

# Dynamic Stress due to End Effects in Non-bonded Flexible Pipes



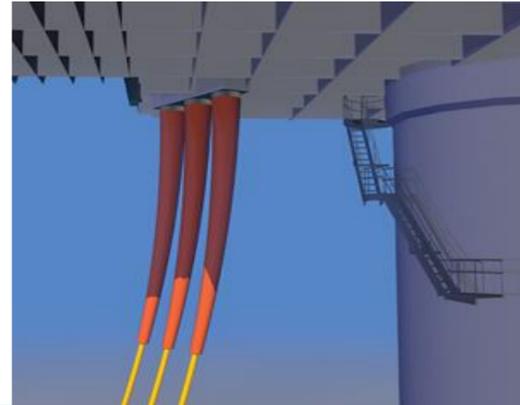
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## Introduction

The flexible riser represent a vital part of many oil and gas production systems. Failure in the riser section may cause loss of lives, environmental pollution and threaten the field economy. One of the most critical failure modes is corrosion fatigue in the tensile armour steel layers due to the combined action of dynamic loads and corrosion from the annulus and seawater environments.



A flexible pipe is terminated with an end fitting where all layers are anchored and clamped in a special end structure. To limit the bending stresses and excessive curvature a bend stiffener is added to improve the stiffness of the flexible pipe which connecting the end fitting. There are two kinds of flexible pipes which named as bonded and non-bonded pipe. For non-bonded pipes, the cylindrical layer is able to slide relative to adjacent layers.



## objective and scope

- Establish necessary input for flexible riser local stress and fatigue analysis for two cross-sections.
- Establish local Bflex models for the flexible pipe cross-section using ITCODE 0 and ITCODE31 for two cross-sections and for start BS at 0, 0.25 , 0.5 and 0.75 pitch from end fitting.
- Perform fatigue stress analysis in Bflex using the above models and compare the results in terms of stress history plots and fatigue contribution from each load case at different longitudinal load for a typical SN curve.

## Methods and Assumptions

- Non-linear finite element method
- Local stress analysis
- Plane surfaces remain plane until slip
- Geodesic and Loxodromic assumptions

## Modeling

Two types of models with different cross sections are used for analysis in this thesis: ITCODE 0 and ITCODE 31. Original model refers to the model with 0 pitch gap between the end fitting and bend stiffener; modified model refers to the model with 0.25, 0.5, 0.75pitch length gap.

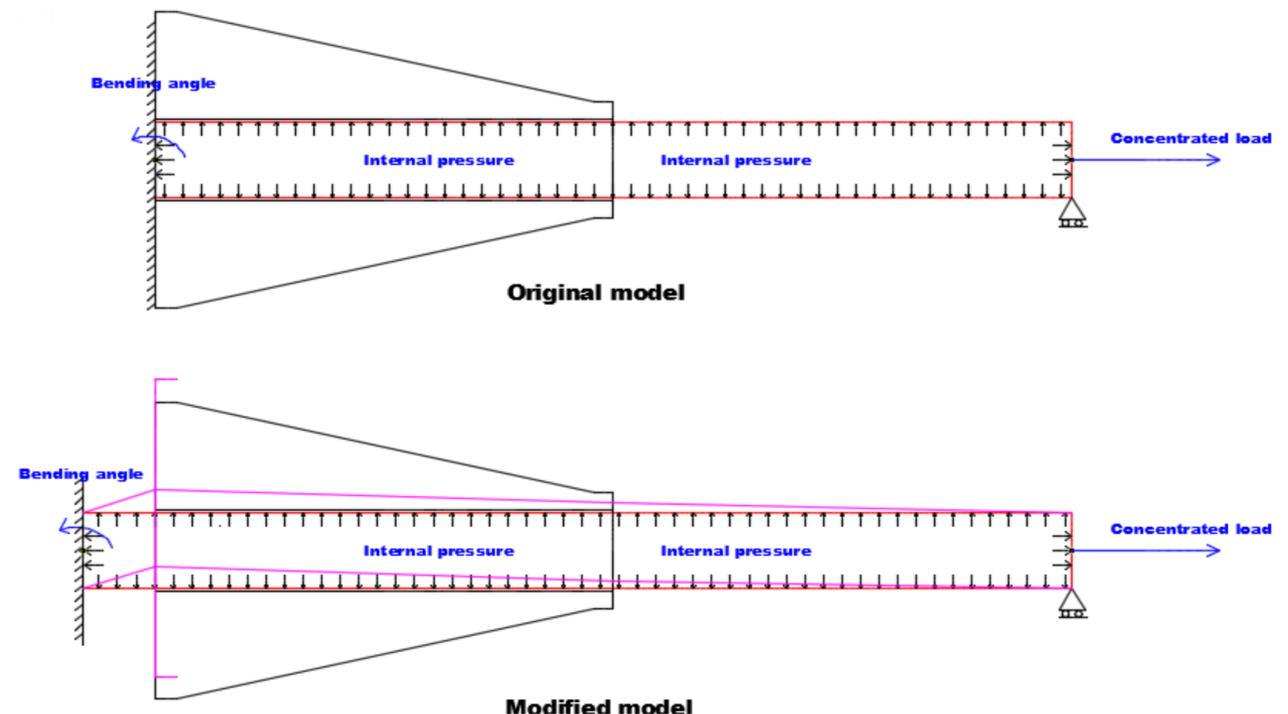
### Model (Inner Tension Layer and Bending Stiffener)

