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REAL-TIME PARAMETER ESTIMATION OF NONLINEAR VESSEL STEERING MODEL USING SUPPORT VECTOR MACHINE

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ABSTRACT

The Least-square support vector machine (LS-SVM) is used to estimate the dynamic parameters of a nonlinear marine vessel steering model in real-time. First, manoeuvring tests are carried out based on a scaled free-running ship model. The parameters are estimated using standard LS-SVM and compared with the theoretical solutions. Then, an online version, a sequential least square support vector machine, is derived and used to estimate the parameters of vessel steering in real-time. The results are compared with the values estimated by standard LS-SVM with batched training data. By comparison, sequential least square support vector machine can dynamically estimate the parameters successfully, and it can be used for designing a dynamic model-based controller of marine vessels.

NOMENCLATURE

M_R	Rigid-body mass matrix			
N_R	Damping matrix			
\boldsymbol{B}_R	Rudder parameter matrix			

$N_{_{\boldsymbol{v}}},N_{_{\boldsymbol{r}}},N_{_{\boldsymbol{\delta}}},N_{_{\dot{\boldsymbol{v}}}},N_{_{\dot{\boldsymbol{r}}}}$	Hydrodynamic coefficients of yaw motion
$Y_{v}, Y_{r}, Y_{\delta}, Y_{\dot{v}}, Y_{\dot{r}}$	Hydrodynamic coefficients of sway
	motion
v	Generalized velocity in body-fixed frame
δ	Rudder angle
r	Yaw rate
a	The coefficient of nonlinear term in
	Nomoto model
T_1, T_2, T_3	Nomoto constant
K_{δ}	Rudder constant
w	Weight matrix
$\boldsymbol{\varphi}(\cdot)$	Kernel function
C	Regularization factor
$\sum_{i=1}^N e_i^2$	Empirical error
b	Bias term
$\mathcal{L}(\mathbf{w},b,e_i,\alpha_i)$	Lagrange function
A_{N}	Input matrix
\boldsymbol{Y}_{N}	Output matrix
$oldsymbol{ heta}_N$	Parameter matrix

INTRODUCTION

Mathematical models of marine vehicles are playing a more important role in marine control with the development of numerical computation. Linear Nomoto model is widely used for heading control, but due to its over-simplified structure [1], Nomoto model with fixed parameters usually cannot provide an accurate prediction of heading response due to the environmental disturbances. A model with dynamic parameters is a good option and is now drawing more attention [2]. A steering model with dynamic parameters can provide more accurate response compared with the static model, and it is more capable of dealing with the dynamic environment disturbance due to waves, wind and current.

System identification has been used to improve and validate models with data from either free-model or full-scale tests [3]. Various techniques have been proposed for mathematical modelling of marine vessels. For example, in [4], a neural network was used to identify the nonlinear and coupled damping for an underwater vehicle. In [5], the nonlinear viscous damping forces in the horizontal plane of a surface vessel at low speed was estimated using the least square method. The least square method is very classic technique for system identification. It was used to estimate the hydrodynamic coefficients based on Planar Motion Mechanism (PMM) tests by Ross and Hassani et. al. [6,7]. But it usually will drop into local optimum and is largely affected by the noise of training data [8]. In [9, 10], the least square method was used to estimate the parameters of a nonlinear manoeuvring mathematical model, and a classic genetic algorithm, which is an intelligent algorithm for solving both constrained and unconstrained optimization problems [11], is used to search the global optimum of a cost function using free-running model test data. In [12], a regularized least-squares method was used to solve the hyper-parameter estimation problem with large data sets and ill-conditioned computations. Truncated singular value decomposition (TSVD) [13] is also a popular method to solve the ill-conditioned problem of least square method, and its application for parameters estimation of ship manoeuvring model is presented in [14].

Extended Kalman filter (EKF) is an optimal recursive estimator, so it can update the unknown variables in real-time when new measurements arrive. In [2, 15], the extended Kalman filter was used to estimate the dynamic parameters of a modified Nomoto model for vessel steering. Fossen *et al.* discussed an off-line parallel extended Kalman filter (EKF) algorithm utilizing two measurement series in parallel to estimate the parameters in the DP ship model [16]. In [17], the maximum likelihood method was used to determine ship steering dynamics.

