

# Ice-induced vibrations of the Norströmsgrund lighthouse

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## Abstract

The signature and occurrence of frequency lock-in (FLI) vibrations of full-scale offshore structures are not well understood. Although several structures have experienced FLI, limited amounts of time histories of the responses alongside measured met-ocean data are available in the literature. This paper presents an analysis of 61 measured events of resonant vibrations of the Norströmsgrund lighthouse from 2001 until 2003. The vibrations of most of these events did not reach a steady state; thus, they violate an often-quoted criterion for frequency lock-in vibrations and remain outside any modes of ice-induced vibrations suggested in standards.

Met-ocean data from both in situ measurements and from the Copernicus marine service information database are further used to better understand the occurrence of resonant ice-induced vibrations. All events between 2001 and 2003 occurred during days with ice concentrations of 8-10/10, closely packed consolidated drift ice. The locally measured ice velocity and thickness ranged from 0.023 to 0.075 m s<sup>-1</sup> and from 0.26 to 1.9 m, respectively. These measurements included level ice, rafted ice and ridged ice. The events of resonant vibrations are further compared with measurements from the same structure between 1979 and 1988. Most events of resonant vibrations were recorded in the winter of 1988, followed by the

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24 winters of 2003 and 1980. The winter of 1988 had fewer freezing degree days (FDD) than did  
25 the 65-year average, whereas the winters of 2003 and 1980 had more FDD than did the 65-year  
26 average.

## 27 **Keywords:**

28 Ice-induced vibrations

29 Resonant vibrations

30 Frequency lock-in

31 Norströmsgrund lighthouse

## 32 **1 Introduction**

33 Structures exposed to drifting ice may experience ice-induced vibrations (IIV). These vibrations  
34 may cause fatigue damage of offshore structures and discomfort for personnel. IIV are a result  
35 of the dynamic interaction between ice and structure, mostly associated with crushing failure at  
36 the ice-structure interface. The three regimes of IIV are defined as intermittent crushing,  
37 frequency lock-in (FLI) and continuous brittle crushing (ISO, 2010). These regimes are  
38 typically observed for different ice speeds for a structure interacting with level ice, where  
39 intermittent crushing occurs for low ice speeds, FLI occurs for intermediate ice speeds, and  
40 continuous brittle crushing occurs for high ice speeds (Yue et al., 2009). FLI is the most violent  
41 regime, characterized by Hendrikse (2017) as periodic oscillations near one of the natural  
42 frequencies of the structure, while the ISO/FDIS 19906 standard states that FLI causes typically  
43 sinusoidal responses at the top of the structure when the ice failure frequency is locked at one  
44 of the lowest modes of the structure (ISO, 2010). The FLI term is, however, not unique to  
45 describe this phenomenon; this non-uniqueness originates from the physical interpretation in  
46 terms of mechanical oscillations. Peyton (1967) and Blenkarn (1970) measured IIV on

47 structures in the Cook-Inlet, from which Blenkarn introduced terminology such as steady-state  
48 oscillations and resonant self-excited vibrations to the ice-structure interaction community.  
49 These terms are used as alternative definitions for what we usually refer to as FLI (ISO, 2010),  
50 and they are often presented alongside with phenomenological models to predict IIV, see Sodhi  
51 (1988) and Hendrikse and Metrikine (2015) for an overview. Määttänen (1975) measured FLI  
52 on the KEMI-1 steel lighthouse in both the first and second modes of the structure. Only months  
53 after deployment in the Gulf of Bothnia, the structure collapsed because of IIV. FLI has been  
54 measured on narrow structures (Määttänen, 2008; Nordlund et al., 1988), wide structures  
55 (Jefferies and Wright, 1988) and jacket structures (Yue and Bi, 2000). Despite the structural  
56 differences, the response signals share the rise of high-amplitude oscillations near a natural  
57 frequency. Examples of this phenomenon can be seen when comparing selected responses from  
58 the Norströmsgrund lighthouse (Nord et al., 2016) and from the MS jacket platform (Yue and  
59 Bi, 2000). Because of the limited selection of signals in publications, these are often cases for  
60 which there is practically no doubt whether they belong to FLI and result in little discussion on  
61 the actual classification. Cases of vibrations near a natural frequency of a structure that violate  
62 the steady-state oscillations also violate the ISO 19906 (ISO, 2010) definition of FLI, which  
63 states that the response inherits a sinusoidal shape.

64 In this paper, resonant vibrations are used as a common term for vibrations near a natural  
65 frequency of the structure, which also includes FLI, and hence, no specific type of oscillator is  
66 assigned to the ice-structure interaction system (Rajasekar and Sanjuan, 2016). We show the  
67 encountered difficulty to classify IIV events as FLI when we present an analysis of 61 events  
68 of resonant vibrations that were measured on Norströmsgrund lighthouse between 2001 and  
69 2003.

70 The signatures in the measured structural responses are discussed alongside the ice conditions  
71 under the occurrences of these events and the inherent uncertainties in the measurements and

72 analysis. The 61 events are compared to earlier measurements of resonant vibrations on the  
73 same structure (Engelbrektson, 1987a; Engelbrektson, 1987b; Engelbrektson, 1989;  
74 Engelbrektson and Janson, 1985), which together total more than 200 events.

## 75 **2 Measurements**

76 This chapter briefly describes two measurement campaigns on the Norströmsgrund lighthouse:  
77 one in the time period 2001-2003 and another in the time period 1979-1988. The differences in  
78 measurement techniques between the two measurement campaigns affect the current results to  
79 an unknown extent and are almost impossible to quantify because the measurement techniques  
80 varied from year to year, and often uncertainties in the measurements vary between the different  
81 ice conditions. Table 1 summarizes how structural response, ice thicknesses and ice velocities  
82 were measured.

### 83 **2.1 Instrumentation, measurements and post-processing of data on Norströmsgrund 2001-2003**

84 The STRICE (STRuctures In ICE) measurements in 2001-2003 were published in reports (e.g.,  
85 Haas et al., 2003; Kärnä and Yan, 2009), a thesis (Bjerkås, 2006a) and several papers that  
86 discuss more detailed events of IIV (e.g., Bjerkås, 2006b; Bjerkås et al., 2013b), events of ice  
87 ridge actions (Bjerkås and Bonnemaire, 2004), failure modes (Kärnä and Jochmann, 2003) and  
88 mechanical properties (Fransson and Stenman, 2004). Fig. 1 displays the accelerometer  
89 locations on the lighthouse and a picture of Norströmsgrund surrounded by ice. Measurements  
90 were also performed in 1999 and 2000; however, these measurements are herein excluded  
91 because they lack acceleration measurements. Because instrumentations changed from year to  
92 year, figures of all instrumentation configurations are not provided here; see Bjerkås (2006a)  
93 for details.

94 All events that were judged resonant types of vibrations are given in Table 2, wherein necessary  
95 information is provided for the reader to examine the instances in the original data set.

96 The ice thickness at lighthouse Norströmsgrund was measured both with an upward-looking  
97 sonar (ULS) and an electromagnetic (EM) sensor (Haas and Jochmann, 2003). The ULS was  
98 mounted 5 m southeast of the lighthouse on the submerged caisson (+7.5 m elevation), and the  
99 EM sensor was hung 10 m east of the lighthouse, approximately 2 m above the mean water  
100 level (MWL). The ULS recorded the deepest point of the ice, and the ice surface elevation was  
101 measured with a laser. The ULS was operational in the winters of 2000 and 2001. The EM  
102 thickness was estimated based on a 6-m diameter measurement footprint, and the estimates  
103 depended on the ice conductivity. More information regarding these measurements can be  
104 found in Haas (2000).

105 Although the ice thickness was measured at a certain time, it could take minutes before that ice  
106 appeared at the ice-structure interface. The heterogeneity of the ice cover was also a  
107 complicating factor in the ice-thickness estimation because the ice underneath the EM sensor,  
108 or above the ULS, was at times different than the ice at the ice structure interface. Video records  
109 were then used to estimate the ice thickness at the ice-structure interface.

110 Ice thickness measurements, video records and freezing degree days (FDDs) were used to judge  
111 the types of ice features (level, rafted, or ridged ice) that interacted with the lighthouse during  
112 an event of resonant vibrations. The number of FDDs was calculated based on air temperature  
113 measurements at both Luleå Airport and the Rödkallen meteorological station. The daily mean  
114 temperatures were calculated using the Ekholm-Modèn model that uses weighted averages of  
115 the minimum and maximum temperatures as well as the temperatures measured at 7 am, 1 pm  
116 and 7 pm. See Li et al. (2016) for more details.

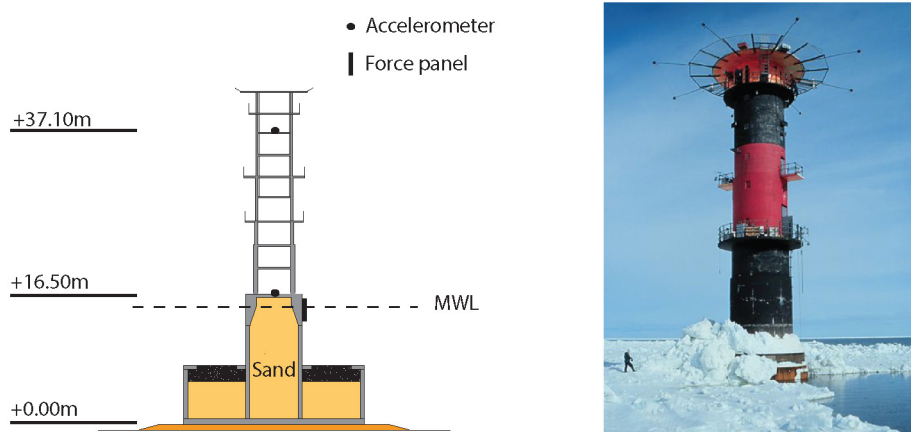
117 EU Copernicus Marine Service Information was used to estimate the local ice concentrations  
118 and ice thicknesses. This information database provided reanalysis using the HIROMB (High-  
119 Resolution Operational Model of the Baltic) model, which may be used to provide mean values

120 for every 6 hours of a variety of met-ocean data. HIROMB has a spatial resolution is 5.5 km,  
121 and the model error (mean RMSE) is 0.08 m and 0.2 for level ice thickness and ice concentration,  
122 respectively (Axell et al., 2017). Note that the model takes into account deformed ice; however,  
123 the error is unknown.

