# A Two-dimensional Study of Green-Water Loading 

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## 0

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Ai miei genitori, aura del mio cammino (To my parents)

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## Abstract

Large relative motions between the ship and the water may cause water shipping on the main deck. In this thesis, the fundamental features of water-on-deck phenomena are in vestigated, together with the "green" water loading on a deck house in the bow region. The studies are relevant for a stationary ship like a FSO in head sea waves.

P otetial flow theory is used to study $n$ umerically a nonlinear two-dimensional problem in a plane containing the ship's centerplane. The developed model is verified byvarious test cases, and v alidated by published as well as new experimental data.

The influence of waveparameters, ship motions and hull geometry is inv estigated. Relevance of three-dimensional effects is discussed.

Dedicated two-dimensional model tests have been performed, both to elucidate the fluid mechanics in volv edin the water shipping and to validate the n umerical method. It is found that the water shipping starts in the form of a plunging wa ve hitting the deck. This could cause structural damages. Most often, the plunging is localized in the bow region and do not affect the main flow at a later stage. In a few cases, larger masses of water bluntly impacting with the deck hav e been observed. The latter is consistent with seldom observations reported in 3-D experiments, with large and steep wa ves plunging directly onto the deck. More often the water flow along the deck resembles the one subsequent to a dam breaking. Both types of ev en tsare in vestigated mmerically. The impact pressures on a vertical wall in the bow area are measured and compare well with the boundary element method.

The reliability of a dam-breaking model and shallow-water approximation to study the propagation of water on the deck is examined. The former can only qualitatively describe the flow ev olution. The latter can in principle be used but needs information from the exterior flow and, thus, the solution of the complete ship-waveinteraction problem.

Water impacts with a deck house in the bow area are studied in details. Use of a similarity solution for a water wedge hitting a rigid wall at $90^{\circ}$ is compared with the fully numerical solution. The method predicts correctly the first stages of the impact with a smaller computational effort. Influence of local flow conditions and wall slope on hydrodynamic loads is discussed. Importance of $h$ ydroelasticity is in vestigatedin case of realistic structural parameters for the deck house. This shows a limited role of structural deformations in determining the maximum loads.

## Nomenclature

## General Rules

- Only the most used symbols are listed in the following sections
- Meaning of symbols is giv erat least when introduced in the thesis
- Sometimes the same symbol is used to indicate different things
- Vectors are represented byin troducing a right arrow above the symbols


## Subscripts

| ca v | Cavity |
| :--- | :--- |
| db | Dam breaking |
| imp | Impact |
| in | Initial |
| max | Maximum |
| shw | Shallow |
| sto | Stokes |
| ver | Vertical |
| wet | Wetted |
| wod | Water on deck |

## Roman Letters

A Amplitude of heav e motion
$d_{s} \quad$ Horizontal distance of superstructure from the bow
$D \quad$ Ship draft
$E \quad$ Youngs modulus

| EI | Beam bending stiffness |
| :--- | :--- |
| $f$ | F reeboard |
| $F_{x}$ | Horizontal force |
| $\vec{g}$ | Gravitational acceleration |
| $h$ | Height of water reservoir. Water depth |
| $h_{w}$ | Water level along the deck |
| $H$ | Incoming wa veheight |
| $I$ | Beam cross-sectional area moment of inertia per unit width about neutral axis |
| $k_{\theta}$ | Spring constant |
| $l_{\text {cav }}$ | Cavity length |
| $L$ | Ship length |
| $L_{\text {beam }}$ | Beam length |
| $m$ | Beam structural mass perunitlength and unit width |
| $\vec{n}$ | normal unit vector |
| $p$ | Pressure |
| $p_{a}$ | Atmospheric pressure |
| $P_{\text {max }}$ | Maximum pressure |
| $Q$ | Volume of shipped water |
| $Q_{0}$ | Number characterizing amount of water of the incident wa ves, defined |
|  | as water v olume abovethe mean free surface ov erone wa elength |
| $r$ | Radius |
| $R$ | Maximum vertical run-up |
| $R_{j}$ | J-th natural wetted-period to j-th natural dry-period ratio |
| $t$ | Time |
| $t_{\text {imp }}$ | Time of initial water impact |
| $t_{\text {wod }}$ | Time when water ondec k starts |
| $t_{\text {last }}$ | Time of zero water flux onto the deck |
| $T$ | Incoming waveperiod |
| $T_{j \text { dry }}$ | J-thbeam natural dry-period |
| $T_{j w}$ | J-thbeam natural wetted-period |
| $\vec{u}$ | Fluid velocity |
| $u$ | Horizontal velocity component. Velocity magnitude |
| $v$ | Vertical velocity component |
| $V$ | Impact velocity |
| $w$ | Beam deformation |
| $x$ | Horizontal axis |
| $x_{\text {shw }}$ | Distance from the bow from where shallow water theory is applicable |
| $z$ | Vertical axis |

## Greek Letters

$\alpha \quad$ Stem angle. Superstructure inclination
$\beta \quad$ Semi-angle of fluid wedge

| $\Delta$ | Difference between two quantities |
| :--- | :--- |
| $\zeta_{j}$ | Amplitude of j-theigeamode |
| $\eta$ | Free surfaceelevation |
| $\eta_{\text {sto }}$ | Stokes wa v eelevation |
| $\lambda$ | Incoming wa velength |
| $\sigma_{\max }$ | Maximum stress |
| $\varphi$ | Velocity potential |
| $\varphi_{\text {sto }}$ | Stokes wa vev elocity potential |
| $\rho$ | Water density |
| $\psi_{j}$ | J-th beam eigenmode |
| $\tau$ | Non-dimensional time |
| $\omega$ | Wavefrequency $(\mathrm{rad} / \mathrm{s})$ |

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## Chapter 1

## Introduction

### 1.1 Green-Water Loads

In rough-sea conditions, both moored and/or dynamically positioned vessels and ships in transit can suffer shipping of water on the deck. This phenomenon can occur everywhere along the hull and it is a consequence of freeboard magnitude and large relative motions between the ship and the water. The picture in figure 1.1 shows an incident occurred to the tanker Golar Siri in the


Figure 1.1 The tanker Golar Siri meets the hurricane "Judy", 1963 (photo by Per Meidel).
h urricane" Judy" in 1963. The water shipping, from the captain's view, appears dramatic: the water enters the deck non-uniformly along the fore part of the ship, and the worst conditions are concentrated at the front of the bow. Here, the water surface is very steep, and in the form
of a wall of water high relative to the ship dimensions. The consequence is a compact mass of water flowing overthe deck (" green" water, "heavy" wetness). Head-sea wavesrepresent a common sea condition in bad weather. This implies that the more severe situations are normally localized in the bow region of the ship, as in the shown incident. When a sufficient amount of water comes onto the deck, a flow with increasing velocity develops, possibly hitting obstacles on its way. Water impacting against the deck and superstructures may cause both high pressures in confined regions and contribute to global ship loads.

Several water-on-deck casualties have also been documented for smaller ships, such as fishing vessels (cf. Storch 1978). A main concern is roll stability. During water on deck, loads distribution along the vessel changes. Large lateral motions can follow and be responsible of ship capsizing. The ship instability is mainly caused by a critical reduction of $\overline{\mathrm{GM}}$ due to the mass of shipped water and consequent free surface area. Howev er, vater sloshing on the deck can also matter.

In this context, water on deck is critical for loaded vessels due to the smaller mean ship freeboard. An increase of forward ship velocity can either be positive or negative for the vessel safety, depending on the ship conditions. F orinstance, in Grochowalski (1989) it was observed that for fishing vessels the increase of forward speed supports the ship capsizing in unloaded conditions. Conv ersely, a greater speed appeared beneficial for a loaded vessel, and in particular counteracted the occurrence of water shipping.

F orward speed is a relevant factor also for larger vessels, influencing mean sinkage and trim and ship motions. Moreover, the steady wavepattern decreases the freeboard in the bow and increases the probability of deck wetness from the ship sides. Higher forward velocities can more easily lead to "light" wetness ("white" water). The latter means a large amount of spray during the water shipping. This can be a danger for the visibility on board and consequently affect deck operations.

### 1.1.1 Framework and Scope of the Present Analysis

The work reported in this thesis concerns water-on-deck phenomena for Floating Production Storage and Offloading (FPSO) units. These represent a relatively new concept of oil platforms, where a floating unit (see left plot in figure 1.2) is used for production, storage and offloading operations. This concept has been adopted in different parts of the world (see right map in figure 1.2). In practice, a FPSO is a ship. It is less expensive than traditional platforms. FPSOs are supposed to be weather-vaning, i.e. that head sea is the most-occurring weather condition. Dynamic positioning may be used to assist the station-keeping. Clearly, the seakeeping properties of a stationary ship are quite different from ships with forward speed. In this context, many factors have to be accounted for, such as wave-frequency motions, station-keping and mean and slow drift motions induced by current, wind and second order wa ve-body itteractions. Examples of important sea loads to consider in a structural analysis are bow stem slamming, green water loads, and global induced bending moments and shear forces.

Water on deck is now considered an important risk for this type of ship, and started to be a factor in defining operational strategies and ship design. Green-water accidents documented both deck wetnesses in the bow region and from the ship sides, with damages for deck house and equipments. The location of the deck house can vary .FPSOs working in the Nortiea usually


Figure 1.2 Left: concept of a FPSO unit. Right: map of the FPSO operations.
have the deck house in the bow region. FPSOs operating in South America have the deck house near the stern.

The occurred water-on-deck casualties in North Sea motivated experimental in vestigations and suggested some modifications of design rules and operational restrictions. An overviewof the most important accidents and of the subsequent requirements of the Norwegian Petroleum Directorate are given b y Ersdal and Kvitrud (2000).

On the above ground, the present work is focused on green-water phenomena occurring in the bow region. These do not cover all the possible netness features, but the most severe even ts may


Figure 1.3 Dam breaking-type water on deck. Left: captain view from 3-D experiments (Marintek, 2000). Right: sketch of the phenomenon from side view.
occur in head-sea conditions. In this case, after the water exceeds the freeboard, two scenarios can take place:
(i) More commonly, the water flows along the deck and resembles the flow generated after the breaking of a dam (see figure 1.3, MARINTEK 2000).
(ii) Occasionally, large breaking wav es plunge directly on the dek house (see figure 1.4, MARINTEK 2000). This even thas been detected in recent model experiments (MARINTEK 2000) and appears typically more severe and dangerous than the type (i).


Figure 1.4 Plunging wave-type water on deck. Left: captain view from 3-D experiments (Marintek, 2000). Right: sketch of the phenomenon from side view.

As we will see later, also type (i) starts in the form of a plunging wavehitting the deck, near the bow. Howev er, this initial phase is localized in time and space relative to the scale of the water shipping itself.

Many physical aspects determine and affect the water-on-deck phenomenon. Wa ve-ship interactions (cf. figure 1.5.A) modify significantly the wavepattern with respect to that of the incident waves. This is related both to local effects and to wavereflection, which in rough sea


Figure 1.5 Some physical aspects involved in the water-on-deck phenomenon: w a -body interaction (A), body motions (B), three-dimensional effects (C).
are highly nonlinear phenomena. Ship motions (figure 1.5.B) can either enhance or prevent the deck-wetness occurrence. Three-dimensional effects are relevant (figure 1.5.C) though less than for cases with forward speed. These factors make it difficult to clearly identify the design parameters relevant for occurrence and severity of water on deck, and for its consequences on the ship.

Obviously the ship freeboard is important. However the effect of other parameters characterizing the ship-bow geometry is far from being clarified. Sometimes, it is not ev enclear whether they enhance or reduce the deck wetness. As an example, O'Dea and Walden's (1984) experiments in regular waves and with forvard speed showed that larger bow flare angles reduce the deck wetness, while Lloyd et al. (1985) experiments in irregular wa ves and with forward speed observed more frequent freeboard exceedances and deck wetness with more heavily flared bows. Newton's (1960) experiments in regular wavesand with forward speed documented that increase of flare, obtained by in troducing a knuckle without changing the actual freeboard, is equally effective, as increasing the latter, in counteracting water shipping. The bow bulb is usu-
ally considered non relevant for the waveinduced body motions. However a bulb may increase the fluid velocities in the bow region and steepen the local waves. This would support deck wetness. On this ground, inv estigations of fundamental type are requested to or ercome this ladk of knowledge and to develop $n$ umerical tools of practical use.

Finally, the present analysis deals mainly with local loads in the deck area. Howev er, global effects in terms of, for instance, midship bending moment should be inv estigated. This may not be dominant (cf. Wang et al. 1998). In this context, the relative phasing between green-water loads and the maximum values of the bending moment is crucial.

### 1.1.2 Historical Developments

Extensive experimental studies of deck wetness have been carried out in the past. Some of the most important ones will be briefly described.
Ships with forward speed. Regular head-sea wav es have been used by Newton (1960) to study the influence of freeboard and flare on deck wetness. A basic model geometry has been varied to identify the relative role of each parameter. Same en vironmental conditions characterized the model tests by O'Dea and Walden (1984). Here a model of a frigate has been altered in the above-water bow shape. Then, absolute and relative motion near the bow and deck wetness were measured. An analysis of these quantities as a function of freeboard, flare and knuckles was carried out. Lloyd et al. (1985) performed experiments in irregular sea states. A frigate model was systematically varied to investigatethe influence of freeboard, flare, stem overhang and stem sharpness. The results were presented in terms of bow wa ve high $t$, frequency of freeboard exceedance, impact frequency and swell-up coefficient.
FPSO units. Buchner (1995) reported head-sea regular wavemodel tests. Relation between relative slip motions and deck wetness was inv estigated, as well as behavior of the green water along the deck and water-impact phenomena with superstructures.

All mentioned studies are relevant for understanding the phenomenon. Howev er, they are not conclusive and giv ein some cases contradictory results in terms of parameter influence. Alternative approximated analyses have also been developed and used to predict green-water loading. In this context experimental observations play ed a fundamental role.

The conv en tionalway of estimating water-on-deck occurrence in a short-term sea state is to combine a probabilistic analysis (cf. Ochi 1964) with a linear hydrodynamic analysis. It implies that the above-vater h ull form is not included in the h ydrodynamic analysis. The important $h$ ydrodynamic variable is the linear relative vertical motion between the ship and the water. Often only the incident waveand not the local waveaccounting for the presence of the ship is used in this context. An effective freeboard is sometimes in troduced for a ship with forward speed. This accounts empirically for the steady wav eprofile and the sinkage of the ship.

In the previous stochastic analysis, the hydrodynamic phenomenon is treated as a black-box. F or a real improvement of the design strategies, the stochastic analysis has to be combined with a h ydrodynamic analysis. In the framework of the potential flow theory, a fully-nonlinear analysis was carried out by Maruo and Song (1994). There, the water-shipping phenomenon of high-speed vessels was analyzed by using $2 \frac{1}{2}$-D Slender-Body Theory. This method may also have relevance for slender-ship bows at moderate forward speed. Buchner and Cozijn (1997) analyzed the bow deck wetness for moored ships, assuming a two-dimensional problem in the
longitudinal ship direction. They presented both numerical simulations and experiments for a simple prototype problem, but no comparisons between simulations and measurements have been shown.

In case of dam breaking-type water on deck, some authors studied the motion of the shipped water along the deck by using shallow-water models. The reliability of this type of approach is dependent on how the initial conditions as well as the inflow boundary conditions are determined. A sensitivity analysis in terms of the inflow velocities was carried out in Mizogushi (1989) by comparing n umerical results and experimental data for the S-175 container ship. The shallowwater equations have been solved for the three-dimensional problem, using experimental results for the water height at the inflow boundary. In the simulation, the ship motion is not taken into account. The author concluded that the flow interactions (between flow on the deck and flow outside the ship) and the efflux occurring between the deck area and the outer region represent important items in the water-on-deck phenomena.

Wan and Wu (1999) studied the water on deck for a moored ship in shallow water due to solitary wa ves. Three-dimensional effects hav e been neglected and the problem was solved with the Volume-of-Fluid method (VOF). The adopted solver was, in principle, a Navier-Stokes solver but apparently the used resolution was not enough to capture viscous effects at the body boundary and at the free surface. Results hav e been presented in terms of velocity field, wav eprofile and pressure evolution along the deck house. The authors stressed some numerical difficulties in ev aluating thelatter quantity. Two main issues have been pointed out: (i) importance of small time steps in the simulation to properly capture rapid pressure changes during the impact, and (ii) limitations of the used first-order pressure differential scheme. No discussion was presented about the importance of the boundary layer developing near the deck during the water shipping. In particular in terms of reduction of the water front velocity relative to the inviscid case. The same method was applied by F ekkn et al. (1999) for studying the three-dimensional flow of water along the deck. This was made by considering an equivalent dam-breaking problem. Comparisons with 3-D experiments of water on deck on a FPSO weresho wn for the water front contours and for the pressure evolution along superstructures with different shapes (flat vertical wall, wedged vertical wall, cylindrical vertical wall). Numerical and experimental water fronts showed clear differences though with a certain global similarity. Numerical and experimental ev olutions of the pressureand total loads were in reasonable agreement, both in magnitude and time duration, in the case of flat vertical superstructure. The agreement in magnitude was not satisfactory for the other studied geometries.

Specific studies of the later water flows along the deck can explain many phenomena and giv esome important suggestion for an improved ship stability. This is relevant for smaller vessels. Much research effort has been spent for this topic. Dillingham (1981) analyzed the phenomenon of interest by solving numerically the two-dimensional shallow-water flow with the Glimm's method (Glimm 1965), that can efficiently capture jump phenomena (discontinuity of some variable of in terest). According to the author, this approach should be suitable for this kind of physical problems where the flow can be characterized by quite steep waves møing back and forth between the lateral barriers. In Dillingham (1981) beam-sea conditions were assumed as incident wavesystem and the linear strip theory by Salvesen et al. (1970) was used to evaluate the h ydrodynamic coefficients. The vessel was considered as a two-degrees-of-freedom system in sway and roll and the rigid-body motions were coupled with the water sloshing on the
deck. The flow of water onto or off the deck was evaluated in a simplified way, by comparing the instantaneous body configuration and the undisturbed incoming waves. Glimm's method was extended to nonlinear three-dimensional water flows onto the deck by Pantazopoulos (1987) and by Dillingham and Falzarano (1988). In both cases, coupling of the water sloshing with the body motions, and on deck-off deck flows of water, are not accounted for. A qualitative study of the water-on-deck effect on response and stability of the vessel is carried out in P artazopoulos (1987) by using simple energy and stability principles. Some numerical shortcomings of the Glimm's method motivated the development of more robust and accurate methodologies (see e.g. Huang and Hsiung 1996).

### 1.2 Present Work

Wa ve-body in teraction, shipping, subsequent flowing of water onto the deck and impact with superstructures, are strongly coupled stages of the problem. Localized structural damages as well as excitation of global response of the ship may occur. The importance of hydroelasticity during water impacts with superstructures needs to be assessed. The main objective of present work is to gain a better understanding of this complicated picture and give answers to some of the related question marks.

Our in vestigationis centered on the deck wetness at the bow region of a FPSO in head-sea. Therefore, forward-speed effects are not investigated. The phenomenon is further idealized by considering the two-dimensional flow in the longitudinal plane of the ship. The resulting problem is studied both numerically and experimentally .In the former case, a fully-nonlinear unsteady problem is solved byassuming inviscid fluid dynamics.

### 1.2.1 Structure of the Thesis

The prototype two-dimensional problem, representative of a FPSO in head-sea conditions, is stated in the next chapter, while the numerical procedure is given and discussed in chapter 3. The obtained formulation is applied to study the water-on-deck phenomenon due to regular incoming wa ves. The influence of main waveand ship parameters on the occurrence and characteristics of water shipping is analyzed in chapter 4.

Water impact with superstructures along the deck is then considered by using a dam breakingflow as initial condition for the shipped water flow. The resulting problem is numerically solved and discussed. The obtained results are compared with analytical solutions and experimental data. A parametric analysis for the impact phenomenon is also carried out in terms of local water details at the impact instant, wall slope and hydroelastieha vior of the structure.

After n umerical solutions of the "exact" problem hav e been obtained, in chapter 6 simplified methods for the water flow along the deck are discussed and judged. In particular, the shallowwater theory and the dam-breaking model are considered, and their advantages and shortcomings are pointed out.

Two-dimensional water-on-deck experiments performed at the Dept. of Marine Hydrodynamics of NTNU are described in chapter 7. The experimental set-up is discussed, and possible error
sources in the tests are indicated.
The main physical aspects of the initial stages of water shipping and its late evolution are discussed in chapter 8 , where experimental data and $n$ umerical results are used in a combined way to gain a deeper understanding of the basic physics. In the same chapter, a simplified water-on-deck analysis in terms of incoming waveparameters and ship-stem overhangis also carried out.

Significant information gained from this study is summarized in chapter 9. Some suggestions for future work are also outlined.

### 1.2.2 Major Findings

As stated, the present analysis is limited to the shipping of water in the bow region of a $\mathbb{P S O}$ in head-sea conditions, and without forward-speed. A simplified two-dimensional problem is considered and in vestigatedby n umerics and a dedicated experimental activity. The major findings of present study are summarized as follo ws.
Global features of water shipping Occurrence of plunging of large wa ves on the deck (cf. figure 1.4) seems to be related to the interaction of steep wavesalready prone to break, more than to the wa ve-body in teraction byitself. However, the influence of severe ship motions can not be excluded.

F rom our model experiments, we discov ered that the dam breaking-type water on deck starts also as a plunging wave hitting the dek. This phase is rather spatially confined around the bow and takes place in a short time relative to the whole water-shipping event, and may cause local damages in the deck. T oour knowledge, this phenomenon has not been reported before.
Deck wetness analysis. The effect of the main parameters causing and affecting the shipping of water are analyzed numerically. The steepness of incident wavesresults to be the main wave parameter. Stem ov erhang reduces the relative amount ofshippent ater, though less efficiently than the freeboard. A trim angle (a quasi-steady pitch angle) has a small effect on the amount of shipped water. The influence of normal type of bulb is limited.
Impact with the deck house. The impact of shipped water against a deck house in the bow area is inv estigated by quasi-two dimensional experiments and by n umerics. F ordam breakingtype water on deck, the numerical wavefront has a wedge form. This is also observed in the experiments, with the exception of the rather small tip region, where the free surface meets the deck and the front is rounded because of viscous and surface tension effects. This small detail is not important for structural loads, as confirmed by the agreement between n umerics and experiments. Also, in the first stages of the impact, gravit y does not matter.

In particular, it is shown that the water front velocity $V$ and the angle $\beta$ between the free surface and the deck at the impact instant, characterizing the wedge-shaped front, are the main water-impact parameters. F or $\beta<\sim 40^{\circ}, V$ represents the dominant parameter.

The stem overhangreduces the water level along the deck, but increases the in voled flow velocities. Due to this, it is hard to find a conclusive statement about its positive or negative effects on water impacts with a superstructure.

A trim angle (a quasi-steady pitch angle) has a small influence on the water impact with the deck house. A reduced inclination of the impacted wall reduces the loads during the run-up of water along the structure. When an angle $\alpha=40^{\circ}$ (relative to the vertical direction) is
considered, the maximum normal force becomes $\sim 50 \%$ of the maximum normal force in the case of vertical wall. In the analyzed range of angles, the force reduction seems almost linear with $\alpha$.

