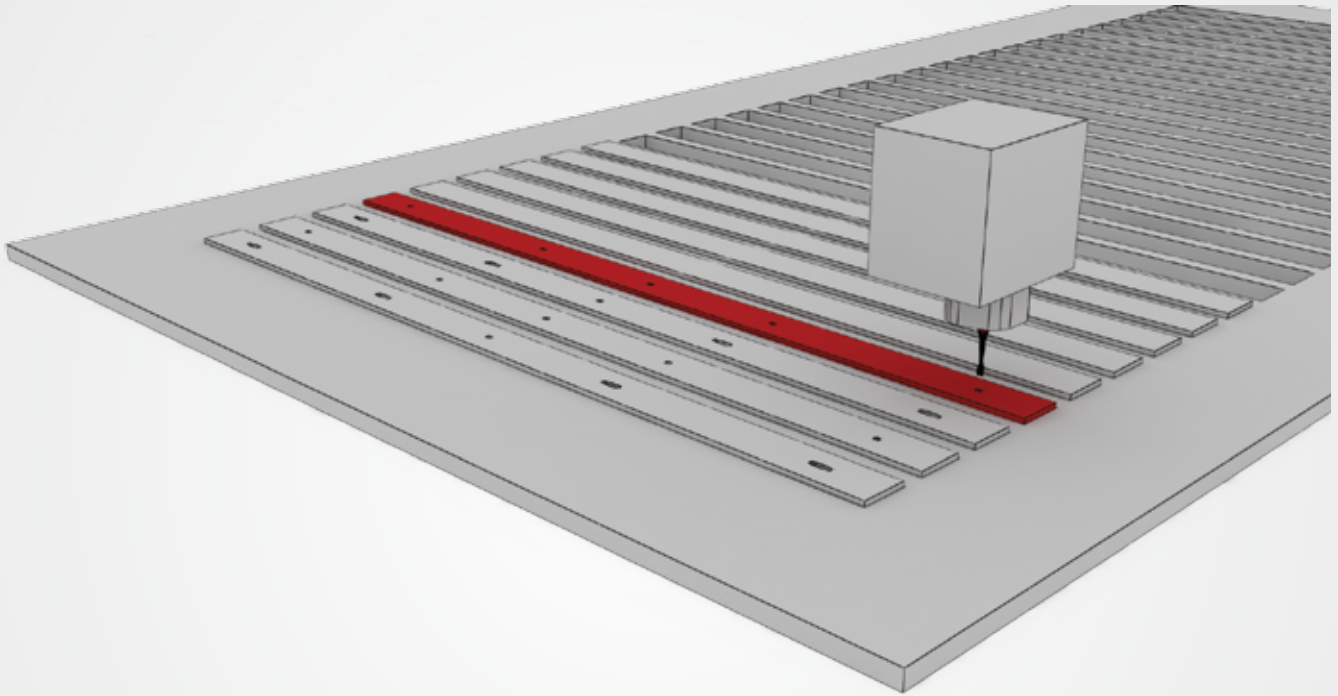


EXPLANATION

The saw-mill can often precut the timber to desired length. This is only recommended with well sorted timber with little knots.

An alternative is to precut piece by piece, removing the knots.

02: Cutting holes

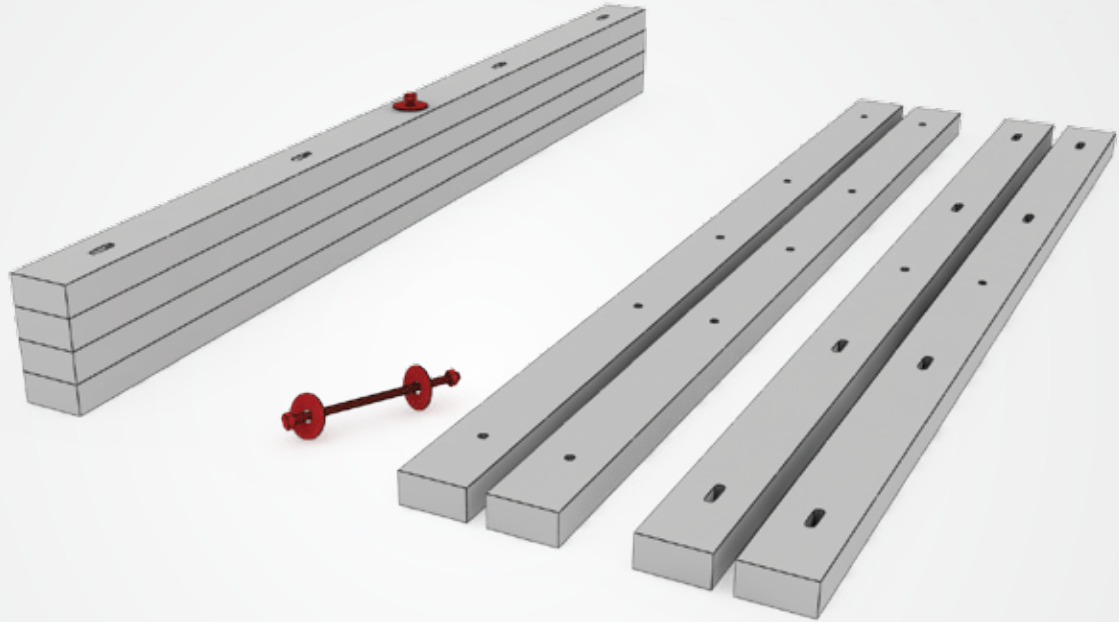


EXPLANATION

A cnc-mill cuts holes and slotted holes in the laths. 38 laths requires 15 minutes, including off/on-loading. This results in 2.5 laths/minute.