124 Video footage was used in conjunction with an ice drift tracking routine (Leese et al., 1971;  
125 Samardzija, 2018) to obtain the ice velocities during the events of resonant vibrations. This  
126 process was necessary because logbook values of ice velocities were often not written at the  
127 time during events, and video records clearly showed changes in ice velocity. Instances when  
128 ice velocities were written into the data logbook were used as benchmark values for the image  
129 correlation routine. The routine compares two subsequent grayscale frames by taking a  
130 subsection of one image and moving it stepwise on top of the other image until a perfect overlap  
131 is found. A bivariate correlation coefficient is calculated between the image subsection and the  
132 underlying image for each step and further populated into a two dimensional matrix. Each  
133 matrix element corresponds to a specific spatial lag in horizontal and vertical direction. The  
134 matrix element with the maximum correlation coefficient is proportional to the displacement  
135 vector of the ice surface, from which we obtained the ice velocity.

136 Accelerometers installed at +16.5 m and +37.1 m elevation were used to measure accelerations  
137 in two directions in the horizontal plane. The sampling frequency varied from 1 to 100 Hz.  
138 Some events with low sampling frequency that showed tendencies to resonant vibrations were  
139 excluded from further analysis because the low sampling frequency made it too difficult to  
140 interpret the signals. Whenever filters or resampling routines are applied in this paper, it is  
141 specified in the text. Nine panels measured local ice forces and covered the outer perimeter

142 from 0 to 162°. Global ice forces can be estimated from the panels (Nord et al., 2016); however,  
 143 such estimation is outside the scope of this paper.



144

145 **Fig. 1.** Illustration of the accelerometer and force panel locations and picture of the  
 146 Norströmsgrund lighthouse.

147 **2.2 Supplementary measurements from reports: Norströmsgrund 1979-1988**

148 The Norströmsgrund lighthouse was equipped with accelerometers on two levels to measure  
 149 the structural vibrations since the winter of 1973, after service staff noticed that the structure  
 150 oscillated. The first records of resonant vibrations were published in Engelbrektson (1977), in  
 151 which he reported the maximum recorded accelerations on the lighthouse to be 0.33 g. Every  
 152 time the accelerations exceeded 0.07 g, the system stored time histories automatically. In 1980,  
 153 video footage was included in the measurements, but the acceleration trigger level was kept to  
 154 0.07 g. A summary of the measurement program is given in the publication of Engelbrektson  
 155 (1983), which includes a description of the strongest event of resonant vibrations ever recorded  
 156 on the Norströmsgrund lighthouse that occurred on February 28, 1979 at 14.54 h. The same  
 157 event was also described in a later publication (Engelbrektson and Janson, 1985).

158

**Table 1. Measurement methods.**

Measurement type	Accelerations	Ice thickness	Ice velocity

Method 1979-1988	Automatically activated at 0.07 g (1979-1985) and 0.03 g (1985-1988) (Engelbrektsen, 1983; Engelbrektsen, 1987b; Engelbrektsen and Janson, 1985).	Reported from ice breakers and available ice charts (Engelbrektsen, 1987a).	Measurements from ice breakers and calculations based on forecast models (Engelbrektsen, 1987a).
Method 2001-2003	Manually activated during ice-structure interaction (Bjerkås, 2006a).	Measured by sonar, electromagnetic instruments and laser (Haas et al., 2003).	Measured using grid on the video screens (Jochmann and Schwarz, 1999).

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### 160 3 Methods

#### 161 3.1 The signature 2001-2003

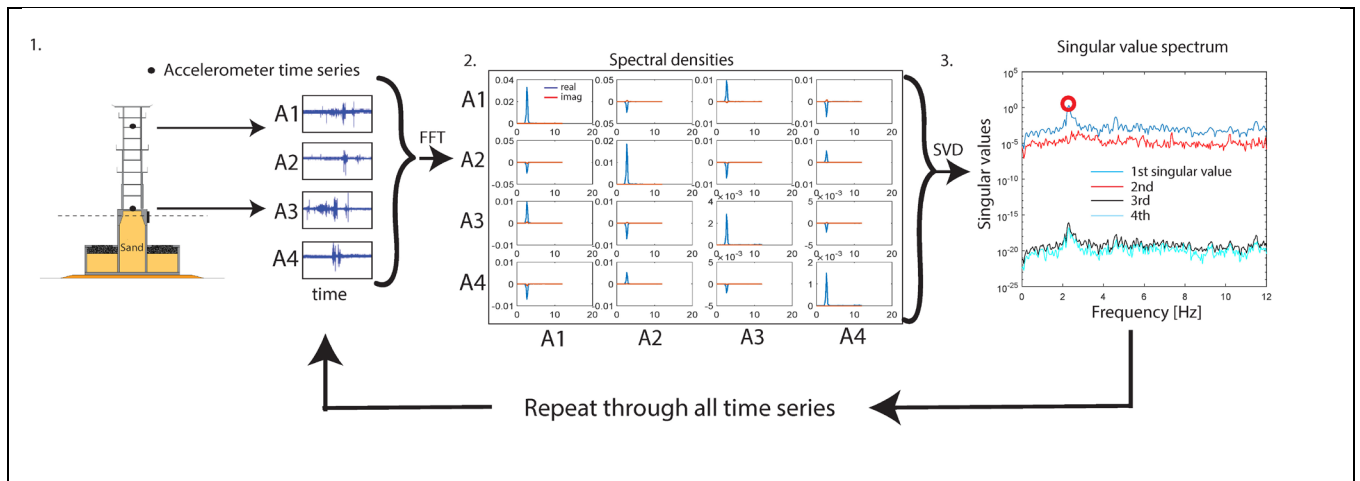
162 This section aims to show how the time series of acceleration measurements were used to define  
163 an event of resonant vibrations. The inherent features in the signals are called the *signature*.

164 The criteria for considering a time series as a resonant vibration event were that the response  
165 showed a) an increase of the amplitude, and b) the dominant response was close to a natural  
166 frequency of the structure. Because the natural frequencies are in fact unknown and may be  
167 closely separated (Nord et al., 2017; Nord et al., 2016), we assumed that responses with a  
168 dominant frequency between 2.0-2.7 Hz could be considered as resonant vibrations. The events  
169 were first selected by visual inspection of all the acceleration response time series in the  
170 STRICE data set. When high amplitudes were observed, the response dominant frequency



171 component was verified by examining the first singular value of the cross power spectral  
 172 densities (Fig. 2): the cross power-spectral densities were calculated from the four acceleration  
 173 time histories. Thereafter, the singular values were extracted using a singular value  
 174 decomposition (SVD) and plotted against frequency.

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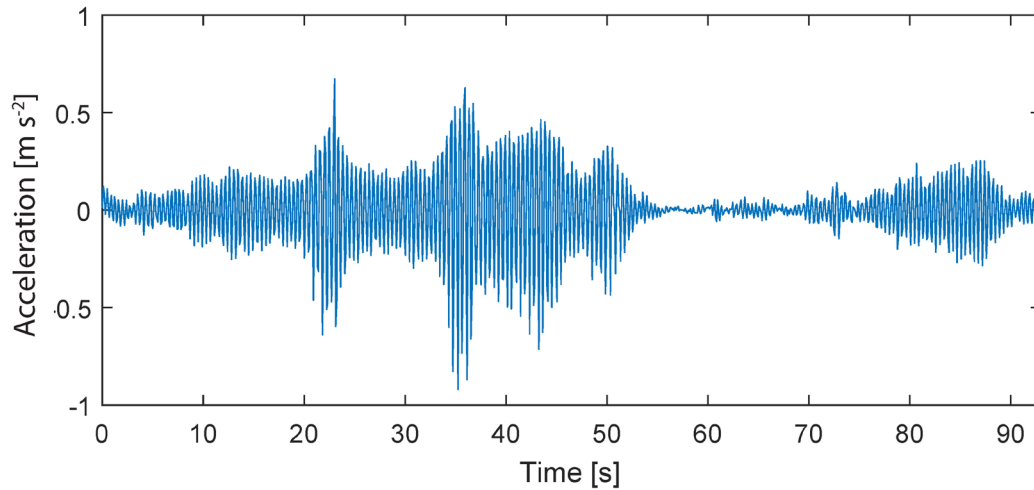


176 **Fig. 2.** Schematic of the data processing flow.

177 The majority of events had variable amplitudes, making it difficult to well-define the durations  
 178 of the individual events: One example that illustrates the variability of the response amplitudes  
 179 and thus the difficulty to choose an event length is shown in Fig. 3. Here, the response fulfilled  
 180 the requirement of a dominant frequency component; however, the response amplitudes are  
 181 small, when compared in particular to the highest acceleration ever recorded of  $6 \text{ m s}^{-2}$ . When  
 182 all events were resampled down to 10 Hz, the power spectral densities showed that most events  
 183 had dominant frequencies between 2.2-2.4 Hz. Three events showed a dominant frequency at  
 184 2.7 Hz, and one event showed a dominant frequency at 2 Hz.

185 For years 1979-1988, no digital data was available, and the judgment is based on statements of  
 186 “resonant vibrations” and inspection of the plotted time histories of acceleration in the  
 187 appendices of Engelbrektsen (1987a) and Engelbrektsen (1989). Note that, in what follows, the

188 numbers of days and events of resonant vibrations are uncertain and depend on both the  
189 measurement system and the level of details in the reports.



