

Testing and modelling of flow-drill screw connections under quasi-static loadings

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Abstract

The behaviour of a flow-drill screw connection under different quasi-static loadings was simulated using finite element models with detailed solid element meshes. The numerical models were developed with a rate-independent isotropic hypoelastic-plastic material model. A process-effect analysis was conducted, including investigation of the microstructure as well as hardness tests. Based on the investigation, the process effects were considered negligible. A simple approach for building up the geometry of the connection was presented. An experimental programme consisting of five different single-connector tests was carried out to characterise the connection, and was presented in detail. Each test was simulated, allowing for one-to-one comparisons between tests and simulations. Satisfactory results were achieved.

Keywords: Flow-drill screw, Connection, Finite element, Experiments, Automotive

1. Introduction

Flow-drill screws (FDS) are commonly used to join parts of dissimilar materials in the load-bearing structure of cars. Since connections play important roles for the crashworthiness of vehicles, knowledge about their physical behaviour under impact loadings is important for design decisions. Necessary knowledge and physical insight is usually gained through extensive experimental programmes, which typically involve loading specimens consisting of two or more plates joined with one or more connectors until failure (Sønstabø et al., 2015). Various loadings are achieved by changing the specimen design and loading directions.

A limited number of experimental studies on FDS connections can be found in the open literature. Szlosarek et al. (2013) presented a novel testing and analysis method. It was demonstrated for an FDS connection between plates of a carbon fibre reinforced polymer and aluminium. Skovron et al. (2014) studied the FDS process for a connection between sheets of aluminium alloy AA 5052-O. They explored feasible design space regions to determine how process parameters affect the geometry of the assembled connection. Mechanical tests were

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13 performed to validate the findings. Sønstabø et al. (2015) carried out a large experimental programme to
14 characterize an FDS connection between sheets of AA 6016 T4. The results were compared to equivalent tests on
15 self-piercing rivet connections. Skovron et al. (2015) studied the effect of thermally assisting the FDS process (i.e.
16 pre-heating the plates with an external heat source), and performed mechanical tests on a connection between
17 sheets of AA 6063 T5A. Sønstabø et al. (2016) presented experiments on connections between an AA 6016 T4
18 sheet and an AA 6063 T6 extrusion, which they used to evaluate state-of-the-art macroscopic large-scale finite
19 element modelling techniques. A *macroscopic model* here means a simplified model used to represent connections
20 in large-scale analyses where time step restrictions prohibit detailed modelling of the connections. On the other
21 hand, a *mesoscopic model* is a detailed three-dimensional finite element model with a fine solid mesh, where the
22 actual geometry of the connection is taken into account.

23 To the best of the authors' knowledge limited scientific literature exist on mesoscopic modelling of FDS
24 connections. A literature survey revealed one paper by Grujicic et al. (2016), who made an attempt to simulate the
25 FDS process. The results from the process simulation were mapped to finite element models of different coupon
26 tests. The global force-displacement curves from the coupon simulation results were qualitatively compared to
27 corresponding curves from the experiments of Sønstabø and Holmstrøm (2013) which have been presented in
28 the journal article of Sønstabø et al. (2015). These experiments were with a different screw and different plate
29 materials.

30 In addition to complement experiments with additional information not otherwise achievable, a validated
31 mesoscopic model of the connection may be used to explore the design space as function of e.g. thicknesses,
32 materials and screw geometries in an efficient way, or for example to investigate particular deformation or
33 failure modes. Another incentive for building a validated mesoscopic model is to use it for virtual testing of
34 the connections. Experiments are costly and time consuming, and from an industrial perspective it would be
35 beneficial to replace experiments with validated simulations. The results can for instance be used to calibrate
36 macroscopic connection models for large-scale simulations.

37 Although little information is available for FDS connections, detailed numerical studies using mesoscopic
38 models have been carried out on other connection types, some examples of which are presented in the following.
39 Bouchard et al. (2008) used three-dimensional numerical models to study the behaviour of self-piercing rivet
40 (SPR) connections under quasi-static loading conditions. They included mechanical properties obtained with
41 two-dimensional axisymmetric riveting process simulations, and were in most cases able to reproduce the correct
42 behaviour of the connection with reasonable accuracy in terms of force-displacement response and deformation
43 mode. Chen et al. (2014) conducted a numerical and experimental study of a riveted joint, including the riveting
44 process and tension tests, to investigate the failure modes under tensile loads. Kong et al. (2008) predicted
45 the plastic and failure behaviour of a single lap-joint test of a resistance spot-weld between two steel sheets.
46 Constitutive models were calibrated for different weld zones and coupled with a failure model. The finite element
47 model was used to study the effect of nugget size and sheet thickness. A similar study was carried out by Nielsen

48 (2008), who used a modified Gurson material model to successively model plug failure for sufficiently large
49 spot-weld diameter. Interface failure typically seen for smaller weld diameters was not well described. This was
50 achieved later by Nielsen and Tvergaard (2010) by modifying an extension to the Gurson model. Sabuwala et al.
51 (2005) used finite element analysis to study the behaviour of fully restrained steel connections subjected to blast
52 loads. The results revealed that design criteria for steel connections subjected to blast loads were inadequate, and
53 recommendations for modifications were presented. Liu et al. (2015) performed experimental tests to investigate
54 the dynamic response of top-and-seat with web angle steel beam-column connections subjected to a sudden
55 column removal. They employed three-dimensional finite element simulations to understand the deformation
56 and failure mechanisms that were observed in the experimental tests.

57 Numerical simulations of the FDS process are difficult to set up. The process physics are complex, involving for
58 instance friction, large plastic deformations and thermal softening. A coupled thermo-mechanical finite element
59 model would be required, and accurate description of the different phenomena would be difficult. Moreover, the
60 large deformations would cause numerical challenges, introducing the need for e.g. remeshing. In addition, one
61 would need data of the process input parameters, e.g. rotational speed, torque and driving force. Besides, such
62 a process simulation would be difficult to validate.

63 The present article explores the possibilities of modelling FDS connections between aluminium plates with a
64 mesoscopic model, without taking the process into account. The developed numerical model was validated using
65 experiments, both with respect to deformation modes and force-deformation characteristics. A simple approach
66 for building up a sufficiently accurate model is presented. Five different finite element models were built up, each
67 one resembling an experimental test, allowing for direct comparisons between simulations and experiments. The
68 experimental programme consisted of cross tension, cross mixed, cross shear, single lap-joint and peeling tests.
69 The novelty of this paper is related to the mesoscopic modelling of FDS connections, as well as the validation
70 carried out using a new cross test set-up.

71 The experiments are explained and presented first, followed by a discussion about process effects. The finite
72 element model is subsequently presented, and finally the simulation results are discussed.

73 2. Experiments

74 The term *connection* is in the present article defined as *a system that mechanically fastens two or more parts*
75 *together* (Sønstabø et al., 2015, 2016), implying that it consists of the screw itself plus some surrounding plate
76 materials. The connection investigated in this work consisted of an M5 through-hardened steel screw connecting
77 a 2 mm thick rolled sheet of AA 6016 in temper T4 to a 2 mm thick extrusion of AA 6063 in temper T6. A
78 schematic drawing with nominal dimensions and a cross-section picture of the connection are presented in Fig. 1.
79 This material combination was chosen since it is representative of a typical FDS connection in cars, with the top
80 sheet having a yield stress of approximately 120 MPa and the bottom extrusion a yield stress of approximately

210 MPa. A pre-hole of 7 mm diameter was used in the top plate. Engineering stress-strain curves for the plate and screw materials are presented in Fig. 2. As seen, the extrusion (6063) had a higher yield stress, but the rolled sheet (6016) had stronger work-hardening and was significantly more ductile.

The connection was studied by means of cross tests in three loading directions (tension, shear, and combined tension and shear), and single lap-joint and peeling tests. Schematic drawings of the test specimens are presented in Fig. 3, where clamped areas are indicated with grey colour. The dark grey colour in Fig. 3a indicates where a smaller clamp was used in the cross mixed and shear tests. All tests were quasi-static. Three to five repetitions were carried out for each test. The global responses (force-displacement curves) are reported, together with detailed descriptions of the tests and post-mortem pictures of specimens. The global response in the single lap-joint and peeling tests has been briefly reported before (Sønstabø et al., 2016).

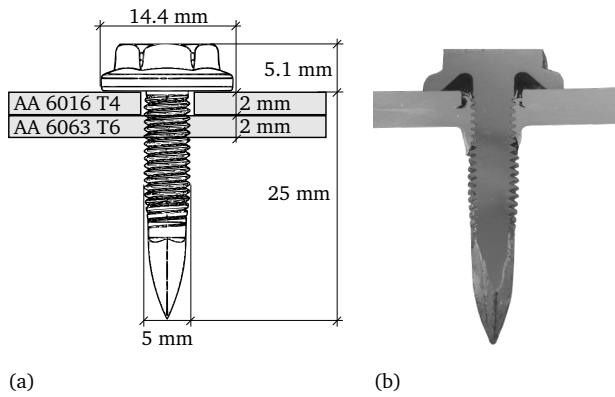


Fig. 1. FDS connection. (a) Schematic drawing. (b) Picture of the cross-section.

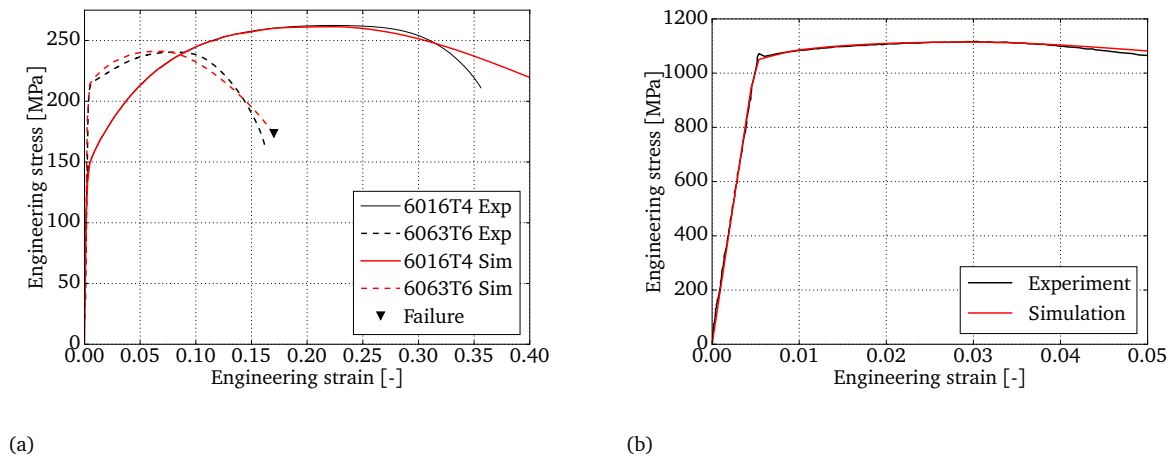


Fig. 2. Engineering stress-strain curves for the (a) plate materials and (b) screw material. Curves from simulations of the material tests are included (see Section 4.2).

