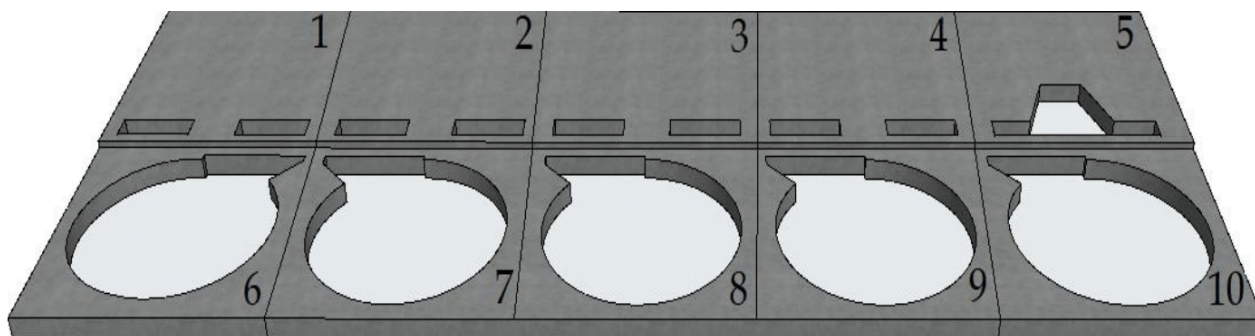


Vedlegg

Vedleggsliste

Vedlegg A : Artikkel.....	2
Vedlegg B: Plakat	5
Vedlegg C:Tegninger og skisser.....	7
Vedlegg C.1 : Armeringstegning	8
Vedlegg C.2: Plate inndeling (sett fra siden).....	10
Vedlegg C.3: Plate inndeling (sett ovenfra)	12
Vedlegg C.4: plassering av snitt	14
Vedlegg C.5: Plantegning dekke	16
Vedlegg D:Beregninger	18
Vedlegg D.1: Snitt 1	19
Vedlegg D.2: Snitt 2	31
Vedlegg D.3: Snitt 3	43
Vedlegg D.4: Snitt 4	55
Vedlegg D.5: Snitt 5	67
Vedlegg D.6: Snitt 6	79
Vedlegg D.7: Snitt 7	91
Vedlegg D.8: Snitt 8	103
Vedlegg D.9: Snitt 9 (snitt 2 med redusert armeringstverrsnitt)	115
Vedlegg D.10: Toveisplate (plate 1-4)	124

Vedlegg A : Artikkel



Skisse av betongdekket som blir dimensjonert i oppgaven (Privat, 2023)

Integritetskontroll av betongdekke

Av Håkon Bendik Pedersen og Vegard Mortensen Eide

To studenter fra NTNU har skrevet bacheloroppgave hvor det er gjort nye beregninger av det snart 70 år gamle betongdekket til Yara i Glomfjord, og sammenlignet mot dagens krav i Eurocode 2.

Syrebelastet miljø

Området betongdekket befinner seg i er påvirket av et aggressivt syremiljø. Fabrikken produserer blant annet salpetersyre opp til 60% konsentrasjon, noe betongdekket bærer synlig preg av.

Utforming og

beregningsgrunnlag

Det armerte betongdekket er satt opp i et statisk system hvor platene er fast innspenne. Dette tillater studentene å beregne dekket både som enveisplate og som toveisplate

Kapasitet

Beregningen beviser at dimensjoneringen tilfredsstiller de fleste kravene i Eurocode 2, og at alle snittene har tilstrekkelig kapasitet.

Befaring

Studentene var på befaring av fabrikken i februar. Dette ga et godt bilde og grunnlag for oppstarten av oppgaven, sier studentene. På befaringen ble det blant annet oppdaget større mengder med synlig eksponert og korrodert armering på undersiden av dekket



Undersiden av dekket bærer preg av eksponert og korrodert armering (Privat, 2023)

Redusert Armeringstverrsnitt

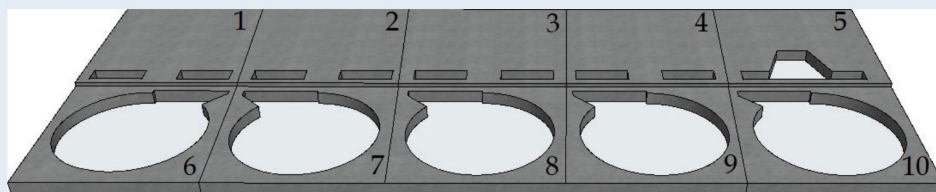
Observasjonene på befaring gjorde at studentene har beregnet et av snittene med lavere armeringstverrsnitt enn det som opprinnelig er. Resultatet viser at også her tilfredsstiller det snart 70 år gamle dekket dagens krav i Eurocoden.

Studentene konkluderer med at betongdekket tilfredsstiller kravene, bortsett fra rissviddekontrollen. Her er dekkets verdier for lave, noe som skyldes den lave overdekningen på 10 mm.

Videre konkluderes det med at dekkets skader skyldes syreangrep fra lekkasjer og damp fra utstyret i fabrikken.

Vedlegg B: Plakat

Prosjektnr 2023-33



Håkon Bendik Pedersen, Vegard Mortensen Eide

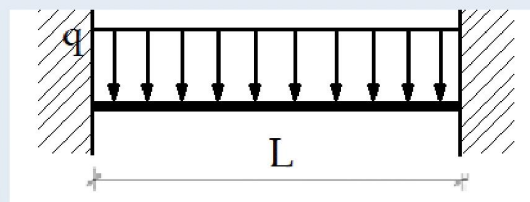
Intern veileder: Arne Mathias Selberg
Ekstern kontakt: Helge Hamnevoll (Yara)

Integritetskontroll av betongdekke

Integrity control of floor divider in concrete

Prosjektbeskrivelse

Formålet med oppgaven er å teste og gjøre nye beregninger på et betongdekke som er fra 1954. For å kunne konkludere om kapasiteten er tilstrekkelig eller ikke.



Illustrasjon av statisk modell



Fotografi av målt overdekning

Analyseområder

- Overdekning
- Kloridinnhold
- Karbonatiseringsdybde
- Nedbøyning
- Riss
- Syreskader



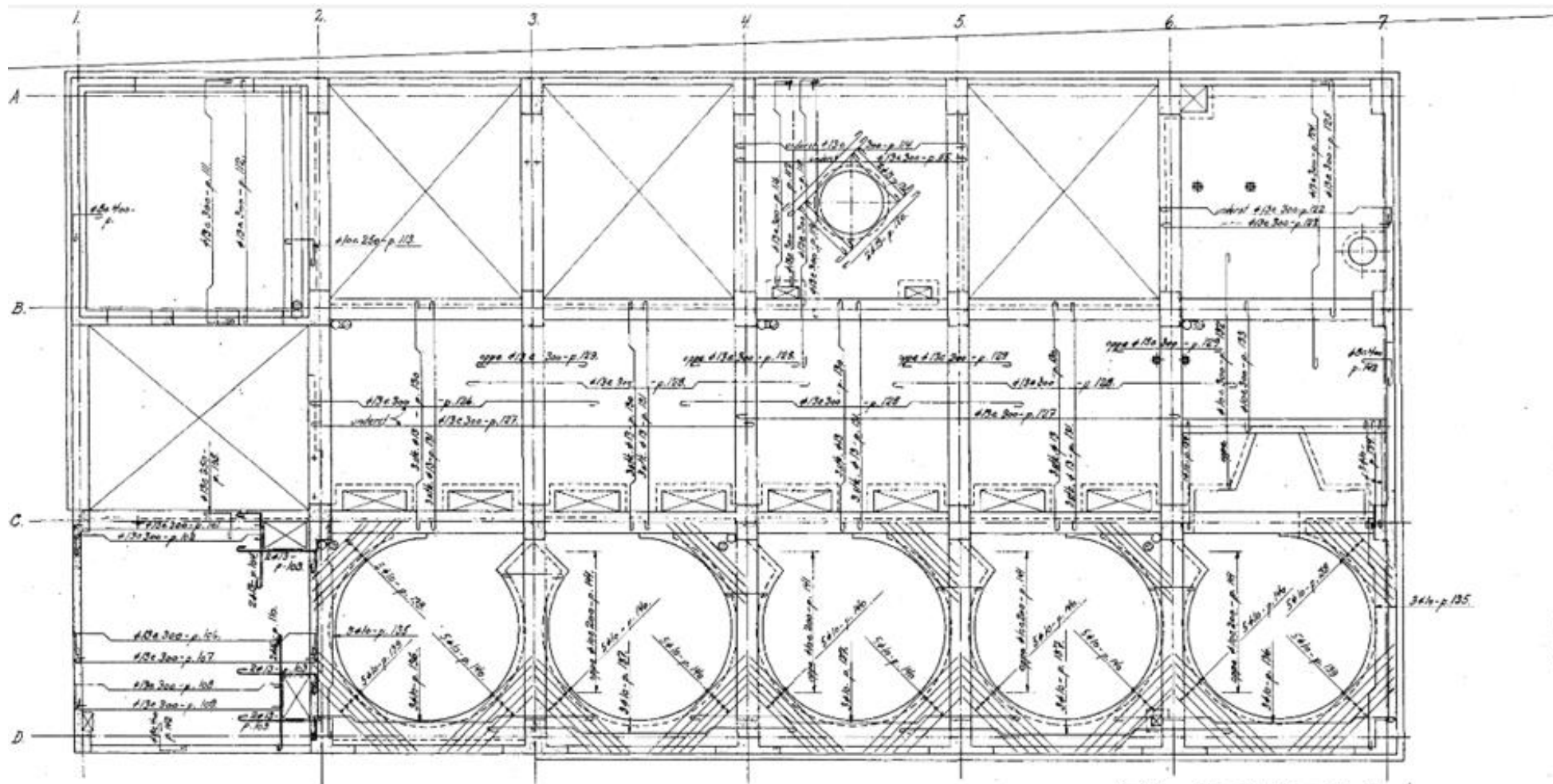
Fotografering av skadet betong

Konklusjon

Oppgaven har konkludert med tilstrekkelig kapasitet for betongdekke, men kravet til rissvidde blir ikke innfridd ved de fleste anledningene. I tillegg til dette er det blitt konstantert at skadene på betongen skyldes det syrlige miljøet og lekkasjer fra anlegget

Vedlegg C:Tegninger og skisser

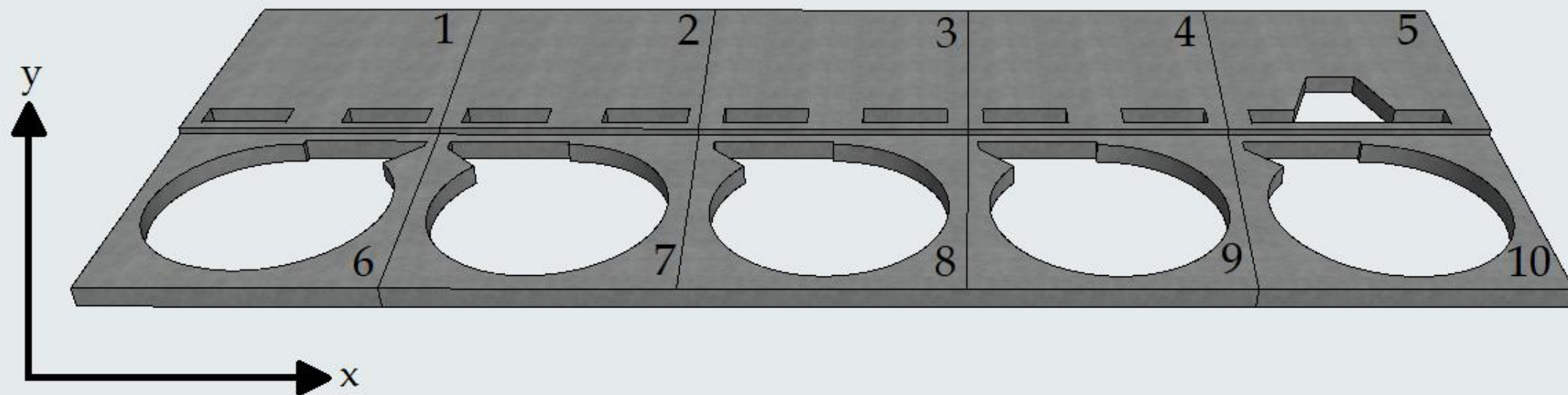
Vedlegg C.1 : Armeringstegning



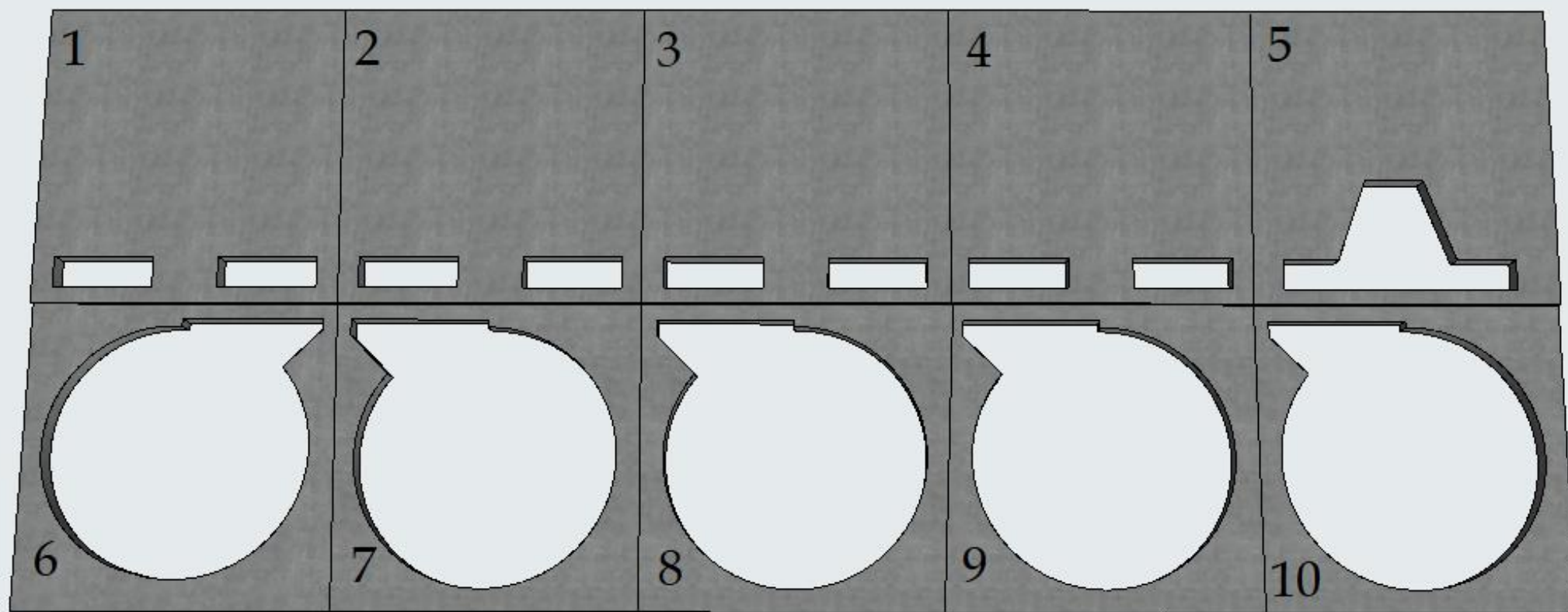
Byggetsk nr 385, side 4-7, par. 101-149.
 For mål, dragerarmoring m.v. henvises til tegn. nr. IF. 31108.
 Hvor annet ikke er angitt bygges 24/3 elektr. rundt alle utpøringer.
 Fordelingsjern i alle armingspister 4/0a 250.
 I topp av alle oppklender bygges inn 1stk. 4/0a 250.

Antall	Egenstand	Nr.	Materialkde	Tegn. nr.	Vækt	Arbeidsføring
NORSK HYDRO-ELEKTRISK KVÆLSTOFKAPITIESELSKAB						
Gitt på kote 119.20 - Armering				Målestokk:	Tegn. 1.1a. 19.3.34	
Sk. 119.20-36				1:50		
Grunn 75.3152-36					38-122	
Tegningen må ikke kopieres, eller offentliggjort uten tillatelse fra selskapet. Den kan bli brukt som referanse i forbindelse med byggingen av andre bygninger. Tegningen skal oppbevares i original i selskapets arkiv.						Erstatning for: 1.F. 31344 A

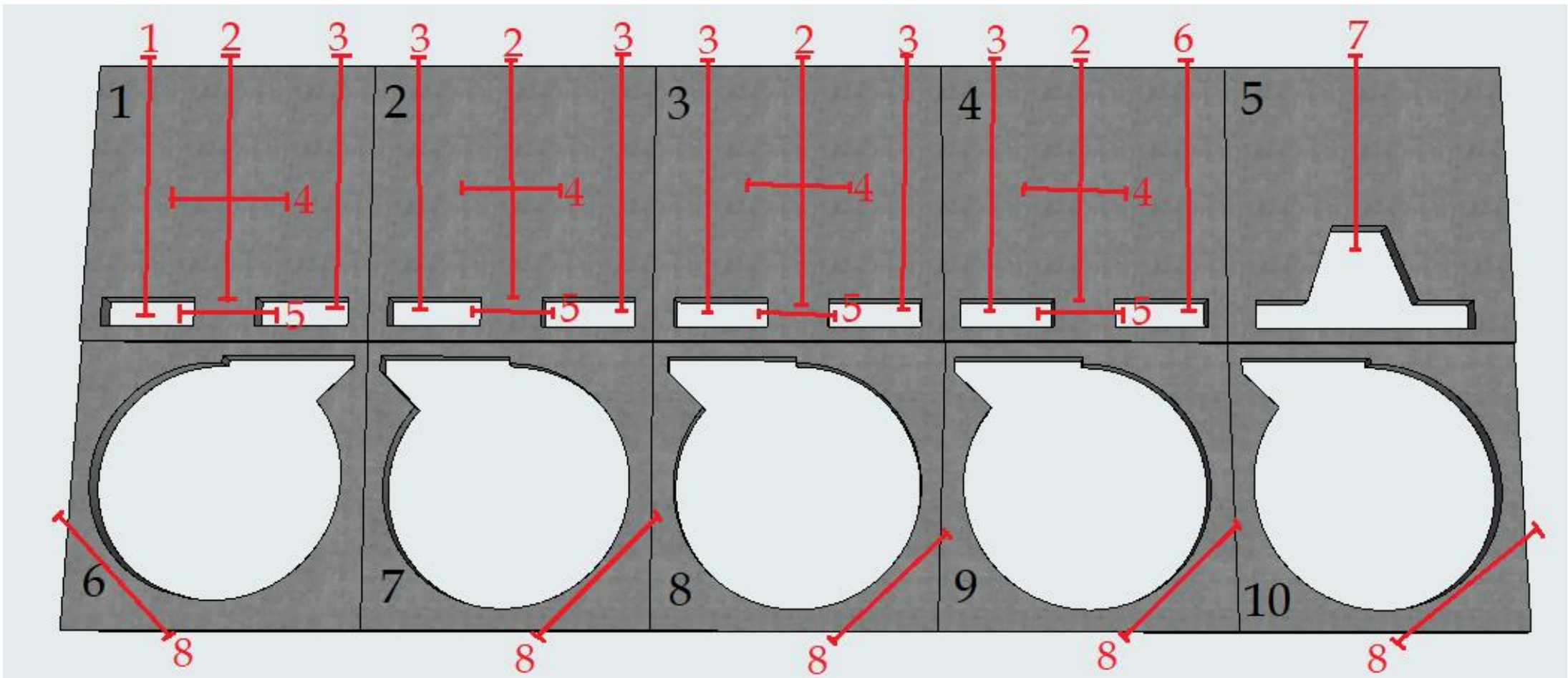
Vedlegg C.2: Plate inndeling (sett fra siden)



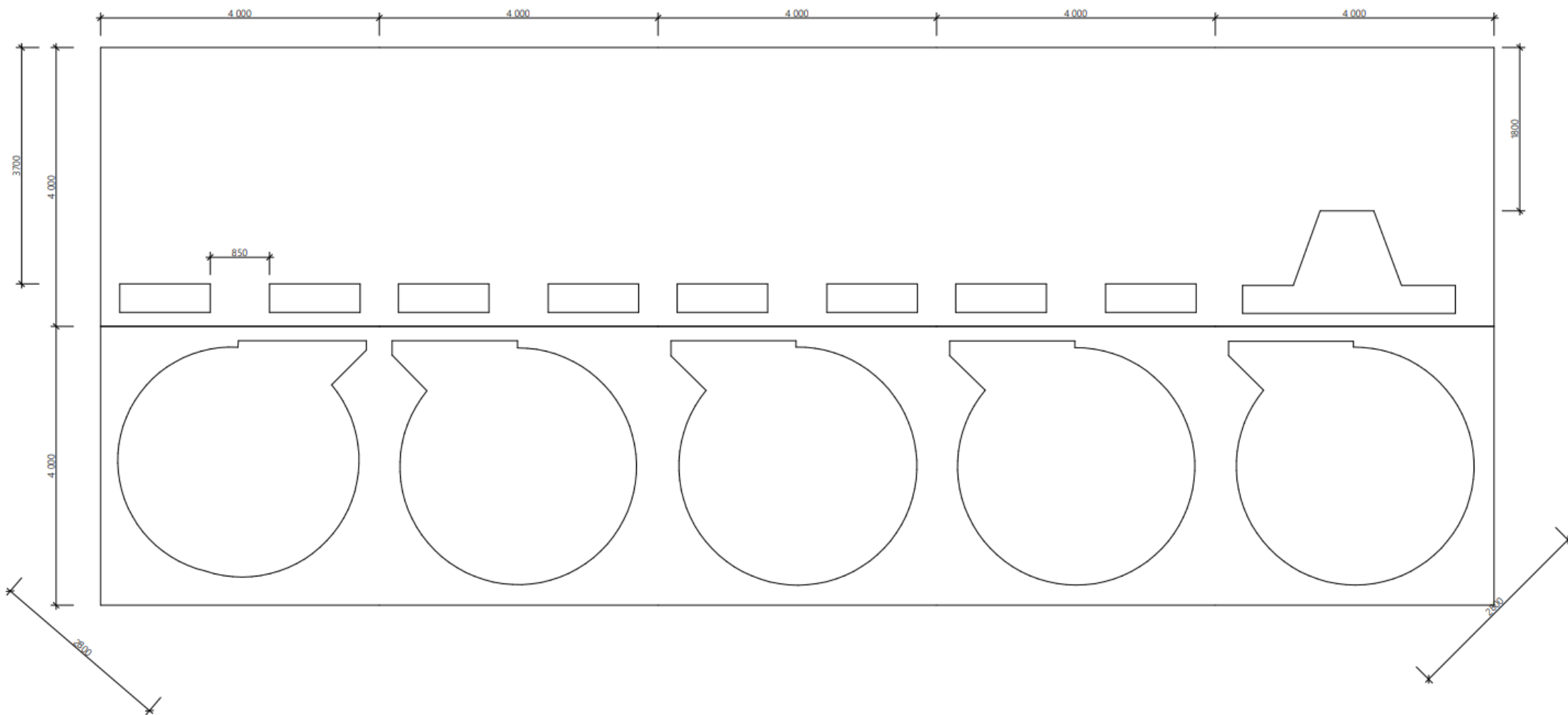
Vedlegg C.3: Plate inndeling (sett ovenfra)



Vedlegg C.4: plassering av snitt



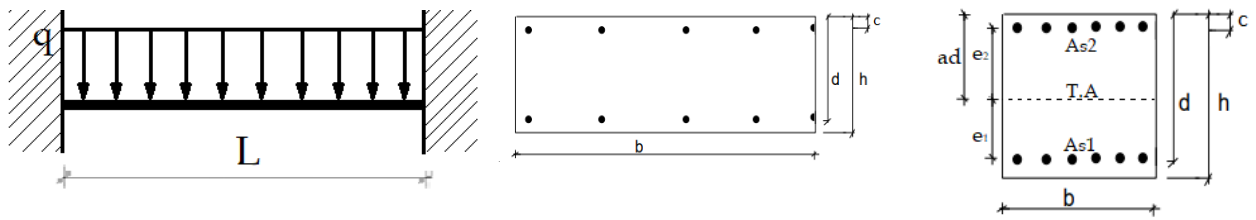
Vedlegg C.5: Plantegning dekke



Vedlegg D: Beregninger

Vedlegg D.1: Snitt 1

Snitt 1:



Sikkerhets faktor

$$\gamma_c = 1.5$$

$$\gamma_s = 1.15$$

$$\alpha_{cc} = 0.85$$

$$\gamma_G = 1.2$$

$$\gamma_Q = 1.5$$

EC2-Tabell 2.1N

EC2-Tabell 2.1N

EC2- NA.3.1.6(1)

EC - Tabell NA.A1.2(A)

EC - Tabell NA.A1.2(A)

Last:

$$p = 7.5 \text{ kN/m}^2 * 1\text{m} = 7.5 \text{ kN/m}$$

(EC1-Tabell 6.4)

$$g_1 = 0$$

$$g_2 = 25\text{kN/m}^3 * 0.3\text{m} * 1\text{m} = 7.5 \text{ kN/m}$$

$$q_{Ed} = \gamma_G * g + \gamma_Q * p = 1.2 * 7.5 + 1.5 * 7.5 = 20.25 \text{ kN/m} \quad (\text{betongelementboka s304})$$

Geometri:

$$h = 300 \text{ mm}$$

$$b = 1000 \text{ mm}$$

$$d = 300 - 10 - \frac{13}{2} = 283.5 \text{ mm}$$

$$c = 10 + \frac{13}{2} = 16.5 \text{ mm}$$

$$h' = h - 2 * c = 267$$

$$L = 4000 \text{ mm}$$

$$e = \frac{h}{2} - (h - d) = 133.5 \text{ mm}$$

Betong: B300 (V413 tabell 2.1.2-1)

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_{cd} = \alpha_{cc} \frac{f_{ck}}{\gamma_c} = 11.3 \text{ N/mm}^2$$

$$f_{cm} = 28 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$f_{ctm} = 2.2 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

Standard armering

$$f_{yk} = 400 \text{ N/mm}^2$$

V413 Tabell 2.1.2-2

$$f_{yd} = \frac{f_{yk}}{\gamma_s} = 347.8 \text{ N/mm}^2$$

$$E_s = 200000 \text{ N/mm}^2$$

EC2- 3.2.7(4)

Betong styrke ved: $t = 3$ dager

EC2-3.1.2

$s = 0.38$ For sement klasse S

$$\beta_{cc}(3) = \exp(s(1 - (\frac{28}{t})^{0.5})) = 0.458$$

$$f_{cm}(3) = \beta_{cc}(3) f_{cm} = 12.8 \text{ N/mm}^2$$

$$f_{ck}(3) = f_{cm}(3) - 8 \text{ MPa} = 4.8 \text{ N/mm}^2$$

$$f_{cd}(3) = \alpha_{cc} \frac{f_{ck}(3)}{\gamma_c} = 2.72 \text{ N/mm}^2$$

EC2-3.1.6

Minimums armering: (EC2-9.2.1.1)

$$A_{s,min} = \max \{ 0.26 \frac{f_{ctm}}{f_{yk}} b_t d; 0.0013 b_t d \} =$$

$$\max \{ 0.26 \frac{2.2}{400} * 1000 * 283.5; 0.0013 * 1000 * 283.5 \} = 405.4 \text{ mm}^2$$

$$\text{Antall jern} = \frac{28 \text{ jern}}{3.7m} = 7.5$$

$$A_s = \pi (\frac{13}{2})^2 * 7.5 = 995.5 \text{ mm}^2$$

$$A_{s1} = A_s / 2 = 497.75 \text{ mm}^2$$

$$A_{s2} = A_s / 2 = 497.75 \text{ mm}^2$$

Minste overdekning: (EC2-4.4.1.2 og NA)

$$c_{min,b} = 13 \text{ mm}$$

$$c_{min,dur} = 60 \text{ mm}$$

EC2-Tabell NA.4.4N

$$\Delta c_{dur,\gamma} = 0$$

$$\Delta c_{dur,st} = \text{ikke gjeldende}$$

$$\Delta c_{dur,add} = \text{ikke gjeldende}$$

$$c_{min} = \max \{ c_{min,b}; c_{min,dur} + \Delta c_{dur,\gamma} - \Delta c_{dur,st} - \Delta c_{dur,add}; 10 \text{ mm} \} = 60 \text{ mm}$$

Nominell overdekning:

(EC2-4.4.1.1(2))

$$c_{nom} = c_{min} + \Delta c_{dev} = 60 + 10 = 70 \text{ mm}$$

Faktisk overdekning = 10mm

$$c_{nom} = 10 \text{ mm}$$

Kapasitetskontroll (M-N diagram)

Punkt 1: Rent trykk

$$\varepsilon_c = \varepsilon_{c3} = 0.00175$$

EC2-Tabell 3.1

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174 < \varepsilon_{c3} \rightarrow \text{armeringen flyter}$$

$$T_c = f_{cd} * b * h = 11.3 * 1000 * 300 = 3390000 \text{ N} = 3390 \text{ kN}$$

$$S_1 = \frac{f_{yk}}{\gamma_s} * A_{s1} = f_{yd} * A_{s1} = 347.8 * 497.75 = 173117.45 \text{ N} = 173 \text{ kN}$$

$$S_2 = S_1$$

$$\text{Aksiell likevekt: } N_1 = T_c + S_1 + S_2 = 3390 + 173 + 173 = \mathbf{3736 \text{ kN}}$$

$$\text{Momentlikevekt: } M_1 = \mathbf{0}$$

Punkt 2: Trykkbrudd i betong

Betong svikter samtidig som stål gir etter

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{s1} = c * \varepsilon_{cu} / h = 16.5 * 0.0035 / 300 = 0.00019 < \varepsilon_{yd} \rightarrow \text{ikke flyting}$$

$$\sigma_{sd} = E_s * \varepsilon_{s1} = 200000 * 0.00019 = 38 \text{ N/mm}^2$$

$$T_c = f_{cd} * b * 0.8h = 11.3 * 1000 * 0.8 * 300 = 2712000 \text{ N} = 2712 \text{ kN}$$

$$S_1 = \sigma_{sd} * A_{s1} = 38 * 497.75 = 11647 \text{ N} = 18.9 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 497.75 = 173117 \text{ N} = 173 \text{ kN}$$

$$\text{Aksiell likevekt: } N_2 = T_c + S_1 + S_2 = 2712 + 18.9 + 173 = \mathbf{2903.9 \text{ kN}}$$

$$\text{Momentlikevekt: } M_2 = T_c * (0.5h - 0.4h) + S_2 * h / 2 - S_1 * h / 2 =$$

$$2712 * (0.5 * 0.300 - 0.4 * 0.300) + 173 * 0.267 / 2 - 18.9 * 0.267 / 2 = \mathbf{102 \text{ kNm}}$$

Punkt 3: Trykkbrudd i betong samtidig med flytning i armering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_s = \varepsilon_{yd}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668$$

$$\alpha d = 0.668 * 283.5 = 189.4 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{189.4 - 16.5}{189.4} * 0.0035 = 0.0032 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d = 11.3 * 1000 * 0.8 * 189.4 = 1712176 \text{ N} = 1712 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 497.75 = 173117 \text{ N} = 173 \text{ kN}$$

$$S_2 = S_1$$

$$\text{Aksiell likevekt : } N_3 = T_c + S_2 - S_1 = 1712 + 173 - 173 = \mathbf{1712 \text{ kN}}$$

$$\begin{aligned} \text{Momentlikevekt : } M_3 &= T_c * (0.5h - 0.4 \alpha d) + S_1 * h' = \\ 1712 * (0.5 * 300 - 0.4 * 189.4) + 173 * 267 &= \mathbf{173 \text{ kNm}} \end{aligned}$$

Punkt 4: Trykkbrudd i betong og dobbel flytetøyning i strekkarmering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 2\varepsilon_{yk}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 2\varepsilon_{yk}} = \frac{0.0035}{0.0035 + 2 * 0.002} = 0.467$$

Sørensen (4.22)

$$\alpha d = 0.467 * 283.5 = 132.4 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{132.4 - 16.5}{132.4} * 0.0035 = 0.003 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d = 11.3 * 1000 * 0.8 * 132.4 = 1196896 \text{ N} = 1196.9 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 497.75 = 173117 \text{ N} = 173 \text{ kN}$$

$$S_2 = S_1$$

$$\text{Aksiell likevekt : } N_4 = T_c + S_2 - S_1 = 1196.9 + 173 - 173 = \mathbf{1196.9 \text{ kN}}$$

$$\begin{aligned} \text{Momentlikevekt : } M_4 &= T_c * (0.5h - 0.4 \alpha d) + S_1 * h' = \\ 1196.9 * (0.5 * 300 - 0.4 * 132.4) + 173 * 267 &= \mathbf{160 \text{ kNm}} \end{aligned}$$

Punkt 5: Trykkbrudd i betong og stor armeringstøyning

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 0.015$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 0.015} = \frac{0.0035}{0.0035 + 0.015} = 0.189$$

Sørensen (4.22)

$$\alpha d = 0.189 * 283.5 = 53.6 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{53.6 - 16.5}{53.6} * 0.0035 = 0.0024 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d = 11.3 * 1000 * 0.8 * 53.6 = 484544 \text{ N} = 485 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 497.75 = 173117 \text{ N} = 173 \text{ kN}$$

$$S_2 = S_1$$

$$\text{Aksiell likevekt : } N_5 = T_c + S_2 - S_1 = 485 + 173 - 173 = \mathbf{485 \text{ kN}}$$

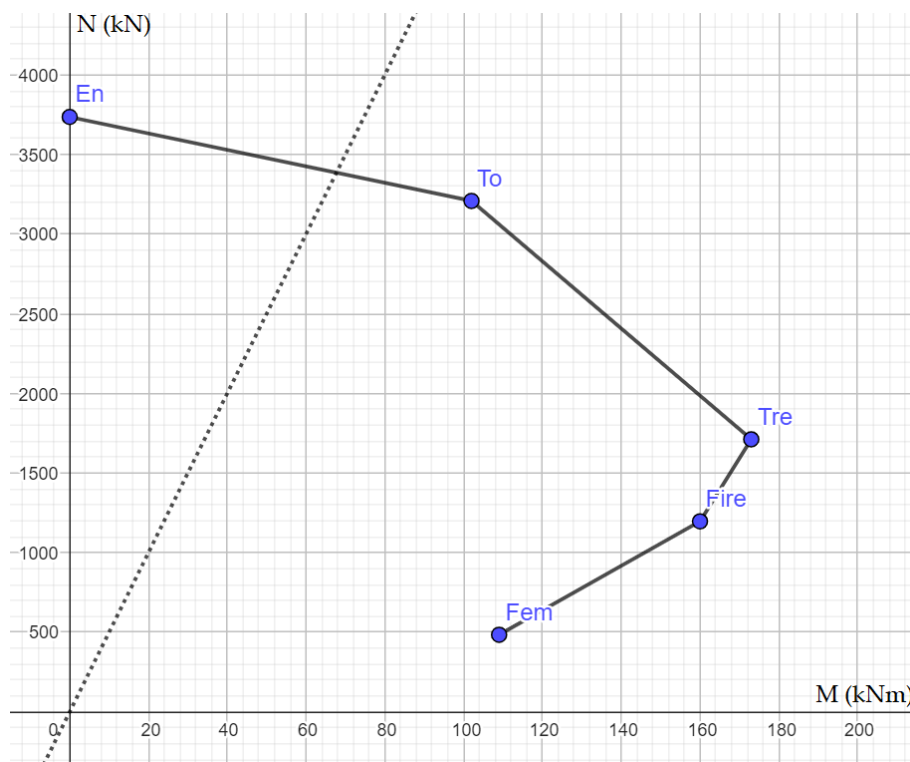
$$\text{Momentlikevekt : } M_5 = T_c * (0.5h - 0.4 \alpha d) + S_1 * h/2 + S_2 * h/2 =$$

$$485 * (0.5 * 300 - 0.4 * 53.6) + 173 * 267/2 + 173 * 267/2 = \mathbf{109 \text{ kNm}}$$

$$e_0 = \max \{h/30, 20\text{mm}\} = 20\text{mm}$$

EC2-6.1 (4)

Resulterende interaksjonsdiagram:



Skjærkapasitet:

Dimensjonerende skjærkraft: $V_{Ed} = \frac{q_{Ed} * L}{2} = \frac{20.25 * 4}{2} = 40.5 \text{ kN}$

Skjærstrekkapasitet: $V_{Rd,c} = C_{Rd,c} * K * (100 * P_L * f_{ck})^{\frac{1}{3}} * b_w * d$ Sørensen (4.43)

$$K = 1 + \sqrt{\frac{200}{d}} \leq 2.0$$

$$= 1 + \sqrt{\frac{200}{283.5}} = 1.84$$

$$P_L = \frac{A_{sL}}{b_w * d} \leq 0.02$$

$$= \frac{497.75}{1000 * 283.5} = 0.00176$$

$$K_2 = 0.15 \quad \text{EC2-NA.6.2.2 (1)}$$

$$C_{Rd,c} = \frac{K_2}{\gamma_c} = \frac{0.15}{1.5} = 0.1$$

$$V_{Rd,c} = 0.1 * 1.84 * (100 * 0.00176 * 20)^{\frac{1}{3}} * 1000 * 283.5 = 79350.9 \text{ N} = \mathbf{79.3 \text{ kN}}$$

$$V_{Rd,c} > V_{Ed}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 79.3 \rightarrow p = \mathbf{20.4 \text{ kN/m}}$$