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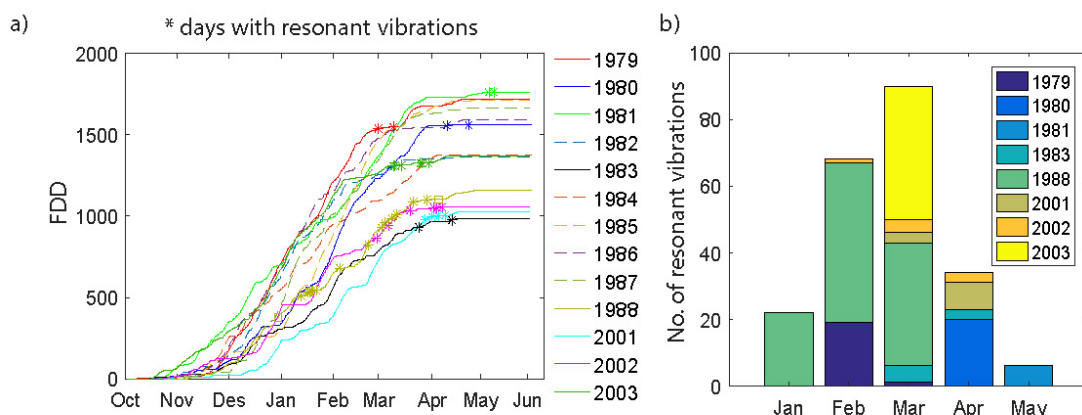
191 **Fig. 3.** Response during a low-amplitude resonant vibration event (# 44 in Table 2).

## 192 **4 Results**

### 193 **4.1 Seasonal overview from 1979-2003**

194 The 37 days in which resonant vibrations were measured (and reported) are plotted against FDD  
195 in Fig. 4 a. The cold winters, 1979, 1980 and 1981 all had two days when resonant vibrations  
196 were measured. Based upon the available literature, no projects were assigned to the winter of  
197 1982; this lack of projects may also explain why no events were reported. The warmest winter  
198 (1983) had two days when resonant vibrations were measured. During the winters of 1984 and  
199 1985, no accelerations exceeded 0.07 g (Engelbrektson, 1987a). In the winters of 1986 and  
200 1987, no resonant vibration events of interest were recorded (Engelbrektson, 1989). The winter  
201 of 1988, which was slightly warmer than the 65 year average (Li et al., 2016), had 13 such days  
202 of resonant vibrations and the largest number of events, followed by the winters of 2003 and

203 1980 (Fig. 4b). The earliest events occurred in January, and the latest occurred in May; most  
 204 events occurred during March, followed by February and April (Fig. 4b).



205  
 206 **Fig. 4.** Seasonal overview of resonant vibration events: a) freezing degree days and days with  
 207 resonant vibrations from 1979-2003 according to Li et al. (2016); b) number of events per  
 208 month for different years.

209 **4.2 Results from measurements 2001-2003**

210 In total, 61 events of resonant vibrations were identified in the data from 2001-2003 (Table 2).  
 211 Figures of the upper level acceleration (cf. Fig. 1) for all events are given in Appendix 1. Except  
 212 for the dominant frequency component, the response and force time histories varied notably. A  
 213 steady-state response with constant amplitudes seldom occurred. At times, the response  
 214 appeared close to steady-state; however, with closer inspection, the amplitudes changed from  
 215 cycle to cycle.

216 **Table 2.** Events of resonant vibration measured between 2001 and 2003.

No	Date of event [DD.MM.YYY Y]	Data file id	Start time [hhmmss]	End time [hhmmss]	Ice thickness s [m]	Ice velocity [m s <sup>-1</sup> ]	Peak acceleratio n [m s <sup>-2</sup> ]	10 peaks average acceleratio n [m s <sup>-2</sup> ]
1	28.03.2001	01_2803_03 00	081123	081132	0,33	0,028	0,31	0,27

2	28.03.2001	01_2803_03 00	084230	084237	0,26	0,028	0,70	0,34
3	28.03.2001	01_2803_03 00	090538	090547	0,27	0,028	0,60	0,41
4	01.04.2001	01_0104_04 00	093357	093405	0,40	0,046	1,40	1,07
5	01.04.2001	01_0104_04 00	093847	093927	0,40	0,038	1,63	1,24
6	05.04.2001	01_0504_04 00	154755	154802	0,90	0,075	1,65	1,31
7	09.04.2001	01_0904_04 00	223741	223807	0,63	0,050	1,69	1,43
8	09.04.2001	01_0904_04 00	223830	223845	0,66	0,050	1,03	0,78
9	09.04.2001	01_0904_04 00	223920	223953	0,57	0,050	2,13	1,84
10	09.04.2001	01_0904_04 00	224012	224023	0,62	0,050	0,96	0,76
11	09.04.2001	01_0904_04 00	224157	224233	0,65	0,050	1,66	1,52
12	27.02.2002	02_2702_02 00	191534	191612	1,67	0,041	0,31	0,27
13	06.03.2002	02_0603_01 00	002310	002345	0,78	0,051	2,15	1,37
14	19.03.2002	02_1903_07 00	215818	215830	0,60	0,026	0,67	0,52
15	19.03.2002	02_1903_07 00	220044	220102	0,60	0,023	1,00	0,87
16	19.03.2002	02_1903_07 00	220600	220610	0,60	0,024	0,45	0,37

17	02.04.2002	02_0204_02 00	064842	064856	0,40	0,026	1,11	0,67
18	04.04.2002	02_0404_02 00	103826	103847	0,40	0,027	1,08	0,60
19	04.04.2002	02_0404_03 00	104315	104323	0,48	0,027	0,82	0,58
20	07.04.2002	02_0704_02 00	54040	054046	1,08	0,042	0,81	0,50
21	09.03.2003	03_0903_02 00	005607	005640	0,60	0,041	1,57	1,18
22	09.03.2003	03_0903_02 00	010023	010040	0,60	0,059	1,98	1,46
23	09.03.2003	03_0903_02 00	010340	010401	0,60	0,048	1,41	1,20
24	10.03.2003	03_1003_02 00	035915	035922	0,73	0,056	2,54	1,24
25	10.03.2003	03_1003_02 00	040112	040118	0,79	0,058	0,90	0,58
26	10.03.2003	03_1003_02 00	040136	040142	0,79	0,058	0,55	0,40
27	14.03.2003	03_1403_04 00	221620	221627	0,80	0,037	0,36	0,32
28	25.03.2003	03_2503_06 00	153247	153258	0,90	0,052	1,92	1,18
29	25.03.2003	03_2503_06 00	153343	153403	0,98	0,050	2,24	1,57
30	25.03.2003	03_2503_06 00	153617	153623	0,95	0,052	1,44	1,05
31	25.03.2003	03_2503_06 00	153640	153653	0,95	0,051	1,73	1,34

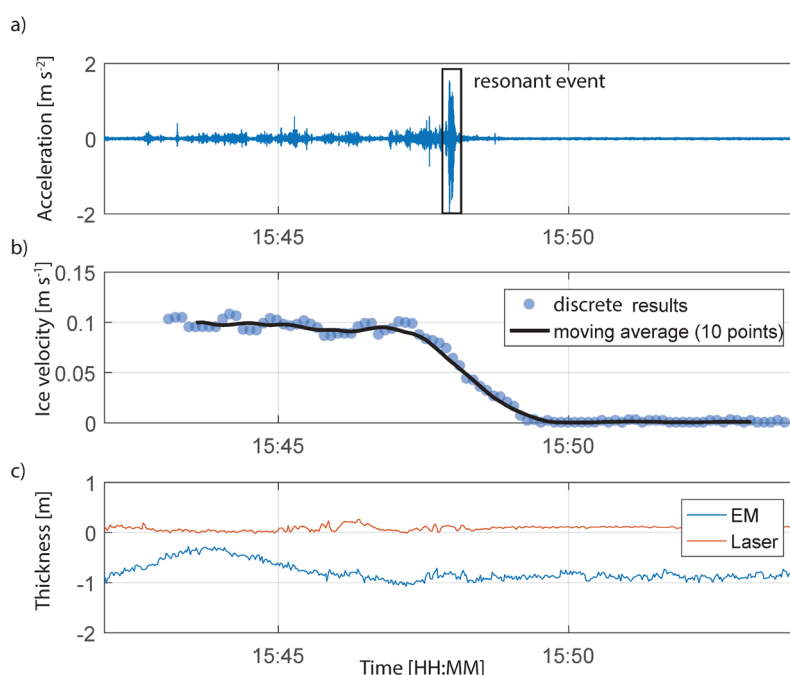
32	25.03.2003	03_2503_06 00	153708	153722	0,93	0,053	1,60	1,28
33	25.03.2003	03_2503_06 00	154318	154327	0,89	0,054	0,82	0,73
34	25.03.2003	03_2503_06 00	155658	155743	0,88	0,045	1,58	1,29
35	25.03.2003	03_2503_06 00	160101	160105	0,86	0,043	1,60	0,95
36	25.03.2003	03_2503_06 00	160234	160240	0,95	0,039	0,75	0,63
37	25.03.2003	03_2503_06 00	160632	160751	1,08	0,041	1,77	1,58
38	25.03.2003	03_2503_06 00	162054	162139	0,98	0,042	1,15	1,11
39	25.03.2003	03_2503_06 00	162255	162305	0,98	0,041	0,93	0,78
40	25.03.2003	03_2503_06 00	163159	163212	0,86	0,040	1,02	0,92
41	25.03.2003	03_2503_06 00	170523	170530	0,84	0,031	0,90	0,67
42	25.03.2003	03_2503_06 00	171120	171130	0,88	0,027	1,16	0,91
43	25.03.2003	03_2503_06 00	171242	171253	0,84	0,027	0,85	0,62
44	25.03.2003	03_2503_07 00	192148	192320	1,50	0,036	1,00	0,79
45	25.03.2003	03_2503_07 00	192448	192514	1,90	0,035	0,54	0,47
46	26.03.2003	03_2603_02 00	121746	121825	1,00	0,043	0,73	0,58