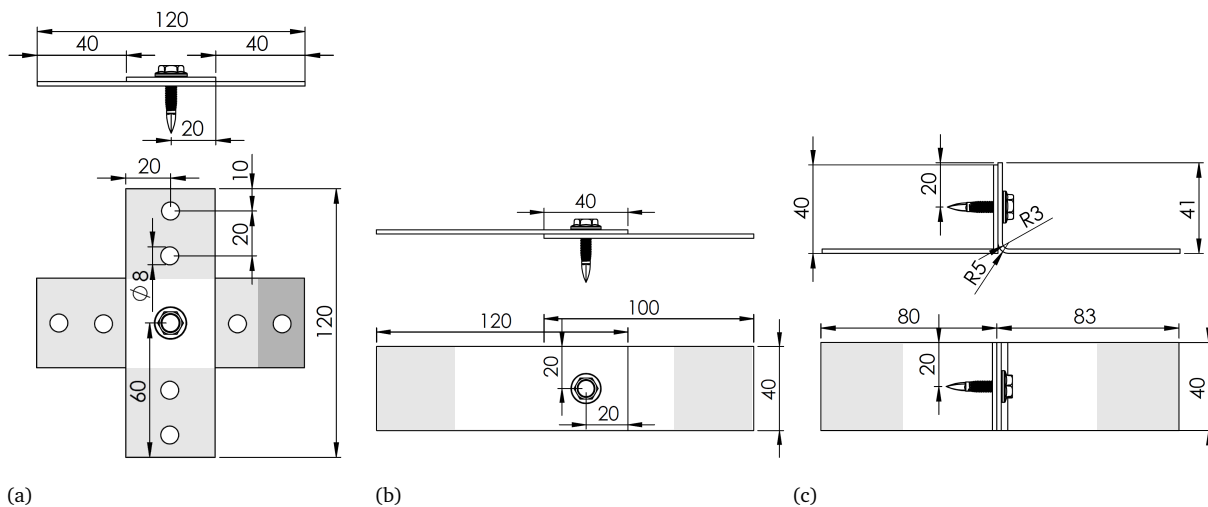


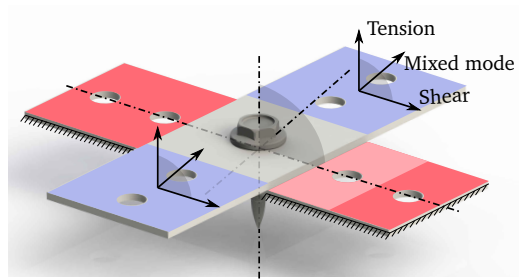
Fig. 3. Drawings of test specimens. (a) Cross test. (b) Single lap-joint test. (c) Peeling test. Clamped areas are coloured grey. The dark grey colour in (a) indicates the area where a smaller clamp was used in the cross mixed and cross shear tests.

91 2.1. Cross tests

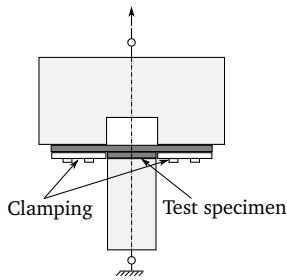
92 Fig. 4a illustrates the principle of the cross tests. The coloured areas in the figure were clamped in the tests.
 93 The red parts were fixed, while the blue parts were pulled in the directions of the arrows corresponding to tension-
 94 , mixed- and shear loading. To allow for relative sliding of the plates, only half of the area on one side of the
 95 bottom plate was clamped in the cross mixed and shear tests. This is indicated with a lighter red colour where
 96 the clamping was omitted. The bottom plate was fixed, while the top plate was pulled in the direction of the
 97 arrows in the figure.

98 Fig. 4b shows a principle drawing of the cross tension test set-up. The specimen was mounted on two steel
 99 fixtures, using screws and clamping blocks. A picture of the set-up is shown in Fig. 4c. The steel fixtures
 100 were placed in a regular Instron tensile testing machine, where they were pulled apart in the vertical direction.
 101 Pure tensile loading was ensured by hinging the fixture in each end. The pulling force was measured with a
 102 load cell mounted in series between the top fixture and the cross beam of the testing machine. A camera was
 103 used to take photographs during the tests to record the relative displacement of the steel fixtures with a digital
 104 image correlation (DIC) method (readers are referred to Fagerholt (2012) for details on DIC). Black and white
 105 checkerboard markers were glued on the steel fixtures, for the DIC analysis.

106 The shear and mixed mode cross tests were carried out using the rig shown in Figs. 4d to 4f. The test rig was
 107 designed so that it was easy to control the support conditions, such that a one-to-one relationship with numerical
 108 boundary conditions could be obtained. Principle drawings of the set-up are shown in Figs. 4d and 4e, and Fig. 4f
 109 shows a picture of the mixed-mode set-up. The cross specimen was clamped to two main steel parts (denoted
 110 as part 1 and part 2 in Fig. 4) with screws and clamping blocks. The main steel parts were placed inside a
 111 cylindrical steel casing, to control their motion, thus ensuring controlled boundary conditions in the test. Part 1



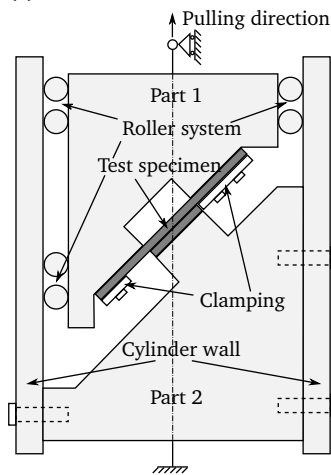
(a)



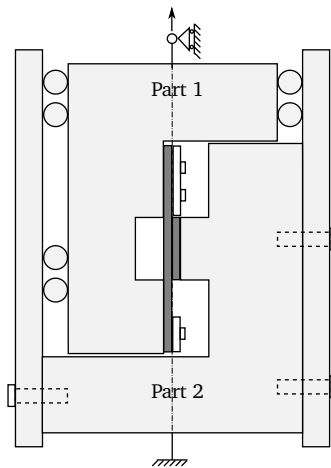
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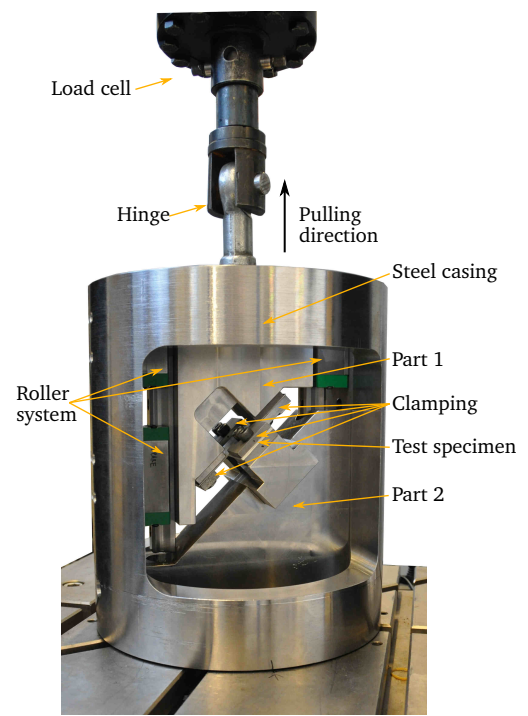
(c)



(d)



(e)



(f)

Fig. 4. Illustrations of the set-ups in the cross tests. (a) Principle of the cross tests. (b) Principle drawing of the tension set-up. (c) Picture of the tension set-up. (d) Principle drawing of the mixed-mode set-up. (e) Principle drawing of the shear set-up. (f) Picture of the mixed mode set-up.

112 was attached to the cylinder with a roller system, allowing for smooth motion in the loading direction, whereas
 113 part 2 was bolted to the casing.

114 The rig was placed in a regular Instron tensile testing machine. The rig was hinged in the top, and attached
 115 to the testing machine with a single bolt between the centre of the bottom of part 2 and the testing machine.
 116 A load cell was mounted between the top hinge and the cross-beam of the testing machine. It was confirmed
 117 by in-house testing that the friction forces in the rollers were negligible compared to the pulling force, and thus

118 that the force measured was equal to the force transmitted through the specimen. The clamping was carefully
 119 monitored to verify that no slipping occurred. A camera was used to take photographs during the tests. The
 120 pictures were used to monitor the rigid-body motion of parts 1 and 2 using DIC. Black and white checkerboard
 121 markers were glued on parts 1 and 2, for the DIC analysis. It was verified that the rotation and translation in
 122 other directions than the pulling direction were negligible. The cross-head velocity in all cross tests was set to 5
 123 mm/min, which was assumed to render quasi-static conditions.

124 All three cross test set-ups were designed such that the load application line passed exactly through the centre
 125 of the specimen (as indicated with stippled-dotted lines in Figs. 4a, 4b, 4d and 4e).

126 Force-displacement curves from the cross tests are shown in Fig. 5 and deformed specimens are depicted
 127 in Figs. 6a to 6d. The displacement plotted here is the relative displacement between parts 1 and 2 which
 128 was measured with DIC. As seen, the connection was strongest in shear and weakest in tension. The shear
 129 mode exhibited highest ductility while the tensile mode exhibited lowest. The mixed mode response showed
 130 intermediate force level and ductility. Large variation in initial stiffness was seen for the mixed mode and shear
 131 tests. This was due to the pre-hole which allowed for relative sliding between the top and bottom plate under
 132 shear loading. The force required to give sliding varied from specimen to specimen, which might be due to
 133 variations in the screw-driving process (e.g. pre-stressing, surface finish, cleanliness). Apart from this variation
 134 the repeatability of the test results was acceptable.

135 In tension significant plate yielding caused a distinct knee in the force-displacement curve after approximately
 136 1 mm displacement. The force increased until approximately 3.2 kN where the threads were stripped from the

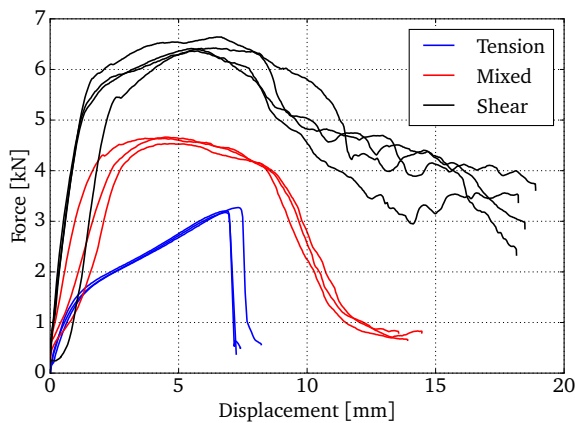


Fig. 5. Force-displacement curves from cross tests.

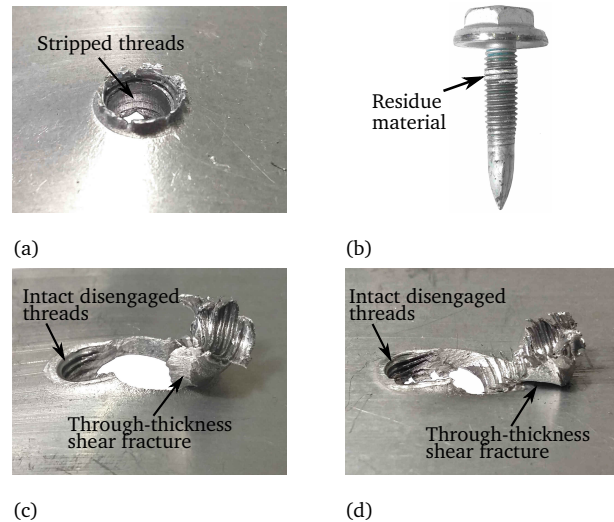


Fig. 6. Photographs of representative post mortem specimens from cross tests. (a) Cross tension, top side of bottom plate. (b) Cross tension, screw. (c) Cross mixed mode, top side of bottom plate. (d) Cross shear, top side of bottom plate.

137 bottom plate. This is clearly seen in Figs. 6a and 6b, where residue material from the stripped threads is seen on
138 the screw. There were limited deformation of the top plates, therefore they are left out from Fig. 6.

139 A stiffer response was observed for the mixed mode tests. The force reached a maximum of approximately
140 4.6 kN. Fig. 6c indicates that the main failure mechanism was through-thickness shear fracture of the bottom
141 plate material. The tangential component of the displacement of the top plate pushed the screw sideways such
142 that the threads were engaged only on one side of the hole. Fig. 6c clearly shows intact disengaged threads on
143 the left side of the hole and through-thickness shear fracture on the right.