Recently, support vector machine (SVM) was applied to estimate the hydrodynamic coefficients of ship model [18, 19].

SVM is a universal learning machine in the framework of structural risk minimization (SRM) [20]. In [21, 22], a modified version, Least Squares Support Vector Machines, was applied to model the controller of the marine surface vehicle for path following scenarios based on the manoeuvring tests. In order to estimate the parameters in real-time, an incremental update algorithm for training SVM online was proposed by Cauwenberghs et al. [23]. A nonlinear generalized predictive controller based on online LS-SVM was presented in [24]. Tang et al. [25] used an online sequential weighted LS-SVM to identify the structural parameters and their changes.

The main result of this paper is the implementation of online parameter estimations of nonlinear vessel steering model based on LS-SVM. Firstly, a nonlinear 2nd order Nomoto model for ship steering is briefly introduced and manoeuvring tests recommended by ITTC [26] have been carried out based on a scaled free-running ship model. The standard LS-SVM is introduced and used to estimate the parameters of vessel steering model using batched training data. The effectiveness of parameters estimation based on standard LS-SVM is demonstrated by comparison with the theoretical solution.

Then, a sequential LS-SVM is derived based on incremental updating algorithm. It is different from the online SVM using dynamic windows, which usually train the model using the truncated data. Sequential LS-SVM can estimate the parameters dynamically with the arrival of a new measurement. Parameters are updating in an incremental way, which avoids expensive inversion operation for training the model. Last, sequential LS-SVM is used to estimate the parameters of nonlinear Nomoto model with the free-running test data.

This paper is organized as follows: Section 2 is a brief introduction of the nonlinear model for ship steering. Section 3 offers a detail description of the principle of standard LS-SVM and sequential LS-SVM based on incremental updating algorithm. In section 4, Free-running model test is presented using a scaled ship model. In section 5, the validation of parameter estimation using standard LS-SVM is presented and sequential LS-SVM is used to estimate the parameters in real-time. The conclusions are presented in Section 6.

NONLINEAR MATHEMATICAL MODEL FOR SHIP STEERING

The Abkowitz model [27] is widely used to describe the ship dynamic motion. It is obtained using Newton's laws, and the hydrodynamic forces are approximated using Taylor expansions. In order to simplify the control problem, surge speed can be assumed as a constant value, so the surge force equation can be decoupled from the other two and plays no

further part in any linear treatment of ship steering. The linear expansions of *Y* and *N* can be expressed:

$$(m - Y_{v})\dot{v} + (mx_{G} - Y_{r})\dot{r} + mur = Y_{v}v + Y_{r}r + Y_{\delta}\delta$$

$$(mx_{G} - N_{v})\dot{v} + (I_{Z} - N_{r})\dot{r} + mx_{G}ur = N_{v}v + N_{r}r + N_{\delta}\delta$$
(1)

Rewrite the equation (1) in the state-space representation [28], which gives as:

$$\boldsymbol{M}_{R}\dot{\boldsymbol{v}} + \boldsymbol{N}_{R}(\boldsymbol{v})\boldsymbol{v} = \boldsymbol{B}_{R}\boldsymbol{\delta}_{R} \qquad (2)$$

where $\mathbf{v} = [\mathbf{v}, r]^T$ is the sway velocity and yaw rate in the body-fixed frame. The matrices $\mathbf{M}_R, \mathbf{N}_R(\mathbf{v})$ and \mathbf{B}_R are:

$$\boldsymbol{M}_{R} = \begin{bmatrix} m - Y_{v} & mx_{G} - Y_{r} \\ mx_{G} - N_{v} & I_{z} - N_{r} \end{bmatrix}$$

$$\boldsymbol{N}_{R}(u) = \begin{bmatrix} -Y_{v} & mu - Y_{r} \\ -N_{v} & mx_{G}u - N_{r} \end{bmatrix}$$

$$\boldsymbol{B}_{R} = \begin{bmatrix} Y_{\delta} \\ N_{\delta} \end{bmatrix}$$
(3)

The inertia matrix, M_R , is positive and reversible. The sate-space model, as described in Eq.3, can be rewritten as:

$$\dot{\mathbf{v}} = \underbrace{-\mathbf{M}_{R}^{-1} \mathbf{N}_{R}(\mathbf{u})}_{A} \mathbf{v} + \underbrace{\mathbf{M}_{R}^{-1} \mathbf{B}_{R}}_{B} \delta_{R}$$
 (4)