It is shown that the effect of hydroelasticity man in general be neglected.
Simplified methods for the water flows on the deck. A theoretical dam-breaking model gives only a qualitative description of the flow features, and should be considered only in a preliminary study. In fact, the actual waveconditions determining the water shipping are not properly described. Therefore, ambiguities exist when choosing the height of the "equivalent" reservoir of water and the time instant when the dam breaks. Moreover, in principle shallowwater approximations are appropriate and accurate in certain domains along the deck. However, in practice, they would need data that are unav ailable without solving the complete ship-wave in teraction problem.

As an example, among the simplified approaches, Ritter's model (cf. Ritter 1892) would lead to too conservative estimates of impact loads on a deck house in the bow area. F orthe dambreaking problem, with an initial reservoir of height $h$, this solution would predict a constant water front velocity $V=2 \sqrt{g h}, g$ being the gravity acceleration. Actually, the "exact" dambreaking solution shows an initially zero velocity, increasing as the water front ev olv es. The ev olution of the ratio $V / 2 \sqrt{g h}$ is giv enin figure 1.6 as a function of the distance $x$ co veredby the water, and is smaller than one for $x \leq 3 h$. Thus the shallow-water solution over-estimates


Figure 1.6 Evolution of the water-froth velocit $y V$ along the deck due to the breaking of a dam with height $h . g$ is the gravit y acceleration. The solid line shows the numerical solution of the "exact" problem. The value $V / 2 \sqrt{g h}=1$ results from the approximate Ritter's shallow-water method.
the impact velocity if the superstructure is located at $x \leq 3 h$ from the dam. Since $h$ is a measure of the freeboard exceedance during the water shipping, and it is large for significant water-on-deck events, $x \leq 3 h$ is a reasonable condition in practical cases.

The impact phenomenon is not handled by the shallow water approximation and requires the combination with suitable local solutions, such as a similarity solution. Actually, the water front predicted by the shallow water solution is not wedge shaped, but, neglecting the detail of the tip, the wave profile at the front is well env eloped by a wedge, and a comparison is still possible. In general both $V$ and $\beta$ must be considered to estimate, for instance, the maximum pressure along the wall. Howev er, if $\beta$ is smaller than $\sim 40^{\circ}$, which occurs for $x>\sim 0.65 h$ in the "exact" problem, $V$ is the main parameter and the squared ratio $(V / 2 \sqrt{g h})^{2}$ can be interpreted as ratio
between "exact" and shallow-water maximum pressures.

## Chapter 2

## Mathematical Model

In the follo wing, the wave-shipinteraction in the bow region of a FPSO is idealized in the form of a two-dimensional problem. The general physical assumptions are discussed and the corresponding mathematical problem is stated. The model is described in detail in case of a rigid body. The fluid-structure coupling to account for h ydroelastic effects during impact is discussed in the final section.

### 2.1 General Assumptions

As already discussed, the present analysis is limited to the case of a ship in head-sea conditions with zero forward speed. This is the rather common case of a FPSO unit, which is typically characterized bya blunt bow.

In this framework, the problem is idealized b y considering the two-dimensional flow in the longitudinal plane of the ship. In reality, the neglected three-dimensional effects are relevant, though less than for the case with non-zero forward speed. In the latter situation, additional sources of three-dimensionality come from the interaction with the steady and unsteady wave patterns. In fact, when the ship advances the freeboard along the vessel is more non-uniform because of the steady wav epattern and it is generally reduced with respect to the zeroforw ard speed case, at least in the bow region. The forward speed will also influence mean sinkage and trim of the ship. Finally, the run-up at the bow of ambient wa ves is generally larger in case of an advancing body.
In spite of the above limitations, a two-dimensional analysis gives important insights of the water-on-deck phenomenon, and useful information about the role of the many parameters in volv ed.

In practical cases, the Reynolds number of the flow is high. Therefore, for unseparated flows, the vorticity is concentrated in the thin boundary lay er at thebody boundary, and a potentialflow model can be used to describe quantitatively the main features of the flow field, including the wa ve evolution around the hull and the induced pressure distribution. Boundary lay er effects may be relevant also in case of thin fluid lay ers on solid boundaries, as in case of the water front
propagating on the deck. Moreover, the edge of the ship deck may induce separation and large vortex shedding. In present analysis, such phenomena are not modeled a priori.
In general, surface-tension effects are negligible because of the relatively large spatial scales in rolv edin practical cases. Howev er, high curvature of the free surface may exist at the bodyfree surface in tersection and in plunging waves. There surface tension may be relevant.
Finally, unless otherwise stated, structural elastic deformations are not considered and the body is assumed perfectly rigid.

With these premises, a potential flow model is adopted and the "heavy" water-on-deck is analyzed by fully retaining the nonlinearities associated with body and free-surface motions. This physical model is applied to solve sev eraltwo-dimensional prototype problems, related to the topic of our in terest. The objectives are (i) to verify and validate the method by comparisons with published analytical, numerical and experimental results, and (ii) to gain a physical and quantitative understanding of the water-on-deck phenomenon and of the role of the many parameters affecting it.
In the next section, the mathematical formulation is described in a general way. Problemdependent variables and treatments are detailed in the sections where specific cases are studied.

### 2.2 Statement of the Mathematical Problem

A two-dimensional problem (cf. figure 2.1) is studied, where the fluid domain, $\Omega(t)$, is bounded by thfree surface $\partial \Omega_{F S}$, thew etted surface of a rigid body $\partial \Omega_{B O}$, and a control surface $\partial \Omega_{\infty}$.


Figure 2.1 Sk etch of the o-dimensional problem of inerest.
In general, the boundary $\partial \Omega$ varies with time because of

- free-surface motion
- pressure distribution along $\partial \Omega_{F S}$
- rigid-body motions at $\partial \Omega_{B O}$
- non-zero or prescribed fluid motion at portions of the control surface $\partial \Omega_{\infty}$

These disturbances propagate through the fluid, in particular causing loads on the body and motions, if the body is not restrained to move.

We assume the fluid to be incompressible, inviscid, and in irrotational motion. A potentialflow model is therefore applicable. The velocity potential $\varphi(\vec{P}, t)$, defined as $\vec{u}=\nabla \varphi$ where $\vec{u}$ is the fluid velocity, satisfies the Laplace equation

$$
\begin{equation*}
\nabla^{2} \varphi=0 \tag{2.1}
\end{equation*}
$$

ev erywherein the fluid domain.

Kinematic condition at boundaries Fluid particles cannot cross the portion $\partial \Omega-\partial \Omega_{\infty}$ of the domain boundary, therefore

$$
\begin{equation*}
\frac{\partial \varphi}{\partial n}=\vec{V}_{\left(\partial \Omega-\partial \Omega_{\infty}\right)} \cdot \vec{n} \quad \forall t, \forall \vec{P} \in \partial \Omega-\partial \Omega_{\infty} \tag{2.2}
\end{equation*}
$$

where $\vec{n}$ is the unit normal vector to the surface assumed pointing out of the fluid domain. In equation (2.2) $\vec{V}_{\left(\partial \Omega-\partial \Omega_{\infty}\right)}$ is the velocity associated with a geometric point along the surface, and a separate discussion is needed for the body boundary and for the free surface.

Body boundary The velocity onthe instantaneous wetted surface of the body is

$$
\begin{equation*}
\vec{V}_{P}=\vec{V}_{G}+\vec{\omega} \times \overrightarrow{G P} . \tag{2.3}
\end{equation*}
$$

Here $G$ is the center of mass of the structure, $\vec{V}_{G}$ is the translatory velocity of $G$ and $\vec{\omega}$ is the angular velocity of the rigid body. In case of captive body motions, $\vec{V}_{P}$ is a priori known. In case of a floating structure, $\vec{V}_{P}$ has to be determined b y solving the equations of body motion, coupled with the fluid dynamic problem through the pressure

$$
\begin{equation*}
p=p_{e}-\rho\left(\frac{\partial \varphi}{\partial t}+\frac{1}{2}|\nabla \varphi|^{2}+g z\right) \tag{2.4}
\end{equation*}
$$

acting along the wetted surface $\partial \Omega_{B O}{ }^{1}$. More precisely, the pressure acting along $\partial \Omega_{B O}$ gives the h ydrodynamic force $\vec{F}$ and moment $\vec{M}_{G}$ about $G$

$$
\begin{align*}
& \vec{F}=\int_{\partial \Omega_{B O}} p \vec{n} \mathrm{~d} \ell  \tag{2.5}\\
& \vec{M}_{G}=\int_{\partial \Omega_{B O}} p \overrightarrow{G P} \times \vec{n} \mathrm{~d} \ell
\end{align*}
$$

which depend on the body position, on the rigid body velocity and acceleration and are in general a function of the previous time history of the fluid motion. The hydrodynamic loads enter explicitly into the equations of body motion which therefore have to be solved simultaneously with the fluid dynamic problem. In practice, we may hav eto account also for viscous loads due to current, wind and viscous damping of the body motions. Mooring and/or thruster forces have to be considered in a station-keeping analysis.

[^0]Conditions at the free surface The free surface configuration, $\partial \Omega_{F S}$, is in general unknown and the kinematic condition given above has to be complemented by a dynamic condition. Upon neglecting surface tension effects, the free-surface dynamic condition enforces the pressure to be continuous across $\partial \Omega_{F S}$ :

$$
\begin{equation*}
p=p_{e}(\vec{P}, t) \quad \forall t, \forall \vec{P} \in \partial \Omega_{F S} \tag{2.6}
\end{equation*}
$$

F orthe cases of in terest $p_{e}$ coincides with the atmospheric pressure, $p_{a}$, which is set equal to zero. Through the Bernoulli equation (2.4) and by using a Lagrangian description (the motion of the fluid particles is followed), we can write the free-surface conditions as

$$
\left\{\begin{array}{l}
\frac{D \vec{P}}{D t}=\nabla \varphi  \tag{2.7}\\
\frac{D \varphi}{D t}=\frac{1}{2}|\nabla \varphi|^{2}-g \eta-\frac{1}{\rho} p_{e}
\end{array} \quad \forall t, \forall \vec{P} \in \partial \Omega_{F S}\right.
$$

where $\eta$ is the waveelevation. Equations (2.7) are well known and simply state that the free surface is made by fluid particles moving with the fluid velocity $\nabla \varphi$ and carrying a value of the potential $\varphi$ which evolv es according to the second equation. Consistently, $D / D t=\partial / \partial t+\nabla \varphi \cdot \nabla$ is the standard total, or material, derivative. Finally, it is worth to mention that the first equation of (2.7) is consistent with the kinematic condition (2.2).

Conditions at control surfaces The geometry and location ofie control surface $\partial \Omega_{\infty}$ are a priori known, and for the problems of interest are time independent. In the case of a ship in a region of water with depth $h$ this surface can bemade $y$ two vertical barriers, upstream and downstream the body, and bythe portion of the bottom between them. Along the bottom the velocity potential is unknown, while its normal derivative is zero due to the impermeability of the surface.

On the lateral portions both $\varphi$ and $\partial \varphi / \partial n$ would be in general unknown. Howev er, simplified assumptions can be made if these surfaces are chosen far enough from the body. In fact, let us assume the two-dimensional initial value problem is characterized by an impulsive pressure acting on the free surface. In this case, for a finite time $t$ asymptotically zero motion is felt at great distance from the initial disturbance (Mei 1983). This implies that the velocity potential is asymptotically zero as the distance from the disturbance goes to infinity. This argument can be applied to the present problem since the body disturbance may be described as a distributed pressure disturbance along the free surface. Actually, the disturbances expected in the present case are weaker than in the impulsive problem referred to above. Therefore, a faster decaying asymptotic behavior of the velocity potential is expected.

In a finite interval of time, the leading disturbances due to the body remain spatially confined, and become practically negligible beyond a suitable large horizontal distance, sa y $d$, from the body. This implies a small error when setting them equal to zero from $d$ on. Clearly, the distance $d$ increases with time as radiated or reflected waves propagate outwards, and, in numerical computations, one should use a large domain compared with the considered time scale for the in troduced errors to be small. This could represent a severe difficulty in terms of computational costs. T olimit the horizontal extension of the fluid domain the free-surface conditions are
modified to damp out outgoing waves and to preent unphysical reflections. The use of damping lay ersat the edges of the computational domain is described in the next chapter.

F romthe above discussion, the lateral portions of $\partial \Omega_{\infty}$ are placed at a suitable distance $d$, and $\varphi$ and $\partial \varphi / \partial n$ are prescribed. In particular, at the downstream barrier both functions are assumed to be zero. The same treatment would be used at the upstream barrier in case of a radiation problem, while, for the case of head-sea incident wa ves, the solution is analytically prescribed consistently with the desired waves.

F or deep-vater conditions, we assume the horizontal portion of the control surface at a depth large enough to neglect its influence. This implies both $\partial \varphi / \partial n$ and $\varphi$ are zero. Strictly speaking, nonlinear interactions among wave componets can give rise to a slow decay of the potential and, in particular, the asymptotic value of the potential is non-zero (while $\nabla \varphi \rightarrow 0$ ). This behaviour can have a special importance in case of microseism, as discussed by Longuett-Higgins (1953). Despite this special case, in the present work we use also $\varphi=0$ alonghe horizontal portion of the control surface without influencing the solution ohe considered problem.

A different treatment of the boundary $\partial \Omega_{\infty}$ is adopted for the simulation of a physical wave flume, shown in section 3.2.2, where the wavemaler and the bottom of the channel have to be modeled. The treatment is more conventional, with the velocity component normal to such boundaries a priori known. In the specific case, due to the presence of the wavemakr, $\partial \Omega_{\infty}$ is time dependent.

### 2.3 Modeling of the Hydroelastic Problem

T oa certain extent, all structures deform under the action of fluid loads. In many cases, structural deformations are not relevant to determine the fluid flow and the problem can be treated as that of a perfectly rigid body. In other circumstances, the motion of the body boundary due to elastic deformations takes place on spatial scales and frequencies suitable to significantly influence the fluid motion. In this context it is fundamental that the time scale of the considered fluid motion (loading time) is comparable with structural elastic natural periods. When this occurs, the fluid dynamic problem and the structural problem are coupled and have to be simultaneously solved (h ydroelastic problem).

In the present context, when the shipped water hits structures along the deck, elastic deformations may have a certain importance and may influence the flow conditions. T oassess the role of hydroelasticity, analyzed in chapter 5, we need to formulate a hydroelastic model. In particular, within the present two-dimensional analysis, the fluid-structure interaction is studied by coupling the nonlinear potential flow model with a linear Euler beatro represen $t$ a portion of the deck house under the action of the shipped water.
The use of a rather simple structural model makes the analysis rather faster and easier. For a more realistic treatment, one should use a more complicated structural model. However main focus is to assess the importance of hydroelasticity for a stiffened flat steel panel, and the beam model represents a satisfactory approximation for the considered structure. Small beam deformations are assumed and, consistently with the Euler beam model, rotations of the beam sections are neglected. Finally, structural damping is assumed negligible.

Let us consider a Cartesian frame of reference $(\chi, \xi)$, with the $\xi$-axis along the undeformed
beam (see sk etc h2.2). The transverse deformation $w(\xi, t)$ of the beam is approximated as

$$
\begin{equation*}
w(\xi, t) \simeq \sum_{j=1}^{N} \zeta_{j}(t) \psi_{j}(\xi) \tag{2.8}
\end{equation*}
$$

with $N<\infty$. Here $\psi_{j}(\xi)$ is the $j$-th dry mode of the beam and $\zeta_{j}(t)$ its amplitude. The former can be analytically determined according to the specific boundary conditions at the beam ends,


Figure 2.2 Sk etch of the o-dimensional problem of itherest.
$\xi=0$ and $\xi=L_{\text {beam }}, L_{\text {beam }}$ being the beam length. The modal amplitudes are the unknowns of the problem.

The algorithm used for solving the described problem is the following. At a given instant of time, the beam geometry, $w$, and the deformation velocity, $\partial w / \partial t$, are known and the boundaryvalue problentlfer potential $\varphi$ can besolv ed byimposing the impermeability condition

$$
\frac{\partial \varphi}{\partial n}=\frac{\partial w}{\partial t}
$$

along the instantaneous wetted portion of the beam. It is worth to stress that in the fluiddynamic computations, in spite of the linearized structural model, the beam is deformed according to $w(\xi, t)$.

The rate of change of the potential, $\partial \varphi / \partial t$, is also needed to ev aluate the hydrodynamic pressure ( $c f$. equation (2.4)) forcing the beam to deform (see equation (2.11) below). Since $\partial \varphi / \partial t$ is a harmonic function, it can be found by solving a suitable boundary-value problem for the Laplace equation $\nabla^{2}[\partial \varphi / \partial t]=0$. The boundary conditions on the free and rigid boundaries follo w from the Bernoulli equation and from the no-penetration boundary condition, respectiely. A boundary condition on the instantaneous wetted portion of the beam is also requested, having
the less common form of a non-homogeneous Robin condition:

$$
\begin{equation*}
\frac{\partial^{2} \varphi}{\partial t \partial n}=-\frac{\rho}{m} \frac{\partial \varphi}{\partial t}+b_{1}+b_{2} \tag{2.9}
\end{equation*}
$$

Here $\rho$ is the water density, $m$ the structural mass per unit length and unit width of the beam and $b_{1}$ and $b_{2}$ are known functions of the longitudinal coordinate $\xi$. Equation (2.9) follows by inserting the condition for $\partial^{2} \varphi / \partial t \partial n(c f$. T anizava 1999)

$$
\begin{equation*}
\frac{\partial^{2} \varphi}{\partial t \partial n}=\frac{\partial^{2} w}{\partial t^{2}}-k\left(\frac{\partial w}{\partial t}\right)^{2}-\frac{\partial}{\partial n}\left(\frac{1}{2}|\nabla \varphi|^{2}\right) \tag{2.10}
\end{equation*}
$$

in to the beam equation

$$
\begin{align*}
m \frac{\partial^{2} w}{\partial t^{2}}+\mathrm{EI} \frac{\partial^{4} w}{\partial \xi^{4}} & =p\left(w, \frac{\partial w}{\partial t}, \frac{\partial^{2} w}{\partial t^{2}}\right)  \tag{2.11}\\
& =-\rho\left(\frac{1}{2}|\nabla \varphi|^{2}+\frac{\partial \varphi}{\partial t}-\vec{g} \cdot \vec{P}\right)
\end{align*}
$$

In condition (2.10), $k=\left|\partial^{2} w / \partial \xi^{2}\right| /\left[1+(\partial w / \partial \xi)^{2}\right]^{3 / 2}$ is the local curvature of the beam. In equation (2.11) $\vec{g}$ is the gravity acceleration, $\vec{P}$ represents a generic point $(\chi, \xi)$ of the deformed beam and EI is the beam bending stiffness, where $E$ is the Youngs modulus and $I$ the area moment of inertia per unit width of the beam about the neutral axis. Therefore, $b_{1}$ and $b_{2}$ are given by

$$
\left\{\begin{array}{l}
b_{1}=-k\left(\frac{\partial w}{\partial t}\right)^{2}-\frac{\partial}{\partial n}\left(\frac{1}{2}|\nabla \varphi|^{2}\right)  \tag{2.12}\\
b_{2}=-\frac{1}{m}\left(\mathrm{EI} \frac{\partial^{4} w}{\partial \xi^{4}}+\rho \frac{1}{2}|\nabla \varphi|^{2}-\rho \vec{g} \cdot \vec{P}\right)
\end{array} .\right.
$$

F rom the assumption of small structural deformations the local curvature $k$ can be approximated as $\sim\left|\partial^{2} w / \partial \xi^{2}\right|$. This term is multiplied by $(\partial w / \partial t)^{2}$ in $(2.10)$ thus the resulting contribution is $\mathcal{O}\left(|w|^{3}\right)$ and can be neglected consistently with the assumption of linear beam.
Once $\partial \varphi / \partial t$ is known, $\partial^{2} w / \partial^{2} t$ can be ev aluated and fluid motion and structural deformation can be updated in time. A procedure, similar to the one discussed above, has been in troduced in T anizava (1999) to analyze the impact ©fllexible body with the free surface.

Similarly to the case of rigid-body motions, the right-hand-side of equation (2.11) depends also on terms proportional to the acceleration. This may lead to numerical instabilities in the time integration.

## Chapter 3

## Numerical Solution

In the follo wing, a n umerical procedure to solve the mathematical problem stated in the previous chapter is described. The adopted algorithm, presented in section 3.1, is the well known Mixed Eulerian-Lagrangian method, where the problem is split into a two-step procedure: the ev aluation of the velocity field ("kinetic problem" or "Eulerian step"), and a time-evolution problem (the "Lagrangian step"). Motivations and limits related to the present implementation are discussed. Practical details of the $n$ umerical procedure are reported in appendix A.

### 3.1 Solution Algorithm

As discussed in the previous chapter, the two-dimensional free-surface flow around a surfacepiercing body is studied within the frameworkof in viscid irrotational fluid mechanics.
In this context, a possible strategy to numerically solve the problem consists in the following procedure.

0 Let us assume that, at a given instant of time $t_{0}$, the boundary geometry $\partial \Omega$ is known together with the potential along the free surface, and the component of the velocity normal to impermeable boundaries.

1 A boundary value problem (b.v.p.) for the Laplace equation can be stated as:

$$
\left\{\begin{array}{l}
\nabla^{2} \varphi=0  \tag{3.1}\\
\varphi \text { giv en on } \partial \Omega_{\mathcal{D}} \\
\frac{\partial \varphi}{\partial n} \text { given on } \partial \Omega_{\mathcal{N}}
\end{array} .\right.
$$

In general, the Dirichlet boundary $\partial \Omega_{\mathcal{D}}$ and the Neumann boundary $\partial \Omega_{\mathcal{N}}$ are only a subset of the domain boundary, since along some parts of $\partial \Omega$ both $\varphi$ and its normal derivative are known.

By solving the b.v.p. (3.1), we determine the fluid velocity, and (3.1) can be referred to as the "kinetic problem". This is also said to be the "Eulerian step" of the procedure because the problem (3.1) is solved for a frozen configuration of the flow field.
As we will discuss, at this stage the term $\partial \varphi / \partial t$, necessary for the pressure evaluation, can also be calculated.

2 The kinematic and dynamic conditions giving, respectively, the evolution of the free-surface geometry and of the free-surface potential can be stepped forward in time. If a Lagrangian formulation for the free surface is used this step can be properly defined as the "Lagrangian step" of the procedure.
The pressure along the instantaneous wetted surface of the body can be evaluated and the body motions, if not restrained, can be calculated.
This provides new values for the boundary data along the Dirichlet and the Neumann boundaries, and the procedure can be repeated from Step 1 above.
The described solution strategy was elaborated in Ogilvie (1967), but was introduced into practical n umerical calculations by Longuett-Higgins and Cokelet (1976) and by F altinsen (1977), independently. F orthe specific considered cases, the portion $\partial \Omega_{\infty}$ of the boundary can be of Dirichlet type, Neumann type, or can be a boundary where the boundary data are en tirely specified.

### 3.1.1 Kinetic Problem

In the present approach, the kinetic problem

$$
\begin{cases}\nabla^{2} \varphi=0 & \forall \vec{P} \in \Omega  \tag{3.2}\\ \varphi=f(\vec{P}) & \forall \vec{P} \in \partial \Omega_{\mathcal{D}} \\ \frac{\partial \varphi}{\partial n}=g(\vec{P}) & \forall \vec{P} \in \partial \Omega_{\mathcal{N}}\end{cases}
$$

is recast in terms of boundary-integral equations, and solved bya boundary-element method (BEM).
F eatures and drawbacks of using boundary-integral equations for free-surface flows have been discussed at length by many authors (see e.g. Yeung 1982). Here, we only mention that the simplicity of handling highly distorted configurations such those appearing during water shipping, formation of plunging waves, and impact against structures gies a decisive advantage over discretization-field methods, where a gid co vering the whole fluid domain is required ${ }^{1}$.