144 The connection gave stiffest response under pure shear loading. The maximum force was approximately 6.5
145 kN. As for the mixed mode tests the tangential displacement pushed the screw sideways and disengaged the
146 threads on one side. Fig. 6d indicates that failure occurred by through-thickness shear fracture of the bottom
147 plate. Slight plastic bending of the screw shaft was observed for some of the cross shear tests.

148 There was no clear end of the pure shear tests. In pure tension and mixed mode, the end of test was clearly
149 seen as the force dropped to nearly zero and the plates were completely separated. This was not the case under
150 pure shear loading (see Fig. 5). As the cross shear specimen was deformed the screw rotated and tried to push the
151 plates apart. However, the steel casing of the testing rig prevented any motion other than the pulling direction,
152 with the consequence that the screw was squeezed between the plates. Thus the force level did not drop to zero
153 even after fracture took place, probably due to high frictional and contact forces between the screw and plates.

154 The top plate did not experience failure in any of the tests, only plastic deformations. They are therefore not
155 depicted.

156 2.2. Single lap-joint and peeling tests

157 The single lap-joint and peeling tests were done using the set-up described by Sønstabø et al. (2015), who
158 carried out similar tests for a different connection. The specimens (illustrated in Figs. 3b and 3c) were clamped
159 in a standard Instron tensile test machine using mechanical grips with a clamping length of 40 mm. The clamps
160 were centred along the load application line, such that the single lap-joint specimen was slightly deformed during
161 clamping (this is illustrated in Fig. 7). The deformation was purely elastic. The force was measured using an
162 Instron load cell and the displacement was recorded from the cross-head displacement of the test machine. The
163 cross-head velocity was set to 10 mm/min.

164 The force-displacement response in the single lap-joint tests (Fig. 8a) was similar to the cross shear test. The
165 maximum force was slightly lower (approximately 5.9 kN) and the ductility was comparable. A clear failure

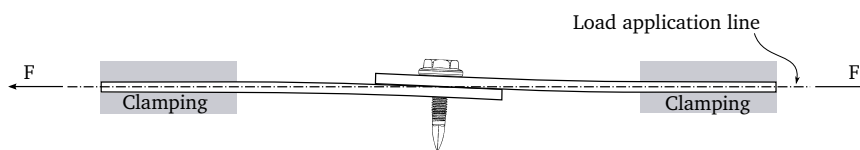
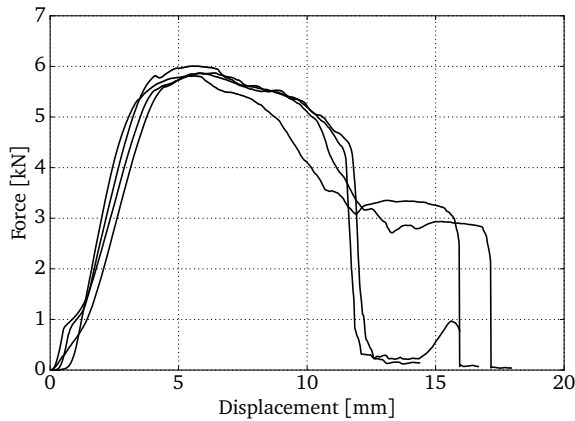
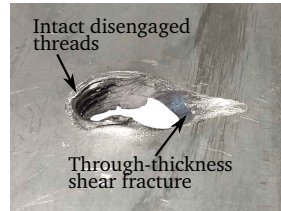


Fig. 7. Illustration of clamping in the single lap-joint test.



(a)



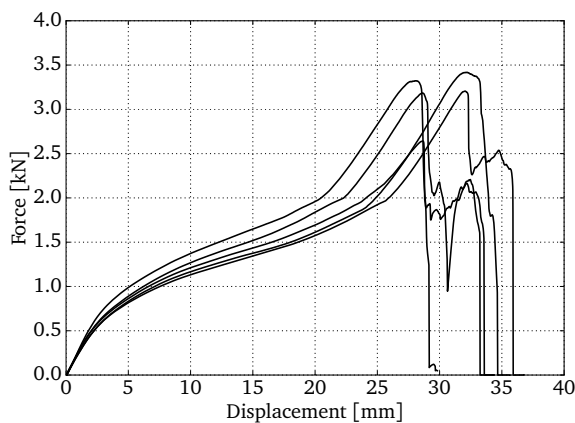
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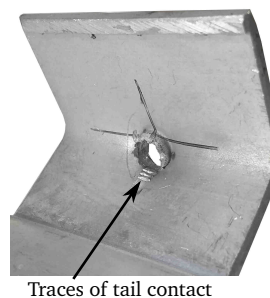
(c)

Fig. 8. Results from single lap-joint tests as (a) force-displacement curves, and representative post-mortem pictures of (b) top side of bottom plate and (c) screw.

166 was seen in the force curves, probably due to less restrictive clamping than in the cross shear tests. The simpler
 167 clamping conditions allowed the plates to bend more, possibly rotating the entire connection. This probably
 168 introduced tensile loading on the connection. Significant scatter is seen for the displacement at failure, which
 169 is not uncommon for tests on connections such as FDS. As for the cross mixed and shear tests the presence of
 170 the pre-hole caused large variation in initial stiffness. Parts of post-mortem specimens are depicted in Figs. 8b
 171 and 8c. As seen, the failure mechanism was similar to the cross shear tests, with through-thickness shear fracture
 172 of the bottom plate. Significant plastic bending of the screw shaft occurred in the single lap-joint tests.



(a)



(b)



(c)

Fig. 9. Results from peeling tests as (a) force-displacement curves, and representative post-mortem pictures of (b) top side of bottom plate and (c) underside of bottom plate.

173 Fig. 9a shows the force-displacement curve from the peeling tests. A knee was observed after ca. 2.5 mm
174 displacement, caused by yielding of the plate materials. The force gradually increased up to 2 kN where the slope
175 abruptly increased due to contact between the shaft of the screw and the bottom plate (traces of the contact
176 visible in Fig. 9b). Some variation was evident in the force level as well as in the displacement at the time of
177 shaft contact. These variations were probably caused by discrepancies in the position of the screw. The maximum
178 force was approximately 3.2 kN and failure occurred by thread stripping in the bottom plate (see Fig. 9c).

179 3. Process effects

180 In the FDS process flow-drilling and thread forming is combined into a single procedure where the screw is
181 both used as tool to generate the hole and as fastener. The process (illustrated in Fig. 10) consists of the following
182 six stages (Skovron et al., 2014; Sønstabø et al., 2015): *heating*, *penetration*, *extrusion forming*, *thread forming*,
183 *screw driving* and *tightening*. In the heating stage the screw is forced against the plate material while rotating
184 (usually 2000-6000 rpm) to heat up the material. Subsequently an increasing downward force is applied and the
185 screw penetrates the plate. Material flows up and down along the length of the screw and forms a boss (material
186 that flows upwards between the plate and the screw head). When the tail of the screw pierces the bottom surface
187 of the plate a so-called extrusion is formed as material flows downwards along the screw shaft. Threads are
188 created by a thread-forming zone on the fastener, and the screw is driven in until the head hits the top plate. A
189 final torque is applied to a pre-set value in order to ensure a tight connection. The whole process usually takes
190 between 1.5 and 4 seconds, depending on the material combination, plate thickness and type of screw.

191 During the process the plate material close to the screw simultaneously undergoes a temperature increase
192 and significant plastic straining. The plastic straining leads to a work-hardened zone of unknown size. Skovron

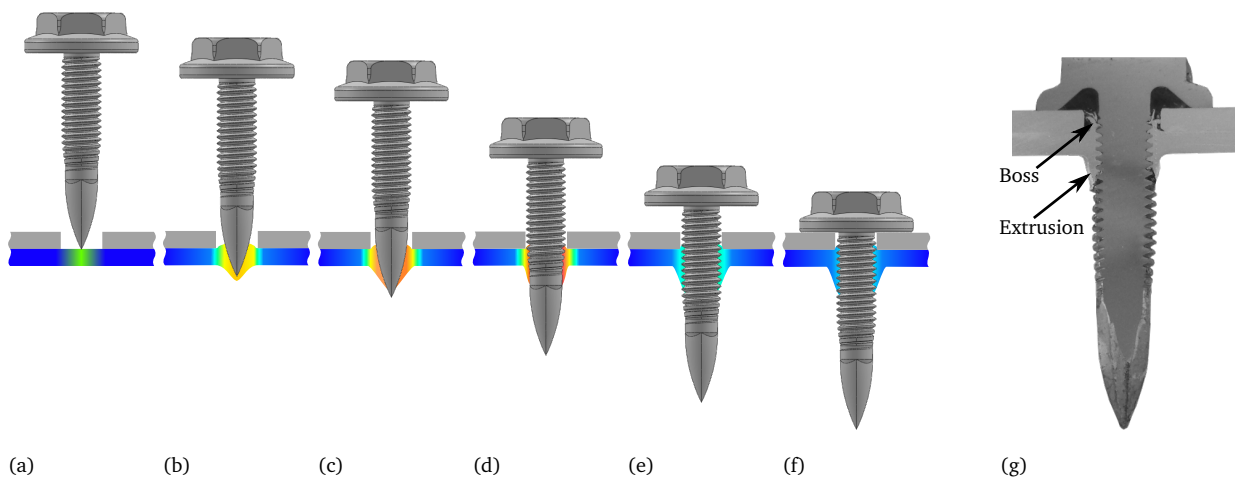


Fig. 10. The FDS process. (a) Heating. (b) Penetration. (c) Extrusion forming. (d) Thread forming. (e) Screw driving. (f) Tightening. A picture of an FDS connection is shown in (g), with the boss and extrusion indicated.

193 et al. (2014) measured the surface temperature during the process for different fastener forces (which is inversely
194 related to the temperature), and reported temperatures between 150 °C and 330 °C. The increased temperature
195 may have two consequences. First, it leads to thermal softening which reduces the resistance against the plastic
196 deformations during the process, which would facilitate penetration of the screw into the bottom plate. Second,
197 the higher temperature might lead to permanent changes in mechanical properties of the aluminium alloy. This
198 would imply that there is a process-affected zone of unknown size due to the process.

199 As explained in Section 4, potential process effects were neglected in the simulations. To assess this
200 assumption, a study consisting of a microstructural analysis and Vickers hardness tests was carried out and is
201 presented in the following.

202 3.1. Microstructural Analysis

203 Fig. 11 presents a metallographic photograph of the bottom plate cross-section (excluding the screw), where
204 different colours indicate particular grain orientations. Various details are highlighted by zoomed-in pictures.
205 When examining the pictures it is seen that the grains are markedly deformed close to the screw, implying that
206 large plastic strains have occurred during the process. The deformation appears to be most severe near the surface
207 of the threads (closest to the screw). Inside the boss and extrusion all grains seem deformed. This was expected,
208 since these areas were formed by plastic material flow during the process. In the internal area close to the screw
209 the deformations seem less severe, except for very close to the screw. At a distance of approximately 0.5 mm (one
210 thread-width) away from the screw the grains are seemingly undeformed (see lower left part of Fig. 11). This
211 observation indicates that the plastic deformations are localised and that the width of the plastically deformed
212 zone is small.

213 3.2. Vickers Hardness Tests

214 Vickers hardness tests were carried out on the cross-section surface of the bottom plate to further study
215 the effect of the process. The measurements were done with HV0.5 with 0.5 mm distance between dents. This
216 produced dents with a diameter of approximately 115 µm. A smaller weight and denser indenting pattern (micro
217 hardness) were not desirable as individual grains would be indented. The results would then be more affected
218 by the different grain orientations and produce more scatter. The grain size for this alloy typically ranges from
219 60 to 80 µm (Fig. 11). The measurements were done along two horizontal and one vertical line on both sides of
220 the screw. Fig. 12a shows the measurement locations and illustrates the naming convention used to identify the
221 individual dents. Each row was assigned a label (e.g. A2), and a location number. As an example, point A2-14
222 corresponds to the leftmost dent in the upper horizontal line on the left side.