By eliminating the equation of sway motion in Eq.4, the resulted equation is the 2nd order linear yaw motion, which is well known as 2nd- Nomoto model [29].

$$T_1 T_2 \ddot{r} + (T_1 + T_2) \dot{r} + r = K_{\delta} (\delta_R + T_3 \dot{\delta}_R)$$
 (5)

The yaw rate equation is widely used to describe the course keeping behaviour of a ship and its Laplace Transform version is used in many ship control and autopilot studies [30]. The transfer function of 2nd-Nomoto model is given as:

$$\frac{r}{-\delta_R} = \frac{K_{\delta}(1 + T_3 s)}{(1 + T_1 s)(1 + T_2 s)} \tag{6}$$

The 2nd-order linear Nomoto model can be used for the course control but its accuracy for the prediction of the yaw rate is not adequate due to the over-simplified structure [1]. Therefore, the nonlinear Nomoto model can get by including the nonlinear term in Eq.5

$$T_1 T_2 \ddot{r} + (T_1 + T_2) \dot{r} + ar^3 + r = K_\delta (\delta_R + T_3 \dot{\delta}_R)$$
 (7)

where a is the coefficient of the nonlinear term. In Eq.6, the pole term $(1+T_2s)$ and the zero term $(1+T_3s)$ nearly cancel each other [17, 31, 32], because the difference between T_2 and T_3 is small, they are usually of the same order of magnitude. Therefore, the pole-zero cancellation can be implied to simplify this equation. The resulted equation is the well-known 1st-order Nomoto model.

$$T\dot{r} + r = K_{s}\delta_{p}$$
 (8)

NONLINEAR MATHEMATICAL MODEL FOR SHIP STEERING

In this section, the standard LS-SVM [33] will be introduced briefly and an extended version, the sequential LS-SVM based on incremental updating algorithm, is also derived. The sequential LS-SVM can update the estimated parameters in real-time when new data added to the training set.

Standard LS-SVM for parameter estimation

Firstly considering the training set, $S = \{s_i \mid s_i = (x_i, y_i), x_i \in \mathbb{R}^n, y_i \in \mathbb{R}^n\}_{i=1}^N$, where x_i is the input and y_i is the output. For regression purposes, Support Vector Regression (SVR) gives a general approximation function form:

$$\mathbf{v}(\mathbf{x}) = \mathbf{w}^T \mathbf{o}(\mathbf{x}) + b \tag{9}$$

where x is the training sample; y(x) is the target value; b is the bias term; w is a weight matrix; $\varphi(x)$ is kernel function, which is used to map the training sample to a higher dimensional feature space. For parameter estimation purpose using LS-SVM, the following optimization problem is formulated:

$$\min_{\mathbf{w}, b, e_i} f(w, e) = \frac{1}{2} \mathbf{w}^T \mathbf{w} + \frac{1}{2} C \sum_{i=1}^{N} e_i^2$$
s.t.
$$y_i = \mathbf{w}^T \boldsymbol{\varphi}(x_i) + b + e_i$$
(10)

where $e_i, i = 1 \cdots N$, is the error, and C is the regularization factor. As presented in Eq.10, the minimization of $\mathbf{w}^T \mathbf{w}$ is closely related to the use of a weight decay term in the training of neural networks, and the $\sum_{i=1}^N e_i^2$ is the empirical error. Therefore, the regularization factor, C balance the model accuracy and the model complexity, which also known as structural risk.

The corresponding Lagrange function is given by:

$$\mathcal{L}(\mathbf{w}, b, e_i, \alpha_i) = \frac{1}{2} \mathbf{w}^T \mathbf{w} + \frac{1}{2} C \sum_{i=1}^{N} e_i^2 - \sum_{i=1}^{N} \alpha_i [\mathbf{w}^T \boldsymbol{\varphi}(x_i) + b + e_i - y_i]$$
(11)

where α_i is the Lagrange multipliers. The optimality condition, Karush-Kuhn-Tucker conditions (KKT) [33], are defined by computing the derivative of Eq.11 with respect to w,b,e_i,α_i :

