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Modeling porous coastal structures using a level set method based VRANSsolver on staggered grids

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ABSTRACT

Several engineering problems in the field of coastal and offshore engineering involve flow interaction with porous structures such as breakwaters, sediment screens, and scour protection devices. In this paper, the interaction of waves with porous coastal structures using an opensource computational fluid dynamics (CFD) model is presented. The fluid flow through porous media is modeled using the Volume-averaged Reynolds-averaged Navier-Stokes (VRANS) equations. Novel improvements to the numerical grid architecture and discretization schemes are made, with a staggered numerical grid for better pressure-velocity coupling and higherorder schemes for convection and time discretization. New interpolation schemes required for the VRANS equations on a staggered grid are implemented. The flow problem is solved as a two-phase problem and the free surface is captured with the level set function. The model is validated by comparing the numerical results to experimental data for different cases such as flow through crushed rock, solitary, and regular wave interaction with a porous abutment and wave interaction with a breakwater considering the three different porous layers. The numerical results are also seen to be highly grid-independent according to the grid convergence study and show a significantly better agreement to experimental data in comparison to current literature.

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VRANS; numerical wave tank; porous; breakwater; CFD; REEF3D

1. Introduction

One of the important hydrodynamic processes in the coastal regions is the interaction of water waves with permeable coastal structures such as breakwaters. A rubble mound breakwater typically consists of a core layer, which is covered by filter layers to protect core material from erosion and then the outermost armor layer. Wave interaction with such structures has generally been investigated using model tests and empirical coefficients have then been determined to describe the flow. Recent advances in computing power have presented a great opportunity to obtain further insight into the hydrodynamic processes in the coastal zone using advanced numerical modeling approaches. There are several approaches to numerical modeling of the hydrodynamics of coastal structures, such as nonlinear shallow water equations (Kobayashi and Wurjanto 1989; Hu, Mingham, and Causon 2000) Boussinesq-type equations (Madsen, Murray, and Sørensen 1991; Fuhrman, Bingham, and Madsen 2005; Engsig-Karup et al. 2008; Liu, Fang, and Cheng 2018), smoothed particle hydrodynamics (Shao 2010; Gui, Shao, and Chen 2015; Ren et al. 2016) and Reynolds averaged Navier-Stokes (RANS) equations (Li, Troch, and de Rouck 2004; Higuera, Lara, and Losada 2013; Kamath et al. 2017) to name a few. A large amount of progress has been achieved in the last decade in the numerical modeling of wave-structure

interaction based on the RANS equations. This suggests that these models will become increasingly important for coastal engineers, as few simplifying assumptions are made compared to other approaches. In literature, the flow through porous media is classified based on the Reynolds number calculated based on pore size and pore velocity into Darcy flow, Forchheimer flow, unsteady laminar, and fully turbulent flow (Dybbs and Edwards 1984). For these different classes, different formulations are proposed for the calculation of the flow (Darcy 1856; Forchheimer 1901; Polubarinova-Kochina 1962). They have a relatively narrow range of applicability within the flow regimes that are assumed in the derivation of the relations and highly dependent on the associated empirical coefficients. The challenge lies in quantifying the flow through porous media while not resolving the flow through every single pore in the volume.

As an advance in modelingthe of coastal structures based on the RANS equations, a method for analyzing flow through porous breakwater layers was proposed by van Gent (1995), where the effects of the porous medium are included through resistance coefficients. Liu et al. (1999) implemented the same method in their work. The resistance coefficients formulated in these works are still relevant and are relied on for the modeling of porous media in the current literature. In order

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to account for the intrinsic flow through the randomly arranged pores, volume averaged RANS (VRANS) equations were introduced (Hsu, Sakakiyama, and Liu 2002). This formulation was later applied in two-dimensional models to evaluate wave interaction with low crested and submerged porous structures (Garcia, Lara, and Losada 2004; Lara, Garcia, and Losada 2006).

Furthermore, Del Jesus, Lara, and Losada (2012) presented a three-dimensional VRANS model with a new implementation of the governing equations to provide a general approach to modeling porous media with more appropriate assumptions. The resistance terms are based on the relations between Darcy-Forchheimer coefficients and physical parameters such as grain diameter and porosity (Engelund 1953). Turbulence modeling for the flow through porous media is accounted for through a volume averaged $k - \omega$ SST model. A similar approach was included in OpenFOAM by Higuera, Lara, and Losada (2014). Further changes to the continuity and momentum equations were introduced by Jensen, Jacobsen, and Christensen (2014) for a more physically correct implementation, similar to that shown by Hsu, Sakakiyama, and Liu (2002). The eddyviscosity in the porous media is not considered as wave breaking near the structure was not expected. The validation of the VRANS model for irregular wave interaction with a breakwater was presented by Jacobsen, van Gent, and Wolters (2015). The aforementioned developments in the area of porous media modeling using RANS equations show the relevance of the field and the scope for further research.

The modeling approaches in the current literature are mostly based on a collocated unstructured grid architecture in a finite volume framework with secondorder schemes for spatial and temporal discretization and a volume of fluids method to obtain the free surface. A novel numerical approach to the grid architecture and discretization schemes can improve the modeling accuracy of porous coastal structures. A structured grid allows for easy implementation of higher-order schemes which provide more accurate results. In addition, accurate calculation of the pore pressures is essential to obtain a good representation of the fluid-porous media interaction. This can be achieved through the use of a staggered grid that allows for better pressure-velocity coupling. Along with the use of an immersed boundary method, complex geometries can be modeled on a staggered structured grid. The level set method provides a sharp interface which helps in the sharp representation of the fluid-porous media interface. Additional interpolation schemes to account for the porous media relations between the different interfaces between the fluid and porous media and porous media of different characteristics are then required. With the aforementioned implementation, a consistent, numerically stable and accurate model for porous media interaction can be built.