[^1]T oderive suitable integral equations, we consider the Green's second identity

$$
\begin{equation*}
c(\vec{P}) \varphi(\vec{P})=\int_{\partial \Omega}\left(\varphi \frac{\partial G}{\partial n_{Q}}-\frac{\partial \varphi}{\partial n_{Q}} G\right) \mathrm{d} \ell_{Q} . \tag{3.3}
\end{equation*}
$$

Here

$$
c(\vec{P})= \begin{cases}2 \pi & \vec{P} \in \Omega  \tag{3.4}\\ 0 & \vec{P} \notin \Omega \cup \partial \Omega \\ \theta & \vec{P} \in \partial \Omega\end{cases}
$$

In (3.3), $\vec{Q}$ is a point along the domain boundary, $\vec{n}_{Q}$ is the unit normal vector along the boundary pointing out of the fluid domain (see figure 2.1), and

$$
\begin{equation*}
G(\vec{P}, \vec{Q})=\ln (R) \quad R=|\vec{P}-\vec{Q}| \tag{3.5}
\end{equation*}
$$

is the two-dimensional free-space Green function. Finally, $\theta$ is the inner angle (relative to the fluid domain) at point $\vec{P}$ along the boundary.

The in tegral representation (3.3) gives the velocity potential within the fluid domain, once $\varphi$ and $\partial \varphi / \partial n$ are known along the boundary. Conv ersely, for points $\vec{P}$ on the boundary, (3.3) gives a compatibility condition on the boundary data. In particular, if only some of them are known we can write in tegral equations to determine the remaining unknown boundary data. More specifically, for points belonging to Dirichlet and Neumann boundaries, respectively, we have

$$
\begin{align*}
-\int_{\partial \Omega_{\mathcal{D}}} \frac{\partial \varphi}{\partial n_{Q}} G \mathrm{~d} \ell_{Q}+\int_{\partial \Omega_{\mathcal{N}}} \varphi \frac{\partial G}{\partial n_{Q}} \mathrm{~d} \ell_{Q} & =\mathcal{T}_{\mathcal{D}} & \vec{P} \in \partial \Omega_{\mathcal{D}}  \tag{3.6}\\
-\int_{\partial \Omega_{\mathcal{D}}} \frac{\partial \varphi}{\partial n_{Q}} G \mathrm{~d} \ell_{Q}-c \varphi(\vec{P})+\int_{\partial \Omega_{\mathcal{N}}} \varphi \frac{\partial G}{\partial n_{Q}} \mathrm{~d} \ell_{Q} & =\mathcal{T}_{\mathcal{N}} & \vec{P} \in \partial \Omega_{\mathcal{N}}
\end{align*}
$$

The functions in the right-hand-sides are

$$
\begin{array}{ll}
\mathcal{T}_{\mathcal{D}}=c f(\vec{P})-\int_{\partial \Omega_{\mathcal{D}}} f(\vec{Q}) \frac{\partial G}{\partial n_{Q}} \mathrm{~d} \ell_{Q} & +\int_{\partial \Omega_{\mathcal{N}}} g(\vec{Q}) G \mathrm{~d} \ell_{Q}  \tag{3.7}\\
\mathcal{T}_{\mathcal{N}}= & -\int_{\partial \Omega_{\mathcal{D}}} f(\vec{Q}) \frac{\partial G}{\partial n_{Q}} \mathrm{~d} \ell_{Q}
\end{array}+\int_{\partial \Omega_{\mathcal{N}}} g(\vec{Q}) G \mathrm{~d} \ell_{Q}, ~ l
$$

In this work, the in tegral equations (3.6) are solved bya panel method with piecewise-linear shape functions both for geometry and for boundary data. This was preferred to higher-order schemes (e.g. Landrini et al. 1999) which may lead to n umerical difficulties at the body-free surface intersection point. Clearly, a lower-order method requires a finer discretization in regions with high curvature of the boundary. In particular, it is important to satisfy conservation of fluid mass. Therefore, an accurate tracking of the free boundary is crucial in areas with high free-surface curvature. During the simulation, this has been ac hieved byinserting dynamically new points where appropriate.

In the present implementation of the method, the collocation points are placed at the edges of each element. This results in a smoother distribution of the velocity potential along the free
surface with respect to piecewise constant panel methods. Continuit y of the velocity potential is assumed at those points where the free surface meets a solid boundary. Though no rigorous justification is available, this procedure gives conv ergence of the numerical results under grid refinement (cf. Dommermuth and Yue 1987). Occasionally, when the contact angle becomes too small, numerical problems still may occur and the jet-like flow created during a water-entry phase is partially cut ( $c f$. Zhao and F altinsen 1993).

The discretization procedure by the boundary element method is well known, and we give just few details. The boundaries $\partial \Omega_{\mathcal{D}}$ and $\partial \Omega_{\mathcal{N}}$ are divided into $N_{\mathcal{D}}$ and $N_{\mathcal{N}}$ elements, respectively, and the discretization of the contour integrals in (3.6-3.7) leads to the system of linear algebraic equations

$$
\left[\begin{array}{cc}
A_{i j} & B_{i j}  \tag{3.8}\\
C_{i j} & D_{i j}
\end{array}\right]\left\{\begin{array}{c}
\frac{\partial \varphi}{\partial n} \mathcal{D}_{j} \\
\varphi_{\mathcal{N} j}
\end{array}\right\}=\left\{\begin{array}{l}
f_{i} \\
g_{i}
\end{array}\right\}
$$

where the unknown vector $\left\{\partial \varphi /\left.\left.\partial n\right|_{\mathcal{D}} \quad \varphi\right|_{\mathcal{N}}\right\}^{T}$ has $N=N_{\mathcal{D}}+N_{\mathcal{N}}$ components.
We remark that in a fully-nonlinear simulation, the right-hand-side of (3.8), as well as the matrix coefficients on the left-hand-side, have to be evaluated each time the geometry and the boundary data change.
Once the system (3.8) has been solved, $\varphi$ and its normal derivative become availablealong the whole boundary. Differently, the tangential velocity $\partial \varphi / \partial \tau$ along $\partial \Omega$ is determined by using finite-difference operators. The two velocity components are then used for the Lagrangian tracking of the free surface, as described in section 3.1.3.

### 3.1.2 Evaluation of $\partial \varphi / \partial t$

The evaluation of the pressure along the body-wetted surface, $\partial \Omega_{B O}$, requires the rate-of-change $\partial \varphi / \partial t$ of the velocity potential. Howev er, with moving boundaries (e.g. the free surface, or the body boundary when motions are not restrained), the Eulerian derivative $\partial \varphi(\vec{P}, t) / \partial t$ is not even defined because the point $\vec{P}$ on the considered boundary is changing in time. Therefore, some practical difficulties are expected.

Rigid body motions Cointe (1989b) observed that $\partial \varphi / \partial t$ is solution of the Laplace equation with a Dirichlet condition on the free surface and Neumann condition on the body boundary. The latter requires high-order derivatives of the fluid velocity along the body. The problem is formally equivalent to the kinetic problem discussed above and the computation of $\partial \varphi / \partial t$ by BEM does not change significantly the computational effort.

In a different approach, the time derivative following the rigid body motion is introduced

$$
\begin{equation*}
\frac{D_{B O} \varphi}{D t}=\frac{\partial \varphi}{\partial t}+\vec{V}_{P} \cdot \nabla \varphi, \tag{3.9}
\end{equation*}
$$

with $\vec{V}_{P}$ giv enb y equation (2.3). The left-hand side can be ev aluatedeven by umerical differen tiation, andthe $\partial \varphi / \partial t$ is obtained by subtracting the transfer term $\vec{V}_{P} \cdot \nabla \varphi$.

In this work, we we the property that the function $\psi(\vec{P}, t)=\partial \varphi / \partial t+\vec{V}_{P} \cdot \nabla \varphi$ is a harmonic function that satisfies a boundary value problem formally identical to the problem (3.1) for the
velocity potential $\varphi$ (see appendix B). In this case, the body Neumann condition is simpler to evaluate than in the Cointe's approach. By using the boundary-element method already described, we obtain a system of linear algebraic equations with the same matrix as in case of $\varphi$ and no additional computational effort is requested. In fact, at each time instant we can factorize once and for all the common matrix, and perform two back-substitutions for the $\varphi$ and for the $D_{B O} \varphi / D t$ problem, respectively.

Hydroelastic problem In this case $\partial \varphi / \partial t$ is determined bysolving æac $h$ time instant the b.v.p. described in section 2.3. Due to the Robin boundary condition along the beam wetted length, the latter is not formally the same as the problem for the velocity potential. As a result, in the discrete form, the matrix associated with the system to solve is different and additional CPU-time is needed.

### 3.1.3 Time Integration

A standard fourth-order Runge-Kutta scheme is adopted to step forward in time the ev olution equations associated with the problem. This method represents a good compromise between accuracy and computational costs. Its stability limits usually are not very sev ere.In particular, in a linear stability analysis we can show that the scheme becomes unstable only by using very large time step $\Delta t$, which is never adopted because the tracking of the fast physical dynamics of water shipping limits more severely the choice of the time step. Finally, the method is slightly dissipative. The dissipation rate decreases as the time step decreases, and for the global time scales here analyzed (of the order of few periods of the incoming wa ve) this is negligible.

The scheme is well known. Let us consider equations of the form $\partial y / \partial t=f(\vec{P}, t)$, where $y$ is the variable of interest and $f(\vec{P}, t)$ is a known function of space and time. This gives

$$
y^{n+1}=y^{n}+\frac{1}{6} k_{1}+\frac{1}{3} k_{2}+\frac{1}{3} k_{3}+\frac{1}{6} k_{4}
$$

with

$$
\left\{\begin{array}{l}
k_{1}=\Delta t f\left(t^{n}, y^{n}\right) \\
k_{2}=\Delta t f\left(t^{n}+\frac{1}{2} \Delta t, y^{n}+\frac{1}{2} k_{1}\right) \\
k_{3}=\Delta t f\left(t^{n}+\frac{1}{2} \Delta t, y^{n}+\frac{1}{2} k_{2}\right) \\
k_{4}=\Delta t f\left(t^{n}+\Delta t, y^{n}+k_{3}\right)
\end{array}\right.
$$

This scheme requires the solution of four kinetic problems for each physical time interval due to the introduced (fictitious) auxiliary time instants. F or a linearized problem, this procedure vould be equivalent to a fourth-order Taylor expansion in time with an error of $\mathcal{O}\left(\Delta t^{5}\right)$. Though less demanding schemes are conceivable, we adopted the described scheme becausef the simplicit y in c hanging dynamically the time step. This was found crucial to keep under control the accuracy of the solution during the development of jet flows, impacts, and breaking waves.

### 3.2 Generation of Incoming Waves

The incident wavesare far from being regularin the real case. This means they are associated with a certain spectrum of energy distributed along a continuous range of frequencies. Despite this fact, in this work regular incoming wa veshave been considered because it is simpler to link waveparameters, such as wavelength $\lambda$ and waveheight $H$, with occurrence andev erit y of the phenomenon. Present study is useful when specified design conditions are analyzed. In this case the regular waveconditions can be applied to describe the sea state of interest. However one must note that the n umerical method described in this work can also be applied in the case of a more general type of incoming wav esystem.

In an ideally unbounded domain, regular incident wavesare permanent in shape, namely the wa ve profile remains undianged in a frame of reference moving with the phase velocity. The latter is not only a function of the wavenumber $k=2 \pi / \lambda$ but also of the wavesteepness $k a$, a being the waveamplitude, so that the different Fouriercomponents of the waveare phase bounded with each other. P ermanert waveforms have been analytically discovered by Stokes. They may be generated experimentally but it has been prov ed by Benjamin and Feir (1967), for deep water, and by Benjamin (1967), for arbitrary water depth, that Stokes wavescan be unstable when perturbed. Benjamin and F eirdiscov ered theoretically the instability by considering the problem of a periodic wave train, with frequency $\omega$, perturbed by side-band frequencies $\omega(1 \pm \delta)$. This gave that Stokes waves where $k h<1.363$, are stable. Here $h$ is the water depth. Differently, those propagating in sufficiently deep water, so that $k h>1.363$, can be unstable. In particular this occurs when the condition of instability

$$
\begin{equation*}
0<\delta<k a \sqrt{2 \frac{X(k h)}{Y(k h)}}=\delta_{c} \tag{3.10}
\end{equation*}
$$

is satisfied. Here $X$ and $Y$ are two known functions of $k h$. Condition (3.10) implies that, for unstable growth, the side-band frequencies need to be sufficiently close to the fundamental frequency. The asymptotic growth of the side-band amplitudes is

$$
\sim \exp \left\{\frac{1}{2} \delta \sqrt{Y\left(2 k^{2} a^{2} X-\delta^{2} Y\right)} \omega t\right\} \quad \text { as } \quad t \rightarrow \infty
$$

This has a maximum value for $\delta=\delta_{c} / \sqrt{2}$. The growth rate of the Benjamin and Feir instability decreases as the steepness of the carrier decreases. In addition to these longitudinal instabilities, Stokes wavesare also subjected to cross-wise instabilities (cf. McLean et al. 1981).
In this work, the incoming wavesare generated in t wo alternative ways:

1. Stokes wavesare analytically prescribed at the upstream barrier of $\partial \Omega_{\infty}$, or
2. a wa ve flume is numerically simulated and the upstream barrier is replaced by a wavemakr. The first strategy is used both in deep water and finite water depth and it is used to carry out the parametric analysis in terms of the deck wetness, as described in chapter 4, and in general in the conducted studies of water-on-deck phenomena.
The second approach has been applied for finite water depth to reproduce the experiments carried out at NTNU, discussed in chapter 8.

### 3.2.1 Use of the Analytical Incident-Wa ve Solution

The vertical downstream portion of the surface $\partial \Omega_{\infty}$ is chosen far enough from the body to giv enegligible contributions in terms of disturbances generated by wa ve-body interactions (cf. section 2.2). Along the vertical upstream barrier, both $\varphi$ and $\partial \varphi / \partial n$ are specified bya truncated F ourierrepresentation of the Stokes wav efor arbitrary steepness (Bryant 1983, see also Rienecker and Fenton 1981 for finite water depth). The horizontal location of this barrier is chosen far enough (order of ten wav elengths) from the body so that within the time scale of the simulation (at most the order of ten wave periods) disturbances due to ve reflection are small in proximity of the inflow boundary. F or deep vater problems its vertical extent is truncated at a suitable large depth, and the contribution from the horizontal bottom boundary is neglected. No approximations are in troduced in case of finite water depth, and the no-penetration boundary condition is enforced on the bottom.

Semi-analytical solutions of the two-dimensional problem of nonlinear gravity wavescan be derived by using perturbation expansion in terms of a small parameter $\epsilon$ inv olv ed in the problem. In this way the nonlinear solution is expressed as a power series $\sum \epsilon^{i} \varphi_{i}$, where each term $\varphi_{i}$ is the solution of a linear mathematical problem. For water waves,this approach has beeim troduced by Stokes, who chose as small parameter the amplitude $a_{1}$ of the first harmonic in the F ourier expansion of the wa ve elevation. Later on it was proved by Sch wartz (1974) that the conv ergence of the related power series is not ensured for each value of $a_{1}$ and that a more suitable parameter is the wav esteepness $\epsilon=2 \pi a / \lambda$.

F or deepwater, the solution of the problem

$$
\begin{array}{ll}
\nabla^{2} \varphi=0 & \forall z<\varepsilon \eta(x, t) \\
\frac{\partial \varphi}{\partial x}, \frac{\partial \varphi}{\partial z} \rightarrow 0, & \forall z \rightarrow-\infty \\
\begin{cases}\frac{\partial \eta}{\partial t}-\frac{\partial \varphi}{\partial z}+\varepsilon \nabla \eta \cdot \nabla \varphi=0 & \forall z=\varepsilon \eta(x, t) \\
\eta+\frac{\partial \varphi}{\partial t}+\frac{1}{2} \varepsilon|\nabla \varphi|^{2}=0 & \end{cases} \tag{3.11}
\end{array}
$$

has been obtained follo wing Bryant (1983). An earth-fixed frame of reference is assumed, with the $z$-axis parallel and opposite to the gravity acceleration $\vec{g}, z=0$ corresponds to mean water level. The equations of the problem and the solution are given in terms of the non-dimensional v ariables:

$$
\left\{\begin{array}{rl}
(x, z, \eta)_{\operatorname{dim}} & =(x, z, \eta) \frac{\lambda}{2 \pi} \\
t_{\operatorname{dim}} & =t \sqrt{\frac{\lambda}{2 \pi g}} \\
\varphi_{\operatorname{dim}} & =\varphi a \sqrt{\frac{g \lambda}{2 \pi}}
\end{array} .\right.
$$

In the n umerical method the solution of the problem is expressed in terms of truncated F ourier
series for the wav eelevation and the velocity potential,

$$
\left\{\begin{array}{l}
\eta=\sum_{k=1}^{N} a_{k} \cos [k(x-c t)]  \tag{3.12}\\
\varphi=\sum_{k=1}^{N} b_{k} e^{k z} \sin [k(x-c t)]
\end{array}\right.
$$

Here, the phase velocity $c$ depends on the steepness $\epsilon$, and the number $N$ of harmonic components results from the computation so that the approximate solution satisfies the nonlinear problem within an accuracy $\delta$ decided $a b$ initio. This means that the contribution of the first harmonic neglected is smaller than $\delta$. When expressions (3.12) are substituted intothe problem (3.11), a Newton-Raphson method can beapplied to determine $c$ and the amplitudes $a_{k}$ and $b_{k}$ with the specified error.

F or finite vater depth, sa y when the depth $h$ is less than $\frac{1}{2} \lambda$, the problem (3.11) is modified by the impermeability condition along the bottom, and the solution procedure adopted, here not described, can be found in Fen ton(1988).

### 3.2.2 Wa vemaker

A water region with finite depth $h$ is considered. The boundary surface $\partial \Omega_{\infty}$ is formed bya straight vertical downstream portion (upstanam portion (3) con taining the instantaneous wetted surface of the wavemakr and a straight horizontal portion between them (2), see figure 3.1. As discussed in section 2.2, the portion (1) is a control surface taken far enough from the


Figure 3.1 Flap wavemaler: sketch of the numerical tw o-dimensional problem.
body so that both the velocity potential and its normal derivative can be set equal to zero along it. The remaining two parts of $\partial \Omega_{\infty}$ are physical boundaries, where the impermeability condition applies, and $\varphi$ follo wsfrom the solution of the integral equations (3.6). In the studied cases, the geometry of the upstream boundary reproduces that of the physical waveflume at NTNU, where a flap wavemakr is hinged at a distance $z_{r}$ from the bottom (the portion underneath is vertical and fixed). The motion of the wavemaker can be freely prescribed to produce different kind of waves. In particular, for the purpose of comparison with experiments, the motion of the wa vemaker is directly defined byusing the recorded motion of the physical waveflume.

### 3.3 Modeling of the Flow Field during Water Shipping

A crucial aspect of the water-on-deck problem is represented bythe prediction of the shipping occurrence. Also, the behaviour of the fluid flow during the initial stage, when freeboard is exceeded, represents a physical interesting and still rather unclear stage of the whole even $t$. Therefore, n umerical modeling hasto rely upon experimental observations in the hope to grasp correctly the physics.


Figure 3.2 Left: "initial" Kutta-like condition at the edge of the deck. Right: "contin uous" Kutta-like condition at the edge of the deck.
"Initial" Kutta-like condition At tle beginning of the present work, the quasi-two dimensional experiments reported in Cozijn (1995) has been used as a guidance. F rom thesestudies, after the freeboard is exceeded and in case of water shipping, it resulted that the fluid flows tangentially along the deck, resembling the fluid motion after a dam breaking.

On this ground, we devised a first modeling of the flow at the edge of the deck, which is sk ethed in the left plot of figure 3.2. In particular, the fluid is allowed to leave tangentially the bow when water reaches the instantaneous freeboard. After this initial event, once the freeboard is exceeded, the fluid velocity relative to the ship determines whether the deck will be wetted or the water will be diverted in the opposite direction. In the first case, the fluid particle closest to the deck is allo ved to move tangentially along it.
We verified a posteriori that this treatment allows a good prediction of water-on-deck occurrence, and of the subsequent evolution of the flow field along the deck.
"Continuous" Kutta-like condition Two-dimensional experiments performed in a small waveflume at the Hydrodynamics Department of NTNU, highlighted the local behavior of the water during the first stage of the shipping. In particular, it has been observed that the beginning of water shipping initiates in the form of a wave crest plunging orto the deck. In most observations, the spatial scale in volved is small (compared with the ship draft), as well as the time scale for the impact to occur. After that the flow field evolves according to the "usual" description of dam breaking-type water-on-deck. Our experimental observations will be better discussed in chapter 8, and for the present purpose the above description suffices to justify a second treatment we devised for the flow at the bow edge. This is drawn in the right plot of figure 3.2, and consists in enforcing the fluid to leav etangentially the bow contin uously during the whole evolution. We named this treatment "continuous" Kutta-like condition.

This description turned out to be quite successful in describing the formation of the wa ve plunging onto the deck, although the numerical simulation breaks down when the free surface hits the solid boundary. A description of the following impact flow is possible, for example by matching with a local high-spodadion, although it has not been presently attempted.

As we already stressed, after the initial impact, the long-time evolution of the flow field follows the better known dam breaking-type water-on-deck (cf. chapter 1). Therefore, phenomena occurring on a larger time scale than the initial plunging breaking wavecan be studied by applying the initial Kutta-like condition, while we limited the use of the continuous Kutta-like condition to describe the initial water impact with the deck.

### 3.4 Absorbing Boundary Conditions

We will study water-on-deck induced by head-sea regular waves, with either incident wa ves analytically prescribed or generated bya given motion of a wavemakr. In the formerase, the distance $d$ of the vertical portions of the control surface $\partial \Omega_{\infty}$ from the body can not be taken arbitrarily large due to obvious limitations of memory requirements and computational time. Therefore, disturbances radiated by, as well as transmitted and reflected wa ves due to the body may reach the edges of the computational domain within a time-scale smaller than that needed bythe simulation. This can cause unphysical reflections, and hamper the results.

T oprevent this problem, damping lay ers are used in proximity of the lateral boundaries of the computational domain to damp out progressively the outgoing wavemotion. In practice this is obtained by modifying the free-surface conditions. This represents a pragmatic solution, apparently without any assumption that the flow is linear or nonlinear (cf. Ohkusu 1996). In this way, although the waveevolution is altered along the damping region, the solution is not modified within the inner computational domain where the "physical" free-surface conditions are used. Many wa ys exist for applying a damping region: apparently, Israeli and Orszag (1989) in troduced the idea in a general framenork, probably Cointe (1989a) was the first to apply it for studying wave-body irteractions. Further Clément (1996) pointed out the need of complementing the damping lay erwith piston-like conditions to increase the effectiveness in the low-frequency regime.