$$\frac{\partial \mathcal{L}}{\partial \mathbf{w}} = 0 \quad \rightarrow \quad \mathbf{w} = \sum_{i=1}^{N} \alpha_{i} \boldsymbol{\varphi}(x_{i})$$

$$\frac{\partial \mathcal{L}}{\partial b} = 0 \quad \rightarrow \quad \sum_{i=1}^{N} \alpha_{i} = 0$$

$$\frac{\partial \mathcal{L}}{\partial e_{i}} = 0 \quad \rightarrow \quad \alpha_{i} = Ce_{i}$$

$$\frac{\partial \mathcal{L}}{\partial \alpha_{i}} = 0 \quad \rightarrow \quad \mathbf{w}^{T} \boldsymbol{\varphi}(x_{i}) + b + e_{i} - y_{i} = 0$$
(12)

where $i = 1 \cdots N$. Eliminating variables w and e_i and rewriting Eq.12 in matrix representation.

$$\begin{bmatrix}
0 & \vec{1} \\
\vec{1} & K(\cdot) + C^{-1} \mathbf{I}
\end{bmatrix}
\begin{bmatrix}
b \\
\vec{\alpha}
\end{bmatrix} = \begin{bmatrix}
0 \\
\vec{Y}
\end{bmatrix}$$

$$\theta_{N} & Y_{N}$$
(13)

where I is an $N \times N$ identity matrix. $\vec{\alpha} = [\alpha_1, \cdots \alpha_N]^T$, $\vec{Y} = [y_1, \cdots, y_N]^T$. $K(x_k \cdot x_i) = \varphi(x_k)^T \varphi(x_i), i = 1 \cdots N$ is the kernel function that represents an inner product between its operands. It is positive definite and satisfies the Mercer condition [34, 35]. In this paper, the linear kernel function is used for parameter identification. LS-SVM model for function estimation yield:

$$y(x) = \sum_{i=1}^{N} \alpha_i K(x \cdot x_i) + b \qquad (14)$$

Sequential LS-SVM

Based on the above discussion, assume the LS-SVM has been trained using the first N pairs of data, and a new data pair (x_{N+1}, y_{N+1}) is observed. As presented in Eq.13, when a new data added to the train set, LS-SVM can be written as:

$$A_{N+1}\theta_{N+1} = Y_{N+1} \rightarrow \theta_{N+1} = A_{N+1}^{-1}Y_{N+1}$$
 (15)

where

$$\mathbf{A}_{N+1} = \begin{bmatrix} \mathbf{A}_{N} & \mathbf{b} \\ \mathbf{b}^{T} & c \end{bmatrix}$$
 (16)
$$\mathbf{b} = \begin{bmatrix} 1, K_{1,N+1}, K_{2,N+1}, \cdots, K_{N,N+1} \end{bmatrix}^{T}$$
 (17)
$$c = C^{-1} + K_{N+1,N+1}$$
 (18)

$$\boldsymbol{Y}_{N+1} = \begin{bmatrix} \boldsymbol{Y}_N \\ \boldsymbol{y}_{N+1} \end{bmatrix} \tag{19}$$

Now, in order to get the new parameters matrix, $\boldsymbol{\theta}_{N+1}$, the problem is how to find the solution of the matrix \boldsymbol{A}_{N+1} . In batched LS-SVM, matrix inversion is calculated directly. But for real-time parameter estimated, computing of the matrix inverse is impractical, because it is usually time-consuming and needs a lot of memory when handling large sets of data. In the following part, an incremental updating algorithm will be presented for calculation of the inverse of the matrix \boldsymbol{A}_{N+1} . Two lemmas need to be given first. As presented in [36]:

Lemma 1. The matrix A is invertible if A_{11} and A_{22} exist, and the inverse matrix, A^{-1} is given as:

$$\boldsymbol{A} = \begin{bmatrix} \boldsymbol{A}_{11} & \boldsymbol{A}_{12} \\ \boldsymbol{A}_{21} & \boldsymbol{A}_{22} \end{bmatrix}$$

