

1 **Total Experimental Uncertainty in Hydrodynamic Testing of a Semisubmersible Wind Turbine,**
2 **Considering Numerical Propagation of Systematic Uncertainty**

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13 **Abstract**

14 Quantifying the uncertainty in experimental results is a critical step in properly validating numerical
15 simulation tools for designing floating wind turbines; without a good understanding of the experimental
16 uncertainties, it is impossible to determine if numerical simulation tools can capture the physics with
17 acceptable accuracy. Recent validation studies suggest that the wave-induced, low-frequency surge and
18 pitch motions of semisubmersible-type floating wind turbines are consistently underpredicted by
19 numerical simulations, but it has not been possible to state whether or not this underprediction is within
20 the level of experimental error. In the present work, previously assessed systematic uncertainty
21 components in hydrodynamic tests of the OC5-DeepCwind semisubmersible are propagated to response
22 metrics of interest using numerical simulation tools, and combined with the random uncertainty to obtain
23 the total experimental uncertainty. The uncertainty in the low-frequency response metrics is found to be
24 most sensitive to the system properties (e.g., mooring stiffness and center of gravity), but also the wave
25 elevation. The results of the present study suggest that the underprediction of the low-frequency
26 response behavior observed in previous validation studies is larger than the experimental uncertainty.

27 **Keywords:** Floating Offshore Wind, Uncertainty Analysis, OC5, Validation, Nonlinear Wave Mechanics

28 1 Introduction

29 Floating wind turbines (FWTs) represent a growing area of both academic and industrial interest, and a
30 wide range of numerical tools have been developed to predict their responses in wind and waves.
31 Recently, participants in the international Offshore Code Comparison Collaboration, Continued, with
32 Correlation (OC5) project attempted to validate models of a floating semisubmersible tested in the
33 offshore basin at MARIN (in May 2013) by the DeepCwind consortium (Goupee et al. 2014). Although
34 state-of-the-art tools captured some of the dynamics and loads of the complex floating wind turbine,
35 there were persistent differences between the simulated results and measurements, the reasons for
36 which could not be ascertained.

37 The discrepancies are exemplified by an under-prediction of the ultimate and fatigue loads across multiple
38 load cases, which were shown to be dominated by the under-prediction of the loads at the pitch and
39 tower natural frequencies (Robertson et al. 2017). Similar discrepancies in the low-frequency response of
40 other model-scale semisubmersible platforms for offshore wind have also been observed (Cermelli
41 and Roddier 2005, Philippe et al. 2013, Berthelsen et al. 2016). In order to assess whether or not the
42 observed differences between numerical and experimental results are meaningful, an assessment of the
43 level of experimental uncertainty in the response behavior needs to be determined.

44 To that end, additional testing of the semisubmersible structure from the OC5 study (in a simplified
45 configuration) was carried out at MARIN through the MaRINET2 grant. These simplified tests were aimed
46 toward better understanding the hydrodynamic loading and assessing uncertainty in the test campaign.
47 The generic open-access design (OC5-DeepCwind floating semisubmersible) was tested at 1/50 scale with
48 the same floating substructure as was examined in OC5, but with a rigid tower, a mass representing the
49 rotor-nacelle assembly, and with a simplified soft-spring mooring system representing the linear stiffness
50 of the original catenary configuration. The wind turbine and flexible tower were replaced by rigid
51 components to limit uncertainty sources and better focus on the hydrodynamic loading on the structure.
52 Due to the limited testing time in the basin, a single configuration was considered, and a limited number
53 of wave conditions were tested (Gueydon 2017). Extensive repetition tests were included in the test
54 matrix to assess the random uncertainty in the experiment.

55 Response metrics, low-dimensional representations of the important features of the time series of results,
56 are used to represent the results and the associated uncertainty. The experimental uncertainty originates
57 from uncertainties in the excitation of the system and the properties of the test specimen, and the

58 accuracy and precision of the measurement equipment. Several standards provide guidance on
59 uncertainty assessment, such as the International Standards Organization (ISO, 1993), American Society
60 of Mechanical Engineers (ASME, 2013), and The International Towing Tank Conference (ITTC, 2008). Here,
61 we apply the ASME terminology, categorizing the sources of uncertainty as either random or systematic.
62 Systematic uncertainties may result in an unknown bias in the test, while random uncertainties result in
63 randomly varying uncertainties which can be measured through repetition tests.

64 The contributions to the experimental uncertainty in the new set of tests were identified and documented
65 in previous work (Robertson et al. 2018). Among the main findings, it was shown that the uncertainty in
66 the wave elevation was small, and was dominated by the random uncertainty. It should be noted,
67 however, that the uncertainties in the wave loads (not measured) may be larger than the uncertainties in
68 the wave elevation. The physical properties of the model itself were found to have more significant
69 systematic uncertainties, and the measurement cable contributed significantly to the uncertainty in the
70 mass and in the center of mass. The measurement of motion responses was precise, while the tension
71 measurements had relatively high random uncertainty.

72 The present work seeks to identify the total uncertainty of the response metrics of interest. This is
73 accomplished by first propagating the systematic uncertainties to the response metrics through
74 numerical simulations, and then combining with the calculated random uncertainty. Three state-of-the-
75 art simulation tools – applied by four different users, and considering several modeling approaches – were
76 used to assess the consequences of changes in the input parameters (corresponding to the systematic
77 uncertainty levels) on responses such as the low-frequency surge and pitch motions and wave-frequency
78 surge and pitch motions. In the remainder of the paper, the model tests and response metrics of interest
79 are briefly described (Sections 2 and 3). Next, the uncertainty sources identified by Robertson et al. (2018)
80 are summarized, and the most important of these are identified (Section 4). The methodology for
81 propagating systematic uncertainties is explained, and the total uncertainty is examined (Sections 5 and
82 6).

83 2 Test Description

84 The floating semisubmersible model consisted of the existing MARIN model 9697, whose geometry
85 corresponds to the DeepCWind semisubmersible floater (Goupee et al. 2012) at 1/50 scale, and a rigid
86 aluminum tower designed to mimic the mass and inertia of the NREL 5 MW wind turbine tower and rotor-
87 nacelle-assembly (Jonkman et al. 2009, Jonkman 2010). A brief overview of the model setup (Figure 1) is
88 given here; additional details may be found in Robertson et al. 2018. The test setup and all results are
89 presented at full scale, following Froude scaling. The difference in density between sea water (1025 kg/m^3)
90 and fresh water in the basin (998.6 kg/m^3) is accounted for in the scaling of masses, inertias, forces,
91 moments, and derived quantities.

92 A simplified mooring system was designed and constructed for the new tests. Three mooring lines,
93 consisting of a soft spring and rigid wire, were attached to the model. A pulley system was used such that
94 the spring could be vertical and dry, while the anchor positions were low enough that the surge-pitch
95 coupling from the mooring system was similar to the original catenary system.

96

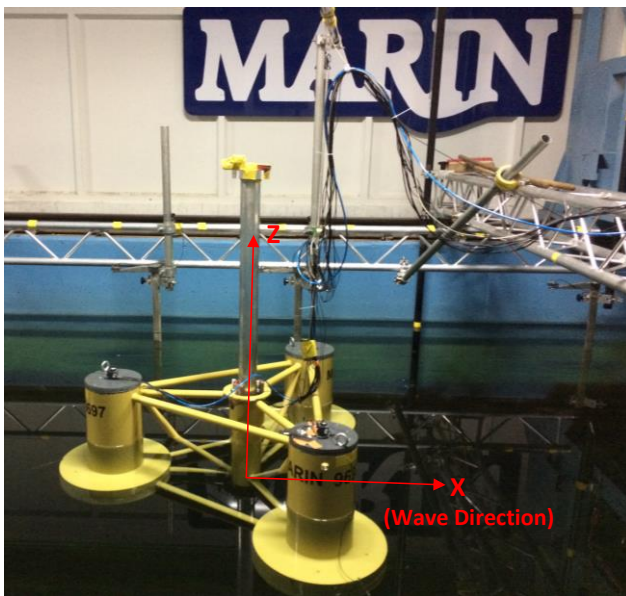


Figure 1: Floating test set-up. Waves propagate from left to right in this figure, and positive surge motion is defined in the same direction as the wave propagation (Image by: Amy Robertson).

97 **2.1 Model Properties**

98 The main characteristics of the floater geometry are shown in Table 1, while the hydrodynamic properties
99 and mass properties are given in Table 2 and Table 3, respectively. The mooring system, which included
100 thin wires attached to springs, is described in Table 4.