223 The results show no significant variation in hardness in the horizontal direction away from the screw
224 (Fig. 12b), except points A1-1 and B1-1 where a somewhat lower hardness was measured. These points were
225 closest to the screw, located in the area between two threads. The measurements in the vertical direction along

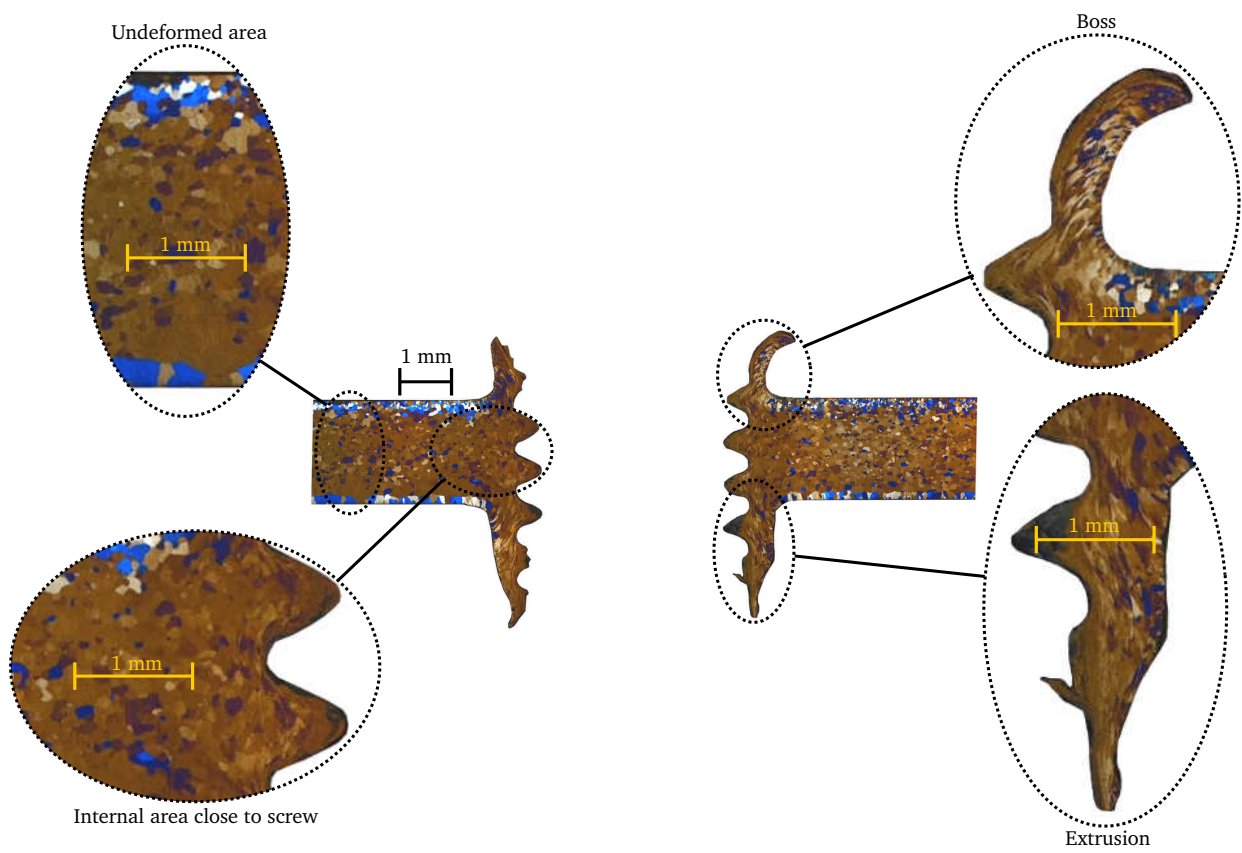


Fig. 11. Metallographic photograph of a cut FDS cross-section excluding the screw. Zoomed-in details are included.

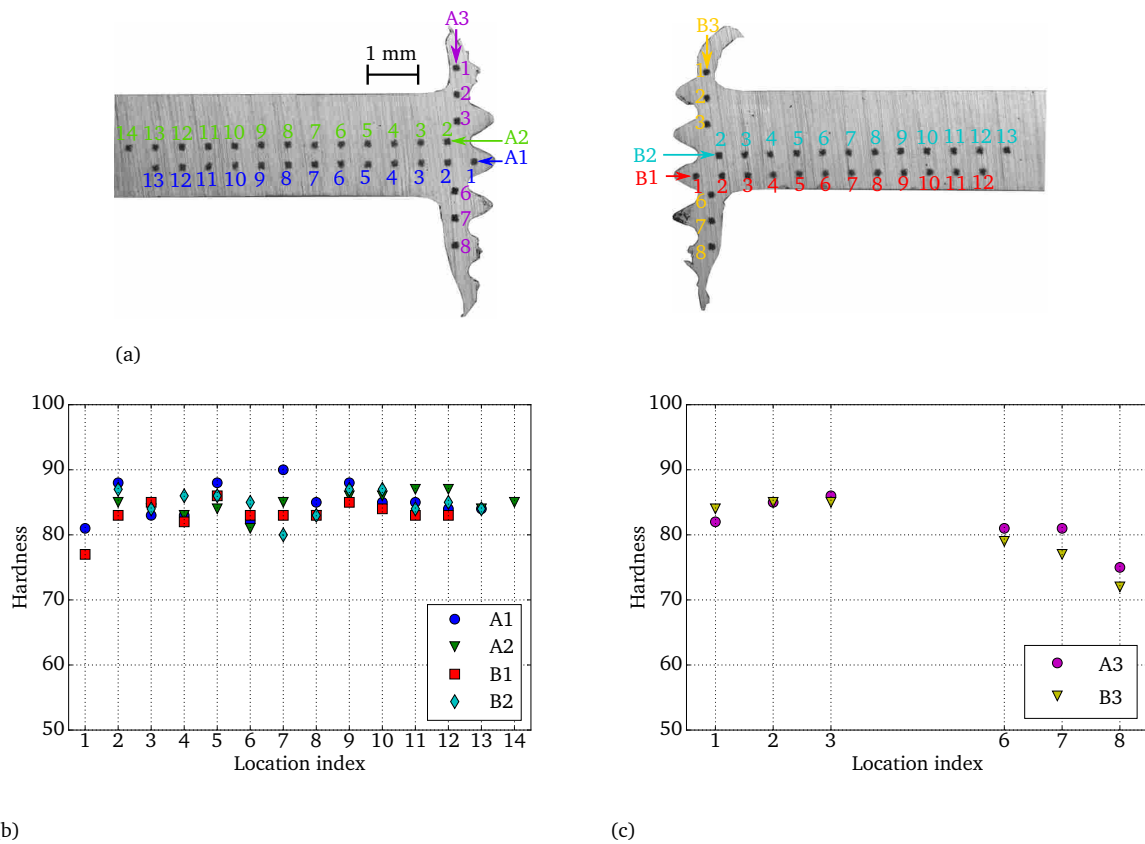


Fig. 12. Vickers hardness tests. (a) Dent locations. (b) Hardness values along horizontal lines. (c) Hardness values along vertical lines.

226 the boss and extrusion are given in Fig. 12c. Insignificant variation was observed for the three uppermost points
 227 (location 1, 2 and 3), compared to measurements far away from the screw in Fig. 12b, while somewhat lower
 228 hardness was measured for the three lowermost points (location 6, 7 and 8). It is noted that points A1-1, B1-
 229 1, A3-1, A3-8, B3-1 and B3-8 were close to the free edge which might affect the measured hardness for these
 230 points. The results from the Vickers hardness tests conform to findings by Skovron et al. (2014) and support the
 231 hypothesis that the process-affected zone is small.

232 4. Numerical model set-up

233 4.1. Finite element models

234 In this section the finite element models and the material models used are presented and discussed.

235 A circular finely meshed model of the connection was generated and tied to five more coarsely meshed models
 236 corresponding to the five experimental tests (see Fig. 13). The connection model was generated as follows. Three
 237 parts were defined: the screw, the bottom plate and the top plate. Because the precise geometry of the screw
 238 was unknown an approximate geometry was measured using a simple camera technique, illustrated in Fig. 14. A

239 screw was cut in half and a computer programme used to measure the outline of the screw cross-section from a
 240 picture, which was subsequently utilised to revolve a 3D part. This operation implies that the helix shape of the
 241 threads was neglected. This simplification was studied by Chen and Shih (1999), who observed small changes
 242 in the load distribution compared with including the helix shape, but otherwise similar results. The outer edge
 243 of the boss and extrusion of the hole in the bottom plate was modelled in a general way by straight lines and
 244 circular arcs (see magenta lines in Fig. 15), and their dimensions were chosen based on the picture in Fig. 1b.
 245 The bottom plate was generated without a hole, and the screw was positioned in place such that the two parts
 246 overlapped. The overlapping volume was then removed from the bottom plate, such that a hole with identical
 247 geometry as the screw was generated, including internal threads. With this technique the internal threads of the
 248 bottom plate coincided with the external threads of the screw, which facilitates the meshing operation. Hence
 249 possible gaps between the screw and bottom plate were not accounted for. The top plate was modelled with a
 250 pre-hole of 7 mm diameter.

251 The screw was discretised using 10-node modified quadratic tet elements, while the plates were comprised
 252 of 8-node hex elements with reduced integration. As seen in Fig. 15, a fine mesh was required to resolve the
 253 geometry of the threads. The smallest element size of the bottom plate was approximately 0.03 mm, while the
 254 coarse parts were modelled with five elements through the plate thickness.

255 Fig. 16 illustrates the finite element models corresponding to the five tests. Figs. 16a and 16b show which
 256 parts of the cross specimens that were modelled. As seen, only the deformed part of the specimens were included
 257 (clamped areas were omitted), and displacements were prescribed on the surfaces corresponding to the clamped
 258 parts. For the bottom plate prescribed displacements were zero (fixed surfaces), while for the top plate they were
 259 zero in all directions except in the loading direction where a displacement was applied (indicated with arrows in
 260 Figs. 16c to 16g). The deformation during clamping in the single lap-joint tests was accounted for by applying a

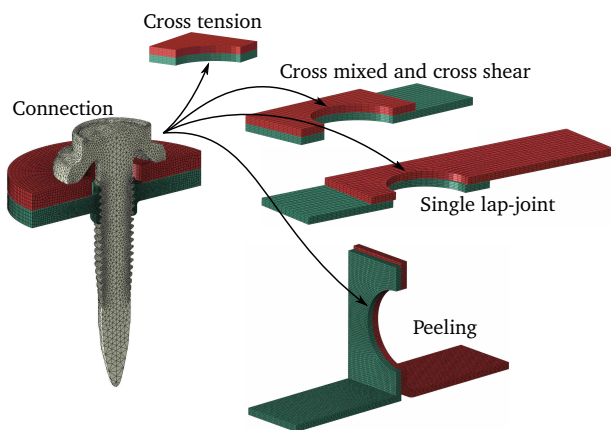


Fig. 13. Illustration of how the connection mesh was inserted into coarser specimens with tie constraints.

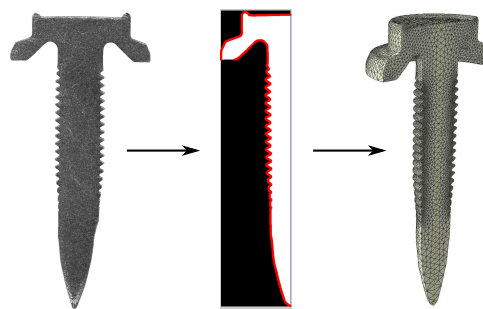


Fig. 14. Illustration of how the geometry of the screw part was generated.