In the current study, wave interaction with porous media is simulated using the open-source hydrodynamics model REEF3D (Bihs et al. 2016). The model is based on a finite-difference framework with a staggered structured numerical grid and obtains the free surface using the level set method. The model has been previously applied to study several complex-free surface phenomena such as focussed wave forces (Bihs et al. 2017), hydrodynamics of semi-submerged cylinders (Ong et al. 2017), water impact and entry (Kamath, Bihs, and Arntsen 2017), and floating bodies in waves (Bihs and Kamath 2017). The wave interaction with an impervious submerged step is simulated and the wave kinematics are compared to data obtained from experiments carried out at NTNU Trondheim. In order to validate the VRANS implementation in the model, a 2D dam break case through porous media from the experiments carried out by Liu et al. (1999) is replicated in this study. Wave interaction with a porous abutment is simulated using both solitary and regular waves. The numerical results for the free surface and pore pressure are compared to the experimental data from Lara, Del Jesus, and Losada (2012). Regular wave interaction with a rubble mound breakwater with core, filter, and armor layers is simulated and the calculated pore pressures in the different layers are compared to the measured values from the experiments conducted at the hydraulic laboratory at SINTEF/NTNU in Trondheim (Arntsen et al. 2003). The study presents a novel numerical approach to modeling flow through porous media while building upon previous works by Jensen, Jacobsen, and Christensen (2014) for the VRANS formulation. The current paper extends the current state-of-the-art to numerical implementation on a staggered grid with the ghost cell immersed boundary method and the level set method for the free surface to provide an improved representation of both the free surface features and the pore pressures under wave interaction with porous coastal structures. The robustness of the model is demonstrated through free surface and pore pressure calculations in various case scenarios with porous objects of different shapes and with multiple porous layers.

2. Numerical approach

2.1. VRANS equations

When modeling flow through porous media, the presence of grains and voids and their effect on the flow are described as a resistance to the flow that dissipates energy. Darcy (1856) stated that the flow velocity in the porous medium is proportional to the pressure gradient *I* as shown in Equation (1).

$$I = a u^f \tag{1}$$

where a is the inverse of hydraulic conductivity K which represents the permeability of the porous

medium and u^{f} is the filter velocity in the x – direction. The filter velocity is the actual pore velocity averaged over the pores and is defined in Equation (2).

$$u_f = \frac{1}{A} \iint u dA = n.u \tag{2}$$

where A is the cross-sectional area of the porous medium, u is the actual pore velocity, n is the porosity, which can be expressed as the ratio of the pore volume to the total volume, $n = V_{pore}/V_{total}$.

This formulation is only applicable for laminar flow where pore sizes and velocities are small and the linear relationship is not valid when these quantities increase. In the case of flow through coarse material, Forchheimer (1901) included friction terms and the pressure gradient is composed of a linear term that relates to the laminar flow. Turbulent flow is included by the non-linear term as shown in Equation (3).

$$I = au^f + bu^f |u^f| \tag{3}$$

where a and b are dimensionless coefficients referred to as friction factors. These factors depend on the fluid viscosity, the specific granular composition of the porous medium and the flow regime. This means that the factors a and b are not constants for a given material and are influenced by the Reynolds number (Re). The Forchheimer relations are empirical, but can also be derived from the Navier-Stokes equations (Burcharth and Christensen 1995). These relations are valid only in the case of stationary flow and an inertia term for unsteady flow was suggested by Polubarinova-Kochina (1962), given in Equation (4).

$$l = au^{f} + bu^{f} |u^{f}| + c \frac{\partial u^{f}}{\partial t}$$
(4)

where *c* is also a coefficient applied in case of local accelerations. Dybbs and Edwards (1984) identified four main flow regimes based on the Reynolds number $Re = u^p D_p/v$ related to the pore size D_p and pore velocity u^p shown in Table 1. By incorporating the porous media equations into the RANS equations, different flow regimes can be evaluated without the limitations of the individual equations discussed above.

An illustration of the volume averaging process is provided in Figure 1. The surface S includes both the

Table 1. Porous flow regimes.

Regime	Re – range	Flow characteristics
Darcy flow	Re < 1-10	Flow dominated by viscous forces, velocity distribution depends on local geometry
Forchheimer flow	1-10 < Re < 150	Development of an inertial "core" flow outside the boundary layers
Unsteady laminar flow	150 < Re < 300	Transitional flow regime between inertial, Forchheimer and fully turbulent flow
Fully-turbulent flow	300 < Re	Highly unsteady and chaotic flow regime

solid phase and the fluid phase, and creates the averaging volume with the radius *r*. The total volume *V* remains the same while the actual volume of the fluid phase may vary depending on the position of averaging volume. The volume averaging process is applied with the length scale constraints defined by $l \ll r \ll L$, where *l* is the pore length scale and *L* is the macroscopic length scale.

From current literature, it is evident that there is no unique method for volume averaging the RANS equations to model porous media flow. In this study, Volumeaveraged Reynolds-Averaged Navier-Stokes equations (VRANS) formulation proposed by Jensen, Jacobsen, and Christensen (2014) is chosen and implemented in a finite difference framework for a staggered numerical grid using higher-order discretization schemes. Additional interpolations required for the implementation on such a grid architecture. For the purpose of volume averaging, the velocity at a point is assumed to consist of an ensemble average velocity $(\overline{u_i})$ and a temporally fluctuating velocity (u'_i) as shown in Equation (5). When volume averaging is applied to an ensemble average value, it is convenient to introduce the velocity decomposition as shown in Equation (6) (Gray 1975).

$$u_i = \overline{u_i} + u'_i \tag{5}$$

$$\overline{u_i} = \langle \overline{u_i} \rangle^f + u_i'' \tag{6}$$

where $\langle \overline{u_i} \rangle^f$ is the intrinsic volume averaged value and u_i^r is the spatial fluctuation, $\langle \rangle$ denotes the volume averaged over the entire control volume including solids and $\langle \rangle^f$ denotes the volume averaged over pore volume only.