101 *Table 1: Key geometric parameters*

GEOMETRIC PROPERTIES	
Center column diameter [m]	6.5
Side column diameter [m]	12.0
Base column diameter [m]	24.0
Draft [m]	20.0
Base column height [m]	6.0
Side column freeboard [m]	10.0
Tower top height over keel [m]	77.3

102

103 *Table 2: Hydrodynamic properties*

HYDRODYNAMIC PROPERTIES	
Water depth [m]	180.0
Water density [kg/m ³]	1025.0
Displaced volume [m ³]	14040

104

105 *Table 3: Masses and inertia of entire system (tower+platform). CG: center of gravity.*

MASSES/INERTIAS	
Overall system mass [kg]	1.4196E+7
Overall system CG (z) [m below SWL]	7.53
Ixx abt system CG [kg-m ²]	1.2898E+10
Iyy abt system CG [kg-m ²]	1.2851E+10
Izz abt system CG [kg-m ²]	1.4189E+10

106

107 *Table 4: Mooring line properties. EA: Young's modulus multiplied by cross-sectional area.*

MOORING LINES	
Line angle [deg]	55.5
EA [N]	2.7106E+6
Unstretched line length [m]	55.432
Preload [kN]	1122.5

Mooring stiffness [kN/m]	48.9
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108

109 When modelling the system numerically, we strived to use the properties of the system as measured,
 110 where possible. For a floating system, the first step is to ensure that the system is in equilibrium for the
 111 prescribed values of the draft, mass, mooring tensions, and displaced water volume. For this test, we
 112 directly measured the draft, mass, and tensions. The displaced water volume can be calculated from the
 113 geometry, but since it is not directly measured, we considered this property as the most unknown. We
 114 did not tune the other properties mentioned, but prescribed the displaced water volume such that the
 115 system was in equilibrium (Table 5).

116

Table 5: Balance of Vertical Forces

BALANCE OF VERTICAL FORCES	
Total vertical mooring force [N]	-1.9074E+06
Total gravity force [N]	-1.3922E+08
Displacement needed for equilibrium [m³]	14040
Buoyancy Force [N]	1.4113E+08
SUM [N]	0.0000E+00

117

118 2.2 Test Matrix

119 The tests in this campaign included a hammer test, free decay tests and wave excitation tests. Only the
 120 wave excitation tests are of interest here, and are summarized in Table 6. As shown, multiple repetitions
 121 were carried out for the model in waves, which will be used to assess the random uncertainty in the
 122 response behavior. The repetitions were performed with the same wave realization, with the goal of have
 123 having the identical wave time series.

124

Table 6: Test matrix – wave cases.

Test Name	Waves	Number of repetitions
Regular wave 1	H=7.1 m, T=12.1 s	5
Regular wave 2	H=4 m, T=9 s	2
White noise	Hs=7.1 m, T=6-26 s	2
Irregular wave	Hs=7.1 m, Tp=12.1 s	5

125

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126 3 Response Metrics

127 The objective of the larger validation campaign related to these experiments is to better understand the
128 ability of simulation tools to predict the response of the OC5-DeepCwind semisubmersible to
129 hydrodynamic loading, especially the low-frequency (resonant) responses in pitch and surge. To assess
130 the capabilities of the tools in this area, response metrics were identified to represent these important
131 physical quantities of interest. The response metrics are scalar values that can be computed from the time
132 series results from either simulations or experiments. A simulation tool that can reproduce the response
133 metrics within the obtained uncertainty bounds can then be considered validated.

134 The response metrics in the present work focus on the surge, heave, and pitch responses of the
135 semisubmersible, in particular: the mean response in surge, and the wave-frequency and low-frequency
136 responses in all three degrees of freedom. The response metrics are chosen with the objective of
137 representing these different response components, rather than selecting metrics that are useful for
138 design (such as the 90th percentile maximum 3-hour motions), but do not distinguish among different
139 frequency ranges.

140 The response metrics in the present work are:

- 141 M1. **RAO**: the response amplitude operator (RAO) in surge, heave, and pitch at 6 discrete frequency
142 points within the wave energy range;
- 143 M2. **PSD Sum, Low Frequencies**: the integral of the power spectral density (PSD) of surge and pitch
144 motions over the low-frequency range;
- 145 M3. **PSD Sum, Wave Frequencies**: the integral of the PSD of surge and pitch motions over the wave-
146 frequency range and
- 147 M4. **Mean Surge Offset**.

148 For all of the metrics, only a limited time window of the analysis is considered (Table 7), in an attempt to
149 focus on data after start-up transient behavior and also address the effect of reflected waves. The irregular
150 wave window consists of the last three hours (after reflections are established), while the regular wave
151 window includes 10 minutes of data once the ramp in the waves has passed but before any reflections
152 arrive from the beach or wavemaker. Furthermore, all of the time series are resampled with a time step
153 of 0.1 s prior to computing any metrics. Response metrics M2 and M3 are only computed for the irregular
154 wave cases.

155

Table 7: Time windows for calculation of response metrics

Wave	Start of window	Duration of window
Regular wave 1	600 s	600 s
Regular wave 2	1000 s	600 s
White noise	1870 s	10800 s
Irregular wave	1870 s	10800 s

156

157 Metric M1, the RAO, is defined as the amplitude of the response divided by the amplitude of the incoming
 158 wave at a given frequency. Six discrete frequencies are considered for the RAO calculations, as shown in
 159 Table 8.

160

Table 8: Wave frequencies for RAO calculations

Frequency Pt.	Frequency	
1	0.065 Hz	
2	0.075 Hz	
3	0.0826 Hz	Frequency of regular wave 1
4	0.095 Hz	
5	0.105 Hz	
6	0.1105 Hz	Frequency of regular wave 2

161

162 The algorithm applied for computing the RAO, denoted $H(\omega)$, is based on the cross spectral density:

163

$$H = \frac{yu^*}{uu^*}$$

164 where u and y are the Fourier transforms of the wave elevation and the motion response, respectively,
 165 and the asterisk indicates the complex conjugate.

166 The integrals of the PSDs of the response (referred to as "PSD sums" – metrics M2 and M3) are chosen to
 167 capture frequency-dependent responses both in and outside the wave frequency range in irregular sea
 168 states. Compared to other possible metrics, such as RMS values, this approach keeps some frequency
 169 information. When calculating the PSD sums, all time series (measured and simulated) are first cut and
 170 sampled such that they have identical discretization in time (time step and duration). The same PSD

171 calculation algorithm, without smoothing, is then applied to all time series. The PSD sums are computed
172 based on the one-sided, unsmoothed, discrete power density functions:

173
$$S_{sum} = \sum_{i=j}^k S_{resp}(f_i) \Delta f$$

174 where S_{resp} is the discrete power spectral density of the response at frequency f_i , Δf is the
175 corresponding frequency increment, j is the index of the first frequency of interest, and k is the index of
176 the last frequency of interest. The frequency limits for the low- (M2) and wave-frequency (M3)
177 components of the spectrum are given in Table 9. These are based on identifying the ranges over which
178 the wave spectra were defined, and then encompassing the lower frequencies below that range, without
179 considering the zero-frequency mean value.

180 *Table 9: Frequency limits for summation of power spectral density function for response metrics M2 and M3*

Wave	Low-frequency window	Wave-frequency window
White noise	0.005 Hz – 0.038 Hz	0.038 Hz – 0.14 Hz
Irregular wave	0.005 Hz – 0.05 Hz	0.05 Hz – 0.14 Hz

181

182 4 Uncertainty Sources

183 4.1 Random Uncertainty

184 Robertson, et al. (2018) identified a number of sources for random uncertainty in the response metrics.
185 However, since repeated measurements of the quantities of interest were available, the random
186 uncertainty could be calculated directly from the measurements without the need to assess the source of
187 the uncertainties. The random standard uncertainty, s_x , is calculated as the standard deviation, s_x , of the
188 metric (X) across the repeated tests, divided by the square root of the number of observations (N):

$$189 \quad s_x = \frac{s_x}{\sqrt{N}}$$

190 4.2 Systematic Uncertainty

191 Systematic uncertainty is a representation of the possible bias in a test campaign, and cannot be
192 calculated directly from measurements. Instead, the sources of systematic uncertainty throughout the
193 test must be identified, their individual effect on the metrics calculated, and then those effects combined.
194 The sources of uncertainty in this test campaign include the wave excitation, system properties and
195 configuration, and output measurements. Expert analysis of the systematic uncertainties in the test
196 campaign identified 24 separate parameters with significant levels of systematic uncertainty. These
197 parameters are listed in Table 10. Robertson, et al. (2018) provide a thorough discussion on the
198 assessment of the uncertainty levels for these parameters.