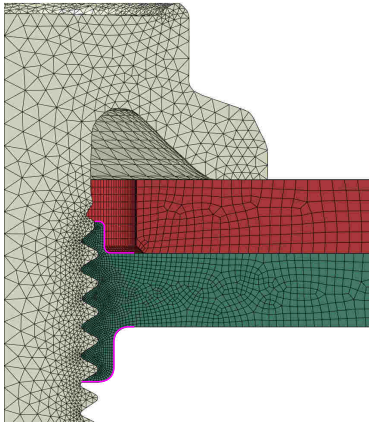


Fig. 15. Half cross-section of the finite element model.

261 2 mm displacement perpendicular to the loading direction before the main loading was applied (see Fig. 7).

262 The simulations were carried out using the Abaqus v6.11 explicit solver with double precision. Symmetry was
263 utilised where possible, mass scaling was applied (inertia effects were ensured negligible), and a general surface-
264 to-surface contact algorithm was used between the different parts. A friction coefficient of 0.1 was chosen. For
265 reference, Porcaro et al. (2006) chose a friction coefficient of 0.15. Prescribed displacements were applied with
266 a smooth amplitude. Fracture was modelled with element erosion.

267 4.2. Material model

268 The aluminium plates and steel screw materials were modelled using a rate-independent isotropic hypoelastic-
269 plastic material model. It is, however, well known that the herein used aluminium alloys exhibit orthotropic
270 plastic anisotropy, for instance as shown by Lademo et al. (1999), Lademo et al. (2009) and Sønstabø et al.
271 (2016). To obtain a more accurate description of local deformations one could use anisotropic phenomenological
272 plasticity or even crystal plasticity together with the finite element method. The crystallographic texture varied
273 through the thickness of the 6063-extrusion (Fig. 11). Khadyko et al. (2016) showed that a very similar 6063-
274 extrusion had a central layer with approximately cube orientation, an intermediate layer with random texture,
275 and a small outer layer with Goss orientation. In spite of this an isotropic phenomenological plasticity material
276 model was chosen in this work. A more advanced anisotropic phenomenological yield function or a crystal
277 plasticity material model would greatly increase the computational time, due to the large number of elements
278 in the mesh. It would require three different yield surfaces through the thickness. In addition, the mesh size
279 was some places smaller than and some places larger than the grain size. Moreover, the global results of the
280 simulations in this work were satisfactory, which indicates that the anisotropy of the material does not affect the
281 global behaviour in a significant way. Therefore the marginal improvements crystal plasticity or a more advanced
282 phenomenological yield surface could bring, do not justify the increase in computational time.

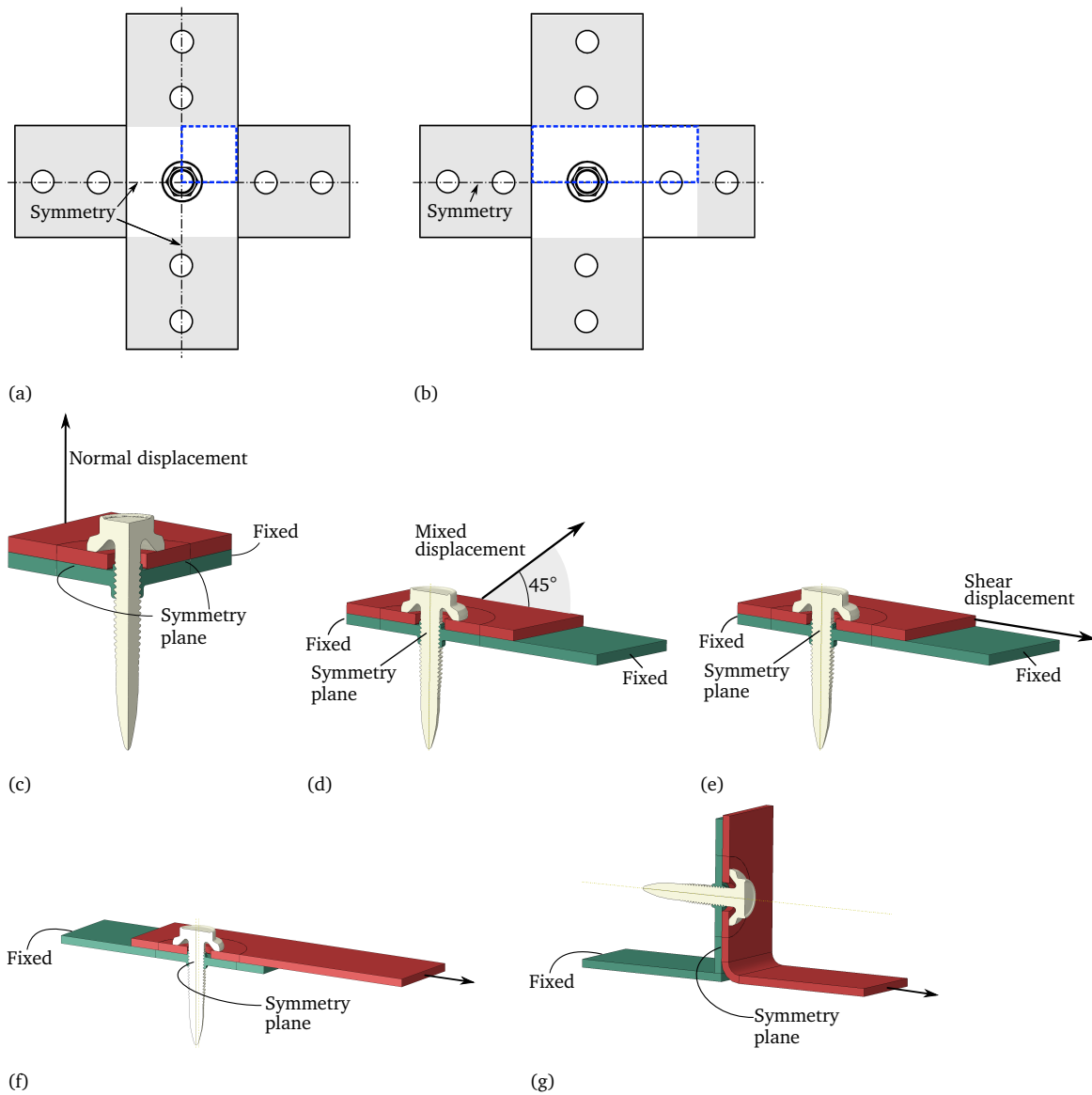


Fig. 16. Illustration of how each test was modelled. (a) and (b) shows which parts of the cross specimens that were modelled. (c) Cross tension model. (d) Cross mixed model. (e) Cross shear model. (f) Single lap-joint model. (g) Peeling model.

283 To model plasticity the von Mises yield surface was used, associated flow assumed, and isotropic hardening
 284 applied. The yield function may be written as

$$f = \sigma_{\text{eq}} - (\sigma_0 + R) \leq 0,$$

285 where σ_{eq} is the von Mises equivalent stress, σ_0 is the initial yield stress, and R is an isotropic hardening variable.
 286 The Voce hardening law was selected,

$$R = \sum_{i=1}^N Q_{Ri} \left(1 - \exp\left(-\frac{\theta_{Ri}}{Q_{Ri}} p\right) \right), \quad (1)$$

287 where p is the equivalent plastic strain, N is the number of terms used, and Q_{Ri} and θ_{Ri} are the saturation stress
 288 and initial hardening modulus for term i , respectively. Two terms were sufficient for the bottom plate while three
 289 terms were needed for the top plate and screw material.

290 In the experiments material fracture took place only in the bottom plate, the top plate and screw material did
 291 not fail. To model fracture in the bottom plate, element erosion with the Cockcroft-Latham criterion (Cockcroft
 292 and Latham, 1968) was included for this part. The criterion states that failure occurs when the integral

$$W = \int_0^p \langle \sigma_1 \rangle dp \quad (2)$$

293 attains a critical value W_C . Here σ_1 is the maximum principal stress and $\langle \cdot \rangle$ denotes the Macauley brackets. Hence
 294 damage grows for a positive principal stress only. The criterion is easy to calibrate from a single uniaxial tensile
 295 test and was chosen for its simplicity.

296 The procedure to calibrate the initial yield stress and hardening parameters for the plate materials has been
 297 reported by Sønstabø et al. (2016). The parameters were obtained by reverse engineering uniaxial tensile tests
 298 with finite element simulations. Fig. 2a shows adequate correlation between tests and simulations.

299 The critical failure value W_C was obtained from the uniaxial tensile test simulation of the bottom plate
 300 material, by calculating the integral in Eq. (2) in the most critical element when the nominal strain in the
 301 simulation matched the experimental nominal strain at time of fracture (see Fig. 2a). The mesh size in the
 302 neck area of the tensile simulation was approximately 0.06 mm. It is known that W_C is a mesh size dependent
 303 parameter, due to increased strain gradients for denser meshes (Björklund et al., 2013). The mesh size
 304 dependency was, however, not accounted for here, one value for W_C was used for all elements, which was
 305 considered representative for the mesh size where fracture took place in the FDS simulations. Fig. 17 shows the
 306 resulting failure loci for generalised tension ($L = -1$), generalised shear ($L = 0$) and generalised compression
 307 ($L = 1$), where L is the Lode parameter defined as $L = -\cos 3\theta_L$ and θ_L is the Lode angle.

308 The screws were subjected to limited plastic deformations, and a simpler approach could be used to calibrate
 309 the hardening parameters. Uniaxial tensile tests of the screw material were carried out, using axisymmetric
 310 specimens which were cut out from the screw shaft (resulting engineering stress-strain curve is shown in Fig. 2b).

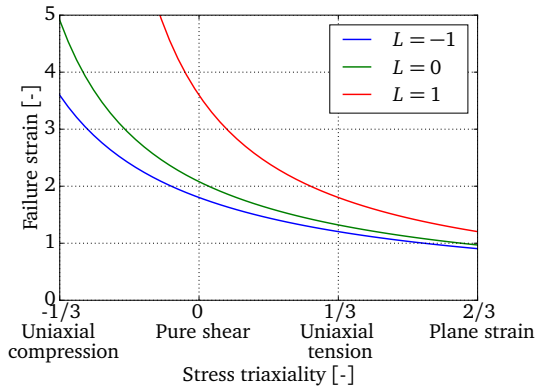


Fig. 17. Cockcroft-Latham failure loci for generalised tension ($L = -1$), generalised shear ($L = 0$) and generalised compression ($L = 1$).

311 The nominal strain was measured using an extensometer, and a digital camera was employed to track the diameter
 312 of the specimen. The post-necking plastic strain was calculated from the diameter measurements assuming plastic
 313 incompressibility. The post-necking equivalent stress was approximated using Bridgman correction (Bridgman,
 314 1944), where the radius of the neck was measured from the digital images. Eq. (1) was then fitted to the obtained
 315 equivalent stress-plastic strain curve. Fig. 2b shows the result from a simulation of the material test using the
 316 obtained hardening parameters. As seen, the correlation was excellent for the relevant strain level.

317 Typical steel and aluminium values were used for the Young's modulus E and the Poisson ratio ν . The
 318 material model parameters are summarised in Table 1.

319 4.3. Process effects

320 Possible process effects were discussed in Section 3. Metallographic photographs and Vickers hardness tests
 321 indicated that there was a local process-affected zone extending approximately 0.5 mm from the screw into the
 322 bottom plate. In the present finite element models, process effects were not taken into account. Satisfactory
 323 results were nevertheless obtained, which indicates that the process effects do not significantly affect the global
 324 behaviour.

Table 1

Material model parameters for the screw and plate materials.

	E	ν	σ_0	Q_{R1}	θ_{R1}	Q_{R2}	θ_{R2}	Q_{R3}	θ_{R3}	W_C
	[MPa]	[-]	[MPa]	[MPa]	[MPa]	[MPa]	[MPa]	[MPa]	[MPa]	[MPa]
Screw (steel)	210000	0.3	1051.1	16.8	12507	89.6	5726	1885	267	-
Top plate (AA 6016 T4)	70000	0.35	117.6	29.2	25000	149.5	2011	100	230	320
Bottom plate (AA 6063 T6)	70000	0.35	204.6	8.0	12300	55	1472	-	-	-

325 5. Simulation results

326 In this section the results from the finite element simulations of the experimental tests are presented
327 and discussed. Global force-displacement curves are graphed, the simulated deformation modes and failure
328 mechanisms are explained, and various field variables are plotted when needed for discussion. The cross test
329 simulations are presented first, followed by the single lap-joint and peeling test simulations.