$$\boldsymbol{A}^{-1} = \begin{bmatrix} \begin{bmatrix} \boldsymbol{A}_{11} - \boldsymbol{A}_{12} \boldsymbol{A}_{21}^{-1} \boldsymbol{A}_{21} \end{bmatrix}^{-1} & \boldsymbol{A}_{11}^{-1} \boldsymbol{A}_{12} \begin{bmatrix} \boldsymbol{A}_{21} \boldsymbol{A}_{12}^{-1} \boldsymbol{A}_{12}^{-1} - \boldsymbol{A}_{22} \end{bmatrix}^{-1} \\ \begin{bmatrix} \boldsymbol{A}_{21} \boldsymbol{A}_{11}^{-1} \boldsymbol{A}_{12} - \boldsymbol{A}_{22} \end{bmatrix}^{-1} \boldsymbol{A}_{21} \boldsymbol{A}_{11}^{-1} & \begin{bmatrix} \boldsymbol{A}_{22} - \boldsymbol{A}_{21}^{-1} \boldsymbol{A}_{11}^{-1} \boldsymbol{A}_{12} \end{bmatrix}^{-1} \end{bmatrix}$$

Lemma 2. The matrixs A, B, C, D, where A^{-1} , C^{-1} exist, then the following equation is true:

$$(A + BCD)^{-1} = A^{-1} - A^{-1}B(C^{-1} + DA^{-1}B)^{-1}DA^{-1}$$

According to the *Lemma 1* and *Lemma 2*, obviously, the inverse matrix of A_N and c exist. Therefore, the inverse matrix, A_{N+1}^{-1} is given:

$$\boldsymbol{A}_{N+1}^{-1} = \begin{bmatrix} \boldsymbol{A}_{N} & \boldsymbol{b} \\ \boldsymbol{b}^{T} & c \end{bmatrix}^{-1} = \begin{bmatrix} \begin{bmatrix} \boldsymbol{A}_{N} - \frac{1}{c}\boldsymbol{b}\boldsymbol{b}^{T} \end{bmatrix}^{-1} & \boldsymbol{A}_{N}^{-1}\boldsymbol{b} \begin{bmatrix} \boldsymbol{b}^{T}\boldsymbol{A}_{N}^{-1}\boldsymbol{b} - c \end{bmatrix}^{-1} \\ \begin{bmatrix} \boldsymbol{b}^{T}\boldsymbol{A}_{N}^{-1}\boldsymbol{b} - c \end{bmatrix}^{-1}\boldsymbol{b}\boldsymbol{A}_{N}^{-1} & \begin{bmatrix} c - \boldsymbol{b}^{T}\boldsymbol{A}_{N}^{-1}\boldsymbol{b} \end{bmatrix}^{-1} \end{bmatrix}$$

(20)

In which, the top left submatrix in Eq.20 can be rewritten as:

$$\left[\boldsymbol{A}_{N} - \frac{1}{c}\boldsymbol{b}\boldsymbol{b}^{T}\right]^{-1} = \boldsymbol{A}_{N}^{-1} + \boldsymbol{A}_{N}^{-1}\boldsymbol{b}\left[c - \boldsymbol{b}^{T}\boldsymbol{A}_{N}^{-1}\boldsymbol{b}\right]\boldsymbol{b}^{T}\boldsymbol{A}_{N}^{-1} \quad (21)$$

Assume, $\Delta = \left[c - \boldsymbol{b}^T \boldsymbol{A}_N^{-1} \boldsymbol{b}\right]^{-1}$, then Eq.20 can be rewritten in matrix expression:

$$\boldsymbol{A}_{N+1}^{-1} = \begin{bmatrix} \boldsymbol{A}_{N}^{-1} & \vec{0} \\ \vec{0} & 0 \end{bmatrix} + \Delta \begin{bmatrix} \boldsymbol{A}_{N}^{-1} \boldsymbol{b} \\ -1 \end{bmatrix} \begin{bmatrix} \boldsymbol{A}_{N}^{-1} \boldsymbol{b} & -1 \end{bmatrix}$$
 (22)

With Eq.22, the inverse matrix of A_N is computed in an incremental way, which avoids expensive inversion operation. The parameter matrix can be updated with the new data added to the training set. Therefore, the real-time parameters estimation can be implemented with Eq.22.

FREE-RUNNING MODEL TESTS

In this section, the results of manoeuvring tests onboard a self-running ship model are presented. The self-propelled vehicle is a scaled ship model of a chemical tanker, and the total length is 2.58 meters. On the ship, various sensors have been equipped. The tests were conducted in an open-door pool with moderate wind conditions.