Skjærtrykkapasitet: $V_{Rd,max} = 0.5 * b_w * d * v * f_{cd}$

$$v = 0.6 * (1 - \frac{f_{ck}}{250}) = 0.6 * (1 - \frac{20}{250}) = 0.552 \quad \text{Sørensen (4.51)}$$

$$V_{Rd,max} = 0.5 * 1000 * 283.5 * 0.552 * 11.3 = 884179.8 \text{ N} = \mathbf{884 \text{ kN}}$$

$$V_{Rd,max} > V_{Ed}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 884 \rightarrow p = \mathbf{288 \text{ kN/m}}$$

Momentkapasitet:

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174$$

$$\alpha_b = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668 \quad \text{Sørensen (4.20)}$$

$$\lambda = 0.8 \quad \text{EC2-3.1.7 (3)}$$

$$\eta = 1.0 \quad \text{EC2-3.1.7 (3)}$$

$$A_{s,b} = \lambda \eta * \frac{f_{cd}}{f_{yd}} * b * d * \alpha_b = 0.8 * 1.0 * \frac{11.3}{347.8} * 1000 * 283.5 * 0.668 = 4922 \text{ mm}^2 \quad \text{Sørensen (4.21)}$$

$$\rightarrow A_s < A_{s,b}$$

$$\lambda * \eta * f_{cd} * b * d * \alpha - f_{yd} * A_s = 0 \quad \text{Sørensen (4.19)}$$

$$\rightarrow \alpha = \frac{f_{yd} * A_s}{\lambda * \eta * f_{cd} * b * d} = \frac{347.8 * 995.5}{0.8 * 1.0 * 11.3 * 1000 * 283.5} = 0.135$$

$$\varepsilon_s = \frac{1 - \alpha}{\alpha} * \varepsilon_{cu} = \frac{1 - 0.135}{0.135} * 0.0035 = 0.0224$$

$$\rightarrow \varepsilon_s < \varepsilon_{ud} = 0.03 \quad \text{EC2- Tabell NA.3.5 (901)}$$

$$M_{Rd} = \lambda \eta \alpha * (1 - 0.5 * \lambda \alpha) * f_{cd} * b * d^2 \quad \text{Sørensen (4.14)}$$

$$= 0.8 * 1.0 * 0.135 * (1 - 0.5 * 0.8 * 0.135) * 11.3 * 1000 * 283.5^2$$

$$= 92789634 \text{ Nmm} = \mathbf{92.7 \text{ kNm}}$$

$$M_{Ed} = \frac{[1.2(g_1 + g_2) + 1.5 \cdot p] * L^2}{12} = \frac{(1.2 * 7.5 + 1.5 * 7.5) * 4^2}{12} = \mathbf{27 \text{ kNm}}$$

$$M_{Rd} > M_{Ed} \text{ OK.}$$

$$\text{Max nyttelast : } \frac{(7.5 * 1.2 + p * 1.5) * 4^2}{12} = 92.7 \rightarrow p = \mathbf{40 \text{ kN/m}}$$

Aksialkraftkapasitet:

$$A_c = b * h = 1000 * 300 = 300000 \text{ mm}^2$$

$$N_{Rd} = f_{cd} (A_c - A_s) + f_{yd} * A_s \quad \text{Sørensen (4.5)}$$

$$= 11.3 * (300000 - 995.5) + 347.8 * 995.5 = 3724985.75 \text{ N} = \mathbf{3724 \text{ kN}}$$

Nedbøyning:

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_s = 200000 \text{ N/mm}^2$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{995.5}{1000 \cdot 283.5} = 0.0035$$

$$\eta\rho = 6.667 \cdot 0.0035 = 0.023$$

$$\alpha = \sqrt{(\eta\rho)^2 + 2\eta\rho} - \eta\rho = \sqrt{0.023^2 + 2 \cdot 0.023} - 0.023 = 0.19$$

Sørensen (5.5)

$$I_s = A_s \cdot (1-\alpha) \cdot \left(1 - \frac{\alpha}{3}\right) \cdot d^2 = 995.5 \cdot (1-0.19) \cdot \left(1 - \frac{0.19}{3}\right) \cdot 283.5^2 = 6.07 \cdot 10^7 \text{ mm}^4$$

Sørensen (5.11)

$$EI = E_s \cdot I_s = 200000 \cdot 6.07 \cdot 10^7 = 1.21 \cdot 10^{13} \text{ Nmm}^2$$

Sørensen (5.12)

$$q = 15 \text{ kN/m}$$

$$\text{Nedbøyning (bruksgrensetilstand)} : \delta_{II} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{15 \cdot 4000^4}{384 \cdot 1.21 \cdot 10^{13}} = \mathbf{0.83 \text{ mm}}$$

Langtidsnedbøyning:

permanent last:

$$g = 7.5 \cdot 1.2 = 9 \text{ kN/m}$$

$$p = 7.5 \cdot 1.5 = 11.25 \text{ kN/m (antar 100\% permanent)}$$

$$\text{lasttilfelle 1: } g = 9 \text{ kN/m, } \varphi(\infty, 3)$$

$$\text{lasttilfelle 2: } p = 11.25 \text{ kN/m, } \varphi(\infty, 28)$$

$$h_0 = \frac{2A_c}{u} = \frac{2 \cdot 300 \cdot 1000}{2 \cdot (300 + 1000)} = 231 \text{ mm}$$

Kryptall : utendørsforhold

EC2-Tillegg B

$$\varphi(t, t_0) = \varphi_0 \cdot \beta(t, t_0)$$

$$\varphi_0 = \varphi_{RH} \cdot \beta(f_{cm}) \cdot \beta(t_0)$$

$$RH = 80 \text{ (utendørsforhold)}$$

$$\varphi_{RH} = 1 + \frac{1 - \frac{RH}{100}}{0.1 \cdot \sqrt[3]{h_0}} = 1 + \frac{1 - \frac{80}{100}}{0.1 \cdot \sqrt[3]{231}} = 1.33$$

$$\beta(f_{cm}) = \frac{16.8}{\sqrt{f_{cm}}} = \frac{16.8}{\sqrt{28}} = 3.17$$

$$\beta(t_0) = \frac{1}{(0.1 + t_0^{0.20})}$$

$$\beta(3) = \frac{1}{(0.1 + 3^{0.20})} = 0.74$$

$$\beta(28) = \frac{1}{(0.1 + 28^{0.20})} = 0.49$$

$$\varphi_3 = 1.33 \cdot 3.17 \cdot 0.74 = 3.12$$

$$\varphi_{28} = 1.33 \cdot 3.17 \cdot 0.49 = 2.07$$

$$\beta(t, t_0) = \left[\frac{(t - t_0)}{(\beta_H + t - t_0)} \right]^{0.3}$$

$$\beta(\infty, 3) \rightarrow 1$$

$$\beta(\infty, 28) \rightarrow 1$$

$$\varphi(\infty, 3) = 4.96 \cdot 1 = 3.12$$

$$\varphi(\infty, 28) = 4.71 \cdot 1 = 2.07$$

$$E_{c1} = \frac{E_{cm}}{1 + \varphi(t, t_0)}$$

$$E_{c1} = \frac{30000}{1+3.12} = 7282 \text{ MPa}$$

$$E_{c2} = \frac{30000}{1+2.07} = 9772 \text{ MPa}$$

$$M_1 = \frac{q \cdot L^2}{12} = \frac{(9) \cdot 4^2}{12} = 12 \text{ kNm}$$

$$M_2 = \frac{q \cdot L^2}{12} = \frac{(11.25) \cdot 4^2}{12} = 15 \text{ kNm}$$

$$E_{c, \text{middle}} = \frac{\frac{M_1 + M_2}{\frac{M_1}{E_{c1}} + \frac{M_2}{E_{c2}}}}{\frac{12+15}{\frac{12}{7282} + \frac{15}{9772}}} = 8483 \text{ MPa}$$

$$\eta = \frac{E_s}{E_{c, \text{middle}}} = \frac{200000}{8483} = 23.6$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{995.5}{1000 \cdot 283.5} = 0.0035$$

$$\eta \rho = 23.6 \cdot 0.0035 = 0.083$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.083^2 + 2 \cdot 0.083} - 0.083 = 0.33$$

Sørensen (5.5)

$$I_c = 0.5 \cdot \alpha^2 \cdot (1 - \frac{\alpha}{3}) \cdot b \cdot d^3 = 0.5 \cdot 0.33^2 \cdot (1 - \frac{0.33}{3}) \cdot 1000 \cdot 283.5^3 = 1.10 \cdot 10^9 \text{ mm}^4$$

Sørensen (5.9)

$$EI = E_{c, \text{middle}} \cdot I_c = 8483 \cdot 1.10 \cdot 10^9 = 9.3 \cdot 10^{12} \text{ Nmm}^2$$

Sørensen (5.10)

Nedbøyning midt på bjelken:

$$\delta_{\text{Lang}} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{20.25 \cdot 4000^4}{384 \cdot 9.3 \cdot 10^{12}} = 1.45 \text{ mm}$$

Nedbøyning pga svinn:

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot \alpha_{ds1}) \cdot e^{\frac{(-\alpha_{ds2} \cdot f_{cm})}{f_{cm0}}}] \cdot 10^{-6} \cdot \beta_{RH}$$

Sørensen (5.27)

$$f_{cm0} = 10 \text{ MPa}$$

$$\alpha_{ds1} = 3$$

(Sement klasse S)

$$\alpha_{ds2} = 0.13$$

(Sement klasse S)

$$\beta_{RH} = 1.55 [1 - (\frac{RH}{RH_0})^3] = 1.55 [1 - (\frac{80}{100})^3] = 0.76$$

Sørensen (5.28)

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot 3) \cdot e^{\frac{(-0.13 \cdot 28)}{10}}] \cdot 10^{-6} \cdot 0.76 = 2.47 \cdot 10^{-4}$$

$$\epsilon_{cd}(t) = \beta_{ds}(t, t_s) \cdot k_h \cdot \epsilon_{cd,0}$$

Sørensen (5.29)

$$\beta_{ds}(t, t_s) = \frac{(t - t_s)}{(t - t_s) + 0.4 \sqrt{h_0^3}} : t \rightarrow \infty \rightarrow \beta_{ds} = 1$$

$$k_h = 0.78$$

EC2-Tabell 3.3

$$\epsilon_{cd}(\infty) = 1 \cdot 0.78 \cdot 2.47 \cdot 10^{-4} = 1.93 \cdot 10^{-4}$$

$$\epsilon_{ca}(\infty) = 2.5 (f_{ck} - 10) \cdot 10^{-6} = 2.5 (20 - 10) \cdot 10^{-6} = 2.5 \cdot 10^{-5}$$

Sørensen (5.31)

$$\epsilon_{cs} = \epsilon_{cd} + \epsilon_{ca} = 1.93 \cdot 10^{-4} + 2.5 \cdot 10^{-5} = 2.18 \cdot 10^{-4}$$

Sørensen (5.26)

Svinnkrumning:

$$K_s = \epsilon_{cs} * \eta * \frac{A_s * e}{I}$$

Sørensen (s.135)

$$\alpha d = \frac{h}{2} = \frac{300}{2} = 150$$

$$e = d - \alpha d = 283.5 - 150 = 133.5$$

$$I = \frac{b * h^3}{12} + b * h * \left(\alpha d - \frac{h}{2} \right)^2 + \eta * A_s * e^2$$

$$= \frac{1000 * 300^3}{12} + 1000 * 300 * \left(150 - \frac{300}{2} \right)^2 + 23.6 * 995.5 * 133.5^2 = 26.69 * 10^8 \text{ mm}^4$$

$$K_s = 2.18 * 10^{-4} * 23.6 * \frac{995.5 * 133.5}{26.69 * 10^8} = 2.56 * 10^{-7} \text{ mm}^{-1}$$

$$\delta_{svinn} = \frac{K_s * L^2}{8} = \frac{2.56 * 10^{-7} * 4000^2}{8} = \mathbf{0.51 \text{ mm}}$$

$$\delta_{total} = \delta_{lang} + \delta_{svinn} = 1.45 + 0.51 = \mathbf{1.96 \text{ mm}}$$

$$\delta_{maks} = \frac{L}{250} = \frac{4000}{250} = 16 \text{ mm} > 1.93 \rightarrow \text{ok}$$

EC2-7.4.1 (4)

$$\text{Max nyttelast : } 16 = \frac{(7.5 * 1.2 + 1.5 * q) * 4000^4}{384 * 9.3 * 10^{12}} + 0.51 \rightarrow q = 138 \text{ kN/m}$$

Rissviddekontroll:

$$k_c = c_{nom} / c_{min, dur} = 10 / 60 = 0.1667$$

$$w_{max} = 0.3 * k_c = 0.3 * 0.1667 = 0.05 \text{ mm}$$

Sørensen (tabell 5.2)

$$M = \frac{20.25 * 4^2}{12} = 27 \text{ kNm}$$

$$\sigma_s = E_s * \frac{M(1-\alpha)d}{EI} = 200000 * \frac{27 * 10^6 * (1-0.33) * 283.5}{9.3 * 10^{12}} = 110 \text{ MPa}$$

Sørensen (5.55)

$$k_t = 0.4 \text{ (langvarig last)}$$

$$f_{ct, eff} = f_{cmt} = 2.2 \text{ MPa}$$

EC2-Tabell 3.1

$$h_{c, eff} = \min \left\{ 2.5(h-d); \left(\frac{h-\alpha d}{3} \right); \frac{h}{2} \right\} = \min \left\{ 2.5(300-283.5); \left(\frac{300-0.33*283.5}{3} \right); \frac{300}{2} \right\} = 41.25$$

$$\rho_{p, eff} = \frac{A_s}{A_{c, eff}} = \frac{995.5}{1000 * 41.25} = 0.024$$

Sørensen (s.153)

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{\sigma_s - k_t * \frac{f_{ct, eff}}{\rho_{p, eff}} * (1 + \eta \rho_{p, eff})}{E_s} \geq 0.6 * \frac{\sigma_s}{E_s}$$

Sørensen (5.59)

$$\epsilon_{sm} - \epsilon_{cm} = \frac{110 - 0.4 * \frac{2.2}{0.024} * (1 + 6.667 * 0.024)}{200000} = 3.37 * 10^{-4} \geq 0.6 * \frac{110}{200000} = 3.3 * 10^{-4}$$

$$C_{nom} = 10 \text{ mm}$$

$$5 * (C_{nom} + \frac{\emptyset}{2}) = 5 * (10 + \frac{13}{2}) = 82.5 < \text{senteravstand} = 300$$

$$S_{r, max} = 1.3 * (h - \alpha d) = 1.3 * (300 - 0.33 * 283.5) = 268.4$$

Sørensen (5.61)

$$w_k = S_{r, max} * (\epsilon_{sm} - \epsilon_{cm}) = 268.4 * 3.37 * 10^{-4} = \mathbf{0.09}$$

Sørensen (5.58)

$$w_k > w_{max} = 0.05 \text{ (Rissviddekrav ikke oppfylt)}$$

Max nyttelast:

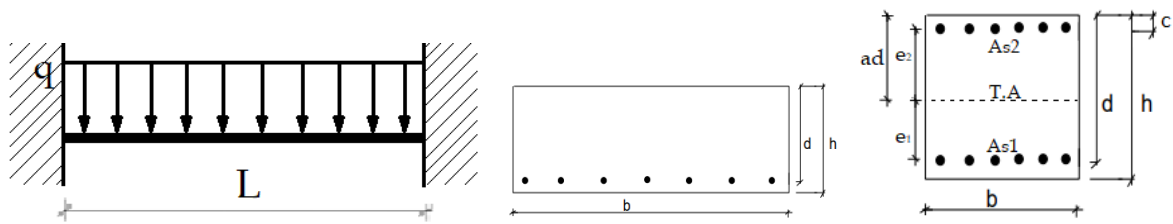
$$268.4 * \frac{\sigma_s - 0.4 * \frac{2.2}{0.024} * (1 + 6.667 * 0.024)}{200000} = 0.05 \rightarrow \sigma_s = 79.7$$

$$200000 * \frac{M * 10^6 * (1 - 0.33) * 283.5}{9.3 * 10^{12}} = 79.7 \rightarrow M = 19.5$$

$$\frac{(1.2 * 7.5 + 1.5 * q) * 4^2}{12} = 19.5 \rightarrow q = 3.7$$

Vedlegg D.2: Snitt 2

Snitt 2:



Sikkerhets faktor

$$\gamma_c = 1.5$$

EC2-Tabell 2.1N

$$\gamma_s = 1.15$$

EC2-Tabell 2.1N

$$\alpha_{cc} = 0.85$$

EC2- NA.3.1.6(1)

$$\gamma_G = 1.2$$

EC - Tabell NA.A1.2(A)

$$\gamma_Q = 1.5$$

EC - Tabell NA.A1.2(A)

Last:

$$p = 7.5 \text{ kN/m}^2 * 1\text{m} = 7.5 \text{ kN/m}$$

(EC1-Tabell 6.4)

$$g_1 = 0$$

$$g_2 = 25 \text{ kN/m}^3 * 0.3\text{m} * 1\text{m} = 7.5 \text{ kN/m}$$

$$q_{Ed} = \gamma_G * g + \gamma_Q * p = 1.2 * 7.5 + 1.5 * 7.5 = 20.25 \text{ kN/m} \quad (\text{betongelementboka s304})$$

Geometri:

$$h = 300 \text{ mm}$$

$$b = 1000 \text{ mm}$$

$$d = 300 - 10 - \frac{13}{2} = 283.5 \text{ mm}$$

$$c = 10 + \frac{13}{2} = 16.5 \text{ mm}$$

$$h' = h - 2 * c = 267$$

$$L = 4000 \text{ mm}$$

Betong: B300 (V413 tabell 2.1.2-1)

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_{cd} = \alpha_{cc} \frac{f_{ck}}{\gamma_c} = 11.3 \text{ N/mm}^2$$

$$f_{cm} = 28 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$f_{ctm} = 2.2 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

Standard armering:

$$f_{yk} = 400 \text{ N/mm}^2$$

V413 Tabell 2.1.2-2

$$f_{yd} = \frac{f_{yk}}{\gamma_s} = 347.8 \text{ N/mm}^2$$

$$E_s = 200000 \text{ N/mm}^2$$

EC2- 3.2.7(4)

Betong styrke ved: $t = 3$ dager

EC2-3.1.2

$s = 0.38$ For sement klasse S

$$\beta_{cc}(3) = \exp\left(s\left(1 - \left(\frac{28}{t}\right)^{0.5}\right)\right) = 0.458$$

$$f_{cm}(3) = \beta_{cc}(3) f_{cm} = 12.8 \text{ N/mm}^2$$

$$f_{ck}(3) = f_{cm}(3) - 8 \text{ MPa} = 4.8 \text{ N/mm}^2$$

$$f_{cd}(3) = \alpha_{cc} \frac{f_{ck}(3)}{\gamma_c} = 2.72 \text{ N/mm}^2$$

EC2-3.1.6

Minimums armering: (EC2-9.2.1.1)

$$A_{s,min} = \max \left\{ 0.26 \frac{f_{ctm}}{f_{yk}} b_t d; 0.0013 b_t d \right\} =$$

$$\max \left\{ 0.26 \frac{2.2}{400} * 1000 * 283.5; 0.0013 * 1000 * 283.5 \right\} = 405.4 \text{ mm}^2$$

$$\text{Antall jern} = \frac{28 \text{ jern}}{3.7m} = 7.5$$

$$A_s = \pi \left(\frac{13}{2}\right)^2 * 7.5 = 995.5 \text{ mm}^2$$

$$A_{s1} = A_s = 995.5 \text{ mm}^2$$

$$A_{s2} = 0 = 0 \text{ mm}^2$$

Minste overdekning: (EC2-4.4.1.2 og NA)

$$c_{min,b} = 13 \text{ mm}$$

$$c_{min,dur} = 60 \text{ mm}$$

EC2-Tabell NA.4.4N

$$\Delta c_{dur,\gamma} = 0$$

$$\Delta c_{dur,st} = \text{ikke gjeldende}$$

$$\Delta c_{dur,add} = \text{ikke gjeldende}$$

$$c_{min} = \max\{c_{min,b}; c_{min,dur} + \Delta c_{dur,\gamma} - \Delta c_{dur,st} - \Delta c_{dur,add}; 10\text{mm}\} = 60 \text{ mm}$$

Nominell overdekning:

(EC2-4.4.1.1(2))

$$c_{nom} = c_{min} + \Delta c_{dev} = 60 + 10 = 70 \text{ mm}$$

Faktisk overdekning = 10mm

$$c_{nom} = 10\text{mm}$$

Kapasitetskontroll (M-N diagram)

$$\eta = \frac{E_s}{E_{c,middel}} = \frac{200000}{8483} = 23.6 \text{ (se langtidsnedbøyning)}$$
$$\alpha d = \frac{A_c * 0.5h + \eta * A_s * d}{A_c + \eta * A_s} = \frac{300000 * 0.5 * 300 + 23.6 * 995.5 * 283.5}{300000 + 23.6 * 995.5} = 160$$
$$e = d - \alpha d = 283.5 - 160 = 123.5$$

Punkt 1: Rent trykk

$$\varepsilon_c = \varepsilon_{c3} = 0.00175$$

EC2-Tabell 3.1

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174 < \varepsilon_{c3} \rightarrow \text{armeringen flyter}$$

$$T_c = f_{cd} * b * h = 11.3 * 1000 * 300 = 3390000 \text{ N} = 3390 \text{ kN}$$

$$S_1 = \frac{f_{yk}}{\gamma_s} * A_{s1} = f_{yd} * A_{s1} = 347.8 * 995.5 = 346235 \text{ N} = 346 \text{ kN}$$

$$S_2 = 0$$

$$\text{Aksiell likevekt: } N_1 = T_c + S_1 + S_2 = 3390 + 346 = \mathbf{3736 \text{ kN}}$$

$$\text{Momentlikevekt: } M_1 = T_c * (\alpha d - 0.5h) - S_1 * e$$

$$3390 * (160 - 150) - 346 * 123.5 = \mathbf{-8.8}$$

Punkt 2: Trykkbrudd i betong

Betong svikter samtidig som stål gir etter

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{s1} = c * \varepsilon_{cu} / h = 16.5 * 0.0035 / 300 = 0.00019 < \varepsilon_{yd} \rightarrow \text{ikke flyting}$$

$$\sigma_{sd} = E_s * \varepsilon_{s1} = 200000 * 0.00019 = 38 \text{ N/mm}^2$$

$$T_c = f_{cd} * b * 0.8h = 11.3 * 1000 * 0.8 * 300 = 2712000 \text{ N} = 2712 \text{ kN}$$

$$S_1 = \sigma_{sd} * A_{s1} = 38 * 995.5 = 37829 \text{ N} = 38 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 0 = 0 \text{ N} = 0 \text{ kN}$$

$$\text{Aksiell likevekt: } N_2 = T_c + S_1 + S_2 = 2712 + 38 = \mathbf{2750 \text{ kN}}$$

$$\text{Momentlikevekt: } M_2 = T_c * (\alpha d - 0.4h) + S_2 * e_2 - S_1 * e_1 =$$

$$2712 * (160 - 0.4 * 300) - 38 * 123.5 = \mathbf{104 \text{ kNm}}$$

Punkt 3: Trykkbrudd i betong samtidig med flytning i armering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_s = \varepsilon_{yd}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668$$

$$\alpha d_2 = 0.668 * 283.5 = 189.4 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{189.4 - 16.5}{189.4} * 0.0035 = 0.0032 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d = 11.3 * 1000 * 0.8 * 189.4 = 1712176 \text{ N} = 1712 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 995.5 = 346234.9 \text{ N} = 346 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 0 = 0 \text{ N} = 0 \text{ kN}$$

$$\text{Aksiell likevekt : } N_3 = T_c + S_2 - S_1 = 1712 - 346 = \mathbf{1366 \text{ kN}}$$

$$\text{Momentlikevekt : } M_3 = T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e = \\ 1712 * (160 - 0.4 * 189.4) + 346 * 123.5 = \mathbf{187 \text{ kNm}}$$

Punkt 4: Trykkbrudd i betong og dobbel flytetøyning i strekkarmering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 2\varepsilon_{yk}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 2\varepsilon_{yk}} = \frac{0.0035}{0.0035 + 2*0.002} = 0.467$$

Sørensen (4.22)

$$\alpha d_2 = 0.467 * 283.5 = 132.4 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{132.4 - 16.5}{132.4} * 0.0035 = 0.003 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 132.4 = 1196896 \text{ N} = 1196.9 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 995.5 = 346234.9 \text{ N} = 346 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 0 = 0 \text{ N} = 0 \text{ kN}$$

$$\text{Aksiell likevekt : } N_4 = T_c + S_2 - S_1 = 1196.9 - 346 = \mathbf{850.9 \text{ kN}}$$

$$\text{Momentlikevekt : } M_4 = T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e + S_2 * h' / 2 = \\ 1196.9 * (160 - 0.4 * 132.4) + 346 * 123.5 = \mathbf{171 \text{ kNm}}$$

Punkt 5: Trykkbrudd i betong og stor armeringstøyning

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 0.015$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 0.015} = \frac{0.0035}{0.0035 + 0.015} = 0.189$$

Sørensen (4.22)

$$\alpha d_2 = 0.189 * 283.5 = 53.6 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{53.6 - 16.5}{53.6} * 0.0035 = 0.0024 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 53.6 = 484544 \text{ N} = 485 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 995.5 = 346234.9 \text{ N} = 346 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 0 = 0 \text{ N} = 0 \text{ kN}$$

$$\text{Aksiell likevekt : } N_5 = T_c + S_2 - S_1 = 484 + 0 - 346 = \mathbf{138 \text{ kN}}$$

$$\text{Momentlikevekt : } M_5 = T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e =$$

$$485 * (160 - 0.4 * 53.6) + 346 * 123.5 = \mathbf{110 \text{ kNm}}$$

$$e_0 = \max \{h/30, 20\text{mm}\} = 20\text{mm}$$

EC2-6.1 (4)

Resulterende interaksjonsdiagram:



Skjærkapasitet:

$$\text{Dimensjonerende skjærkraft: } V_{Ed} = \frac{q_{Ed} * L}{2} = \frac{20.25 * 4}{2} = 40.5 \text{ kN}$$

$$\text{Skjærstrekkapasitet: } V_{Rd,c} = C_{Rd,c} * K * (100 * P_L * f_{ck})^{\frac{1}{3}} * b_w * d \quad \text{Sørensen (4.43)}$$

$$K = 1 + \sqrt{\frac{200}{d}} \leq 2.0$$

$$= 1 + \sqrt{\frac{200}{283.5}} = 1.84$$

$$P_L = \frac{A_{sL}}{b_w * d} \leq 0.02$$

$$= \frac{995.5}{1000 * 283.5} = 0.0035$$

$$K_2 = 0.15 \quad \text{EC2-NA.6.2.2 (1)}$$

$$C_{Rd,c} = \frac{K_2}{\gamma_c} = \frac{0.15}{1.5} = 0.1$$

$$V_{Rd,c} = 0.1 * 1.84 * (100 * 0.0035 * 20)^{\frac{1}{3}} * 1000 * 283.5 = 79350.9 \text{ N} = \mathbf{99.8 \text{ kN}}$$

$$V_{Rd,c} > V_{Ed} \text{ (ok)}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 99.8 \rightarrow p = \mathbf{27 \text{ kN/m}}$$

$$\text{Skjærtrykkapasitet: } V_{Rd,max} = 0.5 * b_w * d * v * f_{cd}$$

$$v = 0.6 * (1 - \frac{f_{ck}}{250}) = 0.6 * (1 - \frac{20}{250}) = 0.552 \quad \text{Sørensen (4.51)}$$

$$V_{Rd,max} = 0.5 * 1000 * 283.5 * 0.552 * 11.3 = 884179.8 \text{ N} = \mathbf{884 \text{ kN}}$$

$$V_{Rd,max} > V_{Ed}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 884 \rightarrow p = \mathbf{288 \text{ kN/m}}$$

Momentkapasitet:

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174$$

$$\alpha_b = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668 \quad \text{Sørensen (4.20)}$$

$$\lambda = 0.8 \quad \text{EC2-3.1.7 (3)}$$

$$\eta = 1.0 \quad \text{EC2-3.1.7 (3)}$$

$$A_{s,b} = \lambda \eta * \frac{f_{cd}}{f_{yd}} * b * d * \alpha_b = 0.8 * 1.0 * \frac{11.3}{347.8} * 1000 * 283.5 * 0.668 = 4922 \text{ mm}^2 \quad \text{Sørensen (4.21)}$$

$$\rightarrow A_s < A_{s,b}$$

$$\lambda * \eta * f_{cd} * b * d * \alpha - f_{yd} * A_s = 0 \quad \text{Sørensen (4.19)}$$

$$\rightarrow \alpha = \frac{f_{yd} * A_s}{\lambda * \eta * f_{cd} * b * d} = \frac{347.8 * 995.5}{0.8 * 1.0 * 11.3 * 1000 * 283.5} = 0.135$$

$$\varepsilon_s = \frac{1 - \alpha}{\alpha} * \varepsilon_{cu} = \frac{1 - 0.135}{0.135} * 0.0035 = 0.0224$$

$$\rightarrow \varepsilon_s < \varepsilon_{ud} = 0.03 \quad \text{EC2- Tabell NA.3.5 (901)}$$

$$M_{Rd} = \lambda \eta \alpha * (1 - 0.5 * \lambda \alpha) * f_{cd} * b * d^2 \quad \text{Sørensen (4.14)}$$

$$= 0.8 * 1.0 * 0.135 * (1 - 0.5 * 0.8 * 0.135) * 11.3 * 1000 * 283.5^2$$

$$= 92789634 \text{ Nmm} = \mathbf{92.7 \text{ kNm}}$$

$$M_{Ed} = \frac{[1.2(g_1 + g_2) + 1.5 \cdot p] * L^2}{24} = \frac{(1.2 * 7.5 + 1.5 * 7.5) * 4^2}{24} = \mathbf{13.5 \text{ kNm}}$$

$$M_{Rd} > M_{Ed} \text{ OK.}$$

$$\text{Max nyttelast : } \frac{(7.5 * 1.2 + p * 1.5) * 4^2}{24} = 92.7 \rightarrow p = \mathbf{86.7 \text{ kN/m}}$$

Aksialkraftkapasitet:

$$A_c = b * h = 1000 * 300 = 300000 \text{ mm}^2$$

$$N_{Rd} = f_{cd} (A_c - A_s) + f_{yd} * A_s \quad \text{Sørensen (4.5)}$$

$$= 11.3 * (300000 - 995.5) + 347.8 * 995.5 = 3724985.75 \text{ N} = \mathbf{3725 \text{ kN}}$$

Nedbøyning:

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_s = 200000 \text{ N/mm}^2$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{995.5}{1000 \cdot 283.5} = 0.0035$$

$$\eta \rho = 6.667 \cdot 0.0035 = 0.023$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.023^2 + 2 \cdot 0.023} - 0.023 = 0.19$$

Sørensen (5.5)

$$I_s = A_s \cdot (1 - \alpha) \cdot \left(1 - \frac{\alpha}{3}\right) \cdot d^2 = 995.5 \cdot (1 - 0.19) \cdot \left(1 - \frac{0.19}{3}\right) \cdot 283.5^2 = 6.07 \cdot 10^7 \text{ mm}^4$$

Sørensen (5.11)

$$EI = E_s \cdot I_s = 200000 \cdot 6.07 \cdot 10^7 = 1.21 \cdot 10^{13} \text{ Nmm}^2$$

Sørensen (5.12)

$$q = 15 \text{ kN/m}$$

$$\text{Nedbøyning (bruksgrensetilstand)} : \delta_{II} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{15 \cdot 4000^4}{384 \cdot 1.21 \cdot 10^{13}} = \mathbf{0.83 \text{ mm}}$$

Langtidsnedbøyning:

permanent last:

$$g = 7.5 \cdot 1.2 = 9 \text{ kN/m}$$

$$p = 7.5 \cdot 1.5 = 11.25 \text{ kN/m (antar 100\% permanent)}$$

$$\text{lasttilfelle 1: } g = 9 \text{ kN/m, } \varphi(\infty, 3)$$

$$\text{lasttilfelle 2: } p = 11.25 \text{ kN/m, } \varphi(\infty, 28)$$

$$h_0 = \frac{2A_c}{u} = \frac{2 \cdot 300 \cdot 1000}{2 \cdot (300 + 1000)} = 231 \text{ mm}$$

Kryptall : utendørsforhold

EC2-Tillegg B

$$\varphi(t, t_0) = \varphi_0 \cdot \beta(t, t_0)$$

$$\varphi_0 = \varphi_{RH} \cdot \beta(f_{cm}) \cdot \beta(t_0)$$

$$RH = 80 \text{ (utendørsforhold)}$$

$$\varphi_{RH} = 1 + \frac{1 - \frac{RH}{100}}{0.1 \cdot \sqrt[3]{h_0}} = 1 + \frac{1 - \frac{80}{100}}{0.1 \cdot \sqrt[3]{231}} = 1.33$$

$$\beta(f_{cm}) = \frac{16.8}{\sqrt{f_{cm}}} = \frac{16.8}{\sqrt{28}} = 3.17$$

$$\beta(t_0) = \frac{1}{(0.1 + t_0^{0.20})}$$

$$\beta(3) = \frac{1}{(0.1 + 3^{0.20})} = 0.74$$

$$\beta(28) = \frac{1}{(0.1 + 28^{0.20})} = 0.49$$

$$\varphi_3 = 1.33 \cdot 3.17 \cdot 0.74 = 3.12$$

$$\varphi_{28} = 1.33 \cdot 3.17 \cdot 0.49 = 2.07$$

$$\beta(t, t_0) = \left[\frac{(t - t_0)}{(\beta_H + t - t_0)} \right]^{0.3}$$

$$\beta(\infty, 3) \rightarrow 1$$

$$\beta(\infty, 28) \rightarrow 1$$

$$\varphi(\infty, 3) = 4.96 \cdot 1 = 3.12$$

$$\varphi(\infty, 28) = 4.71 \cdot 1 = 2.07$$

$$E_{c1} = \frac{E_{cm}}{1 + \varphi(t, t_0)}$$

$$E_{c1} = \frac{30000}{1+3.12} = 7282 \text{ MPa}$$

$$E_{c2} = \frac{30000}{1+2.07} = 9772 \text{ MPa}$$

$$M_1 = \frac{q \cdot L^2}{24} = \frac{(9) \cdot 4^2}{24} = 6 \text{ kNm}$$

$$M_2 = \frac{q \cdot L^2}{24} = \frac{(11.25) \cdot 4^2}{24} = 7.5 \text{ kNm}$$

$$E_{c, \text{middle}} = \frac{\frac{M_1 + M_2}{\frac{M_1}{E_{c1}} + \frac{M_2}{E_{c2}}}}{\frac{6 + 7.5}{\frac{6}{7282} + \frac{7.5}{9772}}} = 8483 \text{ MPa}$$

$$\eta = \frac{E_s}{E_{c, \text{middle}}} = \frac{200000}{8483} = 23.6$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{995.5}{1000 \cdot 283.5} = 0.0035$$

$$\eta \rho = 23.6 \cdot 0.0035 = 0.083$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.083^2 + 2 \cdot 0.083} - 0.083 = 0.33$$

Sørensen (5.5)

$$I_c = 0.5 \cdot \alpha^2 \cdot (1 - \frac{\alpha}{3}) \cdot b \cdot d^3 = 0.5 \cdot 0.33^2 \cdot (1 - \frac{0.33}{3}) \cdot 1000 \cdot 283.5^3 = 1.10 \cdot 10^9 \text{ mm}^4$$

Sørensen (5.9)

$$EI = E_{c, \text{middle}} \cdot I_c = 8483 \cdot 1.10 \cdot 10^9 = 9.3 \cdot 10^{12} \text{ Nmm}^2$$

Sørensen (5.10)

Nedbøyning midt på bjelken:

$$\delta_{\text{Lang}} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{20.25 \cdot 4000^4}{384 \cdot 9.3 \cdot 10^{12}} = 1.45 \text{ mm}$$

Nedbøyning pga svinn:

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot \alpha_{ds1}) \cdot e^{\frac{(-\alpha_{ds2} \cdot f_{cm})}{f_{cm0}}}] \cdot 10^{-6} \cdot \beta_{RH}$$

Sørensen (5.27)

$$f_{cm0} = 10 \text{ MPa}$$

$$\alpha_{ds1} = 3$$

(Sement klasse S)

$$\alpha_{ds2} = 0.13$$

(Sement klasse S)

$$\beta_{RH} = 1.55 [1 - (\frac{RH}{RH_0})^3] = 1.55 [1 - (\frac{80}{100})^3] = 0.76$$

Sørensen (5.28)