The gap lengths for the modified models are calculated according to the pitch length of the inner layer (tenslayer1). All the important parameters are shown in table below:

|                     | Original<br>(0 pitch gap) |          | 0.25 pitch gap |          | 0.5 pitch gap |          | 0.75 pitch gap |          |
|---------------------|---------------------------|----------|----------------|----------|---------------|----------|----------------|----------|
| $L_0 [mm]$          | 10000                     |          | 10252.95       |          | 10505.89      |          | 10758.84       |          |
| Tenslayer           | 1                         | 2        | 1              | 2        | 1             | 2        | 1              | 2        |
| $R [mm]$            | 135.1                     | 141.2    | 135.1          | 141.2    | 135.1         | 141.2    | 135.1          | 141.2    |
| $\alpha [rad]$      | -0.69806                  | 0.69808  | -0.69806       | 0.69808  | -0.69806      | 0.69808  | -0.69806       | 0.69808  |
| $L_p [mm]$          | -1011.79                  | 1057.419 | -1011.79       | 1057.419 | -1011.79      | 1057.419 | -1011.79       | 1057.419 |
| $\theta_1 [^\circ]$ | -62.1                     | 59.42    | -63.671        | 60.923   | -65.242       | 62.426   | -66.812        | 63.929   |
| $\theta_0 [^\circ]$ | 0                         | 0        | -1.5708        | 1.503    | -3.1416       | 3.006    | -4.7124        | 4.509    |

### Model simplification

The model with the boundary condition and the load history can be simplified as the figure below:

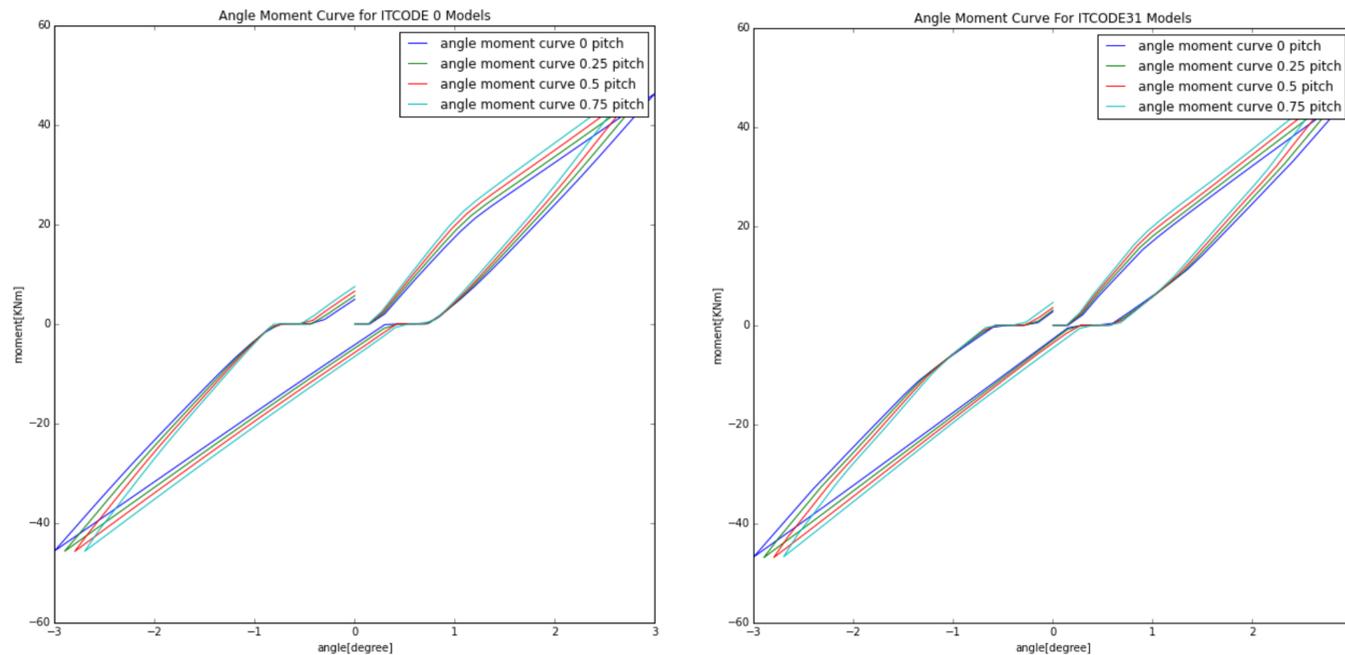


## Results and Discussion

### Comparison and summary of moment and angle curve of both model itcode0 and itcode31

Keep node 501 (the end node of the bending stiffener) has the same largest moment during the load history. The results of the relative bending angle are show in the table and figure below:

| Gap length | 0 pitch length |              | 0.25 pitch length |              | 0.5 pitch length |              | 0.75 pitch length |              |
|------------|----------------|--------------|-------------------|--------------|------------------|--------------|-------------------|--------------|
| Units      | Angle [degree] | Moment [KNm] | Angle [degree]    | Moment [KNm] | Angle [degree]   | Moment [KNm] | Angle [degree]    | Moment [KNm] |
| ITCODE0    | 3              | 46.293       | 2.9               | 46.412       | 2.8              | 46.563       | 2.7               | 46.686       |
| ITCODE31   | 3              | 46.720       | 2.9               | 46.885       | 2.8              | 46.874       | 2.7               | 46.692       |



## Summary and Further work

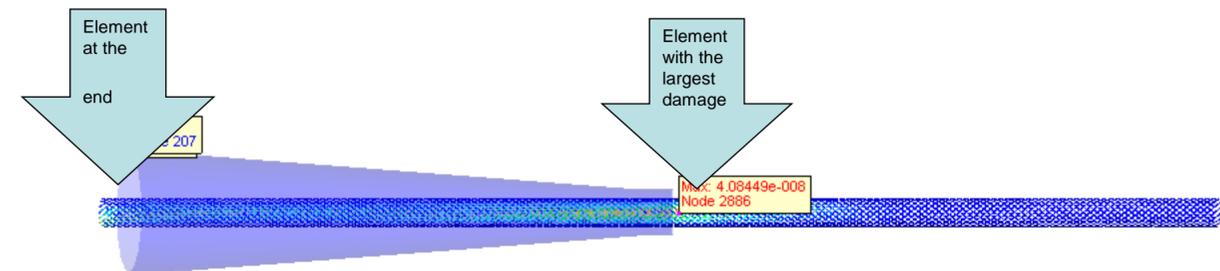
In this case analysis, the largest damage happens at the end of the bend stiffener (outside), this situation should not happen in a real case. So in the next step, larger longitudinal force (from 0.1MN to 0.5 MN) should be added, then get the largest damage and analysis the stress again,

## Results and Discussion

### Stress analysis and Fatigue

Look into the stress range ( $\Delta\sigma_{ax}$ ,  $\Delta\sigma_{my}$ ,  $\Delta\sigma_{mz}$ ,  $\Delta\sigma_{xx}$ ) at the end of the pipe and at the other side of the bending stiffener. Compare the stress range of the element where has the largest fatigue damage.

