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Fatigue Strength Assessment of Steel Rollers: On the Reliability of the Strain Energy Density Approach on Real Components

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Abstract: Welded joints are one of the most widely applied methods to join different steel components. However, they introduce stress concentrators that are commonly known to reduce the fatigue strength of structures. Several methods have been developed to assess the fatigue behavior of welded components, such as the Notch Stress Intensity Factors (NSIFs) approach. However, this approach has been reported to be geometry dependent, and does not allow for a direct comparison of failures occurring at the weld toes with those occurring at the weld roots. This drawback has been overcame by considering the value of the strain energy density (SED) range averaged in a control volume ahead of the notch tip. More than 900 fatigue data of welded joints have been summarized within a single scatter band ΔW -N (strain energy range–umber of cycles to failure) using this approach. The reliability of the just mentioned scatter band in summarizing the fatigue data of real components such as steel welded rollers produced by Rulmeca is herein evaluated. The results prove the reliability of the SED approach to assess the fatigue behavior of welded rollers, paving the way to its diffusion in assessing real components.

Keywords: welded joints; fatigue strength; strain energy density; rollers; notch

1. Introduction

Welding procedures have allowed the simple realization of many complex structural connections in several different applications, such as bridges, cranes, offshore structures, and buildings [1]. Besides the optimization of the process parameters [2–4], researchers have focused on the fatigue behavior of welded components. All the aforementioned applications are in fact subjected to repetitive loading and hence the fatigue of welded structures has become one of the greatest matters of concern [5]. Welds represent local regions of higher stresses (i.e., stress concentrators) and fatigue failure is widely known to be sensitive to local peak stresses. Thus, over the years, several methods have been developed to assess the fatigue behavior of welds, and among these the Notch Stress Intensity Factor (NSIF) approach is worth mentioning [6–8]. In fact, since experimental observations have revealed that the most used welding procedures, such as arc and laser welding, are characterized by a very small weld toe radius, it is acceptable to model it as a sharp notch and the fatigue behavior can thus be correlated to the NSIFs [9,10]. Fatigue life can be divided into two different phases; i.e., nucleation and growth of cracks—and NSIFs were found to be able to predict either the initiation phase or the whole fatigue life [11–14]. This holds when the majority of the propagation phase has been spent within the region governed by the stress singularity. Several studies proved this behavior. Lassen demonstrated that in transverse, non-load-carrying joints manufactured via different welding procedures the nucleation of a 0.1 mm long crack required up to 40% of the whole fatigue life [15]. In addition, Singh et al. reported that in load-carrying AISI 304L fillet joints up to 70% of the fatigue life was spent propagating the original lack of a penetration crack of 0.5 mm [16,17]. However, the results are highly dependent of the on the stress distribution ahead of the point of singularity and, since time consuming FE analyses are required, this has limited the diffusion of the NSIFs approach in the assessment of real structures. Furthermore, the main limitation of this method consists in its geometry dependency. Its unit depends in fact on the notch opening angle according to Williams' formulations [18]. Different notch geometries are not thus comparable but ad-hoc material properties are required for each geometry. A breakthrough in the fatigue assessment of welded joints is represented by the strain energy density (SED) method, capable of overcoming all the limitations of the NSIFs approach [19]. The SED is evaluated averaging the range value of the strain energy in a cylindrical volume sector of radius R_c centered at the notch tip. According to this approach, fatigue failure occurs then this scalar quantity reaches its critical value ΔW_c . Both the radius R_c and the critical energy range ΔW_c . depend only on material properties [11] and shall be assumed to be independent of the load mode. Using this approach, Livieri and Lazzarin [20] summarized more than 600 experimental data obtained from different welded joints within a single narrow SED scatter-band. Failures occurred either at the weld root or at the weld toe. This work has then been extended by Berto and Lazzarin [21], including hollow section joints, and now more than 900 fatigue data are summarized in a single scatter band as depicted in Figure 1.

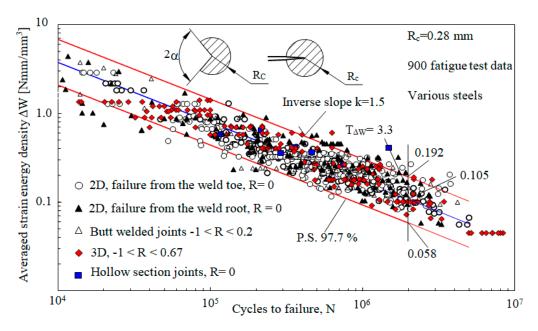


Figure 1. Fatigue behavior of welded joints as a function of the averaged local strain energy density range ΔW ; *R* is the nominal load ratio.