199 *Table 10: Sources of systematic uncertainty, CM: center of mass.*

	Parameter	Baseline Value	Uncertainty Level
1	Platform mass [kg]	1.4196E+7	8.75E+4
2	CM, x direction [m]	0	0.22
3	CM, y direction [m]	0	0.22
4	CM, vertical [m]	-7.53	0.21
5	Platform inertia, Ixx abt CM [kg-m ²]	1.2898E+10	1.2898E+8
6	Platform inertia, Iyy abt CM [kg-m ²]	1.2851E+10	1.2851E+8
7	Platform inertia, Izz abt CM [kg-m ²]	1.4189E+10	1.4189E+8
8	Draft [m]	20	0.25
9	Column angle, [deg]	0	0.5
10	Column diameter, [m]	12 or 24	0.1
11	Mooring stiffness [kN/m]	48.9	5.2
12	Mooring pretension [kN]	1122.5	62
13	Anchor position x [m]	Radially outward	0.25

14	Anchor position y [m]	Radially outward	0.25
15	Anchor position z [m]	Up/down	0.25
16	Mooring fairlead position [m]	Radially outward	0.05
17	Initial position [m]	0	0.12
18	Initial orientation [deg]	0	0.062
19	Water depth [m]	180	2
20	Water density [kg/m ³]	1025	10.25
21	Wave elevation – due to sensor drift [m]	measured	0.03
22	Wave elevation – due to probe location and tilt [m]	measured	negligible
23	Translation measurement [m]	0	0.03
24	Rotation measurement [deg]	0	0.3

200

201 From this original set of systematic uncertainty sources, the parameters were down-selected based on
 202 their influence on the response metrics. They were thresholded by examining the total combined
 203 estimated systematic uncertainty of the response metrics. Parameters whose effect on the change across
 204 all metrics was less than 10% were removed. In the end, the original set of 24 parameters was down-
 205 selected to 8, which are summarized in Table 11. Note that only parameters related to the system
 206 properties and configuration remain in the list, and no measurement or wave excitation uncertainties are
 207 included.

208

Table 11: Selected parameters for uncertainty propagation

	Parameter	Abbreviation
1	Center of mass, x direction	CMx
2	Center of mass, vertical	CMz
3	Mooring stiffness	Stiff
4	Draft	Draft
5	Column diameter	CoDia
6	Wave elevation – due to sensor drift	WaveElev
7	Platform inertia, I _{yy} abt CM	I _{yy}
8	Platform mass + Displaced Volume	Mass+Buoy

209

210 In this new list, when the platform mass was changed, the displaced volume was adjusted to ensure the
 211 heave equilibrium position was not altered. The goal was to have each of these parameters be
 212 independent of one another. If just the mass were altered, the draft would have changed, which is a
 213 separate parameter.

214 Many of these variations act on the response of the system without directly changing the wave excitation.
215 Variation 1 increases the cross-coupling of inertia contributions (surge/pitch, heave/pitch). Variations 2
216 and 7 change the inertia moment in pitch and consequently the pitch natural period. Variation 3 results
217 in a change of the surge natural period. On the other hand, variations 4, and 5 directly affect the wave
218 excitation by changing the volume exposed to the waves, while also changing the pitch natural period. For
219 variation 4, the pitch period is modified through the shift of the buoyancy point and the variation of
220 displacement. Variation 5 results in a change in the metacentric height and hence in the pitch period.
221 Variation 8 affects the surge and heave natural periods, while variation 6 only affects the wave excitation.

222 5 Uncertainty Propagation

223 “Uncertainty propagation” is determining the sensitivity of the output
224 response to the input and model uncertainties. If a closed-form solution is known for this relationship,
225 then the uncertainty can be propagated analytically. However, for complex problems such as the
226 dynamics of a floating offshore wind system, a closed-form solution may not be available. In these
227 situations, numerical methods can be used instead. A common approach is to use a Monte Carlo
228 approach to sample the input uncertainty distribution, and calculate the effective output distribution. The
229 calculation itself can be accomplished through simulation of a numerical model of the system.
230 Reduced-order models are often used because of their computational efficiency,
231 e.g., polynomial chaos expansion (Murcia, et al. 2017) and machine learning techniques (Clifton, et al.
232 2014). An even simpler method is sequential perturbation (Manteufel, 2012 and Figliola and Beasley,
233 2011), which requires just two simulations at the bounds of the input or model uncertainty to assess the
234 uncertainty bounds on the response metric of interest. Sequential perturbation is used here to limit the
235 computation time and maintain the use of sufficiently accurate models.
236 Carlo analysis with a reduced order model was not considered as the authors believed that this would

237
238 The process of using a model to propagate uncertainty can be problematic because it relies on
239 the use of the modeling tools that are to be validated to perform the uncertainty propagation. If the tools
240 do not represent the phenomena of interest accurately, they may not provide an accurate assessment of
241 the sensitivity of parameter variations on that phenomena. To address this issue, multiple
242 numerical modeling tools and multiple modeling approaches were used to propagate the uncertainties in
243 this work. The largest positive and negative contributions (out of
244 all simulation approaches) are then used as the sensitivity coefficient for each parameter of interest.
245 Within the limits of the numerical models, this approach is expected to give a
246 conservative estimate of the uncertainty for validation purposes.
247 systematic uncertainty sources in Table 11 are independent of each other.

248 5.1 Approach

249 The systematic uncertainty of an output response metric, b_R , is calculated by combining each of the
250 elemental systematic output standard uncertainties, b_i .

251

$$b_R^2 = \sum_{i=1}^N b_i^2$$

252 For the systematic uncertainties related to the input waves or model properties, these uncertainty values
253 (d_i) must be first propagated to their effect on the response metric uncertainty:

254

$$b_i = \theta_i d_i$$

255 where $\theta_i = \partial X / \partial p_i$ are the sensitivity coefficients of individual parameters, p_i , on the metric of interest,
256 X ; and, d_i are the elemental input/model systematic uncertainties (as summarized in [Table 11](#)). Once
257 propagated, each of the output metric uncertainty sources may be summed. The sensitivity coefficients
258 represent the influence that the input/model uncertainties have on the output metrics, and are typically
259 calculated analytically; but, if that is not possible, numerical models of the system can be used to estimate
260 them.

261 In this work, the systematic uncertainty of the response metrics due to a given uncertainty source is
262 estimated by sequential perturbation by first simulating the model using the baseline
263 properties and calculating the associated response metrics. Then, the system is simulated using a new
264 value for one of the six uncertain parameters, based on the uncertainty level described in Table 11
265 (changes are made in both the positive and negative directions), and the response metrics are again
266 calculated. The difference between the response metrics calculated using the baseline properties and
267 when changing one of the uncertain parameters is the systematic uncertainty for that parameter.
268 Systematic uncertainties will be calculated based on both a positive and negative change in the parameter,
269 and the resulting level of propagated uncertainty may not be the same (see Section 5.2). This process is
270 repeated for all six parameters, and then those individual uncertainty sources combined in quadrature.

271 This method assumes that each of the systematic uncertainty sources in Table 11 are independent of each
272 other.

273 ~~This process can be problematic in that it relies on the use of the modeling tools that are to be validated~~

274 Asymmetric Uncertainty

275 The propagation results in non-symmetric uncertainty bounds for the metrics; meaning that the
276 uncertainty on the positive end is sometimes different from the level on the negative end of the metric
277 value. This situation creates a complication in combining the different systematic uncertainty sources as
278 the straightforward method of adding them in quadrature no longer works. Different approaches can be

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279 used to address this. The simplest approach is to add the negative uncertainty bounds in quadrature, and
280 the positive uncertainty bounds in quadrature, separately; but, this approach has been shown to be
281 inaccurate. Another approach is proposed by Dieck (2007) and uses the calculation of a central value for
282 the nonsymmetric uncertainty bounds, which is then used to adjust the final uncertainty summed across
283 multiple sources. This approach was used here. The systematic response metric uncertainty, b_i , for an
284 individual parameter (i) is calculated as:

$$285 \quad b_i = \frac{(\bar{X} + b_i^+) - (\bar{X} - b_i^-)}{2}$$

286 where \bar{X} is the mean measured value for a given metric. The total estimated systematic standard
287 uncertainty, b_R , is then calculated. The asymmetry of the systematic uncertainty is further addressed in
288 the calculation of the total uncertainty (Section 6.1).