47	26.03.2003	03_2603_02 00	122829	122955	1,00	0,040	0,99	0,85
48	26.03.2003	03_2603_02 00	123118	123218	1,00	0,031	0,92	0,78
49	30.03.2003	03_3003_04 00	120338	120352	0,91	0,037	0,76	0,54
50	30.03.2003	03_3003_04 00	120524	120539	1,03	0,038	1,13	0,90
51	30.03.2003	03_3003_04 00	120547	120624	0,90	0,041	1,52	1,18
52	30.03.2003	03_3003_04 00	121419	121431	0,88	0,047	1,09	0,87
53	30.03.2003	03_3003_04 00	121500	121514	0,91	0,047	1,26	0,99
54	30.03.2003	03_3003_04 00	121738	121748	0,87	0,045	0,65	0,58
55	30.03.2003	03_3003_04 00	122538	122700	0,70	0,049	1,96	1,82
56	30.03.2003	03_3003_04 00	122950	123007	0,80	0,050	0,99	0,82
57	30.03.2003	03_3003_04 00	123301	123311	0,70	0,052	0,86	0,58
58	30.03.2003	03_3003_04 00	124243	124253	0,77	0,051	0,58	0,41
59	30.03.2003	03_3003_05 00	125818	125847	0,78	0,053	0,73	0,61
60	30.03.2003	03_3003_05 00	130144	130148	1,20	0,053	0,85	0,61
61	30.03.2003	03_3003_05 00	130918	130928	1,20	0,057	0,89	0,64

217

#### 218 4.2.1 Ice velocity

219 Several events had significant changes in ice velocity prior to, during and after an event of  
220 resonant vibrations, as illustrated in Fig. 5, wherein the acceleration ice velocity and ice  
221 thickness are given for April 5, 2001. Here, the event started at 15.47.55 and lasted for  
222 approximately 7 seconds, during which the structural responses significantly increased (Fig.  
223 5a), the mean ice velocity was approximately  $0.075 \text{ m s}^{-1}$  (Fig. 5b) and the ice thickness was  
224 approximately 0.9 m (Fig. 5c). When the ice velocity slowed down to zero, the acceleration  
225 decreased and resulted in ductile (creep) interaction.



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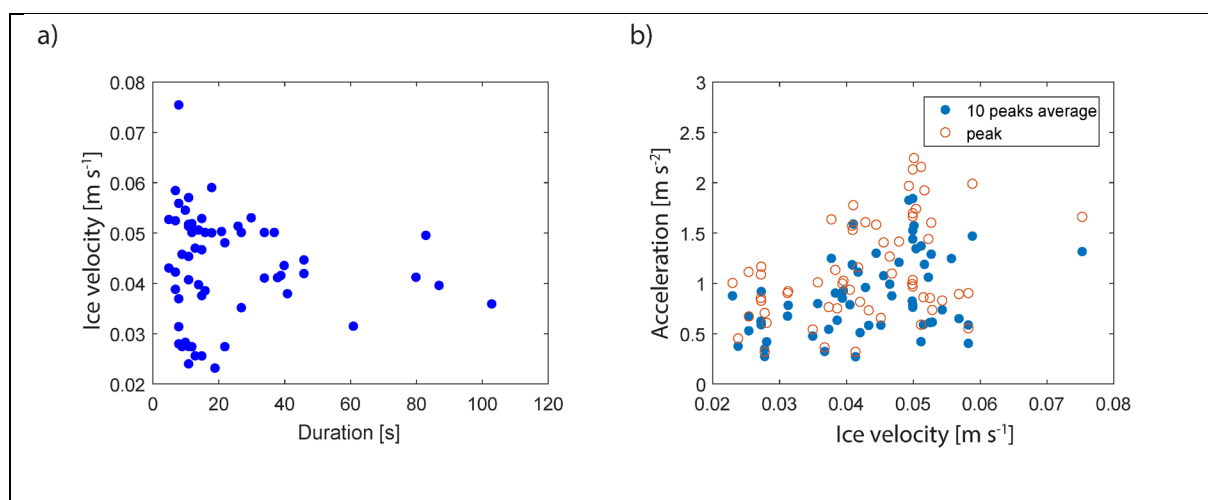
227 **Fig. 5.** Acceleration (a), ice-drift velocity (b) and ice thickness (c) on April 5, 2001.

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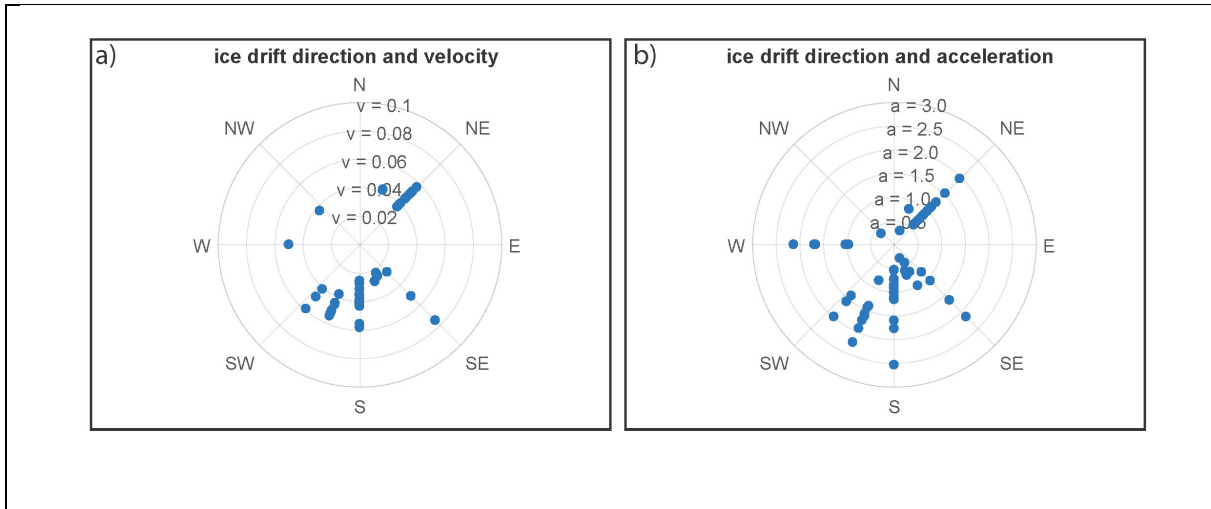
229 The mean duration of the events was approximately 22 seconds, while only 5 events were longer  
230 than 60 seconds (Fig. 6a). The mean ice velocity was  $0.043 \text{ m s}^{-1}$ ; hence, the average event  
231 crushed approximately 0.9 m of ice. The highest measured acceleration at the top of the



232 structure occurred with an ice velocity of  $0.055 \text{ m s}^{-1}$ . The average of the 10 highest acceleration  
233 peaks in an event was often significantly lower than the highest peak (Fig. 6b). Note that the  
234 accelerations used in this as well as the following figures and text are the absolute values of the  
235 two sensors at top and that the acceleration time series are resampled down to 10 Hz to make  
236 them comparable with each other. At times, the resampling affected the amplitudes; as a result,  
237 quantities derived from the values presented in the figures and Table 2 may be erroneous. The  
238 mean of the maximum accelerations at the top for all events was  $1.15 \text{ m s}^{-2}$ . The events that had  
239 ice velocities of less than  $0.03 \text{ m s}^{-1}$  were primarily caused by ice drift from south and southeast  
240 (Fig. 7a), and top accelerations exceeding  $2 \text{ m s}^{-2}$  occurred with ice-drift from west, southwest,  
241 south, southeast and northeast (Fig. 7b). Four out of five events with durations in excess 60  
242 seconds were caused by ice drift from south, while the fifth was caused by ice drift from  
243 northeast.



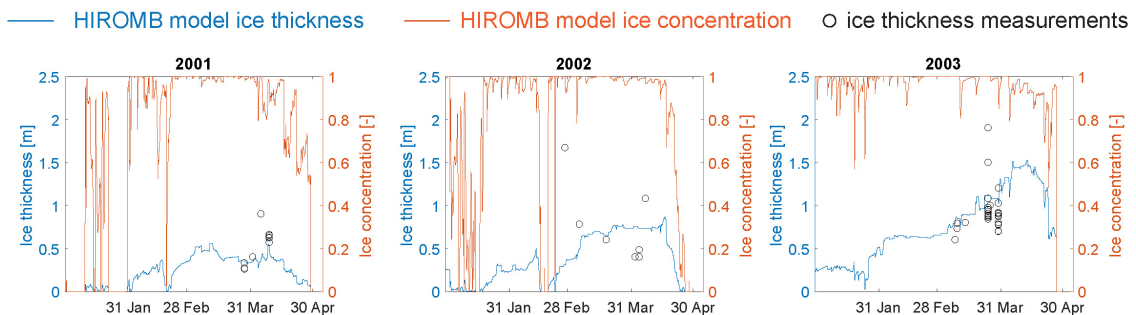
244 **Fig. 6.** Ice velocity versus duration of the events (a) and acceleration at the upper level versus  
245 ice velocity (b).



246 **Fig. 7.** Ice drift direction versus a) ice velocity and b) event peak acceleration at the top level.

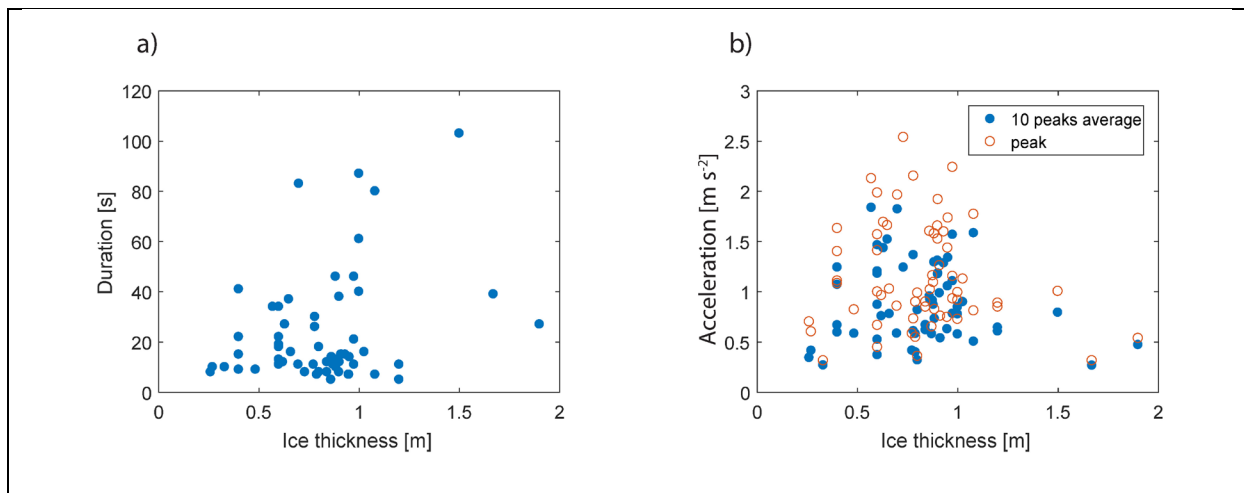
247 **4.2.2 Ice thickness and ice concentration**

248 The six hour mean ice thickness and ice concentration generated using E.U. Copernicus Marine  
 249 Service Information (E.U.Copernicus, 2017) are given in Fig. 8. The ice thickness  
 250 measurements in 2001 coincide the most with the model (Fig. 8), whereas measurements in  
 251 2002 correspond to the single largest difference between the model and the measurement. All  
 252 events of resonant vibrations occurred with ice concentrations in excess 0.85. Based on the  
 253 measured thickness in conjunction with video records, resonant vibrations occurred during  
 254 interaction with both rafted and ridged ice. Events that lasted longer than a minute occurred for  
 255 ice thicknesses between 0.7 and 1.5 m (Fig. 9a), and events with the highest accelerations  
 256 occurred for ice thickness between 0.4 and 1.2 m (Fig. 9b).