Applying the volume averaging theorem to the continuity equation together with the assumption that the velocities on the solids being zero results in Equation (7). Here, $\langle \bar{u}_i \rangle$ is the velocity averaged over the volume, called the filter velocity. The correct representation of the continuity equation for porous media is that the divergence of the filter velocity is zero, $\Delta \langle \bar{u} \rangle = 0$. This keeps the filter velocity constant in the flow direction and results in a zero flux for the velocity field when averaged over the entire volume, providing a divergence-free velocity field.

$$\frac{\partial \langle \bar{u}_i \rangle}{\partial x_i} = 0 \tag{7}$$

Similarly, each term is volume averaged for the momentum equations. The formulations are based on filter velocities which are divided by the porosity to get the correct momentum contributions as shown in Equation 8. The use of a filter velocity in the momentum equations results in different values for pressure gradients both inside and outside the porous media. So, the pressure is defined as the pore pressure in the momentum equations so that the hydrostatic pressure



Figure 1. Volume averaging in porous media.

distribution both inside and outside are linear and identical.

$$(1+C_m)\frac{\partial}{\partial t}\frac{\langle \bar{u}_i \rangle}{n} + \frac{1}{n}\frac{\partial}{\partial x_j}\frac{\langle \bar{u}_i \rangle \langle \bar{u}_j \rangle}{n} \\ = -\frac{1}{\rho}\frac{\partial \langle \bar{\rho} \rangle^f}{\partial x_j} + \frac{1}{n}\frac{\partial}{\partial x_j}v\left(\frac{\partial \langle \bar{u}_i \rangle}{\partial x_j} + \frac{\partial \langle \bar{u}_j \rangle}{\partial x_i}\right) + g_j + F_i \quad (8)$$

where C_m is the added mass coefficient which takes into account the grain–water interaction, calculated as shown in Equation 9 (van Gent 1993).

$$C_m = \gamma_p \frac{1-n}{n} \tag{9}$$

where n is the porosity and empirical coefficient $\gamma_p = 0.34$, F_i represents the effect of turbulence in terms of additional resistance, which is modeled using the extended Darcy-Forchheimer equation including linear, non-linear forces, and inertial forces for local accelerations as shown in Equation 10.

$$F_{i} = -a\rho \langle \overline{u_{i}} \rangle - b\rho \sqrt{\langle \overline{u_{j}} \rangle \langle \overline{u_{j}} \rangle \langle \overline{u_{i}} \rangle}$$
(10)

where a and b are the resistance coefficients, theoretically described in Eqs. 11 and 12 following van Gent (1993).

$$a = \alpha \frac{(1-n)^2}{n^3} \frac{v}{\rho d_{50}^2}$$
(11)

$$b = \beta \left(1 + \frac{7.5}{KC} \right) \frac{(1-n)}{n^3} \frac{1}{d_{50}}$$
(12)

where d_{50} is the grain diameter and KC is the Keulegan– Carpenter number, which indicates the stationarity of the flow as a ratio between the turbulence and inertia effects. The coefficients α and β depend on the Reynolds number, shape of the stones, permeability, and grade of porous material and have to be determined through experiments. A broad overview of the values of α and β is given by Troch (2000), comprising of publications by various authors using different types of materials in laminar, fully turbulent, steady, and unsteady flow conditions. The precise description of α and β coefficients are still not fully understood. Different values for these coefficients have been suggested based on experiments incorporating the effect of an oscillating flow via the KC number (van Gent 1995; Burcharth and Christensen 1995). It has been generally experienced over the years that under oscillatory flow and waves propagating over slopes or breaking, values existing in literature may not be valid anymore. In the absence of predictive methodology to determine the values of a and β , calibration has to be performed.

2.2. Numerical model

The VRANS equations described above are implemented in the open-source CFD model REEF3D (Bihs et al. 2016). The accurate modeling of wave-structure interaction requires higher order discretization schemes and a sharp representation of the free surface. This is accomplished with the conservative fifth-order WENO scheme (Jiang and Shu 1996) for discretizing the convective terms in the momentum equations. The pressure is treated using Chorin's projection method (Chorin 1968) and the resulting Poisson pressure equation is solved using a geometric preconditioned Bi-Conjugate Gradients multigrid Stabilized (BiCGStab) (Ashby and Falgout 1996) available from the high-performance solver library HYPRE (Center for Applied Scientific Computing 2006). A staggered numerical grid is employed for better velocity-pressure coupling. This is achieved by determining the pressure and other scalar quantities at the cell centers and the velocities are determined at the cell faces. Turbulence is modeled with the two-equation $k - \omega$ model (Wilcox 1994) with the transport equations for the turbulent kinetic energy k and the specific turbulent dissipation rate ω are presented in Equation (13) and (14).

$$\frac{\partial k}{\partial t} + u_j \frac{\partial k}{\partial x_j} = \frac{\partial}{\partial x_j} \left[\left(v + \frac{v_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] + P_k - \beta_k k \omega \quad (13)$$
$$\frac{\partial \omega}{\partial t} + u_j \frac{\partial \omega}{\partial t} = \frac{\partial}{\partial t} \left[\left(v + \frac{v_t}{\sigma_k} \right) \frac{\partial \omega}{\partial t} \right] + \frac{\omega}{\sigma} \alpha P_k - \beta \omega^2$$

$$\frac{\partial u}{\partial t} + u_j \frac{\partial u}{\partial x_j} = \frac{\partial}{\partial x_j} \left[\left(v + \frac{u}{\sigma_\omega} \right) \frac{\partial u}{\partial x_j} \right] + \frac{u}{k} \alpha P_k - \beta \omega^2$$
(14)

where P_k is the production rate and the closure coefficients $\sigma_k = 2$, $\sigma_\omega = 2$, $\alpha = 5/9$, $\beta = 3/40$ and $\beta_k = 9/100$ and the eddy viscosity v_t is defined in Equation (15).

$$v_t = \frac{k}{\omega} \tag{15}$$

The large strain in the flow due to wave propagation leads to unphysical overproduction of turbulence. Eddy-viscosity limiters (Durbin 2009) are used to avoid this. In a two-phase CFD model, the large difference in density at the interface between air and water causes an overproduction of turbulence at the interface. Free surface turbulence damping (Naot and Rodi 1982) is carried out only at the interface using the Dirac delta function. REEF3D is fully parallelized using the domain decomposition strategy and MPI (Message Passing Interface). Time discretization is performed with a third-order accurate total variation diminishing (TVD) Runge-Kutta scheme (Shu and Osher 1988). A ghost-cell immersed boundary method based upon the local directional by Berthelsen and Faltinsen (2008) is employed to account for the solid boundaries of the fluid domain and represent complex geometries without explicitly specifying the boundary conditions. The fluid flow properties at the boundaries of the porous objects are accounted for in the same manner.