Both the free-surface conditions are modified in the present work. In particular, close to the barrier downstream of the body, the dynamic condition in (2.7) is altered byintroducing a damping term proportional to $\varphi$, namely

$$
\begin{equation*}
\frac{D \varphi}{D t}=\frac{1}{2}|\vec{u}|^{2}-g \eta-\nu(\vec{P}) \varphi \quad \forall t, \forall \vec{P} \in \partial \Omega_{F S} \tag{3.13}
\end{equation*}
$$

A damping term proportional to the free surface elevation $\eta$ is introduced in the kinematic condition

$$
\begin{equation*}
\frac{D \vec{P}}{D t}=\nabla \varphi-\nu(\vec{P}) \eta \vec{e}_{z} \quad \forall t, \forall \vec{P} \in \partial \Omega_{F S} \tag{3.14}
\end{equation*}
$$

where $\vec{e}_{z}$ is the unit vector along $z$-axis. Some stretching of the panels is used to obtain a large reduction of the low-frequency components (cf. Cao et al. 1993).

The treatment of the upstream edge of the computational domain is slightly modified because of the generation of incoming Stokes waves. In facts, in this case the damping terms are proportionalthe perturbation variables $\left(\varphi-\varphi_{\text {sto }}\right)$ and $\left(\eta-\eta_{\text {sto }}\right)$, respectively. Here $\varphi_{\text {sto }}$ and $\eta_{\text {sto }}$ are the velocity poten tial and wav eelevation $\delta$ the unperturbed Stokes wave,respectively. F or thedamping coefficient $\nu(\vec{P})$, we adopted the following expression

$$
\nu(\vec{P})= \begin{cases}0 & \forall \vec{P} \in \partial \Omega_{F S}-\mathcal{L}  \tag{3.15}\\ \nu_{\max }\left(-2 \xi^{3}+3 \xi^{2}\right) & \forall \vec{P} \in \mathcal{L}_{1} \\ \nu_{\max } & \forall \vec{P} \in \mathcal{L}_{2}\end{cases}
$$

where

$$
\xi=\frac{d-d_{0}}{\operatorname{meas}\left(\mathcal{L}_{1}\right)} .
$$

Here, $d$ is the horizontal distance from the body of a generic point $\vec{P} \in \partial \Omega_{F S}, d_{0}$ is the horizontal distance from the body where the damping region begins and meas $\left(\mathcal{L}_{1}\right)$ is the length dimension of $\mathcal{L}_{1}$. Thus, the numerical "beach" $\mathcal{L}=\mathcal{L}_{1} \cup \mathcal{L}_{2}$ is made by a first portion $\mathcal{L}_{1}$, where the damping coefficient increases smoothly as a cubic function of the distance from $d_{0}$, reaching a maximum value $\nu_{\max }$ (see sketch 3.3). The latter represents the constant value of $\nu$ in the second


Figure 3.3 Sk etchof the numerical damping region. The horizontal distances are compressed with respect to those adopted in actual computations.
portion $\mathcal{L}_{2}$. Clearly, $\nu$ is zero for points $\vec{P}$ outside the n umerical beach, where the free-surface conditions reduce to the original ones.

The length of the n umerical beach, as well as the value of $\nu_{\max }$, have to be empirically determined. In this work, meas $\left(\mathcal{L}_{1}\right)$ has been chosen at least equal to twice the incoming wave length $\lambda$, while $\operatorname{meas}\left(\mathcal{L}_{2}\right)$ could be muc hlarger, in particular in the downstream region, to damp out low-frequency components. In fact, analogously to the physical case, the shorter the wavelength is relative to $\mathcal{L}$, the more efficiently the wave motion is damped out. It is worth to mention that for green-water loading long wavescompared with the ship draft are of in terest. This requires a suitable "design" of the computational domain and of the duration of the simulation to balance the computational effort with the quality of the results needed.

The damping term $\nu_{\max }$, which has the same dimensions as frequency, was c hosen in the form

$$
\begin{equation*}
\frac{\nu_{\max }}{\sqrt{g k}}=\frac{1}{\sqrt{2 \pi}} \sqrt{\frac{\lambda}{D}} \tag{3.16}
\end{equation*}
$$

where $k$ is the wa ve number and $D$ the ship draft. This choice is based on empirical studies conducted by Greco (1997). This procedure worked efficiently for the considered cases, as confirmed $b y$ the good agreement of the numerical simulations with experimental data, reported later.

The Lagrangian drift of surface points is eliminated through periodic regridding of the upstream region. In varianceof the results have been checked byincreasing the upstream length of the domain. The reproduction of exact Stokes waveconditions hav e been check ed inside the domain $\Omega$ in absence of the body.

Finally, in case of the numerical simulation of the NTNU wa ve flume we did not use damping layer in proximity of the wavemaker. In facts, in the physical waveflume an automatic control system adjusts thew avemaker motion to absorb reflected wa ves and to ensure the desired wave conditions. We used the actual wavemakr motion during the experiments to drive our numerical wavemakr and absorption of reflected wavesfrom the ship to the same degree as in the experiments is expected also in the simulations.

## Chapter 4

## Water on Deck

In this chapter the water-on-deck phenomenon is analyzed. A parametric analysis of the water shipping is carried out b yv arying incoming wavesand main ship parameters. The influence of body motions on the amount of shipped water and on the occurrence of the plunging wave-t ype water on deck (see section 1.1) is also discussed.

### 4.1 General Remarks

Water-on-deck is a complex phenomenon. Roughly speaking, we may distinguish three different stages: i) the run-up of the water at the bow, ii) the water shipping onto the deck, iii) the subsequent flow developing along the deck. In practical cases, also iv) the impact with ship equipments or deck house can be observed.
When the waveelevation exceeds the freeboard, two main scenarios have been observed:
Type I: the water-on-deck is characterized bya large waveplunging directly against the deck house or equipments. We will refer to this ev en tas "plunging wa ee-type water on deck".

Type II: the mass of water above the deck level flows along the deck and resembles the flow field after a dam breaking. In the following, we will refer to this scenario as "dam breaking-type water on deck".

In principle, although less commonly observed, the Type I water-on-deck is more dangerous for ship structures than the Type II because of the more violent impact wf ater.

Two-dimensional water-on-deck experiments performed at the Department of Marine Hydrodynamics of NTNU revealed that also the Type II water-on-deck starts in the form of a plunging breaker hitting the deck. These observations are extensively described in chapter 8, and here we simply anticipate that the observed phenomenon takes place in small time and space scales relative to those of the water shipping itself. Probably, because of its localized character and
therefore of the difficulties to detect it, this plunging-wavephase has not been documented in previous two-dimensional experiments reported in Cozijn (1995), discussed in the following section. In any ev ent, after this initial stage, the water shipping has been observed to develop in the Type II form, i.e. as a dadoreaking-t ype water on deck.

As anticipated in the previous chapter, comparisons with experiments have shown that smallscale details of the flow at the bow are properly modeled and recovered by a "contin uous" Kutta-like condition. The follo winglong-time ev olution is not affected by these small details which can be neglected, and the use of the "initial" Kutta-like condition allows to describe efficiently the water shipping.
Therefore, throughout the following sections, the initial Kutta-like condition has been solely applied to focus on the global features of water-on-deck. A parameter analysis is carried out in terms of the amount of shipped water in the first part. Then the occurrence of the less common Type I water-on-deck is inv estigated.

### 4.2 Preliminary Studies and Validation

In the follo wing, regularwa ves incident on a fixed rectangular body are considered. The initial Kutta-like condition that enforces the flow to leave tangentially the bow when the water reaches the instantaneous freeboard, $f$, is adopted. Once the freeboard is exceeded, the fluid velocity relative to thehip determines whether the deck will be wetted or the water will be diverted in the opposite direction.

Numerical solutions hav e been compared with two-dimensional experiments b y Cozijn (1995). In the experiment, sketched in figure 4.1, a wavemakr was used to generate regular waves


Figure 4.1 Sketch of the tw o-dimensional experimenal set-up by Cozijn (1995) and definition of main parameters.
in teracting with a rectangular bottom-mounted structure, placed at the opposite end of the tank, 1.028 m (h) deep. The freeboard $f$ was 0.1 m , and water-on-deck ev erts have been recorded bya video camera.
Figure 4.2 shows the comparison between n umerical, solid lines, and experimental, circles, freesurfaces profiles for the case with waveheight $H=0.128 \mathrm{~m}$ and frequency $\omega=5 \mathrm{rad} / \mathrm{s}$, corresponding to $\lambda=2.50 \mathrm{~m}$. Linear theory would in this case giv e $\lambda=2.44 \mathrm{~m}$. The reported experimental sequence is coded 5:36:12-19 from test No. A03 of Cozijn's data. The snapshots, labeled 1 through 8, giv ethe free surface as time increases, showing the occurrence of a dam
breaking-type water on deck. The first frame (cf. figure 4.2.1) reproduces the free-surface configuration just before the shipping of water. The following waveprofiles are reported for a time in terval of $\Delta t=0.04 \mathrm{~s}$. The global behavior of the free surface is well reproduced $\mathrm{b} y$ the nu-


Figure 4.2 Water-on-deck on a rectangular structure caused by incoming regular waves ( $H=0.128 \mathrm{~m}$, $\omega=5 \mathrm{rad} / \mathrm{s}$ ). The initial freeboard is $f=0.1 \mathrm{~m}$. The snapshots are enumerated as the time increases. Experimental data (circles) are from Cozijn (1995, experimental sequence coded 5:36:12-19 from test No. A03).
merical solution, ev enif the local details of the flow at the edge of the deck are approximated.

In the late ev olution, the numerical solution predicts a fluid front moving faster than in the experiments. Nevertheless, the water level along the deck is rather similar for the two results.
A possible explanation of the differences could be given by surface tension effects which are not modeled by present method. In facts, the thickness of the fluid lay er is of the order of 0.01 m , and the high curvature of the free surface at the water front requires a more complex description of the dynamics of the contact point (cf. Dussan 1979). This is supported bythe observation that the measured shape appears "rounded" and highly curved in proximity of the contact point. Viscous effects and turbulent resistance could also matter. Dressler (1954) performed twodimensional model tests for the dam-breaking problem. The experiments showed a division of the flow evolution into distinct regimes. At the beginning the flow was dominated bylaminar viscous effects, and the related importance grew with decreasing the scale of the experiment. In the second regime, the flow was dominated byinviscid hydrostatic pressure effects. Finally, turbulent effects became important and tended to slow down the wavefront velocity. The speed reduction occurred sooner when the bottom roughness was increased. Qualitatively these results can be applied to interpret the considered water-on-deck experiments. In particular, a non sufficiently smooth deck can cause a non-negligible decrease of the wave-fron velocity with respect to the in viscidsolution.
Anyway, since the deviation between the two results is strongly localized, it is believed unimportant in terms of effects for the possible impact problem where a superstructure is hit by the water flowing along the deck. On this ground, differences in the pressure o ver the structure are expected during the very initial time scale, which is unimportant from the structural reaction point of view.

A more realistic set of parameters is analyzed in the following. A FPSO in long and steep head-sea regular waves(Buchner 1995) is considered to determine the main parameters for the two-dimensional simulations. The draft of the ship is $D=17.52 \mathrm{~m}$, while the relative length and freeboard are respectively $L=14.86 D$ and $f=0.507 D$. In the experiments, a superstructure is located at a distance $d_{s}=2.05 \mathrm{D}$ from the bow. For simplicity, a straight vertical bow and restrained body motions are assumed. The follo wing analysisis for the first water-on-deck occurrence caused by incident waves with elength $\lambda=0.75 L$ and wave steepness $H / \lambda=0.09$. The top plot of figure 4.3 shows the free surface just after the initiation of the water shipping, and some follo wingconfigurations. The latest is after the shipped water has impacted against the vertical superstructure. At first, a steep water front grows at the bow (dash-dotted line), then the flow develops along the deck (dotted line), eventually hitting the deck house (solid line). The four bottom plots report the time ev olution of the water level at the locations A through D along the deck, shown in the top plot. The n umerical resultsare compared with the (three-dimensional) experiments by Buchner (1995). In the experimental set-up, the water level sensors were located along the centerplane of the ship. In spite of the three-dimensionality of the phenomenon, and that in our simulation body motions are restrained, the numerical simulation reproduces reasonably well the propagation of the water front. We observe that the scale of this experiment is muc h larger than that used ly Cozijn (1995). This supports our speculations about the role of surface tension in the previous case.
In more detail, in location A we observe a strong local effect associated with the first even tof water on deck and a clear ov erprediction of $h_{w}$ relative to the experiments. One must recall that geometrical details of the bow, and the wave-inducedbody motions prevent us from making a



Figure 4.3 T op: sketch and free-surface evolution during the shipping of w ater. Bottom: history of waterlevel $h_{w}$ (meters) at locations A-D along the deck. Numerical results (solid lines) and threedimensional experiments (dashed lines) by Buchner (1995). Time is expressed in seconds and $t_{\text {wod }}$ is the instant when the water shipping starts.
finer comparison. The relative difference is smaller for locations C-D, where $n$ umerical results underpredict the experimental values. This suggests an increasing three-dimensional behavior of the flow developing along the deck, in particular because of the additional contributions to the water lev el coming from thelateral sides of the ship.
Finally, for this particular choice of the parameters, the local wavesteepness in the bow region, the amount of water shipped on deck and the propagating flow velocity are observed to decrease when then umber of shipping even tsincreases. We will see in the next section that this is not a general result.

### 4.3 Influence of Main Geometric Parameters

A simplified parametric analysis of deck wetness has been made by using the amount of shipped water during one water-on-deck cycle, Q , as a measure of the water-on-deck sev erit. Q is the in tegrated flux of water overthe freeboard during one single water-shipping event, without any further consideration about residue of water from previous events. Therefore, at each water-
shipping cycle the deck is modeled as perfectly dry. In this way,it is assumed that the fluid flowing back along and outside the deck is not relevant for the free-surface dynamics and the back flow is not modeled at all. This means that we neglect (i) the in teraction of the water leaving the deck and returning to the sea with the bow-flow region, and (ii) the in teraction of fresh shipped water with residual water from a previous water-on-deck even t. Howev er, (i) in the real case the water lea es the deck mainly from the ship sides, and only a minor percentage lea vesthe deck along the ship centerplane. Thus we expect the committed error to be small. F urthermore, (ii) we will see how the water on deck even ts occur approximatively with the period of the incoming waves, while usually almost all the water leaves the deck in a shorter time (cf. Zhou et al. 1999). Thus also in this case we expect a small error.

Systematic variations of body geometry and of incoming-wa ve characteristics hav e been considered. In particular, the geometric parameters shown in figure 4.4 are examined, with the ship
Incident Wave


Figure 4.4 Sk etch of the main geometrical parameters considered.
draft used as reference length. The shipped water Q is made non dimensional by the amount of water $Q_{0}$ within a crest of the incoming waveand above the mean free-surface level (see figure 4.4).

Ship parameters At first, we analyze cases where the body motion is restrained. F our freeboard-to-waveheight ratios $(f / H=0.05,0.24,0.36$ and 0.55$)$ are considered and the in-


Figure 4.5 Influence of ship length and stem overhang on the bow deck wetness.
fluence of the stem ov erhang angle $\alpha$ and of the length-to-draft ratio $L / D$ of the ship is studied
for waves with $H / \lambda=0.06$ and $\lambda / D=6.6$. Results are presented in figure 4.5 , where the relative amount of shipped water is plotted versus $f / H$. As it can be expected, $Q / Q_{0}$ is strongly influenced by the freeboard of the ship. The length $L$ does not significantly affect the deck wetness sev erit y Howev er, if wave-inducedbody motions were considered, we would expect a stronger influence of the ship length.

A positive bow stem overhangreduces the relative amount of shipped water due to a larger wavereflection by the ship. Howev er, in the present case, the deck-wetness severit y does not dramatically change in the two considered geometries $\left(\alpha=0^{\circ}, 45^{\circ}\right)$. This is more evident for larger values of $f / H$. But, if we interpret $f$ as the instantaneous freeboard due to heave and pitch, $f / H$ can be quite small. This shows that the stem-angle effect could have some importance, depending also on the actual ship loading conditions.

According to recent proprietary experimental studies (Korbijn, personal communication), a bulbous bow may influence the water-on-deck phenomenon. Intuitively this can qualitatively be explained by considering the effect of the bulb on the flow equivalent to the disturbance caused bysources centered along the bulb axis. In particular, this means that the bulb causes


Figure 4.6 Influence of bulb at the bow on the deck wetness. Left top plot: analyzed bow geometries. Case a: vertical bow. Case b: bow with stem angle $\alpha=28^{\circ}$. Case c: bulb bow.
an additional vertical flow velocity at the free surface which can affect also the steepness of free-surface wavesand, therefore, the water shipping may increase because of the bulb. This explanation does not account for the presence of the free surface. The latter can either magnify (the high frequency limit giv es $\varphi=0$ as combined free surface condition) or reduce (the low frequency limit giv es $\partial \varphi / \partial z=0$ as combined free surface condition) the influence of the bulb. F or the specific study, wavelengthslong relative to the ship draft are of interest. This means that the free surface tends to reduce the effects of the bulb onthe local flow conditions.

As a simple heuristic study of the influence of bow geometry, we compared the flow in case of a vertical bow, a bow with stem angle $\alpha=28^{\circ}$, and a bow with bulb (cases a through c shown in the top left plot of figure 4.6). The main parameters used in the analysis are: $L / D \simeq 15.24, f / D=0.67, D=16.5 \mathrm{~m}$, for the ship, and $H / \lambda=0.095$ and $\lambda / L=1$, for the chosen regular incoming wa ves. In figures 4.6.a-.c free-surface configurations during the first water-on-deck ev en tare shown for the three geometries. In all cases, the latest reported configuration refers to the end of water shipping, i.e. when the fluid at the bow edge ceases to move rightwards. The role of stem overhangalone can be inferred by comparing cases a and b .

F roma global point of view the three cases are quite similar, with $Q$ about $13 \%$ of $Q_{0}$. A more local analysis would show that the water lev elfor cases b and c is smaller than in case a , while the water-front velocity is larger. The slope of the water front along the deck is always rather small, though it is slightly larger in case a. As it will be discussed in chapter 5 , the slope of the water front affects the severit y of the impact with dedk structures. However for slopes less than approximatively $40^{\circ}$ it does not represent anymore an important factor for the effects of the water impact with a superstructure. On the other hand, the loads depend strongly on the impact velocity, thus on the wave-fron velocity. Therefore, in this respect, the water impact due to an inclined bow can be worse even if the amount of shipped water remains roughly the same. Cases b and c do not exhibit a marked difference between them. Therefore, within the present two-dimensional analysis, the considered rather standard bulb does not seem to significantly influence the green-water loading.

Incoming wa veparameters In the following, the body parameters are kept fixed, and the influence of steepness, $H / \lambda$, and wavelength-to-draft ratio, $\lambda / \mathrm{D}$, on the relative amount of shipped water $\mathrm{Q} / \mathrm{Q}_{0}$ are discussed in left and right plots of figure 4.7, respectively. As expected,


Figure 4.7 Left: influence of nonlinearity of incoming wa ves on the bow-deck wetness. Right: influence of wavelength-to-draft ratio on the bow-deck wetness.
b y increasing $H / \lambda$ we observe a larger amount of shipped water. There is an almost linear trend for small $f / H$. When $f / H$ is larger, the nonlinear dependence of $Q / Q_{0}$ on the wav esteepness is more pronounced. The reason is that $Q$ becomes more strongly dependent on the wavecrest flow, which will have an increased nonlinear behavior with increased wavesteepness.

In the second plot, the effect of the wavelength-to-draftratio is shown for a constant wave steepness and zero stem overhang. The deck-wetness severity changes a lot from case to case,
though the nonlinearities associated with the incoming wa ves are the same. The worst conditions occur for large wav elength-to-draft ratios wherea smaller wav ereflection is observed. The long wav elengthcase is also the more interesting from a practical point of viw.

Time history of water-on-deck events In the previous analysis, only the first water-ondeck occurrence has been considered. Longer ev olutionsare now examined, and the history of shipping ev en tis analyzed. In particular, figure 4.8 gives the amount of shipped water $Q / Q_{0}$ as a function of the time. The time origin has been shifted to coincide with the instant $t_{\text {wod1 }}$


Figure 4.8 Time evolution of the relative amount of shipped water $Q / Q_{0}$. The considered cases A-E are described in table 4.1. F or all the test-conditions $f / H=0.24$.
of the first water-shipping even $t$ and the time is normalized $b y$ the waveperiod. For all the cases summarized in table 4.1, the same freeboard relative to the wav eheight $f / H=0.24$ has

| case | $\alpha$ | $\lambda / L$ | $H / \lambda$ |
| :---: | :---: | :---: | :---: |
| A | $0^{0}$ | 0.33 | 0.064 |
| B | $45^{0}$ | 0.33 | 0.064 |
| C | $0^{0}$ | 0.33 | 0.095 |
| D | $0^{0}$ | 0.05 | 0.095 |
| E | $0^{0}$ | 0.67 | 0.095 |

Table 4.1 Synopsis of cases considered for studying the history of water shipping.
been considered. Even if the chosen $\lambda / L$ are small relative to design conditions, we should recall the previous shown insensitivity of $Q / Q_{0}$ to $\lambda / L$. Water-on-deck events (represented by the symbols) occur approximatively with the period of the incoming waves. Large changes of $Q / Q_{0}$ with respect to the first occurrence are observed in all cases. On a long time-scale $Q / Q_{0}$ seems to attain a nearly constant value. Clearly, this result is not general because more realistic sea-state conditions are characterized by irregular waves. However, large wa ves may reach the ship in groups and, in this context, the present result becomes relevant. Figure 4.8 indicates that if two succeeding waveswith nearly the same height and wavelengthcause deck wetness, the last one gives the most severe condition.

In more details, the figure shows that the worst water shippings happen for the steepest conditions (cases C and E ). The corresponding $Q / Q_{0}$ tend almost to the same value, confirming the steepness as the most important waveparameter for long waves(in both cases the wavelength is large with respect to the draft). In case D , the steepness is the same but with shorter wa velength, equal to the draft, and the shipped water is comparable with that computed for a longer and less steep wave (case A). Case B (same parameters as case A but with $\alpha=45^{\circ}$ ) shows a certain effect of the stem ov erhang in reducing the sev erit yof the deck wetness.

Figure 4.9 shows the free-surface profiles for cases A and B, left and right plots respectively, corresponding to the first four water-shipping events. Two configurations are given in each plot:


Figure 4.9 First four water-shipping events for cases A, left,and B, right. For each ev en t,the freesurface configurations reported correspond to the maximum freeboard exceedance (solid line), and to zero-water flux entering the deck (circles).
the one with maximum freeboard exceedance (solid lines), and the one with zero flux of water onto the deck (circles).
Focusingn case A (left plots), we observe that the wav epattern in front of the body does not reproduce itself at each water-shipping cycle. This is reasonable because of the complexity of
wa vereflection, with higher harmonics generated and reflected with non-trivial phase relations. In spite of this, the waveforms in the very near field and on the deck are rather similar for all the three latest even ts, consistently with the observation that an almost constant value of $Q / Q_{0}$ is measured. Here, $t_{\text {wod }}$ is the time just after the freeboard exceedance, for which there is a positive inflow onto the deck, and $t_{\text {last }}$ is the time when the shipping of water stops. With these definitions, we observe that the time duration of a water-on-deck cycle is roughly constant and about $40 \%$ of the wav eperiod T .
Case B refers to a geometry with stem angle of $45^{\circ}$. From a global point of view, the relative amount of shipped water is not significantly affected by the stem angle (cf. right plots of figure 4.8), at least for the present choice of $\alpha$.