257

258 **Fig. 8.** Ice thickness and ice concentration obtained from the HIROMB model displayed  
 259 together with ice thickness measurements during the resonant vibrations events.



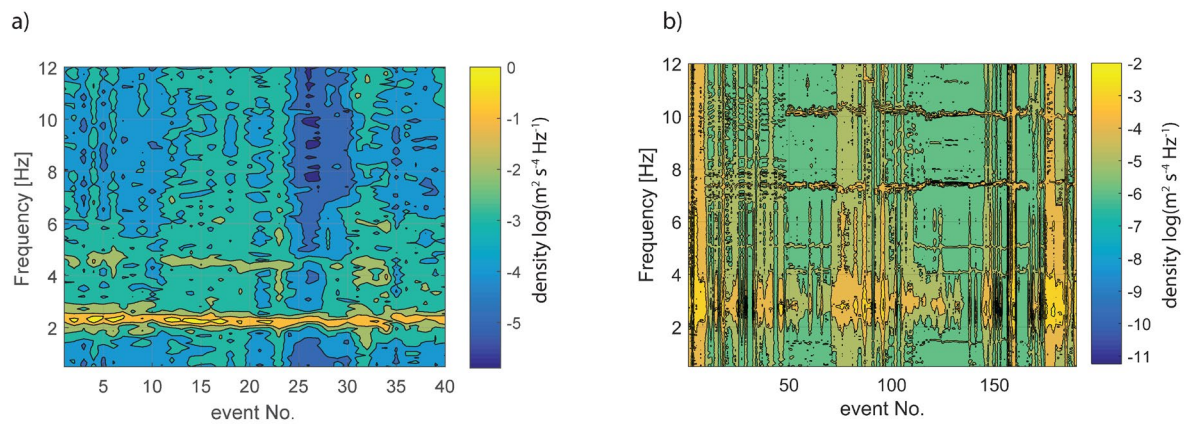
260 **Fig. 9.** Event duration versus ice thickness (a) and event peak acceleration at the top level  
 261 versus ice thickness (b).

## 262 **5 Discussion**

263

### 264 **5.1 The signature**

265 For events where the acceleration signal sampling frequency was 30 Hz or higher, it was  
 266 effective to plot the first singular value of the cross power spectral density of each event in a  
 267 colormap to determine whether events fulfilled the criterion of a dominant frequency  
 268 component (Fig. 10a). Each event was also compared with a colormap that was generated using  
 269 the same method and same sensors but for events in which other failure modes governed the  
 270 interaction, e.g., flexural failures, splitting, creep, and brittle crushing (Fig. 10b). Nord et al.  
 271 (2017) explained the details of the selection criteria for these events that were used in a system  
 272 identification study. The resonant events display a much narrower band between 2.0-2.7 Hz  
 273 (mostly 2.2-2.4 Hz), whereas other interaction regimes spread the energy over several  
 274 frequencies.



275

276 **Fig. 10.** Singular value colormap of a) resonant vibration events and b) other interaction regimes.

277

278 The resonant vibration events had a large range of response amplitudes, partly because of the  
 279 limited constraints on the selection. At times, the response amplitudes were lower than those  
 280 for some cases of continuous brittle crushing. Because of the lack of a response amplitude  
 281 threshold, the duration was dependent on the analyst interpretation. Attempts to better define  
 282 durations by using response amplitudes from instances in which other failure modes governed  
 283 the interaction as a lower threshold did not succeed because: a) the response prior to and after  
 284 an event was often governed by different failure modes (e.g., flexural failure prior to the event  
 285 and limit-force stalling after the event) and b) the ice conditions were often heterogeneous,  
 286 resulting in variability in the acceleration response, which made it difficult to decide upon a  
 287 threshold. Any instance of a sudden global ice failure may also lead to transient responses which  
 288 may appear as resonant ice-induced vibrations. It is herein assumed that such transient  
 289 responses would not inherit a response amplitude build up and cycles of sustained high-  
 290 amplitude vibrations.

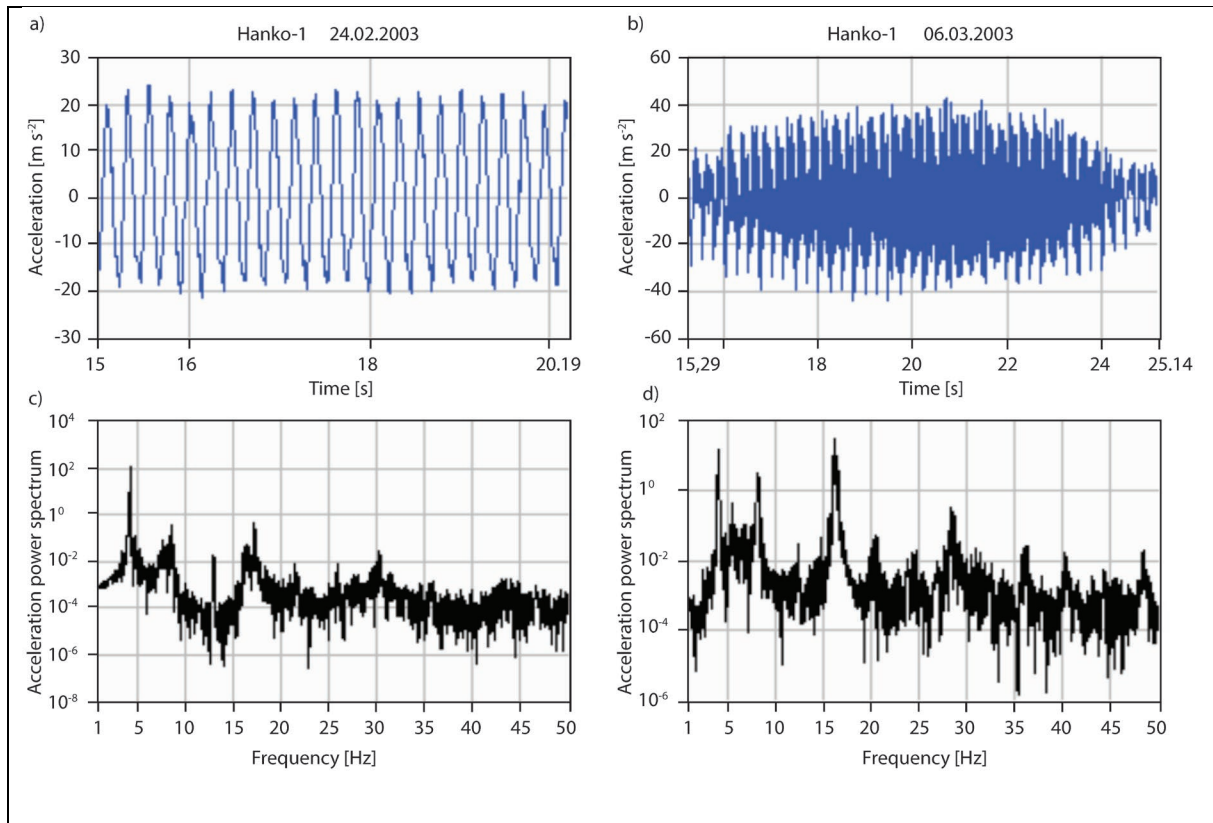
291 Given the wide range of ice velocities and ice thicknesses for which resonant vibration occurred,  
 292 the observed response differences between resonant vibration events may not be surprising. If  
 293 the crushing failure process is sensitive to small variations in the ice conditions, so will the

294 response. It was, however, difficult to determine the failure process from the video records.  
295 Panel forces may be used as a means to study how the level of synchronization between the  
296 panel forces affects the resonant vibration events. Such a study requires careful treatment of the  
297 varying sampling frequency between the events and falls outside the scope of this paper. In  
298 addition, in many of the 61 events, the ice approached from directions in which the lighthouse  
299 had no or limited coverage of load panels.