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot 3) \cdot e^{\frac{(-0.13 \cdot 28)}{10}}] \cdot 10^{-6} \cdot 0.76 = 2.47 \cdot 10^{-4}$$

$$\epsilon_{cd}(t) = \beta_{ds}(t, t_s) \cdot k_h \cdot \epsilon_{cd,0}$$

Sørensen (5.29)

$$\beta_{ds}(t, t_s) = \frac{(t - t_s)}{(t - t_s) + 0.4 \sqrt{h_0^3}} : t \rightarrow \infty \rightarrow \beta_{ds} = 1$$

$$k_h = 0.78$$

EC2-Tabell 3.3

$$\epsilon_{cd}(\infty) = 1 \cdot 0.78 \cdot 2.47 \cdot 10^{-4} = 1.93 \cdot 10^{-4}$$

$$\epsilon_{ca}(\infty) = 2.5 (f_{ck} - 10) \cdot 10^{-6} = 2.5 (20 - 10) \cdot 10^{-6} = 2.5 \cdot 10^{-5}$$

Sørensen (5.31)

$$\epsilon_{cs} = \epsilon_{cd} + \epsilon_{ca} = 1.93 \cdot 10^{-4} + 2.5 \cdot 10^{-5} = 2.18 \cdot 10^{-4}$$

Sørensen (5.26)

Svinnkrumning:

$$K_s = \epsilon_{cs} * \eta * \frac{A_s * e}{I} \quad \text{Sørensen (s.135)}$$

$$\alpha d = \frac{A_c * 0.5h + \eta * A_s * d}{A_c + \eta * A_s} = \frac{300000 * 0.5 * 300 + 23.6 * 995.5 * 283.5}{300000 + 23.6 * 995.5} = 160$$

$$e = d - \alpha d = 283.5 - 160 = 123.5$$

$$I = \frac{b * h^3}{12} + b * h * \left(ad - \frac{h}{2}\right)^2 + \eta * A_s * e^2$$

$$= \frac{1000 * 300^3}{12} + 1000 * 300 * \left(160 - \frac{300}{2}\right)^2 + 23.6 * 995.5 * 123.5^2 = 26.38 * 10^8 \text{ mm}^4$$

$$K_s = 2.18 * 10^{-4} * 23.6 * \frac{995.5 * 123.5}{26.38 * 10^8} = 2.40 * 10^{-7} \text{ mm}^{-1}$$

$$\delta_{svinn} = \frac{K_s * L^2}{8} = \frac{2.40 * 10^{-7} * 4000^2}{8} = \mathbf{0.48 \text{ mm}}$$

$$\delta_{total} = \delta_{lang} + \delta_{svinn} = 1.45 + 0.48 = \mathbf{1.93 \text{ mm}}$$

$$\delta_{maks} = \frac{L}{250} = \frac{4000}{250} = 16 \text{ mm} > 1.93 \rightarrow \text{ok} \quad \text{EC2-7.4.1 (4)}$$

$$\text{Max nyttelast : } 16 = \frac{(7.5 * 1.2 + 1.5 * q) * 4000^4}{384 * 9.3 * 10^{12}} + 0.48 \rightarrow q = 138 \text{ kN/m}$$

Rissviddekontroll:

$$k_c = c_{nom} / c_{min, dur} = 10 / 60 = 0.1667$$

$$w_{max} = 0.3 * k_c = 0.3 * 0.1667 = 0.05 \text{ mm} \quad \text{Sørensen (tabell 5.2)}$$

$$M = \frac{20.25 * 4^2}{24} = 13.5 \text{ kNm}$$

$$\sigma_s = E_s * \frac{M(1-\alpha)d}{EI} = 200000 * \frac{13.5 * 10^6 * (1-0.33) * 283.5}{9.3 * 10^{12}} = 55 \text{ MPa} \quad \text{Sørensen (5.55)}$$

$$k_t = 0.4 \text{ (langvarig last)}$$

$$f_{ct, eff} = f_{cmt} = 2.2 \text{ MPa} \quad \text{EC2-Tabell 3.1}$$

$$h_{c, eff} = \min \left\{ 2.5(h-d); \left(\frac{h-\alpha d}{3}\right); \frac{h}{2} \right\} = \min \left\{ 2.5(300-283.5); \left(\frac{300-0.33*283.5}{3}\right); \frac{300}{2} \right\} = 41.25$$

$$\rho_{p, eff} = \frac{A_s}{A_{c, eff}} = \frac{995.5}{1000 * 41.25} = 0.024 \quad \text{Sørensen (s.153)}$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{\sigma_s - k_t * \frac{f_{ct, eff}}{\rho_{p, eff}} * (1 + \eta \rho_{p, eff})}{E_s} \geq 0.6 * \frac{\sigma_s}{E_s} \quad \text{Sørensen (5.59)}$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{55 - 0.4 * \frac{2.2}{0.024} * (1 + 6.667 * 0.024)}{200000} = 6.23 * 10^{-5} \geq 0.6 * \frac{55}{200000} = 1.65 * 10^{-4}$$

$$C_{nom} = 10 \text{ mm}$$

$$5 * (C_{nom} + \frac{\emptyset}{2}) = 5 * (10 + \frac{13}{2}) = 82.5 < \text{senteravstand} = 300$$

$$S_{r, max} = 1.3 * (h - \alpha d) = 1.3 * (300 - 0.33 * 283.5) = 268.5 \quad \text{Sørensen (5.61)}$$

$$w_k = S_{r, max} * (\epsilon_{sm} - \epsilon_{cm}) = 268.4 * 1.65 * 10^{-4} = \mathbf{0.044} \quad \text{Sørensen (5.58)}$$

$$w_k < w_{max} = 0.05 \text{ (Rissviddekrav oppfylt)}$$

Max nyttelast:

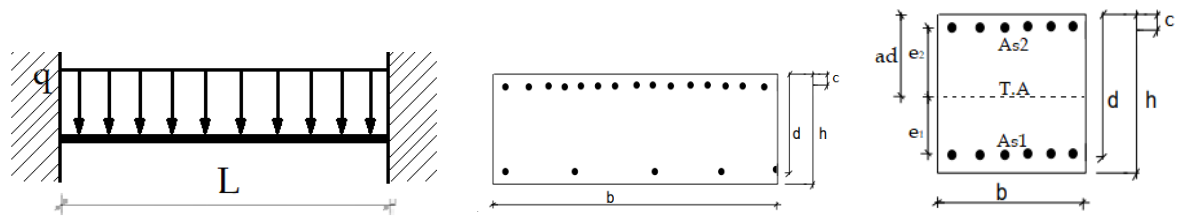
$$0.6 * \frac{\sigma_s}{200000} * 268.5 = 0.05 \rightarrow \sigma_s = 62$$

$$200000 * \frac{M * 10^6 * (1 - 0.33) * 283.5}{9.3 * 10^{12}} = 62 \rightarrow M = 15.1$$

$$\frac{(1.2 * 7.5 + 1.5 * q) * 4^2}{24} = 15.1 \rightarrow q = 9.1$$

Vedlegg D.3: Snitt 3

Snitt 3:



Sikkerhets faktor

$$\gamma_c = 1.5$$

$$\gamma_s = 1.15$$

$$\alpha_{cc} = 0.85$$

$$\gamma_G = 1.2$$

$$\gamma_Q = 1.5$$

EC2-Tabell 2.1N

EC2-Tabell 2.1N

EC2- NA.3.1.6(1)

EC - Tabell NA.A1.2(A)

EC - Tabell NA.A1.2(A)

Last:

$$p = 7.5 \text{ kN/m}^2 * 1\text{m} = 7.5 \text{ kN/m}$$

(EC1-Tabell 6.4)

$$g_1 = 0$$

$$g_2 = 25\text{kN/m}^3 * 0.3\text{m} * 1\text{m} = 7.5 \text{ kN/m}$$

$$q_{Ed} = \gamma_G * g + \gamma_Q * p = 1.2 * 7.5 + 1.5 * 7.5 = 20.25 \text{ kN/m} \quad (\text{betongelementboka s304})$$

Geometri:

$$h = 300 \text{ mm}$$

$$b = 1000 \text{ mm}$$

$$d = 300 - 10 - \frac{13}{2} = 283.5 \text{ mm}$$

$$c = 10 + \frac{13}{2} = 16.5 \text{ mm}$$

$$h' = h - 2 * c = 267$$

$$L = 4000 \text{ mm}$$

Betong: B300 (V413 tabell 2.1.2-1)

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_{cd} = \alpha_{cc} \frac{f_{ck}}{\gamma_c} = 11.3 \text{ N/mm}^2$$

$$f_{cm} = 28 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$f_{ctm} = 2.2 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

Standard armering:

$$f_{yk} = 400 \text{ N/mm}^2$$

V413 Tabell 2.1.2-2

$$f_{yd} = \frac{f_{yk}}{\gamma_s} = 347.8 \text{ N/mm}^2$$

$$E_s = 200000 \text{ N/mm}^2$$

EC2- 3.2.7(4)

Betong styrke ved: $t = 3$ dager

EC2-3.1.2

$s = 0.38$ For sement klasse S

$$\beta_{cc}(3) = \exp\left(s\left(1 - \left(\frac{28}{t}\right)^{0.5}\right)\right) = 0.458$$

$$f_{cm}(3) = \beta_{cc}(3) f_{cm} = 12.8 \text{ N/mm}^2$$

$$f_{ck}(3) = f_{cm}(3) - 8 \text{ MPa} = 4.8 \text{ N/mm}^2$$

$$f_{cd}(3) = \alpha_{cc} \frac{f_{ck}(3)}{\gamma_c} = 2.72 \text{ N/mm}^2$$

EC2-3.1.6

Minimums armering: (EC2-9.2.1.1)

$$A_{s,min} = \max \left\{ 0.26 \frac{f_{ctm}}{f_{yk}} b_t d; 0.0013 b_t d \right\} =$$

$$\max \left\{ 0.26 \frac{2.2}{400} * 1000 * 283.5; 0.0013 * 1000 * 283.5 \right\} = 405.4 \text{ mm}^2$$

$$\text{Antall jern} = \frac{56 \text{ jern}}{3.7m} = 15$$

$$A_s = \pi \left(\frac{13}{2}\right)^2 * 15 = 1991 \text{ mm}^2$$

$$A_{s1} = A_s * 25\% = 497.75 \text{ mm}^2$$

$$A_{s2} = A_s * 75\% = 1493.25 \text{ mm}^2$$

Minste overdekning: (EC2-4.4.1.2 og NA)

$$c_{min,b} = 13 \text{ mm}$$

$$c_{min,dur} = 60 \text{ mm}$$

EC2-Tabell NA.4.4N

$$\Delta c_{dur,\gamma} = 0$$

$$\Delta c_{dur,st} = \text{ikke gjeldende}$$

$$\Delta c_{dur,add} = \text{ikke gjeldende}$$

$$c_{min} = \max\{c_{min,b}; c_{min,dur} + \Delta c_{dur,\gamma} - \Delta c_{dur,st} - \Delta c_{dur,add}; 10\text{mm}\} = 60 \text{ mm}$$

Nominell overdekning:

(EC2-4.4.1.1(2))

$$c_{nom} = c_{min} + \Delta c_{dev} = 60 + 10 = 70 \text{ mm}$$

Faktisk overdekning = 10mm

$$c_{nom} = 10\text{mm}$$

Kapasitetskontroll (M-N diagram)

$$\alpha d = \frac{A_c * 0.5h + \eta * A_s * d}{A_c + \eta * A_s} = \frac{300000 * 0.5 * 300 + 23.6 * (1493.25 - 497.75) * 283.5}{300000 + 23.6 * (1493.25 - 497.75)} = 160 \rightarrow 140$$

$$e_2 = d - \alpha d = 283.5 - 160 = 123.5 \text{ (avstand } A_{s2} \text{ til T.A)}$$

$$e_1 = h - e_2 = 267 - 123.5 = 143.5 \text{ (avstand } A_{s1} \text{ til T.A)}$$

Punkt 1: Rent trykk

$$\varepsilon_c = \varepsilon_{c3} = 0.00175$$

EC2-Tabell 3.1

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174 < \varepsilon_{c3} \rightarrow \text{armeringen flyter}$$

$$T_c = f_{cd} * b * h = 11.3 * 1000 * 300 = 3390000 \text{ N} = 3390 \text{ kN}$$

$$S_1 = \frac{f_{yk}}{\gamma_s} * A_{s1} = f_{yd} * A_{s1} = 347.8 * 497.75 = 173117.45 \text{ N} = 173 \text{ kN}$$

$$S_2 = \frac{f_{yk}}{\gamma_s} * A_{s2} = f_{yd} * A_{s2} = 347.8 * 1493.25 = 519352.35 \text{ N} = 519 \text{ kN}$$

$$\text{Aksiell likevekt: } N_1 = T_c + S_1 + S_2 = 3390 + 173 + 519 = \mathbf{4082 \text{ kN}}$$

$$\begin{aligned} \text{Momentlikevekt: } M_1 &= T_c * (\alpha d - 0.5h) + S_2 * e_2 - S_1 * e_1 \\ &= 3390 * (140 - 300/2) + 519 * 123.5 - 173 * 143.5 = \mathbf{5.4} \end{aligned}$$

Punkt 2: Trykkbrudd i betong

Betong svikter samtidig som stål gir etter

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{s1} = c * \varepsilon_{cu} / h = 16.5 * 0.0035 / 300 = 0.00019 < \varepsilon_{yd} \rightarrow \text{ikke flyting}$$

$$\sigma_{sd} = E_s * \varepsilon_{s1} = 200000 * 0.00019 = 38 \text{ N/mm}^2$$

$$T_c = f_{cd} * b * 0.8h = 11.3 * 1000 * 0.8 * 300 = 2712000 \text{ N} = 2712 \text{ kN}$$

$$S_1 = \sigma_{sd} * A_{s1} = 38 * 497.75 = 18914.5 \text{ N} = 19 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 1493.25 = 519352 \text{ N} = 519 \text{ kN}$$

$$\text{Aksiell likevekt: } N_2 = T_c + S_1 + S_2 = 2712 + 19 + 519 = \mathbf{3250 \text{ kN}}$$

$$\text{Momentlikevekt: } M_2 = T_c * (\alpha d - 0.4h) + S_2 * e_2 - S_1 * e_1 =$$

$$3250 * (140 - 0.4 * 300) + 519 * 123.5 - 19 * 143.5 = \mathbf{126 \text{ kNm}}$$

Punkt 3: Trykkbrudd i betong samtidig med flytning i armering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_s = \varepsilon_{yd}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668$$

$$\alpha d_2 = 0.668 * 283.5 = 189.4 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{189.4 - 16.5}{189.4} * 0.0035 = 0.0032 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 189.4 = 1712176 \text{ N} = 1712 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 497.75 = 173117.45 \text{ N} = 173 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 1493.25 = 519352.35 \text{ N} = 519 \text{ kN}$$

$$\text{Aksiell likevekt : } N_3 = T_c + S_2 - S_1 = 1712 + 519 - 173 = \mathbf{2058 \text{ kN}}$$

$$\begin{aligned} \text{Momentlikevekt : } M_3 &= T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e_1 + S_2 * e_2 = \\ 1712 * (140 - 0.4 * 189.4) &+ 173 * 143.5 + 519 * 123.5 = \mathbf{199 \text{ kNm}} \end{aligned}$$

Punkt 4: Trykkbrudd i betong og dobbel flytetøyning i strekkarmering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 2\varepsilon_{yk}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 2\varepsilon_{yk}} = \frac{0.0035}{0.0035 + 2 * 0.002} = 0.467$$

Sørensen (4.22)

$$\alpha d_2 = 0.467 * 283.5 = 132.4 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{132.4 - 16.5}{132.4} * 0.0035 = 0.003 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 132.4 = 1196896 \text{ N} = 1196.9 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 497.75 = 173117.45 \text{ N} = 173 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 1493.25 = 519352.35 \text{ N} = 519 \text{ kN}$$

$$\text{Aksiell likevekt : } N_4 = T_c + S_2 - S_1 = 1196.9 + 519 - 173 = \mathbf{1543 \text{ kN}}$$

$$\begin{aligned} \text{Momentlikevekt : } M_4 &= T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e_1 + S_2 * e_2 = \\ 1196.9 * (140 - 0.4 * 132.4) &+ 173 * 143.5 + 519 * 123.5 = \mathbf{193 \text{ kNm}} \end{aligned}$$

Punkt 5: Trykkbrudd i betong og stor armeringstøyning

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 0.015$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 0.015} = \frac{0.0035}{0.0035 + 0.015} = 0.189$$

Sørensen (4.22)

$$\alpha d_2 = 0.189 * 283.5 = 53.6 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{53.6 - 16.5}{53.6} * 0.0035 = 0.0024 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 53.6 = 484544 \text{ N} = 485 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 497.75 = 173117.45 \text{ N} = 173 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 1493.25 = 519352.35 \text{ N} = 519 \text{ kN}$$

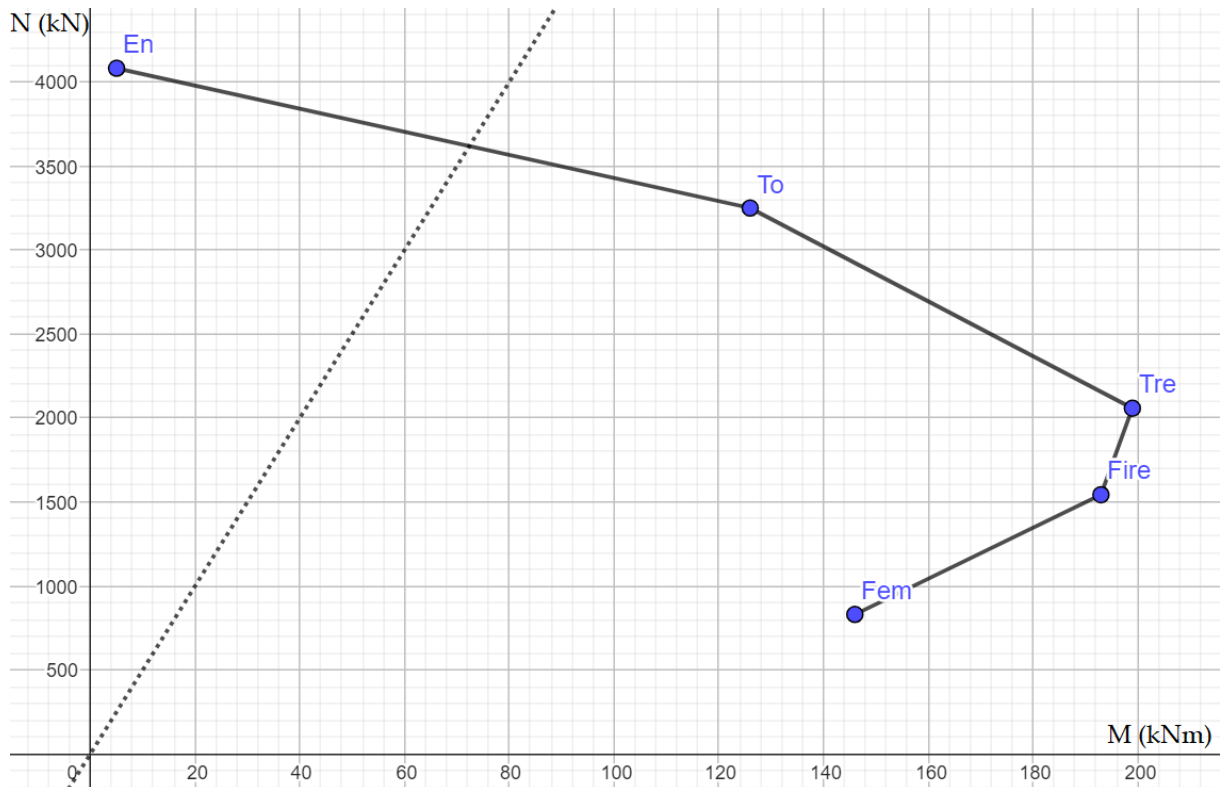
$$\text{Aksiell likevekt : } N_5 = T_c + S_2 - S_1 = 484 + 519 - 173 = \mathbf{830 \text{ kN}}$$

$$\begin{aligned} \text{Momentlikevekt : } M_5 &= T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * h' / 2 + S_2 * h' / 2 = \\ &= 485 * (140 - 0.4 * 53.6) + 173 * 143.5 + 519 * 123.5 = \mathbf{146 \text{ kNm}} \end{aligned}$$

$$e_0 = \max \{h/30, 20\text{mm}\} = 20\text{mm}$$

EC2-6.1 (4)

Resulterende interaksjonsdiagram:



Skjærkapasitet:

$$\text{Dimensjonerende skjærkraft: } V_{Ed} = \frac{q_{Ed} * L}{2} = \frac{20.25 * 4}{2} = 40.5 \text{ kN}$$

$$\text{Skjærstrekkapasitet: } V_{Rd,c} = C_{Rd,c} * K * (100 * P_L * f_{ck})^{\frac{1}{3}} * b_w * d \quad \text{Sørensen (4.43)}$$

$$K = 1 + \sqrt{\frac{200}{d}} \leq 2.0$$

$$= 1 + \sqrt{\frac{200}{283.5}} = 1.84$$

$$P_L = \frac{A_{sL}}{b_w * d} \leq 0.02$$

$$= \frac{497.75}{1000 * 283.5} = 0.00176$$

$$K_2 = 0.15 \quad \text{EC2-NA.6.2.2 (1)}$$

$$C_{Rd,c} = \frac{K_2}{\gamma_c} = \frac{0.15}{1.5} = 0.1$$

$$V_{Rd,c} = 0.1 * 1.84 * (100 * 0.00176 * 20)^{\frac{1}{3}} * 1000 * 283.5 = 79350.9 \text{ N} = \mathbf{79.3 \text{ kN}}$$

$$V_{Rd,c} > V_{Ed}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 79.3 \rightarrow p = \mathbf{20.4 \text{ kN/m}}$$

$$\text{Skjærtrykkkapasitet: } V_{Rd,max} = 0.5 * b_w * d * v * f_{cd}$$

$$v = 0.6 * \left(1 - \frac{f_{ck}}{250}\right) = 0.6 * \left(1 - \frac{20}{250}\right) = 0.552 \quad \text{Sørensen (4.51)}$$

$$V_{Rd,max} = 0.5 * 1000 * 283.5 * 0.552 * 11.3 = 884179.8 \text{ N} = \mathbf{884 \text{ kN}}$$

$$V_{Rd,max} > V_{Ed}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 884 \rightarrow p = \mathbf{288 \text{ kN/m}}$$

Momentkapasitet:

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174$$

$$\alpha_b = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668 \quad \text{Sørensen (4.20)}$$

$$\lambda = 0.8 \quad \text{EC2-3.1.7 (3)}$$

$$\eta = 1.0 \quad \text{EC2-3.1.7 (3)}$$

$$A_{s,b} = \lambda \eta * \frac{f_{cd}}{f_{yd}} * b * d * \alpha_b = 0.8 * 1.0 * \frac{11.3}{347.8} * 1000 * 283.5 * 0.668 = 4922 \text{ mm}^2 \quad \text{Sørensen (4.21)}$$

$$\rightarrow A_s < A_{s,b}$$

$$\lambda * \eta * f_{cd} * b * d * \alpha - f_{yd} * A_s = 0 \quad \text{Sørensen (4.19)}$$

$$\rightarrow \alpha = \frac{f_{yd} * A_s}{\lambda * \eta * f_{cd} * b * d} = \frac{347.8 * 1991}{0.8 * 1.0 * 11.3 * 1000 * 283.5} = 0.270$$

$$\varepsilon_s = \frac{1 - \alpha}{\alpha} * \varepsilon_{cu} = \frac{1 - 0.27}{0.27} * 0.0035 = 0.0095$$

$$\rightarrow \varepsilon_s < \varepsilon_{ud} = 0.03 \quad \text{EC2- Tabell NA.3.5 (901)}$$

$$M_{Rd} = \lambda \eta \alpha * (1 - 0.5 * \lambda \alpha) * f_{cd} * b * d^2 \quad \text{Sørensen (4.14)}$$

$$= 0.8 * 1.0 * 0.27 * (1 - 0.5 * 0.8 * 0.27) * 11.3 * 1000 * 283.5^2$$

$$= 174985948.3 \text{ Nmm} = \mathbf{175 \text{ kNm}}$$

$$M_{Ed} = \frac{[1.2(g_1 + g_2) + 1.5 \cdot p] * L^2}{12} = \frac{(1.2 * 7.5 + 1.5 * 7.5) * 4^2}{12} = \mathbf{27 \text{ kNm}}$$

$$M_{Rd} > M_{Ed} \text{ OK.}$$

$$\text{Max nyttelast : } \frac{(7.5 * 1.2 + p * 1.5) * 4^2}{12} = 175 \rightarrow p = \mathbf{81.5 \text{ kN/m}}$$

Aksialkraftkapasitet:

$$A_c = b * h = 1000 * 300 = 300000 \text{ mm}^2$$

$$N_{Rd} = f_{cd} (A_c - A_s) + f_{yd} * A_s \quad \text{Sørensen (4.5)}$$

$$= 11.3 * (300000 - 1991) + 347.8 * 1991 = 4059971.5 \text{ N} = \mathbf{4060 \text{ kN}}$$

Nedbøyning:

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_s = 200000 \text{ N/mm}^2$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{1991}{1000 \cdot 283.5} = 0.007$$

$$\eta\rho = 6.667 \cdot 0.007 = 0.047$$

$$\alpha = \sqrt{(\eta\rho)^2 + 2\eta\rho} - \eta\rho = \sqrt{0.047^2 + 2 \cdot 0.047} - 0.047 = 0.26$$

Sørensen (5.5)

$$I_s = A_s \cdot (1-\alpha) \cdot \left(1 - \frac{\alpha}{3}\right) \cdot d^2 = 1991 \cdot (1-0.26) \cdot \left(1 - \frac{0.26}{3}\right) \cdot 283.5^2 = 10.8 \cdot 10^7 \text{ mm}^4$$

Sørensen (5.11)

$$EI = E_s \cdot I_s = 200000 \cdot 10.8 \cdot 10^7 = 2.16 \cdot 10^{13} \text{ Nmm}^2$$

Sørensen (5.12)

$$q = 15 \text{ kN/m}$$

$$\text{Nedbøyning (bruksgrensetilstand)} : \delta_{II} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{15 \cdot 4000^4}{384 \cdot 2.16 \cdot 10^{13}} = \mathbf{0.46 \text{ mm}}$$

Langtidsnedbøyning:

permanent last:

$$g = 7.5 \cdot 1.2 = 9 \text{ kN/m}$$

$$p = 7.5 \cdot 1.5 = 11.25 \text{ kN/m (antar 100\% permanent)}$$

lasttilfelle 1: $g = 9 \text{ kN/m}$, $\varphi(\infty, 3)$ lasttilfelle 2 : $p = 11.25 \text{ kN/m}$, $\varphi(\infty, 28)$

$$h_0 = \frac{2A_c}{u} = \frac{2 \cdot 300 \cdot 1000}{2 \cdot (300 + 1000)} = 231 \text{ mm}$$

Kryptall : utendørsforhold

EC2-Tillegg B

$$\varphi(t, t_0) = \varphi_0 \cdot \beta(t, t_0)$$

$$\varphi_0 = \varphi_{RH} \cdot \beta(f_{cm}) \cdot \beta(t_0)$$

RH = 80 (utendørsforhold)

$$\varphi_{RH} = 1 + \frac{1 - \frac{RH}{100}}{0.1 \cdot \sqrt[3]{h_0}} = 1 + \frac{1 - \frac{80}{100}}{0.1 \cdot \sqrt[3]{231}} = 1.33$$

$$\beta(f_{cm}) = \frac{16.8}{\sqrt{f_{cm}}} = \frac{16.8}{\sqrt{28}} = 3.17$$

$$\beta(t_0) = \frac{1}{(0.1 + t_0^{0.20})}$$

$$\beta(3) = \frac{1}{(0.1 + 3^{0.20})} = 0.74$$

$$\beta(28) = \frac{1}{(0.1 + 28^{0.20})} = 0.49$$

$$\varphi_3 = 1.33 \cdot 3.17 \cdot 0.74 = 3.12$$

$$\varphi_{28} = 1.33 \cdot 3.17 \cdot 0.49 = 2.07$$

$$\beta(t, t_0) = \left[\frac{(t - t_0)}{(\beta_H + t - t_0)} \right]^{0.3}$$

$$\beta(\infty, 3) \rightarrow 1$$

$$\beta(\infty, 28) \rightarrow 1$$

$$\varphi(\infty, 3) = 4.96 \cdot 1 = 3.12$$

$$\varphi(\infty, 28) = 4.71 \cdot 1 = 2.07$$

$$E_{c1} = \frac{E_{cm}}{1 + \varphi(t, t_0)}$$

$$E_{c1} = \frac{30000}{1+3.12} = 7282 \text{ MPa}$$

$$E_{c2} = \frac{30000}{1+2.07} = 9772 \text{ MPa}$$

$$M_1 = \frac{q \cdot L^2}{12} = \frac{(9) \cdot 4^2}{12} = 12 \text{ kNm}$$

$$M_2 = \frac{q \cdot L^2}{12} = \frac{(11.25) \cdot 4^2}{12} = 15 \text{ kNm}$$

$$E_{c, \text{middle}} = \frac{\frac{M_1 + M_2}{\frac{M_1}{E_{c1}} + \frac{M_2}{E_{c2}}}}{\frac{12+15}{\frac{12}{7282} + \frac{15}{9772}}} = 8483 \text{ MPa}$$

$$\eta = \frac{E_s}{E_{c, \text{middel}}} = \frac{200000}{8483} = 23.6$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{1995}{1000 \cdot 283.5} = 0.007$$

$$\eta \rho = 23.6 \cdot 0.007 = 0.165$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.165^2 + 2 \cdot 0.165} - 0.165 = 0.43$$

Sørensen (5.5)

$$I_c = 0.5 \cdot \alpha^2 \cdot (1 - \frac{\alpha}{3}) \cdot b \cdot d^3 = 0.5 \cdot 0.43^2 \cdot (1 - \frac{0.43}{3}) \cdot 1000 \cdot 283.5^3 = 1.80 \cdot 10^9 \text{ mm}^4$$

Sørensen (5.9)

$$EI = E_{c, \text{middel}} \cdot I_c = 8483 \cdot 1.80 \cdot 10^9 = 1.5 \cdot 10^{13} \text{ Nmm}^2$$

Sørensen (5.10)

Nedbøyning midt på bjelken:

$$\delta_{\text{Lang}} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{20.25 \cdot 4000^4}{384 \cdot 1.5 \cdot 10^{13}} = 0.9 \text{ mm}$$

Nedbøyning pga svinn:

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot \alpha_{ds1}) \cdot e^{\frac{(-\alpha_{ds2} \cdot f_{cm})}{f_{cm0}}}] \cdot 10^{-6} \cdot \beta_{RH}$$

Sørensen (5.27)

$$f_{cm0} = 10 \text{ MPa}$$

$$\alpha_{ds1} = 3$$

(Sement klasse S)

$$\alpha_{ds2} = 0.13$$

(Sement klasse S)

$$\beta_{RH} = 1.55 [1 - (\frac{RH}{RH_0})^3] = 1.55 [1 - (\frac{80}{100})^3] = 0.76$$

Sørensen (5.28)

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot 3) \cdot e^{\frac{(-0.13 \cdot 28)}{10}}] \cdot 10^{-6} \cdot 0.76 = 2.47 \cdot 10^{-4}$$

$$\epsilon_{cd}(t) = \beta_{ds}(t, t_s) \cdot k_h \cdot \epsilon_{cd,0}$$

Sørensen (5.29)

$$\beta_{ds}(t, t_s) = \frac{(t - t_s)}{(t - t_s) + 0.4 \sqrt{h_0^3}} : t \rightarrow \infty \rightarrow \beta_{ds} = 1$$

$$k_h = 0.78$$

EC2-Tabell 3.3

$$\epsilon_{cd}(\infty) = 1 \cdot 0.78 \cdot 2.47 \cdot 10^{-4} = 1.93 \cdot 10^{-4}$$

$$\epsilon_{ca}(\infty) = 2.5 (f_{ck} - 10) \cdot 10^{-6} = 2.5 (20 - 10) \cdot 10^{-6} = 2.5 \cdot 10^{-5}$$

Sørensen (5.31)

$$\epsilon_{cs} = \epsilon_{cd} + \epsilon_{ca} = 1.93 \cdot 10^{-4} + 2.5 \cdot 10^{-5} = 2.18 \cdot 10^{-4}$$

Sørensen (5.26)

Svinnkrumning:

$$K_s = \epsilon_{cs} * \eta * \frac{A_s * e}{I} \quad \text{Sørensen (s.135)}$$

$$\alpha d = \frac{A_c * 0.5h + \eta * A_s * d}{A_c + \eta * A_s} = \frac{300000 * 0.5 * 300 + 23.6 * (1493.25 - 497.75) * 283.5}{300000 + 23.6 * (1493.25 - 497.75)} = 160 \rightarrow 140$$

$$e_2 = d - \alpha d = 283.5 - 160 = 123.5 \text{ (avstand } A_{s2} \text{ til T.A)}$$

$$e_1 = h - e_2 = 267 - 123.5 = 143.5 \text{ (avstand } A_{s1} \text{ til T.A)}$$

$$I = \frac{b * h^3}{12} + b * h * \left(ad - \frac{h}{2}\right)^2 + \eta * A_s * e^2$$

$$= \frac{1000 * 300^3}{12} + 1000 * 300 * \left(140 - \frac{300}{2}\right)^2 + 23.6 * 1493.25 * 123.5^2 + 23.6 * 497.75 * 143.5^2$$

$$= 30.6 * 10^8 \text{ mm}^4$$

$$K_s = 2.18 * 10^{-4} * 23.6 * \frac{1493.25 * 123.5 + 497.75 * 143.5}{30.6 * 10^8} = 4.3 * 10^{-7} \text{ mm}^{-1}$$

$$\delta_{svinn} = \frac{K_s * L^2}{8} = \frac{4.3 * 10^{-7} * 4000^2}{8} = \mathbf{0.86 \text{ mm}}$$

$$\delta_{total} = \delta_{lang} + \delta_{svinn} = 0.9 + 0.86 = \mathbf{1.76 \text{ mm}}$$

$$\delta_{maks} = \frac{L}{250} = \frac{4000}{250} = 16 \text{ mm} > \delta_{total} \rightarrow \text{ok} \quad \text{EC2-7.4.1 (4)}$$

$$\text{Max nyttelast : } 16 = \frac{(7.5 * 1.2 + 1.5 * q) * 4000^4}{384 * 1.5 * 10^{13}} + 0.86 \rightarrow q = 221 \text{ kN/m}$$

Rissviddekontroll:

$$k_c = c_{nom} / c_{min, dur} = 10 / 60 = 0.1667$$

$$w_{max} = 0.3 * k_c = 0.3 * 0.1667 = 0.05 \text{ mm} \quad \text{Sørensen (tabell 5.2)}$$

$$M = \frac{20.25 * 4^2}{12} = 27 \text{ kNm}$$

$$\sigma_s = E_s * \frac{M(1-\alpha)d}{EI} = 200000 * \frac{27 * 10^6 * (1-0.43) * 283.5}{1.5 * 10^{13}} = 58 \text{ MPa} \quad \text{Sørensen (5.55)}$$

$$k_t = 0.4 \text{ (langvarig last)}$$

$$f_{ct, eff} = f_{cmt} = 2.2 \text{ MPa} \quad \text{EC2-Tabell 3.1}$$

$$h_{c, eff} = \min \left\{ 2.5(h-d); \left(\frac{h-\alpha d}{3}\right); \frac{h}{2} \right\} = \min \left\{ 2.5(300-283.5); \left(\frac{300-0.33*283.5}{3}\right); \frac{300}{2} \right\} = 41.25$$

$$\rho_{p, eff} = \frac{A_s}{A_{c, eff}} = \frac{1991}{1000 * 41.25} = 0.048 \quad \text{Sørensen (s.153)}$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{\sigma_s - k_t * \frac{f_{ct, eff}}{\rho_{p, eff}} * (1 + \eta \rho_{p, eff})}{E_s} \geq 0.6 * \frac{\sigma_s}{E_s} \quad \text{Sørensen (5.59)}$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{58 - 0.4 * \frac{2.2}{0.048} * (1 + 6.667 * 0.048)}{200000} = 1.69 * 10^{-4} \geq 0.6 * \frac{58}{200000} = 1.74 * 10^{-4}$$

$$C_{nom} = 10 \text{ mm}$$

$$5 * (C_{nom} + \frac{\emptyset}{2}) = 5 * (10 + \frac{13}{2}) = 82.5 < \text{senteravstand} = 300$$

$$S_{r, max} = 1.3 * (h - \alpha d) = 1.3 * (300 - 0.43 * 283.5) = 231.5 \quad \text{Sørensen (5.61)}$$

$$w_k = S_{r, max} * (\epsilon_{sm} - \epsilon_{cm}) = 231.5 * 1.74 * 10^{-4} = \mathbf{0.04} \quad \text{Sørensen (5.58)}$$

$$w_k < w_{max} = 0.05 \text{ (Rissviddekrav oppfylt)}$$

Max Nyttelast :