2.2.1. Level set method

In order to obtain the free surface, the level set method (Osher and Sethian 1988) is used. In this method, the zero level set of a signed distance function, $\phi(\vec{x}, t)$ called the level set function, represents the interface between water and air. For the rest of the domain, the level set function represents the closest distance of each point in the domain from the interface and the sign distinguishes the two fluids across the interface. The level set function is defined in Equation (16).

$$\phi(\vec{x},t) \begin{cases} > 0 & \text{if } \vec{x} \text{ is in phase } 1(Water) \\ = 0 & \text{if } \vec{x} \text{ is at the interface} \\ < 0 & \text{if } \vec{x} \text{ is in phase } 2(Air) \end{cases}$$
(16)

The level set function is smooth across the interface and provides a sharp description of the free surface. The values for the physical properties such as density and viscosity of the two fluids across the interface are interpolated using a Heaviside function $H(\phi)$ over a distance of $\epsilon = 2.1 dx$, where dx is the grid size, around the interface as shown in Equation (17).

$$H(\phi) = \begin{cases} 0 & \text{if } \phi < -\epsilon \\ \frac{1}{2} \left(1 + \frac{\phi}{\epsilon} + \frac{1}{\pi} \sin\left(\frac{\pi\phi}{\epsilon}\right) \right) & \text{if } |\phi| < \epsilon \\ 1 & \text{if } \phi > \epsilon \end{cases}$$
(17)

This smoothens the discontinuity caused by the abrupt change in the physical properties of the fluids across the interface. The value of $\epsilon = 2.1 dx$ is chosen such that at least one cell in each direction is included in the interpolation and the density profiles across the interface are smooth as shown by Bihs et al. (2016). The density at the cell face is then calculated through averaging as shown in Equation (18).

$$\rho_{i+\frac{1}{2}} = \rho_1 H\left(\phi_{i+\frac{1}{2}}\right) + \rho_2 \left(1 - H\left(\phi_{i+\frac{1}{2}}\right)\right),$$
(18)

where ρ_1 and ρ_2 are the densities of the two phases, air and water, respectively. The values of the fluid viscosity are interpolated in the same manner. To obtain the change in the free surface, the level set function is convected under the velocity field in the wave tank (Equation 19).

$$\frac{\partial \phi}{\partial t} + u_j \frac{\partial \phi}{\partial x_j} = 0 \tag{19}$$

Inside the porous media, the velocity field u_j is replaced by the filter velocity field $\frac{\langle u_j \rangle}{n}$. The signed distance property of the function is lost by the motion of the free surface and it is restored by reinitializing the function after every iteration using the partial differential equations (Peng et al. 1999).

2.3. Numerical wave tank

REEF3D can be used as a numerical wave tank using the wave generation and absorption boundary conditions implemented in the model. The two major methods provided for wave generation are the relaxation method (Engsig-Karup et al. 2008) and the Dirichlettype method. In the first method, a part of the wave tank is reserved for the purpose of wave generation and absorption using relaxation functions. The relaxation functions then modulate the computational values with a theoretical value to either generate or absorb waves (Bihs et al. 2016). In the Dirichlet-type method, the desired values for velocities and the free surface elevation are directly prescribed at the inlet boundary. In this way, reserving additional zones in the wave tank for wave generation and absorption are avoided. The current study employs the Dirichlettype method for wave generation and no numerical beach is used in the cases simulated in this study. A Cartesian grid is employed in the study and dx =dy = dz in all the simulations.

3. Results and discussion

Several cases are presented in this paper to validate the VRANS implementation in the numerical model with both two- and three-dimensional scenarios and investigate the wave-porous structure interaction. The following sections present the numerical results from simulating the experiments carried out by Liu et al. (1999) for dam break against a porous medium, solitary wave interaction with a porous abutment by Del Jesus, Lara, and Losada (2012), regular wave interaction with a porous abutment by Lara, Del Jesus, and Losada (2012) and regular wave interaction with a multilayered breakwater section by Arntsen et al. (2003).

3.1. Dam break

The two-dimensional study with a dam break on a porous medium made of crushed rocks by Liu et al. (1999) is simulated. The experimental data provide the free surface evolution both inside and outside the porous medium. In the experiments, crushed rock with a median grain size $d_{50} = 0.0159$ m and porosity n = 0.49 is placed in the tank in the form of a porous dam with a length of 0.29 m and a height of 0.58 m. A reservoir of water is created beside the porous dam with a length of 0.28 m and the height of the reservoir is set to 0.35, 0.25 and 0.14 m in the different trials. The reservoir is separated from the porous dam with a 0.02 m thick gate which is operated manually. In addition, 0.025 m layer of water is allowed at the bottom of the tank. The numerical setup is the same as the experimental setup and is illustrated in Figure 2. A grid size of dx = 0.005 m is used for this simulation.

The resistance coefficients α and β are calibrated by completing a simulation matrix, where the 2 coefficients are varied as $\alpha = [500, 650, 750, 1000, 2500]$ and $\beta = [1, 1.5, 2, 2.2, 3]$. The best agreement between the numerical and experimental results is found for the combination $\alpha = 650$ and $\beta = 2.2$. The simulated evolution of the flow through the porous dam is compared to the experimental data and presented in Figure 3. In the initial stage of the dam break, there is a small disagreement between the experimental and numerical results, especially inside the porous medium. This is due to the difference in the initial flow in the experiments and in the numerical model. In the experiments, the water is blocked with a gate and opening of the gate results in water being rushed to the porous medium. The impact of the water leads to a small upward jet on the surface of the porous medium (Liu et al. 1999). The gate is opened manually in the experiments within a finite duration (0.1 s) and the water close to the bottom to moves earlier than the water at free surface. In the simulations, the dam break occurs by an instantaneous release of the water column. Thus, the entire water column is set into motion at once and explains the small difference in the calculated water surface and the observed values at t = 0.2 s and 0.4 s in Figure 3(b,c) respectively.