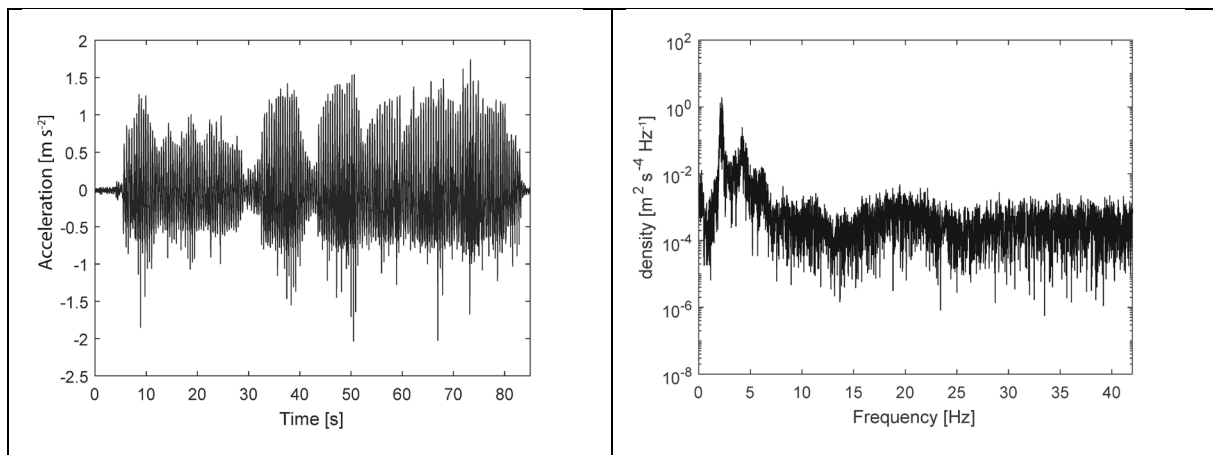
300 Määttänen (1975) and Nordlund et al. (1988) also reported differences among FLI type of ice-  
301 induced vibration. The latter measured 29 events of FLI on the KR11 channel marker, from  
302 which events were subdivided into high and low-level amplitudes. The lower the amplitudes,  
303 the more random were the vibrations. The durations varied between 2 and 53 minutes and often  
304 occurred with long periods of steady-state response (Kärnä, 1994; Nordlund et al., 1988). For  
305 offshore structures in the Bohai Bay, steady-state vibrations are also a common signature of  
306 measured FLI events (Yue et al., 2009), with durations up to 10 minutes (Yue et al., 2002). At  
307 Norströmsgrund, most events were less than 20 seconds, and few showed steady-state  
308 vibrations. Examples of steady-state vibrations can be found in Appendix 1 in Engelbrektsen  
309 (1987a). The most violent event of resonant vibration measured on Norströmsgrund showed,  
310 however, no steady-state.

311 Although it appears as Norströmsgrund's vibration response varies more than for other  
312 structures exposed to IIV, these response differences are also reported from structures located  
313 in different areas. In the Gulf of Finland, resonant vibrations were measured on the Hanko-1  
314 channel marker on February 24, 2003 and March 6, 2003 (Fig. 11) (Määttänen, 2003; Määttänen,  
315 2008). The first event showed steady-state FLI vibrations (Fig. 11a), whereas the second event  
316 showed less steady-state character (Fig. 11b). The first event was found to have a dominant  
317 frequency component near the first natural frequency (Fig. 11c), whereas the second event was  
318 found to have a dominant frequency component close to one of the higher modes (Fig. 11d).

319 Similarities between the February 24 event and a Norströmsgrund event (Fig. 12) can be seen  
320 comparing the frequency ranges 1-10 Hz for Hanko-1 (Fig. 11c) and 1-5 Hz for Norströmsgrund  
321 (Fig. 12b); the most striking difference is that the Hanko-1 steel structure has much higher  
322 contributions in the higher modes. The modal damping and the force influence at the ice action  
323 point to the modes are important for determining which modes are susceptible to FLI and thus  
324 influence its signature. The signature of resonant vibrations found for one structure is therefore  
325 not necessarily a valid signature for other structures and may largely be influenced of the sensor  
326 location. Consequently, there are measurements in field and laboratory of vibrations that fall  
327 outside the definition of FLI used in the standard. As a result, uncertainty in fatigue life  
328 predictions and confusion exists around the definition of FLI. More full-scale time series of ice-  
329 induced vibrations may lead to precise signatures of regimes of ice-induced vibrations, which  
330 in turn influence how to design structures and how to design laboratory experiments; such data  
331 may elucidate the most important and least understood process, namely, the occurrence of FLI.  
332



333 **Fig. 11.** Vibration events of the Hanko-1 Channel Marker: a) and b) time series of  
 334 acceleration, c) and d) power spectrum of the acceleration (Courtesy of Määtänen (2003)).



335 **Fig. 12.** Vibrations on Norströmsgrund lighthouse March 30, 2003: a) time series plot of  
 336 acceleration and b) power spectral density of acceleration (from Nord et al. (2016)).

337

## 338 5.2 The occurrence aspect

339 The events of resonant vibrations occurred for days with very different FDDs; however, for  
 340 each year, little increase in the FDD occurred after the last day of resonant vibrations (cf. Fig.  
 341 4). Besides the observations that the resonant vibrations on Norströmsgrund occurred when the

342 ice concentration exceeded 0.85, the ice thickness exceeded 0.26 m and the ice velocity  
343 exceeded  $0.023 \text{ m s}^{-1}$ , the onset conditions remain unsolved. Several ice thicknesses and ice  
344 velocities that were present during resonant vibrations overlap with instances where other  
345 modes of ice-structure interaction were present. The wider the structure, the more susceptible  
346 it becomes to failure modes other than crushing (Daley et al., 1998; Sanderson, 1988; Timco,  
347 1987), and with the great uncertainty in the ice thickness and ice velocity, predicting the failure  
348 mode becomes difficult.

349 The ice drift in the northern Gulf of Bothnia is mainly driven by winds, and local ice drift near  
350 Norströmsgrund is also influenced by the lead created by ice breakers and the edge to the  
351 landfast ice. The Farstugrund lighthouse, which is located approximately 29 km northeast of  
352 Norströmsgrund, has a slightly stiffer substructure and was equipped with the same data  
353 acquisition system for monitoring vibrations during the winter of 1988. Engelbrektsen (1989)  
354 noted only a few events of resonant vibrations on the Farstugrund lighthouse during the full  
355 1988 winter season (the days are marked with squares in Fig. 4) and explained this observation  
356 by more stationary ice conditions than those at Norströmsgrund.

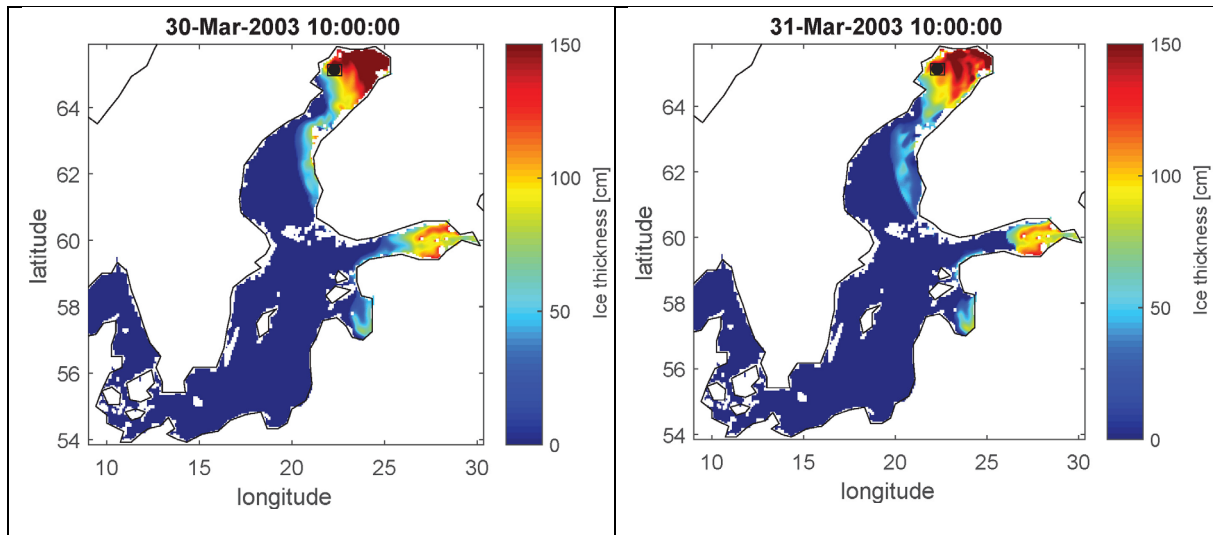
357 Bjerckås et al. (2012) showed that, from February 14 to March 31 in 2003, a large lead opened  
358 in the northern Gulf of Bothnia. They estimated the open lead to be 15 km wide, although little  
359 is known about the time history of the lead opening. It was possible to track the ice thickness  
360 spatiotemporal variation using the ice thickness reanalysis available in the E.U. Copernicus  
361 Marine Service Information. March 25 and March 30 were the days in the STRICE project that  
362 had the most events of resonant vibrations. No significant changes were discovered around  
363 March 25, whereas from the evening on March 30 until the afternoon on March 31, the ice  
364 thickness (Fig. 13) and the ice concentration in the northern Gulf of Bothnia changed  
365 significantly. As most events of resonant vibrations occurred during the daytime and early



366 afternoon, it is unclear whether the days in which drastic changes occur in the whole ice cover  
367 in northern Gulf of Bothnia are the days to expect resonant vibrations.

368 Temperature affects the ice mechanical properties through the porosity, and many of the events  
369 in 2001-2003 occurred during days in which the air temperatures exceeded 0°C. The mean and  
370 standard deviation of the air temperatures were -0.29°C and 2.58°C, respectively. Four events  
371 occurred at air temperatures less than -4°C, and four events had air temperatures greater than  
372 +4°C. Bjerkås et al. (2013a) estimated ice growth from FDD and studied measured ice  
373 temperature profiles collected at Norströmsgrund, and discussed their influence on the crushing  
374 behavior and occurrence of frequency lock-in vibrations. They showed that the temperature  
375 profiles changed from linear on February 28 in 2003 to irregular and c-shaped on March 9 and  
376 10, respectively. March 9 and 10 were the first days during which resonant vibrations occurred  
377 that winter (Table 2). Their observations of the changed crushing behavior together with the  
378 decaying ice growth (Fig. 4a) and changed ice temperature profiles led to the hypothesis stating  
379 that frequency lock-in vibrations were more likely to occur late in winter because high ice  
380 temperatures would cause a more uniform contact at the ice-structure interface. However, Fig.  
381 4a also shows considerable increase in FDD between end of February to mid-March in 1988,  
382 also a time period during which resonant vibrations occurred. Despite this increase in FDD, it  
383 does not necessarily refute the hypothesis of Bjerkås et al. (2013a), as other factors may  
384 influence the ice temperature profile, and thus the mechanical properties.