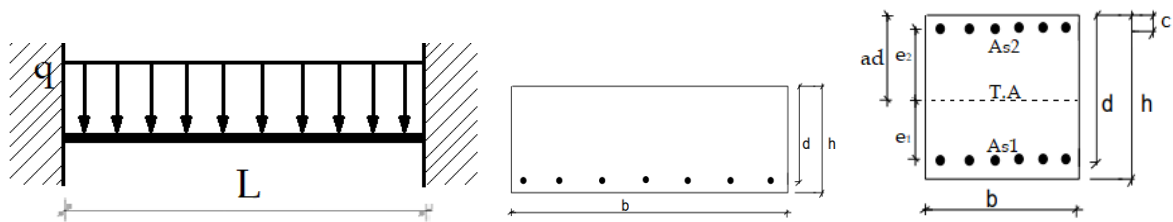
$$0.6 * \frac{\sigma_s}{200000} * 231.5 = 0.05 \rightarrow \sigma_s = 71.9$$

$$200000 * \frac{M * 10^6 * (1 - 0.43) * 283.5}{1.5 * 10^{13}} = 71.9 \rightarrow M = 33.3$$

$$\frac{(1.2 * 7.5 + 1.5 * q) * 4^2}{12} = 33.3 \rightarrow q = 10$$

Vedlegg D.4: Snitt 4

Snitt 4:



Sikkerhets faktor

$\gamma_c = 1.5$

EC2-Tabell 2.1N

$$\gamma_s = 1.15$$

EC2-Tabell 2.1N

$$\alpha_{cc} = 0.85$$

EC2- NA.3.1.6(1)

$\gamma_G = 1.2$

EC - Tabell NA.A1.2(A)

$\gamma_Q = 1.5$

EC - Tabell NA.A1.2(A)

Last:

$$p = 7.5 \text{ kN/m}^2 * 1\text{m} = 7.5 \text{ kN/m}$$

(EC1-Tabell 6.4)

$$g_1 = 0$$

$$g_2 = 25 \text{ kN/m}^3 * 0,3 \text{ m} * 1 \text{ m} = 7.5 \text{ kN/m}$$

$$q_{Ed} = \gamma_G * g + \gamma_Q * p = 1.2 * 7.5 + 1.5 * 7.5 = 20.25 \text{ kN/m}$$

(betongelementboka s304)

Geometri:

$$h = 300 \text{ mm}$$

$$b = 1000 \text{ mm}$$

$$d = 300 - 10 - 13 - \frac{13}{2} = 270.5 \text{ mm}$$

$$c = 10 + 13 + \frac{13}{2} = 29.5\text{mm}$$

$$h' = h - 2 * c = 241$$

$$L = 4000 \text{ mm}$$

Betong: B300 (V413 tabell 2.1.2-1)

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_{cd} = \alpha_{cc} \frac{f_{ck}}{\gamma_c} = 11.3 \text{ N/mm}^2$$

$$f_{cm} = 28 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$f_{ctm} = 2.2 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

Standard armering:

$$f_{yk} = 400 \text{ N/mm}^2$$

V413 Tabell 2.1.2-2

$$f_{yd} = \frac{f_{yk}}{\gamma_s} = 347.8 \text{ N/mm}^2$$

$$E_s = 200000 \text{ N/mm}^2$$

EC2- 3.2.7(4)

Betong styrke ved: $t = 3$ dager

EC2-3.1.2

$s = 0.38$ For sement klasse S

$$\beta_{cc}(3) = \exp(s(1 - (\frac{28}{t})^{0.5})) = 0.458$$

$$f_{cm}(3) = \beta_{cc}(3) f_{cm} = 12.8 \text{ N/mm}^2$$

$$f_{ck}(3) = f_{cm}(3) - 8 \text{ MPa} = 4.8 \text{ N/mm}^2$$

$$f_{cd}(3) = \alpha_{cc} \frac{f_{ck}(3)}{\gamma_c} = 2.72 \text{ N/mm}^2$$

EC2-3.1.6

Minimums armering: (EC2-9.2.1.1)

$$A_{s,min} = \max \{ 0.26 \frac{f_{ctm}}{f_{yk}} b_t d; 0.0013 b_t d \} =$$

$$\max \{ 0.26 \frac{2.2}{400} * 1000 * 270.5; 0.0013 * 1000 * 270.5 \} = 386.8 \text{ mm}^2$$

$$\text{Antall jern} = \frac{6 \text{ jern}}{0.85m} = 7$$

$$A_s = \pi \left(\frac{13}{2} \right)^2 * 7 = 929 \text{ mm}^2$$

$$A_{s1} = A_s = 929 \text{ mm}^2$$

$$A_{s2} = 0 = 0 \text{ mm}^2$$

Minste overdekning: (EC2-4.4.1.2 og NA)

$$c_{min,b} = 13 \text{ mm}$$

$$c_{min,dur} = 60 \text{ mm}$$

EC2-Tabell NA.4.4N

$$\Delta c_{dur,\gamma} = 0$$

$$\Delta c_{dur,st} = \text{ikke gjeldende}$$

$$\Delta c_{dur,add} = \text{ikke gjeldende}$$

$$c_{min} = \max \{ c_{min,b}; c_{min,dur} + \Delta c_{dur,\gamma} - \Delta c_{dur,st} - \Delta c_{dur,add}; 10 \text{ mm} \} = 60 \text{ mm}$$

Nominell overdekning:

(EC2-4.4.1.1(2))

$$c_{nom} = c_{min} + \Delta c_{dev} = 60 + 10 = 70 \text{ mm}$$

Faktisk overdekning = 10mm

$$c_{nom} = 10 \text{ mm}$$

Kapasitetskontroll (M-N diagram)

$$\eta = \frac{E_s}{E_{c,middel}} = \frac{200000}{8483} = 23.6 \text{ (se langtidsnedbøyning)}$$
$$\alpha d = \frac{A_c * 0.5h + \eta * A_s * d}{A_c + \eta * A_s} = \frac{300000 * 0.5 * 300 + 23.6 * 929 * 270.5}{300000 + 23.6 * 929} = 158$$
$$e = d - \alpha d = 270.5 - 158 = 112.5$$

Punkt 1: Rent trykk

$$\varepsilon_c = \varepsilon_{c3} = 0.00175$$

EC2-Tabell 3.1

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174 < \varepsilon_{c3} \rightarrow \text{armeringen flyter}$$

$$T_c = f_{cd} * b * h = 11.3 * 1000 * 300 = 3390000 \text{ N} = 3390 \text{ kN}$$

$$S_1 = \frac{f_{yk}}{\gamma_s} * A_{s1} = f_{yd} * A_{s1} = 347.8 * 929 = 323106 \text{ N} = 323 \text{ kN}$$

$$S_2 = 0$$

$$\text{Aksiell likevekt: } N_1 = T_c + S_1 + S_2 = 3390 + 323 = \mathbf{3713 \text{ kN}}$$

$$\text{Momentlikevekt: } M_1 = T_c * (\alpha d - 0.5h) - S_1 * e$$

$$3390 * (158 - 150) - 323 * 112.5 = \mathbf{-92}$$

Punkt 2: Trykkbrudd i betong

Betong svikter samtidig som stål gir etter

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{s1} = c * \varepsilon_{cu} / h = 16.5 * 0.0035 / 300 = 0.00034 < \varepsilon_{yd} \rightarrow \text{ikke flyting}$$

$$\sigma_{sd} = E_s * \varepsilon_{s1} = 200000 * 0.00034 = 68 \text{ N/mm}^2$$

$$T_c = f_{cd} * b * 0.8h = 11.3 * 1000 * 0.8 * 300 = 2712000 \text{ N} = 2712 \text{ kN}$$

$$S_1 = \sigma_{sd} * A_{s1} = 68 * 929 = 63172 \text{ N} = 63 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 0 = 0 \text{ N} = 0 \text{ kN}$$

$$\text{Aksiell likevekt: } N_2 = T_c + S_1 + S_2 = 2712 + 63 = \mathbf{2775 \text{ kN}}$$

$$\text{Momentlikevekt: } M_2 = T_c * (\alpha d - 0.4h) + S_1 * e =$$

$$2712 * (158 - 0.4 * 300) - 63 * 112.5 = \mathbf{96 \text{ kNm}}$$

Punkt 3: Trykkbrudd i betong samtidig med flytning i armering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_s = \varepsilon_{yd}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668$$

$$\alpha d_2 = 0.668 * 270.5 = 180.7 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{180.7 - 29.5}{180.7} * 0.0035 = 0.003 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 180.7 = 1633528 \text{ N} = 1634 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 929 = 323106.2 \text{ N} = 323 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 0 = 0 \text{ N} = 0 \text{ kN}$$

$$\text{Aksiell likevekt : } N_3 = T_c + S_2 - S_1 = 1634 - 323 = \mathbf{1311 \text{ kN}}$$

$$\text{Momentlikevekt : } M_3 = T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e = \\ 1712 * (158 - 0.4 * 180.7) + 323 * 112.5 = \mathbf{183 \text{ kNm}}$$

Punkt 4: Trykkbrudd i betong og dobbel flytetøyning i strekkarmering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 2\varepsilon_{yk}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 2\varepsilon_{yk}} = \frac{0.0035}{0.0035 + 2 * 0.002} = 0.467$$

Sørensen (4.22)

$$\alpha d_2 = 0.467 * 270.5 = 126.3 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{126.3 - 29.5}{126.3} * 0.0035 = 0.0027 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 126.3 = 1141752 \text{ N} = 1142 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 929 = 323106.2 \text{ N} = 323 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 0 = 0 \text{ N} = 0 \text{ kN}$$

$$\text{Aksiell likevekt : } N_4 = T_c + S_2 - S_1 = 1142 - 323 = \mathbf{819 \text{ kN}}$$

$$\text{Momentlikevekt : } M_4 = T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e = \\ 1142 * (158 - 0.4 * 126.3) + 323 * 112.5 = \mathbf{159 \text{ kNm}}$$

Punkt 5: Trykkbrudd i betong og stor armeringstøying

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 0.015$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 0.015} = \frac{0.0035}{0.0035 + 0.015} = 0.189$$

Sørensen (4.22)

$$\alpha d_2 = 0.189 * 270.5 = 51 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{51 - 29.5}{51} * 0.0035 = 0.0015 \text{ (flyter)}$$

$$\sigma_{sd} = E_s * \varepsilon_{s1} = 200000 * 0.0015 = 300 \text{ N/mm}^2$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 51 = 461040 \text{ N} = 461 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 929 = 323106.2 \text{ N} = 323 \text{ kN}$$

$$S_2 = \sigma_{sd} * A_{s2} = 300 * 0 = 0 \text{ N} = 0 \text{ kN}$$

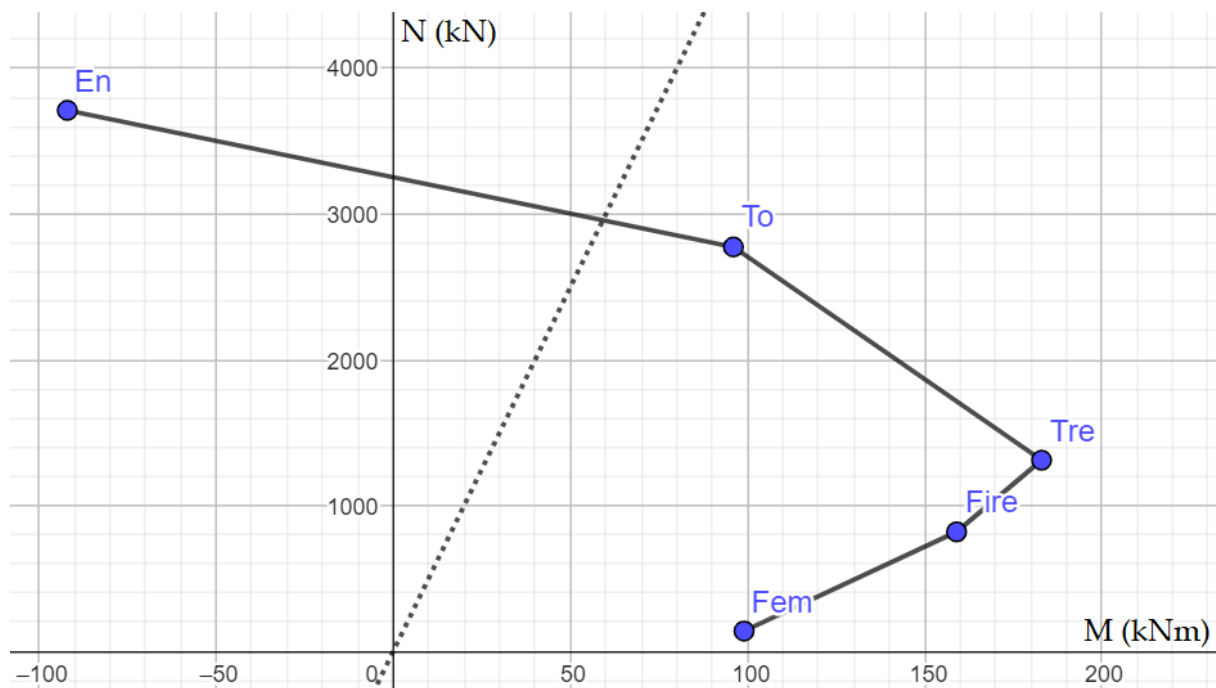
$$\text{Aksiell likevekt : } N_5 = T_c + S_2 - S_1 = 461 + 0 - 323 = \mathbf{138 \text{ kN}}$$

$$\text{Momentlikevekt : } M_5 = T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e = 461 * (158 - 0.4 * 53.6) + 323 * 112.5 = \mathbf{99 \text{ kNm}}$$

$$e_0 = \max \{h/30, 20\text{mm}\} = 20\text{mm}$$

EC2-6.1 (4)

Resulterende interaksjonsdiagram:



Skjærkapasitet:

$$\text{Dimensjonerende skjærkraft: } V_{Ed} = \frac{q_{Ed} * L}{2} = \frac{20.25 * 4}{2} = 40.5 \text{ kN}$$

$$\text{Skjærstrekkapasitet: } V_{Rd,c} = C_{Rd,c} * K * (100 * P_L * f_{ck})^{\frac{1}{3}} * b_w * d \quad \text{Sørensen (4.43)}$$

$$K = 1 + \sqrt{\frac{200}{d}} \leq 2.0$$

$$= 1 + \sqrt{\frac{200}{270.5}} = 1.86$$

$$P_L = \frac{A_{sL}}{b_w * d} \leq 0.02$$

$$= \frac{929}{1000 * 270.5} = 0.0034$$

$$K_2 = 0.15 \quad \text{EC2-NA.6.2.2 (1)}$$

$$C_{Rd,c} = \frac{K_2}{\gamma_c} = \frac{0.15}{1.5} = 0.1$$

$$V_{Rd,c} = 0.1 * 1.86 * (100 * 0.0034 * 20)^{\frac{1}{3}} * 1000 * 270.5 = 95319.8 \text{ N} = \mathbf{95.3 \text{ kN}}$$

$$V_{Rd,c} > V_{Ed} \text{ (ok)}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 95.3 \rightarrow p = \mathbf{25.7 \text{ kN/m}}$$

$$\text{Skjærtrykkapasitet: } V_{Rd,max} = 0.5 * b_w * d * v * f_{cd}$$

$$v = 0.6 * (1 - \frac{f_{ck}}{250}) = 0.6 * (1 - \frac{20}{250}) = 0.552 \quad \text{Sørensen (4.51)}$$

$$V_{Rd,max} = 0.5 * 1000 * 270.5 * 0.552 * 11.3 = 843635.4 \text{ N} = \mathbf{843 \text{ kN}}$$

$$V_{Rd,max} > V_{Ed}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 843 \rightarrow p = \mathbf{275 \text{ kN/m}}$$

Momentkapasitet:

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174$$

$$\alpha_b = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668 \quad \text{Sørensen (4.20)}$$

$$\lambda = 0.8 \quad \text{EC2-3.1.7 (3)}$$

$$\eta = 1.0 \quad \text{EC2-3.1.7 (3)}$$

$$A_{s,b} = \lambda \eta * \frac{f_{cd}}{f_{yd}} * b * d * \alpha_b = 0.8 * 1.0 * \frac{11.3}{347.8} * 1000 * 270.5 * 0.668 = 4697 \text{ mm}^2 \quad \text{Sørensen (4.21)}$$

$$\rightarrow A_s < A_{s,b}$$

$$\lambda * \eta * f_{cd} * b * d * \alpha - f_{yd} * A_s = 0 \quad \text{Sørensen (4.19)}$$

$$\rightarrow \alpha = \frac{f_{yd} * A_s}{\lambda * \eta * f_{cd} * b * d} = \frac{347.8 * 929}{0.8 * 1.0 * 11.3 * 1000 * 270.5} = 0.132$$

$$\varepsilon_s = \frac{1 - \alpha}{\alpha} * \varepsilon_{cu} = \frac{1 - 0.132}{0.132} * 0.0035 = 0.023$$

$$\rightarrow \varepsilon_s < \varepsilon_{ud} = 0.03 \quad \text{EC2- Tabell NA.3.5 (901)}$$

$$M_{Rd} = \lambda \eta \alpha * (1 - 0.5 * \lambda \alpha) * f_{cd} * b * d^2 \quad \text{Sørensen (4.14)}$$

$$= 0.8 * 1.0 * 0.132 * (1 - 0.5 * 0.8 * 0.132) * 11.3 * 1000 * 270.5^2$$

$$= 82702490.9 \text{ Nmm} = \mathbf{82.7 \text{ kNm}}$$

$$M_{Ed} = \frac{[1.2(g_1 + g_2) + 1.5 \cdot p] * L^2}{24} = \frac{(1.2 * 7.5 + 1.5 * 7.5) * 4^2}{24} = \mathbf{13.5 \text{ kNm}}$$

$$M_{Rd} > M_{Ed} \text{ OK.}$$

$$\text{Max nyttelast : } \frac{(7.5 * 1.2 + p * 1.5) * 4^2}{24} = 82.7 \rightarrow p = \mathbf{76.7 \text{ kN/m}}$$

Aksialkraftkapasitet:

$$A_c = b * h = 1000 * 300 = 300000 \text{ mm}^2$$

$$N_{Rd} = f_{cd} (A_c - A_s) + f_{yd} * A_s \quad \text{Sørensen (4.5)}$$

$$= 11.3 * (300000 - 929) + 347.8 * 929 = 3702608.5 \text{ N} = \mathbf{3703 \text{ kN}}$$

Nedbøyning:

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_s = 200000 \text{ N/mm}^2$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{929}{1000 \cdot 270.5} = 0.0034$$

$$\eta\rho = 6.667 \cdot 0.0034 = 0.023$$

$$\alpha = \sqrt{(\eta\rho)^2 + 2\eta\rho} - \eta\rho = \sqrt{0.023^2 + 2 \cdot 0.023} - 0.023 = 0.21$$

Sørensen (5.5)

$$I_s = A_s \cdot (1-\alpha) \cdot \left(1 - \frac{\alpha}{3}\right) \cdot d^2 = 929 \cdot (1-0.21) \cdot \left(1 - \frac{0.21}{3}\right) \cdot 270.5^2 = 4.99 \cdot 10^7 \text{ mm}^4$$

Sørensen (5.11)

$$EI = E_s \cdot I_s = 200000 \cdot 4.99 \cdot 10^7 = 9.98 \cdot 10^{12} \text{ Nmm}^2$$

Sørensen (5.12)

$$q = 15 \text{ kN/m}$$

$$\text{Nedbøyning (bruksgrensetilstand)} : \delta_{II} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{15 \cdot 4000^4}{384 \cdot 9.98 \cdot 10^{12}} = \mathbf{1.00 \text{ mm}}$$

Langtidsnedbøyning:

permanent last:

$$g = 7.5 \cdot 1.2 = 9 \text{ kN/m}$$

$$p = 7.5 \cdot 1.5 = 11.25 \text{ kN/m (antar 100\% permanent)}$$

$$\text{lasttilfelle 1: } g = 9 \text{ kN/m, } \varphi(\infty, 3)$$

$$\text{lasttilfelle 2: } p = 11.25 \text{ kN/m, } \varphi(\infty, 28)$$

$$h_0 = \frac{2A_c}{u} = \frac{2 \cdot 300 \cdot 1000}{2 \cdot (300 + 1000)} = 231 \text{ mm}$$

Kryptall : utendørsforhold

EC2-Tillegg B

$$\varphi(t, t_0) = \varphi_0 \cdot \beta(t, t_0)$$

$$\varphi_0 = \varphi_{RH} \cdot \beta(f_{cm}) \cdot \beta(t_0)$$

$$RH = 80 \text{ (utendørsforhold)}$$

$$\varphi_{RH} = 1 + \frac{1 - \frac{RH}{100}}{0.1 \cdot \sqrt[3]{h_0}} = 1 + \frac{1 - \frac{80}{100}}{0.1 \cdot \sqrt[3]{231}} = 1.33$$

$$\beta(f_{cm}) = \frac{16.8}{\sqrt{f_{cm}}} = \frac{16.8}{\sqrt{28}} = 3.17$$

$$\beta(t_0) = \frac{1}{(0.1 + t_0^{0.20})}$$

$$\beta(3) = \frac{1}{(0.1 + 3^{0.20})} = 0.74$$

$$\beta(28) = \frac{1}{(0.1 + 28^{0.20})} = 0.49$$

$$\varphi_3 = 1.33 \cdot 3.17 \cdot 0.74 = 3.12$$

$$\varphi_{28} = 1.33 \cdot 3.17 \cdot 0.49 = 2.07$$

$$\beta(t, t_0) = \left[\frac{(t - t_0)}{(\beta_H + t - t_0)} \right]^{0.3}$$

$$\beta(\infty, 3) \rightarrow 1$$

$$\beta(\infty, 28) \rightarrow 1$$

$$\varphi(\infty, 3) = 4.96 \cdot 1 = 3.12$$

$$\varphi(\infty, 28) = 4.71 \cdot 1 = 2.07$$

$$E_{c1} = \frac{E_{cm}}{1 + \varphi(t, t_0)}$$

$$E_{c1} = \frac{30000}{1+3.12} = 7282 \text{ MPa}$$

$$E_{c2} = \frac{30000}{1+2.07} = 9772 \text{ MPa}$$

$$M_1 = \frac{q \cdot L^2}{24} = \frac{(9) \cdot 4^2}{24} = 6 \text{ kNm}$$

$$M_2 = \frac{q \cdot L^2}{24} = \frac{(11.25) \cdot 4^2}{24} = 7.5 \text{ kNm}$$

$$E_{c, \text{middle}} = \frac{\frac{M_1 + M_2}{\frac{M_1}{E_{c1}} + \frac{M_2}{E_{c2}}}}{\frac{6 + 7.5}{\frac{6}{7282} + \frac{7.5}{9772}}} = 8483 \text{ MPa}$$

$$\eta = \frac{E_s}{E_{c, \text{middle}}} = \frac{200000}{8483} = 23.6$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{929}{1000 \cdot 270.5} = 0.0034$$

$$\eta \rho = 23.6 \cdot 0.0034 = 0.08$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.08^2 + 2 \cdot 0.08} - 0.08 = 0.33$$

Sørensen (5.5)

$$I_c = 0.5 \cdot \alpha^2 \cdot (1 - \frac{\alpha}{3}) \cdot b \cdot d^3 = 0.5 \cdot 0.33^2 \cdot (1 - \frac{0.33}{3}) \cdot 1000 \cdot 270.5^3 = 9.59 \cdot 10^8 \text{ mm}^4$$

Sørensen (5.9)

$$EI = E_{c, \text{middle}} \cdot I_c = 8483 \cdot 9.59 \cdot 10^8 = 8.1 \cdot 10^{12} \text{ Nmm}^2$$

Sørensen (5.10)

Nedbøyning midt på bjelken:

$$\delta_{\text{Lang}} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{20.25 \cdot 4000^4}{384 \cdot 8.1 \cdot 10^{12}} = 1.67 \text{ mm}$$

Nedbøyning pga svinn:

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot \alpha_{ds1}) \cdot e^{\frac{(-\alpha_{ds2} \cdot f_{cm})}{f_{cm0}}}] \cdot 10^{-6} \cdot \beta_{RH}$$

Sørensen (5.27)

$$f_{cm0} = 10 \text{ MPa}$$

$$\alpha_{ds1} = 3$$

(Sement klasse S)

$$\alpha_{ds2} = 0.13$$

(Sement klasse S)

$$\beta_{RH} = 1.55 [1 - (\frac{RH}{RH_0})^3] = 1.55 [1 - (\frac{80}{100})^3] = 0.76$$

Sørensen (5.28)

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot 3) \cdot e^{\frac{(-0.13 \cdot 28)}{10}}] \cdot 10^{-6} \cdot 0.76 = 2.47 \cdot 10^{-4}$$

$$\epsilon_{cd}(t) = \beta_{ds}(t, t_s) \cdot k_h \cdot \epsilon_{cd,0}$$

Sørensen (5.29)

$$\beta_{ds}(t, t_s) = \frac{(t - t_s)}{(t - t_s) + 0.4 \sqrt{h_0^3}} : t \rightarrow \infty \rightarrow \beta_{ds} = 1$$

$$k_h = 0.78$$

EC2-Tabell 3.3

$$\epsilon_{cd}(\infty) = 1 \cdot 0.78 \cdot 2.47 \cdot 10^{-4} = 1.93 \cdot 10^{-4}$$

$$\epsilon_{ca}(\infty) = 2.5 (f_{ck} - 10) \cdot 10^{-6} = 2.5 (20 - 10) \cdot 10^{-6} = 2.5 \cdot 10^{-5}$$

Sørensen (5.31)

$$\epsilon_{cs} = \epsilon_{cd} + \epsilon_{ca} = 1.93 \cdot 10^{-4} + 2.5 \cdot 10^{-5} = 2.18 \cdot 10^{-4}$$

Sørensen (5.26)

Svinnkrumning:

$$K_s = \epsilon_{cs} * \eta * \frac{A_s * e}{I} \quad \text{Sørensen (s.135)}$$

$$\alpha d = \frac{A_c * 0.5h + \eta * A_s * d}{A_c + \eta * A_s} = \frac{300000 * 0.5 * 300 + 23.6 * 929 * 270.5}{300000 + 23.6 * 929} = 158$$

$$e = d - \alpha d = 270.5 - 158 = 112.5$$

$$I = \frac{b * h^3}{12} + b * h * \left(ad - \frac{h}{2}\right)^2 + \eta * A_s * e^2$$

$$= \frac{1000 * 300^3}{12} + 1000 * 300 * \left(158 - \frac{300}{2}\right)^2 + 23.6 * 929 * 112.5^2 = 25.5 * 10^8 \text{ mm}^4$$

$$K_s = 2.18 * 10^{-4} * 23.6 * \frac{929 * 112.5}{25.5 * 10^8} = 2.1 * 10^{-7} \text{ mm}^{-1}$$

$$\delta_{svinn} = \frac{K_s * L^2}{8} = \frac{2.1 * 10^{-7} * 4000^2}{8} = \mathbf{0.42 \text{ mm}}$$

$$\delta_{total} = \delta_{lang} + \delta_{svinn} = 1.67 + 0.42 = \mathbf{2.09 \text{ mm}}$$

$$\delta_{maks} = \frac{L}{250} = \frac{4000}{250} = 16 \text{ mm} > \delta_{total} \rightarrow \text{ok} \quad \text{EC2-7.4.1 (4)}$$

$$\text{Max nyttelast : } 16 = \frac{(7.5 * 1.2 + 1.5 * q) * 4000^4}{384 * 8.1 * 10^{12}} + 0.42 \rightarrow q = 120 \text{ kN/m}$$

Rissviddekontroll:

$$k_c = c_{nom} / c_{min, dur} = 10 / 60 = 0.1667$$

$$w_{max} = 0.3 * k_c = 0.3 * 0.1667 = 0.05 \text{ mm} \quad \text{Sørensen (tabell 5.2)}$$

$$M = \frac{20.25 * 4^2}{24} = 13.5 \text{ kNm}$$

$$\sigma_s = E_s * \frac{M(1-\alpha)d}{EI} = 200000 * \frac{13.5 * 10^6 * (1-0.33) * 270.5}{8.1 * 10^{12}} = 60 \text{ MPa} \quad \text{Sørensen (5.55)}$$

$$k_t = 0.4 \text{ (langvarig last)}$$

$$f_{ct, eff} = f_{cmt} = 2.2 \text{ MPa} \quad \text{EC2-Tabell 3.1}$$

$$h_{c, eff} = \min \left\{ 2.5(h-d); \left(\frac{h-\alpha d}{3}\right); \frac{h}{2} \right\} = \min \left\{ 2.5(300-270.5); \left(\frac{300-0.33*270.5}{3}\right); \frac{300}{2} \right\} = 70.25$$

$$\rho_{p, eff} = \frac{A_s}{A_{c, eff}} = \frac{929}{1000 * 70.25} = 0.013 \quad \text{Sørensen (s.153)}$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{\sigma_s - k_t * \frac{f_{ct, eff}}{\rho_{p, eff}} * (1 + \eta \rho_{p, eff})}{E_s} \geq 0.6 * \frac{\sigma_s}{E_s} \quad \text{Sørensen (5.59)}$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{60 - 0.4 * \frac{2.2}{0.013} * (1 + 6.667 * 0.013)}{200000} = 6.78 * 10^{-5} \geq 0.6 * \frac{60}{200000} = 1.8 * 10^{-4}$$

$$C_{nom} = 10 \text{ mm}$$

$$5 * (c_{nom} + \frac{\emptyset}{2}) = 5 * (10 + \frac{13}{2}) = 82.5 < \text{senteravstand} = 300$$

$$S_{r, max} = 1.3 * (h - \alpha d) = 1.3 * (300 - 0.33 * 270.5) = 274 \quad \text{Sørensen (5.61)}$$

$$w_k = S_{r, max} * (\epsilon_{sm} - \epsilon_{cm}) = 274 * 1.8 * 10^{-4} = \mathbf{0.049} \quad \text{Sørensen (5.58)}$$

$$w_k < w_{max} = 0.05 \text{ (Rissviddekrav oppfylt)}$$

Max nyttelast:

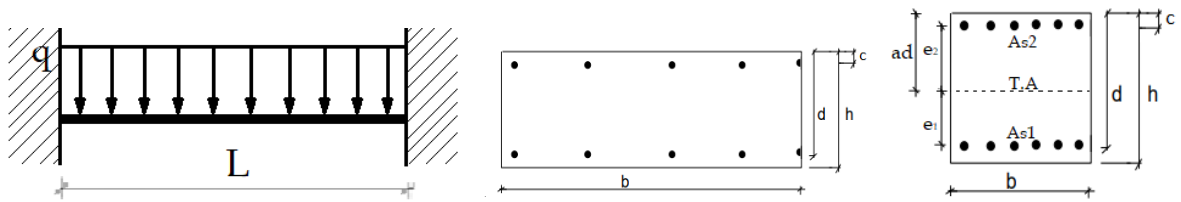
$$0.6 * \frac{\sigma_s}{200000} * 274 = 0.05 \rightarrow \sigma_s = 60.8$$

$$200000 * \frac{M * 10^6 * (1 - 0.33) * 270.5}{8.1 * 10^{12}} = 60.8 \rightarrow M = 13.5$$

$$\frac{20.25 * 4^2}{24} = 13.5 \text{ kNm} \rightarrow 7.5$$

Vedlegg D.5: Snitt 5

Snitt 5:



Sikkerhets faktor

$$\gamma_c = 1.5$$

$$\gamma_s = 1.15$$

$$\alpha_{cc} = 0.85$$

$$\gamma_G = 1.2$$

$$\gamma_Q = 1.5$$

EC2-Tabell 2.1N

EC2-Tabell 2.1N

EC2- NA.3.1.6(1)

EC - Tabell NA.A1.2(A)

EC - Tabell NA.A1.2(A)

Last:

$$p = 7.5 \text{ kN/m}^2 * 1\text{m} = 7.5 \text{ kN/m}$$

(EC1-Tabell 6.4)

$$g_1 = 0$$

$$g_2 = 25 \text{ kN/m}^3 * 0.3\text{m} * 1\text{m} = 7.5 \text{ kN/m}$$

$$q_{Ed} = \gamma_G * g + \gamma_Q * p = 1.2 * 7.5 + 1.5 * 7.5 = 20.25 \text{ kN/m} \quad (\text{betongelementboka s304})$$

Geometri:

$$h = 300 \text{ mm}$$

$$b = 1000 \text{ mm}$$

$$d = 300 - 10 - 13 - \frac{13}{2} = 270.5 \text{ mm}$$

$$c = 10 + 13 + \frac{13}{2} = 29.5 \text{ mm}$$

$$h' = h - 2 * c = 241$$

$$L = 4000 \text{ mm}$$

$$e = h' / 2 = 241 / 2 = 120.5$$

$$\alpha d = h / 2 = 300 / 2 = 150$$

Betong: B300 (V413 tabell 2.1.2-1)

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_{cd} = \alpha_{cc} \frac{f_{ck}}{\gamma_c} = 11.3 \text{ N/mm}^2$$

$$f_{cm} = 28 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$f_{ctm} = 2.2 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

Standard armering

$$f_{yk} = 400 \text{ N/mm}^2$$

V413 Tabell 2.1.2-2

$$f_{yd} = \frac{f_{yk}}{\gamma_s} = 347.8 \text{ N/mm}^2$$

$$E_s = 200000 \text{ N/mm}^2$$

EC2- 3.2.7(4)

Betong styrke ved: $t = 3$ dager

EC2-3.1.2

$s = 0.38$ For sement klasse S

$$\beta_{cc}(3) = \exp(s(1 - (\frac{28}{t})^{0.5})) = 0.458$$

$$f_{cm}(3) = \beta_{cc}(3) f_{cm} = 12.8 \text{ N/mm}^2$$

$$f_{ck}(3) = f_{cm}(3) - 8 \text{ MPa} = 4.8 \text{ N/mm}^2$$

$$f_{cd}(3) = \alpha_{cc} \frac{f_{ck}(3)}{\gamma_c} = 2.72 \text{ N/mm}^2$$

EC2-3.1.6

Minimums armering: (EC2-9.2.1.1)

$$A_{s,min} = \max \{ 0.26 \frac{f_{ctm}}{f_{yk}} b_t d; 0.0013 b_t d \} =$$

$$\max \{ 0.26 \frac{2.2}{400} * 1000 * 270.5; 0.0013 * 1000 * 270.5 \} = 386.8 \text{ mm}^2$$

$$\text{Antall jern} = \frac{6 \text{ jern}}{0.85m} = 7$$

$$A_s = \pi (\frac{13}{2})^2 * 7 = 929 \text{ mm}^2$$

$$A_{s1} = A_s / 2 = 464.5 \text{ mm}^2$$

$$A_{s2} = A_s / 2 = 464.5 \text{ mm}^2$$

Minste overdekning: (EC2-4.4.1.2 og NA)

$$c_{min,b} = 13 \text{ mm}$$

$$c_{min,dur} = 60 \text{ mm}$$

EC2-Tabell NA.4.4N

$$\Delta c_{dur,\gamma} = 0$$

$$\Delta c_{dur,st} = \text{ikke gjeldende}$$

$$\Delta c_{dur,add} = \text{ikke gjeldende}$$

$$c_{min} = \max \{ c_{min,b}; c_{min,dur} + \Delta c_{dur,\gamma} - \Delta c_{dur,st} - \Delta c_{dur,add}; 10 \text{ mm} \} = 60 \text{ mm}$$

Nominell overdekning:

(EC2-4.4.1.1(2))

$$c_{nom} = c_{min} + \Delta c_{dev} = 60 + 10 = 70 \text{ mm}$$

Faktisk overdekning = 10mm

$$c_{nom} = 10 \text{ mm}$$

Kapasitetskontroll (M-N diagram)

Punkt 1: Rent trykk

$$\varepsilon_c = \varepsilon_{c3} = 0.00175$$

EC2-Tabell 3.1

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174 < \varepsilon_{c3} \rightarrow \text{armeringen flyter}$$

$$T_c = f_{cd} * b * h = 11.3 * 1000 * 300 = 3390000 \text{ N} = 3390 \text{ kN}$$

$$S_1 = \frac{f_{yk}}{\gamma_s} * A_{s1} = f_{yd} * A_{s1} = 347.8 * 464.5 = 161553.1 \text{ N} = 162 \text{ kN}$$

$$S_2 = S_1$$

$$\text{Aksiell likevekt: } N_1 = T_c + S_1 + S_2 = 3390 + 162 + 162 = \mathbf{3714 \text{ kN}}$$

$$\text{Momentlikevekt: } M_1 = \mathbf{0}$$

Punkt 2: Trykkbrudd i betong

Betong svikter samtidig som stål gir etter

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{s1} = c * \varepsilon_{cu} / h = 29.5 * 0.0035 / 300 = 0.00034 < \varepsilon_{yd} \rightarrow \text{ikke flyting}$$

$$\sigma_{sd} = E_s * \varepsilon_{s1} = 200000 * 0.00034 = 68 \text{ N/mm}^2$$

$$T_c = f_{cd} * b * 0.8 * h = 11.3 * 1000 * 0.8 * 300 = 2712000 \text{ N} = 2712 \text{ kN}$$

$$S_1 = \sigma_{sd} * A_{s1} = 68 * 464.5 = 17651 \text{ N} = 31.6 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 464.5 = 161553.1 \text{ N} = 162 \text{ kN}$$

$$\text{Aksiell likevekt: } N_2 = T_c + S_1 + S_2 = 2712 + 31.6 + 173 = \mathbf{2916.6 \text{ kN}}$$

$$\text{Momentlikevekt: } M_2 = T_c * (0.5h - 0.4h) + S_2 * h / 2 - S_1 * h / 2 =$$

$$2712 * (0.5 * 0.300 - 0.4 * 0.300) + 162 * 0.241 / 2 - 31.6 * 0.241 / 2 = \mathbf{104.7 \text{ kNm}}$$