A tip is to create a jig that ensures easy unloading/loading, but still keeps the laths in place.

03: Element-assembly

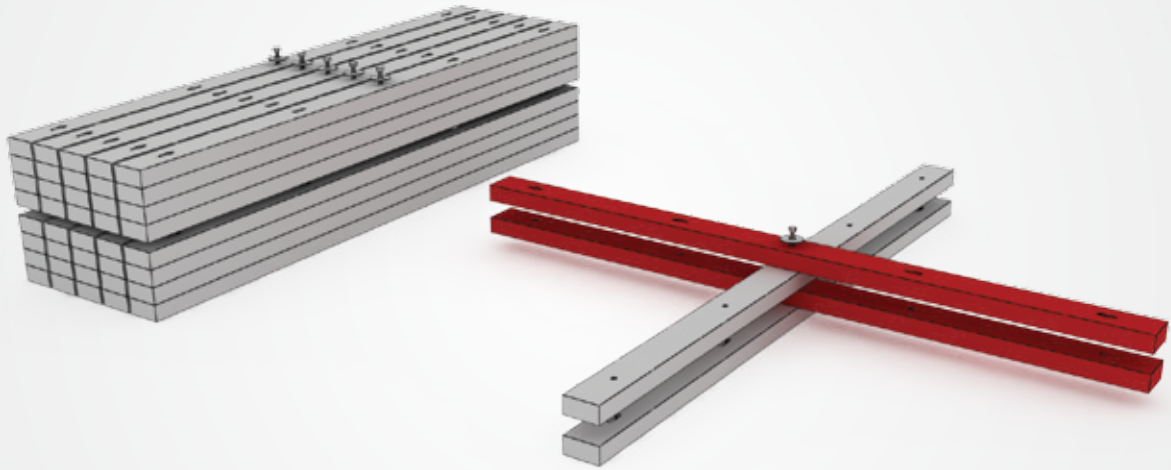


EXPLANATION

Two laths with slotted holes, two laths with straight holes, one bolt, one nut and two washers creates the element prefabricated in the workshop.

The detailing makes the element very transport-friendly.

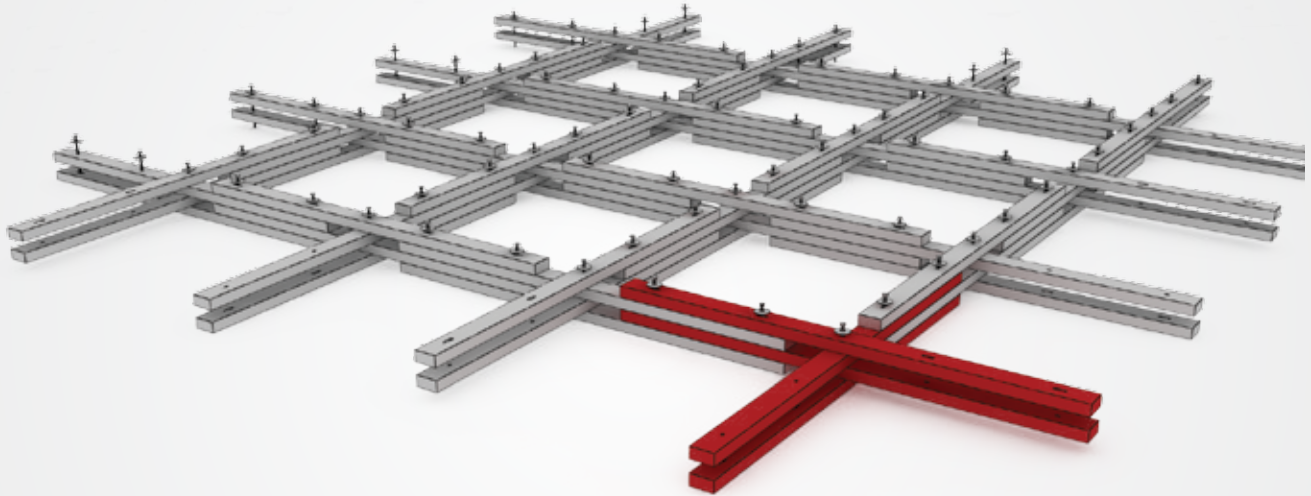
04: The cross



EXPLANATION

The one cross is the base for the hole gridshell and represent the verticies in the grid.

05: Grid-assembling

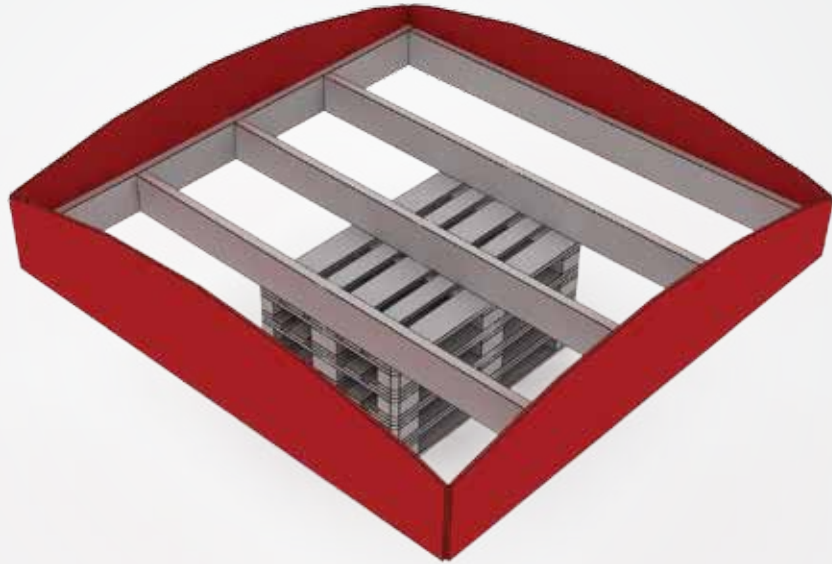


EXPLANATION

Weaving the crosses repeatedly, you can create what ever grid-shape you want.