385 Little is reported on floe size and confinement around structures susceptible to resonant  
386 vibrations. As more abundant and accurate met-ocean data can be retrieved for today's ice  
387 conditions in the Baltic Sea, new measurements of resonant vibrations and FLI may be better  
388 understood.



389 **Fig. 13.** HIROMB model estimate of the ice thickness on March 30-31, 2003.

390

## 391 **6 Conclusions**

392 Available data on the Norströmsgrund lighthouse in the northern Baltic were examined, and  
 393 events with resonant vibrations were identified and discussed. For the STRICE data collected  
 394 between 2001 and 2003, all time series of accelerations were used to identify events of resonant  
 395 vibrations and to understand their inherent characteristics, i.e., their so-called signature. An  
 396 attempt was further made to quantify the ice conditions for which resonant vibrations occur.  
 397 The major findings can be summarized as follows:

- 398 • Sixty-one events of ice-induced vibrations measured on the Norströmsgrund lighthouse  
 399 were classified as resonant vibrations between 2001 and 2003. The events were  
 400 governed by response oscillations with a dominant frequency component between 2 and  
 401 2.7 Hz, with most between 2.2 and 2.4 Hz.
- 402 • Steady-state acceleration responses were seldom observed.
- 403 • The events encompassed level ice, rafted ice and ridges, in which ice thicknesses and  
 404 ice velocities ranged from 0.26 to 1.9 m and from 0.023 to 0.075 m s<sup>-1</sup>, respectively.

405 The longest event lasted for 100 seconds, and the average event lasted 22 seconds, which  
406 is significantly shorter than FLI reported on other structures.

- 407 • All events occurred on days in which the ice concentration was estimated as 0.85 or  
408 greater.

409 The results were compared with measurements of resonant vibrations from 1979-1988. In  
410 summary, most events occurred in the winter of 1988, followed by the winters of 2003 and  
411 1980.

412 Furthermore, once resonant ice-induced vibrations violate the steady-state signature of FLI,  
413 they fall outside definitions of modes of ice-induced vibrations in the standards. Because the  
414 strongest resonant vibrations of Norströmsgrund violated this steady-state condition, we  
415 suggest that the steady-state or sinusoidal response is not a necessary and sufficient condition  
416 for FLI.

## 417 **7 Acknowledgements**

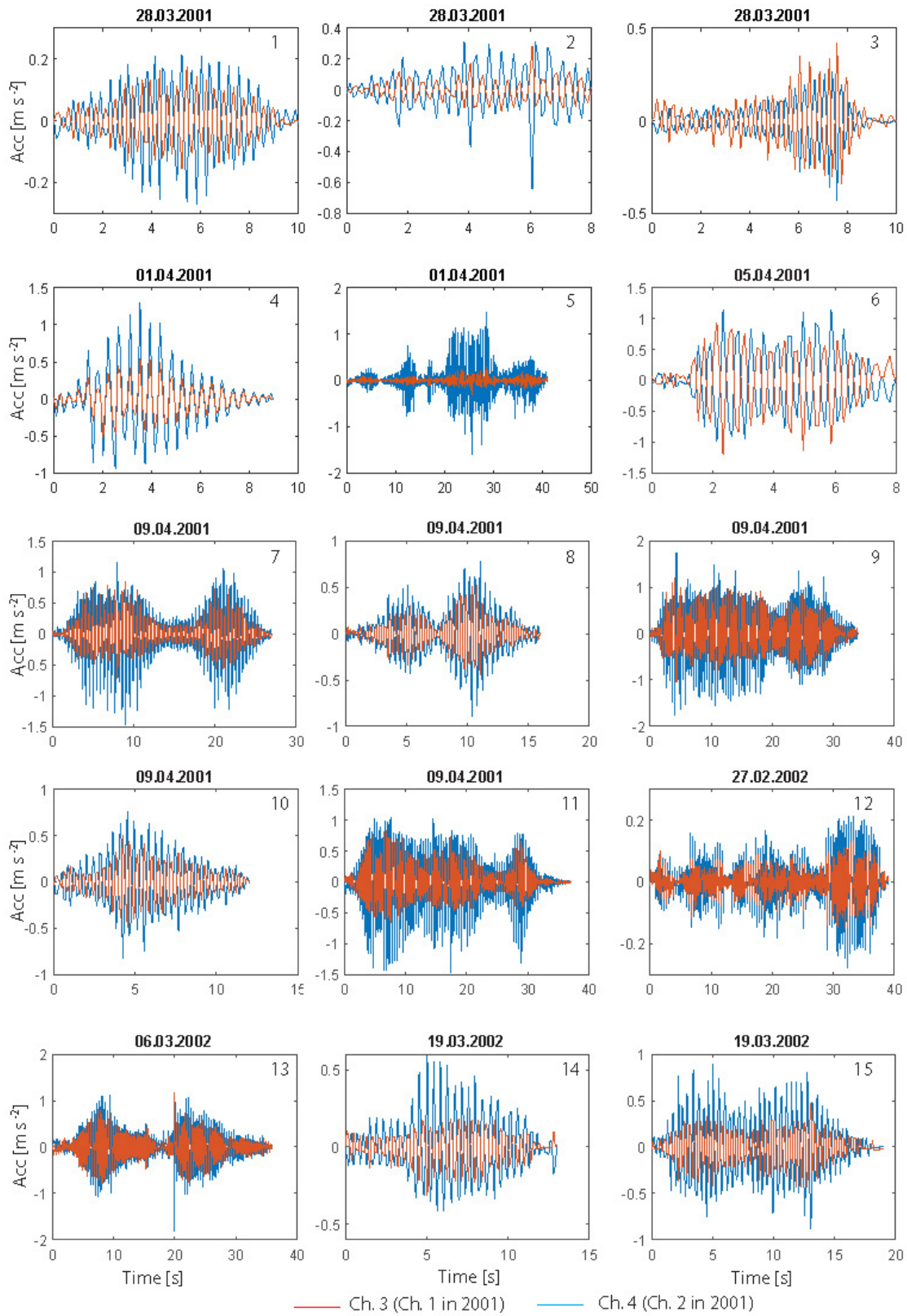
418 The authors wish to acknowledge the support of the Research Council of Norway through the  
419 Centre for Research-based Innovation, SAMCoT and the support of the SAMCoT partners.

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422 Environment and Sustainable Development (EESD) Program under the Key Action RTD  
423 activities of a generic nature (Contract No. EVG1-CT-2000-00024).

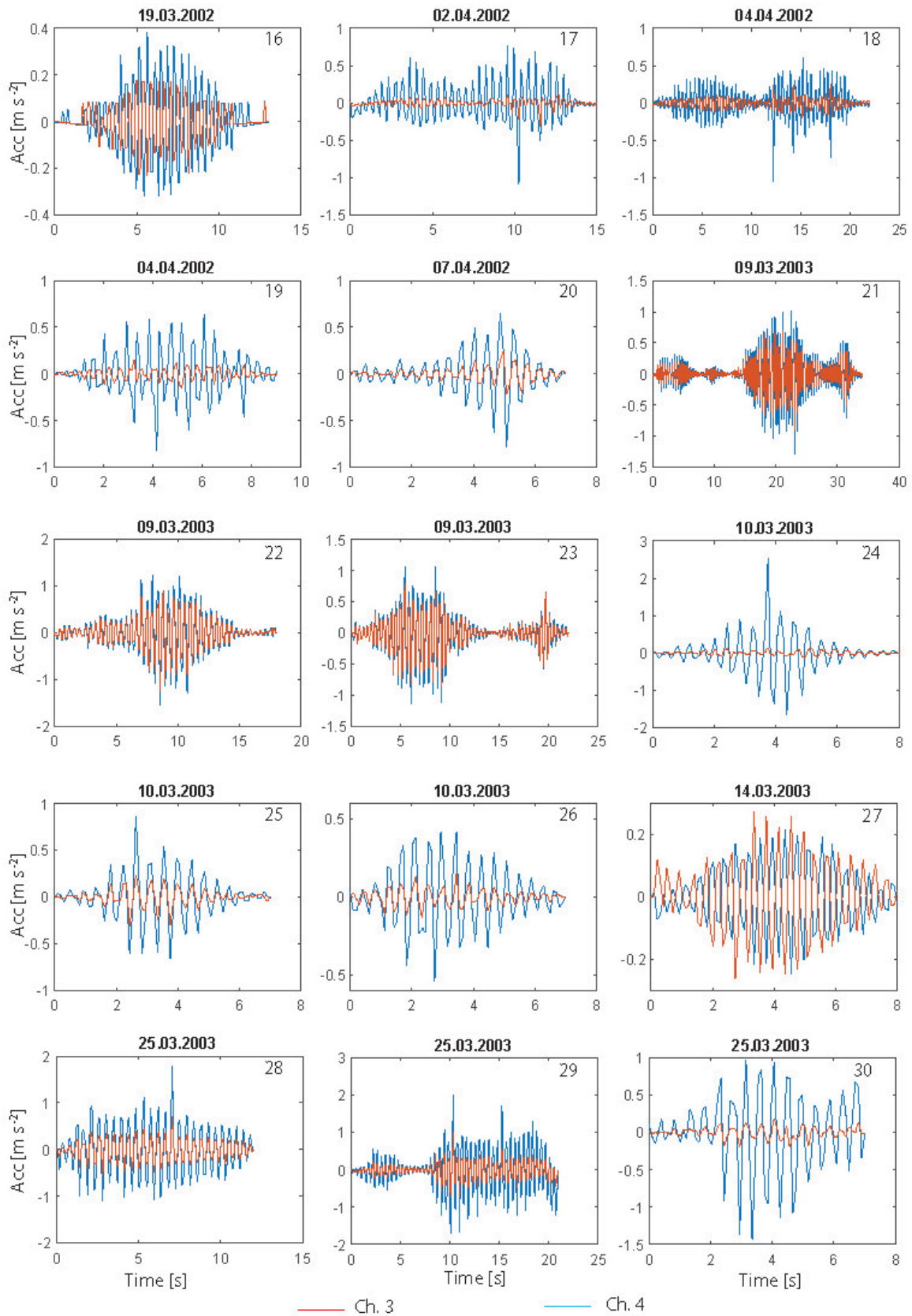
424 The authors wish to further acknowledge Lennart Fransson, Peter Jochmann and Mauri  
425 Määttänen for their efforts to provide information and insight to the measurements of ice-  
426 induced vibrations in the Baltic Sea.