Punkt 3: Trykkbrudd i betong samtidig med flytning i armering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_s = \varepsilon_{yd}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668$$

$$\alpha d = 0.668 * 270.5 = 180.7 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{180.7 - 29.5}{180.7} * 0.0035 = 0.0029 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d = 11.3 * 1000 * 0.8 * 180.7 = 1633528 \text{ N} = 1634 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 464.5 = 161553.1 \text{ N} = 162 \text{ kN}$$

$$S_2 = S_1$$

$$\text{Aksiell likevekt : } N_3 = T_c + S_2 - S_1 = 1634 + 162 - 162 = \mathbf{1634 \text{ kN}}$$

$$\begin{aligned} \text{Momentlikevekt : } M_3 &= T_c * (0.5h - 0.4 \alpha d) + S_1 * h' = \\ 1634 * (0.5 * 300 - 0.4 * 180.7) + 162 * 241 &= \mathbf{166 \text{ kNm}} \end{aligned}$$

Punkt 4: Trykkbrudd i betong og dobbel flytetøyning i strekkarmering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 2\varepsilon_{yk}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 2\varepsilon_{yk}} = \frac{0.0035}{0.0035 + 2 * 0.002} = 0.467$$

Sørensen (4.22)

$$\alpha d = 0.467 * 270.5 = 126.3 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{126.3 - 29.5}{126.3} * 0.0035 = 0.0027 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d = 11.3 * 1000 * 0.8 * 126.3 = 1196896 \text{ N} = 1142 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 464.5 = 161553.1 \text{ N} = 162 \text{ kN}$$

$$S_2 = S_1$$

$$\text{Aksiell likevekt : } N_4 = T_c + S_2 - S_1 = 1142 + 162 - 162 = \mathbf{1142 \text{ kN}}$$

$$\begin{aligned} \text{Momentlikevekt : } M_4 &= T_c * (0.5h - 0.4 \alpha d) + S_1 * h' = \\ 1142 * (0.5 * 300 - 0.4 * 126.3) + 162 * 241 &= \mathbf{152.6 \text{ kNm}} \end{aligned}$$

Punkt 5: Trykkbrudd i betong og stor armeringstøying

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 0.015$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 0.015} = \frac{0.0035}{0.0035 + 0.015} = 0.189$$

Sørensen (4.22)

$$\alpha d = 0.189 * 270.5 = 51.1 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{51.1 - 29.5}{51.1} * 0.0035 = 0.0015 \text{ (flyter ikke)}$$

$$\sigma_{sd} = E_s * \varepsilon_{s2} = 200000 * 0.0015 = 300 \text{ N/mm}^2$$

$$T_c = f_{cd} * b * 0.8 * \alpha d = 11.3 * 1000 * 0.8 * 51.1 = 461944 \text{ N} = 462 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 464.5 = 161553.1 \text{ N} = 162 \text{ kN}$$

$$S_2 = \sigma_{sd} * A_{s2} = 300 * 464.5 = 139350 \text{ N} = 139 \text{ kN}$$

$$\text{Aksiell likevekt : } N_5 = T_c + S_2 - S_1 = 462 + 162 - 162 = \mathbf{462 \text{ kN}}$$

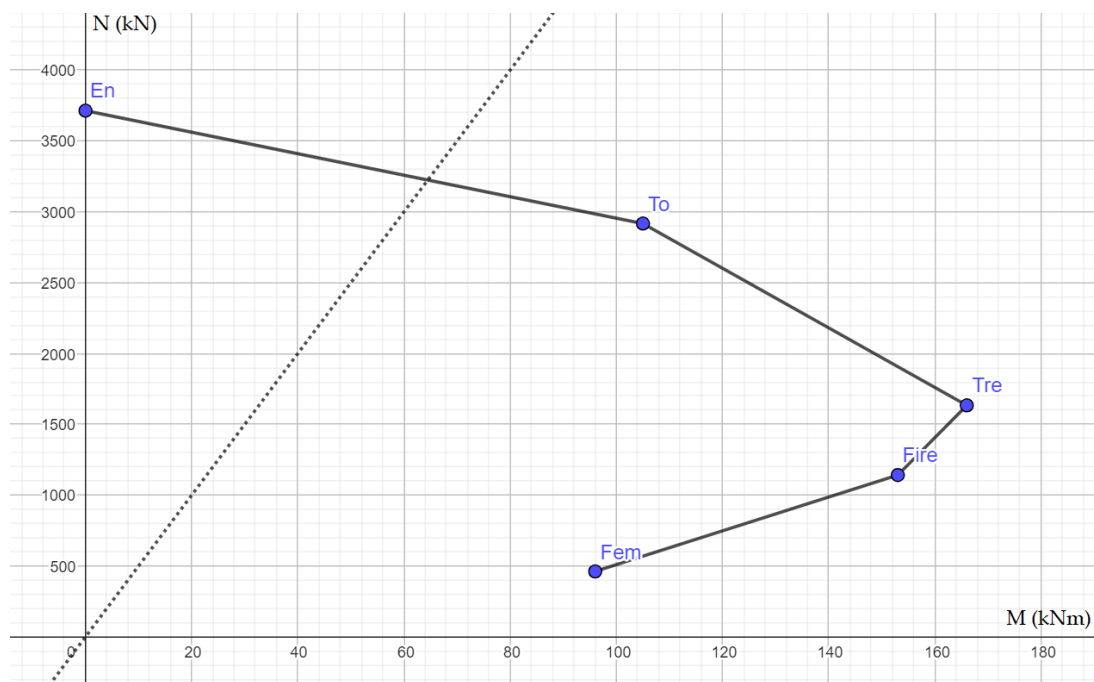
$$\text{Momentlikevekt : } M_5 = T_c * (0.5h - 0.4 \alpha d) + S_1 * h/2 + S_2 * h/2 =$$

$$462 * (0.5 * 300 - 0.4 * 51.1) + 162 * 241/2 + 139 * 241/2 = \mathbf{96 \text{ kNm}}$$

$$e_0 = \max \{h/30, 20\text{mm}\} = 20\text{mm}$$

EC2-6.1 (4)

Resulterende interaksjonsdiagram:



Skjærkapasitet:

$$\text{Dimensjonerende skjærkraft: } V_{Ed} = \frac{q_{Ed} * L}{2} = \frac{20.25 * 4}{2} = 40.5 \text{ kN}$$

$$\text{Skjærstrekkapasitet: } V_{Rd,c} = C_{Rd,c} * K * (100 * P_L * f_{ck})^{\frac{1}{3}} * b_w * d \quad \text{Sørensen (4.43)}$$

$$K = 1 + \sqrt{\frac{200}{d}} \leq 2.0$$

$$= 1 + \sqrt{\frac{200}{270.5}} = 1.86$$

$$P_L = \frac{A_{sL}}{b_w * d} \leq 0.02$$

$$= \frac{464.5}{1000 * 270.5} = 0.0017$$

$$K_2 = 0.15$$

EC2-NA.6.2.2 (1)

$$C_{Rd,c} = \frac{K_2}{\gamma_c} = \frac{0.15}{1.5} = 0.1$$

$$V_{Rd,c} = 0.1 * 1.86 * (100 * 0.0017 * 20)^{\frac{1}{3}} * 1000 * 270.5 = 75655.4 \text{ N} = \mathbf{75.7 \text{ kN}}$$

$$V_{Rd,c} > V_{Ed}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 75.7 \rightarrow p = \mathbf{19.2 \text{ kN/m}}$$

$$\text{Skjærtrykkapasitet: } V_{Rd,max} = 0.5 * b_w * d * v * f_{cd}$$

$$v = 0.6 * (1 - \frac{f_{ck}}{250}) = 0.6 * (1 - \frac{20}{250}) = 0.552$$

Sørensen (4.51)

$$V_{Rd,max} = 0.5 * 1000 * 270.5 * 0.552 * 11.3 = 843935.4 \text{ N} = \mathbf{844 \text{ kN}}$$

$$V_{Rd,max} > V_{Ed}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 844 \rightarrow p = \mathbf{275 \text{ kN/m}}$$

Momentkapasitet:

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174$$

$$\alpha_b = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668 \quad \text{Sørensen (4.20)}$$

$$\lambda = 0.8 \quad \text{EC2-3.1.7 (3)}$$

$$\eta = 1.0 \quad \text{EC2-3.1.7 (3)}$$

$$A_{s,b} = \lambda \eta * \frac{f_{cd}}{f_{yd}} * b * d * \alpha_b = 0.8 * 1.0 * \frac{11.3}{347.8} * 1000 * 270.5 * 0.668 = 4696.6 \text{ mm}^2 \quad \text{Sørensen (4.21)}$$

$$\rightarrow A_s < A_{s,b}$$

$$\lambda * \eta * f_{cd} * b * d * \alpha - f_{yd} * A_s = 0 \quad \text{Sørensen (4.19)}$$

$$\rightarrow \alpha = \frac{f_{yd} * A_s}{\lambda * \eta * f_{cd} * b * d} = \frac{347.8 * 929}{0.8 * 1.0 * 11.3 * 1000 * 270.5} = 0.132$$

$$\varepsilon_s = \frac{1 - \alpha}{\alpha} * \varepsilon_{cu} = \frac{1 - 0.132}{0.132} * 0.0035 = 0.0230$$

$$\rightarrow \varepsilon_s < \varepsilon_{ud} = 0.03 \quad \text{EC2- Tabell NA.3.5 (901)}$$

$$M_{Rd} = \lambda \eta \alpha * (1 - 0.5 * \lambda \alpha) * f_{cd} * b * d^2 \quad \text{Sørensen (4.14)}$$

$$= 0.8 * 1.0 * 0.132 * (1 - 0.5 * 0.8 * 0.132) * 11.3 * 1000 * 270.5^2$$

$$= 82702490.9 \text{ Nmm} = \mathbf{82.7 \text{ kNm}}$$

$$M_{Ed} = \frac{[1.2(g_1 + g_2) + 1.5 \cdot p] * L^2}{12} = \frac{(1.2 * 7.5 + 1.5 * 7.5) * 4^2}{12} = \mathbf{27 \text{ kNm}}$$

$$M_{Rd} > M_{Ed} \text{ OK.}$$

$$\text{Max nyttelast : } \frac{(7.5 * 1.2 + p * 1.5) * 4^2}{12} = 82.7 \rightarrow p = \mathbf{35.3 \text{ kN/m}}$$

Aksialkraftkapasitet:

$$A_c = b * h = 1000 * 300 = 300000 \text{ mm}^2$$

$$N_{Rd} = f_{cd} (A_c - A_s) + f_{yd} * A_s \quad \text{Sørensen (4.5)}$$

$$= 11.3 * (300000 - 929) + 347.8 * 929 = 3702608.5 \text{ N} = \mathbf{3703 \text{ kN}}$$

Nedbøyning:

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_s = 200000 \text{ N/mm}^2$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{929}{1000 \cdot 270.5} = 0.0034$$

$$\eta\rho = 6.667 \cdot 0.0034 = 0.023$$

$$\alpha = \sqrt{(\eta\rho)^2 + 2\eta\rho} - \eta\rho = \sqrt{0.023^2 + 2 \cdot 0.023} - 0.023 = 0.19$$

Sørensen (5.5)

$$I_s = A_s \cdot (1-\alpha) \cdot \left(1 - \frac{\alpha}{3}\right) \cdot d^2 = 929 \cdot (1-0.19) \cdot \left(1 - \frac{0.19}{3}\right) \cdot 270.5^2 = 5.16 \cdot 10^7 \text{ mm}^4$$

Sørensen (5.11)

$$EI = E_s \cdot I_s = 200000 \cdot 5.16 \cdot 10^7 = 1.03 \cdot 10^{13} \text{ Nmm}^2$$

Sørensen (5.12)

$$q = 15 \text{ kN/m}$$

$$\text{Nedbøyning (bruksgrensetilstand)} : \delta_{II} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{15 \cdot 4000^4}{384 \cdot 1.03 \cdot 10^{13}} = \mathbf{0.97 \text{ mm}}$$

Langtidsnedbøyning:

permanent last:

$$g = 7.5 \cdot 1.2 = 9 \text{ kN/m}$$

$$p = 7.5 \cdot 1.5 = 11.25 \text{ kN/m (antar 100\% permanent)}$$

$$\text{lasttilfelle 1: } g = 9 \text{ kN/m, } \varphi(\infty, 3)$$

$$\text{lasttilfelle 2: } p = 11.25 \text{ kN/m, } \varphi(\infty, 28)$$

$$h_0 = \frac{2A_c}{u} = \frac{2 \cdot 300 \cdot 1000}{2 \cdot (300 + 1000)} = 231 \text{ mm}$$

Kryptall : utendørsforhold

EC2-Tillegg B

$$\varphi(t, t_0) = \varphi_0 \cdot \beta(t, t_0)$$

$$\varphi_0 = \varphi_{RH} \cdot \beta(f_{cm}) \cdot \beta(t_0)$$

$$RH = 80 \text{ (utendørsforhold)}$$

$$\varphi_{RH} = 1 + \frac{1 - \frac{RH}{100}}{0.1 \cdot \sqrt[3]{h_0}} = 1 + \frac{1 - \frac{80}{100}}{0.1 \cdot \sqrt[3]{231}} = 1.33$$

$$\beta(f_{cm}) = \frac{16.8}{\sqrt{f_{cm}}} = \frac{16.8}{\sqrt{28}} = 3.17$$

$$\beta(t_0) = \frac{1}{(0.1 + t_0^{0.20})}$$

$$\beta(3) = \frac{1}{(0.1 + 3^{0.20})} = 0.74$$

$$\beta(28) = \frac{1}{(0.1 + 28^{0.20})} = 0.49$$

$$\varphi_3 = 1.33 \cdot 3.17 \cdot 0.74 = 3.12$$

$$\varphi_{28} = 1.33 \cdot 3.17 \cdot 0.49 = 2.07$$

$$\beta(t, t_0) = \left[\frac{(t - t_0)}{(\beta_H + t - t_0)} \right]^{0.3}$$

$$\beta(\infty, 3) \rightarrow 1$$

$$\beta(\infty, 28) \rightarrow 1$$

$$\varphi(\infty, 3) = 4.96 \cdot 1 = 3.12$$

$$\varphi(\infty, 28) = 4.71 \cdot 1 = 2.07$$

$$E_{c1} = \frac{E_{cm}}{1 + \varphi(t, t_0)}$$

$$E_{c1} = \frac{30000}{1+3.12} = 7282 \text{ MPa}$$

$$E_{c2} = \frac{30000}{1+2.07} = 9772 \text{ MPa}$$

$$M_1 = \frac{q \cdot L^2}{12} = \frac{(9) \cdot 4^2}{12} = 12 \text{ kNm}$$

$$M_2 = \frac{q \cdot L^2}{12} = \frac{(11.25) \cdot 4^2}{12} = 15 \text{ kNm}$$

$$E_{c, \text{middle}} = \frac{\frac{M_1 + M_2}{\frac{M_1}{E_{c1}} + \frac{M_2}{E_{c2}}}}{\frac{12+15}{\frac{12}{7282} + \frac{15}{9772}}} = 8483 \text{ MPa}$$

$$\eta = \frac{E_s}{E_{c, \text{middle}}} = \frac{200000}{8483} = 23.6$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{929}{1000 \cdot 270.5} = 0.0034$$

$$\eta \rho = 23.6 \cdot 0.0034 = 0.080$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.08^2 + 2 \cdot 0.08} - 0.08 = 0.33$$

Sørensen (5.5)

$$I_c = 0.5 \cdot \alpha^2 \cdot (1 - \frac{\alpha}{3}) \cdot b \cdot d^3 = 0.5 \cdot 0.33^2 \cdot (1 - \frac{0.33}{3}) \cdot 1000 \cdot 270.5^3 = 0.96 \cdot 10^9 \text{ mm}^4$$

Sørensen (5.9)

$$EI = E_{c, \text{middle}} \cdot I_c = 8483 \cdot 0.96 \cdot 10^9 = 8.1 \cdot 10^{12} \text{ Nmm}^2$$

Sørensen (5.10)

Nedbøyning midt på bjelken:

$$\delta_{\text{Lang}} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{20.25 \cdot 4000^4}{384 \cdot 8.1 \cdot 10^{12}} = 1.67 \text{ mm}$$

Nedbøyning pga svinn:

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot \alpha_{ds1}) \cdot e^{\frac{(-\alpha_{ds2} \cdot f_{cm})}{f_{cm0}}}] \cdot 10^{-6} \cdot \beta_{RH}$$

Sørensen (5.27)

$$f_{cm0} = 10 \text{ MPa}$$

$$\alpha_{ds1} = 3$$

(Sement klasse S)

$$\alpha_{ds2} = 0.13$$

(Sement klasse S)

$$\beta_{RH} = 1.55 [1 - (\frac{RH}{RH_0})^3] = 1.55 [1 - (\frac{80}{100})^3] = 0.76$$

Sørensen (5.28)

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot 3) \cdot e^{\frac{(-0.13 \cdot 28)}{10}}] \cdot 10^{-6} \cdot 0.76 = 2.47 \cdot 10^{-4}$$

$$\epsilon_{cd}(t) = \beta_{ds}(t, t_s) \cdot k_h \cdot \epsilon_{cd,0}$$

Sørensen (5.29)

$$\beta_{ds}(t, t_s) = \frac{(t - t_s)}{(t - t_s) + 0.4 \sqrt{h_0^3}} : t \rightarrow \infty \rightarrow \beta_{ds} = 1$$

$$k_h = 0.78$$

EC2-Tabell 3.3

$$\epsilon_{cd}(\infty) = 1 \cdot 0.78 \cdot 2.47 \cdot 10^{-4} = 1.93 \cdot 10^{-4}$$

$$\epsilon_{ca}(\infty) = 2.5 (f_{ck} - 10) \cdot 10^{-6} = 2.5 (20 - 10) \cdot 10^{-6} = 2.5 \cdot 10^{-5}$$

Sørensen (5.31)

$$\epsilon_{cs} = \epsilon_{cd} + \epsilon_{ca} = 1.93 \cdot 10^{-4} + 2.5 \cdot 10^{-5} = 2.18 \cdot 10^{-4}$$

Sørensen (5.26)

Svinnkrumning:

$$K_s = \epsilon_{cs} * \eta * \frac{A_s * e}{I}$$

Sørensen (s.135)

$$\alpha d = \frac{h}{2} = \frac{300}{2} = 150$$

$$e = d - \alpha d = 270.5 - 150 = 120.5$$

$$I = \frac{b * h^3}{12} + b * h * \left(\alpha d - \frac{h}{2} \right)^2 + \eta * A_s * e^2$$

$$= \frac{1000 * 300^3}{12} + 1000 * 300 * \left(150 - \frac{300}{2} \right)^2 + 23.6 * 929 * 120.5^2 = 25.68 * 10^8 \text{ mm}^4$$

$$K_s = 2.18 * 10^{-4} * 23.6 * \frac{929 * 120.5}{25.68 * 10^8} = 2.24 * 10^{-7} \text{ mm}^{-1}$$

$$\delta_{svinn} = \frac{K_s * L^2}{8} = \frac{2.24 * 10^{-7} * 4000^2}{8} = \mathbf{0.45 \text{ mm}}$$

$$\delta_{total} = \delta_{lang} + \delta_{svinn} = 1.67 + 0.45 = \mathbf{2.01 \text{ mm}}$$

$$\delta_{maks} = \frac{L}{250} = \frac{4000}{250} = 16 \text{ mm} > \delta_{total} \rightarrow \text{ok}$$

EC2-7.4.1 (4)

$$\text{Max nyttelast : } 16 = \frac{(7.5 * 1.2 + 1.5 * q) * 4000^4}{384 * 8.1 * 10^{12}} + 0.45 \rightarrow q = 119.9 \text{ kN/m}$$

Rissviddekontroll:

$$k_c = c_{nom} / c_{min, dur} = 10 / 60 = 0.1667$$

$$w_{max} = 0.3 * k_c = 0.3 * 0.1667 = 0.05 \text{ mm}$$

Sørensen (tabell 5.2)

$$M = \frac{20.25 * 4^2}{12} = 27 \text{ kNm}$$

$$\sigma_s = E_s * \frac{M(1-\alpha)d}{EI} = 200000 * \frac{27 * 10^6 * (1-0.33) * 270.5}{8.1 * 10^{12}} = 121 \text{ MPa}$$

Sørensen (5.55)

$$k_t = 0.4 \text{ (langvarig last)}$$

$$f_{ct, eff} = f_{cmt} = 2.2 \text{ MPa}$$

EC2-Tabell 3.1

$$h_{c, eff} = \min \left\{ 2.5(h-d); \left(\frac{h-\alpha d}{3} \right); \frac{h}{2} \right\} = \min \left\{ 2.5(300-270.5); \left(\frac{300-0.33*270.5}{3} \right); \frac{300}{2} \right\} = 70.25$$

$$\rho_{p, eff} = \frac{A_s}{A_{c, eff}} = \frac{929}{1000 * 70.25} = 0.013$$

Sørensen (s.153)

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{\sigma_s - k_t * \frac{f_{ct, eff}}{\rho_{p, eff}} * (1 + \eta \rho_{p, eff})}{E_s} \geq 0.6 * \frac{\sigma_s}{E_s}$$

Sørensen (5.59)

$$\epsilon_{sm} - \epsilon_{cm} = \frac{121 - 0.4 * \frac{2.2}{0.013} * (1 + 6.667 * 0.013)}{200000} = 2.37 * 10^{-4} \geq 0.6 * \frac{121}{200000} = 3.63 * 10^{-4}$$

$$C_{nom} = 10 \text{ mm}$$

$$5 * (C_{nom} + \frac{\emptyset}{2}) = 5 * (10 + \frac{13}{2}) = 82.5 < \text{senteravstand} = 300$$

$$S_{r, max} = 1.3 * (h - \alpha d) = 1.3 * (300 - 0.33 * 270.5) = 274$$

Sørensen (5.61)

$$w_k = S_{r, max} * (\epsilon_{sm} - \epsilon_{cm}) = 274 * 3.63 * 10^{-4} = \mathbf{0.10}$$

Sørensen (5.58)

$$w_k > w_{max} = 0.05 \text{ (Rissviddekrav ikke oppfylt)}$$

Max nyttelast :

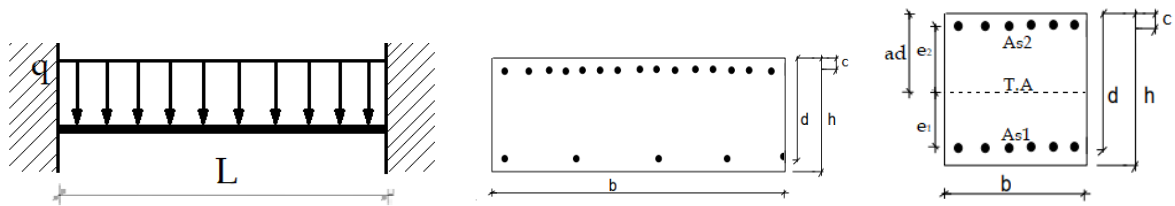
$$0.6 * \frac{\sigma_s}{200000} * 275 = 0.05 \rightarrow \sigma_s = 60.6$$

$$200000 * \frac{M * 10^6 * (1 - 0.33) * 270.5}{8.1 * 10^{12}} = 60.6 \rightarrow M = 13.5$$

$$\frac{(1.2 * 7.5 + 1.5 * q) * 4^2}{12} = 13.5 \rightarrow q = 0.75$$

Vedlegg D.6: Snitt 6

Snitt 6:



Sikkerhets faktor

$$\gamma_c = 1.5$$

$$\gamma_s = 1.15$$

$$\alpha_{cc} = 0.85$$

$$\gamma_G = 1.2$$

$$\gamma_Q = 1.5$$

EC2-Tabell 2.1N

EC2-Tabell 2.1N

EC2- NA.3.1.6(1)

EC - Tabell NA.A1.2(A)

EC - Tabell NA.A1.2(A)

Last:

$$p = 7.5 \text{ kN/m}^2 * 1\text{m} = 7.5 \text{ kN/m}$$

(EC1-Tabell 6.4)

$$g_1 = 0$$

$$g_2 = 25 \text{ kN/m}^3 * 0.3\text{m} * 1\text{m} = 7.5 \text{ kN/m}$$

$$q_{Ed} = \gamma_G * g + \gamma_Q * p = 1.2 * 7.5 + 1.5 * 7.5 = 20.25 \text{ kN/m} \quad (\text{betongelementboka s304})$$

Geometri:

$$h = 300 \text{ mm}$$

$$b = 1000 \text{ mm}$$

$$d = 300 - 10 - \frac{13}{2} = 283.5 \text{ mm}$$

$$c = 10 + \frac{13}{2} = 16.5 \text{ mm}$$

$$h' = h - 2 * c = 267$$

$$L = 4000 \text{ mm}$$

Betong: B300 (V413 tabell 2.1.2-1)

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_{cd} = \alpha_{cc} \frac{f_{ck}}{\gamma_c} = 11.3 \text{ N/mm}^2$$

$$f_{cm} = 28 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$f_{ctm} = 2.2 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

Standard armering:

$$f_{yk} = 400 \text{ N/mm}^2$$

V413 Tabell 2.1.2-2

$$f_{yd} = \frac{f_{yk}}{\gamma_s} = 347.8 \text{ N/mm}^2$$

$$E_s = 200000 \text{ N/mm}^2$$

EC2- 3.2.7(4)

Betong styrke ved: $t = 3$ dager

EC2-3.1.2

$s = 0.38$ For sement klasse S

$$\beta_{cc}(3) = \exp\left(s\left(1 - \left(\frac{28}{t}\right)^{0.5}\right)\right) = 0.458$$

$$f_{cm}(3) = \beta_{cc}(3) f_{cm} = 12.8 \text{ N/mm}^2$$

$$f_{ck}(3) = f_{cm}(3) - 8 \text{ MPa} = 4.8 \text{ N/mm}^2$$

$$f_{cd}(3) = \alpha_{cc} \frac{f_{ck}(3)}{\gamma_c} = 2.72 \text{ N/mm}^2$$

EC2-3.1.6

Minimums armering: (EC2-9.2.1.1)

$$A_{s,min} = \max \left\{ 0.26 \frac{f_{ctm}}{f_{yk}} b_t d; 0.0013 b_t d \right\} =$$

$$\max \left\{ 0.26 \frac{2.2}{400} * 1000 * 283.5; 0.0013 * 1000 * 283.5 \right\} = 405.4 \text{ mm}^2$$

$$\text{Antall jern} = \frac{42 \text{ jern}}{3.7m} = 11.35$$

$$A_s = \pi \left(\frac{13}{2}\right)^2 * 11.35 = 1506 \text{ mm}^2$$

$$A_{s1} = A_s * \frac{1}{3} = 502 \text{ mm}^2$$

$$A_{s2} = A_s * \frac{2}{3} = 1004 \text{ mm}^2$$

Minste overdekning: (EC2-4.4.1.2 og NA)

$$c_{min,b} = 13 \text{ mm}$$

$$c_{min,dur} = 60 \text{ mm}$$

EC2-Tabell NA.4.4N

$$\Delta c_{dur,\gamma} = 0$$

$$\Delta c_{dur,st} = \text{ikke gjeldende}$$

$$\Delta c_{dur,add} = \text{ikke gjeldende}$$

$$c_{min} = \max\{c_{min,b}; c_{min,dur} + \Delta c_{dur,\gamma} - \Delta c_{dur,st} - \Delta c_{dur,add}; 10\text{mm}\} = 60 \text{ mm}$$

Nominell overdekning:

(EC2-4.4.1.1(2))

$$c_{nom} = c_{min} + \Delta c_{dev} = 60 + 10 = 70 \text{ mm}$$

Faktisk overdekning = 10mm

$$c_{nom} = 10\text{mm}$$

Kapasitetskontroll (M-N diagram)

$$\eta = \frac{E_s}{E_{c,middel}} = \frac{200000}{8483} = 23.6 \text{ (fra Langtidsnedbøynig)}$$

$$\alpha d = \frac{A_c * 0.5h + \eta * A_s * d}{A_c + \eta * A_s} = \frac{300000 * 0.5 * 300 + 23.6 * (1004 - 502) * 283.5}{300000 + 23.6 * (1004 - 502)} = 155 \rightarrow 145$$

$$e_2 = d - \alpha d = 283.5 - 155 = 128.5 \text{ (avstand } A_{s2} \text{ til T.A)}$$

$$e_1 = h - e_2 = 267 - 128.5 = 138.5 \text{ (avstand } A_{s1} \text{ til T.A)}$$

Punkt 1: Rent trykk

$$\varepsilon_c = \varepsilon_{c3} = 0.00175$$

EC2-Tabell 3.1

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174 < \varepsilon_{c3} \rightarrow \text{armeringen flyter}$$

$$T_c = f_{cd} * b * h = 11.3 * 1000 * 300 = 3390000 \text{ N} = 3390 \text{ kN}$$

$$S_1 = \frac{f_{yk}}{\gamma_s} * A_{s1} = f_{yd} * A_{s1} = 347.8 * 502 = 175 \text{ kN}$$

$$S_2 = \frac{f_{yk}}{\gamma_s} * A_{s2} = f_{yd} * A_{s2} = 347.8 * 1004 = 349 \text{ kN}$$

$$\text{Aksiell likevekt: } N_1 = T_c + S_1 + S_2 = 3390 + 175 + 349 = \mathbf{3914 \text{ kN}}$$

$$\text{Momentlikevekt: } M_1 = T_c * (\alpha d - 0.5h) + S_2 * e_2 - S_1 * e_1$$

$$= 3390 * (145 - 300/2) + 349 * 128.5 - 175 * 138.5 = \mathbf{37 \text{ kNm}}$$

Punkt 2: Trykkbrudd i betong

Betong svikter samtidig som stål gir etter

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{s1} = c * \varepsilon_{cu} / h = 16.5 * 0.0035 / 300 = 0.00019 < \varepsilon_{yd} \rightarrow \text{ikke flyting}$$

$$\sigma_{sd} = E_s * \varepsilon_{s1} = 200000 * 0.00019 = 38 \text{ N/mm}^2$$

$$T_c = f_{cd} * b * 0.8h = 11.3 * 1000 * 0.8 * 300 = 271200 \text{ N} = 2712 \text{ kN}$$

$$S_1 = \sigma_{sd} * A_{s1} = 38 * 502 = 18914.5 \text{ N} = 19 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 1004 = 349 \text{ kN}$$

$$\text{Aksiell likevekt: } N_2 = T_c + S_1 + S_2 = 2712 + 19 + 349 = \mathbf{3080 \text{ kN}}$$

$$\text{Momentlikevekt: } M_2 = T_c * (\alpha d - 0.4h) + S_2 * e_2 - S_1 * e_1 =$$

$$2712 * (145 - 0.4 * 300) + 349 * 128.5 - 19 * 138.5 = \mathbf{110 \text{ kNm}}$$

Punkt 3: Trykkbrudd i betong samtidig med flytning i armering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_s = \varepsilon_{yd}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668$$

$$\alpha d_2 = 0.668 * 283.5 = 189.4 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{189.4 - 16.5}{189.4} * 0.0035 = 0.0032 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 189.4 = 1712176 \text{ N} = 1712 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 502 = 174596 \text{ N} = 175 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 1004 = 349191.2 \text{ N} = 349 \text{ kN}$$

$$\text{Aksiell likevekt : } N_3 = T_c + S_2 - S_1 = 1712 + 349 - 175 = \mathbf{1886 \text{ kN}}$$

$$\begin{aligned} \text{Momentlikevekt : } M_3 &= T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e_1 + S_2 * e_2 = \\ 1712 * (145 - 0.4 * 189.4) &+ 175 * 138.5 + 349 * 128.5 = \mathbf{188 \text{ kNm}} \end{aligned}$$

Punkt 4: Trykkbrudd i betong og dobbel flytetøyning i strekkarmering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 2\varepsilon_{yk}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 2\varepsilon_{yk}} = \frac{0.0035}{0.0035 + 2 * 0.002} = 0.467$$

Sørensen (4.22)

$$\alpha d_2 = 0.467 * 283.5 = 132.4 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{132.4 - 16.5}{132.4} * 0.0035 = 0.003 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 132.4 = 1196896 \text{ N} = 1196.9 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 502 = 174596 \text{ N} = 175 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 1004 = 349191.2 \text{ N} = 349 \text{ kN}$$

$$\text{Aksiell likevekt : } N_4 = T_c + S_2 - S_1 = 1196.9 + 349 - 175 = \mathbf{1371 \text{ kN}}$$

$$\begin{aligned} \text{Momentlikevekt : } M_4 &= T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e_1 + S_2 * e_2 = \\ 1196.9 * (145 - 0.4 * 132.4) &+ 175 * 138.5 + 349 * 128.5 = \mathbf{179 \text{ kNm}} \end{aligned}$$

Punkt 5: Trykkbrudd i betong og stor armeringstøying

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 0.015$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 0.015} = \frac{0.0035}{0.0035 + 0.015} = 0.189$$

Sørensen (4.22)

$$\alpha d_2 = 0.189 * 283.5 = 53.6 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{53.6 - 16.5}{53.6} * 0.0035 = 0.0024 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 53.6 = 484544 \text{ N} = 485 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 502 = 174596 \text{ N} = 175 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 1004 = 349191.2 \text{ N} = 349 \text{ kN}$$

$$\text{Aksiell likevekt : } N_5 = T_c + S_2 - S_1 = 484 + 349 - 175 = \mathbf{658 \text{ kN}}$$

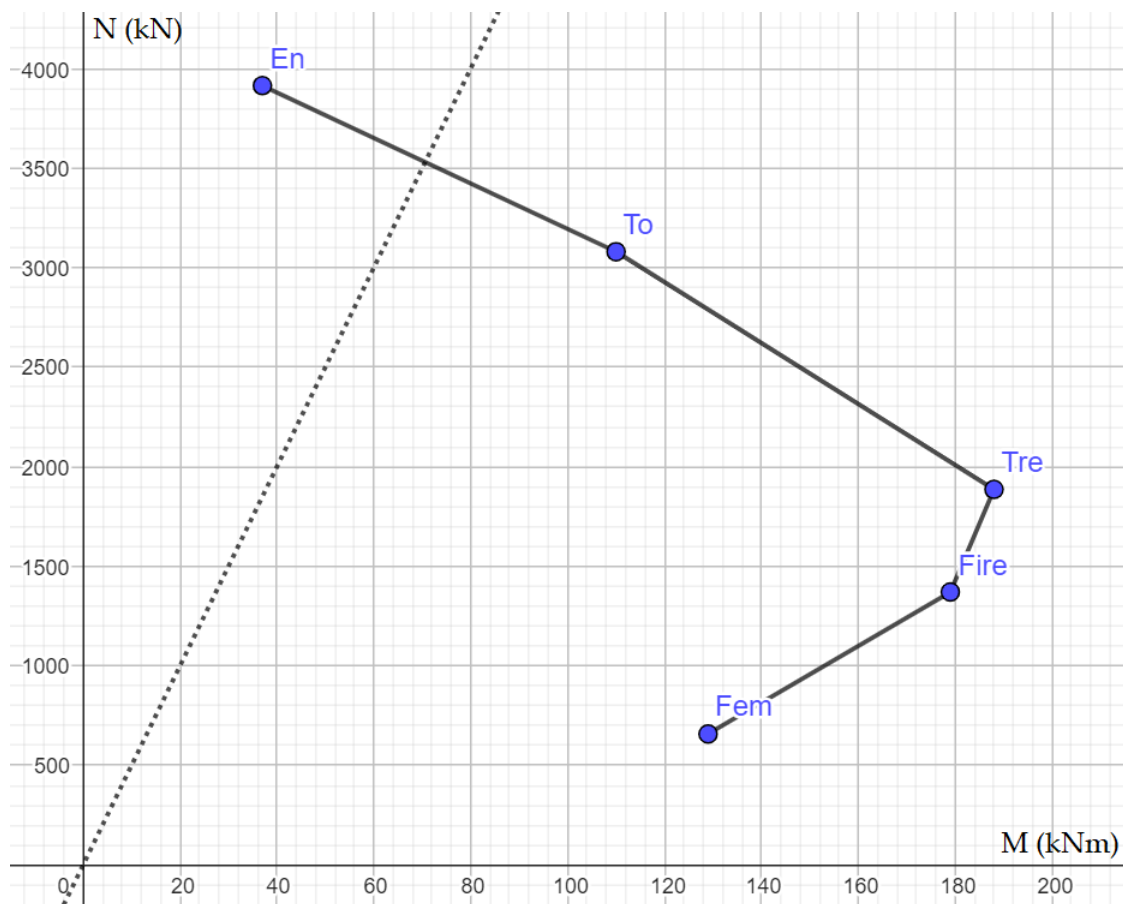
$$\text{Momentlikevekt : } M_5 = T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e_1 + S_2 * e_2 =$$

$$485 * (145 - 0.4 * 53.6) + 175 * 138.5 + 349 * 128.5 = \mathbf{129 \text{ kNm}}$$

$$e_0 = \max \{h/30, 20\text{mm}\} = 20\text{mm}$$

EC2-6.1 (4)