330 Overall good agreement was obtained between the simulations and experiments, both in terms of force-
331 displacement responses and deformation modes, despite the simplifications made in the model (see Section 4).

332 5.1. Cross test simulations

333 As discussed in Section 2.1, variations in initial stiffness in the cross mixed and cross shear experiments
334 occurred due to the pre-hole in the top plate, which allowed for relative sliding between the top and bottom
335 plates (recall Fig. 5). The force required for sliding to occur was different from specimen to specimen, and was
336 a function of unknown process parameters and the amount of prestress in the screw. Therefore this sliding could
337 not be captured accurately by the finite element models. Acknowledging that the simulations did not capture the
338 sliding accurately, it was chosen to shift the cross mixed and shear experimental curves to match the displacement
339 of the simulations at 2 kN force. By doing this, the effect of the relative sliding in the experiments, and the poor
340 representation of it in the simulations, was eliminated. It was assumed that all sliding occurred before 2 kN force
341 was reached, and thus that the results afterwards could be compared. The shifting is illustrated in Fig. 18, which
342 shows the start of the curves without and with shifting of the experimental curves. As seen, all shifted curves
343 coincide at 2 kN force.

344 The force-displacement response from the cross test simulations are compared to the experimental results in
345 Fig. 19, with the mixed and shear experimental curves shifted as explained above. As shown, overall satisfactory
346 results were obtained. The force levels and shape of the curves match well with the experiments.

347 Throughout the cross tension test simulation the initial stiffness and force level were somewhat higher than in
348 the experiments. Good agreement was obtained for the displacement at global failure. The overall deformation
349 mode and failure mechanism of the specimen agreed with the experiment. As the bottom plate was bent upward
350 the topmost threads were disengaged such that the three bottommost carried all the load. This is seen in Figs. 20a
351 and 20b where the equivalent plastic strain field is plotted on the initial and deformed configurations a short
352 instance before failure, which occurred by fracture in the threads. Agreement in deformation and failure mode
353 with the experiment may be seen when comparing Fig. 20b with Fig. 6a.

354 The over-estimated stiffness in the cross tension simulation may indicate inaccuracies in the boundary
355 conditions. In the experiment the plates were subjected to membrane forces and bending, which could lead to
356 some deformation of the material in the edge of the clamping, which was not accounted for in the finite element
357 model. In an effort to evaluate this effect, a finite element model with a simple model of the clamping was

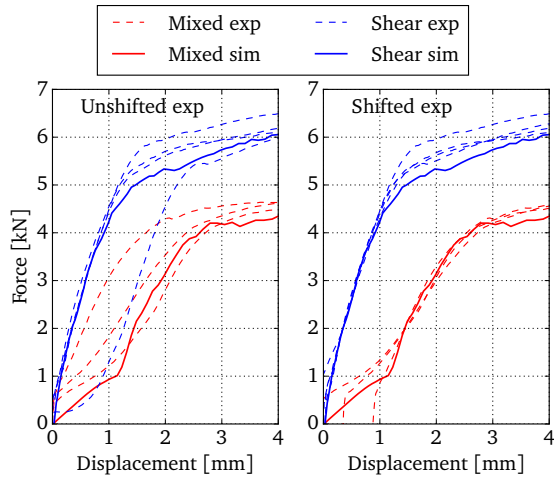


Fig. 18. Illustration of shifting of cross mixed and cross shear experimental curves.

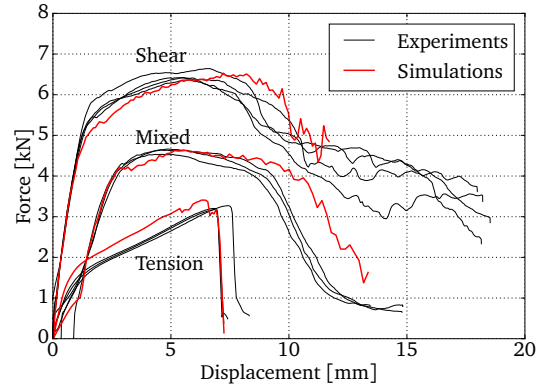


Fig. 19. Force-displacement curves from cross test simulations compared to experiments.

358 made, see Fig. 21a. The clamps were modelled as rigid, and the clamping was handled by increasing the friction
 359 coefficient to 0.6 between the clamps and plates, which ensured little slipping. The result is graphed in Fig. 21b
 360 and shows better agreement for the initial stiffness and force level, suggesting that the overestimated stiffness
 361 and force by the constrained model was indeed caused by inaccurate boundary conditions. The maximum force
 362 was, as expected, unchanged.

363 In cross shear and mixed mode excellent agreement in stiffness and maximum force level was achieved
 364 when accounting for the pre-hole sliding. Deformed specimens with equivalent plastic strain fields on initial
 365 and deformed configurations are shown in Figs. 20c to 20f. As seen, the deformation modes in cross mixed and
 366 shear were somewhat similar. In mixed mode the screw was pushed sideways and pulled upwards by the top
 367 plate, causing the screw to rotate slightly and stressing the threads on the right side of the hole. In shear the screw
 368 was pushed sideways by the top plate, causing the screw to rotate significantly. However, in both simulations
 369 failure occurred later and the failure took place closer to the screw than in the experiments, which can be seen by
 370 comparing Figs. 20d and 20f with Figs. 6c and 6d, respectively. This is possibly explained by the Cockcroft-Latham
 371 failure model. As seen in Fig. 17, the model predicts a higher failure strain for pure shear and compressive stress
 372 states than under uniaxial tension (for which it was calibrated), and goes to infinity for pure compressive stress
 373 states. It has, however, been shown that for some ductile metals in the low stress triaxiality regime the failure
 374 strain does not increase monotonically with decreased hydrostatic stress (stress triaxiality) (Bao and Wierzbicki,
 375 2004; Barsoum and Faleskog, 2007). In the cross mixed and cross shear test simulations the stress triaxiality in the
 376 area where failure took place in the experiments was low (≤ 0), suggesting that an over-estimation of the failure
 377 strain by the Cockcroft-Latham model was expected. Furthermore, as seen in Fig. 22 the stress state in the area
 378 where fracture took place in the cross shear experiment was purely compressive (negative main principal stress),

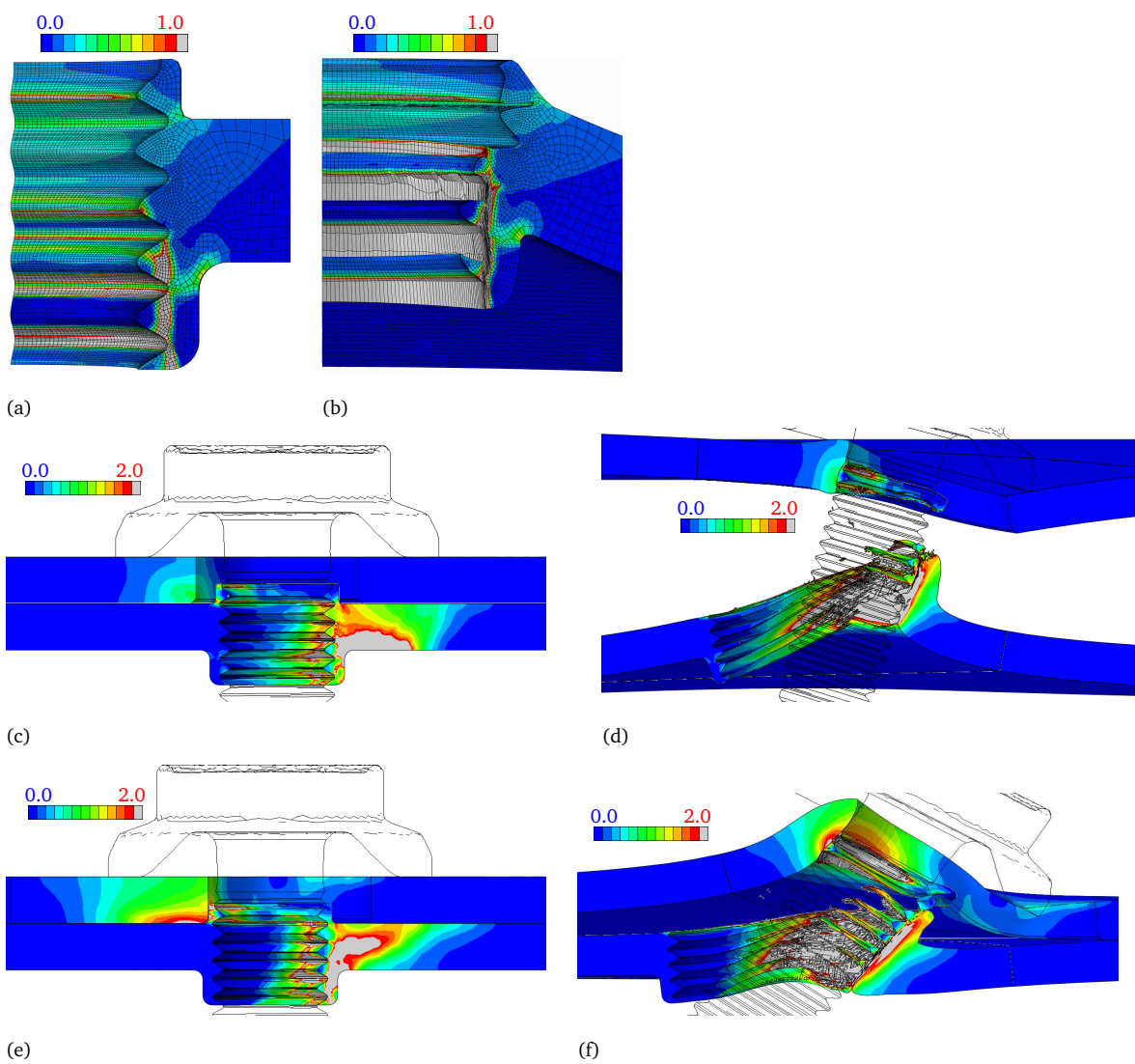


Fig. 20. Equivalent plastic strain field on undeformed and deformed configuration in (a and b) tension (right before failure), (c and d) mixed mode (last frame) and (e and f) shear (last frame).

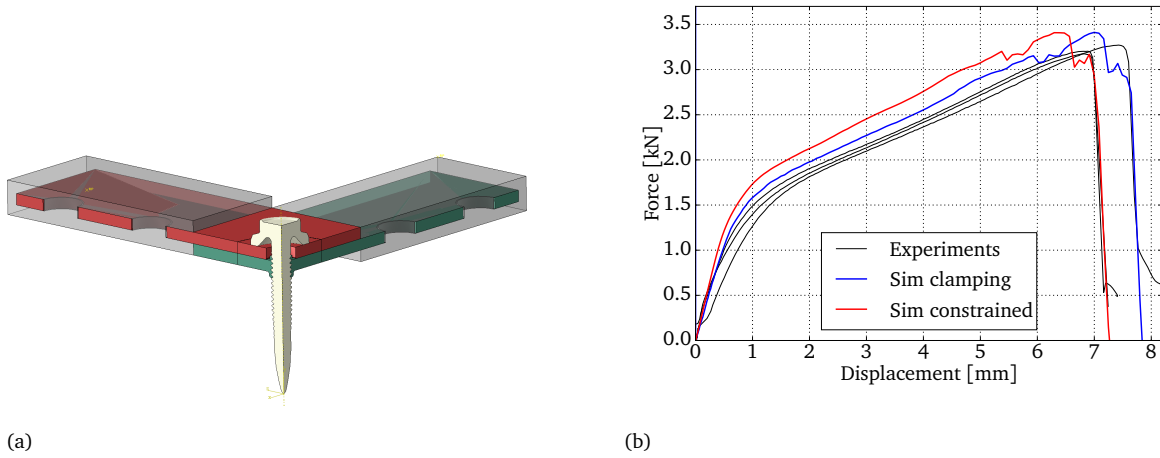


Fig. 21. Finite element model to check the effect of the clamping. (a) Finite element model. (b) Force-displacement results compared to the original constrained simulation and experiments.