289 5.45.3 Modeling Tools / Methods

290 Three different simulation tools were used to propagate the systematic uncertainty in the model
291 properties to the response metrics, and several different users contributed results. A variety of tools and
292 users was employed since the approach used to model the behavior of the floating wind system may
293 affect the propagation of uncertainty. Ideally, the modeling tools that are to be validated would not be
294 the same ones used to perform the uncertainty propagation, but this is the only option for a complex
295 system such as a floating wind turbine. The largest propagated uncertainty found across the different
296 tools and users was used to help assuage this limitation.

297 All of the simulation approaches represent the floating wind system as a rigid body with linear elastic
298 mooring lines. For the hydrodynamic loading, second-order diffraction is
299 considered in addition to first-order potential flow contributions (added mass, radiation damping, and
300 excitation). The smaller braces and pontoons were ignored in the potential flow solution. Different
301 meshes and potential flow solvers were used (WAMIT – WAMIT, 2011 and DIFFRAC – Buchner, 2001),
302 and so the first- and second-order potential flow solutions differ among the simulation approaches.
303 Overall, when the same modeling approach is used (but different modeling tools), there is reasonable
304 agreement of the wave and low-frequency motions (Gueydon et al, 2014); however, differences in the
305 modeling of the first-order and second-order wave excitations and damping lead to differences in the
306 motion responses, especially around the resonance frequencies in surge, heave and roll/pitch (Robertson
307 et al, 2017).

308 For this study, five modeling approaches were followed with three distinct simulation tools to propagate
 309 deviations in the set of parameters of Table 11. The main differences between these modeling approaches
 310 are summarized in Table 12. Two fundamentally different approaches were used to account for linear and
 311 quadratic damping effects. A subset of the numerical models used Morison-type drag to compute
 312 quadratic damping loads on the substructure members (FAST, SIMA, aNySIM), while another subset of
 313 models used a tuned linear (P) and quadratic damping (Q) matrix (FAST_PQ, aNySIM_PQ), also referred
 314 to as the PQ-approach in this paper. The tuning was conducted based on decay tests in surge, heave and
 315 pitch. The PQ-approach was included here because it has demonstrated improved model predictions for
 316 the low-frequency pitch motion response of the system in past projects (Gueydon, 2016). The
 317 corresponding damping matrices are shown in Table 13.

318 *Table 12: Numerical modelling approaches*

Model ID	Global linear and quadratic drag	Morison drag on vertical columns	Morison drag on heave plates	Wave loads above still water level
FAST		x	x	Morison-type drag up to 1 st order free surface based on constant potential
FAST_PQ	x			
SIMA		x	x	Morison-type drag up to 1 st order free surface based on constant potential
aNySIM			x	Morison loads applied on heave plate only, Therefore, no wave loads act above still water level.
aNySIM_PQ	x			

319
 320 *Table 13: Global linear and quadratic damping coefficients applied in the PQ modelling approaches.*

DOF	Linear Damping	Quadratic Damping
Surge	1.83E+5 N/(m/s)	0.0 N/(m/s) ²
Heave	0.0 N/(m/s)	3.04E+6 N/(m/s) ²
Pitch	6.47E+7 Nm/(rad/s)	2.26E+10 Nm/(rad/s) ²

321

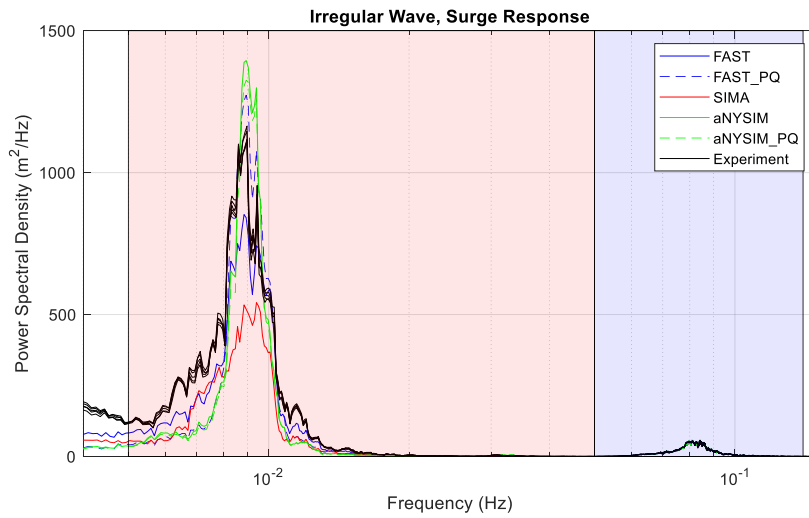
322 Furthermore, the models using Morison elements don't apply the coefficients identically: the location of
323 these elements and values of the coefficients are different. While all five models accounted for second-
324 order difference frequency [diffraction](#), the quadratic transfer functions (QTF) are different. The
325 quadratic terms of the QTF used in the aNySIM and aNySIM_PQ simulations were updated based on the
326 motion RAO of the floater of the present study, while all other simulations were performed with QTFs
327 based on the OC5-DeepCwind system (Robertson et al. 2017). Even though none of these models is
328 perfect, it is assumed that the choice of several tools and modeling approaches should enable an
329 assessment of realistic trends for the propagation of the uncertainty linked to the 8 most influential
330 parameters of Table 11.

331 Figure 2- Figure 5 show a comparison of the PSDs of the surge and pitch responses for the experimental
332 measurements and the baseline simulations. The integration limits for the low-frequency and wave-
333 frequency PSD sums are illustrated using the colored pink and blue regions in the plots. As shown, the
334 responses around the natural frequencies in surge (~0.01 Hz) and pitch (~0.03 Hz) are significant
335 compared to the wave-frequency responses, and the experimental measurements show high levels of
336 repeatability in the experiments. Figure 6 compares the PSD sum metrics (calculated from these values)
337 between experiment and baseline simulations.

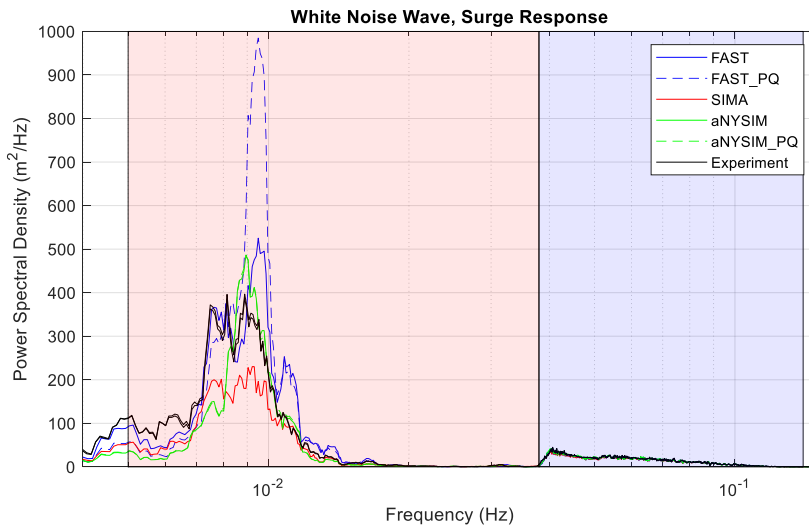
338 The wave-frequency surge and pitch responses are captured fairly well by all of the approaches, though
339 the PQ approaches tend to underpredict the pitch response in this frequency range. Due to the resonance,
340 small deviations of the wave loads and/or the damping can result in differences among simulations. Every
341 modeler was free to choose his/her own approach to account for the damping and the wave excitation.
342 As a consequence, the predictions of the responses around the resonance frequencies in surge and pitch
343 are far less consistent between the different simulation tools than those in the wave-frequency region, as
344 evident from the response metrics in Figure 6.

345 This discrepancy represents an important limitation in the propagation of systematic uncertainty through
346 the use of simulation models. Can a simulation tool accurately propagate uncertainty in a metric that it
347 does not accurately represent? As shown in Figure 6, there is varying levels of agreement for the low-
348 frequency PSD sums between simulation and experiment, with the simulations sometimes over-predicting
349 the metric value (e.g., FAST and FAST_PQ for the white noise cases), but mostly under-prediction. Since
350 there is a reasonable level of agreement for some tools, it is assumed that the physics included in the
351 numerical simulation tools should be able to capture the relative change in platform responses due to

352 small modifications in the input. The consistency of the propagated uncertainty between different
353 modeling approaches will later be examined to assess the validity of this statement.

