

*restart*

#Initialize linear algebra  
*with(LinearAlgebra) :*  
*with(CodeGeneration) :*

**#Import expressions from other worksheets:**

*read "../Equations\_of\_motion/eom.m";*

**#Inserting for virtual holonomic constraint**

*E := K0 + P0 :*

*Ev := E0 = collect* $\left(\text{subs}(q1 = \text{theta}(t), q2 = \text{phi}(\text{theta}(t)), Dq1 = \text{diff}(\text{theta}(t), t), Dq2 = \text{diff}(\text{phi}(\text{theta}(t)), t), E), \left[\left(\frac{d}{dt} \theta(t)\right)^2\right]\right)$ ;

*eom := M.Vector([DDq1, DDq2]) + Cc.Vector([Dq1, Dq2]) + G :*

*aby1 := collect* $\left(\text{subs}(q1 = \text{theta}(t), q2 = \text{phi}(\text{theta}(t)), Dq1 = \text{diff}(\text{theta}(t), t), Dq2 = \text{diff}(\text{phi}(\text{theta}(t)), t), DDq1 = \text{diff}(\text{diff}(\text{theta}(t), t), t), DDq2 = \text{diff}(\text{diff}(\text{phi}(\text{theta}(t)), t), t), eom(1)), \left[\frac{d^2}{dt^2} \theta(t), \left(\frac{d}{dt} \theta(t)\right)^2\right]\right)$ ;

*aby2 := collect* $\left(\text{subs}(q1 = \text{theta}(t), q2 = \text{phi}(\text{theta}(t)), Dq1 = \text{diff}(\text{theta}(t), t), Dq2 = \text{diff}(\text{phi}(\text{theta}(t)), t), DDq1 = \text{diff}(\text{diff}(\text{theta}(t), t), t), DDq2 = \text{diff}(\text{diff}(\text{phi}(\text{theta}(t)), t), t), eom(2)), \left[\frac{d^2}{dt^2} \theta(t), \left(\frac{d}{dt} \theta(t)\right)^2\right]\right)$ ;

*eom(1),*  $\left[\frac{d^2}{dt^2} \theta(t), \left(\frac{d}{dt} \theta(t)\right)^2\right]$ ;

*aby1 := collect* $\left(aby1, \left[\frac{d^2}{dt^2} \theta(t), \left(\frac{d}{dt} \theta(t)\right)^2\right]\right) :$

*aby2 := collect* $\left(aby2, \left[\frac{d^2}{dt^2} \theta(t), \left(\frac{d}{dt} \theta(t)\right)^2\right]\right) :$

$$\text{alpha1} := \text{coeff}\left(\text{aby1}, \frac{d^2}{dt^2} \theta(t)\right);$$

$$\text{alpha2} := \text{coeff}\left(\text{aby2}, \frac{d^2}{dt^2} \theta(t)\right);$$

$$\text{gamma1} := \text{subs}\left(\left(\frac{d}{dt} \theta(t)\right)^2 = 0, \frac{d^2}{dt^2} \theta(t) = 0, \text{aby1}\right);$$

$$\text{gamma2} := \text{subs}\left(\left(\frac{d}{dt} \theta(t)\right)^2 = 0, \frac{d^2}{dt^2} \theta(t) = 0, \text{aby2}\right);$$

$$\text{beta1} := \text{subs}\left(\frac{d^2}{dt^2} \theta(t) = 0, \left(\frac{d}{dt} \theta(t)\right)^2 = 1, \text{aby1}\right) - \text{gamma1};$$

$$\beta2 := \text{subs}\left(\frac{d^2}{dt^2} \theta(t) = 0, \left(\frac{d}{dt} \theta(t)\right)^2 = 1, \text{aby2}\right) - \gamma2;$$

$$\text{abyEq} := \text{collect}\left(\text{solve}\left(\text{subs}\left(\left(\frac{d}{dt} \theta(t)\right)^2 = \text{placeholder}, \text{diff}(\theta(t), t)^2 = \frac{\alpha2 \cdot \gamma1 - \alpha1 \cdot \gamma2}{\alpha1 \cdot \beta2 - \alpha2 \cdot \beta1}\right), \text{D}^{(2)}(\phi)(\theta(t))\right), \text{placeholder}\right);$$

$$\text{energyEq} := \text{solve}\left(\text{subs}\left(\left(\frac{d}{dt} \theta(t)\right)^2 = \text{placeholder}, \text{Ev}\right), \text{placeholder}\right);$$

$$f := \text{subs}(\text{placeholder} = \text{energyEq}, \text{abyEq});$$

## #Creating Matlab code

$$f0 := \text{algsubs}(\text{D}(\phi)(\theta(t)) = \text{Dphi}, f);$$

$$f0 := \text{algsubs}(\text{phi}(\theta(t)) = \text{phi}, f0);$$

$$f0 := \text{algsubs}(\theta(t) = \text{theta}, f0);$$

$$\text{Matlab}(f0, \text{resultname} = 'f0');$$

$$\text{save } f, \text{"diff_eq_phi.m"};$$