Ship model dimensions and hardware structure

The self-propelled vehicle is presented in Fig.1. The model is constructed from single skin glass reinforced polyester, with plywood framing and its design speed is 0.98 m/s. Its main particularities are given in Table 1.



FIGURE 1: Scaled self-running ship model in the test.

TABLE 1: Main particularities of the ship model

CHEMICAL TANKER MODEL				
Length (m)	2.58			
Breadth (m)	0.43			
Draught (estimated at the tests) (m)	0.10			
Propeller diameter (m)	0.08			
Design speed (m/s)	0.98			
Scaling factor				

The self-running ship model is equipped with several sensors and actuators, i.e. 6-DOF fibre-optic gyrocompass, differential GPS, DC motor, industrial WI-FI communication, Compact-RIO embedded acquisition system, and batteries. All those equipment is controlled and synchronized using LABVIEW 2013 software, based on a real-time acquisition program. The hardware structure is presented as in Fig.2. The software architecture consists of several program loops: FPGA loop, real-time loop and TCP/IP loop [37,38].

Free-running model test results

Free-running model tests on the scaled model were conducted during the period of March 2016 to May 2016 at swimming pool of "Piscina Oceânica", Oeiras, Portugal. The weather was sunny and dry, but some wind was constantly present, changing its speed (approximately in the interval of 1–3 m/s) and direction as time passed. The pool is deep

enough to neglect any shallow-water effects. The pool has a maximum length of 50 m and an average breadth of 20 m.

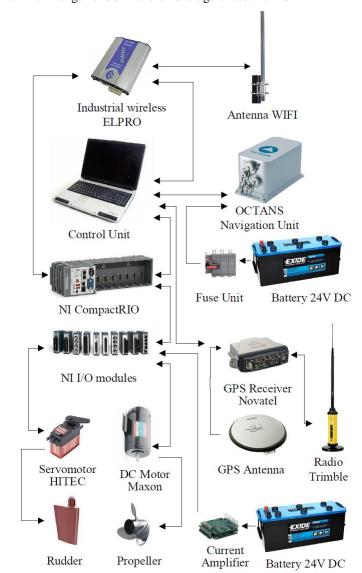


FIGURE 2: Onboard sensors and actuators.

The model was carefully launched in water and partly ballasted to get zero list and trim, although the design draught was not reached in these tests. Also, the model was not calibrated in the sense of reaching the scaled vertical position of the centre of gravity and scaled values of the moments of inertia. During all manoeuvres, the rpm was kept constant. The $20^{\circ}-20^{\circ}$ zigzag manoeuvring tests [26] have been carried out and the results are presented in Fig.3-4. Fig.3 shows that the collected data have a high quality and is suitable to carry out further manoeuvrability analysis of the scaled ship model. In Fig.4, the wind speed is about 2 m/s and the direction are changing rage from $80^{\circ}-100^{\circ}$.

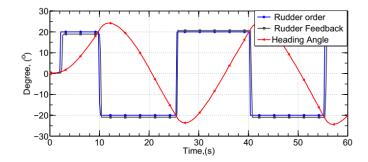


FIGURE 3: The $20^{\circ} - 20^{\circ}$ zigzag manoeuvring test using free-running ship model.

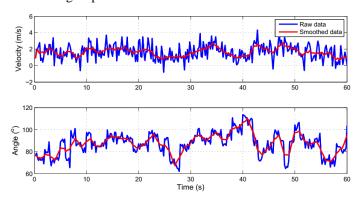


FIGURE 4: Wind conditions during the 20° - 20° zigzag manoeuvring tests.

REAL-TIME PARAMETERS ESTIMATION AND VALIDATION

In this section, the standard LS-SVM is used to estimate the parameters of the 1st-order Nomoto model using batched training data. The validation is presented by comparing the obtained parameters with theoretical solutions, which are calculated directly using $20^{\circ} - 20^{\circ}$ zigzag manoeuvring test. Then, the sequential LS-SVM is used to estimate the parameters of the nonlinear 2nd order Nomoto model in realtime, and the obtained parameters are compared with the results of standard LS-SVM.