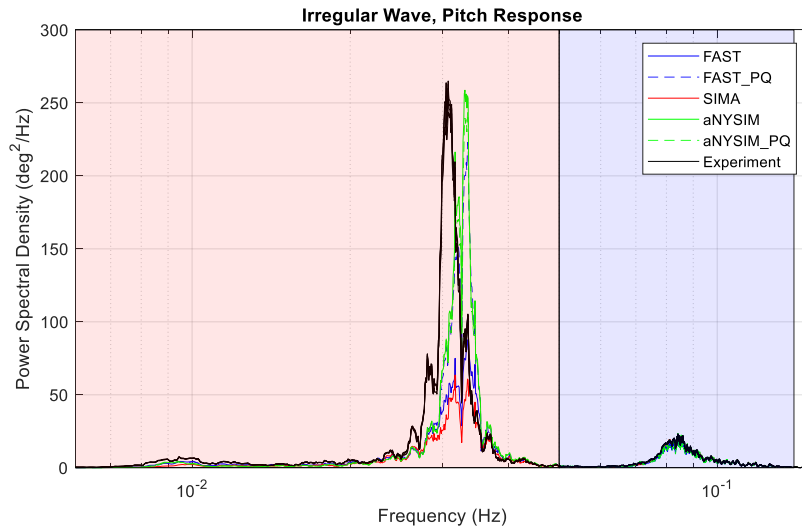


354
355 *Figure 2: Power spectral density (log scale abscissa) of platform response in surge for irregular wave excitation; pink shading*
356 *indicates low-frequency range for metric definition and blue indicates wave-frequency range. All experimental realizations are*
357 *shown.*

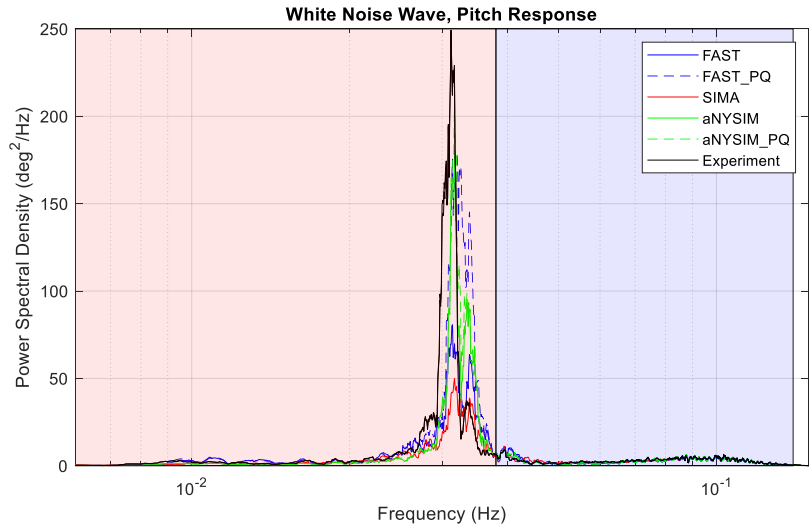


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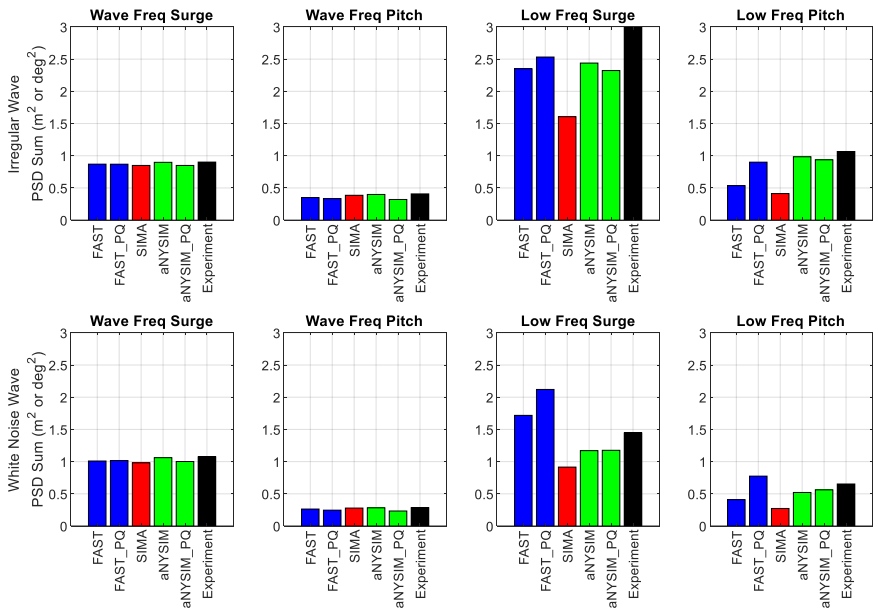
359 Figure 3: Power spectral density (log scale abscissa) of platform response in surge for white noise wave excitation; pink shading
360 indicates low-frequency range for metric definition and blue indicates wave-frequency range. All experimental realizations are
361 shown.



362
363 Figure 4: Power spectral density (log scale abscissa) of platform response in pitch for irregular wave excitation; pink shading
364 indicates low-frequency range for metric definition and blue indicates wave-frequency range. All experimental realizations are
365 shown.



366
 367 *Figure 5: Power spectral density (log scale abscissa) of platform response in pitch for white noise wave excitation; pink shading*
 368 *indicates low-frequency range for metric definition and blue indicates wave-frequency range. All experimental realizations are*
 369 *shown.*



370
 371 *Figure 6: PSD sums: comparison of baseline simulations and measurements.*

372 5.55.4 Implementation of Parameter Variations in Numerical Models

373 The parameter variations considered for the assessment of the systematic uncertainty were implemented
374 with different approaches in the different numerical models. Differences arose because every numerical
375 model has inherently different ways of specifying key modelling parameters. The goal was to isolate
376 modifications to the model properties to only one parameter at a time; but, based on the modeling
377 approach employed, this was not always possible. The different realizations of the model parameter
378 variations for each modelling tool are outlined below.

379 **Variation 1)** CM, x direction, **Variation 2)** CM, z direction, **Variation 7)** Inertia, I_{yy}

380 The systematic uncertainty related to variations in the offset of the system center of mass in the x- and
381 z-directions is investigated with Variation-1 and Variation-2. The x-offset value was specified as +/- 0.22
382 m and the z-offset was specified as +/-0.21 m respectively.

383 FAST and SIMA: For the CM change, only the CM is moved, there is no change in the moment of inertia.
384 Similarly, for Variation 7, only the inertia is changed.

385 aNySIM: In MARIN's simulation tool, the inertia moments are defined at the center of mass. As a
386 consequence, shifting the CM resulted in a change of moments of inertia. For instance,
387 Variation 1 resulted in a change in the pitch period of about 2%. For variation 7, the inertia
388 is changed independently of the mass by defining a new radius of inertia for the pitch
389 rotation. The pitch period varied of 0.3% as a result of this inertia variation.

390 **Variation 3)** Mooring stiffness

391 For Variation 3, the systematic uncertainty related to variations in the mooring stiffness is investigated.

392 FAST and SIMA: For Variation 3, the mooring line stiffness was varied by changing EA together with
393 the unstretched line length (+/- 2.732 m) to ensure that the mooring pre-tension did not
394 change.

395 aNySIM: Variation 3 led to a small change of the pitch period of about 0.02%. The simulation tool
396 accepts the stiffness and pre-tension directly as input parameters while the unstretched
397 length is automatically adjusted.

398 **Variation 4)** Draft, **Variation 5)** Column diameter

399 The systematic uncertainty related to variations in the platform draft (+/- 0.25 m) and column diameter
400 (+/- 0.1 m) are investigated with Variation 4 and Variation 5.

401 FAST and SIMA: To model the impact of changes in the platform draft and column diameter on the
402 hydrodynamic loads without adjusting any additional model parameters (e.g. mass or line
403 tension), the first-order potential flow solution was updated by adjusting the platform
404 geometry mesh that is used in WAMIT. This leads to updated hydrodynamic databases for
405 the radiation and diffraction loads. The hydrostatic restoring matrix is also updated to
406 account for the changes in buoyancy force, center of buoyancy, and waterplane moment of
407 inertia. The Morison-type drag forces on the columns were also updated to reflect the
408 changes in geometry. Note that the 2nd-order solution was not updated.

409 aNySIM: For variations 4 and 5, the corresponding change of volume was used to scale the potential
410 flow database based on the displacement. For the draft variation, the volume was estimated
411 to vary by 0.7%. For the column diameter variation, the volume was estimated to vary by
412 1.2%. Froude scaling was applied to all quantities resulting from the potential flow
413 calculation (i.e. 1st order quantities and the quadratic transfer functions). The linear
414 hydrostatics were updated based on the new submerged geometry (displacement, center of
415 buoyancy, waterline area second moment) while the position of the center of mass with
416 respect to the keel was kept unchanged. When used, the diameter of the Morison elements
417 representing the heave plates was changed with the same value as the diameter of the
418 columns.