The local details of the flow on the deck are more clearly influenced $b$ y the stem overhang. F or both A and B cases, a wedge-like water front is observed but with a smaller interior angle and higher velocity for the geometry with $45^{\circ}$ stem overhang. The water level along the deck is smaller. As we will discuss in chapter 5 , the impact pressures on a deck house are most sensitive to the impact velocity, but are also influenced by the other flow characteristics. Therefore, it is hard to giv econclusive arguments about possible positive or negative effects of $\alpha$ from the impact-problem point of view. We may be naively tempted to believe that a large stem ov erhang prevents the water for coming on deck. On the other hand, it seems difficult that geometrical details could counteract effectively the large horizontal velocity in the incident wave,especially for long waves.

Of course, in this respect, the limitations of present inv estigation should be noted. The analysis is two-dimensional and the body motions are not included. The stem overhang or the flare may affect the ship motions, and in turn the interaction with wa ves. F or instance, Lloyd et al. (1985) reported model-test results where the bow flare caused a clear increase of the relative vertical motions in the bow area. The stem overhangmatters also in the case of breaking waves hitting close to the bow. During the two-dimensional water on deck experiments discussed in chapters 7 and 8, the effects of larger bow forces were noted when a vertical bow was substituted with a $45^{\circ}$ stem angle bow. However bow impact phenomena are not focused on in the present work.

### 4.4 Influence of Body Motions

Body motions play a major role in determining the occurrence and severity of water on deck. Here, we are not solving the problem for a floating body free to respond to incoming waves. More simply, the body motion is prescribed a priori. In particular, since the present work deals with bow-deck wetness in head sea, the effect of forced heav e motion is studied. We have had in mind the relevant local heave at the bow. The effect of the pitch angle both on the outer wave field and on the flow along the deck is neglected. Since the stem overhangangle has a small influence, one could argue that the pitch angle should not be important for shipping of water on the deck. On the other hand, the pitch angle may effect the flow on the deck. The influence of this parameter is studied at the end of this section.

The top left plot of figure 4.10 gives the first water-on-deck occurrence for the case E from the table 4.1, with a freeboard ratio $f / H=0.55$. The body is constrained and $Q \simeq 16 \%$ of $Q_{0}$.


Figure 4.10 Influence of body motion. a) restrained body conditions, b) forced heave initially in phase with the w aterat the bow, c) and d) forced heave initially out-of-phase with the w aterat the bow.

F orthe same parameters, the plots b) through d) show the flow when a forced heave motion is excited at the beginning of the water shipping. The adopted law of the motion is

$$
\begin{equation*}
\zeta_{3}(t)= \pm A \mathcal{H}\left[t-t_{w o d}\right] \sin \left[\frac{2 \pi}{T}\left(t-t_{w o d}\right)\right] \tag{4.1}
\end{equation*}
$$

where $\mathcal{H}$ is the Heaviside function. In all cases the free-surface configuration with almost zero water flux on the deck is shown.
In plot 4.10.b the motion is initially in phase with local wavemotion, corresponding to the plus sign in equation (4.1). The amplitude-to-wa ve height ratio $A / H$ is 0.25 . The phenomenon appeared qualitatively less sev ere, with the amount of shipped water $Q \simeq 6 \%$ of $Q_{0}$. However this nice situation is unlikely to occur in the case of a FPSO unit for the chosen wave-body parameters. Conditions of out-of-phase body motions are more reasonable and can make the water on deck muc hmore sev erethan in the restrained body case. In facts, a heave amplitude $A=0.25 H$, plot 4.10.c, increases the amount of shipped water by a factor 1.9 relative to case a). When $A / H=0.5$ (see plot 4.10.d), the factor becomes 3.2 and reaches 6.2 in the case, not shown, with $A / H=1$.

In the follo wingthe role of pitch angle is examined. Even if the time scales of the water on deck before the water hits the deck house could be $\mathrm{O}(25 \%)$ with respect to the incident wave period, we hav e considered a "quasi-steady" approach as first approximation and studied the influence of a constant pitch angle. Inthis way the pitch angle is considered as a trim angle, in practice. The studied case is defined in the left sk etc hof figure 4.11. In the right of the same figure the first (top) and the second (bottom) water-on-deck ev erts are examined in the case of zero trim angle (dashed lines) and trim angle $\zeta=-5^{\circ}$ (solid lines), with two time instants for each ev en tincreasing from left to right. Restrained body conditions and vertical bow at zero


Figure 4.11 Influence of trim angle. Left: sk etd of the problem. Right: cases $\zeta_{5}=-5$ and 0 degrees are compared for the first (top) and the second (bottom) w ater-on-ded even ts and restrained body conditions. $\alpha=0^{\circ}, L / D=10, \lambda / L=1.5, H / \lambda=0.064$ and $f / H=0.38 . \Delta \tau_{\text {wod }}=\left(t-t_{\text {wod }}\right) \sqrt{g / D}$.
trim, $L / D=10, \lambda / L=1.5, H / \lambda=0.064$ and $f / H=0.38$, are assumed. A negative trim angle (see sketch in figure 4.11) should qualitatively increase the wave reflection from the body in the same way as a positive stem angle. Further, since the component of the gravity acceleration $\vec{g}$ parallel to the inclined deck counteracts the water shipping in the case of a negative trim angle, one should expect reduced wavefront velocity along the deck. F romthe results, however, both the amount of shipped water, the water level and the velocity of the water flow propagating along the deck are practically unaffected by the trim angle.

### 4.5 Occurrence of Waves Plunging on the Deck

The flow along the deck resembles the one after a dam breaking in the most common type of green water even t. Recent experiments in irregular seas (MARINTEK 2000) showed that water on deck can also occur in the form of large wav es plunging directly on the dek or superstructures. This phenomenon appears like a "single" even tassociated with a very steep, almost breaking, incoming wave, usually propagating in small background waves. Actually, one cannot classify this as "freak wave", but it is known that instability and modulation of wavegroups in open sea can lead to the formation of steep highly energetic waves. Their interaction with structures is a known cause of highly nonlinear force components (Chaplin et al. 1997, Welch et al. 1999). Similar circumstances in complex combination with ship motions can cause these extreme events. In this work only regular steep wav eshave been modeled. In spite of this, some extreme cases with emphasis on the effect of body motions hav e been analyzed to gain insights in to this aspect. The geometric parameters hav e been deduced from the MARINTEK experiments ( $L / D=13.75$, $\left.f / D=0.8, d_{s} / D=1.0625\right)$. Due to the limited role of the stem overhang, the bow was
approximated with a straight vertical wall. F urther, a wavetrain of long steep (eventually) regular wav eswith $\lambda / L=1.022$ and $H / \lambda=0.095$ is considered. The focus is on the interaction of the body with the leading wavewhich is characterized by high steepness and strong tendency to break. This makes the analysis more consistent with the features observed in the experiments. F orcedheav e motion is excited at a time instant $t_{0}$ with an amplitude $A$ and a phase $\beta$, in the form

$$
\begin{equation*}
\zeta_{3}(t)=A \mathcal{H}\left[t-t_{0}\right] \sin \left[\frac{2 \pi}{T}\left(t-t_{0}\right)+\beta\right] . \tag{4.2}
\end{equation*}
$$

Here $T$ is the wave period. Wave generation starts at $t=0$, with the upstream vertical boundary (cf. section 2.2) located 5 wavelengthsahead of the bow. The phase angle $\beta$ is selected to giv e a sudden vertical displacement of the ship at $t=t_{0}$. Some of the studied cases, and discussed in the follo wing, are summarized in table 4.2.

| case | $\mathrm{f} / \mathrm{H}$ | $\mathrm{A} / \mathrm{H}$ | $\beta$ | $t_{0} / T$ | $t_{\text {wod }} / T$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| a | 0.6 | 0. | - | - | 10.795 |
| b | 0.6 | 0.5 | $-90^{0}$ | 10.626 | 10.841 |
| c | 0.6 | 0.5 | $-5^{0}$ | 10.783 | 10.844 |
| c 1 | 0.6 | 0.25 | $-10^{0}$ | 10.783 | 10.795 |
| c 2 | 0.6 | 0.125 | $-20.5^{0}$ | 10.783 | 10.790 |
| d | 0.6 | 0.5 | $-11^{0}$ | 10.783 | 10.783 |

T able4.2 Plunging waveanalysis: summary of presented cases.

In left plot of figure 4.12, restrained body conditions are considered, and some free surface configurations are presented. The wave, reaching the bow, is steep and unsymmetric but its tendency to break is reduced during the run-up along the bow. The water shipping starts with already quite large horizontal velocities of the fluid making the phenomenon less similar to the dam breaking problem. Though the shallower water conditions on the deck would amplify the original tendency to wavebreaking, the fast motion of the wavefront has opposite effect and is the main reason why the waveis not breaking before the water impacts on the deck house.


Figure 4.12 Plunging wave analysis: case a (left) and case b (right) in table 4.2.

The heave motion largely affects the phenomenon. In the next figures (right plot of figure 4.12 and plots of figure 4.13), a heav e with amplitude $A / H=0.5$ is considered (see table 4.2 for the other parameters). In case b (right plot of figure 4.12), the motion is excited with a phase such that the instantaneous freeboard at $t=t_{0}$ is higher than the wave eleution at the bow. By "instantaneous freeboard" is meant the mean freeboard plus the change in vertical position due to heave. The upward motion of the bow causes lower trough ahead of the breaking waveand a bow impact occurs. Air entrapment and (probably) a complex two phase flow are expected to occur. By neglecting these phenomena and "stretching" the simulation further, it appeared that the shipping of water is not particularly severe. The upward motion of the bow, in facts, limits the increase of the vertical velocity of the fluid after the impact.
In the plots of figure 4.13 the heav e motion is excited later than in the previous case. This is done in both situations at the same instant but with different initial phase. This means a different instantaneous freeboard, in particular for case d the waveelevation at the bow is equal to the instantaneous freeboard. The larger $t_{0}$ eliminated the bow impact. However other in teresting


Figure 4.13 Plunging wave analysis: case c (left) and case d (right) in table 4.2.
phenomena occurred. In case c, an initial local breaking tendency of the water along the deck is observed. But this is preven tedby an increase of the horizontal velocity of the contact point between water and deck. The subsequent flow is like the one after a dam breaking. In case d, the amount of shipped water is larger and the upward motion of the ship results in a wave plunging onto the deck. The three considered situations could have quite different consequences on the ship.
If case c is modified by taking a heave amplitude $A / H=0.25$ and $A / H=0.125$ but maintaining the same instantaneous freeboard at $t=t_{0}$, the results shown respectively in left and right plots of figure 4.14 follo $w$. The water on deck is still quite serious but the consequences are more dangerous for the superstructure than for the bow or the deck. With $A / H=0.25$, in particular, the faster rate of the water region to become shallower steepens the wavepropagating along the deck. A rather thin jet develops. The jet evolves faster than the water-deck contact point and eventually hits the superstructure. After the impact the simulation was contin ued by a local matching with the similarity solution by Zhang et al. (1996) for an infinite asymmetric fluid wedge hitting a flat wall (see sk etc hD. 1 in appendix D ). If the heave amplitude is further decreased (case c2, right plot of figure 4.14), the velocity of the wa ve fron becomes larger relative


Figure 4.14 Plunging wave analysis:case c1 (left) and case c2 (right) in table 4.2.
to the plunging jet velocity. This implies that the impact with the superstructure occurs from the deck. The plunging wave hits the mass rising along the vertical wall after the impact. This causes an air pock et to be formed. The relative velocity between the developing plunging jet and the wavefront depends on the rising rate of the deck. This has an important influence on the possibility of a plunging breaker hitting the superstructure.

F romthe n umerical inv estigations, the occurrence of this extreme event seems to be related to the in teraction with a steep wavealmost breaking, more than to the wa ve-body interaction byitself. Howev er, the influence of ship motion to enhance or reduce its severit y can not be excluded, as suggested, for instance, by case d (see figure 4.13.d), though the waveplunges far from the superstructure.

## Chapter 5

## Dam Breaking and Water Impact

In this chapter, a dam-breaking flow is used as a prototype problem to inv estigate the flow along the deck and the subsequent water impact against vertical structures, usually built on decks of ships. Secondly, a parametric analysis of the water impact against a wall is carried out by varying the wall slope and the local characteristics of the incoming flow. The latter are characterized by the wavefront velocity and the local free-surface geometry close to the in tersection point with the deck. Finally, the influence of the hydroelastic interaction between the structure and the surrounding fluid is discussed byusing a linear Euler beam model for the wall.

We briefly mention that other prototype problems have also been investigated, such as the collapse of water columns, the water run-up along straight walls with different slopes, the initial and the later stages of the flow generated after the breaking of a dam, which served to verify the n umerical model and to gain confidence with the physical problem. These cases are collected in appendix C.

### 5.1 Dam Breaking and Water Impact

As we discussed, when the waveelevation exceeds the freeboard, the water can flow o ver the deck. Very often, the resulting flow field resembles the one after a dam breaking (cf. section 1.1). Therefore, the dam-breaking flow represents a natural prototype problem to gain physical understanding of our (more general) problem. Moreover, the simpler flow conditions allows to better verify and validate our n umerical model, and finally a large set of data are a vailable in the literature.

In the following, we consider in details the problem sketc hed in figure 5.1. A reservoir of water with height $h$ and length $2 h$, closed bya dam, is placed at a distance $3.366 h$ from a vertical obstacle. With the present choice of geometrical parameters, the considered problem reproduces the experimental conditions adopted by Zhou et al. (1999). In particular, the authors made av ailablemeasurements of the waveheight at the locations marked by A and B in the figure, and the pressure induced on the vertical wall at location C.


Figure 5.1 Dam-breaking problem and impact against a vertical rigid w all. Sketch of the problem and of the experiment performed by Zhou et al. (1999) with $h=0.6 \mathrm{~m}$. Wave-gaugelocations A and B , and pressure-transducer location C, are shown.

At the beginning, say $t=0$, the dam is suddenly remov ed and the flow develops along the horizontal deck, figure 5.2.a, finally impacting against the vertical wall. The fluid is violently


Figure 5.2 F ree-surfaceflo wand impact against the vertical wall following the breaking of the dam (cf. figure 5.1). $\tau=t \sqrt{g / h}(\mathrm{t}) 2.2(0.54 \mathrm{~s}), 2.6(0.643 \mathrm{~s}), 5.6(1.385 \mathrm{~s}), 6.2(1.534 \mathrm{~s})$.
deviated vertically upwards, figure 5.2.b, rising along the wall in the form of a thin lay er of fluid. At this stage, formation of spray and fragmentation of the free surface may occur. These finer details cannot be handled by the present method. However, it is believed they are irrelevant for computing structural loads. As time increases, under the restoring action of gravit y, the fluid acceleration decreases and the upward velocity in the jet decreases until it becomes negative. The motion of the water is reversed in a waterfall, figure 5.2.c, ov erturning in the form of a wave plunging onto the deck, figure 5.2.d. The n umerical simulation has then to be stopped.

The plots in figure 5.3 give the time evolution of the water height $h_{w}$ at the locations $(x / h)_{\mathrm{A}}=$ 3.721 and $(x / h)_{\mathrm{B}}=4.542$ along the deck ( $c f$. figure 5.1). Both the experiments and our numerical


Figure 5.3 Time evolution of the experimental (Zhou et al. 1999) and numerical water levels $h_{w}$ at $(x / h)_{\mathrm{A}}=3.721$ and $(x / h)_{\mathrm{B}}=4.542$. Wave-gaugelocations A and B are shown in figure 5.1.
simulation allow to identify the three fundamental stages in the evolution of the flow field. The Stage I is characterized bythe sudden rise of the water level $h_{w}$, due to the transition from dry-deck conditions to wet-deck conditions. Clearly, the shape of the water front determines the growth rate of $h_{w}$, and some differences can be detected between the numerical solution and the experimental measurements, which we will comment later on.
The main feature of the following Stage II is the much slower growth rate of the water lev el because of the almost flat free surface above the wa vegauges. This is well confirmed by plots b and c in figure 5.2 , which correspond to the physical times of 0.643 s and 1.385 s , respectively. Finally, the n umerical simulation allows to understand the origin of Stage III, characterized by a new steep increase of $h_{w}$. This is apparently due to the water overturning (cf. plots 5.3.c and 5.3.d) which giv esan additional contribution to the waveheight measured at the location B. Later on, also the signal recorded by the gauge located in A displays this phenomenon, which cannot be follo ved further on $\mathrm{b} y$ the present n umerical method which breaks down when the free surface plunges on itself.
Due to lack of details about the experiments, the n umerical simulation and the experimental record at location A have been synchronized when $h_{w}$ attains a non-zero value.

We discuss now the impact of the water front against the vertical structure. During the first stage of the impact, the flow resembles that due to a (half) wedge of fluid hitting a straight wall. Apparently, the rest of the flow field is nearly unaffected by the impact. Since the vertical acceleration of the fluid around the contact point is $\mathcal{O}(5 \mathrm{~g})$, the gravity plays a minor role. This is better shown in plots 5.4.a1-a4, where the free surface near the wall, after the impact, is plotted together with the zero-gravit ysimilarity solution by Zhang et al. (1996), where we considered an infinite wedge of fluid hitting the wall at $90^{\circ}$. Plots are progressively enumerated as the time increases. More specifically, by defining $\tau_{\mathrm{imp}}=t_{\mathrm{imp}} \sqrt{g / h}$ as the initial non-dimensional impact time, we report the time instants $\Delta \tau_{\mathrm{imp}}=\tau-\tau_{\mathrm{imp}}=0.0138,0.0243,0.0738$ and 0.1338 . The two solutions remain in qualitative agreement even for a non-dimensional time $\Delta \tau_{\mathrm{imp}}=0.1338$ after the impact, confirming a limited role of the gravity in the early stage of the impact.

The impact pressures are now discussed in more detail. Plots bl-l4 in giure 5.4 present the pressure distributions corresponding to the free-surfaces configurations a1-a4. According to the


Figure 5.4 F ree-surface profiles (a1-a4) and pressure distributions (b1-b4) during the initial stage of the impact against the vertical w all. Solid lines: present numerical simulations; • similarity solution from Zhang et al. (1996); $\Delta \tau_{\mathrm{imp}}=\tau-\tau_{\mathrm{imp}}=0.0138,0.0243,0.0738,0.1338 . \tau_{\mathrm{imp}}$ is the initial nondimensional impact time. Plots are progressively enumerated as the time increases.
n umerical results (solid lines), at eadh time instant the maximum value of the pressure is located at the initial impact position and attains the highest values just after the impact. In the region
of the thin jet along the wall, the pressure is almost equal to the atmospheric one, which we conventionally set to zero.
The symbols represent the pressure distribution from the gravit y-lesssolution of a fluid wedge hitting a flat wall. A formula for the pressure distribution is not av ailable inthe original paper by Zhang et al. (1996), and this has been evaluated by solving numerically the integral equation for the velocity potential along the wall, where the boundary data on the free surface have been taken from the similarity solution of Zhang et al. (1996). Details on this procedure and the correction of some misprints in the original paper by Zhang et al. (1996) are reported in appendix D.

At the beginning, the agreement between the two different analyses is good (solid lines vs circles), consistently with the agreement between the corresponding free surfaces. As time goes on, pressure distributions seem to disagree more rapidly than the free-surface profiles, although they qualitatively remain of the same shape for all the considered time instants. T obe noted, in particular, is the tendency of the gravity to weaken the maximum pressure, while it remains constant in the zero-gravity case. This is due to a reduction of the $-\rho \partial \varphi / \partial t$ contribution to


Figure 5.5 Water impact against the vertical wall. T erms cotributing to the dynamic pressure along the wall: comparison betw eenthe numerical solution with gra vit y solid lines, and without gravity (with free surface data from the similarity solution by Zhang et al. 1996), bullet symbols. Left plot: $-\partial \varphi / \partial t / g h$. Right plot: $-u^{2} / 2 / g h=-|\nabla \varphi|^{2} / 2 / g h . \Delta \tau_{\mathrm{imp}}=\tau-\tau_{\mathrm{imp}} . \tau_{\mathrm{imp}}=$ initial non-dimensional impact time.
the pressure ( $c f$. left plot of figure 5.5 for $\Delta \tau_{\mathrm{imp}}=0.1338$ ), as we can infer bylooking at the $-\rho|\nabla \varphi|^{2} / 2$ term, plotted in the right of figure 5.5. Near the initial impact position, the difference in the prediction of the $-\rho \partial \varphi / \partial t$ term is more pronounced than that of the velocity contribution to the pressure. In the latter case, near the initial impact position the two solutions are roughly superimposed.

The n umerical solution was verified by comparing the horizontal force $F_{x}(t)$ exerted on the wall as evaluated b y direct pressure integration and b y conservation of fluid momentum (see e.g. F altinsen 1990). In the latter case, a control volume bounded bythe instantaneous wetted surface of the wall, $l_{W}$, a vertical control surface, $l_{C}$, at a distance $x / h=1$ from the wall, and the portions of free surface, $l_{F S}$, and deck, $l_{B}$, between them, has been considered (see left plot of figure 5.6). The two results agree well, except at the very beginning (cf. right plot of figure 5.6).


Figure 5.6 Left: control volume where the conservation of the fluid momentum is applied. Right: time history of the horizontal force $F_{x}$ on the vertical w allsho wnin figure 5.1. Numerical results obtained with direct pressure integration (solid lines) and conservation of fluid momentum (circles).

Zhou et al. (1999) measured the wavepressure on the vertical wall during the impact bya circular shaped gauge, with diameter 0.09 m and centered at the location C on the wall (see figure 5.1) and sketc hed on the left of the figure 5.7. In the right plot, the time evolution of the measured pressure (dashed line) is given together with the pressure obtained by the present n umerical simulations.



Figure 5.7 Left: position of the pressure gauge in experiments by Zhou et al. $\quad(1999, h=0.6 \mathrm{~m})$. Right: experimental and numerical evolutions of the pressure along the vertical wall (see sketch 5.1).

The dash-dotted line refers exactly to location C. The two curves attain non-zero values almost at the same instant, confirming the global agreement between the numerical simulation and the experiment. It is worth stressing that the two signal have been shifted consistently with the shift used to synchronize the wavedata at location A.

A certain difference between theory and experiments is apparent, though mesh refinement and local regridding have been used to achieve invariance of the solution and to rule out the dependence on the discretization parameters. On the other hand, the complexity of the experiment makes it difficult to identify the error sources. Actually Zhou et al. (1999) commented that it was difficult to ac hieve repeatability of the results. Similar difficulties have also been observed during the two-dimensional water-on-deck experiments described in chapters 7 and 8. In the latter case, the main error source was the sensitivity of the pressure gauges to temperature
changes, primarily caused bydry-wet-dry cycles in the sensors conditions.
It can be observed that, for the actual scales of the experiment by Zhou et al. (1999), even a non perfectly dry deck (for example because of a previous experiment) can introduce significant differences in the measured data. This seems plausible also in the present case if we observe the water level comparison in figure 5.3. In facts, though the experimental and numerical evolutions are globally in satisfactory agreement, the n umerical solution underpredicts the measured data in proximity of the instant of time when the water lev elattains non-zero $v$ alue. In particular, the measured $h_{w}$ has a maximum (for example around $t=0.4 \mathrm{~s}$ for the location A ) which is not present in the numerical results. This experimental feature can be conv erted from a temporal to a spatial point of view and, in particular, suggests a hump in the free surface close to the contact point. This is not visible in the dam-breaking free-surface profiles reported in Dressler (1954), and could be due to the presence of a layer of water before the dam breaks. Dam-breaking experiments byStansby et al. (1998) show that, if the deck is not perfectly dry due to leakage (in those experiments a film of water with a thickness about 1-2 mm was present downstream of the dam) a horizontal bulge of fluid develops just after the dam release, resulting in a small h ump around the water front. This very peculiar local flow is consistent with the recorded water levels taken by Zhou et al. (1999). Unfortunately, the limited set of data availabledoes not allow for a better verification of the present speculation.