Validation of standard LS-SVM

In order to validate the effectiveness of standard LS-SVM, the analysis method presented in Refs. [39, 40, 41] will be used to obtain the parameters. Integrate Eq.8 with respect to time t, gives as:

$$T \int_0^t \dot{r} dt + \int_0^t r dt = K_{\delta} \int_0^t \delta_R dt \qquad (23)$$

By choosing the range of time, the parameters and can be given by the following equation

$$K_{\delta} = -\frac{\psi_1 - \psi_2}{\int_{0}^{t_2} \delta_R dt}$$
 (24)

$$K_{\delta} = -\frac{\psi_{1} - \psi_{2}}{\int_{t_{1}}^{t_{2}} \delta_{R} dt}$$
 (24)
$$\frac{K_{\delta}}{T} = -\frac{r_{3} - r_{4}}{\int_{t_{3}}^{t_{4}} \delta_{R} dt}$$
 (25)

As shown in Fig.5, the shaded area gives the integral term at points delimited by the cross, where the yaw rate r is zero. According to the Eq.24 the parameter K_{δ} can be found, as $K_{\delta} = 0.2062$. Similarly, the Eq.25 is applied to the first two zero crossing points of the heading record as shown in the Fig.5. In this case, the heading equal to zero and T = 2.5221can be calculated from Eq.25. As presented in Table 2, the difference between estimated and theoretical values is small. Therefore, standard LS-SVM based on batched training data is an effective method and can provide accurate parameters. It will be used to estimate the parameters of nonlinear 2nd-order Nomoto model in the following part.

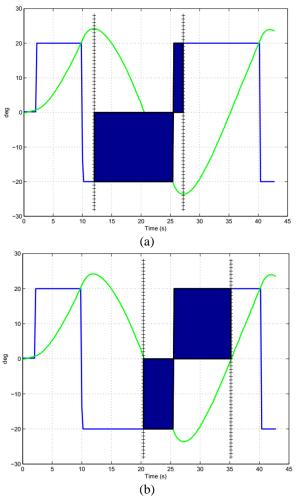


FIGURE 5: Calculation of K_{δ} (5a) and T (5b) using $20^{\circ} - 20^{\circ}$ zigzag manoeuvring test data.

TABLE 2: The values of the parameters of 1st-order Nomoto model

Method	T	Κδ
Theoretical values	2.5221	0.2062
LS-SVM	2.8540	0.2036

Real-Time parameter estimation using sequential LS-SVM

In this part, $20^{\circ} - 20^{\circ}$ and $30^{\circ} - 30^{\circ}$ zigzag manoeuvring tests are used as training data. Firstly, the stranded LS-SVM is used to estimate the parameters of nonlinear 2^{nd} order Nomoto model. In order to simulate the online situation, the sample in the training set will feed into the Sequential LS-SVM by time step. Therefore, the dynamic parameters can be obtained and updated with the feedback measurement at each time step. Before the simulation, the number of the initial training set (*N*) need to be defined. It is used to estimate the initial parameters. In this paper, the size of the initial training set is 10. The Sequential LS-SVM is described in the Algorithm (1).

Initialize: Set $C \leftarrow 10^4$; $N \leftarrow 10$; $K(x_k \cdot x_i) \leftarrow \varphi(x_k)^T \varphi(x_i)$ Result: θ_{N+1} If New measurement (x_{N+1}, y_{N+1}) Then | Compute the parameter \boldsymbol{b} , c; | Compute the inverse matrix A_{N+1}^{-1} ; | Update the parameter matrix θ_{N+1} ;

Algorithms 1: Sequential LS-SVM algorithm

else
Output the previous parameter θ_N

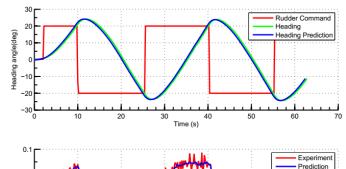
 $N \leftarrow N+1$:

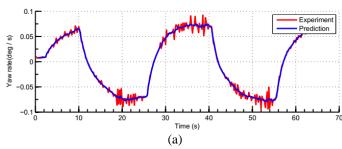
The standard LS-SVM is used to estimate the parameters of nonlinear Nomoto model using the batched 20° – 20° and $30^{\circ} - 30^{\circ}$ zigzag manoeuvring data. The obtained parameters are given in Table 3. The parameters K_{δ} has a bit drift from the theoretical value since the nonlinear model is selected. Usually, parameter T can be estimated using the empirical formula $(T=T_1+T_2-T_3=2.8011 \text{ and } 2.5049, \text{ respectively})$. It is close to the theoretical value. Then the obtained Nomoto model is used to predict the response of yaw and yaw rate during the $20^{\circ} - 20^{\circ}$ and $30^{\circ} - 30^{\circ}$ zigzag manoeuvring test. prediction and experimental results are presented in Fig.6, and they are in good agreement. The dynamic estimation of nonlinear parameters using sequential LS-SVM is presented in Fig.7. As shown in the figure 7a, the parameters are zero at the begin, because initial training set needs to be built first. Then the parameters converge to the values, which are estimated using standard LS-SVM. After 30 seconds, most the parameters converge the estimated values, it means that the sequence LS-

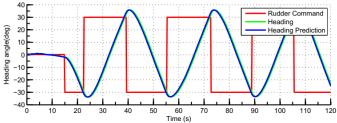
SVM can find the optimal values with limited samples, which is an advantageous feature compared with the least square method. The least squares method, theoretically, need an infinity training data to find the optimal values, but in most cases, the training data is limited. In Fig. 7b, the parameters, T_I and K_δ , converges to the estimated values after \$20\$ seconds. For both cases, the coefficient of the nonlinear term donot converge due to the change of the environmental disturbance.

TABLE 3: The parameters of Nonlinear 2nd order Nomoto Model using standard LS-SVM.

Data	T_1	T_2	<i>T</i> ₃	а	K_{δ}
20° - 20°	2.7879	0.1716	0.1585	-0.2807	0.2028
$30^{\circ} - 30^{\circ}$	2.2464	0.4667	0.2082	-0.4222	0.1647







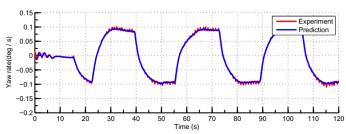


FIGURE 6: Prediction of $20^{\circ} - 20^{\circ}$ (6a) and $30^{\circ} - 30^{\circ}$ (6b) Zigzag manoeuvre using nonlinear 2nd order Nomoto model.

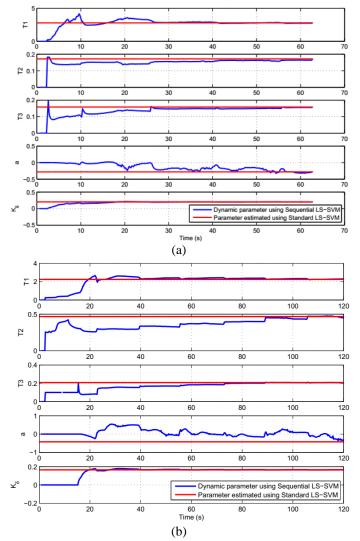


FIGURE 7: Real-time parameters estimation of nonlinear 2nd order Nomoto model using $20^{\circ} - 20^{\circ}$ (7a) and $30^{\circ} - 30^{\circ}$ (7b) Zigzag manoeuvre test data.

CONCLUSIONS

In this paper, a nonlinear mathematical model for ship steering was introduced. It is an extended version of 2nd order Nomoto model by including nonlinear terms. In order to estimate the parameters, a scaled ship model was built, and a control and measure system was programmed in platform using LABVIEW. Various manoeuvring test has been carried out in a swimming pool successfully. Then Standard LS-SVM is introduced briefly and used to estimate the parameters of the manoeuvring model. The obtained parameters agree well with the theoretical values, which validate its effectiveness.

In order to estimate the parameters dynamically, a sequential LS-SVM was derived based on an incremental

updating algorithm. Sequential LS-SVM can update the parameters dynamically when a new data feedback into the identification system. It is different from the well-established estimation method based on a dynamic window. For the estimation based on the dynamic window, it can estimate the parameters in real-time, but the model needs to be trained in each time step. For sequential LS-SVM, the parameters are updated in an incremental way, which avoids expensive training operation in each time-step. The parameters obtained by sequential LS-SVM are compared with the values estimated using standard LS-SVM and theoretical values. They are in very good agreement, and the parameters converge to the values with limited training data. Therefore, the proposed method can dynamically update the parameters and converge to the true values fast, and it can be used for designing a dynamic modelbased autopilot of marine vessels.

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