Moreover, the SED approach has been also reported to be a reliable tool in multi-axial fatigue assessment. Berto and Lazzarin [22] in fact resumed several experimental fatigue data obtained for structural steel within a single scatter band, drawn according to the following two assumptions: First, the critical value of strain energy density is considered to be independent from the type of loading in the high-cycle fatigue regime, and its value at 2×10^6 cycles has thus been imposed equal to that obtained for welded joints under uniaxial loading; a slope equal to 5/2 as suggested in Ref. [23] has been used. The approach has then been successfully applied to either the tensile or fatigue assessment of several notched materials, from metals [24–32] to polymers [33–35] and ceramics [36,37].

Recently, the SED approach was also preliminarily applied to the fatigue assessment of real components, such as rollers (Figure 2) produced by Rulmeca [38]. Besides surface pitting due to contact fatigue [39,40], rollers are in fact affected by fatigue failures at the weld root. The bearing housings

of the rollers are joint to the tube body by means of welding procedures. Although the connection between the bearing housings and the tube body is fundamental in preventing any imbalance in the roller, it is responsible to the fatigue failure of the rollers due to the lack of penetration at the weld root.

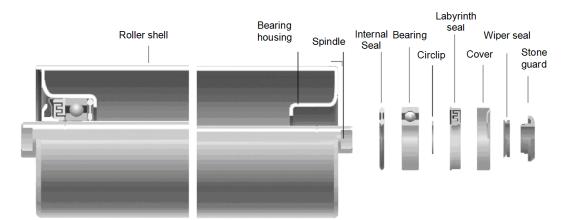


Figure 2. Typical roller assembly.

This work aims to further analyze the problem of fatigue failure at the weld root and to assess the reliability of the SED scatter band reported in Figure 1 in their assessment. Hence, firstly, new fatigue data sets have been obtained for three different roller types; i.e., PSV2, PSV4 and PSV5—and each roller type was characterized by different dimensions. Then, the new fatigue data together with those reported in Ref. [38] were analyzed in terms of SED, and they have been shown to be satisfactorily resumed by the scatter band obtained in Ref. [21]. This represents a breakthrough in the fatigue design of rollers, and in general of welded structures, since the SED scatter band reported in Figure 1 can be reliably used to predict the fatigue behavior of real components, whether they fail at the weld root or at the weld toe.

2. A Brief Description of the Strain Energy Density Approach

Considering the SED criterion [19] statements for dynamic loadings, fatigue failure occurs when the strain energy range $\Delta \overline{W}$ averaged in a control volume of radius R_c ahead of the crack tip reaches its critical value ΔW_c . Simple analytical formulations have been obtained in Ref. [19] for the assessment of the critical value of the strain energy density range ΔW_c (Equation (1)) and of the critical radius R_c (Equation (2)):

$$\Delta W_C = \frac{\Delta \sigma_A^2}{2E} \tag{1}$$

$$R_C = \left(\frac{\sqrt{2e_1}\Delta K_{1A}}{\Delta\sigma_A}\right)^{\frac{1}{1-\lambda_1}} \tag{2}$$

where $\Delta \sigma_A$ is the fatigue limit of the material without geometric singularities, *E* is the Young's modulus of the material, λ_1 is Williams' eigenvalue for mode 1 [18], ΔK_{1A}^N is the amplitude of the Notch Stress Intensity Factors (NSIF) fatigue threshold, and e_1 is a parameter dependent either on geometrical parameters (the notch opening angle 2α) or on material properties (the Poisson's ratio ν). The reader should refer to Ref. [19] for e_1 formulation. Dealing with rollers, the control volume is a circle centered at the weld root tip (blue circle in Figure 3), and its radius, as well as the critical strain energy density range value, is only dependent on the material [11].