Finally, we observe that the pressure undergoes large variation within the area of the transducers, and indeed the experimental pressure curve is closer to the pressure computed at the lo wer location of the transducer, indicated with the letter D in the sk etc hof figure 5.7.

### 5.2 Parameters Influencing the Impact

### 5.2.1 Angle of the Incoming Water Flow and Impact Velocity

Previous results for the impacting flow against the wall suggest the possibility of using a gravit yless similarity solution to explore the parameters influencing the impact, at least for the initial stage when the acceleration is large compared with gravity. In this respect, this simplified approach is equivalent with that used to deal with slamming problems.

On this ground, we will consider the problem of a semi-infinite wedge of fluid impacting on a vertical wall at $90^{\circ}$ incidence. Under the zero-gravit y assumption, the problem is completely specified by the velocity $V$ of the wedge and byits angle $\beta$ (see sketch in figure 5.8). In the actual problem, we will consider $V$ as representative of the velocity of the water front along the deck, and $\beta$ as the slope of the free surface at the contact point with the deck.
With this approximate model (similarity solution by Zhang et al. 1996 plus numerical pressure ev aluation, seeappendix D), we obtained the non-dimensional maximum pressure $P_{\max } / \rho V^{2}$ as function of $\beta$ shown in the center plot of figure 5.8. As it can be expected, the maximum pressure increases as the wedge becomes wider. The spatial distribution of the pressure is giv enin the right plot. When $\beta<35^{\circ}$, the peak pressure occurs at the in tersection between the wall and the deck, while for larger angles $P_{\max }$ is shifted upwards along the wall. Also the shape of the pressure distribution changes gradually as $\beta$ increases, leaving a plateau between the pressure peak and the in tersection of the wall with the deck.


Figure 5.8 Left: sketch of the equivalent problem of a fluid (half) wedge impacting a flat wall at 90 degrees. Center: maximum pressure on a wall due to the w aterimpact. Right: pressure distribution along the vertical wall for $5^{\circ} \leq \beta \leq 75^{\circ}$ with increment $\Delta \beta=10^{\circ}$. The results are numerically obtained by using the similarity solution by Zhang et al. (1996) for the free surface conditions.

It can be seen, that the derivative $\left.d\left[P_{\max } / \rho V^{2}\right)\right] / d \beta$ is large only for $\beta>\sim 60^{\circ}$, and becomes quite small for $\beta<\sim 40^{\circ}$. Therefore, below such angle, the pressure is mainly influenced by the velocity $V$.

When $\beta$ is large enough, the results agree qualitatively with a Wagner (1932)-type analysis (cf. figure 5.9). This analysis implies that the examined fluid particles at initial time of impact are on the surface of the fluid wedge, and that they will move normally to the wall with the initial velocity $V$ increased bya contribution due to the impact against the wall. The Wagner-type


Figure 5.9 Left: distributions of pressure $p$ along a vertical wall due to the impact of an infinite (half) w edgeof fluid. Similarity solution by Zhang et al. (1996), solid lines, Wagner method, dashed lines. Right: maximum pressure along the wall. Similarity solution, solid line, and Wagner method, black squares. $V$ : impact velocit $\mathrm{y}, \beta$ : angle of the (half) wedge.
solution is calculated by a flat-plate approximation, with dynamic free-surface condition $\varphi=0$, where $\varphi$ is the (perturbation) velocity potential caused by the impact. The intersection between the fluid particles and the wall determines the length of wetted wall in an outer-flow domain, which can be matched with an inner-flow domain solution at the spray root. A composite
pressure distribution can be obtained as described by Zhao and F altinsen (1993).
Comparisons between a Wagner-type analysis and the similarity solution are presented in figure 5.9 in terms of pressure distribution (left plot) and maximum pressure along the wall (right plot). The position and the value of the maximum pressure agree well. Differences occur at the upper part of the jet. One reason may be related to the fact that, in the similarity solution by Zhang et al. (1996), the shape of the free surface in proximity of the wall is not consistent with the local free surface in the Wagner-type analysis. On the other hand, the latter does not ensure the conservation of fluid mass when applied to the problem of a fluid wedge hitting a rigid flat wall.

A simplified solution for small interior wedge angles has been derived in appendix E , and the free surface elevation simply reads:

$$
\begin{equation*}
\eta=(x+V t) \tan \beta-\int_{0}^{t} \frac{2 V}{\pi} \ln \left(\tanh \frac{\pi x}{2 a}\right) \mathrm{d} t \tag{5.1}
\end{equation*}
$$

with $a=2 V t \tan \beta$. Figure 5.10 shows a good agreement between the free-surface elevation predicted by the simplified method and the similarity solution.


Figure 5.10 F ree surface elevation close to a wall hit by an infinite fluid wedge with impact velocity $V$ and semi-angle $\beta$. Asymptotic solution for small $\beta$, dashed lines, similarity solution by Zhang et al. (1996), solid lines.

Finally, figure 5.11 shows the comparison of the maximum pressure $P_{\text {max }}$ between the similarity solution, the Wagner method and the asymptotic solution for small $\beta$. It is apparent how the small- $\beta$ solution giv esgood predictions approximatively up to $\beta=30^{\circ}$, while the Wagner-type method agrees satisfactorily for $\beta$ between $\sim 45^{\circ}$ and $90^{\circ}$ ( $c f$. also right plot of figure 5.9). The asymptotic value for $\beta=0^{\circ}$ is the stagnation pressure $0.5 \rho V^{2}$. The $-\rho \partial \varphi / \partial t$ term in the Bernoulli equation plays in general an important role in determining the maximum pressure.

It is then instructive coming back to the dam-breaking problem analyzed at the beginning of this chapter. In this case, the slope of the water front at a distance $\Delta x=0.65 h$ from the dam is $\beta \simeq 40^{\circ}$ and decreases as the ratio $\Delta x / h$ increases. Therefore, for obstacles located farther than


Figure 5.11 Maximum pressure on a wall hit by an infinite fluid wedge with impact velocit y $V$ and semi-angle $\beta$. Asymptotic solution for small $\beta$, triangles, pressure evaluated numerically by using the zero-gravity similarity solution by Zhang et al. (1996), solid line, Wagner method, full squares.
$\Delta x=0.65 h$ the maximum pressure exerted on the wall is not sensitive to the actual impact angle (see left plot of figure 5.8). In this range, from a practical point of viw, an upper bound to the pressure $P_{\max }=f(V, \beta)$ is giv enb $\mathrm{y} P_{\max }(V) \simeq 1.4 \rho V^{2}$.

It is worth stressing that in actual structural-response calculations the estimate of the maximum pressure only is not enough, and the entire (time dependent) pressure distribution on the wall has to be ev aluated. In this respect, the pressure based on the similarity solution (cf. figure 5.4) has the advantage of a simpler numerical evaluation, though for increasing time overpredictsthe exact results.

### 5.2.2 Slope of the Wall

It is known that the use of inclined structures reduces the pressure at the impact. This is confirmed $\mathrm{b} y$ the following computations, reported in figures $5.12-5.13$, where the exact dambreaking problem has been solved to fully include the gravitational effects. For the case studied in section 5.1, the resulting impact parameters are $\beta=11^{\circ}$, and $V=1.983 \sqrt{g h}$, while the slope of the wall $\alpha$ (see sk etc hof figure 5.12) is varied between 0 and 40 degrees. The right plot in figure 5.12 shows the normal force acting on the wall for increasing values of $\alpha$. In particular, as $\alpha$ increases, the force component increases with a smaller rate, resulting in a weaker load for a giv entime. As an example, when $\alpha=40^{\circ}$, at the end of the simulation, $F_{n, \max }^{\alpha}$ is about $50 \%$ of the value $F_{n, \text { max }}^{0}$ obtained for the vertical wall $\left(\alpha=0^{\circ}\right)$. In general, the ratio $F_{n, \text { max }}^{\alpha} / F_{n, \text { max }}^{\alpha=0}$ decreases almost linearly with $\alpha$. The pressure values along the wall (cf. figure 5.13), and in particular the maximum pressure occurring at the position of first impact, decrease as $\alpha$ increases. The differences among the pressure profiles reduce as time increases.

Finally, we stress that in the simulation a rigid wall has been assumed, though the pressure distribution could be influenced by hydroelastic effects. In this case, it is important to introduce


Figure 5.12 Water impacting against an inclined wall. Left: sketch of the problem. Right: time ev olution of the normal force acting on the structure for increasing $\alpha$. The "inflow" conditions are those relative to the case of figure 5.1, where $\beta=11^{\circ}$ and $V=1.983 \sqrt{g h}$. The results are obtained by solving numerically the "exact" problem.


Figure 5.13 Water flow impacting a structure with angle $\beta=11^{\circ}$ and impact velocity $V=1.983 \sqrt{g h}$. The wall has an arbitrary slope $\alpha$. Pressure distributions, related to the values of $\alpha$ considered in figure 5.12, are shown at three time instants after the impact.
the generalized force $\int p \psi_{j} \mathrm{~d} l$, where $\psi_{j}$ is an eigenmode for the local structural vibration. While the generalized forces related to the high initial values are modest ( $z=0$ is a structural node), smaller (but large enough) values of the pressure, distributed on a larger portion of the wall, may excite a hydroelastic response of the structure. On this ground, both the pressure distribution and its time evolution are important for the structural analysis. Hydroelastic effects should be considered if the time duration of the loading ov er the analyzed structural part is the same order or smaller than the highest natural period for the considered structural part (F altinsen2001). These aspects are analyzed in the next section.

### 5.2.3 Fluid-Structure Interaction

In the follo wingthe influence of the h ydroelasticity is inv estigated. Top sketch in figure 5.14 giv es an example of longitudinal steel stiffeners adopted for the dek house in the bow region of a FPSO. The focus is on the effects on the stiffeners between deck 8 and deck 9 in the figure. This


Figure 5.14 Example of stiffeners of a deck house and cross-section of equivalent beam. Lengths are in millimeters.
is done byusing an equivalent Euler beam. The stiffener cross section is shown in the bottom sk eth. The upper portion of the deck house is assumed rigid.

Recent accidents for FPSO units documented in Ersdal and Kvitrud (2000), suggest to use a freeboard exceedance of 10 m . Here, the flow is started as the breaking of a dam located at the bow section, with a water reservoir $h=10 \mathrm{~m}$ high and $2 h$ long ( $c f$. figure 5.15). The beam, representing the wall of a deck house, is placed at $d_{s}=2.139 h$ from the dam, with length $L_{\text {beam }}=0.311 h$. The lower edge is clamped, while rotations at the upper edge are constrained bya spring with elastic constant $k_{\theta}$.

The deformation $w(z, t)$ of the beam is expressed in terms of the known dry modes $\psi_{j}(z)$ of the beam with unknown amplitudes $\zeta_{j}(t)$. Then the fluid-structure interaction is studied by coupling the nonlinear potential-fluid model with the linear-beam model by using the method explained in section 2.3. In the computations shown afterwards, the actual deformation $w(z, t)$ of the beam has been considered, i.e. the no-penetration boundary condition is enforced on the instantaneous configuration attained by the beam. We have also tested the effect of enforcing $\partial \varphi / \partial n=\partial w / \partial t$ on the undeformed beam and the results (not reported) are practically unchanged.

Left plot of figure 5.15 shows the initial condition, $\tau=t \sqrt{g / h}=0$, and a later free-surface configuration, corresponding to a run-up along the vertical wall of about $3 L_{\text {beam }}$. The flow generated after the impact is characterized bya narrow jet of water rising along the wall, also observed in the case of rigid wall studied in section 5.1.

The n umerical solution can be negatively affected byavariety of difficulties. F orinstance spatial and time resolutions decrease progressively for higher-order modes. F urtherconfluence of different boundary conditions at the edges of the beam implies locally a poorer convergence.


| meth. | $\boldsymbol{k}_{\theta}$ | R1 | R2 | R3 | $R j=\frac{T_{j} \text { wet }}{T_{j} \mathrm{dry}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| A | 0 | 2.74 | 2.26 | 1.93 |  |
| $B^{*}$ | 0 | 2.20 | 2.34 | 1.96 |  |
| A | -0 | 2.67 | 2.22 | 1.88 |  |
| $B^{*}$ | $\bigcirc 0$ | 2.50 | 2.20 | 1.87 |  |

${ }^{*} H / h=0.207$

Figure 5.15 Flow impacting with a vertical flexible wall after a dam breaking. Left: sk etc hof the problem and nomenclature adopted. Right: in the table, the "exact" solutions, $A$, for natural periods are compared with results from the simplified analysis, $B$, obtained bysolving the problem shown in the top plot.

Therefore, a simplified analytical analysis (top-right plot in figure 5.15) is also considered to qualitatively check the present results. The incoming water is approximated by a strip of fluid with constant height $H$, and the potential $\varphi_{j}$ due to $j$-th mode oscillations with unit amplitude is computed with $\varphi_{j}=0$ along the free surface. A solution is found by separation of variables and a F ourierexpansion of the mode overthe wetted surface. The related expressions are reported in appendix F . The height $H$ is a free parameter chosen b y the following considerations. In the approximate problem, it is found that the fluid further a wa $y$ than $\sim 0.8 L_{\text {beam }}$ from the beam is practically unaffected by the vibrations. Therefore $H$ is determined by imposing that masses of fluid inv olv ed in the apprximate and exact problems are the same. In this procedure, particles above the beam are neglected because their role in the h ydroelastic problem is expected to be small. This procedure giv esa $H / h=0.207$. One can of course question this procedure but the objective is to show that the n umerical results are reasonable.

The ratio natural wetted-period to natural dry-period $R j=T_{j \text { wet }} / T_{j \text { dry }}$ is computed and compared with results obtained by the "exact" problem. This comparison is tabulated for $j=1,2,3$ in the right of figure 5.15 for $k_{\theta}=0, \infty$ and shows a reasonable agreement, more evident for the higher modes, as one can expect since their sensitivity to the fluid details is smaller. Left plots in figure 5.16 give the time evolution of $\zeta_{j}$ for the first two modes, in the case of $k_{\theta}=0^{1}$. Late stages are presented in the right of the same figure for $j=1, \ldots, 4$. After the beam is completely wetted, $\Delta \tau_{\mathrm{imp}} \simeq 0.12$, the modes oscillate with almost constant period and amplitude. Both the value of $\zeta_{j}$ and the amplitude of oscillations decrease as the order of mode increases. This behavior does not change significantly when the parameter $K_{\theta}=k_{\theta} L_{\text {beam }} / E I$ is varied, where EI is the beam bending stiffness. Qualitatively, as $K_{\theta}$ increases the amplitudes decrease. The influence appears minor for the higher modes which are less sensitive to the boundary conditions. In general, $R j$ decreases as $K_{\theta}$ increases and is smaller for higher $j$ (see table in fighre7). The highest natural wetted-period changes from $\sim 0.018$ to $\sim 0.026 \sqrt{h / g}$ as one goes from $K_{\theta}=\infty$ to 0 . This means $T_{1 \mathrm{w}}$ et is small relative to the time to wet the beam.

[^2]




Figure 5.16 Modal amplitude as a function of time. Left: Time ev olution of the first tw omodes. Right: Enlarged view of the amplitude of the first four modes at large times after the impact.

| $\boldsymbol{K}_{\theta}$ | 0 | 6 | 24 | $\infty$ |
| :--- | :---: | :---: | :---: | :---: |
| $\boldsymbol{R 1}$ | 2.74 | 2.73 | 2.67 | 2.67 |
| $\boldsymbol{R 2}$ | 2.26 | 2.25 | 2.23 | 2.22 |
| $\boldsymbol{R} 3$ | 1.93 | 1.93 | 1.88 | 1.88 |
| $\boldsymbol{R 4}$ | 1.71 | 1.70 | 1.67 | 1.67 |



Figure 5.17 Left: ratio of natural wetted-periods to natural dry-periods for the first four modes of the beam. $K_{\theta}=k_{\theta} L_{\text {beam }} / E I$. Right: free surface for three different instants after the impact. Solid lines: rigid wall, o: h ydroelastic solution with $k_{\theta}=0 . \Delta \tau_{\mathrm{imp}}=0.024,0.13,0.24$.

It implies that the h ydroelasticity does not play an important role for the resulting maximum strains ( $c f$. F altinsen 2001).

The rigid wall results (solid lines) are compared with the clamped-supported beam results, ○, in the right plot of figure 5.17. Here the free-surface configurations at three instants of time after the impact are presented. The overall patternis not affected bywall deformation.
In figure 5.18, the maximum stresses ( $\sigma_{\max }$ ) on the beam are presented as obtained by a hydroelastic analysis and bya quasi-steady model. In the latter, we hav e considered a rigid structure to solve the h ydrodynamic problem, and the resulting loads are used to compute the static structural deformation. Fifteen mohlas vebeen used in the calculations.
F or the considered cases, maxima are alva ys observed at the bottom end. In particular (see left plot of figure 5.19) the fluid-induced bending moment gives tension stresses ( t ) in the wetted side, and compression stresses (c) in the opposite side. This is shown in the right-plot of figure 5.19 through the deformation of the beam at $\Delta \tau=0.12$ after the impact. Here the arrow indicates the direction of the incoming water. Concerning the maximum tension and compression bending


Figure 5.18 Maximum tension ( t ) and compression (c) stresses as a function of time. Quasi-steady (dashed lines) and hydroelastic ( $k_{\theta}=0$, solid lines) analyses.
stresses, the latter reach larger values than the former. This is because the cross-sectional neutral axis is closer to the wetted side. After the transient stage, the mean value of $\sigma_{\max }$ becomes nearly constant and remains with an absolute value less than 220 MPa . This is smaller than the steel yield stress but indicates that other inflow conditions may cause damage to the deck house. One notes that the magnitude of $h$ ydroelastic results oscillates around a mean value close to and slightly larger than the corresponding quasi-steady value. This confirms the unimportance of h ydroelasticity in this case.


Figure 5.19 Left: sketch of the loaded beam. Right: deformation of the beam at $\Delta \tau=0.12$ after the impact. $k_{\theta}=0$.

Chapter 6

## Approximated Methods for the Water Flow along the Deck

In the most common type of water on deck the water behav es qualitatively like the flow originated after the breaking of a dam. A certain region of the water will have a small depth relative to the wetted length.

These aspects lea veopen the possibility of using simplified approaches to analyze this phase of the complicated water-on-deck phenomenon. Questions arise, like: Can the shallow-water approximation be used for the water evolution along the deck? Does an equivalent dam-breaking problem exist for a given water shipping even $t$ ? If $y$ es, how to determine the right values of the parameters and of the conditions involved in the simplified analysis? These questions represent the topic of the next two sections where the applicability of these approximated analyses is in vestigatedb y examples. Their advantages and shortcomings are pointed out by using the n umerical method describedin chapter 3 as reference.

### 6.1 Shallow-Water Approximation

Shallow water approximation here indicates the simplified theory valid for nonlinear very long wa ves propagating in shallow water. This implies, nonlinearities of the problem are retained while dispersion effects are neglected. Such approximation is also referred as Airy's Theory (cf. Mei 1983). In the follo wing thefocus is on dam breaking-type of water on deck.

While close to the bow the dispersion effects remain in general important, a certain distance ( $x_{\text {shw }}$ ) from the bow can exist from where they become negligible. The horizontal velocity becomes then almost independent of the vertical coordinate $z$ and the flow can be described by the water height $(\eta-f)$ along the deck and the mean horizontal fluid velocity $u$. Here $\eta$ is the local waveelevation and $f$ is the freeboard. The shallow water equations require initial conditions for $(\eta-f)$ and $u$, as well as inflow boundary conditions (at $x_{\text {shw }}$ ).

This approximation has been analyzed bystudying the water flow along the deck in the experimental case by Cozijn (1995), described in chapter 4. Initial and boundary conditions (see left sketc h of figure 6.1) hav ebeen obtained by the present panel method and the problem has been solved $n$ umerically with the method of characteristics (see e.g. Mei 1983). Right plot of figure 6.1 giv esthe obtained results when $x_{\text {shw }} /(H-f)=2.2$ is taken as inflow boundary and $t_{\mathrm{in}}=13.19 \mathrm{~T}$ as initial instant in the shallow water problem. Here $H$ is the incident wave


Figure 6.1 Water on deck of a rectangular structure due to incident regularw aveswith $H=0.128$ m and $\omega=5 \mathrm{rad} / \mathrm{s}$. Left: sketc h of the shallow water problem. Right: n umerical free surface profiles obtained with the panel method (solid lines) and with the shallow water approximation (black circles). $t_{\mathrm{in}}$ is the initial time for the shallow water simulation. The panel method simulation starts at $t=0 \mathrm{~s}$.
height and $T$ is the waveperiod. F urther $t=0$ is the time instant of initial generation (in the panel method simulation) of incoming wa ves at a position $6 \lambda$ ahead of the deck structure. F orthis case of water on deck the maximum waveelevation in the vicinity of the bow ( $\eta_{\max }$ ) was about 2.1 times the incident wavecrest elevation. In the figure, the free surface profiles at three time instants after $t_{\mathrm{in}}$ are shown, given by the panel method (solid lines) and the shallow water approximation (black circles). The results agree quite well. However a majorbstacle in applying the shallow water theory in practice is due to the initial and inflow boundary conditions. Since they result from the wave-shipinteraction causing the water on deck, their estimate has to account for the in volv ednonlinearities and remains a difficult task.

An important additional limitation of the shallow water theory is the inability to handle water impacts with the deck house. The reason is simply that the resulting large variations in the vertical direction are inconsistent with the basic assumptions. The theory needs to be combined with some other method. When the flow is two-dimensional and the deck house has vertical sides at the impact position, locally the similarity solution for a fluid wedge hitting a wall at $90^{\circ}$ ( $c f$. chapter 5) can be used. The impact data, $\beta$ and $V$ (see sketch in figure 5.8), are given by the shallow water results. The impact pressure distribution along the structure can then be calculated for any structural distance from the bow. Assuming that initial and boundary conditions for the shallow water problem are properly given, the efficiency of this method depends on the importance of (i) three-dimensionality and (ii) gravit y effects (neglected in the similarity solution). This importance changes according to the location of the superstructure along the deck (i) and the sev erit yof the impact (ii).

This study documented the shallow water approximations can in principle be used in certain domains along the deck. However since they need initial and boundary conditions that are dependent on the external flow, they would in practice require data that are unav ailable without solving the complete ship-waveinteraction problem. This type of analysis is not suitable for solving water impacts with the deck house. In this case the coupling with a suitable local solution is necessary.