419 **Variation 6) Wave Elevation**

420 ALL: A potential 3 cm drift in the wave elevation measurement was estimated based on
421 measurements before and after the wavemaker started. This uncertainty was addressed by
422 adjusting the input wave elevation by a multiplicative factor. This multiplicative factor
423 considered the 3 cm drift as the error in a representative wave amplitude. For the irregular
424 waves with 7.1 m H_s, this factor was thus 1 ± 0.00845 .

425 **Variation 8) Mass**

426 FAST and SIMA: The mass of the floater was adjusted based on the assessed uncertainty. To avoid
427 changing the draft of the structure, another parameter needed to be adjusted to achieve the

428 same equilibrium position. Since the displaced volume of the structure was not directly
429 measured, it was determined to alter this value in conjunction with the mass. The displaced
430 volume was altered by +/- 85.4 m³ in order to maintain the same equilibrium position. The
431 wave excitation loads were not modified due to the change in volume.

432 aNySIM: In the same way as for FAST and SIMA, the displacement was modified in conjunction with
433 the mass to avoid changing the draft. Moreover, the radius of inertia was altered to keep the
434 moment of inertia unchanged. This was done for roll, pitch and yaw.

435 6 Total Uncertainty

436 6.1 Combining all uncertainty sources

437 Once the total estimated systematic and random uncertainty values are calculated, they are combined to
438 determine the total combined uncertainty, u_c for a given output metric:

$$439 \quad u_c = \sqrt{(b_R)^2 + (s_x)^2}$$

440 Confidence intervals are then assigned to this uncertainty to define the expanded uncertainty (U):

$$441 \quad U = k u_c$$

442 where k is the coverage factor. When the expected distribution of the measured data is approximately
443 normal and the effective degrees of freedom (DOF) are large, confidence intervals of 95% to 99% are
444 typically used, which results in a coverage factor of approximately 2 to be applied to the uncertainty bound
445 (Kim and Hermansky, 2014). A representation of a response metric, X , is then given as:

$$446 \quad X = \bar{X} \pm U$$

447 where X is the best available estimate of the measurement, \bar{X} is the mean of the response metric, U is the
448 expanded uncertainty, and $X-U$ and $X+U$ define the uncertainty bounds that would include a large portion
449 of the possible occurrences of the response metric.

450 However, when there is asymmetry in the uncertainties, the definition of the expanded uncertainty
451 bounds must be adjusted. This is accomplished by defining a displacement, q , between the center of each
452 nonsymmetrical systematic uncertainty interval and the average:

$$453 \quad q_i = \frac{(\bar{X} + b_i^+) + (\bar{X} - b_i^-)}{2} - \bar{X}$$

454 This displacement value is used to reinsert the asymmetry so that the total uncertainty interval is
455 nonsymmetrical:

$$456 \quad X = \left(\bar{X} + \sum_{i=1}^N q_i \right) \pm U$$

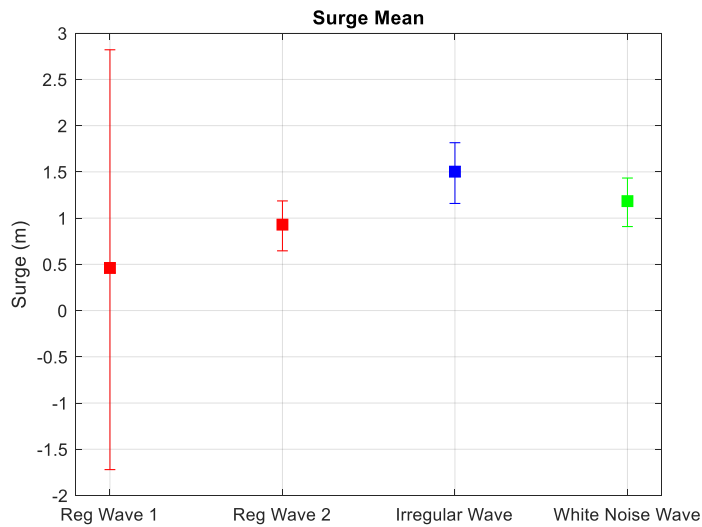
457 When there is more than one nonsymmetrical uncertainty source, the q values are summed algebraically
458 to provide an overall asymmetry level across all nonsymmetrical sources.

459 In the present work, when accounting for the uncertainty contributions from different simulation tools,
460 the largest positive and negative contributions (out of all simulation approaches) are kept for each
461 parameter variation.

462 6.2 Total uncertainty values

463 The calculated uncertainty values for each of the four metrics are shown in Figure 7 - Figure 9. The mean
464 metric values, shown as a square, are calculated from the response measurements averaged over all of
465 the repeated tests. The calculated uncertainty bands are shown using error bars, and represent the
466 expanded uncertainty ($\pm L$) that includes both systematic and random uncertainty sources.

467 Figure 7 shows significant uncertainty in the mean surge metric, especially for the regular wave cases. The
468 mean surge value was typically small, so small changes due to parameter variations can create significant
469 levels of uncertainty in this metric. The main source of the uncertainty in mean surge position was related
470 to the center of mass in the x-direction (CMx) for regular wave case 1, while the mooring pretension and
471 stiffness also contributed for the other waves. The uncertainty in mean surge in regular wave case 1 is
472 probably overstated: the large variation was only seen for one of the simulation tools, and much of the
473 difference is likely related to static effects (which would have been zeroed out in the experimental
474 measurements).

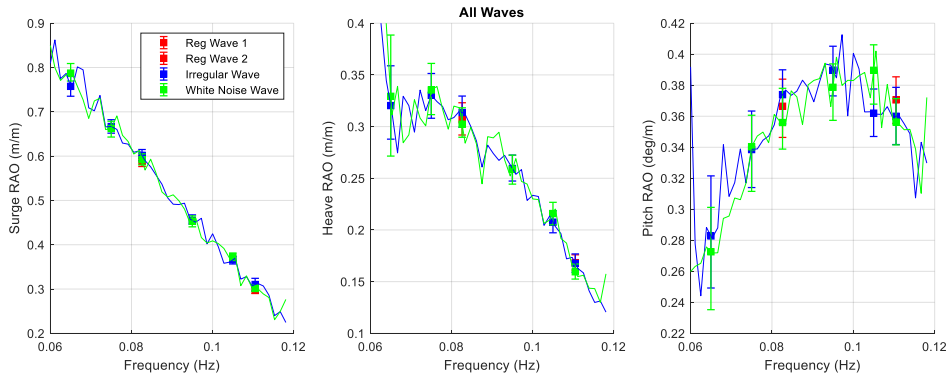


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476
477

Figure 7: Mean surge metric for each wave case. The square indicates the mean value across all repeat tests, and error bars indicate the uncertainty bounds

478 Figure 8 shows the experimentally obtained RAOs for the irregular and white noise waves – averaged over
 479 the repetitions and smoothed. Plotted on top of these curves are the six frequency points computed for
 480 each of the waves, including the expanded uncertainty. Where multiple repetitions are available, the
 481 mean of all of the repetitions is shown. There is generally good agreement in the experimentally obtained
 482 RAOs between different wave conditions. Although some larger discrepancies can be observed in the pitch
 483 RAO at a given frequency, individual wave RAO values fit within the error bars for other wave RAO values.
 484 The uncertainty level depends on the frequency. The uncertainty in the low-frequency responses is larger
 485 than the uncertainty at higher frequencies. The trend toward higher uncertainty at low frequencies is
 486 observed in most of the uncertainty parameters, suggesting that the main reason may be related to the
 487 increasing importance of 1) damping since the excitation frequency approaches the natural frequency
 488 (especially in heave and pitch) and 2) cancellation effects in the excitation (which depend strongly on the
 489 geometry). Although the uncertainty level at a given frequency is similar for all considered waves, it is not
 490 identically reproduced. The main conclusions from Figure 8 are that the uncertainty in the wave-frequency
 491 responses is generally small for wave periods shorter than approximately 14 seconds, and that the pitch
 492 responses are more uncertain than surge responses.