Resulterende interaksjonsdiagram:



Skjærkapasitet:

Dimensjonerende skjærkraft: $V_{Ed} = \frac{q_{Ed} * L}{2} = \frac{20.25 * 4}{2} = 40.5 \text{ kN}$

Skjærstrekkapasitet: $V_{Rd,c} = C_{Rd,c} * K * (100 * P_L * f_{ck})^{\frac{1}{3}} * b_w * d$ Sørensen (4.43)

$$K = 1 + \sqrt{\frac{200}{d}} \leq 2.0$$

$$= 1 + \sqrt{\frac{200}{283.5}} = 1.84$$

$$P_L = \frac{A_{sL}}{b_w * d} \leq 0.02$$

$$= \frac{502}{1000 * 283.5} = 0.00177$$

$$K_2 = 0.15$$

EC2-NA.6.2.2 (1)

$$C_{Rd,c} = \frac{K_2}{\gamma_c} = \frac{0.15}{1.5} = 0.1$$

$$V_{Rd,c} = 0.1 * 1.84 * (100 * 0.00177 * 20)^{\frac{1}{3}} * 1000 * 283.5 = 79500.9 \text{ N} = \mathbf{79.5 \text{ kN}}$$

$$V_{Rd,c} > V_{Ed}$$

Max nyttelast: $\frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 79.5 \rightarrow p = \mathbf{20.5 \text{ kN/m}}$

Skjærtrykkapasitet: $V_{Rd,max} = 0.5 * b_w * d * v * f_{cd}$

$$v = 0.6 * \left(1 - \frac{f_{ck}}{250}\right) = 0.6 * \left(1 - \frac{20}{250}\right) = 0.552$$

Sørensen (4.51)

$$V_{Rd,max} = 0.5 * 1000 * 283.5 * 0.552 * 11.3 = 884179.8 \text{ N} = \mathbf{884 \text{ kN}}$$

$$V_{Rd,max} > V_{Ed}$$

Max nyttelast : $\frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 884 \rightarrow p = \mathbf{288 \text{ kN/m}}$

Momentkapasitet:

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174$$

$$\alpha_b = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668$$

Sørensen (4.20)

$$\lambda = 0.8$$

EC2-3.1.7 (3)

$$\eta = 1.0$$

EC2-3.1.7 (3)

$$A_{s,b} = \lambda \eta * \frac{f_{cd}}{f_{yd}} * b * d * \alpha_b = 0.8 * 1.0 * \frac{11.3}{347.8} * 1000 * 283.5 * 0.668 = 4922 \text{ mm}^2$$

Sørensen (4.21)

$$\rightarrow A_s < A_{s,b}$$

$$\lambda * \eta * f_{cd} * b * d * \alpha - f_{yd} * A_s = 0$$

Sørensen (4.19)

$$\rightarrow \alpha = \frac{f_{yd} * A_s}{\lambda * \eta * f_{cd} * b * d} = \frac{347.8 * 1509}{0.8 * 1.0 * 11.3 * 1000 * 283.5} = 0.205$$

$$\varepsilon_s = \frac{1 - \alpha}{\alpha} * \varepsilon_{cu} = \frac{1 - 0.205}{0.205} * 0.0035 = 0.014$$

$$\rightarrow \varepsilon_s < \varepsilon_{ud} = 0.03$$

EC2- Tabell NA.3.5 (901)

$$M_{Rd} = \lambda \eta \alpha * (1 - 0.5 * \lambda \alpha) * f_{cd} * b * d^2$$

Sørensen (4.14)

$$= 0.8 * 1.0 * 0.205 * (1 - 0.5 * 0.8 * 0.205) * 11.3 * 1000 * 283.5^2$$

$$= 136732293.7 \text{ Nmm} = \mathbf{136.7 \text{ kNm}}$$

$$M_{Ed} = \frac{[1.2(g_1 + g_2) + 1.5 \cdot p] * L^2}{12} = \frac{(1.2 * 7.5 + 1.5 * 7.5) * 4^2}{12} = \mathbf{27 \text{ kNm}}$$

$$M_{Rd} > M_{Ed} \text{ OK.}$$

$$\text{Max nyttelast : } \frac{(7.5 * 1.2 + p * 1.5) * 4^2}{12} = 136.7 \rightarrow p = \mathbf{62 \text{ kN/m}}$$

Aksialkraftkapasitet:

$$A_c = b * h = 1000 * 300 = 300000 \text{ mm}^2$$

$$N_{Rd} = f_{cd} (A_c - A_s) + f_{yd} * A_s$$

Sørensen (4.5)

$$= 11.3 * (300000 - 1506) + 347.8 * 1506 = 4059971.5 \text{ N} = \mathbf{3898 \text{ kN}}$$

Nedbøyning:

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_s = 200000 \text{ N/mm}^2$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{1506}{1000 \cdot 283.5} = 0.005$$

$$\eta \rho = 6.667 \cdot 0.005 = 0.033$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.033^2 + 2 \cdot 0.033} - 0.033 = 0.23$$

Sørensen (5.5)

$$I_s = A_s \cdot (1 - \alpha) \cdot \left(1 - \frac{\alpha}{3}\right) \cdot d^2 = 1506 \cdot (1 - 0.23) \cdot \left(1 - \frac{0.23}{3}\right) \cdot 283.5^2 = 8.6 \cdot 10^7 \text{ mm}^4$$

Sørensen (5.11)

$$EI = E_s \cdot I_s = 200000 \cdot 8.6 \cdot 10^7 = 1.72 \cdot 10^{13} \text{ Nmm}^2$$

Sørensen (5.12)

$$q = 15 \text{ kN/m}$$

$$\text{Nedbøyning (bruksgrensetilstand)} : \delta_{II} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{15 \cdot 4000^4}{384 \cdot 1.72 \cdot 10^{13}} = \mathbf{0.58 \text{ mm}}$$

Langtidsnedbøyning:

permanent last:

$$g = 7.5 \cdot 1.2 = 9 \text{ kN/m}$$

$$p = 7.5 \cdot 1.5 = 11.25 \text{ kN/m (antar 100\% permanent)}$$

$$\text{lasttilfelle 1: } g = 9 \text{ kN/m, } \varphi(\infty, 3)$$

$$\text{lasttilfelle 2: } p = 11.25 \text{ kN/m, } \varphi(\infty, 28)$$

$$h_0 = \frac{2A_c}{u} = \frac{2 \cdot 300 \cdot 1000}{2 \cdot (300 + 1000)} = 231 \text{ mm}$$

Kryptall : utendørsforhold

EC2-Tillegg B

$$\varphi(t, t_0) = \varphi_0 \cdot \beta(t, t_0)$$

$$\varphi_0 = \varphi_{RH} \cdot \beta(f_{cm}) \cdot \beta(t_0)$$

$$RH = 80 \text{ (utendørsforhold)}$$

$$\varphi_{RH} = 1 + \frac{1 - \frac{RH}{100}}{0.1 \cdot \sqrt[3]{h_0}} = 1 + \frac{1 - \frac{80}{100}}{0.1 \cdot \sqrt[3]{231}} = 1.33$$

$$\beta(f_{cm}) = \frac{16.8}{\sqrt{f_{cm}}} = \frac{16.8}{\sqrt{28}} = 3.17$$

$$\beta(t_0) = \frac{1}{(0.1 + t_0^{0.20})}$$

$$\beta(3) = \frac{1}{(0.1 + 3^{0.20})} = 0.74$$

$$\beta(28) = \frac{1}{(0.1 + 28^{0.20})} = 0.49$$

$$\varphi_3 = 1.33 \cdot 3.17 \cdot 0.74 = 3.12$$

$$\varphi_{28} = 1.33 \cdot 3.17 \cdot 0.49 = 2.07$$

$$\beta(t, t_0) = \left[\frac{(t - t_0)}{(\beta_H + t - t_0)} \right]^{0.3}$$

$$\beta(\infty, 3) \rightarrow 1$$

$$\beta(\infty, 28) \rightarrow 1$$

$$\varphi(\infty, 3) = 4.96 \cdot 1 = 3.12$$

$$\varphi(\infty, 28) = 4.71 \cdot 1 = 2.07$$

$$E_{c1} = \frac{E_{cm}}{1 + \varphi(t, t_0)}$$

$$E_{c1} = \frac{30000}{1+3.12} = 7282 \text{ MPa}$$

$$E_{c2} = \frac{30000}{1+2.07} = 9772 \text{ MPa}$$

$$M_1 = \frac{q \cdot L^2}{12} = \frac{(9) \cdot 4^2}{12} = 12 \text{ kNm}$$

$$M_2 = \frac{q \cdot L^2}{12} = \frac{(11.25) \cdot 4^2}{12} = 15 \text{ kNm}$$

$$E_{c, \text{middle}} = \frac{\frac{M_1 + M_2}{\frac{M_1}{E_{c1}} + \frac{M_2}{E_{c2}}}}{\frac{12+15}{\frac{12}{7282} + \frac{15}{9772}}} = 8483 \text{ MPa}$$

$$\eta = \frac{E_s}{E_{c, \text{middle}}} = \frac{200000}{8483} = 23.6$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{1506}{1000 \cdot 283.5} = 0.005$$

$$\eta \rho = 23.6 \cdot 0.005 = 0.118$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.118^2 + 2 \cdot 0.118} - 0.118 = 0.38$$

Sørensen (5.5)

$$I_c = 0.5 \cdot \alpha^2 \cdot (1 - \frac{\alpha}{3}) \cdot b \cdot d^3 = 0.5 \cdot 0.38^2 \cdot (1 - \frac{0.38}{3}) \cdot 1000 \cdot 283.5^3 = 1.44 \cdot 10^9 \text{ mm}^4$$

Sørensen (5.9)

$$EI = E_{c, \text{middle}} \cdot I_c = 8483 \cdot 1.44 \cdot 10^9 = 1.2 \cdot 10^{13} \text{ Nmm}^2$$

Sørensen (5.10)

Nedbøyning midt på bjelken:

$$\delta_{\text{Lang}} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{20.25 \cdot 4000^4}{384 \cdot 1.2 \cdot 10^{13}} = \mathbf{1.13 \text{ mm}}$$

Nedbøyning pga svinn:

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot \alpha_{ds1}) \cdot e^{\frac{(-\alpha_{ds2} \cdot f_{cm})}{f_{cm0}}}] \cdot 10^{-6} \cdot \beta_{RH}$$

Sørensen (5.27)

$$f_{cm0} = 10 \text{ MPa}$$

$$\alpha_{ds1} = 3$$

(Sement klasse S)

$$\alpha_{ds2} = 0.13$$

(Sement klasse S)

$$\beta_{RH} = 1.55 [1 - (\frac{RH}{RH_0})^3] = 1.55 [1 - (\frac{80}{100})^3] = 0.76$$

Sørensen (5.28)

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot 3) \cdot e^{\frac{(-0.13 \cdot 28)}{10}}] \cdot 10^{-6} \cdot 0.76 = 2.47 \cdot 10^{-4}$$

$$\epsilon_{cd}(t) = \beta_{ds}(t, t_s) \cdot k_h \cdot \epsilon_{cd,0}$$

Sørensen (5.29)

$$\beta_{ds}(t, t_s) = \frac{(t - t_s)}{(t - t_s) + 0.4 \sqrt{h_0^3}} : t \rightarrow \infty \rightarrow \beta_{ds} = 1$$

$$k_h = 0.78$$

EC2-Tabell 3.3

$$\epsilon_{cd}(\infty) = 1 \cdot 0.78 \cdot 2.47 \cdot 10^{-4} = 1.93 \cdot 10^{-4}$$

$$\epsilon_{ca}(\infty) = 2.5 (f_{ck} - 10) \cdot 10^{-6} = 2.5 (20 - 10) \cdot 10^{-6} = 2.5 \cdot 10^{-5}$$

Sørensen (5.31)

$$\epsilon_{cs} = \epsilon_{cd} + \epsilon_{ca} = 1.93 \cdot 10^{-4} + 2.5 \cdot 10^{-5} = 2.18 \cdot 10^{-4}$$

Sørensen (5.26)

Svinnkrumning:

$$K_s = \epsilon_{cs} * \eta * \frac{A_s * e}{I} \quad \text{Sørensen (s.135)}$$

$$\alpha d = \frac{A_c * 0.5h + \eta * A_s * d}{A_c + \eta * A_s} = \frac{300000 * 0.5 * 300 + 23.6 * (1004 - 502) * 283.5}{300000 + 23.6 * (1004 - 502)} = 155 \rightarrow 145$$

$$e_2 = d - \alpha d = 283.5 - 155 = 128.5 \text{ (avstand } A_{s2} \text{ til T.A)}$$

$$e_1 = h - e_2 = 267 - 128.5 = 138.5 \text{ (avstand } A_{s1} \text{ til T.A)}$$

$$I = \frac{b * h^3}{12} + b * h * \left(ad - \frac{h}{2}\right)^2 + \eta * A_s * e^2$$

$$= \frac{1000 * 300^3}{12} + 1000 * 300 * \left(145 - \frac{300}{2}\right)^2 + 23.6 * 1004 * 128.5^2 + 23.6 * 502 * 138.5^2$$

$$= 28.7 * 10^8 \text{ mm}^4$$

$$K_s = 2.18 * 10^{-4} * 23.6 * \frac{1004 * 128.5 + 502 * 138.5}{28.7 * 10^8} = 3.56 * 10^{-7} \text{ mm}^{-1}$$

$$\delta_{svinn} = \frac{K_s * L^2}{8} = \frac{3.56 * 10^{-7} * 4000^2}{8} = \mathbf{0.71 \text{ mm}}$$

$$\delta_{total} = \delta_{lang} + \delta_{svinn} = 1.13 + 0.71 = \mathbf{1.84 \text{ mm}}$$

$$\delta_{maks} = \frac{L}{250} = \frac{4000}{250} = 16 \text{ mm} > \delta_{total} \rightarrow \text{ok} \quad \text{EC2-7.4.1 (4)}$$

$$\text{Max nyttelast : } 16 = \frac{(7.5 * 1.2 + 1.5 * q) * 4000^4}{384 * 1.2 * 10^{13}} + 0.71 \rightarrow q = 177 \text{ kN/m}$$

Rissviddekontroll:

$$k_c = c_{nom} / c_{min, dur} = 10 / 60 = 0.1667$$

$$w_{max} = 0.3 * k_c = 0.3 * 0.1667 = 0.05 \text{ mm} \quad \text{Sørensen (tabell 5.2)}$$

$$M = \frac{20.25 * 4^2}{12} = 27 \text{ kNm}$$

$$\sigma_s = E_s * \frac{M(1-\alpha)d}{EI} = 200000 * \frac{27 * 10^6 * (1-0.38) * 283.5}{1.2 * 10^{13}} = 79 \text{ MPa} \quad \text{Sørensen (5.55)}$$

$$k_t = 0.4 \text{ (langvarig last)}$$

$$f_{ct, eff} = f_{cmt} = 2.2 \text{ MPa} \quad \text{EC2-Tabell 3.1}$$

$$h_{c, eff} = \min \left\{ 2.5(h-d); \left(\frac{h-\alpha d}{3}\right); \frac{h}{2} \right\} = \min \left\{ 2.5(300-283.5); \left(\frac{300-0.38*283.5}{3}\right); \frac{300}{2} \right\} = 41.25$$

$$\rho_{p, eff} = \frac{A_s}{A_{c, eff}} = \frac{1506}{1000 * 41.25} = 0.037 \quad \text{Sørensen (s.153)}$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{\sigma_s - k_t * \frac{f_{ct, eff}}{\rho_{p, eff}} * (1 + \eta \rho_{p, eff})}{E_s} \geq 0.6 * \frac{\sigma_s}{E_s} \quad \text{Sørensen (5.59)}$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{79 - 0.4 * \frac{2.2}{0.037} * (1 + 6.667 * 0.037)}{200000} = 2.46 * 10^{-4} \geq 0.6 * \frac{79}{200000} = 2.37 * 10^{-4}$$

$$C_{nom} = 10 \text{ mm}$$

$$5 * (C_{nom} + \frac{\emptyset}{2}) = 5 * (10 + \frac{13}{2}) = 82.5 < \text{senteravstand} = 300$$

$$S_{r, max} = 1.3 * (h - \alpha d) = 1.3 * (300 - 0.38 * 283.5) = 250 \quad \text{Sørensen (5.61)}$$

$$w_k = S_{r, max} * (\epsilon_{sm} - \epsilon_{cm}) = 250 * 2.46 * 10^{-4} = 0.06 \quad \text{Sørensen (5.58)}$$

$$w_k > w_{max} = 0.05 \text{ (Rissviddekrav ikke oppfylt)}$$

Max nyttelast:

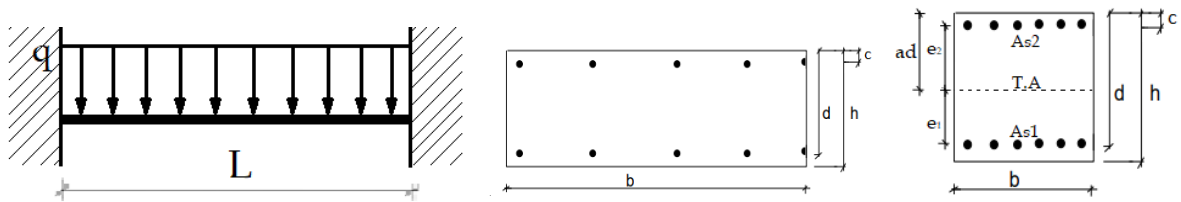
$$\frac{Mpa - 0.4 * \frac{2.2}{0.037} * (1 + 6.667 * 0.037)}{200000} * 250 = 0.05 \rightarrow Mpa = 69.6$$

$$200000 * \frac{M * 10^6 * (1 - 0.38) * 283.5}{1.2 * 10^{13}} = 69.6 \rightarrow M = 23.7$$

$$\frac{(1.2 * 7.5 + q * 1.5) * 4^2}{12} = 23.7 \rightarrow q = 5.8$$

Vedlegg D.7: Snitt 7

Snitt 7:



Sikkerhets faktor

$$\gamma_c = 1.5$$

$$\gamma_s = 1.15$$

$$\alpha_{cc} = 0.85$$

$$\gamma_G = 1.2$$

$$\gamma_Q = 1.5$$

EC2-Tabell 2.1N

EC2-Tabell 2.1N

EC2- NA.3.1.6(1)

EC - Tabell NA.A1.2(A)

EC - Tabell NA.A1.2(A)

Last:

$$p = 7.5 \text{ kN/m}^2 * 1\text{m} = 7.5 \text{ kN/m}$$

(EC1-Tabell 6.4)

$$g_1 = 0$$

$$g_2 = 25 \text{ kN/m}^3 * 0.3\text{m} * 1\text{m} = 7.5 \text{ kN/m}$$

$$q_{Ed} = \gamma_G * g + \gamma_Q * p = 1.2 * 7.5 + 1.5 * 7.5 = 20.25 \text{ kN/m} \quad (\text{betongelementboka s304})$$

Geometri:

$$h = 300 \text{ mm}$$

$$b = 1000 \text{ mm}$$

$$d = 300 - 10 - \frac{10}{2} = 285 \text{ mm}$$

$$c = 10 + \frac{10}{2} = 15 \text{ mm}$$

$$h' = h - 2 * c = 270$$

$$L = 1800 \text{ mm}$$

$$e = \frac{h}{2} - (h - d) = 135 \text{ mm}$$

Betong: B300 (V413 tabell 2.1.2-1)

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_{cd} = \alpha_{cc} \frac{f_{ck}}{\gamma_c} = 11.3 \text{ N/mm}^2$$

$$f_{cm} = 28 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$f_{ctm} = 2.2 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

Standard armering

$$f_{yk} = 400 \text{ N/mm}^2$$

V413 Tabell 2.1.2-2

$$f_{yd} = \frac{f_{yk}}{\gamma_s} = 347.8 \text{ N/mm}^2$$

$$E_s = 200000 \text{ N/mm}^2$$

EC2- 3.2.7(4)

Betong styrke ved: $t = 3$ dager

EC2-3.1.2

$s = 0.38$ For sement klasse S

$$\beta_{cc}(3) = \exp(s(1 - (\frac{28}{t})^{0.5})) = 0.458$$

$$f_{cm}(3) = \beta_{cc}(3) f_{cm} = 12.8 \text{ N/mm}^2$$

$$f_{ck}(3) = f_{cm}(3) - 8 \text{ MPa} = 4.8 \text{ N/mm}^2$$

$$f_{cd}(3) = \alpha_{cc} \frac{f_{ck}(3)}{\gamma_c} = 2.72 \text{ N/mm}^2$$

EC2-3.1.6

Minimums armering: (EC2-9.2.1.1)

$$A_{s,min} = \max \{ 0.26 \frac{f_{ctm}}{f_{yk}} b_t d; 0.0013 b_t d \} =$$

$$\max \{ 0.26 \frac{2.2}{400} * 1000 * 285; 0.0013 * 1000 * 285 \} = 407.6 \text{ mm}^2$$

$$\text{Antall jern} = \frac{30 \text{ jern}}{4m} = 7.5$$

$$A_s = \pi \left(\frac{10}{2} \right)^2 * 7.5 = 589 \text{ mm}^2$$

$$A_{s1} = A_s / 2 = 294.5 \text{ mm}^2$$

$$A_{s2} = A_s / 2 = 294.5 \text{ mm}^2$$

Minste overdekning: (EC2-4.4.1.2 og NA)

$$c_{min,b} = 13 \text{ mm}$$

$$c_{min,dur} = 60 \text{ mm}$$

EC2-Tabell NA.4.4N

$$\Delta c_{dur,\gamma} = 0$$

$$\Delta c_{dur,st} = \text{ikke gjeldende}$$

$$\Delta c_{dur,add} = \text{ikke gjeldende}$$

$$c_{min} = \max \{ c_{min,b}; c_{min,dur} + \Delta c_{dur,\gamma} - \Delta c_{dur,st} - \Delta c_{dur,add}; 10 \text{ mm} \} = 60 \text{ mm}$$

Nominell overdekning:

(EC2-4.4.1.1(2))

$$c_{nom} = c_{min} + \Delta c_{dev} = 60 + 10 = 70 \text{ mm}$$

Faktisk overdekning = 10mm

$$c_{nom} = 10 \text{ mm}$$

Kapasitetskontroll (M-N diagram)

Punkt 1: Rent trykk

$$\varepsilon_c = \varepsilon_{c3} = 0.00175$$

EC2-Tabell 3.1

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174 < \varepsilon_{c3} \rightarrow \text{armeringen flyter}$$

$$T_c = f_{cd} * b * h = 11.3 * 1000 * 300 = 3390000 \text{ N} = 3390 \text{ kN}$$

$$S_1 = \frac{f_{yk}}{\gamma_s} * A_{s1} = f_{yd} * A_{s1} = 347.8 * 294.5 = 102427.1 \text{ N} = 102 \text{ kN}$$

$$S_2 = S_1$$

$$\text{Aksiell likevekt: } N_1 = T_c + S_1 + S_2 = 3390 + 102 + 102 = \mathbf{3594 \text{ kN}}$$

$$\text{Momentlikevekt: } M_1 = \mathbf{0}$$

Punkt 2: Trykkbrudd i betong

Betong svikter samtidig som stål gir etter

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{s1} = c * \varepsilon_{cu} / h = 15 * 0.0035 / 300 = 0.00018 < \varepsilon_{yd} \rightarrow \text{ikke flyting}$$

$$\sigma_{sd} = E_s * \varepsilon_{s1} = 200000 * 0.00018 = 36 \text{ N/mm}^2$$

$$T_c = f_{cd} * b * 0.8 * h = 11.3 * 1000 * 0.8 * 300 = 2712000 \text{ N} = 2712 \text{ kN}$$

$$S_1 = \sigma_{sd} * A_{s1} = 36 * 294.5 = 10602 \text{ N} = 10.6 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 294.5 = 102427.1 \text{ N} = 102 \text{ kN}$$

$$\text{Aksiell likevekt: } N_2 = T_c + S_1 + S_2 = 2712 + 10.6 + 102 = \mathbf{2824.6 \text{ kN}}$$

$$\text{Momentlikevekt: } M_2 = T_c * (0.5h - 0.4h) + S_2 * h / 2 - S_1 * h / 2 =$$

$$2712 * (0.5 * 0.300 - 0.4 * 0.300) + 102 * 0.270 / 2 - 10.6 * 0.270 / 2 = \mathbf{94 \text{ kNm}}$$

Punkt 3: Trykkbrudd i betong samtidig med flytning i armering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_s = \varepsilon_{yd}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668$$

$$\alpha d = 0.668 * 285 = 190.4 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{190.4 - 15}{190.4} * 0.0035 = 0.0032 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d = 11.3 * 1000 * 0.8 * 190.4 = 1721216 \text{ N} = 1721 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 294.5 = 102427.1 \text{ N} = 102 \text{ kN}$$

$$S_2 = S_1$$

$$\text{Aksiell likevekt : } N_3 = T_c + S_2 - S_1 = 1721 + 102 - 102 = \mathbf{1721 \text{ kN}}$$

$$\text{Momentlikevekt : } M_3 = T_c * (0.5h - 0.4 \alpha d) + S_1 * h' = \\ 1721 * (0.5 * 300 - 0.4 * 190.4) + 102 * 270 = \mathbf{155 \text{ kNm}}$$

Punkt 4: Trykkbrudd i betong og dobbel flytetøyning i strekkarmering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 2\varepsilon_{yk}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 2\varepsilon_{yk}} = \frac{0.0035}{0.0035 + 2 * 0.002} = 0.467$$

Sørensen (4.22)

$$\alpha d = 0.467 * 285 = 133 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{133 - 15}{133} * 0.0035 = 0.0031 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d = 11.3 * 1000 * 0.8 * 133 = 1202320 \text{ N} = 1020 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 294.5 = 102427.1 \text{ N} = 102 \text{ kN}$$

$$S_2 = S_1$$

$$\text{Aksiell likevekt : } N_4 = T_c + S_2 - S_1 = 1020 + 102 - 102 = \mathbf{1020 \text{ kN}}$$

$$\text{Momentlikevekt : } M_4 = T_c * (0.5h - 0.4 \alpha d) + S_1 * h' = \\ 1020 * (0.5 * 300 - 0.4 * 133) + 102 * 270 = \mathbf{126 \text{ kNm}}$$

Punkt 5: Trykkbrudd i betong og stor armeringstøyning

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 0.015$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 0.015} = \frac{0.0035}{0.0035 + 0.015} = 0.189$$

Sørensen (4.22)

$$\alpha d = 0.189 * 285 = 53.9 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{53.9 - 15}{53.9} * 0.0035 = 0.0025 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d = 11.3 * 1000 * 0.8 * 53.9 = 487256 \text{ N} = 487 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 294.5 = 102427.1 \text{ N} = 102 \text{ kN}$$

$$S_2 = S_1$$

$$\text{Aksiell likevekt : } N_5 = T_c + S_2 - S_1 = 487 + 102 - 102 = \mathbf{487 \text{ kN}}$$

$$\text{Momentlikevekt : } M_5 = T_c * (0.5h - 0.4 \alpha d) + S_1 * h'/2 + S_2 * h'/2 =$$

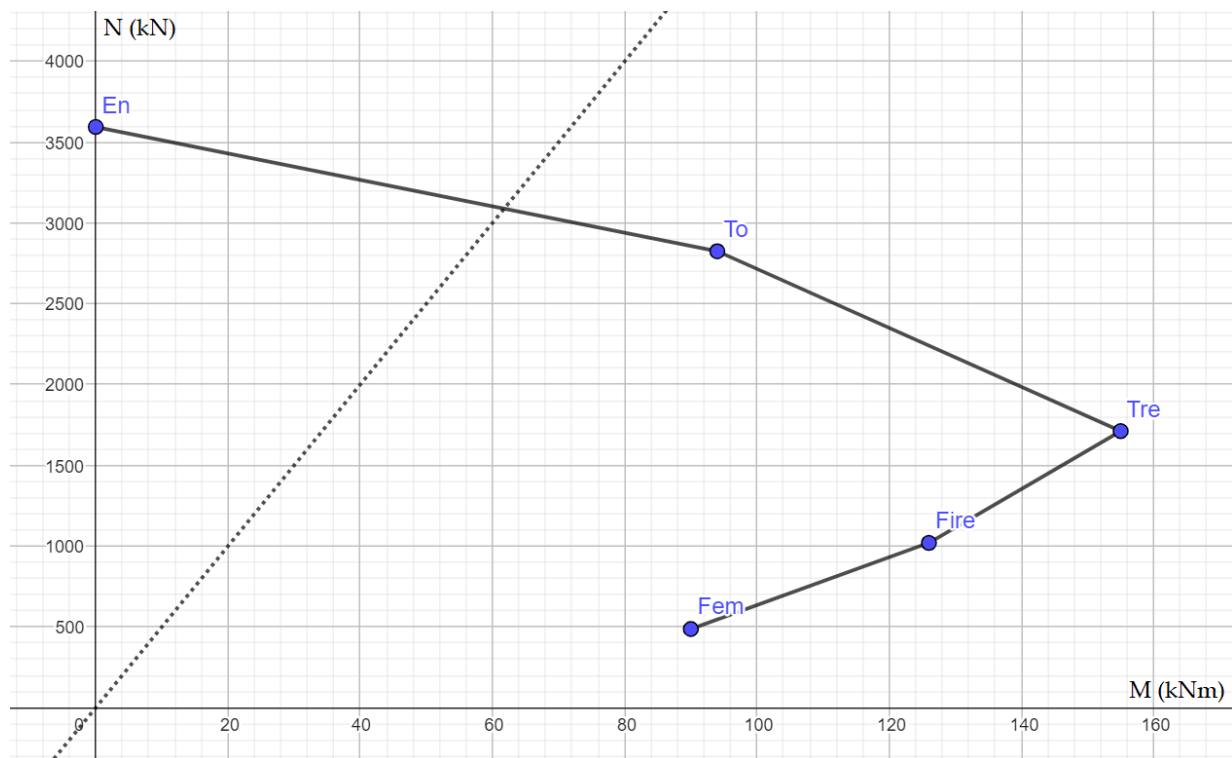
$$487 * (0.5 * 300 - 0.4 * 53.9) + 102 * 270/2 + 102 * 270/2 = \mathbf{90 \text{ kNm}}$$

$$e_0 = \max \{h/30, 20\text{mm}\} = 20\text{mm}$$

EC2-6.1

(4)

Resulterende interaksjonsdiagram:



Skjærkapasitet:

Dimensjonerende skjærkraft: $V_{Ed} = \frac{q_{Ed} * L}{2} = \frac{20.25 * 1.8}{2} = 18.2 \text{ kN}$

Skjærstrekkapasitet: $V_{Rd,c} = C_{Rd,c} * K * (100 * P_L * f_{ck})^{\frac{1}{3}} * b_w * d$ Sørensen (4.43)

$$K = 1 + \sqrt{\frac{200}{d}} \leq 2.0$$

$$= 1 + \sqrt{\frac{200}{285}} = 1.84$$

$$P_L = \frac{A_{sL}}{b_w * d} \leq 0.02$$

$$= \frac{294.5}{1000 * 285} = 0.00103$$

$$K_2 = 0.15$$
 EC2-NA.6.2.2 (1)

$$C_{Rd,c} = \frac{K_2}{\gamma_c} = \frac{0.15}{1.5} = 0.1$$

$$V_{Rd,c} = 0.1 * 1.84 * (100 * 0.00103 * 20)^{\frac{1}{3}} * 1000 * 285 = 66724.5 \text{ N} = \mathbf{66.7 \text{ kN}}$$

$$V_{Rd,c} > V_{Ed}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 1.8}{2} = 66.7 \rightarrow p = \mathbf{43 \text{ kN/m}}$$

Skjærtrykkapasitet: $V_{Rd,max} = 0.5 * b_w * d * v * f_{cd}$

$$v = 0.6 * (1 - \frac{f_{ck}}{250}) = 0.6 * (1 - \frac{20}{250}) = 0.552$$
 Sørensen (4.51)

$$V_{Rd,max} = 0.5 * 1000 * 285 * 0.552 * 11.3 = 888858 \text{ N} = \mathbf{889 \text{ kN}}$$

$$V_{Rd,max} > V_{Ed}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 1.8}{2} = 889 \rightarrow p = \mathbf{652 \text{ kN}}$$

Momentkapasitet:

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174$$

$$\alpha_b = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668 \quad \text{Sørensen (4.20)}$$

$$\lambda = 0.8 \quad \text{EC2-3.1.7 (3)}$$

$$\eta = 1.0 \quad \text{EC2-3.1.7 (3)}$$

$$A_{s,b} = \lambda \eta * \frac{f_{cd}}{f_{yd}} * b * d * \alpha_b = 0.8 * 1.0 * \frac{11.3}{347.8} * 1000 * 285 * 0.668 = 4948 \text{ mm}^2 \quad \text{Sørensen (4.21)}$$

$$\rightarrow A_s < A_{s,b}$$

$$\lambda * \eta * f_{cd} * b * d * \alpha - f_{yd} * A_s = 0 \quad \text{Sørensen (4.19)}$$

$$\rightarrow \alpha = \frac{f_{yd} * A_s}{\lambda * \eta * f_{cd} * b * d} = \frac{347.8 * 589}{0.8 * 1.0 * 11.3 * 1000 * 285} = 0.08$$

$$\varepsilon_s = \frac{1 - \alpha}{\alpha} * \varepsilon_{cu} = \frac{1 - 0.08}{0.08} * 0.0035 = 0.040$$

$$\rightarrow \varepsilon_s > \varepsilon_{ud} = 0.03 \quad \text{ikke ok} \quad \text{EC2- Tabell NA.3.5 (901)}$$

$$M_{Rd} = \lambda \eta \alpha * (1 - 0.5 * \lambda \alpha) * f_{cd} * b * d^2 \quad \text{Sørensen (4.14)}$$

$$= 0.8 * 1.0 * 0.08 * (1 - 0.5 * 0.8 * 0.08) * 11.3 * 1000 * 285^2$$

$$= 56862179 \text{ Nmm} = \mathbf{56.8 \text{ kNm}}$$

$$M_{Ed} = \frac{[1.2(g_1 + g_2) + 1.5 \cdot p] * L^2}{12} = \frac{(1.2 * 7.5 + 1.5 * 7.5) * 1.8^2}{12} = \mathbf{5.5 \text{ kNm}}$$

$$M_{Rd} > M_{Ed} \quad \text{OK.}$$

$$\text{Max nyttelast : } \frac{(7.5 * 1.2 + p * 1.5) * 1.8^2}{12} = 56.8 \rightarrow p = \mathbf{134 \text{ kN/m}}$$

Aksialkraftkapasitet:

$$A_c = b * h = 1000 * 300 = 300000 \text{ mm}^2$$

$$N_{Rd} = f_{cd} (A_c - A_s) + f_{yd} * A_s \quad \text{Sørensen (4.5)}$$

$$= 11.3 * (300000 - 589) + 347.8 * 589 = 3588198.5 \text{ N} = \mathbf{3588 \text{ kN}}$$

Nedbøyning:

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_s = 200000 \text{ N/mm}^2$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{589}{1000 \cdot 285} = 0.002$$

$$\eta \rho = 6.667 \cdot 0.002 = 0.013$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.013^2 + 2 \cdot 0.013} - 0.013 = 0.15$$

Sørensen (5.5)

$$I_s = A_s \cdot (1 - \alpha) \cdot \left(1 - \frac{\alpha}{3}\right) \cdot d^2 = 589 \cdot (1 - 0.15) \cdot \left(1 - \frac{0.15}{3}\right) \cdot 285^2 = 3.86 \cdot 10^7 \text{ mm}^4$$

Sørensen (5.11)

$$EI = E_s \cdot I_s = 200000 \cdot 3.86 \cdot 10^7 = 0.77 \cdot 10^{13} \text{ Nmm}^2$$

Sørensen (5.12)

$$q = 15 \text{ kN/m}$$

$$\text{Nedbøyning (bruksgrensetilstand)} : \delta_{II} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{15 \cdot 1800^4}{384 \cdot 0.77 \cdot 10^{13}} = \mathbf{0.05 \text{ mm}}$$

Langtidsnedbøyning:

permanent last:

$$g = 7.5 \cdot 1.2 = 9 \text{ kN/m}$$

$$p = 7.5 \cdot 1.5 = 11.25 \text{ kN/m (antar 100\% permanent)}$$

$$\text{lasttilfelle 1: } g = 9 \text{ kN/m, } \varphi(\infty, 3)$$

$$\text{lasttilfelle 2: } p = 11.25 \text{ kN/m, } \varphi(\infty, 28)$$

$$h_0 = \frac{2A_c}{u} = \frac{2 \cdot 300 \cdot 1000}{2 \cdot (300 + 1000)} = 231 \text{ mm}$$