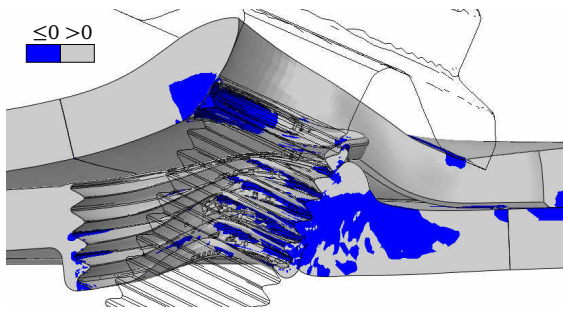


Fig. 22. Sign of main principal stress σ_1 at 8.9 mm displacement (time of maximum force) in the cross shear simulation. Blue colour indicates $\sigma_1 \leq 0$.

379 which implies that damage does not grow (Eq. (2)). Hence the failure model was not able to predict the failure
 380 mode of the experiments correctly, and fracture was forced to occur elsewhere (closer to the screw). However,
 381 the global results were nevertheless satisfactory. Thus such a model can still provide valuable information, and
 382 be used for e.g. calibration of macroscopic connection models.

383 5.2. Single lap-joint and peeling test simulations

384 Fig. 23a shows that the single lap-joint simulation agreed acceptably with the experiments. The maximum
 385 force was slightly over-estimated. In the experiments the maximum force occurred early (approximately 4 mm
 386 displacement) and the force decreased gradually until onset of failure, while in the simulation the force increased
 387 gradually from onset of plasticity to maximum force at approximately 8 mm displacement after which failure
 388 occurred abruptly. A good match was attained for the displacement at failure. The initial stiffness was reasonably
 389 predicted. This may possibly be attributed to the fact that the cross-head displacement was used as displacement

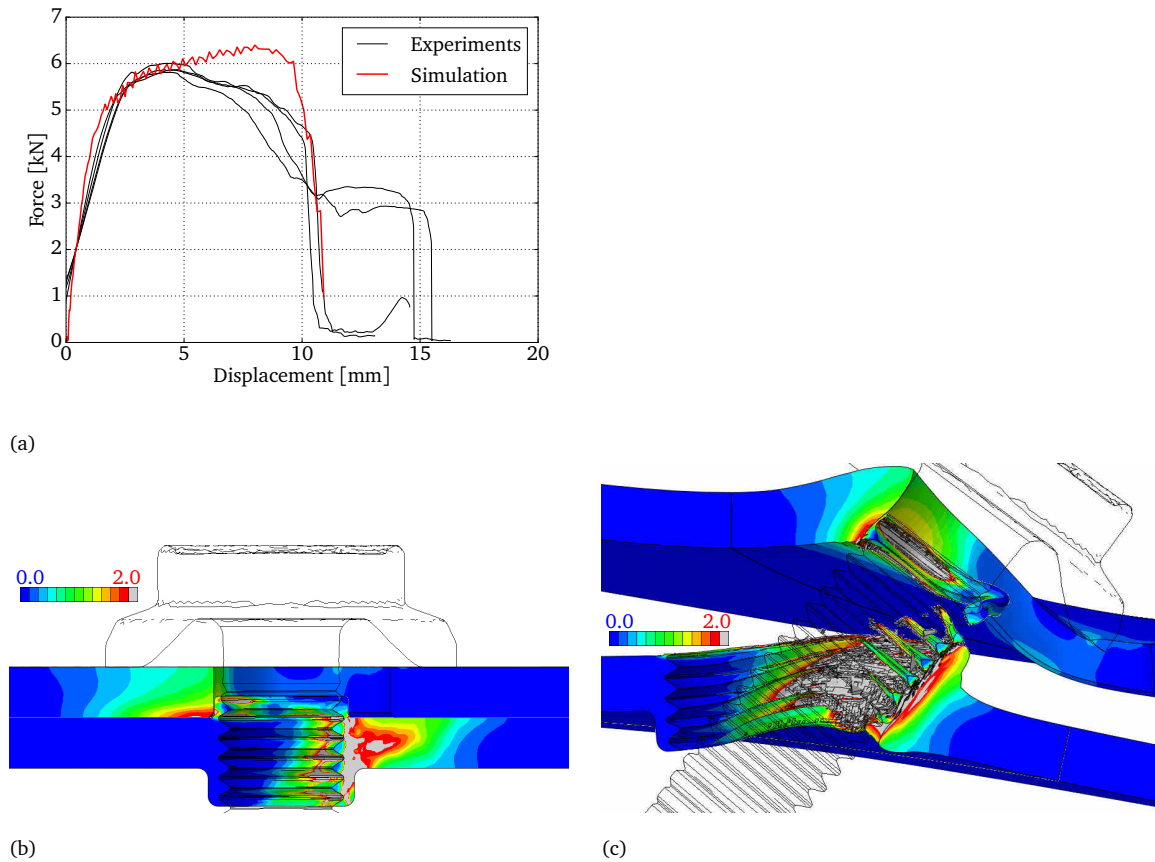


Fig. 23. Results from single lap-joint simulation. (a) Force-displacement curve. (b-c) Equivalent plastic strain field on undeformed and deformed configuration (last frame).

390 measure in the experimental tests, probably affected by compliance in the test set-up. Note that the experimental
 391 curves were shifted to coincide with the simulation at 2 kN force, as for the cross shear test simulations (see
 392 discussion above).

393 Figs. 23b and 23c depict the equivalent plastic strain field close to the screw at the end of the simulation on
 394 initial and deformed configurations, respectively. As seen when comparing with Figs. 20e and 20f the deformation
 395 was similar to the cross shear simulation. The less restrictive clamping in the single lap-joint test is clearly seen
 396 as the plates were further apart than in the cross shear simulation.

397 Favourable agreement was also obtained for the peeling simulation (Fig. 24a). The force level was generally
 398 satisfactory and the maximum force and displacement at failure were correctly predicted. The initial stiffness was
 399 slightly over-estimated, which, as for the single lap-joint tests, might be because the cross-head displacement was
 400 used as displacement measure in the experiments. It is also seen that the abrupt slope increase at 2 kN force
 401 caused by contact between the shaft of the screw and the bottom plate was well captured. Fig. 24b shows the
 402 deformed configuration at the time of maximum force, where the contact between the shaft of the screw and the

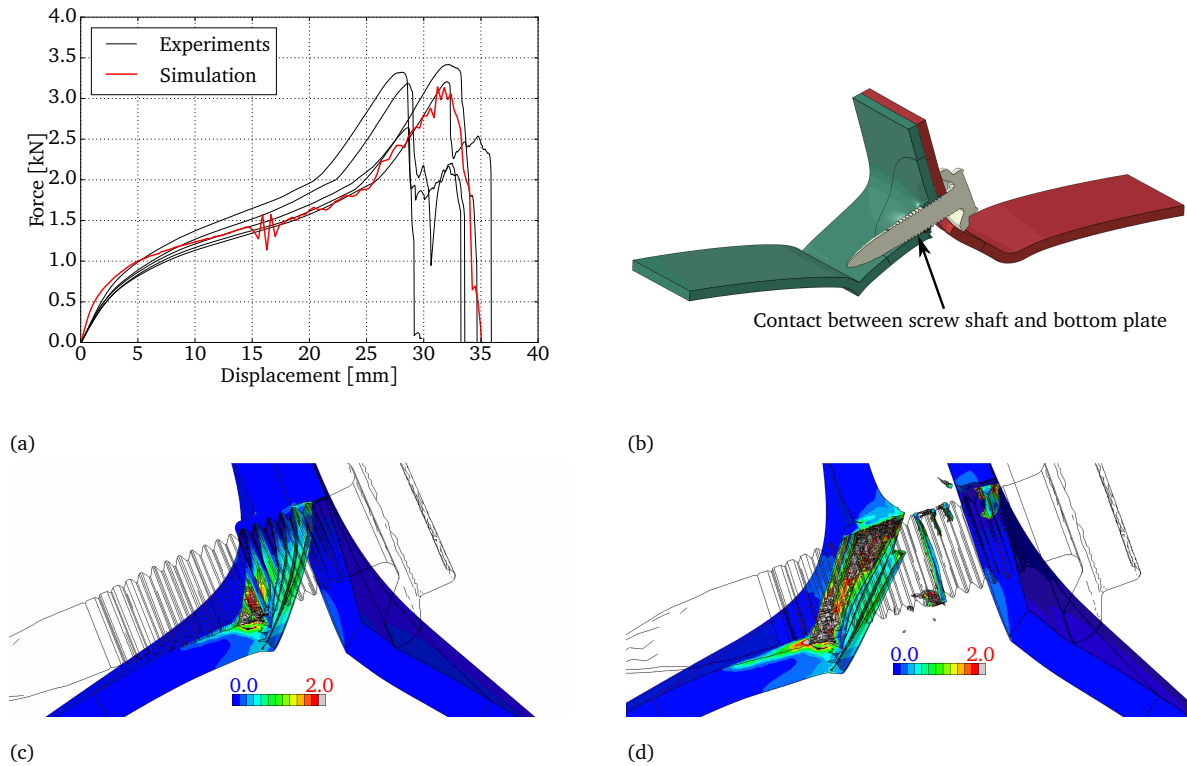


Fig. 24. Results from peeling simulation. (a) Force-displacement curve. (b) Deformed configuration at time of maximum force. (c) Equivalent plastic strain field at time of maximum force. (d) Equivalent plastic strain field after failure.

403 bottom plate is indicated. Figs. 24c and 24d show the equivalent plastic strain field at the time of maximum force
 404 and after failure, respectively. Failure occurred by stripping the still-engaged threads. The deformation mode
 405 and failure mechanism conformed to experimental observations.