The prefabricated holes maintains the correct grid-size.

06: Grid-bed

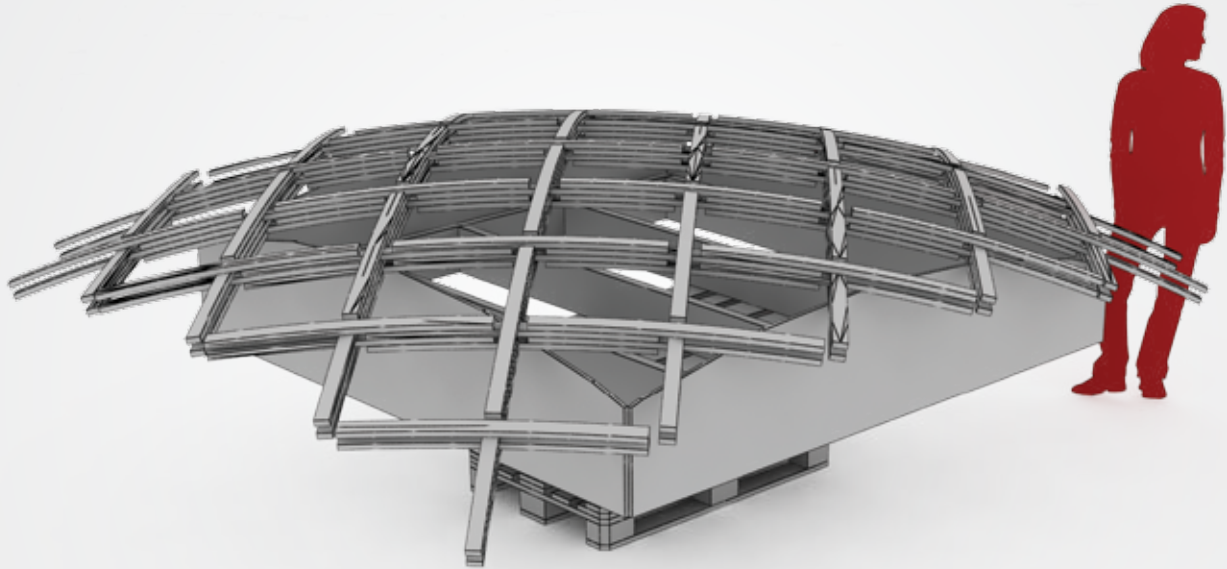


EXPLANATION

When lifting the grid, it is important to distribute the forces as even as possible. A grid-bed, that replicates the shells final shape ensures an even load distribution.

The pallets underneath are progressively added.

07: Laying the grid



EXPLANATION

When laying the grid on the bed, it allows the builder to add crosses keeping a good working position.

08: Raising the structure

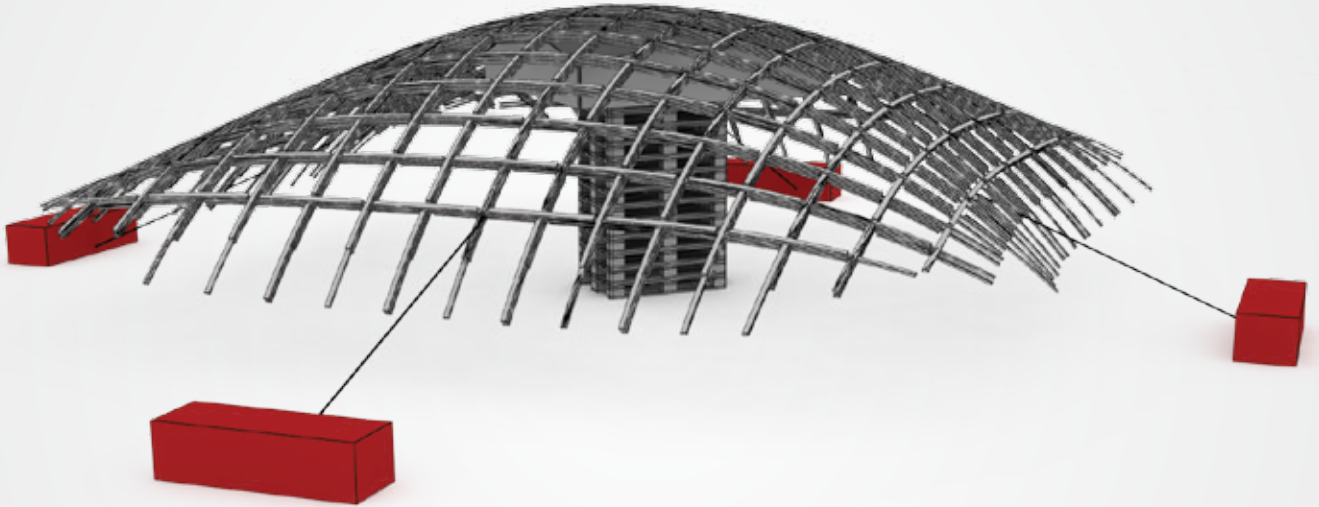


EXPLANATION

Larger structures would of course demand a crane, but low cost-structures can use primitive methods such as a temporary scaffolding or a pallet jack.