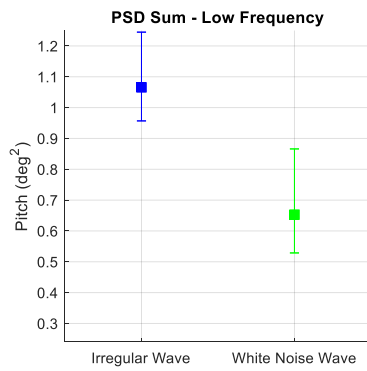
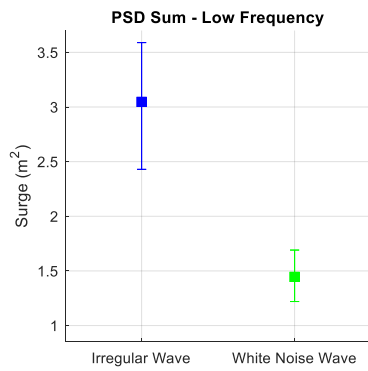
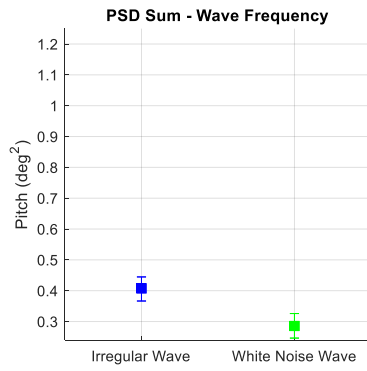
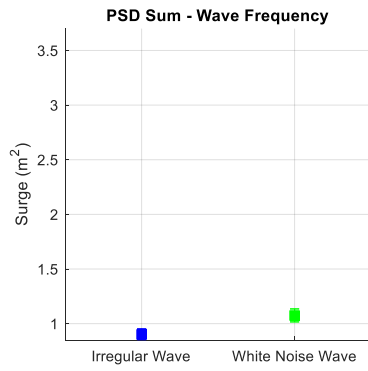
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494 *Figure 8: Comparison of RAO values across wave cases. Mean results at the selected frequencies (for each wave) are shown by*
 495 *squares, and error bars indicate the uncertainty bounds for those frequencies. Lines show the experimentally obtained RAOs by*
 496 *irregular and white noise waves.*

497 The focus of this test campaign is on the low-frequency response of the wind turbine in the surge and
 498 pitch DOFs. Figure 9 shows the PSD sum metric for both the irregular and white noise wave in these two
 499 DOFs in both the wave and low-frequency regions. The uncertainty levels vary between the two irregular
 500 waves (irregular and white noise); the difference is especially pronounced in the low-frequency surge
 501 metric. The amplitude of the total uncertainty in the wave-frequency PSD sum metric is less than 20%,
 502 while the low-frequency PSD sum metric for surge is on the order of 30-50% and the low-frequency PSD
 503 sum metric for pitch is approximately 40% for the white noise wave case.

504 6.3 Contributions to uncertainty

505 To understand what is driving these uncertainties, the individual uncertainty sources (b_i and $s_{\bar{x}}$) are shown
 506 in Figure 10. This figure indicates that the high uncertainty levels in the surge direction come from
 507 uncertainty in the mooring stiffness for the low-frequency response and from the wave elevation, column
 508 diameter and mass/buoyancy for the wave-frequency response. In the pitch direction, uncertainty in the
 509 center of mass offset, and also column diameter and draft, create the largest levels of uncertainty in the
 510 response. These results highlight the fact that the low-frequency responses, which are primarily resonant
 511 responses, are especially sensitive to parameters that affect the stiffness of the system and the inertia of
 512 the system. Changes in stiffness or changes in inertia may shift the natural frequency slightly, and the level
 513 of excitation at the resulting natural frequency may differ compared to the original system. Figure 10 also
 514 confirms that the contribution of the random uncertainty to the total uncertainty is negligible compared
 515 to the systematic uncertainty.



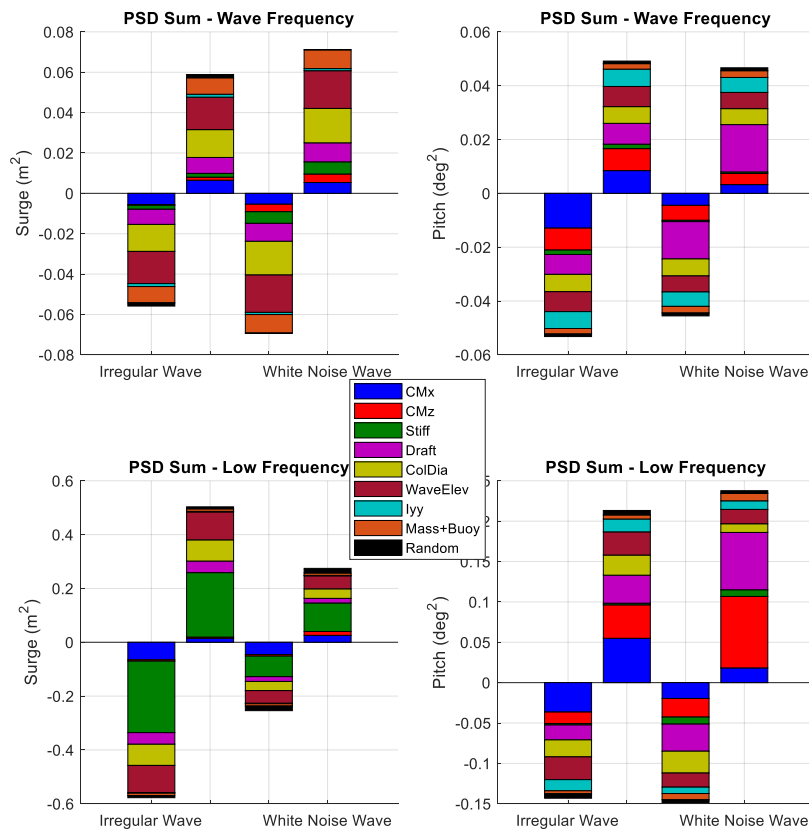
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517 *Figure 9: PSD sum metrics for the irregular and white noise wave cases, in both pitch and surge directions; square indicates the*
 518 *mean value across all repeat tests, and bars indicate the uncertainty bounds*

519

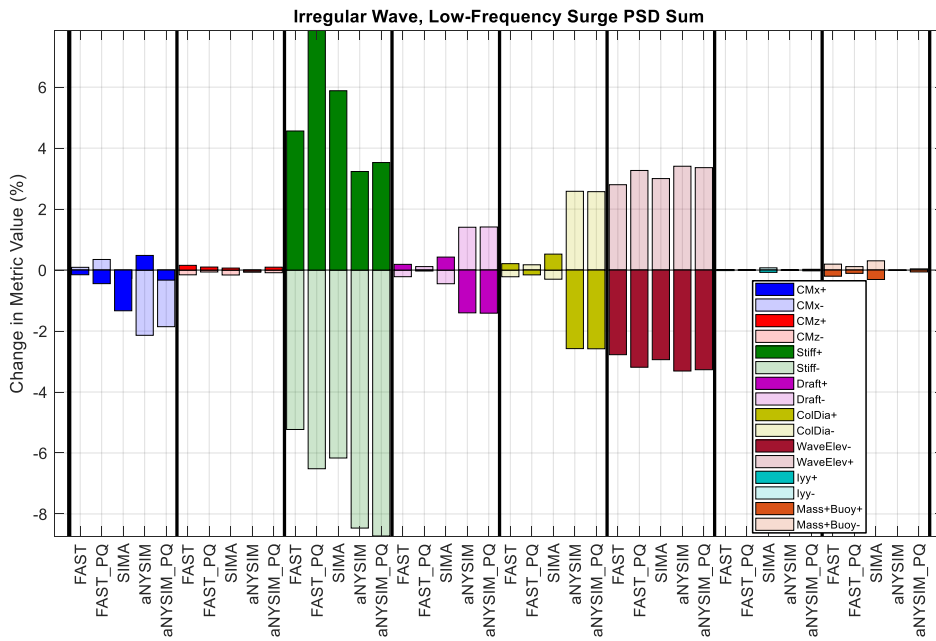
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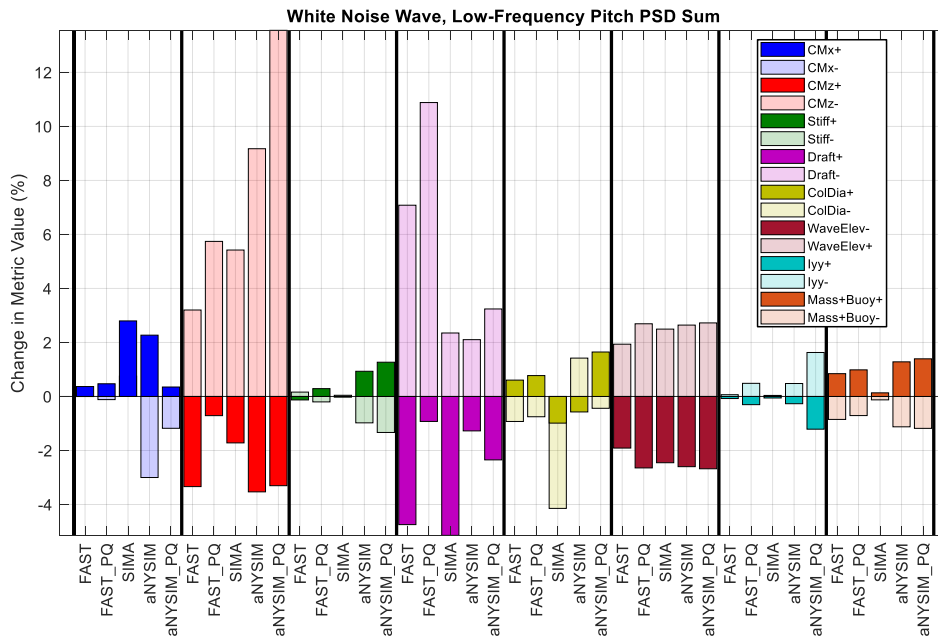
522
 523 *Figure 10: Break-down of sources of uncertainty (random and individual systematic sources) for the PSD sum metric*
 524 Figure 11 and Figure 12 examine the variability in the level of propagated uncertainty for these uncertainty
 525 sources based on what modeling tool is used, considering two of the low-frequency response metrics with
 526 large uncertainty: surge in the irregular wave in Figure 11 and pitch in the white noise wave in Figure 12.
 527 The contributions from each tool for each parameter variation, both positive and negative, are included.
 528 The different simulation tools generally agree regarding *which* parameters give the largest contributions
 529 to uncertainty, such as the mooring stiffness and pretension for the low-frequency surge, and mostly
 530 agree on the direction of the largest changes (i.e. positive or negative change in the metric). On the other
 531 hand, there are significant variations in the magnitude of the changes in the metric depending on which
 532 simulation tool is applied.