406 5.3. Effect of friction coefficient

407 To evaluate the effect of the friction coefficient on the numerical results, the simulations were also carried
 408 out with friction coefficients of 0.0, 0.2 and 0.3, in addition to the original chosen value of 0.1. The coefficient
 409 was varied for three different contact interfaces independently, namely between the screw and the top plate,
 410 between the screw and the bottom plate, and between the two plates. It turned out that for tension loadings the
 411 friction coefficient had a negligible effect, while it was most prominent for shear loadings. Only the curves from
 412 the cross shear simulations are therefore shown. The results are summarised in Fig. 25. As seen, there was an
 413 effect on the maximum force level, while limited effect was seen on the ductility of the connections. Moreover,
 414 the variation due to friction coefficient was in the same order as the variation on the experimental curves. This
 415 is natural, due to uncertainties in the process parameters, such as surface cleanliness, pre-stressing and so on,
 416 causing diversity in friction in the connections. Changes in the friction coefficient did not alter the deformation

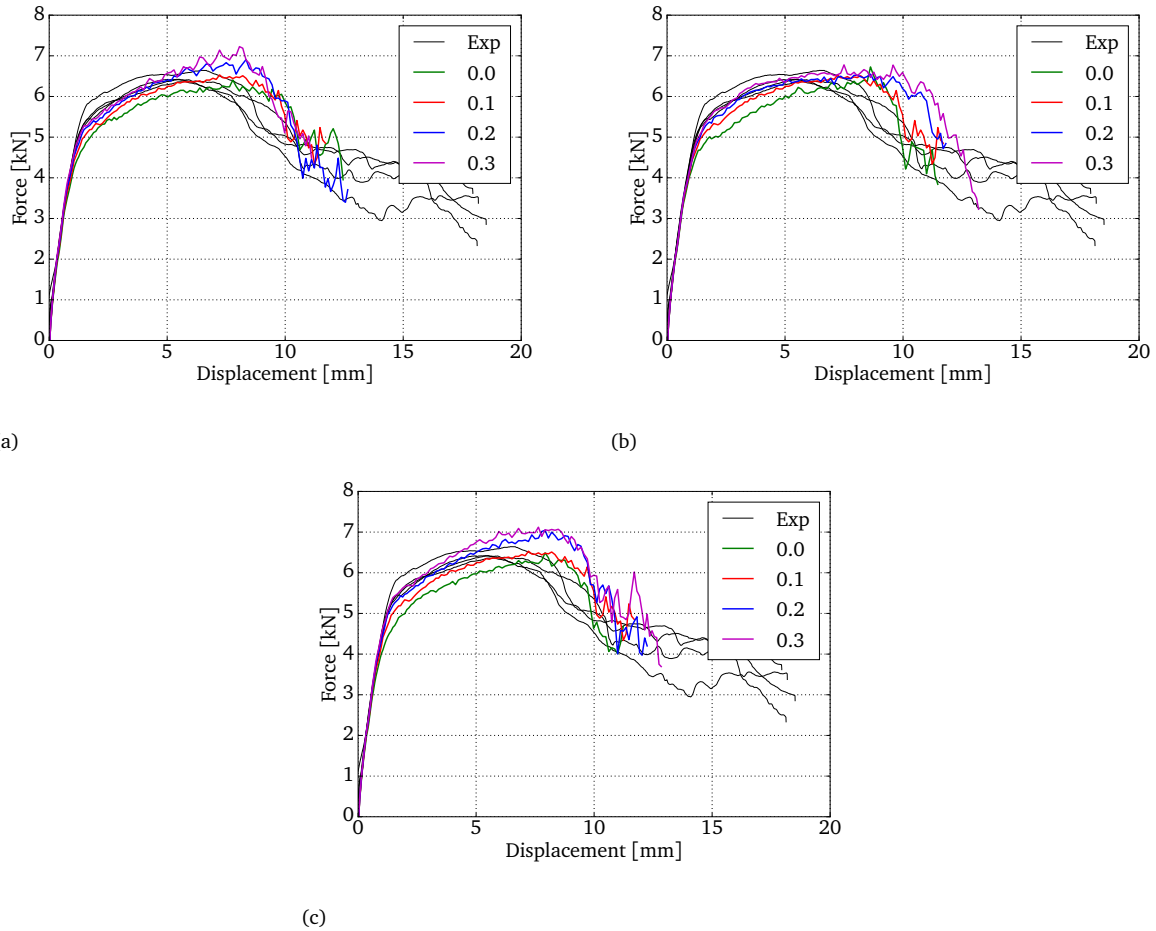


Fig. 25. The effect of friction coefficient on the global force-displacement curves in the cross shear simulation. The coefficient was varied at the contact interfaces between (a) the screw and top plate, (b) the screw and the bottom plate, and (c) between the plates.

417 modes significantly. Thus, changing the friction coefficients did not change the physics, the overall behaviour
 418 remained the same. Except for a slightly different maximum force, no conclusions would have changed if a
 419 friction coefficient of 0.3 had been chosen instead of 0.1.

420 6. Conclusions

421 In the present study the behaviour of flow-drill screw connections in quasi-static tests were simulated using
 422 finite element models with detailed solid element meshes. The experiments were described and presented in
 423 detail, including a new test set-up for cross tests. The numerical models were developed with a rate-independent
 424 isotropic hypoelastic-plastic material model. A simple approach for building up the geometry of the connection
 425 was presented. The following main conclusions may be drawn from the present investigation:

- 426 – A microstructural analysis indicated that the width of the plastically deformed zone due to the process is

- 427 small. This was supported by Vickers hardness tests that showed no significant variation in the horizontal
428 direction away from the screw.
- 429 – The finite element models gave satisfying results despite simplifications such as isotropic materials,
430 simplified connection geometry, a simple failure criterion, and neglected process effects.
 - 431 – Good matches between experimental and numerical global force-displacement curves were obtained for all
432 tests.
 - 433 – Overall deformation and failure modes agreed well with experiments. For shear-dominated loadings
434 fracture tended to occur closer to the screw than in the experiments. This was attributed to the Cockcroft-
435 Latham failure criterion's inability to account for damage at low stress triaxialities.
 - 436 – Overall, the demonstrated modelling strategy was well-suited to investigate the behaviour of FDS
437 connections under quasi-static loadings. This suggests that the approach may be used for virtual testing,
438 for instance to calibrate macroscopic connection models for large-scale analyses.

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445 **References**

- 446 Bao, Y., Wierzbicki, T., 2004. On fracture locus in the equivalent strain and stress triaxiality space. *International Journal of Mechanical*
447 *Sciences* 46 (1), 81 – 98. <https://doi.org/10.1016/j.ijmecsci.2004.02.006>
- 448 Barsoum, I., Faleskog, J., 2007. Rupture mechanisms in combined tension and shear-experiments. *International Journal of Solids and*
449 *Structures* 44 (6), 1768 – 1786, *Physics and Mechanics of Advanced Materials*. <https://doi.org/10.1016/j.ijsolstr.2006.09.031>
- 450 Björklund, O., Larsson, R., Nilsson, L., 2013. Failure of high strength steel sheets: Experiments and modelling. *Journal of Materials Processing*
451 *Technology* 213 (7), 1103 – 1117. <https://doi.org/10.1016/j.jmatprotec.2013.01.027>
- 452 Bouchard, P., Laurent, T., Tollier, L., 2008. Numerical modeling of self-pierce riveting—from riveting process modeling down to structural
453 analysis. *Journal of Materials Processing Technology* 202 (1), 290 – 300. <https://doi.org/10.1016/j.jmatprotec.2007.08.077>
- 454 Bridgman, P., 1944. The stress distribution at the neck of a tension specimen. *Trans. ASM* 32, 553–574.
- 455 Chen, J.-J., Shih, Y.-S., 1999. A study of the helical effect on the thread connection by three dimensional finite element analysis. *Nuclear*
456 *Engineering and Design* 191 (2), 109 – 116. [https://doi.org/10.1016/S0029-5493\(99\)00134-X](https://doi.org/10.1016/S0029-5493(99)00134-X)
- 457 Chen, N., Luo, H., Wan, M., loup Chenot, J., 2014. Experimental and numerical studies on failure modes of riveted joints under tensile load.
458 *Journal of Materials Processing Technology* 214 (10), 2049 – 2058. <https://doi.org/10.1016/j.jmatprotec.2013.12.023>
- 459 Cockcroft, M., Latham, D., 1968. Ductility and the workability of metals. *J Inst Metals* 96 (1), 33–39.

460 Fagerholt, E., 2012. Field measurements in mechanical testing using close-range photogrammetry and digital image analysis. Ph.D. thesis,
461 Norges teknisk-naturvitenskapelige universitet (NTNU).

462 Grujicic, M., Snipes, J., Ramaswami, S., 2016. Process and product-performance modeling for mechanical fastening by flow drilling screws.
463 International Journal of Structural Integrity 7 (3), 370–396. <https://doi.org/10.1108/IJSI-03-2015-0011>

464 Khadyko, M., Dumoulin, S., Hopperstad, O., 2016. Texture gradients and strain localisation in extruded aluminium profile. International
465 Journal of Solids and Structures 97, 239 – 255. <https://doi.org/10.1016/j.ijsolstr.2016.07.024>

466 Kong, X., Yang, Q., Li, B., Rothwell, G., English, R., Ren, X., 2008. Numerical study of strengths of spot-welded joints of steel. Materials &
467 Design 29 (8), 1554 – 1561. <https://doi.org/10.1016/j.matdes.2007.12.001>

468 Lademo, O.-G., Engler, O., Keller, S., Berstad, T., Pedersen, K., Hopperstad, O., 2009. Identification and validation of constitutive
469 model and fracture criterion for AlMgSi alloy with application to sheet forming. Materials & Design 30 (8), 3005 – 3019.
470 <https://doi.org/10.1016/j.matdes.2008.12.020>

471 Lademo, O.-G., Hopperstad, O., Langseth, M., 1999. An evaluation of yield criteria and flow rules for aluminium alloys. International Journal
472 of Plasticity 15 (2), 191 – 208. [https://doi.org/10.1016/S0749-6419\(98\)00064-3](https://doi.org/10.1016/S0749-6419(98)00064-3)

473 Liu, C., Tan, K. H., Fung, T. C., 2015. Investigations of nonlinear dynamic performance of top-and-seat with web angle connections subjected
474 to sudden column removal. Engineering Structures 99 (Supplement C), 449 – 461. <https://doi.org/10.1016/j.engstruct.2015.05.010>

475 Nielsen, K. L., Oct 2008. 3D modelling of plug failure in resistance spot welded shear-lab specimens (DP600-steel). International Journal of
476 Fracture 153 (2), 125–139. <https://doi.org/10.1007/s10704-008-9305-4>

477 Nielsen, K. L., Tvergaard, V., 2010. Ductile shear failure or plug failure of spot welds modelled by modified Gurson model. Engineering
478 Fracture Mechanics 77 (7), 1031 – 1047. <https://doi.org/10.1016/j.engfracmech.2010.02.031>

479 Porcaro, R., Hanssen, A., Langseth, M., Aalberg, A., 2006. The behaviour of a self-piercing riveted connection under quasi-static loading
480 conditions. International Journal of Solids and Structures 43 (17), 5110 – 5131. <https://doi.org/10.1016/j.ijsolstr.2005.10.006>

481 Sabuwala, T., Linzell, D., Krauthammer, T., 2005. Finite element analysis of steel beam to column connections subjected to blast loads.
482 International Journal of Impact Engineering 31 (7), 861 – 876. <https://doi.org/10.1016/j.ijimpeng.2004.04.013>

483 Skovron, J., Mears, L., Ulutan, D., Detwiler, D., Paolini, D., Baeumler, B., Claus, L., 09 2014. Characterization of Flow Drill Screwdriving
484 Process Parameters on Joint Quality. SAE Int. J. Mater. Manf. 8, 35–44. <https://doi.org/10.4271/2014-01-2241>

485 Skovron, J. D., Prasad, R. R., Ulutan, D., Mears, L., Detwiler, D., Paolini, D., Baeumler, B., Claus, L., 2015. Effect of Thermal Assistance on
486 the Joint Quality of Al6063-T5A During Flow Drill Screwdriving. Journal of Manufacturing Science and Engineering 137 (5), 051019.
487 <https://doi.org/10.1115/1.4031242>

488 Sønstabø, J. K., Holmstrøm, P. H., 2013. Behaviour and modelling of self-piercing screw and self-piercing rivet connections: An experimental
489 and numerical investigation. Master's thesis, Institutt for konstruksjonsteknikk, Norwegian University of Science and Technology (NTNU).

490 Sønstabø, J. K., Holmstrøm, P. H., Morin, D., Langseth, M., 2015. Macroscopic strength and failure properties of flow-drill screw connections.
491 Journal of Materials Processing Technology 222, 1 – 12. <https://doi.org/10.1016/j.jmatprotec.2015.02.031>

492 Sønstabø, J. K., Morin, D., Langseth, M., 2016. Macroscopic modelling of flow-drill screw connections in thin-walled aluminium structures.
493 Thin-Walled Structures 105, 185 – 206. <https://doi.org/10.1016/j.tws.2016.04.013>

494 Szlosarek, R., Karall, T., Enzinger, N., Hahne, C., Meyer, N., 2013. Mechanical testing of flow drill screw joints between fibre-reinforced
495 plastics and metals. Materials Testing 55 (10), 737–742. <https://doi.org/10.3139/120.110495>