Since a standard pallet jack only lifts 120mm and the pallet is 144mm, you need to bypass the load and do the lift in two stages.

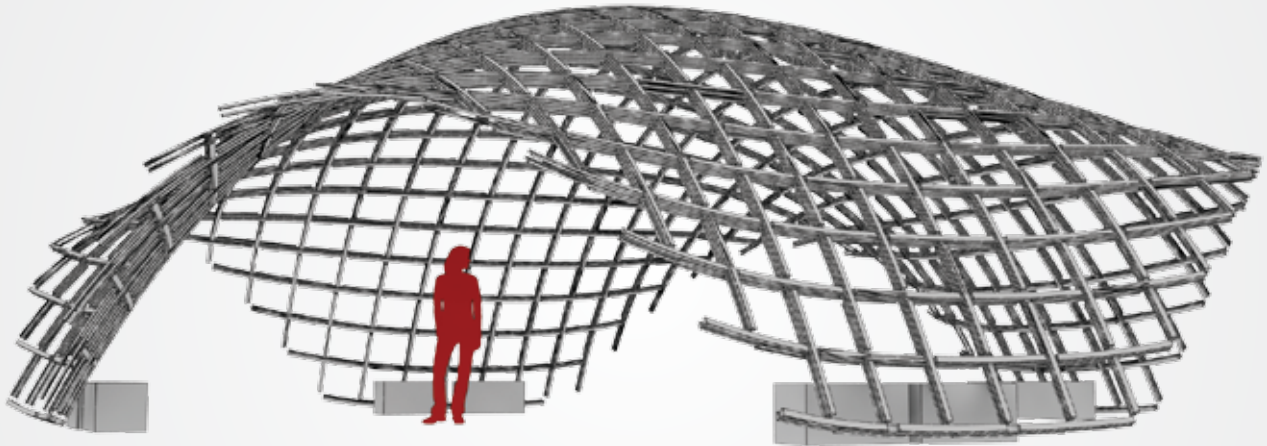
09: Securing the grid



EXPLANATION

The foundations can be used both to shape and to secure the structure. Temporary columns and bracing can also be sensible to add.

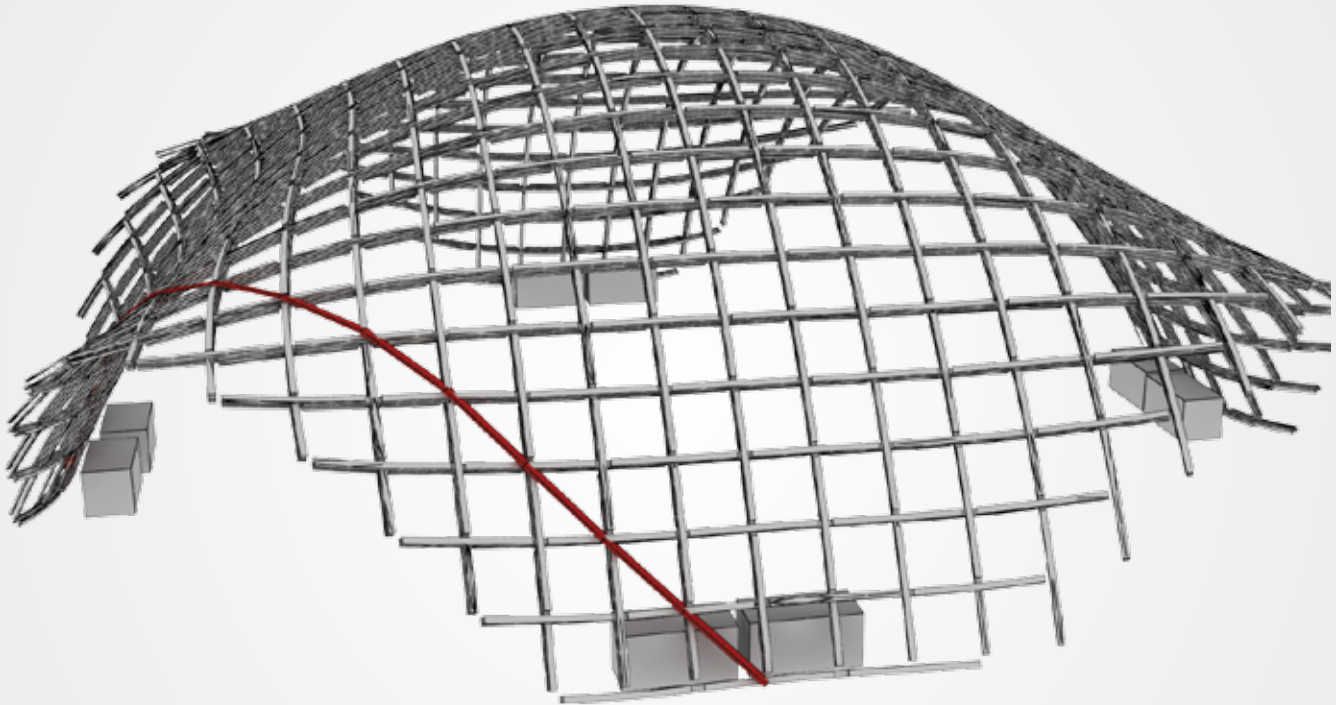
10: Finishing the shape



EXPLANATION

It is important to duplicate the digital shape in the real world. Positioning the foundations accurately can make it easier to find the correct shape.