In Figure 3(d–f), the flow through the porous medium is mainly due to the pressure difference and the agreement gets better as the time progresses. Figure 3(g–j) represents the situation where the water has reached the right wall and is reflected back. This reflected wave breaks again on the porous medium and this is captured well in the numerical model. Figure 3(k,l) represents the period after breaking where water on the right side oscillates a little while water from the left side is still seeping through the porous medium. The flow regime corresponds to a transition between Forchheimer and a fully turbulent flow regime and is very well represented by the model.

3.2. Wave interaction with a porous abutment

A three-dimensional scenario with the interaction of waves with a porous abutment investigated by Lara, Del Jesus, and Losada (2012) is simulated in this section. The domain is 18.2 m long, 8.6 m wide, and 1.0 m high. A porous structure 4.0 m long, 0.5 m wide and 0.6 m high in a water depth d = 0.4 m is built using a metallic mesh filled with granular material. The median particle size of the granular material $d_{50} = 0.015$ m and porosity n = 0.51. The structure is placed perpendicular to the direction of wave propagation at a distance of 10.5 m from the wavemaker. The numerical setup is the same in the experiments and is illustrated in Figure 4. As in the experiments, no beach is used in the numerical wave tank. Since the d_{50} and n values, in this case, are similar to the values for the dam break case in the previous section, the same values of $\alpha = 650$ and $\beta =$ 2.2 are selected for the simulations in this section as well. A grid size of dx = 0.025 m is used in the simulation. The



Figure 2. Dam break-setup for physical experiments.



Figure 3. Free surface in the simulations and experiments for flow passing through porous dam made of crushed rock with $d_{50} = 0.0159$ m and n = 0.49 represented by a = 650 and $\beta = 2.2$.



Figure 4. Numerical setup for porous abutment in wave basin, the location of the pressure gauges is shown in the inset figure.

free surface elevation is recorded at 15 locations in the wave basin and pressure gauges are placed at six locations on the porous structure. The exact positions of wave gauges and pressure gauges are listed in Table 2.

3.2.1. Solitary wave interaction with a porous abutment

First, the interaction of a solitary wave of height H = 0.09 m with the porous abutment is simulated. In the absence of a beach, the solitary wave is reflected from the end of

the domain and propagates toward the wavemaker, interacting with the porous structure for a second time. The free surface elevations calculated numerically at the different locations listed in Table 2 are compared to the experimental results in Figure 5. In Figure 5(a) the incident wave propagating toward the end of the domain and the reflected wave traveling toward the wavemaker at WG1 are seen at t = 4 s and t = 15 s, respectively. The free surface elevation at WG2 in Figure 5(b) shows the incident wave, the partially reflected wave from the structure and

 Table 2. Location of the wave and pressure gauges in the numerical wave tank.

Wave Gauge	<i>x</i> (m)	<i>y</i> (m)	Pressure Gauge	<i>x</i> (m)	<i>y</i> (m)	<i>z</i> (m)
WG1	5.0	7.0	PG1	10.5	3.89	0.11
WG2	5.0	1.0	PG2	10.5	3.69	0.25
WG3	9.5	1.0	PG3	10.89	4.0	0.11
WG4	9.5	3.0	PG4	10.69	4.0	0.25
WG5	10.0	4.0	PG5	11.0	3.70	0.11
WG6	11.0	4.5	PG6	11.0	3.9	0.25
WG7	11.5	3.5				
WG8	12.5	2.5				
WG9	12.0	1.5				
WG10	11.5	0.5				
WG11	13.0	0.5				
WG12	13.5	4.0				
WG13	15.0	2.0				
WG14	12.5	7.0				
WG15	9.5	7.5				

the reflected wave from the end of the domain after interacting with the porous abutment. WG3 and WG4 in Figure 5(c,d) respectively, show a secondary crest beside the primary crest as they are placed just 1 m from the face of the porous abutment and are quickly affected by the

partially reflected wave. The reflected waves from the end of the domain are partially transmitted and seen as the smaller peaks around t = 15 s. Wave gages WG5, WG6, and WG7 are placed around the seaward edge of the porous structure. The reduction of the incident wave height as it crosses the structure is apparent in the visual comparison of the first peaks in Figure 5(e,g) corresponding to WG5 and WG7, respectively. Figure 5(h-k) presents the free surface elevations at WG8-WG11, respectively, which are on the leeward side of the porous abutment. The wave crest calculated at these locations correspond to the incident wave that is damped by the porous structure. The second crest calculated at these locations corresponds to the reflected wave from the end of the domain. WG12 is located 2.5 m behind the seaward edge of the abutment and the incident wave consists of the unaffected part of the wave and the part transmitted through the abutment. In addition, WG12 is also fully exposed to the reflected wave from the end of the domain as seen in Figure 5(I). The free surface elevation 3 m behind the



Figure 5. Numerical and experimental results (Lara, Del Jesus, and Losada 2012) for the free surface elevation for solitary wave interaction with a porous abutment.

structure at WG13 in Figure 5(m) shows a damped incident wave after interaction with the structure, the reflected wave from the end of the domain followed by the partially re-reflected waves from the structure. The locations WG14 and WG15 are exposed to a mostly undisturbed incident and the reflected waves along with some radiated waves from the structure as seen in Figure 5(n,o) respectively. The numerical results agree well with the experimental results both in phase and amplitude of the incident and reflected waves at the different locations.

A grid convergence study is carried out by repeating the simulation with grid sizes dx = 0.03 m, dx = 0.05 m, and 0.075 m. The numerical results for the free surface elevation at locations WG2 and WG13 are presented in Figure 6. The two wave gauges are located on either side of the abutment and receive most of the wave action from both incident and reflected waves. It is seen that the free surface elevations for both WG2 and WG13 in Figure 6(a,b) are similar for all the grid sizes used and exactly the same for dx = 0.03 m and dx = 0.025 m. Thus, the results presented using dx = 0.025 m are grid-independent.