### 6.2 Dam-Breaking Model

An additional simplification of the problem can be obtained bystudying an equivalent dam breaking problem (see left sketch of figure 6.2). As in the shallow water approximation, also


Figure 6.2 Left: w ater on dek and equivalent dam breaking problem. Right: w ater shipping due to incident regular waves with $H / \lambda=0.06$ on the deck of a "deep" rectangular structure. Numerical free surface profiles (solid lines) are compared with dam breaking experiments from Dressler (1954, dashed lines). For the numerical results the vertical axis gives $(\eta-f) / h$, where $f$ is the freeboard, $\eta$ is the wave elev ation and $h=(\eta-f)_{\text {max }}$. F or the experimerts the same axis shows the water level referred to the initial height of the reservoir of water, $h$. The related $h$ is used in both cases to make non-dimensional the horizontal axis. The panel method simulation starts at $t=0 \mathrm{~s}$.
in this case the dependence of the water flow along the deck from the wave-shipinteraction causing the water on deck represents the main obstacle in finding the proper simplified model. This is here ev en more stressed. Indeed, if the height of the "equivalent" reservoir of water can be reasonably fixed $\mathrm{b} y$ the maximum freeboard exceedance b y the water, $h=(\eta-f)_{\max }$, the time instant when the dam breaks depends on the specific water on deck event due to the exterior flow. As an example, right plot of figure 6.2 shows the water on deck of a fixed structure with a "deep" (relative to the wav elength $\lambda$ ) vertical bow caused by incident regular waveswith $H / \lambda=0.06$. Numerical free surface profiles at four time instants (solid lines) are compared with the experimental dam-breaking results by Dressler (1954, dashed lines).

In the experiments the length of the reservoir of water is long compared with the reservoir height, and it does not influence the results. When comparing with Dressler (1954), there is an ambiguity in how to select the equivalent height $h$ of the reservoir and when the dam breaks. Here the following decisions are taken. $h$ is chosen equal to the maximum freeboard exceedance
by the water during the shipping, $(\eta-f)_{\max }$. The time instant of dam breaking is taken as $\sqrt{h / g}$ after the water shipping started. This value is obtained $\mathrm{b} y$ tuning the dam-breaking and water-on-deck free surface ev olutions. Its difference from the time of the shipping starting quantifies in a way the importance of the following error sources: (i) in the dam-breaking model the water reservoir has its maximum level when the dam breaks while at the beginning of the shipping the freeboard exceedance by the water at the bow is zero and increases reaching only after some time its maximum value, (ii) in the dam-breaking thedel water flow is driven by the gravit y while during the shipping the waveconditions outside the deck determine a more complicated driven force system.

Qualitatively the two results confirm the agreement observed experimentally in Buchner (1995), however differences exist both for the water level and for the flow velocities. These differences are clearly due to the wavekinematics inv olved in the water on deck. The specific local wav econditions at the bow enhance or reduce those differences. F or the case shown in the right plot of figure 6.2, the differences between the flow caused bya dabreakimgnd the flow along the deck can be quantified in terms of the consequences on a vertical wall hit by the water. Since the angle $\beta$ ( $c f$. sketch of figure 5.8 ) is small for both the flows (less than $15^{0}$ ), the velocity $V$ is the important impact parameter. The square of the ratio between the (mean) velocities associated with the dam-breaking $\left(V_{\mathrm{db}}\right)$ and the water-on-deck ( $V_{\text {wod }}$ ) problems can be interpreted as the ratio between the maximum pressures on the wall. This ratio is $\left(V_{\mathrm{db}} / V_{\mathrm{wod}}\right)^{2} \simeq 1.67$, indicating a large error in impact pressure predictions. It is worth noting that if the shallow water dam-breaking solution ( $c f$. Ritter 1892) was used, the related impact velocity should be even higher than $V_{\mathrm{db}}$ ( $c f$. figure 1.6and section C.3). This means too conservative estimates of impact loads ona deck house in the bow area.

These results document that a theoretical dam-breaking model can only qualitatively describe the flow on the deck since it does not account for the horizontal fluid motion caused by the flow external to the ship. The latter can significantly influence the characteristics of water impacts with superstructures along the deck.

## Chapter 7

## Two-Dimensional Water-on-Deck Experiments

Two-dimensional water on deck model tests have been carried out in the narrow waveflume at the Department of Marine Hydrodynamics of NTNU. The general objectives of the experimental study are both the $v$ alidation of the $n$ umerical model and a direct in vestigationof the phenomenon. In this chapter, the experimental set-up is described and observations are documented and discussed. Main error sources which may affect the experiments are also indicated and commented.

### 7.1 Choice of Relevant Parameters

Two-dimensional experiments have been realized to study water-on-deck phenomena for a restrained (nearly) rectangular-shaped model.

As we said, focusing our attention on FPSO-type ships, the experimental set-up has been designed by using the DWT FPSO (Buchner 1995) and the Norne (see left plot of figure 1.2, Statoil) as reference for the ship parameters. Experiments of water on deck in regular wa ves b y Buchner (1995), on a three-dimensional model, and by Cozijn (1995), for a two-dimensional configuration, have been examined to determine the suitable wave parameters.Finally, we have also kept in mind the overviewof recent FPSO accidents giv enb y Ersdal and Kvitrud (2000). A summary of the relevant information collected from the above reference sources is presented in the follo wing list. The used symbolsare summarized in figure 7.1.

1) Ship length: $L / D$ is $\simeq 15$ for DWT FPSO and $\simeq 13$ for Norne.
2) F reeboard:design freeboard-to-draft ratio is $\simeq 0.507$ for DWT, and $f / D \simeq 0.76$ for Norne. When Norne accident occurred on March 1998 (cf. Ersdal and Kvitrud 2000), the ship was almost fully loaded with a mean freeboard $f=8 \mathrm{~m}$, resulting in $f / D \simeq 0.35$.
3) Stem angle: both ships have an almost vertical bow below mean waterplane. The upper portion of the bow is inclined outwards, with an angle of $\sim 37$ and $\sim 36$ degrees, respectively.
4) Deck house: Norne has a deck house located at $d_{s} / D \simeq 1.3$ from the bow.
5) Critical sea states: according to the overviewof FPSO accidents by Ersdal and Kvitrud (2000), the recorded sea states responsible for water-on-deck even ts vere normally characterized by log w aves, that is wave lengths of order of the ship length, and usually greater than 200 m in the case of FPSO units. Significant wa ve heights associated with the critical sea states varied between 7 and 13 m . This corresponds to largest waveheights $H_{M}$ of approximately 14 and 26 m , respectively. P eak periods $T_{p}$ were between 11 and 13 s . With the parameters above, combinations ( $H_{M}, T_{p}$ ) imply a broad range of wavesteepnesses.
6) Regular wavelength: in 3-D Buchner's experiments, wavelength-to-ship length ratios $\lambda / L=0.75,1,1.25$ were considered, giving $\lambda / \mathrm{D} \simeq 11,15,19$, respectively.
7) Regular wavesteepness: in 3-D Buchner's experiments, steepness values of $H / \lambda \simeq 0.066$, 0.088 have been analyzed. A steepness $\sim 0.052$ was studied during 2-D experiments by Cozijn.


Figure 7.1 Nomenclature adopted for the main geometrical parameters considered.
In addition to data above, thet wo-dimensional numerical analysis discussed in chapter 4 has been taken into account. F rom numerical results, the ship length does not directly influence the amount of shipped water as long as it is large relative to the draft, and as long as the ship is restrained from oscillating. Since the wave-inducedship motions are not studied in the tests, this gives some freedom when deciding the ratio $L / D$. In particular, $L / D$ can be chosen a bit smaller than in real cases to achieve a good compromise between test scale and flume dimensions. In particular, if the scale is too small, important surface-tension effects would significantly affect the water shipping and the flow evolution along the deck. On the other hand, for large scales, long wa ves have to be generated and a larger influence of the bottom of the flume would be expected, causing steeper waveconditions and occasionally wavebreaking. This would prevent the comparison with our $n$ umerical simulations. In addition, for wav elengths large relative to the flume dimensions, the model would be relatively closer to the wavemakr, th usimplying more pronounced local effects and wa vereflection.

Heave and pitch motions cause a time variation of the ship freeboard relative to the mean waterplane. This has been taken into account when deciding the freeboard of the fixed model. In particular, $f$ has been chosen to giv e realistic values of freeboard exceedance during the
water shipping. The final chosen $f$ was also based on preliminary n umericalstudies, resulting in freeboard smaller than the ship freeboard in calm water.

This information, together with practical aspects related to av ailable instrumertation, wa veflume characteristics, costs and other factors determined the experimental set-up, discussed in the follo wing sections.

### 7.2 Description of the Experimental Set-up

### 7.2.1 Equipment

The flume Two-dimensional water-on-deck model tests hav e been performed in a narrow wave flume. The flume is 13.5 m long, 1.035 m deep and 0.6 m wide. The sides are 19 mm thick glass-plate made to permit flow visualization during tests.
Incoming waves are generated ly a flap wa vemaker hinged at 0.1 m from the bottom. A parabolic beach at the opposite end of the flume reduces the wavereflection. The wavemakr is equipped with a control system constructed by Edinburgh Designs. This is based on monitoring hydrodynamic forces acting on the flap. Details of how the feedback in the system works to counteract the presence of unwanted reflected wavesat the wavemakr is proprietary information.
The position of the model is determined by considering sufficient distance from the wa vemaker to a wid local effects from the flap. F orthe considered waveperiods, we placed the model at $\simeq 5.54 \mathrm{~m}$ from the wavemakr.
Another restriction is given by the optical window seen by the video equipment, with the widest observed-flow area of about 3 m .

The ship model A simplified two-dimensional ship model has been used in the tests, with three different bows, sk etc hedin figure 7.2. The basic configuration is characterized by a trans-


Figure 7.2 Water-on-deck at the bow of a 2-D ship. Bow geometry of the considered models. Side view.
parent nearly rectangular body (a) with draft $D=0.198 \mathrm{~m}$, length $L=1.5 \mathrm{~m}$, freeboard $f=0.05 \mathrm{~m}$ (cf. sketch in figure 7.3). This means $L / D \simeq 7.6$ and $f / D \simeq 0.253$. The model is made in plexiglas. The front part of the transparent model has been placed at $\simeq 5.54 \mathrm{~m}$ from the vertical wavemakr position $\left(\mathrm{wm}_{\mathrm{ver}}\right)$, while the aft part is about 6.46 m far from the opposite side of the flume.

Due to the chosen freeboard, the height of the glass side above the deck is $\sim 0.215 \mathrm{~m}$, as indicated by the double arrow in the side view (right picture) in figure 7.3. In order to take
video images of the water shipping, this height has to be large enough relative to the inv olv ed water lev el along thedeck. Also this deternthed choice of the test scale.

The bottom corner at the bow has a radius of curvature $r=0.08 \mathrm{~m}$ to avoid vortex shedding. The value of $r$ was decided by carrying out a simplified analysis. In particular, in case of oscillatory ambient flow with amplitude $\eta_{a}$ around a fixed horizontal circular cylinder of radius $r$, the experimental threshold (cf. F altinsen 1990) for almost-zero vrtex shedding is

$$
\mathrm{KC}=\frac{U_{M} T}{2 r}=\frac{\pi \eta_{a}}{r}<\sim 3
$$

where KC is the Keulegan-Carpenter number, and $T$ and $U_{M}$ are the period and the velocity amplitude of the ambient oscillatory flow, respectively. By setting $\eta_{a}$ equal to the largest wave amplitude considered in the tests, 0.08 m , we obtain a limit radius $r$ of about 0.08 m . Clearly, this analysis is simplified since it does not account for theomplete model shape. However flow visualization did not detect any vortex shedding during the tests.

In the other configurations, the bow has a stem angle of 45 (b) and -45 (c) degrees, respectively. The remov able bow part is made by divinisel, which, although not transparent, is easier to shape.

Finally, the model is restrained from oscillating in all the tests we performed.
Side, top and lateral views of the experimental set-up together with the definition of main geometric parameters are giv enby figures $7.3,7.4$ and 7.5. In the case of the vertical-bov


Figure 7.3 Water-on-deck at the bow of a 2-D ship. Experimental set-up, main parameters involved and used sensors. Side view.
configuration, tests have been performed both without and with a vertical wall on the deck, located at $d_{s}=0.2275 \mathrm{~m}\left(d_{s} / D \simeq 1.15\right)$ from the bow. Configurations (b) and (c) have been tested only without superstructure. The vertical wall is transparent and made by plexiglas. It is rectangularly shaped, $\sim 0.60 \mathrm{~m}$ large, 0.30 m high and 0.012 m thick. F ourequi-spaced vertical stiffeners on the badk side of the wall (see right plot of figure 7.4 and left photos of figure 7.5) have been in troduced. Among them, the most external ones are placed at the ends of the structure. The stiffeners hav e rectangular cross sections and the same height as the wall. The cross section is $0.033 \mathrm{~m} \times 0.012 \mathrm{~m}$, where 0.033 m corresponds to the side length orthogonal to the wall.
crest of a regular wavetrain. This has to be kept in mind because we will focus on the first water-on-deck event which, in our case, is determined by the interaction of the bow with a highly non uniform wavetrain. Therefore, we have accurately measured the 'actual' wavesinteracting with the model, characterized by the first crest steeper than the wa vesthat would be generated by the wa vemaker for the selected frequency and amplitude after a very long time, in the absence of the body. In our experiments, the latter condition has never been reached.

The instrumentation The used instrumentation is characterized by

- two capacitive waveprobes (with 3 mm diameter) located along the flume: $\mathrm{wp}_{1}$ at 0.8 m from $\mathrm{wm}_{\text {ver }}$ (see sk etc h 7.3 ) and $\mathrm{wp}_{2}$ at 0.104 m from the bow.
- three capacitive waveprobes spaced 0.075 m from each other and placed on top of the deck. When the superstructure is not used, the $\mathrm{wl}_{1}$ center is at the bow. When the wall is introduced, $\mathrm{wl}_{3}$ center is at 0.0405 m from the vertical wall.
- two capacitive wa veprobes along the deck $\left(\mathrm{fd}_{1}, \mathrm{fd}_{2}\right)$.
- one capacitive waveprobe along the vertical superstructure (fw).
- three piezoelectric pressure gauges (diameter of 3 mm ) along the vertical superstructure: $\mathrm{pr}_{1}$ and $\mathrm{pr}_{3}$ at 12 mm from the deck and horizontally spaced 15 cm from each other, $\mathrm{pr}_{2}$ at 32 mm from the deck.
- one digital video camera with a standard 25 Hz sampling frequency.

Wave probes on the ship model are daracterized by two thin metallic ribbons 5 mm wide glued with a separation distance of 5 mm , and finally calibrated in situ. These sensors are used to ev aluate the vater level along the deck $\left(\mathrm{wl}_{1}, \mathrm{wl}_{2}, \mathrm{wl}_{3}\right)$, and to measure the wa ve froft propagation along the deck $\left(\mathrm{fd}_{1}, \mathrm{fd}_{2}\right)$ and during water run-up along the vertical superstructure (fw). The sampling rate of the measured data is generally 100 Hz .

### 7.3 Reliability and Repeatability of the Measurements

Repeatability of the tests has been checked. Here, we consider prescribed (nominal) incoming wa ves with $\lambda=2 \mathrm{~m}$ and $H=0.16 \mathrm{~m}$. Figure 7.6 shows the time histories of the wav eelevation at 0.8 m from $\mathrm{wm}_{\text {ver }}\left(\right.$ left plot, $\left.\mathrm{wp}_{1}\right)$ and at $0.104 \mathrm{~m}\left(\right.$ righ t plot, $\left.\mathrm{wp}_{2}\right)$ from the bow. The basic model with vertical bow is used during the experiments. The curves are related to seven different tests. The measurements agree quite well, though some tests show a certain deviation from the majority. This is mostly true at the beginning of the time evolution, when the sensitivity and dependence on the initial wave conditions in the flume are the largest. The water-level evolution along the deck is presented in figure 7.7. The waveprobes are placed at the bow (top left plot, $\mathrm{wl}_{1}$ ) and at $0.075 \mathrm{~m}\left(\right.$ top right plot, $\left.\mathrm{wl}_{2}\right)$ and 0.15 m (bottom plot, $\mathrm{wl}_{3}$ ) from the bow. The first two water-on-deck even ts are shown and for both of them the incoming wave is steeper than the nominal regular waveprescribed by the wa vemaker settings. The second event is characterized


Figure 7.6 Repeatability of the w avelevation measured bywp (left) and $\mathrm{wp}_{2}$ (right). Seven test results are plotted.
by a larger amount of shipped water than the first one. This is because the wav ecrest reaching the bow steepens because of reflected waves. The repeatability of the measured data appears acceptable, though less good in this case. An important reason is the formation of a cavity of air at the beginning of water on deck, as it will be extensively discussed in section 8.2. In this context, important factors are represented by the high transient behaviour of the cavit y and by the sensitivity of the sensors to the rate of change of the wetted length along the two strips of each sensor.

The propagation of the wavefront along the deck ( $\left.\Delta x_{\text {bow }}=x_{\text {w ave front }}-x_{\text {bow }}\right)$ is analyzed in the left plot of figure 7.8 , which shows a satisfactory repeatability of the experiments. The maximum value reached by the front is about 0.25 m , which is consistent with the length of the metallic ribbons forming the sensor. The water front covers in reality a longer distance than the length of the probe. In the later stages of the first water on deck, the wetted length measured decreases reaching a minimum ${ }^{1}$. After that, it increases due to the starting of the next even $t$, which follo ws asimilar evolution cycle.

The right plot of the same figure gives the comparison between the results obtained with sensors $\mathrm{fd}_{1}$ and $\mathrm{fd}_{2}$, for one of the tests. The probes attain non-zero values at the same time instant, and the curves fit quite well until the end of the first water on deck. This confirms the two-dimensionality of the flow. Differences are observed during the following stages. However, as observed, in this phase the reliability of the measurements is questionable, and the difference is not related to three-dimensional effects, which are negligible according to the analysis of video

[^3]


Figure 7.7 Repeatability of the water level measured by wl (top left) and $\mathrm{wl}_{2}$ (top righ t ) and $\mathrm{wl}_{3}$ (bottom). Seven test results are plotted.
images ${ }^{2}$.
The measured data commented so far refer to a model without a vertical wall on the deck. In figure 7.9 , we consider tests with a vertical wall at 0.2275 m from the bow. The left plot shows the evolution of the wavefront measured $b y f_{1}$. The maximum value measured of the wave front is less than the expected one $(0.2275 \mathrm{~m})$ in this case. The strips of the sensor are longer $(0.25 \mathrm{~m})$ than the wall distance from the bow. This suggests that errors in the measurements are probably associated with the specific flow details close to the wall.

[^4]

Figure 7.8 Left: repeatability of the wave frott propagation measured by $\mathrm{fd}_{1}$, without superstructure along the deck. Seven test results are shown. Right: comparison of $\mathrm{fd}_{1}$ and $\mathrm{fd}_{2}$ measurements for one of the tests, without superstructure along the deck. Five test results are shown.

The vertical wall reflects the water propagating along the deck. This makes the water on deck phenomenon faster relative to the case without the wall. F urther the water level along the deck


Figure 7.9 Left: repeatability of the wavefront propagation measured by $\mathrm{fd}_{1}$, with a superstructure along the deck. Right: repeatability of the water run-up along the vertical superstructure measured by fw. Five test results are shown.
increased and does not become zero between one water-on-deck event and the next one. This is confirmed by the measurements in left plot of figure 7.9 where the wetted length remains almost constant after it has reached a maximum value.
Right plot of the same figure giv esthe ev olution of the water run-up along the wall. Five test
results are shown. As one can observe the repeatability is quite good until the maximum is approached. Then the measurements show a certain difference. The video images show that the flow becomes unstable and three-dimensional during the water rise-up. This explains the differences in the results.
The pressure measurements are analyzed in the plots of figure 7.10. In the left, the pressure measured at 0.012 m from the deck $\left(\mathrm{pr}_{1}\right)$ is examined. F our testresults are shown. In this case


Figure 7.10 Left: repeatability of the pressure ev olution measured by pr ${ }_{1}$. F our test results are shown. Right: comparison of $\mathrm{pr}_{1}$ (lines with squares) and $\mathrm{pr}_{3}$ (lines with circles) measurements. Two test results (full and empty symbols) are shown for each gauge.
the measurements appear similar but not perfectly repeatable. This is both due to the threedimensional effects appearing during the water run-up along the wall and to the sensitivity of the measured pressure to the specific flow and environmental conditions. The latter represents a key factor for the reliability of the pressure measurements. In the right plot, the pressure evolutions at $\mathrm{pr}_{1}$ (lines with squares) and at $\mathrm{pr}_{3}$ (lines with circle) are compared. Two test results (full and empty symbols) are shown for each gauge. The differences between the two sensors results are of the same order as those between results from different tests for the same gauge. This confirms the important role play ed by the pressure sensitivity to the physical conditions, but it does not exclude the influence of three-dimensional effects. However, these start to matter when the water front, rising along the wall, is already far from the pressure sensors and, at least at the beginning, remain localized in the front region.

A cross-check of variables measured on the model was performed to guaranty their reliability. An example of this is given in figure 7.11, where a good agreement between different sensors is documented. The case refers to the first water on deck due to a nominal incoming wavewith length $\lambda=2$ mdan height $H=0.16 \mathrm{~m}$. No vertical wall was used on the deck. Solid line gives the evolution of the wavefront along the deck measured $b y$ the sensor $\mathrm{fd}_{1}$. Lines with squares, circles and rev ersedtriangles represent the water level ev olutionalong the deck measured with $\mathrm{wl}_{1}, \mathrm{wl}_{2}$ and $\mathrm{wl}_{3}$, respectively. The center of the sensor $\mathrm{wl}_{1}$ is at the bow and the centers of the others are respectively at 0.075 m and 0.15 m from the first one. As one can observe the $\mathrm{fd}_{1}$ measurement becomes different than zero almost at the same time instant as the one of $\mathrm{wl}_{1}$. The small delay in the wavefront measurement can be explained by the fact that (cf. chapter
8) the deck is not wetted just after the freeboard is exceeded, but a plunging waveis formed. When this one impacts on the deck the wetting starts. The plunging and impact phenomena are quite rapid in this case, with the impact occurring at about 0.13 s from the instant of freeboard exceedance. As a consequence of the plunging impact a ca vit yis formed that collapses during the water evolution. This explains the better agreement between the $\mathrm{fd}_{1}$ and the following water lev el sensors. As one can observe, the wavefront measured by $\mathrm{fd}_{1}$ reaches thev alues of 0.075 m and 0.15 m almost when $\mathrm{wl}_{2}$ andvl $3_{3}$, respectively, become different than zero.


Figure 7.11 Cross-chec k:w a front propagation $\left(\mathrm{fd}_{1}\right)$, water level at the bow ( $\mathrm{wl}_{1}$ ), at 0.075 m from the bow $\left(\mathrm{wl}_{2}\right)$ and at 0.15 m from the bow $\left(\mathrm{wl}_{3}\right)$.

### 7.4 Error Sources in the Measurements

Both when the experimental set-up is designed and when the results from the tests are analyzed, it is crucial to determine and keep under control possible error sources in the measurements. This can give guidelines for the former process and fixes the validity and reliability limits of the experimental results. The main error sources are analyzed in the follo wing text.

### 7.4.1 Flume

Seiching in the flume Seiching indicates the presence of longitudinal standing wavesin the tank, with wavelength twice the tank length. Since the latter is muc hlarger than the flume depth, this is a shallow water phenomenon. The actual length-to-depth ratio is $b / h \simeq 13.04$ in the tests, where $b=13.5 \mathrm{~m}$ and $h=1.035 \mathrm{~m}$. Since seic hing represents an error source in the
actual waves generated in the flume it is importart to control this resonance phenomenon in the tank.