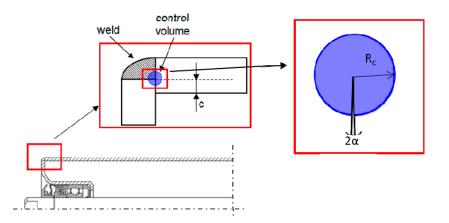


Figure 3. Schematic representation of the weld root, characterized by a weld root length "*c*", and the control volume of the strain energy density (SED) approach (blue circle).

The value of the critical radius has been obtained by leveraging on previously published data either for failures at the weld root or at the weld toe. Concerning the former, considering the value of 211 MPa mm^{0.326} for the amplitude of the Notch Stress Intensity Factors ΔK_{1A}^N obtained by Livieri and Lazzarin [41] for the transverse non-load carrying fillet welded joints, and that of 153 MPa for the fatigue strength $\Delta \sigma_A$ of butt ground welds obtained by Taylor at al. [42], the critical value R_c for steel welded joints corresponds to 0.28 mm. Dealing with the case of failure to occur at the weld root, instead, considering $\Delta K_{1A}^N = 180$ MPa mm^{0.5}, Equation (2) gives a critical value of the radius equal to 0.36 mm. However, being on the safe side, an R_c value of 0.28 mm has been used in this work also for failures occurring at the weld roots.

3. Geometry

In this report rollers belonging to the series PSV were studied. Representing the state of the art of Rulmeca's production [34], these rollers are widely required for conveyors in applications characterized by high working load and by the need to convey large lump size materials. The main components of the roller are reported in Figure 2 and their functions are widely described in Ref. [38]. Among them, the feature investigated in this work is the joint between the roller shell (tube) and the bearing housing, where the failure occurs. Joining these two features optimizes the roller performance, avoiding any imbalance in the rollers and allowing their use at the highest speeds. However, although weldment is of utmost importance for a proper roller operation, it represents the weakest point of the structure considering fatigue behavior, since the lack of penetration at the weld root (Figure 4) leads to the final failure of the roller (Figure 4b,c).



Figure 4. Cont.



Figure 4. Lack of penetration at the weld root (**a**), a detail of the crack through the welded zone (**b**) and typical roller failure (**c**).

The length of the lack of penetration, indicated as *c* in Figure 3, has been determined carrying out micrographic analyses on the welded rollers, resulting in a value of *c* in the range between 0.6 and 1.0 mm. As reported in Ref. [38], the SED value is slightly affected by a variation of c in this range, and thus the length c = 1 mm is set in all the analyses.

The rollers tested in this work belong to three different types of rollers; i.e., PSV2, PSV4 and PSV5. The geometrical parameters are listed in Table 1 in addition to the rollers tested in Ref. [38]; i.e., PSV4 133 315 and PSV4 159 530. See Figure 5 for an explanation of the meaning of the geometrical details.

Table 1. Geometrical parameters of the rollers considered in the present investigation and in Ref. [38] (*).

Model Name	Length of the Roller [mm]	Diameter of the Roller [mm]	Tube Thickness [mm]	Bearing Type
PSV2 133 315	315	133	4	6205
PSV2 133 600	600	133	4	6205
PSV2 159 380	380	159	4.5	6205
PSV2 159 600	600	159	4.5	6205
PSV4 133 315 *	315	133	4	6206
PSV4 159 530 *	530	159	4.5	6206
PSV5 133 315	315	133	4	6306
PSV5 159 530	530	159	4.5	6306

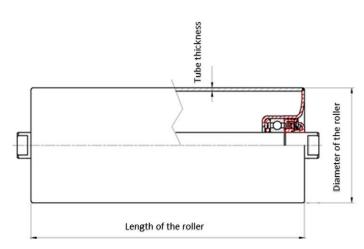


Figure 5. Geometry of the rollers.

4. Results

Seven different roller geometries have been tested under fatigue; i.e., PSV2 133 315, PSV2, PSV2 133 600, PSV2 159 380, PSV2 159 600, PSV4 159 530, PSV5 133 315, PSV5 159 530. The test system mimicking the in-service conditions of the rollers was developed by the authors. An external counter-roll presses the tested roller, which rotates with a constant speed, with a constant pressure, applying the load. Further details about the test system can be found in Ref. [38]. The fatigue results for each geometry are reported in Tables 2–8. In Table 6 the fatigue results obtained in Ref. [38] are also reported. In addition, in Table 9 the experimental data obtained in Ref. [38] for PSV4 133 315 are resumed.