11: Bracing

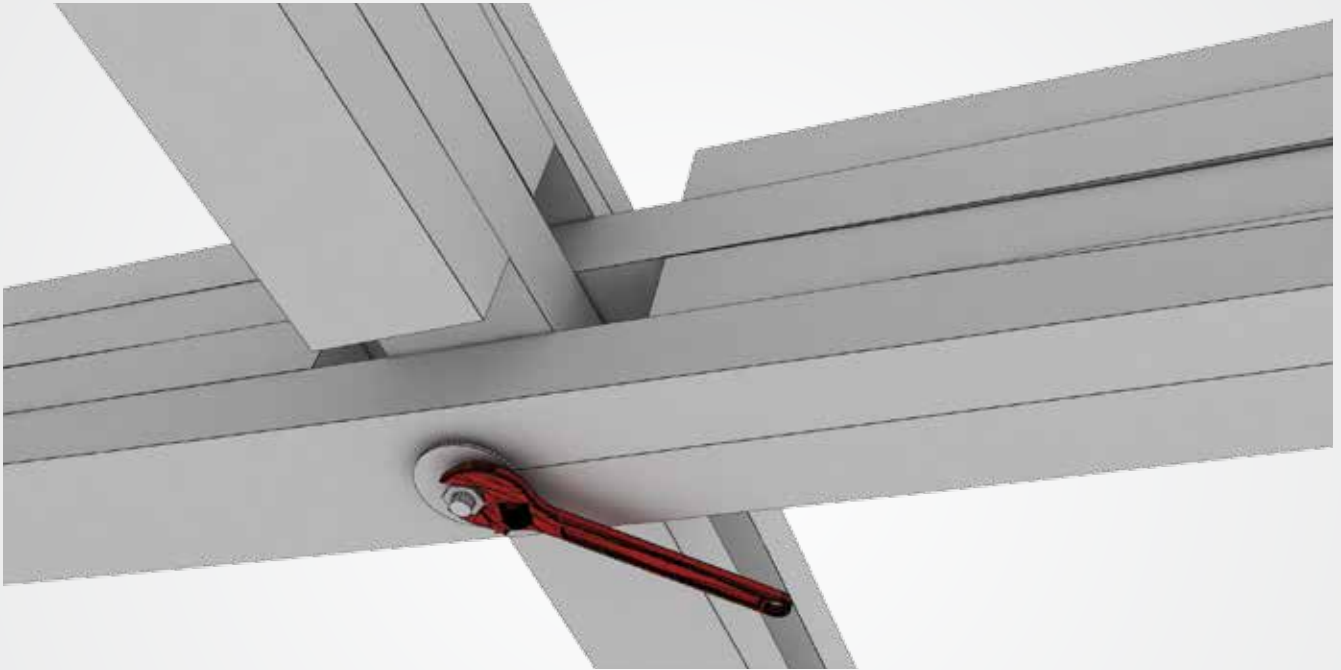


EXPLANATION

Bracing is important to lock the shape. This decreases the outwards force in the foundation and makes it more resistant to un-even loads.

This also assures that tarp will not be disrupted by the bolts.

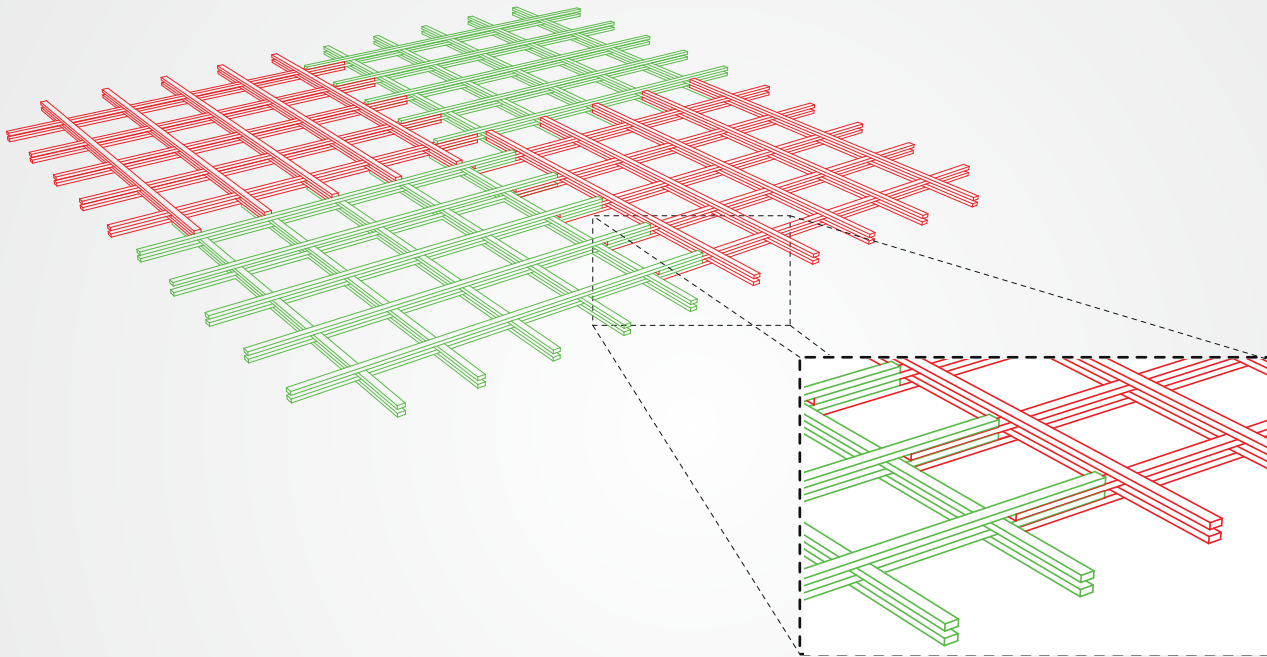
12: Tighten the bolts



EXPLANATION

The last step is to tighten the bolts.
This joins the laths and makes the structure stronger.