#### ITCODE 0



| Gap (pitch length) | Element number | Section | Point | $\Delta\sigma_{xx}$ | $\Delta\sigma_{ax}$ | $\Delta\sigma_{my}$ | $\Delta\sigma_{mz}$ | Maximum damage         |
|--------------------|----------------|---------|-------|---------------------|---------------------|---------------------|---------------------|------------------------|
| 0                  | 1002           | 1       | 2     | 187.328             | 168.353             | 1.922659            | 17.05214            | 4.45883e <sup>-8</sup> |
| 0.25               | 2709           | 1       | 2     | 165.216             | 163.464             | 7.01827             | 1.841331            | 4.08449e <sup>-8</sup> |
| 0.5                | 2776           | 1       | 3     | 164.797             | 163.498             | 7.42554             | 5.72821             | 4.08692e <sup>-8</sup> |
| 0.75               | 2861           | 1       | 3     | 162.784             | 162.455             | 6.76143             | 1.771977            | 4.06779e <sup>-8</sup> |
| 0                  | 2608           | 1       | 3     | 176.169             | 168.353             | 1.922659            | 17.05214            | 4.08419e <sup>-8</sup> |
| 0.25               | 1002           | 1       | 2     | 165.5               | 162.176             | 1.747868            | 15.06827            | 3.98942e <sup>-8</sup> |
| 0.5                | 1002           | 1       | 2     | 150.936             | 149.533             | 1.537703            | 12.65842            | 3.13334e <sup>-8</sup> |
| 0.75               | 1002           | 1       | 2     | 136.003             | 135.191             | 1.386066            | 10.93032            | 2.32109e <sup>-8</sup> |

In this case, only the model with 0 pitch length gap got the largest damage at the left end of the pipe, the other models got the largest damage at the right end of the bending stiffener. The largest damage gradually decreased as the gap length increased.

#### ITCODE 31

| Gap (pitch length) | Element number | Section | Point | $\Delta\sigma_{ax}$ | $\Delta\sigma_{my}$ | $\Delta\sigma_{mz}$ | $\Delta\sigma_{xx}$ | Maximum damage         |
|--------------------|----------------|---------|-------|---------------------|---------------------|---------------------|---------------------|------------------------|
| 0                  | 1100           | 1       | 5     | 160.872             | 9.44839             | 0.370619            | 161                 | 3.89466e <sup>-8</sup> |
| 0.25               | 1105           | 1       | 5     | 160.872             | 9.29412             | 0.383044            | 161                 | 3.89467e <sup>-8</sup> |
| 0.5                | 1110           | 1       | 5     | 160.872             | 9.12623             | 0.394321            | 161                 | 3.89466e <sup>-8</sup> |
| 0.75               | 1115           | 1       | 5     | 160.871             | 8.94326             | 0.404249            | 161                 | 3.89464e <sup>-8</sup> |
| 0                  | 1001           | 1       | 5     | 139.343             | 3.05347             | 0.000356604         | 122                 | 1.70297e <sup>-8</sup> |
| 0.25               | 1001           | 1       | 5     | 136.64              | 2.52834             | 0.000317916         | 124                 | 1.78163e <sup>-8</sup> |
| 0.5                | 1001           | 1       | 5     | 134.419             | 2.09696             | 0.000259467         | 112                 | 1.31e <sup>-8</sup>    |
| 0.75               | 1001           | 1       | 5     | 132.867             | 1.794869            | 0.000213165         | 115                 | 1.45e <sup>-8</sup>    |

In this case, all the models got the largest damage at the node which is at the end of the bending stiffener. The largest damage do not have big change as the gap length increase; while, the damage at the left end point has slightly decrease as the gap length increase.