Samples		Load [Kg]	RPM	Cycles	SED [MJ/mm ³]
PSV2 133 315	1	541	545	2,151,388	0.101
	2	512	545	1,343,313	0.091
	3	466	545	5,328,121	0.075
	4	457	545	2,440,852	0.072
	5	451	545	11,468,429	0.071
	6	420	545	10,198,955	0.061
	7	380	591	8,620,179	0.050

Table 2. Fatigue data for the roller PSV2 133 315.

Table 3	. Fatigue	data	for the	roller	PSV2	133 60	0.
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Samples		Load [Kg]	RPM	Cycles	SED [MJ/mm ³]
PSV2 133 600	1	545	653	6,478,432	0.091
	2	531	653	6,373,931	0.086
	3	522	648	10,132,740	0.083
	4	484	641	10,699,396	0.072
	5	461	641	10,722,269	0.065
	6	395	493	10,075,994	0.048

Table 4. Fatigue data for the roller PSV2 159 380.

Samples		Load [Kg]	RPM	Cycles	SED [MJ/mm ³]
PSV2 159 380	1	1231	534	259,463	0.517
	2	899	534	416,956	0.276
	3	856	534	695,104	0.250
	4	814	534	534,408	0.226
	5	745	534	557,365	0.189
	6	540	534	1,556,243	0.099
	7	448	534	10,752,532	0.068
	8	431	534	5,451,923	0.063
	9	397	534	7,611,444	0.054
	10	344	534	5,958,036	0.040
	11	298	534	10,612,449	0.030
	12	238	534	14,382,785	0.019

Samples		Load [Kg]	RPM	Cycles	SED [MJ/mm ³]
PSV2 159 600	1	561	534	2,119,258	0.101
	2	527	534	3,983,769	0.089
	3	502	534	2,452,618	0.081
	4	471	534	2,809,780	0.071
	5	424	534	10,434,390	0.058
	6	402	534	10,224,224	0.052
	7	373	534	11,459,075	0.045
	8	351	534	14,488,277	0.039
	9	324	534	10,663,603	0.034
	10	302	544	12,563,405	0.029
	11	283	544	10,665,627	0.026
	12	254	544	10,159,436	0.021

Table 5. Fatigue data for the roller PSV2 159 600.

Table 6. Fatigue data for the roller PSV4 159 530.

Samples		Load [Kg]	RPM	Cycles	SED [MJ/mm ³]
PSV4 159 530	1*	1262	541	363,234	0.278
	2 *	1251	541	370,432	0.274
	3 *	994	541	677,279	0.173
	4 *	992	541	747,548	0.172
	5 *	991	541	598 <i>,</i> 390	0.172
	6 *	990	541	619,344	0.171
	7	768	545	6,140,003	0.103
	8	715	545	3,352,651	0.089
	9*	708	545	2,749,333	0.088
	10	681	545	15,139,928	0.081
	11	621	545	5,433,742	0.067
	12	585	545	10,065,572	0.060
	13	536	545	10,791,789	0.050
	14 *	523	545	9,962,179	0.048
	15	480	545	10,690,499	0.040
	16	456	545	11,909,310	0.036
	17	428	545	11,221,894	0.032
	18	401	545	15,489,417	0.028
	19	388	545	11,608,328	0.026
	20	340	545	10,967,692	0.020

Data characterized by * were already presented in Ref. [38].

The fatigue data reported in Tables 2–9 have been analyzed in terms of the SED range by means of FE analyses (details on FE models can be found in Ref. [38]). The results have been compared with the scatter band presented in Ref. [21]. It is worth mentioning that the just mentioned scatter band has been obtained by mostly considering welded joints that fail at the weld toes (Figure 6). It can be seen that the scatter band previously obtained allows reliable predictions of fatigue strength of different roller geometries that fail at the weld root. Therefore, the aforementioned scatter band has revealed to be a reliable tool for the assessment of the fatigue failure of the welded joints regardless of the location of the failure.