Kryptall : utendørsforhold

EC2-Tillegg B

$$\varphi(t, t_0) = \varphi_0 \cdot \beta(t, t_0)$$

$$\varphi_0 = \varphi_{RH} \cdot \beta(f_{cm}) \cdot \beta(t_0)$$

$$RH = 80 \text{ (utendørsforhold)}$$

$$\varphi_{RH} = 1 + \frac{1 - \frac{RH}{100}}{0.1 \cdot \sqrt[3]{h_0}} = 1 + \frac{1 - \frac{80}{100}}{0.1 \cdot \sqrt[3]{231}} = 1.33$$

$$\beta(f_{cm}) = \frac{16.8}{\sqrt{f_{cm}}} = \frac{16.8}{\sqrt{28}} = 3.17$$

$$\beta(t_0) = \frac{1}{(0.1 + t_0^{0.20})}$$

$$\beta(3) = \frac{1}{(0.1 + 3^{0.20})} = 0.74$$

$$\beta(28) = \frac{1}{(0.1 + 28^{0.20})} = 0.49$$

$$\varphi_3 = 1.33 \cdot 3.17 \cdot 0.74 = 3.12$$

$$\varphi_{28} = 1.33 \cdot 3.17 \cdot 0.49 = 2.07$$

$$\beta(t, t_0) = \left[\frac{(t - t_0)}{(\beta_H + t - t_0)} \right]^{0.3}$$

$$\beta(\infty, 3) \rightarrow 1$$

$$\beta(\infty, 28) \rightarrow 1$$

$$\varphi(\infty, 3) = 4.96 \cdot 1 = 3.12$$

$$\varphi(\infty, 28) = 4.71 \cdot 1 = 2.07$$

$$E_{c1} = \frac{E_{cm}}{1 + \varphi(t, t_0)}$$

$$E_{c1} = \frac{30000}{1+3.12} = 7282 \text{ MPa}$$

$$E_{c2} = \frac{30000}{1+2.07} = 9772 \text{ MPa}$$

$$M_1 = \frac{q \cdot L^2}{12} = \frac{(9) \cdot 4^2}{12} = 12 \text{ kNm}$$

$$M_2 = \frac{q \cdot L^2}{12} = \frac{(11.25) \cdot 4^2}{12} = 15 \text{ kNm}$$

$$E_{c, \text{middle}} = \frac{\frac{M_1 + M_2}{\frac{M_1}{E_{c1}} + \frac{M_2}{E_{c2}}}}{\frac{12+15}{\frac{12}{7282} + \frac{15}{9772}}} = 8483 \text{ MPa}$$

$$\eta = \frac{E_s}{E_{c, \text{middel}}} = \frac{200000}{8483} = 23.6$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{589}{1000 \cdot 285} = 0.002$$

$$\eta \rho = 23.6 \cdot 0.002 = 0.065$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.065^2 + 2 \cdot 0.065} - 0.065 = 0.30$$

Sørensen (5.5)

$$I_c = 0.5 \cdot \alpha^2 \cdot (1 - \frac{\alpha}{3}) \cdot b \cdot d^3 = 0.5 \cdot 0.3^2 \cdot (1 - \frac{0.3}{3}) \cdot 1000 \cdot 285^3 = 9.38 \cdot 10^8 \text{ mm}^4$$

Sørensen (5.9)

$$EI = E_{c, \text{middel}} \cdot I_c = 8483 \cdot 9.38 \cdot 10^8 = 7.96 \cdot 10^{12} \text{ Nmm}^2$$

Sørensen (5.10)

Nedbøyning midt på bjelken:

$$\delta_{\text{Lang}} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{20.25 \cdot 1800^4}{384 \cdot 7.96 \cdot 10^{12}} = \mathbf{0.07 \text{ mm}}$$

Nedbøyning pga svinn:

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot \alpha_{ds1}) \cdot e^{\frac{(-\alpha_{ds2} \cdot f_{cm})}{f_{cm0}}}] \cdot 10^{-6} \cdot \beta_{RH}$$

Sørensen (5.27)

$$f_{cm0} = 10 \text{ MPa}$$

$$\alpha_{ds1} = 3$$

(Sement klasse S)

$$\alpha_{ds2} = 0.13$$

(Sement klasse S)

$$\beta_{RH} = 1.55 [1 - (\frac{RH}{RH_0})^3] = 1.55 [1 - (\frac{80}{100})^3] = 0.76$$

Sørensen (5.28)

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot 3) \cdot e^{\frac{(-0.13 \cdot 28)}{10}}] \cdot 10^{-6} \cdot 0.76 = 2.47 \cdot 10^{-4}$$

$$\epsilon_{cd}(t) = \beta_{ds}(t, t_s) \cdot k_h \cdot \epsilon_{cd,0}$$

Sørensen (5.29)

$$\beta_{ds}(t, t_s) = \frac{(t - t_s)}{(t - t_s) + 0.4 \sqrt{h_0^3}} : t \rightarrow \infty \rightarrow \beta_{ds} = 1$$

$$k_h = 0.78$$

EC2-Tabell 3.3

$$\epsilon_{cd}(\infty) = 1 \cdot 0.78 \cdot 2.47 \cdot 10^{-4} = 1.93 \cdot 10^{-4}$$

$$\epsilon_{ca}(\infty) = 2.5 (f_{ck} - 10) \cdot 10^{-6} = 2.5 (20 - 10) \cdot 10^{-6} = 2.5 \cdot 10^{-5}$$

Sørensen (5.31)

$$\epsilon_{cs} = \epsilon_{cd} + \epsilon_{ca} = 1.93 \cdot 10^{-4} + 2.5 \cdot 10^{-5} = 2.18 \cdot 10^{-4}$$

Sørensen (5.26)

Svinnkrumning:

$$K_s = \epsilon_{cs} * \eta * \frac{A_s * e}{I}$$

Sørensen (s.135)

$$\alpha d = \frac{h}{2} = \frac{300}{2} = 150$$

$$e = d - \alpha d = 285 - 150 = 135$$

$$I = \frac{b * h^3}{12} + b * h * \left(\alpha d - \frac{h}{2} \right)^2 + \eta * A_s * e^2$$

$$= \frac{1000 * 300^3}{12} + 1000 * 300 * \left(150 - \frac{300}{2} \right)^2 + 23.6 * 589 * 135^2 = 25.03 * 10^8 \text{ mm}^4$$

$$K_s = 2.18 * 10^{-4} * 23.6 * \frac{589 * 135}{25.03 * 10^8} = 1.63 * 10^{-7} \text{ mm}^{-1}$$

$$\delta_{svinn} = \frac{K_s * L^2}{8} = \frac{1.63 * 10^{-7} * 1800^2}{8} = \mathbf{0.07 \text{ mm}}$$

$$\delta_{total} = \delta_{lang} + \delta_{svinn} = 0.07 + 0.07 = \mathbf{0.14 \text{ mm}}$$

$$\delta_{maks} = \frac{L}{250} = \frac{1800}{250} = 7.2 \text{ mm} > \delta_{total} \rightarrow \text{ok}$$

EC2-7.4.1 (4)

$$\text{Max nyttelast : } 7.2 = \frac{(7.5 * 1.2 + 1.5 * q) * 1800^4}{384 * 7.96 * 10^{12}} + 0.07 \rightarrow q = 1378 \text{ kN/m}$$

Rissviddekontroll:

$$k_c = c_{nom} / c_{min, dur} = 10 / 60 = 0.1667$$

$$w_{max} = 0.3 * k_c = 0.3 * 0.1667 = 0.05 \text{ mm}$$

Sørensen (tabell 5.2)

$$M = \frac{20.25 * 1.8^2}{12} = 5.6 \text{ kNm}$$

$$\sigma_s = E_s * \frac{M(1-\alpha)d}{EI} = 200000 * \frac{5.6 * 10^6 * (1-0.3) * 285}{7.96 * 10^{12}} = 28 \text{ MPa}$$

Sørensen (5.55)

$$k_t = 0.4 \text{ (langvarig last)}$$

$$f_{ct, eff} = f_{cmt} = 2.2 \text{ MPa}$$

EC2-Tabell 3.1

$$h_{c, eff} = \min \left\{ 2.5(h-d); \left(\frac{h-\alpha d}{3} \right); \frac{h}{2} \right\} = \min \left\{ 2.5(300-285); \left(\frac{300-0.3*285}{3} \right); \frac{300}{2} \right\} = 37.5$$

$$\rho_{p, eff} = \frac{A_s}{A_{c, eff}} = \frac{589}{1000 * 37.5} = 0.016$$

Sørensen (s.153)

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{\sigma_s - k_t * \frac{f_{ct, eff}}{\rho_{p, eff}} * (1 + \eta \rho_{p, eff})}{E_s} \geq 0.6 * \frac{\sigma_s}{E_s}$$

Sørensen (5.59)

$$\epsilon_{sm} - \epsilon_{cm} = \frac{28 - 0.4 * \frac{2.2}{0.016} * (1 + 6.667 * 0.016)}{200000} = -1.6 * 10^{-4} \geq 0.6 * \frac{28}{200000} = 8.4 * 10^{-5}$$

$$C_{nom} = 10 \text{ mm}$$

$$5 * (C_{nom} + \frac{\emptyset}{2}) = 5 * (10 + \frac{13}{2}) = 82.5 < \text{senteravstand} = 300$$

$$S_{r, max} = 1.3 * (h - \alpha d) = 1.3 * (300 - 0.3 * 285) = 279$$

Sørensen (5.61)

$$w_k = S_{r, max} * (\epsilon_{sm} - \epsilon_{cm}) = 279 * 8.4 * 10^{-5} = \mathbf{0.02}$$

Sørensen (5.58)

$$w_k > w_{max} = 0.05 \text{ (Rissviddekrav oppfylt)}$$

Max nyttelast:

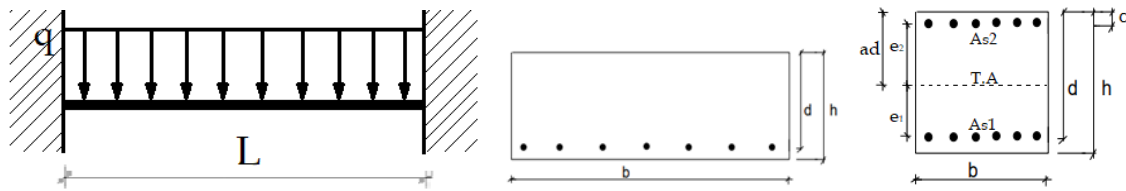
$$0.6 * \frac{\sigma_s}{200000} * 279 = 0.05 \rightarrow \sigma_s = 59.7$$

$$200000 * \frac{M * 10^6 * (1 - 0.3) * 285}{7.96 * 10^{12}} = 59.7 \rightarrow M = 11.9$$

$$\frac{(1.2 * 7.5 + 1.5 * q) * 1.8^2}{12} = 11.9 \rightarrow q = 23.3$$

Vedlegg D.8: Snitt 8

Snitt 8:



Sikkerhets faktor

$$\gamma_c = 1.5$$

EC2-Tabell 2.1N

$$\gamma_s = 1.15$$

EC2-Tabell 2.1N

$$\alpha_{cc} = 0.85$$

EC2- NA.3.1.6(1)

$$\gamma_G = 1.2$$

EC - Tabell NA.A1.2(A)

$$\gamma_Q = 1.5$$

EC - Tabell NA.A1.2(A)

Last:

$$p = 7.5 \text{ kN/m}^2 * 1\text{m} = 7.5 \text{ kN/m}$$

(EC1-Tabell 6.4)

$$g_1 = 0$$

$$g_2 = 25 \text{ kN/m}^3 * 0.3\text{m} * 1\text{m} = 7.5 \text{ kN/m}$$

$$q_{Ed} = \gamma_G * g + \gamma_Q * p = 1.2 * 7.5 + 1.5 * 7.5 = 20.25 \text{ kN/m} \quad (\text{betongelementboka s304})$$

Geometri:

$$h = 300 \text{ mm}$$

$$b = 1000 \text{ mm}$$

$$d = 300 - 10 - \frac{10}{2} = 285 \text{ mm}$$

$$c = 10 + \frac{10}{2} = 15 \text{ mm}$$

$$h' = h - 2 * c = 270$$

$$L = 2800 \text{ mm}$$

Betong: B300 (V413 tabell 2.1.2-1)

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_{cd} = \alpha_{cc} \frac{f_{ck}}{\gamma_c} = 11.3 \text{ N/mm}^2$$

$$f_{cm} = 28 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$f_{ctm} = 2.2 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

Standard armering

$$f_{yk} = 400 \text{ N/mm}^2$$

V413 Tabell 2.1.2-2

$$f_{yd} = \frac{f_{yk}}{\gamma_s} = 347.8 \text{ N/mm}^2$$

$$E_s = 200000 \text{ N/mm}^2$$

EC2- 3.2.7(4)

Betong styrke ved: $t = 3$ dager

EC2-3.1.2

$s = 0.38$ For sement klasse S

$$\beta_{cc}(3) = \exp(s(1 - (\frac{28}{t})^{0.5})) = 0.458$$

$$f_{cm}(3) = \beta_{cc}(3) f_{cm} = 12.8 \text{ N/mm}^2$$

$$f_{ck}(3) = f_{cm}(3) - 8 \text{ MPa} = 4.8 \text{ N/mm}^2$$

$$f_{cd}(3) = \alpha_{cc} \frac{f_{ck}(3)}{\gamma_c} = 2.72 \text{ N/mm}^2$$

EC2-3.1.6

Minimums armering: (EC2-9.2.1.1)

$$A_{s,min} = \max \{ 0.26 \frac{f_{ctm}}{f_{yk}} b_t d; 0.0013 b_t d \} =$$

$$\max \{ 0.26 \frac{2.2}{400} * 1000 * 285; 0.0013 * 1000 * 285 \} = 407.6 \text{ mm}^2$$

$$\text{Antall jern} = \frac{5 \text{ jern}}{1.4m} = 3.57$$

$$A_s = \pi (\frac{10}{2})^2 * 3.57 = 280 \text{ mm}^2$$

$$A_{s1} = A_s = 280 \text{ mm}^2$$

$$A_{s2} = 0 = 0 \text{ mm}^2$$

Minste overdekning: (EC2-4.4.1.2 og NA)

$$c_{min,b} = 13 \text{ mm}$$

$$c_{min,dur} = 60 \text{ mm}$$

EC2-Tabell NA.4.4N

$$\Delta c_{dur,\gamma} = 0$$

$$\Delta c_{dur,st} = \text{ikke gjeldende}$$

$$\Delta c_{dur,add} = \text{ikke gjeldende}$$

$$c_{min} = \max \{ c_{min,b}; c_{min,dur} + \Delta c_{dur,\gamma} - \Delta c_{dur,st} - \Delta c_{dur,add}; 10 \text{ mm} \} = 60 \text{ mm}$$

Nominell overdekning:

(EC2-4.4.1.1(2))

$$c_{nom} = c_{min} + \Delta c_{dev} = 60 + 10 = 70 \text{ mm}$$

Faktisk overdekning = 10mm

$$c_{nom} = 10 \text{ mm}$$

Kapasitetskontroll (M-N diagram)

$$\eta = \frac{E_s}{E_{c,middel}} = \frac{200000}{8483} = 23.6 \text{ (fra langtidsnedbøyning)}$$
$$\alpha d = \frac{A_c * 0.5h + \eta * A_s * d}{A_c + \eta * A_s} = \frac{300000 * 0.5 * 300 + 23.6 * 280 * 285}{300000 + 23.6 * 280} = 153$$
$$e = d - \alpha d = 285 - 153 = 132$$

Punkt 1: Rent trykk

$$\varepsilon_c = \varepsilon_{c3} = 0.00175$$

EC2-Tabell 3.1

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174 < \varepsilon_{c3} \rightarrow \text{armeringen flyter}$$

$$T_c = f_{cd} * b * h = 11.3 * 1000 * 300 = 3390000 \text{ N} = 3390 \text{ kN}$$

$$S_1 = \frac{f_{yk}}{\gamma_s} * A_{s1} = f_{yd} * A_{s1} = 347.8 * 280 = 97384 \text{ N} = 97 \text{ kN}$$

$$S_2 = 0$$

$$\text{Aksiell likevekt: } N_1 = T_c + S_1 + S_2 = 3390 + 97 = \mathbf{3487 \text{ kN}}$$

$$\text{Momentlikevekt: } M_1 = T_c * (\alpha d - 0.5h) - S_1 * e$$

$$3390 * (153 - 150) - 97 * 132 = \mathbf{-26.34}$$

Punkt 2: Trykkbrudd i betong

Betong svikter samtidig som stål gir etter

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{s1} = c * \varepsilon_{cu} / h = 15 * 0.0035 / 300 = 0.00018 < \varepsilon_{yd} \rightarrow \text{ikke flyting}$$

$$\sigma_{sd} = E_s * \varepsilon_{s1} = 200000 * 0.00018 = 36 \text{ N/mm}^2$$

$$T_c = f_{cd} * b * 0.8h = 11.3 * 1000 * 0.8 * 300 = 2712000 \text{ N} = 2712 \text{ kN}$$

$$S_1 = \sigma_{sd} * A_{s1} = 36 * 280 = 10080 \text{ N} = 10 \text{ kN}$$

$$S_2 = f_{yd} * A_{s2} = 347.8 * 0 = 0 \text{ N} = 0 \text{ kN}$$

$$\text{Aksiell likevekt: } N_2 = T_c + S_1 + S_2 = 2712 + 10 = \mathbf{2722 \text{ kN}}$$

$$\text{Momentlikevekt: } M_2 = T_c * (\alpha d - 0.4h) - S_1 * e =$$

$$2712 * (153 - 0.4 * 300) - 10 * 132 = \mathbf{88 \text{ kNm}}$$

Punkt 3: Trykkbrudd i betong samtidig med flytning i armering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_s = \varepsilon_{yd}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668$$

$$\alpha d_2 = 0.668 * 285 = 190.4 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{190.4 - 15}{190.4} * 0.0035 = 0.0032 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 190.4 = 1721216 \text{ N} = 1721 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 280 = 97384 \text{ N} = 97.4 \text{ kN}$$

$$S_2 = 0$$

$$\text{Aksiell likevekt : } N_3 = T_c + S_2 - S_1 = 1721 - 97.4 = \mathbf{1623.6 \text{ kN}}$$

$$\text{Momentlikevekt : } M_3 = T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e = \\ 1721 * (153 - 0.4 * 190.4) + 97.5 * 132 = \mathbf{144 \text{ kNm}}$$

Punkt 4: Trykkbrudd i betong og dobbel flytetøyning i strekkarmering

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 2\varepsilon_{yk}$

$$\varepsilon_{cu} = 0.0035$$

EC2-Tabell 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 2\varepsilon_{yk}} = \frac{0.0035}{0.0035 + 2 * 0.002} = 0.467$$

Sørensen (4.22)

$$\alpha d_2 = 0.467 * 285 = 133 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{133 - 15}{133} * 0.0035 = 0.0031 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 133 = 1202320 \text{ N} = 1020 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 280 = 97384 \text{ N} = 97.4 \text{ kN}$$

$$S_2 = 0$$

$$\text{Aksiell likevekt : } N_4 = T_c + S_2 - S_1 = 1020 + 102 - 102 = \mathbf{1020 \text{ kN}}$$

$$\text{Momentlikevekt : } M_4 = T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e = \\ 1020 * (153 - 0.4 * 133) + 97.4 * 132 = \mathbf{115 \text{ kNm}}$$

Punkt 5: Trykkbrudd i betong og stor armeringstøyning

Bruddkriterium: $\varepsilon_c = \varepsilon_{cu3}$ og $\varepsilon_{s1} = 0.015$

$$\varepsilon_{cu} = 0.0035$$

EC2-Table 3.1

$$\varepsilon_{yk} = \frac{f_{yk}}{E_s} = \frac{400}{200000} = 0.002$$

$$\alpha = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + 0.015} = \frac{0.0035}{0.0035 + 0.015} = 0.189$$

Sørensen (4.22)

$$\alpha d_2 = 0.189 * 285 = 53.9 \text{ mm}$$

$$\varepsilon_{s2} = \frac{\alpha d - c}{\alpha d} * \varepsilon_{cu} = \frac{53.9 - 15}{53.9} * 0.0035 = 0.0025 \text{ (flyter)}$$

$$T_c = f_{cd} * b * 0.8 * \alpha d_2 = 11.3 * 1000 * 0.8 * 53.9 = 487256 \text{ N} = 487 \text{ kN}$$

$$S_1 = f_{yd} * A_{s1} = 347.8 * 280 = 97384 \text{ N} = 97.4 \text{ kN}$$

$$S_2 = 0$$

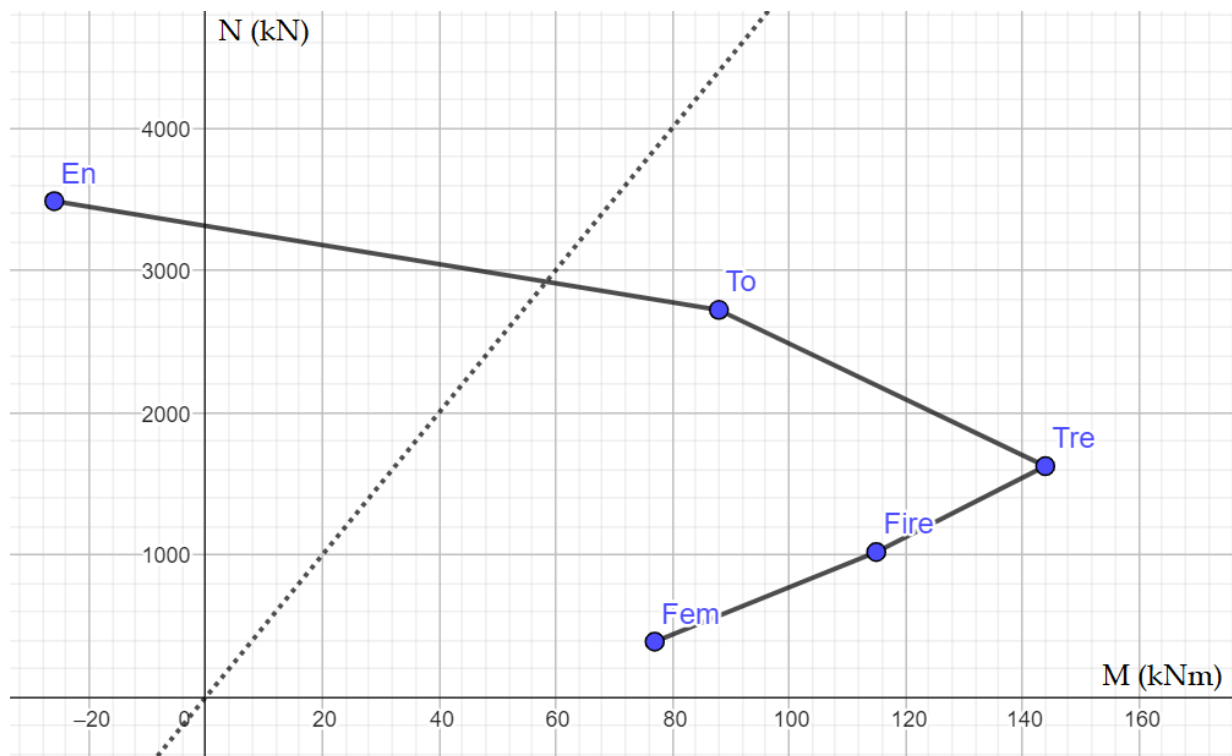
$$\text{Aksiell likevekt : } N_5 = T_c + S_2 - S_1 = 487 - 97.4 = \mathbf{389.6 \text{ kN}}$$

$$\begin{aligned} \text{Momentlikevekt : } M_5 &= T_c * (\alpha d - 0.4 \alpha d_2) + S_1 * e = \\ &= 487 * (153 - 0.4 * 53.9) + 97.4 * 132 = \mathbf{76.9 \text{ kNm}} \end{aligned}$$

$$e_0 = \max \{h/30, 20\text{mm}\} = 20\text{mm}$$

EC2-6.1 (4)

Resulterende interaksjonsdiagram:



Skjærkapasitet:

Dimensjonerende skjærkraft: $V_{Ed} = \frac{q_{Ed} * L}{2} = \frac{20.25 * 2.8}{2} = 28.4 \text{ kN}$

Skjærstrekkapasitet: $V_{Rd,c} = C_{Rd,c} * K * (100 * P_L * f_{ck})^{\frac{1}{3}} * b_w * d$ Sørensen (4.43)

$$K = 1 + \sqrt{\frac{200}{d}} \leq 2.0$$

$$= 1 + \sqrt{\frac{200}{285}} = 1.84$$

$$P_L = \frac{A_{sL}}{b_w * d} \leq 0.02$$

$$= \frac{280}{1000 * 285} = 0.00098$$

$$K_2 = 0.15$$
 EC2-NA.6.2.2 (1)

$$C_{Rd,c} = \frac{K_2}{\gamma_c} = \frac{0.15}{1.5} = 0.1$$

$$V_{Rd,c} = 0.1 * 1.84 * (100 * 0.00098 * 20)^{\frac{1}{3}} * 1000 * 285 = 65950.2 \text{ N} = \mathbf{65.0 \text{ kN}}$$

$$V_{Rd,c} > V_{Ed}$$

Max nyttelast: $\frac{(7.5 * 1.2 + p * 1.5) * 2.8}{2} = 65 \rightarrow p = \mathbf{24.9 \text{ kN}}$

Skjærtrykkapasitet: $V_{Rd,max} = 0.5 * b_w * d * v * f_{cd}$

$$v = 0.6 * (1 - \frac{f_{ck}}{250}) = 0.6 * (1 - \frac{20}{250}) = 0.552$$
 Sørensen (4.51)

$$V_{Rd,max} = 0.5 * 1000 * 285 * 0.552 * 11.3 = 888858 \text{ N} = \mathbf{889 \text{ kN}}$$

$$V_{Rd,max} > V_{Ed}$$

Max nyttelast : $\frac{(7.5 * 1.2 + p * 1.5) * 2.8}{2} = 889 \rightarrow p = \mathbf{417 \text{ kN}}$

Momentkapasitet:

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174$$

$$\alpha_b = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668 \quad \text{Sørensen (4.20)}$$

$$\lambda = 0.8 \quad \text{EC2-3.1.7 (3)}$$

$$\eta = 1.0 \quad \text{EC2-3.1.7 (3)}$$

$$A_{s,b} = \lambda \eta * \frac{f_{cd}}{f_{yd}} * b * d * \alpha_b = 0.8 * 1.0 * \frac{11.3}{347.8} * 1000 * 285 * 0.668 = 4948 \text{ mm}^2 \quad \text{Sørensen (4.21)}$$

$$\rightarrow A_s < A_{s,b}$$

$$\lambda * \eta * f_{cd} * b * d * \alpha - f_{yd} * A_s = 0 \quad \text{Sørensen (4.19)}$$

$$\rightarrow \alpha = \frac{f_{yd} * A_s}{\lambda * \eta * f_{cd} * b * d} = \frac{347.8 * 280}{0.8 * 1.0 * 11.3 * 1000 * 285} = 0.04$$

$$\varepsilon_s = \frac{1-\alpha}{\alpha} * \varepsilon_{cu} = \frac{1-0.04}{0.04} * 0.0035 = 0.084$$

$$\rightarrow \varepsilon_s > \varepsilon_{ud} = 0.03 \quad \text{ikke ok} \quad \text{EC2- Tabell NA.3.5 (901)}$$

$$M_{Rd} = \lambda \eta \alpha * (1 - 0.5 * \lambda \alpha) * f_{cd} * b * d^2 \quad \text{Sørensen (4.14)}$$

$$= 0.8 * 1.0 * 0.04 * (1 - 0.5 * 0.8 * 0.04) * 11.3 * 1000 * 285^2$$

$$= 28901025 \text{ Nmm} = \mathbf{28.9 \text{ kNm}}$$

$$M_{Ed} = \frac{[1.2(g_1 + g_2) + 1.5 \cdot p] * L^2}{12} = \frac{(1.2 * 7.5 + 1.5 * 7.5) * 2.8^2}{12} = \mathbf{13.2 \text{ kNm}}$$

$$M_{Rd} > M_{Ed} \quad \text{OK.}$$

$$\text{Max nyttelast : } \frac{(7.5 * 1.2 + p * 1.5) * 2.8^2}{12} = 28.9 \rightarrow p = \mathbf{23 \text{ kN/m}}$$

Aksialkraftkapasitet:

$$A_c = b * h = 1000 * 300 = 300000 \text{ mm}^2$$

$$N_{Rd} = f_{cd} (A_c - A_s) + f_{yd} * A_s \quad \text{Sørensen (4.5)}$$

$$= 11.3 * (300000 - 280) + 347.8 * 280 = 3484220 \text{ N} = \mathbf{3484 \text{ kN}}$$

Nedbøyning:

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_s = 200000 \text{ N/mm}^2$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{280}{1000 \cdot 285} = 0.00098$$

$$\eta \rho = 6.667 \cdot 0.00098 = 0.0065$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.0065^2 + 2 \cdot 0.0065} - 0.0065 = 0.11$$

Sørensen (5.5)

$$I_s = A_s \cdot (1 - \alpha) \cdot \left(1 - \frac{\alpha}{3}\right) \cdot d^2 = 280 \cdot (1 - 0.11) \cdot \left(1 - \frac{0.11}{3}\right) \cdot 285^2 = 1.95 \cdot 10^7 \text{ mm}^4$$

Sørensen (5.11)

$$EI = E_s \cdot I_s = 200000 \cdot 1.95 \cdot 10^7 = 0.39 \cdot 10^{13} \text{ Nmm}^2$$

Sørensen (5.12)

$$q = 15 \text{ kN/m}$$

$$\text{Nedbøyning (bruksgrensetilstand)} : \delta_{II} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{15 \cdot 2800^4}{384 \cdot 0.39 \cdot 10^{13}} = \mathbf{0.62 \text{ mm}}$$

Langtidsnedbøyning:

permanent last:

$$g = 7.5 \cdot 1.2 = 9 \text{ kN/m}$$

$$p = 7.5 \cdot 1.5 = 11.25 \text{ kN/m (antar 100\% permanent)}$$

$$\text{lasttilfelle 1: } g = 9 \text{ kN/m, } \varphi(\infty, 3)$$

$$\text{lasttilfelle 2: } p = 11.25 \text{ kN/m, } \varphi(\infty, 28)$$

$$h_0 = \frac{2A_c}{u} = \frac{2 \cdot 300 \cdot 1000}{2 \cdot (300 + 1000)} = 231 \text{ mm}$$

Kryptall : utendørsforhold

EC2-Tillegg B

$$\varphi(t, t_0) = \varphi_0 \cdot \beta(t, t_0)$$

$$\varphi_0 = \varphi_{RH} \cdot \beta(f_{cm}) \cdot \beta(t_0)$$

$$RH = 80 \text{ (utendørsforhold)}$$

$$\varphi_{RH} = 1 + \frac{1 - \frac{RH}{100}}{0.1 \cdot \sqrt[3]{h_0}} = 1 + \frac{1 - \frac{80}{100}}{0.1 \cdot \sqrt[3]{231}} = 1.33$$

$$\beta(f_{cm}) = \frac{16.8}{\sqrt{f_{cm}}} = \frac{16.8}{\sqrt{28}} = 3.17$$

$$\beta(t_0) = \frac{1}{(0.1 + t_0^{0.20})}$$

$$\beta(3) = \frac{1}{(0.1 + 3^{0.20})} = 0.74$$

$$\beta(28) = \frac{1}{(0.1 + 28^{0.20})} = 0.49$$

$$\varphi_3 = 1.33 \cdot 3.17 \cdot 0.74 = 3.12$$

$$\varphi_{28} = 1.33 \cdot 3.17 \cdot 0.49 = 2.07$$

$$\beta(t, t_0) = \left[\frac{(t - t_0)}{(\beta_H + t - t_0)} \right]^{0.3}$$

$$\beta(\infty, 3) \rightarrow 1$$

$$\beta(\infty, 28) \rightarrow 1$$

$$\varphi(\infty, 3) = 4.96 \cdot 1 = 3.12$$

$$\varphi(\infty, 28) = 4.71 \cdot 1 = 2.07$$

$$E_{c1} = \frac{E_{cm}}{1 + \varphi(t, t_0)}$$

$$E_{c1} = \frac{30000}{1 + 3.12} = 7282 \text{ MPa}$$

$$E_{c2} = \frac{30000}{1 + 2.07} = 9772 \text{ MPa}$$

$$M_1 = \frac{q \cdot L^2}{12} = \frac{(9) \cdot 4^2}{12} = 12 \text{ kNm}$$

$$M_2 = \frac{q \cdot L^2}{12} = \frac{(11.25) \cdot 4^2}{12} = 15 \text{ kNm}$$

$$E_{c, \text{middle}} = \frac{\frac{M_1 + M_2}{\frac{M_1}{E_{c1}} + \frac{M_2}{E_{c2}}}}{\frac{12 + 15}{\frac{12}{7282} + \frac{15}{9772}}} = 8483 \text{ MPa}$$

$$\eta = \frac{E_s}{E_{c, \text{middle}}} = \frac{200000}{8483} = 23.6$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{280}{1000 \cdot 285} = 0.00098$$

$$\eta \rho = 23.6 \cdot 0.00098 = 0.023$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.023^2 + 2 \cdot 0.023} - 0.023 = 0.19$$

Sørensen (5.5)

$$I_c = 0.5 \cdot \alpha^2 \cdot (1 - \frac{\alpha}{3}) \cdot b \cdot d^3 = 0.5 \cdot 0.19^2 \cdot (1 - \frac{0.19}{3}) \cdot 1000 \cdot 285^3 = 3.91 \cdot 10^8 \text{ mm}^4$$

Sørensen (5.9)

$$EI = E_{c, \text{middle}} \cdot I_c = 8483 \cdot 3.91 \cdot 10^8 = 3.32 \cdot 10^{12} \text{ Nmm}^2$$

Sørensen (5.10)

Nedbøyning midt på bjelken:

$$\delta_{\text{Lang}} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{20.25 \cdot 2800^4}{384 \cdot 3.32 \cdot 10^{12}} = \mathbf{0.98 \text{ mm}}$$

Nedbøyning pga svinn:

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot \alpha_{ds1}) \cdot e^{\frac{(-\alpha_{ds2} \cdot f_{cm})}{f_{cm0}}}] \cdot 10^{-6} \cdot \beta_{RH}$$

Sørensen (5.27)

$$f_{cm0} = 10 \text{ MPa}$$

$$\alpha_{ds1} = 3$$

(Sement klasse S)

$$\alpha_{ds2} = 0.13$$

(Sement klasse S)

$$\beta_{RH} = 1.55 [1 - (\frac{RH}{RH_0})^3] = 1.55 [1 - (\frac{80}{100})^3] = 0.76$$

Sørensen (5.28)

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot 3) \cdot e^{\frac{(-0.13 \cdot 28)}{10}}] \cdot 10^{-6} \cdot 0.76 = 2.47 \cdot 10^{-4}$$

$$\epsilon_{cd}(t) = \beta_{ds}(t, t_s) \cdot k_h \cdot \epsilon_{cd,0}$$

Sørensen (5.29)

$$\beta_{ds}(t, t_s) = \frac{(t - t_s)}{(t - t_s) + 0.4 \sqrt{h_0^3}} : t \rightarrow \infty \rightarrow \beta_{ds} = 1$$

$$k_h = 0.78$$

EC2-Tabell

$$3.3$$

$$\epsilon_{cd}(\infty) = 1 \cdot 0.78 \cdot 2.47 \cdot 10^{-4} = 1.93 \cdot 10^{-4}$$

$$\epsilon_{ca}(\infty) = 2.5 (f_{ck} - 10) \cdot 10^{-6} = 2.5 (20 - 10) \cdot 10^{-6} = 2.5 \cdot 10^{-5}$$

Sørensen (5.31)

$$\epsilon_{cs} = \epsilon_{cd} + \epsilon_{ca} = 1.93 \cdot 10^{-4} + 2.5 \cdot 10^{-5} = 2.18 \cdot 10^{-4}$$

Sørensen (5.26)

Svinnkrumning:

$$K_s = \epsilon_{cs} * \eta * \frac{A_s * e}{I} \quad \text{Sørensen (s.135)}$$

$$\alpha d = \frac{A_c * 0.5h + \eta * A_s * d}{A_c + \eta * A_s} = \frac{300000 * 0.5 * 300 + 23.6 * 280 * 285}{300000 + 23.6 * 280} = 153$$

$$e = d - \alpha d = 285 - 153 = 132$$

$$I = \frac{b * h^3}{12} + b * h * \left(ad - \frac{h}{2}\right)^2 + \eta * A_s * e^2$$

$$= \frac{1000 * 300^3}{12} + 1000 * 300 * \left(153 - \frac{300}{2}\right)^2 + 23.6 * 280 * 132^2 = 23.68 * 10^8 \text{ mm}^4$$

$$K_s = 2.18 * 10^{-4} * 23.6 * \frac{280 * 132}{23.68 * 10^8} = 0.80 * 10^{-7} \text{ mm}^{-1}$$

$$\delta_{svinn} = \frac{K_s * L^2}{8} = \frac{0.80 * 10^{-7} * 2800^2}{8} = \mathbf{0.08 \text{ mm}}$$

$$\delta_{total} = \delta_{lang} + \delta_{svinn} = 0.98 + 0.08 = \mathbf{1.06 \text{ mm}}$$

$$\delta_{maks} = \frac{L}{250} = \frac{2800}{250} = 11.2 \text{ mm} > \delta_{total} \rightarrow \text{ok} \quad \text{EC2-7.4.1 (4)}$$

$$\text{Max nyttelast : } 11.2 = \frac{(7.5 * 1.2 + 1.5 * q) * 2800^4}{384 * 3.32 * 10^{12}} + 0.08 \rightarrow q = 147.7 \text{ kN/m}$$