Others: Extending the laths



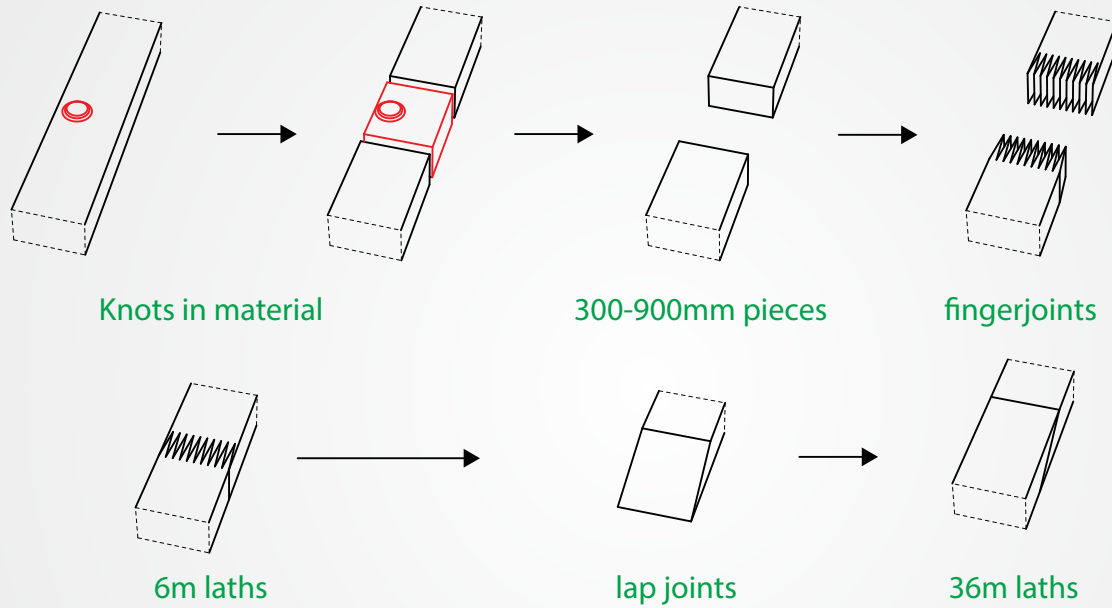
EXPLANATION

The Gridshell.it team uses a detail where they extend the laths for each fifth grid-length.

Our solution, shown earlier, has been developed from this solution, but instead of having the extending as an exception, our detail uses it as a design-rule. This makes the pattern easier, more dynamic and more homogenous.



Others: Extending the laths



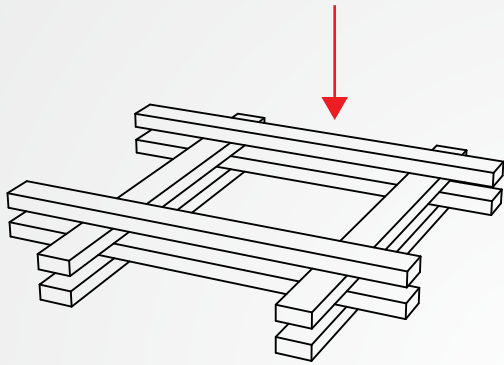
EXPLANATION

This example is from the building of the Savill garden gridshell. In order to produce knot-free, continuous laths up to 36 meters, every piece was cleaned free from knots by cutting them into 300mm to 900mm lengths.

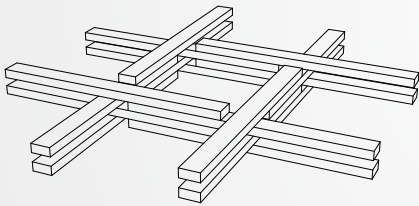
They were thereafter fingerjoint to 6m laths at the workshop and then lap joint to its final length at the building site.



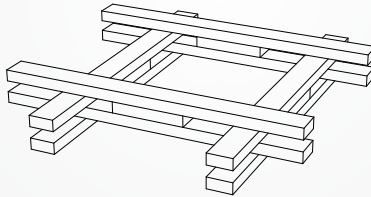
Shear blocks



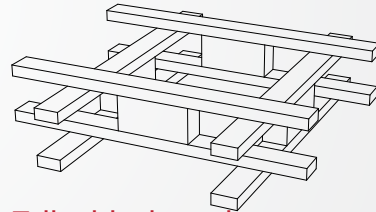
Plain grid has little shear stiffness



Shear blocks through weaving



Same height blocks

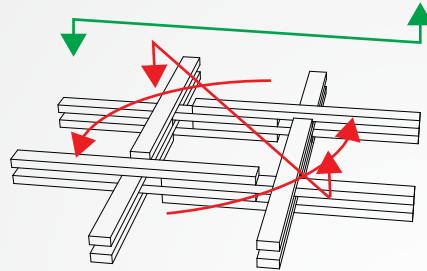


Taller blocks makes an I-profile-like strength

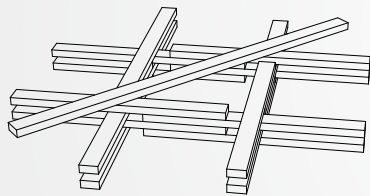
EXPLANATION

To reduce the “span” of each lath, shear blocks are added. They provide shear stiffness to the grid, and could also help making a distance between the top and bottom layer, to create a taller cross-section.