427

428 **Appendix A Acceleration time series of resonant vibrations at +37.1 m elevation.**

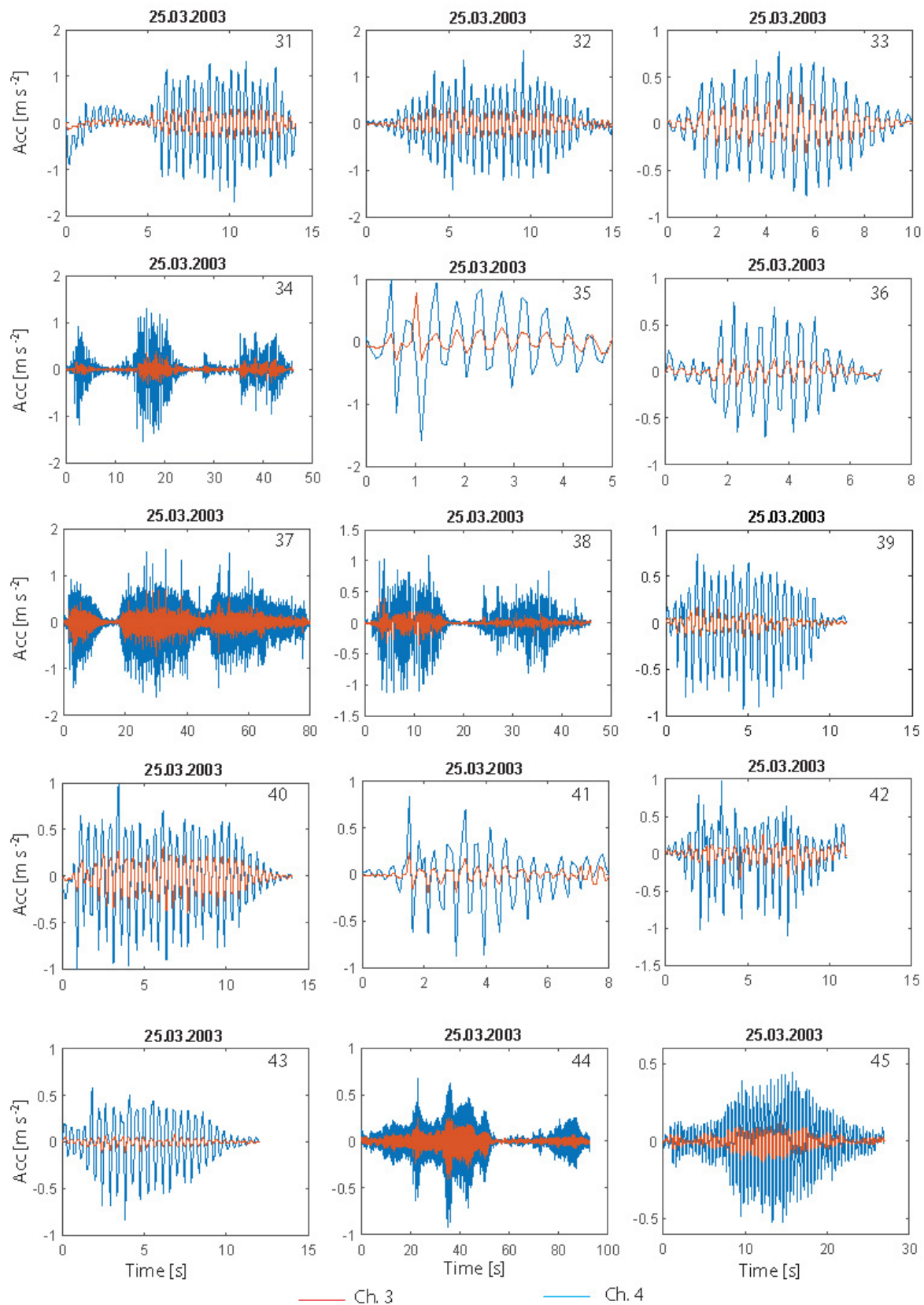


430 **Fig. 14.** Acceleration time series of resonant vibrations at +37.1 m elevation. Red and blue  
431 colors correspond to acceleration channels 3 and 4, respectively (in 2001 channels 1 and 2).



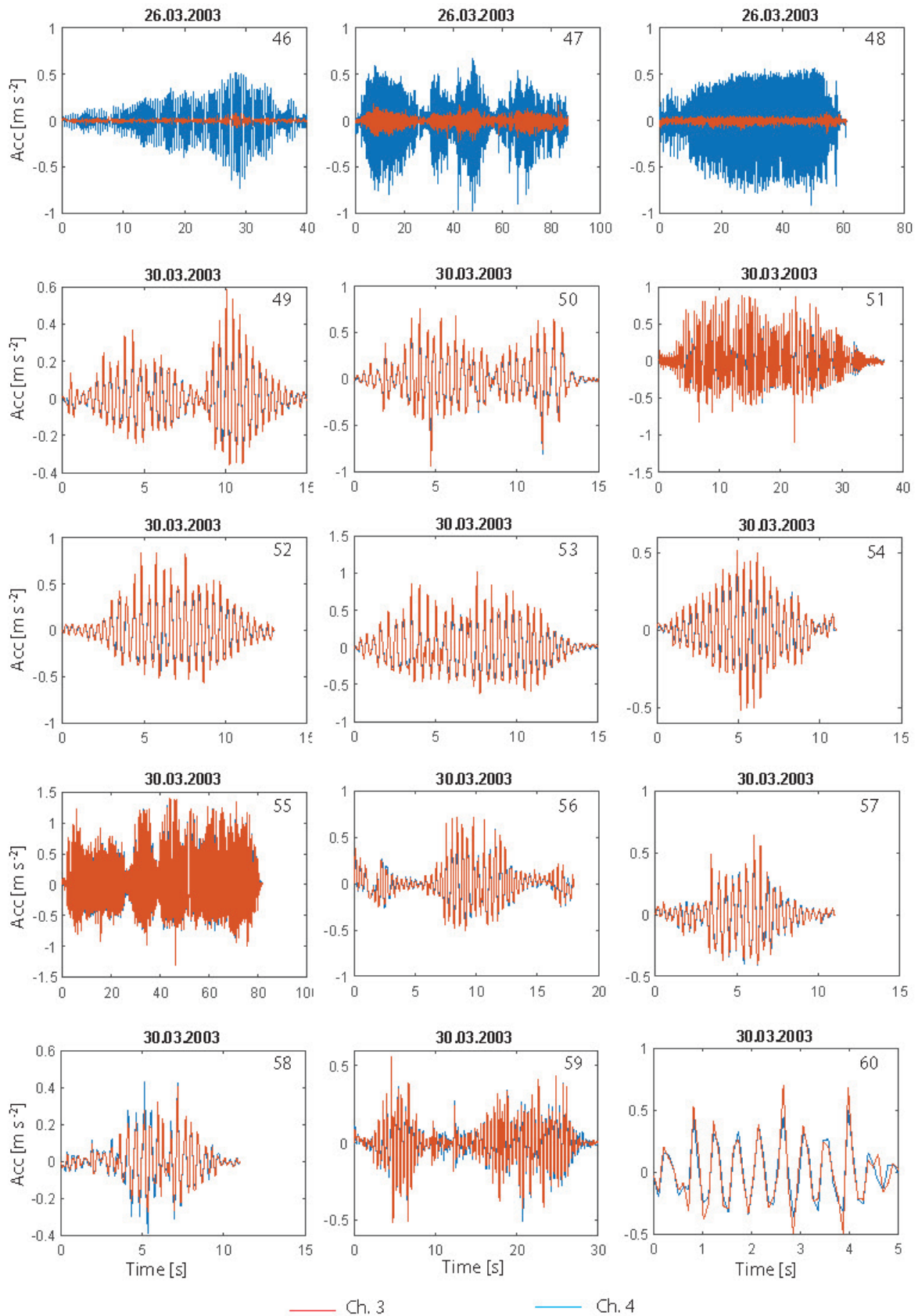
432

433 **Fig. 15.** Acceleration time series of resonant vibrations at +37.1 m elevation. Red and blue  
 434 colors correspond to acceleration channels 3 and 4, respectively.



435

436 **Fig. 16.** Acceleration time series of resonant vibrations at +37.1 m elevation. Red and blue  
 437 colors correspond to acceleration channels 3 and 4, respectively.

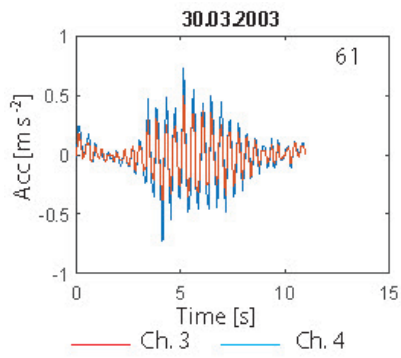


438

439 **Fig. 17.** Acceleration time series of resonant vibrations at +37.1 m elevation. Red and blue  
 440 colors correspond to acceleration channels 3 and 4, respectively.



441



442

443 **Fig. 18.** Acceleration time series of resonant vibrations at +37.1 m elevation. Red and blue  
444 colors correspond to acceleration channels 3 and 4, respectively.

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565 **List of figure captions**

566 Fig. 1. Illustration of the accelerometer and force panel locations and picture of the  
567 Norströmsgrund lighthouse.

568 Fig. 2. Schematic of the data processing flow.

569 Fig. 3. Response during a low-amplitude resonant vibration event (# 44 in Table 2).

570 Fig. 4. Seasonal overview of resonant vibration events: a) freezing degree days and days with  
571 resonant vibrations from 1979-2003 according to Li et al. (2016); b) number of events per  
572 month for different years.

573 Fig. 5. Acceleration (a), ice-drift velocity (b) and ice thickness (c) on April 5, 2001.

574 Fig. 6. Ice velocity versus duration of the events (a) and acceleration at the upper level versus  
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