	Load [Kg]	RPM	Cycles	SED [MJ/mm ³]
1	1251	643	306,221	0.230
2	1245	643	605,933	0.228
3	1200	643	1,399,867	0.212
4	815	638	910,164	0.098
5	807	638	231,3360	0.096
6	795	638	2,089,012	0.093
7	776	638	4,078,198	0.089
8	752	638	10,913,677	0.083
9	713	638	5,059,160	0.075
10	695	638	12,802,353	0.071
11	678	638	3,863,892	0.068
12	657	643	14,832,967	0.064
13	593	641	4,625,783	0.052
14	556	641	12,891,317	0.045
15	508	641	11,974,027	0.038
	2 3 4 5 6 7 8 9 10 11 12 13 14	$\begin{array}{c ccccc} 1 & 1251 \\ 2 & 1245 \\ 3 & 1200 \\ 4 & 815 \\ 5 & 807 \\ 6 & 795 \\ 7 & 776 \\ 8 & 752 \\ 9 & 713 \\ 10 & 695 \\ 11 & 678 \\ 12 & 657 \\ 13 & 593 \\ 14 & 556 \end{array}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	1 1251 643 306,221 2 1245 643 605,933 3 1200 643 1,399,867 4 815 638 910,164 5 807 638 231,3360 6 795 638 2,089,012 7 776 638 4,078,198 8 752 638 10,913,677 9 713 638 5,059,160 10 695 638 12,802,353 11 678 638 3,863,892 12 657 643 14,832,967 13 593 641 4,625,783 14 556 641 12,891,317

Table 7. Fatigue data for the roller PSV5 133 315.

Table 8. Fatigue data for the roller PSV5 159 530.

Samples		Load [Kg]	RPM	Cycles	SED [MJ/mm ³]
PSV5 159 530	1	919	543	1,500,112	0.124
	2	883	543	1,368,180	0.114
	3	832	543	2,351,632	0.101
	4	782	543	3,250,568	0.090
	5	736	543	3,463,929	0.079
	6	727	543	3,203,478	0.077
	7	710	543	4,187,825	0.074
	8	698	543	3,082,748	0.071
	9	660	543	3,361,271	0.064
	10	659	543	3,086,549	0.064
	11	628	543	2,994,251	0.058
	12	615	543	10,945,983	0.055

 Table 9. Fatigue data for the roller PSV4 133 315 from [38].

Samples		Load [Kg]	RPM	Cycles	SED [MJ/mm ³]
PSV4 133 315	1	1700	617	110,000	0.442
	2	1675	617	155,500	0.429
	3	1245	643	1,680,000	0.237
	4	1245	643	521,658	0.237
	5	813	638	3,687,621	0.101
	6	786	638	13,484,745	0.094
	7	760	638	10,728,361	0.088
	8	752	638	10,685,583	0.086
	9	713	638	1,044,041	0.078
	10	647	638	10,164,948	0.064
	11	610	638	11,055,235	0.057
	12	553	646	10,479,312	0.047
	13	510	646	10,615,367	0.040
	14	404	646	11,446,934	0.025

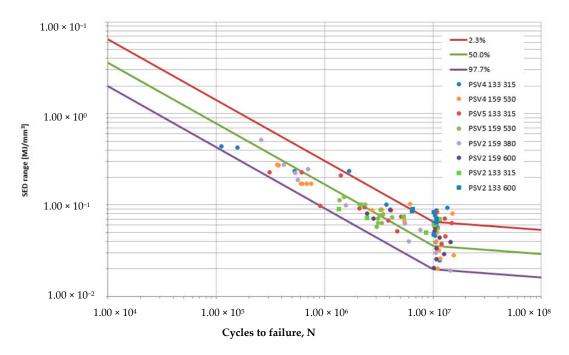


Figure 6. Synthesis of fatigue data for different roller geometries in terms of local SED and a comparison with the scatter band shown in Figure 1.

5. Conclusions

The SED approach has been herein used to assess the fatigue behavior of different types of PSV rollers, representing the state of the art of Rulmeca's production. These rollers are subjected to fatigue failures because of a lack of penetration of the weld root connecting the bearing housings to the tube body. Fatigue tests on seven different roller geometries have been carried out and the results have been analyzed in terms of SED. Together with the data obtained in Ref. [38], they have been reported to fall within the scatter band Δ W-N (strain energy range–number of cycles to failure) obtained in Ref. [21] that summarizes about 900 fatigue data obtained from welded joints characterized by different main plate thicknesses, different transverse plates, and different bead flanks. Although this scatter band was obtained with the majority of the failures occurring at the weld toes, it provides reliable predictions of the fatigue behavior of welded joints with failures from the notch root; i.e., the considered roller geometries.

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