In order to demonstrate the improved numerical results obtained with the current approach, a comparison with the numerical results from Lara, Del Jesus, and Losada (2012) for the free surface elevation around the porous structure is presented along with the experimental data in Figure 7. Itis seen that the reflected wave at WG7 is better represented in the current model in Figure 7(a). The free surface elevations at WG10 in Figure 7(b) are similar in the current work and previously presented numerical results. At the most onshore location behind the porous abutment, WG13, the current model provides a better representation of both the amplitude and phases of the wave crests in Figure 7(c). At WG15 in Figure 7(d), the current model shows better agreement with the experimental data compared to previous numerical results.

The pressure calculated at the six different locations in the porous abutment are compared to the experimental data in Figure 8. Three distinct peaks are seen in each of the figures due to the incident wave, the transmitted wave, and the reflected wave. PG1 and PG2 are placed on the seaward side and the highest peaks are seen to occur when the solitary wave is incident on the abutment in Figure 8(a,b). The pressures inside the abutment measured at PG3 and PG4 are presented in Figure 8(c,d), respectively, and the three peaks are seen to be of comparably similar magnitudes. On the leeward side at PG5 and PG6, the highest peaks result from the wave reflected from the end of the domain as seen in Figure 8(e,f). The numerical results show a good agreement with experimental data for the measured pressures as well.

The interaction of the solitary wave with the porous abutment in the numerical wave tank is presented in Figure 9. The solitary wave approaching the porous abutment at t = 5.0 s is shown in Figure 9(a). At t =6.5 s, the incident wavefront is separated by the abutment and the transmitted wave in the unblocked region is seen in Figure 9(b). Figure 9(c) shows the wave transmitted through and beyond the abutment approach the end of the domain and the first partially reflected wave from the abutment traveling toward the wavemaker at t = 9.0 s. The transmitted wave is reflected back toward the abutment at t = 10.0 s in Figure 9(d). The wave reflected from the end of the domain interacts with the porous abutment again at t = 13.5 s in Figure 9(e). Here, the wavefront is separated by the abutment for the second time resulting in transmitted waves through and beyond the abutment along with a second partially reflected wave. The first partially reflected wave is re-reflected from the wavemaker and reaches the abutment at t = 16.5 s, while the second partially reflected wave is near the end of the domain in Figure 9(f). The interaction processes presented in this figure can be easily identified with the different peaks observed at the different locations in Figure 5.

In order to demonstrate the satisfaction of the continuity at the interface between the water and the porous media, the pressure and horizontal velocity time series on either side of the weather side boundary of the porous abutment at PG8 (10.49, 3.90, 0.25) and PG9 (10.51, 3.90, 0.25) are presented in Figure 10. It is seen that the computed pressures and velocities across the boundary are the same and the continuity condition is satisfied. In addition, the horizontal velocity profiles over the water depth far



Figure 6. Grid convergence study for solitary wave interaction with the porous abutment.



Figure 7. Comparison numerical results with the current approach with numerical results from Lara, Del Jesus, and Losada (2012) and experimental data for solitary wave interaction with a porous abutment.



Figure 8. Numerical and experimental (Lara, Del Jesus, and Losada (2012)) pressure in the structure for solitary wave interaction with a porous abutment.



Figure 9. Free surface elevation in the numerical wave tank for solitary wave interaction with a porous abutment.



Figure 10. Numerical results for the pressure and horizontal velocity on either side of the porous interface at PG8 and PG9 for solitary wave interaction with a porous abutment.

from the abutment (x = 10.0 m), just in front of the abutment (x = 10.49 m), just inside the abutment (x = 10.51 m) and at the center of the abutment (x = 10.75 m), close to the head of the abutment at y = 3.90 m, middle of the abutment at y = 2.00m and close to the wall at y = 0.50 m at t = 6.75s are presented in Figure 11. The solitary wave crest is an incident on the porous abutment at this instance in the simulation. The horizontal velocity profile shows the highest amplitude at the far-field location at x = 10.0 m in Figure 11(a), due to the fact that this location is closer to the head of the abutment and experiences the least resistance to the flow. The horizontal velocity profiles at x = 10.0 m are identical for y = 2.0 m and y = 0.50 m in Figure 11(b,c) respectively. Also, it is seen that the maximum horizontal velocity is damped as wave travels from the far-field location at x = 10.0 m toward the center of the porous abutment at x = 10.75 m at all three locations along the length of the porous abutment.

3.2.2. Regular wave interaction with a porous abutment

The interaction of the porous abutment with waves is further studied with periodic waves in the numerical wave tank. As in the experiments by Lara, Del Jesus, and Losada (2012), waves of period T = 4.0 s and height H = 0.09 m are generated using cnoidal wave theory. The values for the grid size dx = 0.025 m and the porous media resistance coefficients a = 650 and $\beta = 2.2$ are retained from the solitary wave simulation above. The free surface elevations calculated at the different locations listed in Table 2 are compared with the experimental results from Lara, Del Jesus, and Losada (2012) in Figure 12. The present scenario with regular waves involves more interactions compared to the solitary wave scenario due to the periodic nature of the incident waves. First, the wave is partially reflected and transmitted through and beyond the abutment. The transmitted wave is reflected from the end of the domain and interacts with the following



Figure 11. Horizontal velocity profiles over the water depth outside and inside the porous abutment for an incident solitary wave at various x - locations for different locations along the porous abutment.

--- Lara et al. (2012)

Numerica

0.10



Lara et al. (2012)

Numerica

0.10

Figure 12. Numerical and experimental results (Lara, Del Jesus, and Losada 2012) for the free surface elevation regular wave (H = 0.09 m, T = 4.0 s) interaction with a porous abutment.

wave. This transformed wave then interacts with the abutment again, resulting in further transmission toward the wavemaker and partial reflection toward the end of the domain. This process repeats itself over the course of the simulation resulting in complex wave patterns. At locations close to the abutment on the upstream side, several peaks in the wave crests are observed as in Figure 12(b-d). At locations on the leeside of the abutment, cancellation of the transmitted and reflected waves result in periods of near-zero elevations as seen in Figure 12(h-k). The complex wave-wave and wave-structure interactions are well accounted for in the model and the numerical results are seen to be in good agreement with the experimental data at all locations.