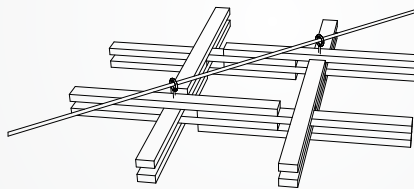
Diagonal bracing



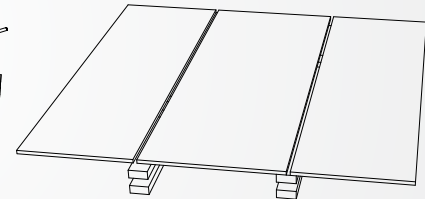
Little in plane stiffness
without triangulation



Diagonal laths



Diagonal wires



(plywood) plates

EXPLANATION

The plain grid has initially no stiffness in its plane. In order to lock the quadrants, it needs to be triangulated. Triangulating the whole grid is not necessarily needed, and it can be done in different ways.



BUDGET

FINANCIAL (A DRAFT!)

The materials listet are from the built example, 132 m². It is important to keep in mind that foundations, tools and unknown costs will be added to a permanent project. Production/Assembling can decrease if more industrialized.

The master-thesis` built project were due to kind sponsors almost free.

Material	Quantity	Unit price	Price
Timber	2034 m	6.25 NOK	12 712 NOK
Bolts/Nuts	2825 stk	3.00 NOK	8475 NOK
Tarpolin	131.5 m ²	200 NOK	26 300 NOK
Production	40 t	750 NOK	30 000 NOK
Assembling	60 t	500 NOK	30 000 NOK
		TOTAL:	≈108 000 NOK
		Price pr m ²	≈820 NOK

OTHER WAYS TO MAKE SPACE

Oppblåsbart salgsteil LDF 7005 90 m²



www.shop.no

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Prisliste

Permanente haller

Storrelse 8 m	Storrelse 10 m	Storrelse 12 m	Storrelse 14 m
10000,-	11 500,-	14 000,-	16 500,-
12 000,-	14 000,-	17 000,-	19 500,-

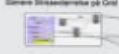
Area: 90 m²
 Price: 75000 NOK
 Price pr m²: 830 NOK

Area: 120 m²
 Price: 107250 NOK
 Price pr m²: 890 NOK

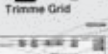
Prices collected at www.finn.no and www.futurehaller.no in march 2015.