Rissviddekontroll:

$$k_c = c_{nom} / c_{min, dur} = 10 / 60 = 0.1667$$

$$w_{max} = 0.3 * k_c = 0.3 * 0.1667 = 0.05 \text{ mm} \quad \text{Sørensen (tabell 5.2)}$$

$$M = \frac{20.25 * 2.8^2}{12} = 13 \text{ kNm}$$

$$\sigma_s = E_s * \frac{M(1-\alpha)d}{EI} = 200000 * \frac{13 * 10^6 * (1-0.19) * 285}{3.32 * 10^{12}} = 181 \text{ MPa} \quad \text{Sørensen (5.55)}$$

$$k_t = 0.4 \text{ (langvarig last)}$$

$$f_{ct, eff} = f_{cmt} = 2.2 \text{ MPa} \quad \text{EC2-Tabell 3.1}$$

$$h_{c, eff} = \min \left\{ 2.5(h-d); \left(\frac{h-\alpha d}{3}\right); \frac{h}{2} \right\} = \min \left\{ 2.5(300-285); \left(\frac{300-0.3 * 285}{3}\right); \frac{300}{2} \right\} = 37.5$$

$$\rho_{p, eff} = \frac{A_s}{A_{c, eff}} = \frac{280}{1000 * 37.5} = 0.0075 \quad \text{Sørensen (s.153)}$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{\sigma_s - k_t * \frac{f_{ct, eff}}{\rho_{p, eff}} * (1 + \eta \rho_{p, eff})}{E_s} \geq 0.6 * \frac{\sigma_s}{E_s} \quad \text{Sørensen (5.59)}$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{181 - 0.4 * \frac{2.2}{0.0075} * (1 + 6.667 * 0.0075)}{200000} = \mathbf{2.9 * 10^{-4}} \geq \mathbf{0.6 * \frac{181}{200000} = 5.43 * 10^{-4}}$$

$$C_{nom} = 10 \text{ mm}$$

$$5 * (C_{nom} + \frac{\emptyset}{2}) = 5 * (10 + \frac{13}{2}) = 82.5 < \text{senteravstand} = 300$$

$$S_{r, max} = 1.3 * (h - \alpha d) = 1.3 * (300 - 0.19 * 285) = 320 \quad \text{Sørensen (5.61)}$$

$$w_k = S_{r, max} * (\epsilon_{sm} - \epsilon_{cm}) = 320 * 5.43 * 10^{-4} = \mathbf{0.17} \quad \text{Sørensen (5.58)}$$

$$w_k > w_{max} = 0.05 \text{ (Rissviddekrav ikke oppfylt)}$$

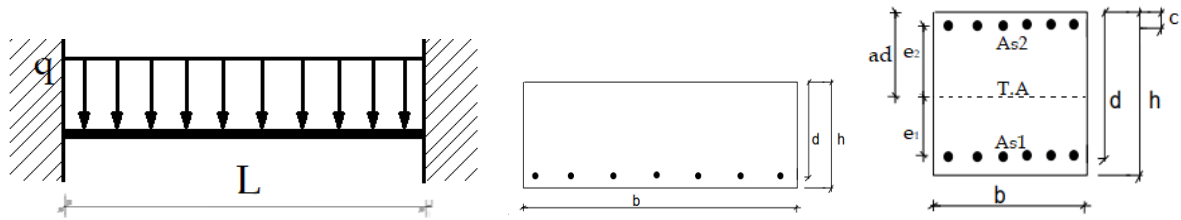
Max nyttelast:

$$320 * (0.6 * \frac{200000 * \frac{M * 10^6 * (1 - 0.19) * 285}{3.32 * 10^{12}}}{200000}) = 0.05 \rightarrow M = 3.74$$

$$\frac{(1.2 * 7.5 + q * 1.5) * 2.8^2}{12} = 3.75 \rightarrow q = -2.17$$

Vedlegg D.9: Snitt 9 (snitt 2 med redusert armeringstverrsnitt)

Snitt 9: Snitt 2 med redusert armeringstverrsnitt (ø13 til ø12)



Sikkerhets faktor

$$\gamma_c = 1.5$$

$$\gamma_s = 1.15$$

$$\alpha_{cc} = 0.85$$

$$\gamma_G = 1.2$$

$$\gamma_Q = 1.5$$

EC2-Tabell 2.1N

EC2-Tabell 2.1N

EC2- NA.3.1.6(1)

EC - Tabell NA.A1.2(A)

EC - Tabell NA.A1.2(A)

Last:

$$p = 7.5 \text{ kN/m}^2 * 1\text{m} = 7.5 \text{ kN/m}$$

(EC1-Tabell 6.4)

$$g_1 = 0$$

$$g_2 = 25 \text{ kN/m}^3 * 0.3\text{m} * 1\text{m} = 7.5 \text{ kN/m}$$

$$q_{Ed} = \gamma_G * g + \gamma_Q * p = 1.2 * 7.5 + 1.5 * 7.5 = 20.25 \text{ kN/m} \quad (\text{betongelementboka s304})$$

Geometri:

$$h = 300 \text{ mm}$$

$$b = 1000 \text{ mm}$$

$$d = 300 - 10 - \frac{12}{2} = 284 \text{ mm}$$

$$c = 10 + \frac{12}{2} = 16 \text{ mm}$$

$$h' = h - 2 * c = 268$$

$$L = 4000 \text{ mm}$$

Betong: B300 (V413 tabell 2.1.2-1)

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_{cd} = \alpha_{cc} \frac{f_{ck}}{\gamma_c} = 11.3 \text{ N/mm}^2$$

$$f_{cm} = 28 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$f_{ctm} = 2.2 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

Standard armering:

$$f_{yk} = 400 \text{ N/mm}^2$$

V413 Tabell 2.1.2-2

$$f_{yd} = \frac{f_{yk}}{\gamma_s} = 347.8 \text{ N/mm}^2$$

$$E_s = 200000 \text{ N/mm}^2$$

EC2- 3.2.7(4)

Betong styrke ved: $t = 3$ dager

EC2-3.1.2

$s = 0.38$ For sement klasse S

$$\beta_{cc}(3) = \exp(s(1 - (\frac{28}{t})^{0.5})) = 0.458$$

$$f_{cm}(3) = \beta_{cc}(3) f_{cm} = 12.8 \text{ N/mm}^2$$

$$f_{ck}(3) = f_{cm}(3) - 8 \text{ MPa} = 4.8 \text{ N/mm}^2$$

$$f_{cd}(3) = \alpha_{cc} \frac{f_{ck}(3)}{\gamma_c} = 2.72 \text{ N/mm}^2$$

EC2-3.1.6

Minimums armering: (EC2-9.2.1.1)

$$A_{s,min} = \max \{ 0.26 \frac{f_{ctm}}{f_{yk}} b_t d; 0.0013 b_t d \} =$$

$$\max \{ 0.26 \frac{2.2}{400} * 1000 * 284; 0.0013 * 1000 * 284 \} = 406.1 \text{ mm}^2$$

$$\text{Antall jern} = \frac{28 \text{ jern}}{3.7m} = 7.5$$

$$A_s = \pi (\frac{12}{2})^2 * 7.5 = 848.2 \text{ mm}^2$$

$$A_{s1} = A_s = 848.2 \text{ mm}^2$$

$$A_{s2} = 0 = 0 \text{ mm}^2$$

Minste overdekning: (EC2-4.4.1.2 og NA)

$$c_{min,b} = 13 \text{ mm}$$

$$c_{min,dur} = 60 \text{ mm}$$

EC2-Tabell NA.4.4N

$$\Delta c_{dur,\gamma} = 0$$

$$\Delta c_{dur,st} = \text{ikke gjeldende}$$

$$\Delta c_{dur,add} = \text{ikke gjeldende}$$

$$c_{min} = \max \{ c_{min,b}; c_{min,dur} + \Delta c_{dur,\gamma} - \Delta c_{dur,st} - \Delta c_{dur,add}; 10 \text{ mm} \} = 60 \text{ mm}$$

Nominell overdekning:

(EC2-4.4.1.1(2))

$$c_{nom} = c_{min} + \Delta c_{dev} = 60 + 10 = 70 \text{ mm}$$

Faktisk overdekning = 10mm

$$c_{nom} = 10 \text{ mm}$$

Skjærkapasitet:

Dimensjonerende skjærkraft: $V_{Ed} = \frac{q_{Ed} * L}{2} = \frac{20.25 * 4}{2} = 40.5 \text{ kN}$

Skjærstrekkapasitet: $V_{Rd,c} = C_{Rd,c} * K * (100 * P_L * f_{ck})^{\frac{1}{3}} * b_w * d$ Sørensen (4.43)

$$K = 1 + \sqrt{\frac{200}{d}} \leq 2.0$$

$$= 1 + \sqrt{\frac{200}{284}} = 1.84$$

$$P_L = \frac{A_{sL}}{b_w * d} \leq 0.02$$

$$= \frac{848.2}{1000 * 284} = 0.003$$

$$K_2 = 0.15$$

EC2-NA.6.2.2 (1)

$$C_{Rd,c} = \frac{K_2}{\gamma_c} = \frac{0.15}{1.5} = 0.1$$

$$V_{Rd,c} = 0.1 * 1.84 * (100 * 0.003 * 20)^{\frac{1}{3}} * 1000 * 284 = 94955.5 \text{ N} = \mathbf{95.0 \text{ kN}}$$

$$V_{Rd,c} > V_{Ed} \text{ (ok)}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 95 \rightarrow p = \mathbf{25.6 \text{ kN/m}}$$

Skjærtrykkapasitet: $V_{Rd,max} = 0.5 * b_w * d * v * f_{cd}$

$$v = 0.6 * (1 - \frac{f_{ck}}{250}) = 0.6 * (1 - \frac{20}{250}) = 0.552$$

Sørensen (4.51)

$$V_{Rd,max} = 0.5 * 1000 * 284 * 0.552 * 11.3 = 885739.2 \text{ N} = \mathbf{885 \text{ kN}}$$

$$V_{Rd,max} > V_{Ed}$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2} = 885 \rightarrow p = \mathbf{289 \text{ kN/m}}$$

Momentkapasitet:

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174$$

$$\alpha_b = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668$$

Sørensen (4.20)

$$\lambda = 0.8$$

EC2-3.1.7 (3)

$$\eta = 1.0$$

EC2-3.1.7 (3)

$$A_{s,b} = \lambda \eta * \frac{f_{cd}}{f_{yd}} * b * d * \alpha_b = 0.8 * 1.0 * \frac{11.3}{347.8} * 1000 * 284 * 0.668 = 4931 \text{ mm}^2$$

Sørensen (4.21)

$$\rightarrow A_s < A_{s,b}$$

$$\lambda * \eta * f_{cd} * b * d * \alpha - f_{yd} * A_s = 0$$

Sørensen (4.19)

$$\rightarrow \alpha = \frac{f_{yd} * A_s}{\lambda * \eta * f_{cd} * b * d} = \frac{347.8 * 848.2}{0.8 * 1.0 * 11.3 * 1000 * 284} = 0.115$$

$$\varepsilon_s = \frac{1 - \alpha}{\alpha} * \varepsilon_{cu} = \frac{1 - 0.115}{0.115} * 0.0035 = 0.0269$$

$$\rightarrow \varepsilon_s < \varepsilon_{ud} = 0.03$$

EC2- Tabell NA.3.5 (901)

$$M_{Rd} = \lambda \eta \alpha * (1 - 0.5 * \lambda \alpha) * f_{cd} * b * d^2$$

Sørensen (4.14)

$$= 0.8 * 1.0 * 0.115 * (1 - 0.5 * 0.8 * 0.115) * 11.3 * 1000 * 284^2$$

$$= 80557200.5 \text{ Nmm} = \mathbf{80.5 \text{ kNm}}$$

$$M_{Ed} = \frac{[1.2(g_1 + g_2) + 1.5 \cdot p] * L^2}{24} = \frac{(1.2 * 7.5 + 1.5 * 7.5) * 4^2}{24} = \mathbf{13.5 \text{ kNm}}$$

$$M_{Rd} > M_{Ed} \text{ OK.}$$

$$\text{Max nyttelast : } \frac{(7.5 * 1.2 + p * 1.5) * 4^2}{24} = 80.5 \rightarrow p = \mathbf{74.5 \text{ kN/m}}$$

Aksialkraftkapasitet:

$$A_c = b * h = 1000 * 300 = 300000 \text{ mm}^2$$

$$N_{Rd} = f_{cd} (A_c - A_s) + f_{yd} * A_s$$

Sørensen (4.5)

$$= 11.3 * (300000 - 848.2) + 347.8 * 848.2 = 3675419.3 \text{ N} = \mathbf{3675 \text{ kN}}$$

Nedbøyning:

$$E_{cm} = 30000 \text{ N/mm}^2$$

EC2-Tabell 3.1

$$E_s = 200000 \text{ N/mm}^2$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{848.2}{1000 \cdot 284} = 0.003$$

$$\eta \rho = 6.667 \cdot 0.003 = 0.020$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.02^2 + 2 \cdot 0.02} - 0.02 = 0.18$$

Sørensen (5.5)

$$I_s = A_s \cdot (1 - \alpha) \cdot \left(1 - \frac{\alpha}{3}\right) \cdot d^2 = 848.2 \cdot (1 - 0.18) \cdot \left(1 - \frac{0.18}{3}\right) \cdot 284^2 = 5.27 \cdot 10^7 \text{ mm}^4$$

Sørensen (5.11)

$$EI = E_s \cdot I_s = 200000 \cdot 5.27 \cdot 10^7 = 1.05 \cdot 10^{13} \text{ Nmm}^2$$

Sørensen (5.12)

$$q = 15 \text{ kN/m}$$

$$\text{Nedbøyning (bruksgrensetilstand)} : \delta_{II} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{15 \cdot 4000^4}{384 \cdot 1.05 \cdot 10^{13}} = \mathbf{0.95 \text{ mm}}$$

Langtidsnedbøyning:

permanent last:

$$g = 7.5 \cdot 1.2 = 9 \text{ kN/m}$$

$$p = 7.5 \cdot 1.5 = 11.25 \text{ kN/m (antar 100\% permanent)}$$

$$\text{lasttilfelle 1: } g = 9 \text{ kN/m, } \varphi(\infty, 3)$$

$$\text{lasttilfelle 2: } p = 11.25 \text{ kN/m, } \varphi(\infty, 28)$$

$$h_0 = \frac{2A_c}{u} = \frac{2 \cdot 300 \cdot 1000}{2 \cdot (300 + 1000)} = 231 \text{ mm}$$

Kryptall : utendørsforhold

EC2-Tillegg B

$$\varphi(t, t_0) = \varphi_0 \cdot \beta(t, t_0)$$

$$\varphi_0 = \varphi_{RH} \cdot \beta(f_{cm}) \cdot \beta(t_0)$$

$$RH = 80 \text{ (utendørsforhold)}$$

$$\varphi_{RH} = 1 + \frac{1 - \frac{RH}{100}}{0.1 \cdot \sqrt[3]{h_0}} = 1 + \frac{1 - \frac{80}{100}}{0.1 \cdot \sqrt[3]{231}} = 1.33$$

$$\beta(f_{cm}) = \frac{16.8}{\sqrt{f_{cm}}} = \frac{16.8}{\sqrt{28}} = 3.17$$

$$\beta(t_0) = \frac{1}{(0.1 + t_0^{0.20})}$$

$$\beta(3) = \frac{1}{(0.1 + 3^{0.20})} = 0.74$$

$$\beta(28) = \frac{1}{(0.1 + 28^{0.20})} = 0.49$$

$$\varphi_3 = 1.33 \cdot 3.17 \cdot 0.74 = 3.12$$

$$\varphi_{28} = 1.33 \cdot 3.17 \cdot 0.49 = 2.07$$

$$\beta(t, t_0) = \left[\frac{(t - t_0)}{(\beta_H + t - t_0)} \right]^{0.3}$$

$$\beta(\infty, 3) \rightarrow 1$$

$$\beta(\infty, 28) \rightarrow 1$$

$$\varphi(\infty, 3) = 4.96 \cdot 1 = 3.12$$

$$\varphi(\infty, 28) = 4.71 \cdot 1 = 2.07$$

$$E_{c1} = \frac{E_{cm}}{1 + \varphi(t, t_0)}$$

$$E_{c1} = \frac{30000}{1+3.12} = 7282 \text{ MPa}$$

$$E_{c2} = \frac{30000}{1+2.07} = 9772 \text{ MPa}$$

$$M_1 = \frac{q \cdot L^2}{24} = \frac{(9) \cdot 4^2}{24} = 6 \text{ kNm}$$

$$M_2 = \frac{q \cdot L^2}{24} = \frac{(11.25) \cdot 4^2}{24} = 7.5 \text{ kNm}$$

$$E_{c, \text{middle}} = \frac{\frac{M_1 + M_2}{\frac{M_1}{E_{c1}} + \frac{M_2}{E_{c2}}}}{\frac{6 + 7.5}{\frac{6}{7282} + \frac{7.5}{9772}}} = 8483 \text{ MPa}$$

$$\eta = \frac{E_s}{E_{c, \text{middle}}} = \frac{200000}{8483} = 23.6$$

$$\rho = \frac{A_s}{b \cdot d} = \frac{848.2}{1000 \cdot 284} = 0.0030$$

$$\eta \rho = 23.6 \cdot 0.003 = 0.071$$

$$\alpha = \sqrt{(\eta \rho)^2 + 2 \eta \rho} - \eta \rho = \sqrt{0.071^2 + 2 \cdot 0.071} - 0.071 = 0.31$$

Sørensen (5.5)

$$I_c = 0.5 \cdot \alpha^2 \cdot (1 - \frac{\alpha}{3}) \cdot b \cdot d^3 = 0.5 \cdot 0.31^2 \cdot (1 - \frac{0.31}{3}) \cdot 1000 \cdot 284^3 = 0.99 \cdot 10^9 \text{ mm}^4$$

Sørensen (5.9)

$$EI = E_{c, \text{middle}} \cdot I_c = 8483 \cdot 0.99 \cdot 10^9 = 8.4 \cdot 10^{12} \text{ Nmm}^2$$

Sørensen (5.10)

Nedbøyning midt på bjelken:

$$\delta_{\text{Lang}} = \frac{1}{384} \cdot \frac{q \cdot L^4}{EI} = \frac{20.25 \cdot 4000^4}{384 \cdot 8.4 \cdot 10^{12}} = \mathbf{1.61 \text{ mm}}$$

Nedbøyning pga svinn:

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot \alpha_{ds1}) \cdot e^{\frac{(-\alpha_{ds2} \cdot f_{cm})}{f_{cm0}}}] \cdot 10^{-6} \cdot \beta_{RH}$$

Sørensen (5.27)

$$f_{cm0} = 10 \text{ MPa}$$

$$\alpha_{ds1} = 3$$

(Sement klasse S)

$$\alpha_{ds2} = 0.13$$

(Sement klasse S)

$$\beta_{RH} = 1.55 [1 - (\frac{RH}{RH_0})^3] = 1.55 [1 - (\frac{80}{100})^3] = 0.76$$

Sørensen (5.28)

$$\epsilon_{cd,0} = 0.85 [(220 + 110 \cdot 3) \cdot e^{\frac{(-0.13 \cdot 28)}{10}}] \cdot 10^{-6} \cdot 0.76 = 2.47 \cdot 10^{-4}$$

$$\epsilon_{cd}(t) = \beta_{ds}(t, t_s) \cdot k_h \cdot \epsilon_{cd,0}$$

Sørensen (5.29)

$$\beta_{ds}(t, t_s) = \frac{(t - t_s)}{(t - t_s) + 0.4 \sqrt{h_0^3}} : t \rightarrow \infty \rightarrow \beta_{ds} = 1$$

$$k_h = 0.78$$

EC2-Tabell 3.3

$$\epsilon_{cd}(\infty) = 1 \cdot 0.78 \cdot 2.47 \cdot 10^{-4} = 1.93 \cdot 10^{-4}$$

$$\epsilon_{ca}(\infty) = 2.5 (f_{ck} - 10) \cdot 10^{-6} = 2.5 (20 - 10) \cdot 10^{-6} = 2.5 \cdot 10^{-5}$$

Sørensen (5.31)

$$\epsilon_{cs} = \epsilon_{cd} + \epsilon_{ca} = 1.93 \cdot 10^{-4} + 2.5 \cdot 10^{-5} = 2.18 \cdot 10^{-4}$$

Sørensen (5.26)

Svinnkrumning:

$$K_s = \epsilon_{cs} * \eta * \frac{A_s * e}{I} \quad \text{Sørensen (s.135)}$$

$$\alpha d = \frac{A_c * 0.5h + \eta * A_s * d}{A_c + \eta * A_s} = \frac{300000 * 0.5 * 300 + 23.6 * 848.2 * 284}{300000 + 23.6 * 848.2} = 158.4$$

$$e = d - \alpha d = 284 - 158.4 = 125.6$$

$$I = \frac{b * h^3}{12} + b * h * \left(ad - \frac{h}{2}\right)^2 + \eta * A_s * e^2$$

$$= \frac{1000 * 300^3}{12} + 1000 * 300 * \left(158.4 - \frac{300}{2}\right)^2 + 23.6 * 848.2 * 125.6^2 = 25.87 * 10^8 \text{ mm}^4$$

$$K_s = 2.18 * 10^{-4} * 23.6 * \frac{848.2 * 125.6}{25.87 * 10^8} = 2.12 * 10^{-7} \text{ mm}^{-1}$$

$$\delta_{svinn} = \frac{K_s * L^2}{8} = \frac{2.12 * 10^{-7} * 4000^2}{8} = \mathbf{0.42 \text{ mm}}$$

$$\delta_{total} = \delta_{lang} + \delta_{svinn} = 1.61 + 0.42 = \mathbf{2.03 \text{ mm}}$$

$$\delta_{maks} = \frac{L}{250} = \frac{4000}{250} = 16 \text{ mm} > \delta_{total} \rightarrow \text{ok} \quad \text{EC2-7.4.1 (4)}$$

$$\text{Max nyttelast : } 16 = \frac{(7.5 * 1.2 + 1.5 * q) * 4000^4}{384 * 8.4 * 10^{12}} + 0.42 \rightarrow q = 124.8 \text{ kN/m}$$

Rissviddekontroll:

$$k_c = c_{nom} / c_{min, dur} = 10 / 60 = 0.1667$$

$$w_{max} = 0.3 * k_c = 0.3 * 0.1667 = 0.05 \text{ mm} \quad \text{Sørensen (tabell 5.2)}$$

$$M = \frac{20.25 * 4^2}{24} = 13.5 \text{ kNm}$$

$$\sigma_s = E_s * \frac{M(1-\alpha)d}{EI} = 200000 * \frac{13.5 * 10^6 * (1-0.31) * 284}{8.4 * 10^{12}} = 63 \text{ MPa} \quad \text{Sørensen (5.55)}$$

$$k_t = 0.4 \text{ (langvarig last)}$$

$$f_{ct, eff} = f_{cmt} = 2.2 \text{ MPa} \quad \text{EC2-Tabell 3.1}$$

$$h_{c, eff} = \min \left\{ 2.5(h-d); \left(\frac{h-\alpha d}{3}\right); \frac{h}{2} \right\} = \min \left\{ 2.5(300-284); \left(\frac{300-0.31*284}{3}\right); \frac{300}{2} \right\} = 40$$

$$\rho_{p, eff} = \frac{A_s}{A_{c, eff}} = \frac{848.2}{1000 * 40} = 0.021 \quad \text{Sørensen (s.153)}$$

$$\eta = \frac{E_s}{E_{cm}} = \frac{200000}{30000} = 6.667$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{\sigma_s - k_t * \frac{f_{ct, eff}}{\rho_{p, eff}} * (1 + \eta \rho_{p, eff})}{E_s} \geq 0.6 * \frac{\sigma_s}{E_s} \quad \text{Sørensen (5.59)}$$

$$\epsilon_{sm} - \epsilon_{cm} = \frac{63 - 0.4 * \frac{2.2}{0.021} * (1 + 6.667 * 0.021)}{200000} = 7.61 * 10^{-5} \geq 0.6 * \frac{63}{200000} = 1.89 * 10^{-4}$$

$$C_{nom} = 10 \text{ mm}$$

$$5 * (C_{nom} + \frac{\emptyset}{2}) = 5 * (10 + \frac{13}{2}) = 82.5 < \text{senteravstand} = 300$$

$$S_{r, max} = 1.3 * (h - \alpha d) = 1.3 * (300 - 0.31 * 284) = 275.5 \quad \text{Sørensen (5.61)}$$

$$w_k = S_{r, max} * (\epsilon_{sm} - \epsilon_{cm}) = 275.5 * 1.89 * 10^{-4} = \mathbf{0.052} \quad \text{Sørensen (5.58)}$$

$$w_k > w_{max} = 0.05 \text{ (Rissviddekrav ikke oppfylt)}$$

Max nyttelast:

$$0.6 * \frac{\sigma_s}{200000} * 275.5 = 0.05 \rightarrow \sigma_s = 60.4$$

$$200000 * \frac{M * 10^6 * (1 - 0.31) * 284}{8.4 * 10^{12}} = 60.4 \rightarrow M = 12.9$$

$$\frac{(1.2 * 7.5 + 1.5 * q) * 4^2}{24} = 12.9 \rightarrow q = 6.9$$

Vedlegg D.10: Toveisplate (plate 1-4)

Toveisplate beregning

Plate: 1-4

Sørensen (tabell 2.1.1 og 2.1.2)

$$L_y/L_x = 4\text{m}/4\text{m} = 1$$

$$\alpha = 27.2$$

$$\beta = 27.2$$

$$\gamma = 0.0485$$

$$\theta_x = 2.96$$

$$\theta_y = 2.96$$

$$d_x = 283.5\text{mm}$$

$$d_y = 283.5 - 13 = 270.5\text{mm}$$

$$A_{sx} = 995.5\text{mm}^2$$

$$A_{sy} = 929\text{mm}^2$$

Moment: (bruddgrense)

$$M_x = qL_x^2/\alpha = \frac{20.25 \cdot 4^2}{27.2} = 11.9 \text{ kNm/m}$$

Sørensen (tabell 2.1.1)

$$M_y = qL_y^2/\beta = \frac{20.25 \cdot 4^2}{27.2} = 11.9 \text{ kNm/m}$$

Sørensen (tabell 2.1.1)

$$\varepsilon_{yd} = \frac{f_{yd}}{E_s} = \frac{347.8}{200000} = 0.00174$$

$$\alpha_b = \frac{\varepsilon_{cu}}{\varepsilon_{cu} + \varepsilon_{yd}} = \frac{0.0035}{0.0035 + 0.00174} = 0.668$$

Sørensen (4.20)

$$\lambda = 0.8$$

EC2-3.1.7 (3)

$$\eta = 1.0$$

EC2-3.1.7 (3)

$$A_{s,b,x} = \lambda \eta * \frac{f_{cd}}{f_{yd}} * 10^3 * d_x * \alpha_b = 0.8 * 1.0 * \frac{11.3}{347.8} * 1000 * 283.5 * 0.668 = 4922 \text{ mm}^2$$

Sørensen (4.21)

$$\rightarrow A_s < A_{s,b,x}$$

$$\lambda * \eta * f_{cd} * 10^3 * d_x * \alpha - f_{yd} * A_{sx} = 0$$

Sørensen (4.19)

$$\rightarrow \alpha = \frac{f_{yd} * A_{sx}}{\lambda * \eta * f_{cd} * 10^3 * d_x} = \frac{347.8 * 995.5}{0.8 * 1.0 * 11.3 * 1000 * 283.5} = 0.135$$

$$\varepsilon_s = \frac{1-\alpha}{\alpha} * \varepsilon_{cu} = \frac{1-0.135}{0.135} * 0.0035 = 0.0224$$

$$\rightarrow \varepsilon_s < \varepsilon_{ud} = 0.03$$

EC2- Tabell NA.3.5 (901)

$$M_{Rdx} = \lambda \eta \alpha * (1 - 0.5 * \lambda \alpha) * f_{cd} * 10^3 * d_x^2$$

Sørensen

$$(4.14)$$

$$= 0.8 * 1.0 * 0.135 * (1 - 0.5 * 0.8 * 0.135) * 11.3 * 1000 * 283.5^2$$

$$= 92789634 \text{ Nmm/m} = \mathbf{92.7 \text{ kNm/m}}$$

$$A_{s,b,y} = \lambda \eta * \frac{f_{cd}}{f_{yd}} * 10^3 * d_y * \alpha_b = 0.8 * 1.0 * \frac{11.3}{347.8} * 1000 * 270.5 * 0.668 = 4696 \text{ mm}^2 \quad \text{Sørensen (4.21)}$$

$$\rightarrow A_s < A_{s,b,y}$$

$$\lambda * \eta * f_{cd} * 10^3 * d_y * \alpha - f_{yd} * A_{sy} = 0 \quad \text{Sørensen (4.19)}$$

$$\rightarrow \alpha = \frac{f_{yd} * A_{sy}}{\lambda * \eta * f_{cd} * 10^3 * d_y} = \frac{347.8 * 929}{0.8 * 1.0 * 11.3 * 1000 * 270.5} = 0.132$$

$$\varepsilon_s = \frac{1-\alpha}{\alpha} * \varepsilon_{cu} = \frac{1-0.132}{0.132} * 0.0035 = 0.0230$$

$$\rightarrow \varepsilon_s < \varepsilon_{ud} = 0.03 \quad \text{EC2- Tabell NA.3.5 (901)}$$

$$M_{Rdy} = \lambda \eta \alpha * (1 - 0.5 * \lambda \alpha) * f_{cd} * 10^3 * d_y^2 \quad \text{Sørensen (4.14)}$$

$$= 0.8 * 1.0 * 0.132 * (1 - 0.5 * 0.8 * 0.132) * 11.3 * 1000 * 270.5^2$$

$$= 82702490.9 \text{ Nmm/m} = \mathbf{82.7 \text{ kNm/m}}$$

$$M < M_{Rd} \text{ (ok)}$$

$$\text{Max nyttelast : } \frac{(7.5 * 1.2 + p * 1.5) * 4^2}{27.2} = 82.7 \rightarrow p = \mathbf{87.7 \text{ kN/m}^2}$$

Nedbøyning: (bruddgrense)

$$E_{c,middel} = 8483 \text{ MPa} \quad \text{(vedlegg D.1)}$$

$$A_{sx} = 995.5 \text{ mm}^2/\text{m} \quad \text{(vedlegg D.1)}$$

$$d_x = 283.5 \text{ mm} \quad \text{(vedlegg D.1)}$$

$$\rho_x = \frac{A_{sx}}{10^3 * d_x} = \frac{995.5}{10^3 * 283.5} = 0.0035 \quad \text{Sørensen (2.1.8)}$$

$$\eta = \frac{E_s}{E_{c,middel}} = \frac{200000}{8483} = 23.6 \quad \text{Sørensen (2.1.9)}$$

$$\eta \rho_x = 0.0035 * 23.6 = 0.083$$

$$\alpha_x = \sqrt{(\eta \rho_x)^2 + 2 * \eta \rho_x} - \eta \rho_x = \sqrt{0.083^2 + 2 * 0.083} - 0.083 = 0.33 \quad \text{Sørensen (2.1.10)}$$

$$I_{cx} = \frac{1}{2} * \alpha_x^2 * \left(1 - \frac{\alpha_x}{3}\right) * 10^3 * d_x^3 \quad \text{Sørensen (2.1.11)}$$

$$\frac{1}{2} * 0.33^2 * \left(1 - \frac{0.33}{3}\right) * 10^3 * 283.5^3 = 1.1 * 10^9$$

$$h_{eff} = \sqrt[3]{\frac{12 * I_{cx}}{10^3}} = \sqrt[3]{\frac{12 * 1.1 * 10^9}{10^3}} = 236.3 \quad \text{Sørensen (2.1.13)}$$

$$Eh^3 = E_{c,middel} * h_{eff}^3$$

$$w = \frac{\gamma * q L_x^4}{Eh^3} = \frac{0.0485 * 20.25 * 10^{-3} * 4000^4}{8483 * 236.3^3} = 2.25 \text{ mm} \quad \text{Sørensen (tabell 2.1.1)}$$

$$\delta_{maks} = \frac{L}{250} = \frac{4000}{250} = 16 \text{ mm} > w \rightarrow \text{ok}$$

$$\text{Max nyttelast: } \frac{0.0485 * (7.5 * 1.2 + p * 1.5) * 10^{-3} * 4000^4}{8483 * 236.3^3} = 16 \rightarrow p = \mathbf{90.1 \text{ kN/m}^2}$$

Skjærkapasitet: (bruddgrense)

Dimensjonerende skjærkraft:

$$V_x = \frac{q \cdot l_x}{\theta_x} = \frac{20.25 \cdot 4}{2.96} = 27.36 \text{ kN}$$

Sørensen (Tabell 2.1.2)

$$V_y = \frac{q \cdot l_y}{\theta_y} = \frac{20.25 \cdot 4}{2.96} = 27.36 \text{ kN}$$

Sørensen (Tabell 2.1.2)

Skjærstrekkapasitet:

$$V_{Rd,c,x} = C_{Rd,c} \cdot K_x \cdot (100 \cdot P_{L,x} \cdot f_{ck})^{\frac{1}{3}} \cdot 10^3 \cdot d_x \quad \text{Sørensen (4.43)}$$

$$K_x = 1 + \sqrt{\frac{200}{d_x}} \leq 2.0$$

$$= 1 + \sqrt{\frac{200}{283.5}} = 1.84$$

$$P_{L,x} = \frac{A_{sL,x}}{10^3 \cdot d_x} \leq 0.02$$

$$= \frac{497.75}{1000 \cdot 283.5} = 0.00176$$

$$K_2 = 0.15 \quad \text{EC2-NA.6.2.2 (1)}$$

$$C_{Rd,c} = \frac{K_2}{\gamma_c} = \frac{0.15}{1.5} = 0.1$$

$$V_{Rd,c,x} = 0.1 \cdot 1.84 \cdot (100 \cdot 0.00176 \cdot 20)^{\frac{1}{3}} \cdot 1000 \cdot 283.5 = 79350.9 \text{ N} = \mathbf{79.3 \text{ kN}}$$

$$V_{Rd,c,y} = C_{Rd,c} \cdot K_y \cdot (100 \cdot P_{L,y} \cdot f_{ck})^{\frac{1}{3}} \cdot 10^3 \cdot d_y \quad \text{Sørensen (4.43)}$$

$$K_y = 1 + \sqrt{\frac{200}{d_y}} \leq 2.0$$

$$= 1 + \sqrt{\frac{200}{270.5}} = 1.86$$

$$P_{L,y} = \frac{A_{sL,y}}{10^3 \cdot d_y} \leq 0.02$$

$$= \frac{464.5}{1000 \cdot 270.5} = 0.00172$$

$$K_2 = 0.15 \quad \text{EC2-NA.6.2.2 (1)}$$

$$C_{Rd,c} = \frac{K_2}{\gamma_c} = \frac{0.15}{1.5} = 0.1$$

$$V_{Rd,c,y} = 0.1 \cdot 1.86 \cdot (100 \cdot 0.00172 \cdot 20)^{\frac{1}{3}} \cdot 1000 \cdot 270.5 = 75950.92 \text{ N} = \mathbf{75.9 \text{ kN}}$$

$$V_{Rd,c} > V$$

$$\text{Max nyttelast: } \frac{(7.5 \cdot 1.2 + p \cdot 1.5) \cdot 4}{2.96} = 75.9 \rightarrow p = \mathbf{31.4 \text{ kN/m}^2}$$

Skjærtrykkapasitet:

$$V_{Rd,max,x} = 0.5 * 10^3 * d_x * v * f_{cd}$$

$$v = 0.6 * \left(1 - \frac{f_{ck}}{250}\right) = 0.6 * \left(1 - \frac{20}{250}\right) = 0.552$$

Sørensen (4.51)

$$V_{Rd,max,x} = 0.5 * 1000 * 283.5 * 0.552 * 11.3 = 884179.8 \text{ N} = \mathbf{884 \text{ kN}}$$

$$V_{Rd,max} > V$$

$$V_{Rd,max,y} = 0.5 * 10^3 * d_y * v * f_{cd}$$

$$v = 0.6 * \left(1 - \frac{f_{ck}}{250}\right) = 0.6 * \left(1 - \frac{20}{250}\right) = 0.552$$

Sørensen (4.51)

$$V_{Rd,max} = 0.5 * 1000 * 270.5 * 0.552 * 11.3 = 843635.4 \text{ N} = \mathbf{843.6 \text{ kN}}$$

$$V_{Rd,max} > V$$

$$\text{Max nyttelast: } \frac{(7.5 * 1.2 + p * 1.5) * 4}{2.96} = 843.6 \rightarrow p = \mathbf{410 \text{ kN/m}^2}$$