Lara et al. (2012)

Numerica

0.10

A grid convergence study is carried out by repeating the simulation with grid sizes dx = 0.03 m, dx =0.05 m and 0.075 m. The numerical results for the free

surface elevation at locations WG2 and WG13 are presented in Figure 13. The two wave gauges are located on either side of the abutment and placed such that they receive most of the wave action from both incident and reflected waves. It is seen that the free surface elevations for both WG2 and WG13 in Figure 13(a,b) are similar for all the grid sizes used and exactly the same for dx = 0.03 m and dx = 0.025 m. Thus, the results presented using dx =0.025 m are grid-independent.

The numerical results for the free surface elevation at selected locations around the porous abutment using the current model are compared with the numerical results from Lara, Del Jesus, and Losada (2012) along with the experimental results in Figure 14. The free surface elevations at WG7 in Figure 14(a) show that the current approach agrees better with the experimental data whereas spurious wave crests are seen in the



Figure 13. Grid convergence study for periodic wave interaction with the porous abutment.



Figure 14. Comparison of numerical results with the current approach with numerical results from Lara, Del Jesus, and Losada (2012) and experimental data for solitary wave interaction with a porous abutment.

previous numerical results. At WG10 in Figure 14(b), the current model represents every wave crest right behind the porous abutment, where both transmitted wave through the porous abutment and the reflected wave from the end of the domain are seen. A change in phase and amplitude, with spurious crests, is seen at WG13 in the previous numerical results, whereas the current model follows the experimental observations in Figure 14(c). At WG15 in Figure 14(d), the current results

show good agreement with the experimental data whereas previous results show an increase in the wave crest elevation over time.

The pressures calculated at the six different locations in the porous abutment listed in Table 2 are compared with the experimental results in Figure 15. The largest pressures are measured on the upstream side of the abutment at PG1 and PG2 shown in Figure 15(a,b). The pressures are slightly reduced inside the abutment as



Figure 15. Numerical and experimental (Lara, Del Jesus, and Losada (2012)) pressure in the structure for regular wave interaction with a porous abutment.

seen in Figure 15(c,d). On the leeside of the abutment, the pressures are initially small and increase when the reflected waves from the end of the domain are incident on the abutment in Figure 15(e,f). The numerical results are seen to agree well with the experimental data in both phase and amplitude, showing that the model represents the physics involved in the flow through porous media well.

The periodic wave interaction with the porous abutment in the numerical wave tank is presented in Figure 16, following the propagation of the second wave crest along the wave tank. The incidence of the second wave crest on the porous abutment at t =9.5 s with the partially reflected wave and the transmitted wave is shown in Figure 16(a). At t = 10.0 s, the partially reflected wave is traveling toward the wavemaker and the transmitted wave is propagating toward the end of the domain in Figure 16(b). Figure 16(c) shows the interaction of the partially reflected wave with the next wave crest upstream of the abutment at t = 11.0 s. The transmitted wave interacts with the crest of the first wave crest reflected from the end of the domain downstream of the abutment in Figure 16(d) at t = 11.5 s. The third wave crest is incident on the abutment at t = 12.5 s in Figure 16(e). Here the part of the wavefront toward the landfast side of the abutment is slightly damped due to its interaction with the partially reflected wave. The first wave crest reflected from the end of the domain is incident on the lee side of the abutment while the second crest is at the end of the domain. Figure 16(f) shows the incidence of the third wave crest on the abutment, while the second wave crest travels toward the abutment after reflecting from the end of the domain at t = 13.5 s. The interaction processes presented in this figure show the additional complexities in the hydrodynamics due to the periodic waves in comparison to the solitary waves and the processes visualized in this figure can be correlated to the wave elevations at the different locations discussed in Figure 12.

3.3. Wave interaction with a rubble mound breakwater

In this section, a rubble mound breakwater is simulated considering the porous media flow through the armor, filter, and core layers in a two-dimensional numerical wave tank. The numerical results for the pore pressure are compared to the data from the experiments conducted at the SINTEF/NTNU Trondheim hydraulic laboratory by Arntsen et al. (2003). The rubble mound breakwater model has a front slope of 1: 1.25, 3 m long and a crest height of 1.1 m. The core is made of wellgraded sand with $d_{50} = 0.0028$ m and porosity n = 0.414. The filter layer is 0.10 m thick and made of gravel with $d_{n50} = 0.02$ m and porosity n = 0.33. The armor layer is composed of one layer of stones with median weight W_{50} of about 1 kg. The median particle size is $d_{n50} = 0.07$ m and the porosity is n = 0.30. Inside the breakwater, pressure cells are installed to measure the pore pressure variations. The rubble mound breakwater model is illustrated in Figure 17 along with the position of the pressure cells inside the breakwater. The locations of the pressure cells used in the experiments are listed in Table 3. Pore pressure cells P1 and P5 are placed at the boundary between the armor and the filter layers. P2 and P6 are placed at the boundary



Figure 16. Free surface elevation in the numerical wave tank for periodic wave (H = 0.09 m, T = 4.0 s) interaction with a porous abutment.



Figure 17. Illustration of the rubble mound breakwater model with three layers and the location of the pressure probes.

between the filter and the core layers. P3, P4, P7, and P8 are placed in the core. The pressure cells P1, P2, P3, P4 are placed along z = 0.25 m above the bottom of the wave tank, and the pressure cells P5, P6, P7, and P8 are placed at a higher elevation of z = 0.45 m above the bottom of the tank. This provides further insight into the wave-porous structure interaction problem. Also, these measurements provide crucial data to validate the model for porous media flow through complex geometry.

The simulations are carried out in a numerical wave tank that is 12 m long and 1.4 m high with a grid size of dx = 0.005 m. The toe of the breakwater is placed x = 7m away from the wave generation boundary (Figure 18). The resistance coefficients a and β are defined based on the calibrated values from the previous sections and from literature (Troch 2000). The material characteristics and the resistance coefficients of the different layers of the breakwater are presented in Table 4. Regular waves with H = 0.22 m, T = 1.5 s are generated using the 5thorder Stokes theory in a water depth d = 0.7 m.