Grid og krefter

1



2



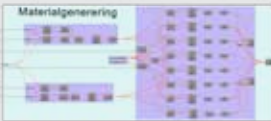
3



Simulering



Færdigberegning

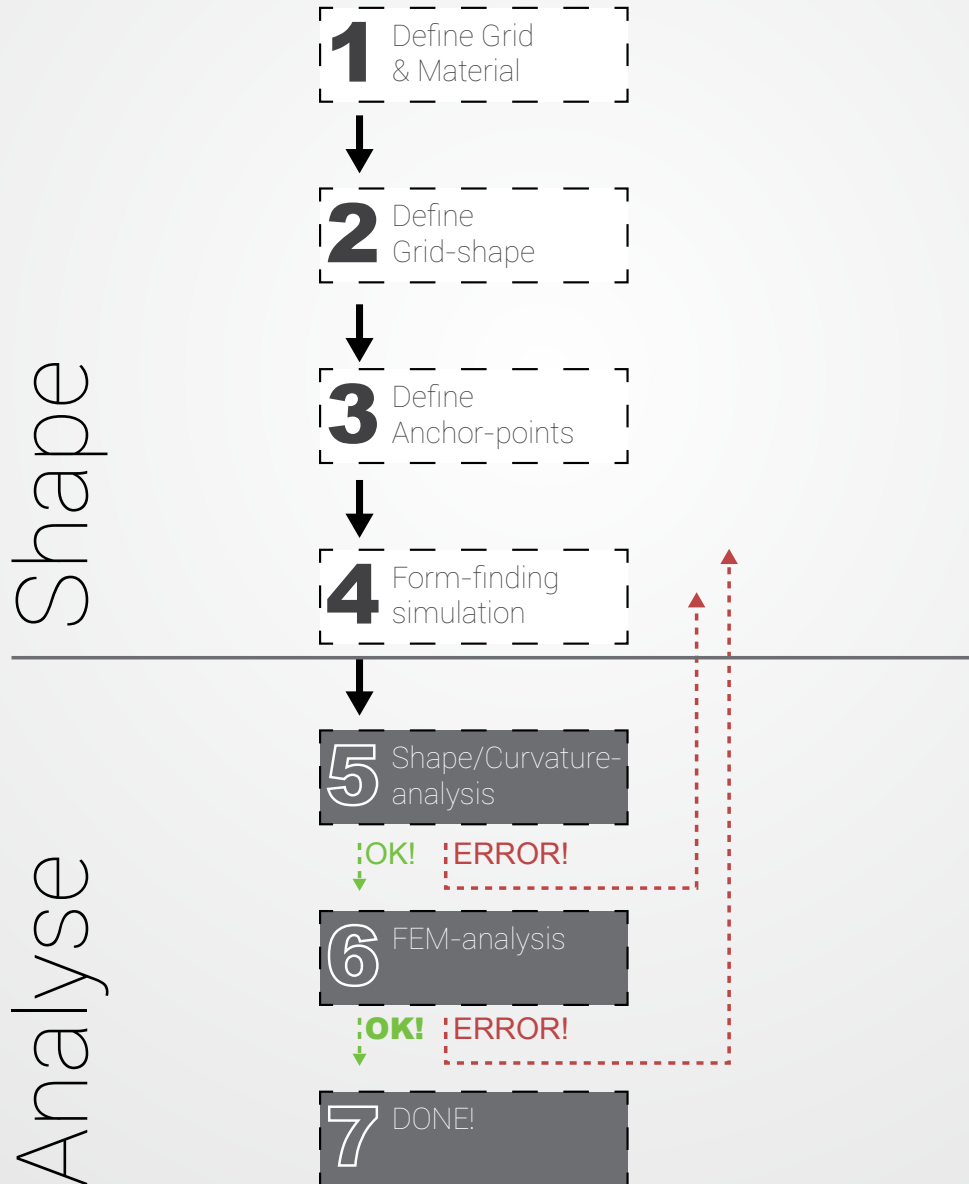


EXTRA INPUT



SOFTWARE

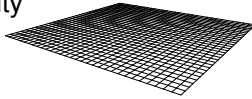
CROSS SECTION



1 Define Grid & Material

Choose a diagonal or orthogonal grid. Also choose the grid-size.

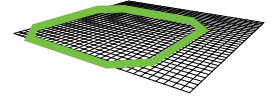
Cross -section and material-quality are also to be choosed, but can easily be changed later.



2 Define grid-shape

Draw a closed curve that defines the grid-shape.

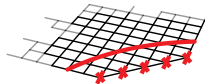
Keep it simple! It is wise to choose either 45° or 90° corners



3 Define foundations

The principle is to choose wich points are to be foundations. These are then connected to a curve that the points should be attached to. This is the foundation.

The software has four foundations, but can easily be expanded



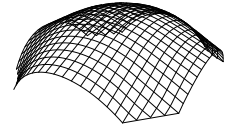
4 Form-finding

The shape is generated based on foundations and forces.

Gravity: The gravity is set up-side down.

Bending-force: Like a beam, the lines tries to resist bending.

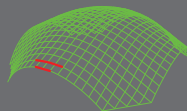
Spring: Each segment is defined as a strong spring.



5 Shape/curvature analysis

Analysis is next when shape is generated. First aestetically and functional. Graphical displays shows if some of the parts will break or some area is to0 flat.

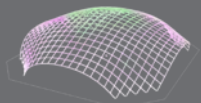
If the shape is not approved, point 1,2 or 3 has to be adjusted.



6 FEM-analysis

A software called Karamba makes it possible to do FEM-analasis. This enables the user to add snow- and other loads on the structure. Results as displacement and forces in the anchor-point can determine if the shape is buildable.

If the shape is not approved, point 1,2 or 3 has to be adjusted.



Software-list

The form-finding and analysis can be done in several different ways and with different softwares. Following are the softwares and purposes used in this thesis.

Rhinoceros 3D

Rhinoceros is the 3D-software that functions as a base for the geometry. This software is also used when manufacturing the elements.



Grasshopper

Grasshopper is a plugin for Rhino. This is a graphical programming language aimed for parametric modelling. Geometry is generated based on a large algorithm.



Kangaroo

Kangaroo is a plug-in for Grasshopper that enables grasshopper to add physics on the 3D. Kangaroo is responsible for the form-finding process.



Karamba

Karamba is a plug-in for Grasshopper that does analysis on a given structure. The plug-in adds material-properties and exports results like displacement and reaction-forces.







Toledo 2.0, Italy



PROPERTIES

Material: Larch
Material-dim: 20x50mm
Total span: 10x10m
Grid-size: 500x500mm
Joint M6 Bolt+washer
Brazing Timber

Function: Eksperiment
Architect: Gridshell.it
Year: 2014
Weigth: 7kg/m²
Mat. Volume: 2m³

Downland gridshell, England



PROPERTIES

Material:	Oak	Function:	Museum
Material-dim:	50x35mm	Architect:	Edward Cullian;
Total span:	50x12,5/16m	Year:	2002
Grid-size:	500x500,1000x1000mm	Price:	1097Pund/m ²
Joint	4stk M8 Bolt+ brackets		
Brazing	Timber		

Mannheim Multihalle, Germany



P: Oliver Lowenstein

PROPERTIES

Material:	Hemlokk Pine	Function:	Swimming pool, restaurant
Material-dim:	50x50mm	Architect:	FreiOtto, OveArup++
Area:	9500m ²	Year:	1972
Grid-size:	500x500mm		
Joint	M8 Bolt, washer		
Brazing	Steel-wire		

Savill Garden, England



P: David Baugh

PROPERTIES

Material: Larch(Quality1&2)
Material-dim: 80x50mm
Total span: 2250m²
Grid-size: 1200x1200mm
Brazing Plywood

Function: Visitor centre
Architect: GlennHowells,
BuroHappold
Year: 2005
Timber length: 20000m

Shell you later.