533 It is important to note that the changes in metrics from different parameter variations are additive, and
 534 that only the largest variations (among different simulation tools) are used in the calculation of total
 535 uncertainty. As a result, the total uncertainty in this study is more conservative than if one had only used
 536 a single simulation tool. There is not a clear pattern suggesting that the PQ- or Morison-type approaches
 537 give larger uncertainty for particular parameter variations, but a closer correlation can be noted based on
 538 simulations using the same modelling tools (comparing, for example, surge results with aNySIM_PQ and
 539 aNySIM, or results from FAST and FAST_PQ). Nonetheless, it is impossible to determine whether or not
 540 the use of engineering models to predict low-frequency responses will give a conservative or non-
 541 conservative estimate of the total uncertainty.



542

543 *Figure 11: Variability of propagated uncertainty for the irregular, low-frequency surge PSD sum metric, based on a variety of*
 544 *modelling approaches; positive metric variations are in bold and negative are shown in a muted color*

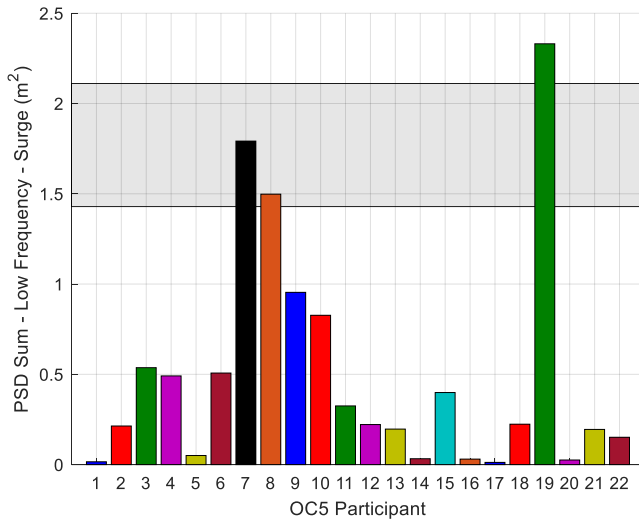


545

546 *Figure 12: Variability of propagated uncertainty for the white noise, low-frequency pitch PSD sum metric, based on a variety of*
 547 *modelling approaches; positive metric variations are in bold and negative are shown in a muted color*

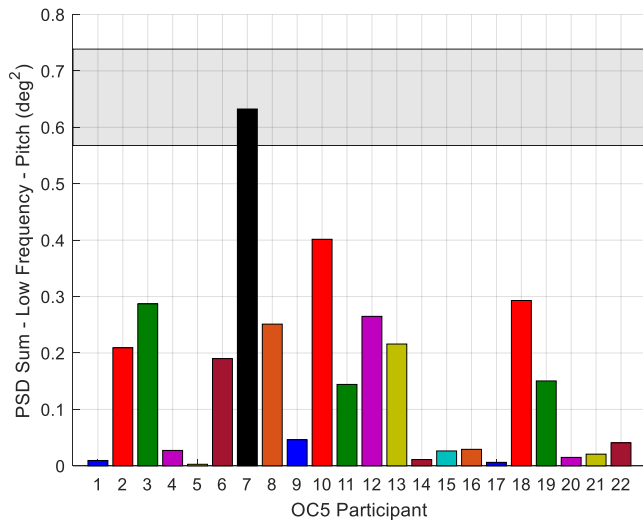
548 6.4 Application to OC5 results

549 In order to understand the magnitude of the experimental uncertainty with respect to numerical
 550 simulations, the original OC5 study results (Robertson et al. 2017) are re-visited here. The experimental
 551 tests which were studied in the OC5 project correspond to a different physical model, in a different basin,
 552 but under similar wave conditions (LC3.3 from Robertson et al. 2017). As shown in Figure 13 and Figure
 553 14, the PSD sums were computed for both the experimental and numerical results in the OC5 study, and
 554 the relative uncertainty from the present tests was applied to the original experimental results. For the
 555 low-frequency surge metric, only one of the numerical results (out of 21 participant results) was within
 556 the error bounds on the experimental result – even after several iterations and tuning. None of the
 557 simulation tools predicted the low-frequency pitch response within the experimental uncertainty. It
 558 should be noted that the tuned PQ approach used for the uncertainty propagation in this paper, which
 559 shows promise in estimating these low-frequency metrics, is not represented in the OC5 study. This
 560 modeling approach, as well as others, were developed as a direct consequence of the issues identified in
 561 OC5.



562

563 *Figure 13: Low-frequency surge PSD sum metric for the original OC5 results (Robertson et al. 2017), with experimental uncertainty*
 564 *indicated based on the present work. OC5 participant 7 (black) refers to the experimental results.*



565

566 *Figure 14: Low-frequency pitch PSD sum metric for the original OC5 results (Robertson et al. 2017), with experimental uncertainty*
 567 *indicated based on the present work. OC5 participant 7 (black) refers to the experimental results.*

568 7 Conclusions

569 The total experimental uncertainty in a set of hydrodynamics model tests with a rigid semisubmersible
570 wind turbine has been estimated through propagation of the systematic uncertainties using several
571 numerical simulation tools. Considering response metrics which give an indication of the wave-frequency
572 and low-frequency responses of the system, the wave frequency responses are found to have relatively
573 small uncertainty, while the uncertainty in the low-frequency responses is somewhat higher (20-40% in
574 the integral of power spectral density over a defined low-frequency range). The random uncertainty,
575 which was found through repeated measurements, is negligible compared to the estimated systematic
576 uncertainty.

577 The main contributions to the propagated systematic uncertainty in low-frequency responses were
578 primarily model characteristics that affected the stiffness: mooring system stiffness for the surge
579 response, and platform draft, and vertical center of gravity for the pitch response. In addition, uncertainty
580 in the wave amplitude also had an impact. The simulation tools applied in the study showed good
581 agreement regarding which parameters were most important, although the magnitude of the propagated
582 uncertainty differed significantly among participants.

583 A major limitation in the present work is the use of simulation tools for uncertainty propagation: the
584 inconsistent estimation of the baseline value of the low-frequency PSD sums suggests that the modelling
585 tools may not be sufficiently accurate to be used for uncertainty propagation. At present, however, these
586 tools represent the state-of-the-art, and the results of the present study suggest that the differences
587 between experiments and simulations are larger than the uncertainty in the experimental results.

588 The results from this study give a measurement of uncertainty that can be used in future validation efforts:
589 the data from the present tests will be studied further using both engineering and high-fidelity models
590 through the OC6 extension of the Offshore Code Comparison Collaboration through the International
591 Energy Agency. Additional tests, where wave and radiation loads were measured directly on the fixed
592 structure, will also be incorporated in the OC6 project in order to better understand the reasons for
593 discrepancies between simulations and experiments.

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