The pore pressures calculated in the simulations at the locations listed in Table 3 are compared with the pore pressures measured at these locations in the experiments in Figure 19. The peak pore pressures at z = 0.25 m above the bottom of the tank are as follows: At location P1, the boundary between the armor and filter layers, the peak pore pressure is calculated to be 525 Pa, while a pressure of 460 Pa is measured in the experiments with an overestimation of 14% as shown in Figure 19(a). At location P2, the boundary between the filter and core layers at z = 0.45 m in Figure 19(b), the numerical and measured values for the peak pore pressure are seen to be 470 Pa and 500 Pa, respectively. The numerical model overestimates the peak pore pressure by about 6%. The deviations at these locations can be attributed to the averaged bulk representation of the porous resistance in the model compared to the instantaneous measurements. In addition, the locations are the boundary between two different porous layers and the numerical values for pressure are further averaged depending on the porous resistance in each of the neighboring cells. Inside the core layer, at locations P3 and P4 in Figure 19(c) and (19d), the difference in the numerical results and the measurements are about 7% and 3%, respectively. The following observations are made for the peak pore pressures at the locations closer to the free surface at z =0.45 m. The numerically calculated peak pore pressure at location P5 at the boundary between the armor and filter layers is 530 Pa, and is within 1% of the measured values as seen in Figure 19(e). At the

Table 3. Position of pressure cells inside the rubble mound breakwater.

Tuble bille	table of roshion of pressure cells inside the rubble mound breakfutch.							
Cell	PG1	PG2	PG3	PG4	PG5	PG6	PG7	PG8
<i>x</i> (m)	7.45	7.525	7.90	8.20	7.70	7.78	7.90	8.20
<i>z</i> (m)	0.25	0.25	0.25	0.25	0.45	0.45	0.45	0.45



Figure 18. Setup for Rubble mound breakwater in the NWT.

 Table 4. Resistance coefficients for different layers in the breakwater.

Layer	$d_{50}(m)$	n (-)	a (-)	β(-)
Armor	0.0596	0.3	100	1.1
Filter	0.02	0.33	600	1.1
Core	0.0028	0.414	50	2

boundary between the filter and core layers at location P6 in Figure 19(f), the numerical peak pore pressure is 520 Pa and within 2% of the measured values. In the core layer at locations P7 and P8 in Figure 19(g,h), values for the numerical peak pore pressure are 470 Pa and 420 Pa, respectively. The numerical values are within 1% of the measurements. Overall, the numerical model calculates the pore pressures atdifferent locations with good accuracy. The maximum deviation between the measurements and the numerical calculations is of the order of the pressure exerted by water in one grid cell, that is 0.005 m.

5

1000

-1000

P (Pa)

Arntsen et al. (2003)

15

Numerical

10

The wave interaction with the porous rubble mound breakwater over half a wave period is presented in Figure 20. The wave crest approaching the breakwater is shown in Figure 20(a). The wave crest impacts the armor layer in Figure 20(b) and the truncation of the wave crest due to the dissipation of a part of the incident wave energy is seen. The wave run up on the breakwater and the seepage into the breakwater is seen in Figure 20(c) and the process of wave run down begins in Figure 20(d). The effect of the porosity imposed by the VRANS formulation to represent the flow through three different porous layers of the breakwater is clearly seen from the velocity contours in Figure 20. The reduction of the velocity contours and the lower values of the pore pressures measured in the core layer demonstrate that most of the wave energy is dissipated within the armor and filter layers of the breakwater and a small amount of flow seeps into the core layer.

--- Arntsen et al. (2003)

15

20

Numerical

10



1000

-1000

ò

5

P (Pa) 0

20

Figure 19. Comparison of pressure measurements for pressure gauges inside rubble mound breakwater for regular waves. Red lines indicate numerical model results and black lines represent experimental results.



Figure 20. Wave interaction with a rubble mound breakwater simulated with three porous layers.

4. Conclusion

The open-source CFD model REEF3D is validated for the wave-porous structure interactions with the newly implemented VRANS method. A brief overview of the derivation of the VRANS equations is presented based on the formulations derived by Jensen, Jacobsen, and Christensen (2014). The model uses higher-order schemes for convection and temporal discretization on a Cartesian grid along with the level set method for the free surface.

The numerical model is validated with two- and three-dimensional simulations for different flow conditions. The flow through a porous medium made of crushed rock is calculated and the free surface evolution is compared to the experimental data from Liu et al. (1999) in a 2D simulation. The numerical results agree with the experimental observations after the first 0.4 s due to the small difference in the dam break mechanism. The interaction of solitary and regular waves with a uniform porous abutment is studied in threedimensional simulations. The numerical results for the free surface at various locations in the wave tank and the pore pressures at different locations in the porous abutment are compared with experimental data from Lara, Del Jesus, and Losada (2012) and a good agreement is seen for both cases. As the properties of the porous medium are the same for the dam break scenario and the porous abutment, the same resistance coefficients are used in the three simulations. The numerical results consistently match the experimental observations, demonstrating the reliability of the numerical model in the prediction of flow through porous media. The current results show a significantly better agreement to the experimental data for solitary and regular wave interaction with a porous abutment compared to numerical results in the current literature.

The numerical model is then used to simulate wave interaction with a rubble mound breakwater with three layers with different material properties. The measured pore pressures in the different layers by Arntsen et al. (2003) are compared to the numerical results. The difference between the numerically calculated pore pressures and the measured values at all the locations closer to the crest of the breakwater is within 1%. A difference of 14% is seen at the boundary between the armor and filter layers at the location closer to the bed. This corresponds to the pressure due to a water height of 0.005 m. At other locations closer to the bed, the pressure values are within 7% of the measurements. The dissipation of the ident wave energy by the rubble mound breakwater with three porous layers is well represented by the numerical model. Overall, the numerical model demonstrates that it can reliably predict the flow through porous media and represent the fluid-structure interaction in a physical manner.

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