The parabolic beach at the opposite side of the wavemakr influences the time necessary for the standing wavesto be set up $\left(t_{\mathrm{sw}}\right)$. However, since it is not designed for such long waves, its absorption efficiency is poor. A first estimate of $t_{\text {sw }}$ can thus be obtained by neglecting the beach and simply considering a rectangular tank. The group velocity for shallow water wav esis $c_{g}=\sqrt{g h}$. This means, the long disturbances generated $\mathrm{b} y$ the wa vemaker reach the opposite side in $b / c_{g} \simeq 4.24 \mathrm{~s}$ after start up and return to the flap after $2 b / c_{g} \simeq 8.47 \mathrm{~s}$. The latter can be taken as a measure of $t_{\mathrm{sw}}$. Once the seic hingis excited the wa ves generated b y the wa vemaker are altered in the flume bythe standing aves. This gives a higher frequency signal modulated by a lower frequency env elope. The latter is associated with the natural period of the flume that can be evaluated by applying the shallow water expression for the highest natural (sloshing) period (cf. F altinsen 1990)

$$
T_{N}=\frac{2 b}{\sqrt{g h}} .
$$

This gives $T_{N} \simeq 8.5 \mathrm{~s}$ in the present case. In figure 7.12 the angle of wavemakr oscillation $(\alpha)$ is shown for the case of nominal wavewith $\lambda=2 \mathrm{~m}$ and $H=0.16 \mathrm{~m}$. The ship model was not used during the test. $\alpha$ does not correspond to the prescribed wavemakr motion but has


Figure 7.12 Wavemaler motion: angle of oscillation (solid line) and its en velope (dashed line). A positive angle corresponds to a flap rotation tow ards the tank.
been directly measured. This was done since the actual wa vemaker motion does not coincide in general with the one set. Indeed, when wavereflection occurs an automatic control system adjusts the flap motion to ensure the desired waveconditions in the flume. F rom the figure, the first part of the time history shows clearly a modulated env elope of the wa vemakr motion, with period consistent with flume natural period. It is difficult to detect when the seic hingstarts to influence $\alpha$ since the initial wavemakr motion is characterized by a ramp function of 2 s . As
the time increases, the low frequency oscillations of the env elope reduce in amplitude due to the control system. In later stages they become negligible.

Seiching modes are excited at the beginning of each experiment, regardless the ramp adopted to start the motion which has to be reasonably short to be of practical use. In principle, it could be possible to use active waveabsorbers on the other side of the tank to reduce if not eliminate the seic hing mode. In the absence of such devices, we cannot avoidthe presence of the slo wly varying oscillations due to these standing waves. The time in terval from one experiment and the following can be made longer but the decay time is rather long because we are dealing with rather long waves. What matters is controlling that: (i) the residual amplitude of the seiching mods small compared with the waveheights we are going to measure, and (ii) the time scale of the seic hing period is not close to those in volved in our experiments. In the specific case of our experiments, boththe requirements are met well.

Initial conditions in the flume A certain time interval is necessary between each test for wavemotions and parasite currents in the flume to die out, and to ensure the same initial conditions in the flume for each test. If the time interval between two follo wingtests is not large enough, the results from test to test can vary in a percentage that depends on the error in the initial conditions and on the sensitivity of the specific measured quantity to the initial conditions. On the other hand, constraints exist also in the other direction. In particular, as it is discussed later in the section, pressure measurements require a strict control of the temperature and of the wetting of the gauges. This limits in practice the duration of the time in tervals between tests. Different in terval durations have been used. A mean value of 5 min was found to be a reasonable compromise of the competitive requirements.

Environmental conditions The environmental conditions are very important for the quality of the test results. The latter can not be achieved if the two following aspects are not accounted for.
First, it is crucial to keep environmental c hanges small during eadı test. From this point of view the temperature represented a key factor in the reliability of the pressure measurements. Second, it is fundamental to control/avoid en vironmertal disturbances in the experimental results. F or instance, the 50 Hz current of the general power system may cause unphysical 50 Hz oscillations in the sensors output. Therefore 40 Hz filter was used in processing measured data to avoid this possible disturbance.

### 7.4.2 Instrumentation

Cavitation and vertilation of the waveprobes The waveprobes used in the flume are cylindrical sensors with a 3 mm diameter. In principle they are capacitive sensors measuring the wetted surface of the cylinder and giving as output the instantaneous elevation of the wave passing by as the time increases. This is given as a mean value among those measured along the circumference of the cylinder. This type of waveprobe is thus not able to measure the free surface configuration in the case of breaking wa veoccurrence.

Close to the probe, surface tension effects matter and alter locally the free surface. This represents an error source in the waveelevation measurements. The latter is expected to be within $\sim 1 \mathrm{~mm}$. The environment where these sensors operate is an oscillatory motion with main period equal to the one of the wavesystem generated in the flume. If the ambient horizontal velocity at the wave probe is too high en tilation can occur at the wa ve probe. This phenomenon has been studied by Wetzel (1958) in a steady current. Related results have been applied to the waveprobe byusing a quasi-steady approach. The reason for doing this is that the KCnumber associated with the oscillatory flow past the wa ve probe would be high ( $83<\mathrm{KC}<168$ ). Environmental conditions have been approximated bythose of a surface piercing cylinder in a slo wly varying current with depth independent velocity. Limit of the velocity values exist (more precisely limit of a related F roudenumber) above which ven tilationand cavitation phenomena occur on the probe. F or the reliability of the experimental results it is crucial to be always under that limit. Otherwise the wav efield close to the "cylinder" is characterized not only by a local water run-up (i) in the body front but also by an important local run-down (ven tilation, ii) in the downstream part. Physically this corresponds in the horizontal plane to respectively an upstream ov er-pressure and a dovnstream under-pressure. In Wetzel (1958) the threshold value for the F roudenumber defined as $U / \sqrt{g D}$ ( $U$ is the current velocity, $g$ the gravity acceleration and $D$ the draft of the cylinder) is given in terms of the geometric parameters of the problem. F or a probe diameter of 3 mm this gives an upper limit of $\sim 1.2 \mathrm{~m} / \mathrm{s}$ for the current velocity without ven tilation. In the performed experiments, the orbital velocity for the prescribed incoming wa ves was at most $0.44 \mathrm{~m} / \mathrm{s}$. This value is below the threshold velocity. As already pointed out (cf. section 7.2) and as it will be extensively discussed later (cf. section 8.1), the actual wave conditions in the flume were not the same as the prescribed ones during the tests. However, this does not compromise the obtained result.

In a preliminary step, cylindrical wa ve probes have also been considered for the measurements on the deck, with diameter of 2 mm . The value of the diameter was chosen as a compromise between different relevant aspects. In particular, the diameter has to be as small as possible to reduce the in trusion, namely the disturbance of the flow field during the delicate phase of the shipping. On the other hand, a too small diameter will not giv ea sufficiently stiff structure to withstand the hydrodynamic loads. In this case an additional support along the wa ve probe may be necessary. For the chosen value of the diameter the upper limit of a current velocity without ven tilation is aboutl. $4 \mathrm{~m} / \mathrm{s}$. Clearly results in Wetzel (1958) are not directly applicable to the case of in terest. However his results indicate possible problems in the measurements for flow velocities of that order of magnitude. Both preliminary numerical studies, made for dimensioning the experimental set-up, and experimental results, confirmed that during the studied water on deck phenomena the wa ve front velocities become order of $1 \mathrm{~m} / \mathrm{s}$. F or these reasons less intrusive waveprobes have been used for the evaluation blfe w ater level evolution during the shipping, described in the follo wing paragraph.

Waveprobes on the model All the waveprobes used on the model $\left(\mathrm{wl}_{1}, \mathrm{wl}_{2}, \mathrm{wl}_{3}, \mathrm{fd}_{1}, \mathrm{fd}_{2}\right.$, fw) are characterized bytwo metal strips 5 mm wide, placed parallel to each other with a 5 mm separation. Also these are capacitive. Main advantages of the specific set-up are the small in trusion of the probe and its tersatility. The latter quality refers to the ease of using the probe in different contexts. In the present case, for example, this type of sensors is used to evaluate
the water level along the deck when the shipping occurred, the wave frort propagation along the deck and its run-up along the vertical wall. The measured value corresponds to the av eraged wetted length of the two strips. It is th usimportant to keep small their separation, otherwise the prediction, for instance, of the local water slope can not be sufficiently satisfactory when the water level is measured. Similarly as for the probes described in the previous paragraph, they can not be used to predict the real free surface configuration when breaking waves and in general ca vitation phenomena occur. F orthe water front ev olutionalong the deck, an error source is related to the ca vit yformation due to the plunging impact near the bow. This phenomenon is described in details in chapter 8. After the water hit the deck, two jets develop in opposite directions of the deck. In this phase the rate of change of the strips wetted length accounts for the ev olutionof both jets. Only after the cavity collapsed the strips wetted length is related to the flow going away from the bow. But bubbles, caused by the cavity collapse, are mixed to the water and represent an error source for the measurements.

Phase delays in the waveinstrumentation In the present experimental arrangement, the electronic equipment driving our waveprobes (both in the flume and on the ship model) in troduces a frequency dependent phase shift which has not been fully characterized in our experiments (this is possible by a dynamic calibration procedure). Moreov er, the phase responses of the probes, in principle, are not the same. This is the main reason for the different phase delays detected for the sensors $f d_{1}$ and $f w$.

Pressure gauges Changes in the temperature due to dry-wet-dry cycles of the pressure gauge conditions can cause a significant shift in the zero value given by the sensors. If this occurs during a measurement, the related results become practically unuseful. To ca trol as much as possible this error source no lamp has been used during the tests. It implies that additional tests were performed for taking the video images. F urther, a great effort was made to keep the pressure cells almost contin uously wet. In particular, a wet towel was applied on the cells between a test and the next one. This was needed to ensure the same conditions and thus the same zero lev el before and after each test. In the later stages of the water on deck event the water level is lo ver than the pressure gauges. This means the sensors should measure atmospheric pressure. This is a good indication of the reliability of the pressure measurements and has been used to check the results from the data base.

Video images We found it effective to take measurements of free-surface profiles by using frames grabbed from the recorded video images. Clearly, also this procedure is affected by uncertainties and possible errors.

First of all, the axis of the video camera lens is aligned with some reference axis on the model, say the edge of the deck at the bow. Therefore, as we move from the focusing point of the lens outwards an error is in troduced in the distances. F urther, the focusing of the optical system, adjusted on the closest side of the water flume, is progressively notcorrect as we movetowards the boundary of the av ailable optical window.

Meniscus effects tend to spread the contact line between the free surface and the lateral tank wall. A similar uncertainty is introduced by the fact that glass walls remain wetted. In
particular, when the water level decreases, a thin layer of water "following" the contact line can be seen. Actually, by adjusting properly the source of light, both effects do not introduce a significant uncertainty in determining the waveprofile along the wall.

We found more important error source the non-perfect perpendicularity of the lens axis to the lateral wall of the flume. In such unlucky cases, the large distortion of the lengths in the plane of the image due to the perspective error preven tscompletely a reliable measurement of the waveprofile.

### 7.4.3 Model

Defects in the model set-up A gap of about 1.5 mm was caused by the imperfect connection in the middle of the deck, between the deck and the vertical wall. Thgap has been co vered by using copper tape, but a certain influence in the results is expected since in this way the deck is not perfectly horizontal.

An offset of $\sim 2 \mathrm{~mm}$ was observed in the divinisel appendix with $45^{\circ}$ (case b in figure 7.2). Due to this, the fore portion of the deck was not perfectly horizontal and the actual stem angle was reduced by 0.57 degrees. In addition, due to the connection mechanisms of the appendix with the rest of the model (only two screws aligned along a horizontal line were used) pitch motion was excited by the loading conditions during the run-up of the water along the bow and the follo wingwater shipping. Related amplitude was howev ersmall. In connection with this, leakage phenomena occurred from the model sides making practically unuseful the water lev el probes along the deck for the tests with this bow geometry.

Elastic behavior of the wall If the loading time of the vertical superstructure is small or comparable with the natural wetted-period of the wall, $h$ ydroelastic effects become important. Since rigid wall conditions are of in terest in present experiments, the wall set-up (cf. section 7.2.1) has been decided to preven $t$ this phenomenon. The fact that hydroelasticity did not matter during the experimental water impact with the wall has been verified by applying the developed n umerical model to the problem. This giv es $\sim 0.14 \mathrm{~s}$ as a measure of the loading time, here taken as the time for the water to rise about the $40 \%$ of the wall. Numerical results were then used for a simplified analysis as described in the follo wing text.

The wall is substituted by an equivalent beam described in figure 7.13, with highest natural dry-period

$$
T_{1, \mathrm{dry}} \simeq 2 \pi\left(\frac{L_{\mathrm{beam}}}{4.73 \pi}\right)^{2} \sqrt{\frac{\rho_{\mathrm{plex}} A}{\mathrm{EI}}} \simeq 0.00011 \mathrm{~s}
$$

Here $\rho_{\text {plex }}$ is the plexiglas density, $A$ is the cross-section area and $L_{\text {beam }}$ is the beam length. $T_{1, \text { dry }}$ is very small compared with the n umerical loading time. This result is in principle not conservative, since one expects the natural wetted-period to be larger than $T_{1, \text { dry }}$, due to the added mass contribution. However, if we use the $n$ umerical analysis conducted in chapter 5 as a reference, $T_{1, \mathrm{w} \text { et }}$ should be at the most three times $T_{1, \text { dry }}$. This rough estimate suggests that with this set-up the experiments are not affected by elastic oscillations of the wall, as confirmed by the test results. In particular, the pressure recordings do not show suspicious oscillation frequencies.


Figure 7.13 Cross section (left) and boundary conditions (right) of the equivalent beam for the vertical wall. Lengths are in millimeters.

Bubbles When the cavit y caused at the beginning of the water shipping collapsed, bubbles are generated and partially convected with the flow to wards the vertical wall. T othese, new bubbles are added during the water rising along the vertical wall, as a consequence of the spray . The bubbles can be responsible for time dependent changes in the wall loading.

Three-dimensional effects During the rise up of the water along the vertical wall, a jet develops causing spray formation. At this stage the flow becomes unstable and three-dimensional effects start to be important (see figure 7.14, back view from the experimental video images).


Figure 7.14 Experimental water run-up along the vertical wall (back view).

F romthis moment on the experimental results loose their reliability from a quantitative point of view.

### 7.4.4 Human Errors

Human error represents an error source difficult to quantify since it influences the test results from many points of view. These are not discussed here. It is only mentioned the one associated with the wetting of the pressure cells (cf. section 7.4.2) since it is specifically related to present tests.

## Chapter 8

## Water-on-Deck Experiments: Analysis

In this chapter, the main physical aspects of the initial stages of water shipping and its late evolution are discussed on the ground of the two-dimensional model tests described in the previous chapter, and complemented by n umerical simulations. Typical time histories of the measured wa vemaker motion for the cases analyzed experimentally are reported in appendix G.

### 8.1 General Remarks

As anticipated, in the following the experimental results are complemented and interpreted also through the use of n umerical simulations. In particular ( $c f$. section 3.2.2), for the purpose of comparison, the physical wa ve flume is numerically modeled and the measured wa vemaker motion is used to drive the flap in the simulation. This motion includes the feedback action that the control system uses to minimize reflections (mainly) from the model. On the other hand, we did not attempt to model the absorbing beach at the end of the waveflume, and the mathematical damping region ( $c f$. section 3.4) used in the n umerics is quite different from the physical one. This represents a source of uncertainty when comparing the two results. Figure 8.1 shows the evolution of the wa ve elevation at two locations, 0.79 m from the flap (left plot), and at 0.104 m upstream the vertical bow ( $c f$. case a in the right plot of figure 7.2). Here, the nominal incoming wa velength is $\lambda=2 \mathrm{~m}$ and the crest-to-trough waveheight is $H=0.16 \mathrm{~m}$. The experimental data are compared with the numerical results. The agreement is rather satisfactory, though, at the beginning, a small difference could be observed from an enlarged plot (not reported). P ossible explanations of the difference, concerning the experimens, are discussed in section 7.4. A possible reason could be the seiching motion, set up initially in the physical tank and not correctly reproduced in the n umerical simulation because of the mentioned difference in the treatment of the downstream end of the tank. Howev er, according to a first estimate presented in chapter 7 , the standing waveswould require about 8.47 s to be set up in the flume. This means a longer time in terval relative to the one of interest. This estimate is quite rough since it does not account for the presence of the damping region and of the ship model. As time


Figure 8.1 Evolution of the wave elev ation recorded at 0.79 m from the flap (left plot) and at 0.104 m from the bow of the model (right plot) for case a in figure 7.2. Nominal incoming wa ves: $\lambda / D=10.1$, $H / D=0.808$. Experimental and numerical waverecords are compared.
increases, the measurements would show a small phase delay relative to the n umerical results. This is practically constant and is probably due to a phase lag introduced bythe waveprobes and their driving electronics.

In the follo wing, the first water-on-deck ev en tis focused on. This implies a quite transient phenomenon because the incoming wavesare far from being regular. This can be appreciated in figure 8.2, which gives the n umerical free-surface configurations for the same case as in the previous plots. F ourtime instants are considered, $t=2.82,4.23,5.63$ and 7.04 s from top to bottom, respectively. The wa vemaker is at the left end of each snapshot, though it is not


Figure 8.2 Numerical free-surface configurations before water shipping occurrence corresponding to nominal incoming w aveswith $\lambda / D=10.1$ and $H / D=0.808$. The plots are in natural scale and the time increases from top to bottom $(t=2.82,4.23,5.63$ and 7.04 s$)$.
represented for simplicity. The settings of the control system in the experiment would give wa ves 2 m long and with a 0.16 m crest-to-trough height. As we can see, the initial portion of the
generated wavetrain is neither symmetric nor with constant amplitude. The differences from the prescribed incoming wav esare better emphasized in figure 8.3, where the portion of the free surface closer to the ship model is plotted for $t=7.04$ and 7.66 s , respectively. In this case,


Figure 8.3 Free-surface configurations near the bow before w ater-shippingoccurrence $(t=7.04$ and 7.66 s , left and righ tplots respectively). Nominal incoming waws: $\lambda / D=10.1, H / D=0.808$. Present numerical solution (solid lines) and permanent-wavesolution (dashed lines) by Fen ton(1988) are compared. The plots are not in natural scale.
plots are not in natural scale. Numerical results (solid lines) are compared with the permanentwavesolution (dashed lines), obtained as in F en ton(1988, cf. section 3.2), corresponding to the prescribed waveconditions. Only a rough resemblance between the two solutions can be observed, with the leading wa ve steeper and shorter than the nominal regular ve. This becomes even more pronounced as wavesapproach the ship, due to wave-bodyin teractions. Therefore, though the prescribed wave parameters will be used to idertify the wave conditions, ve underline the highly transient character of the flow in front of the model.

### 8.2 Water shipping: First Stages

### 8.2.1 General Description

Figure 8.4 is representative of the initial stages of water shipping. The considered ship model has a vertical bow ( $c f$. case a in figure 7.2) and the prescribed incoming waveis 2 m long and with a 0.16 m crest-to-trough height. At the beginning, the fore-part of the deck remains dry, and the shipping of water starts in the form of a rounded jet plunging directly onto the deck. A ca vit yis formed with air trapped inside. This behavior has been observed in all the studied test conditions. Moreov er, though in the particular case shown here the jet hits the deck rather close to the bow edge, cases are recorded where the fluid organizes itself to plunge on the deck further from the bow. Finally, for some waveconditions, even blunter impacts have been observed. In all cases, front-view pictures of the same even $t$ (not reported) confirmed the two-dimensionality of the phenomenon, and excluded that the ca vit yformation is related to localized three-dimensional instabilities. As a consequence, the initiation of deck-wetting should be characterized by localized high impact pressures.

This fluid behavior was not detected in the two-dimensional experiments reported in Cozijn (1995). This may be due to the small time and space scales in volv edIn the reported example,


Figure 8.4 Two-dimensional w ater-on-dek experiments. Initial stages of the w atershipping due to nominal regular w a with $\lambda / D=10.1$ and $H / \lambda=0.08$. The snapshots are en umeratedas time increases, and the time interval is 0.04 s . The smallest grid dimension is 2 mm .
as described below, the time needed before the plunging wavehits the deck is about 0.13 s , and at the instant of impact the en trappedcavity has length $l_{\text {cav }} \simeq 0.2 D$ andeigh $\mathrm{t} h_{\text {cav }} \simeq 0.05 D$.

F rom the point of view of measurements, a consequence of the presence of an air cavit y is that capacity waveprobes do not estimate correctly the free-surface height along the deck.

After the impact of the plunging waveonto the deck, cf. bottom plots in Fig. 8.4, two horizontal jets develop. One of these moves backwards, reducing the cavit yvolume. The other one propagates forwards with higher velocity. As time passes, the whole cavity is drifted forwards, conv ected together with the shipped water. The water level above the cavit y increases and contributes to squeeze it. These combined actions are responsible, together with surface tension, of the follo wing fragmentation of the cavity. However, this ev olution cannot be documented because of the limited frame rate of the video camera and, in any even $t$, the late ev olutionof the en trappedca vity is three-dimensional.

### 8.2.2 Vortex Shedding at the Edge of the Deck

Natrium flourisenium powder, mixed with Dutch syrup, was used as fluorescent material to detect a possible vortex-shedding in the initial stage of the phenomenon. The resulting mixture was placed in the upper-front portion of the bow. During the tests, the running-up water slowly
dissolves the syrup and the fluorescent material is conv ected with the fluid wetting the deck. F orcross flow past blunt bodies, Skomedal (1985) documented that this procedure is suitable for vortex-shedding visualizations. Here, by using this method, we have not detected any clearly defined vortical structure during the initial stages of water shipping.

Later on, after the airen trapment, when the cavity starts to move forwards, the gravit y has already organized the run-down of the fluid in front of the model, preventing the beginning of vortex shedding, at least of strength large enough to be detected $b y$ the used method. This is qualitatively shown in figure 8.5, where an enlarged view of the flow around the bow is giv en


Figure 8.5 Evolution of the flo wfield near the bow edge during the late stages of watershipping. The time increases from left to righ twith time interv al of 0.04 s . Nominal regular incoming waves: $\lambda / D=10.1, H / \lambda=0.08$.
for the later stages of water shipping. The time increases from left to right, and entrapped air bubbles are clearly visible in the water. By tracking their motion, we can see that the bubbles above the deck are convected rightwards, while those in front of the bow move downwards. Therefore, grossly speaking, the flow is divided in to $t$ w streams wetting the deck and inv olv ed in the run-down, respectively, with negligible cross-flow and vortex shedding effects.

### 8.2.3 Wa ve Plunging Evolution

Numerical simulation The plunging phenomenon observed in the experiments is not correctly described by the initial Kutta-like condition, introduced in section 3.3. There, a more suitable model is given through the contin uous Kutta-like condition. Numerical results for the case just discussed are superimposed (red lines) to the experimental profiles in figure 8.6. The time increases from left to right with a constant interval of 0.04 s .

In the experiments, the start of the video camera is not triggered by the wavemakr motion, and the actual instant of time of the reported pictures is not known. Therefore, the corresponding n umerical sequence is determined a posteriori in the following way. First, the numerical free surface in agreement with the last experimental waveprofile is found. In the case presently considered, this corresponds to a time instant $t-t_{\text {wod }}=\Delta t_{\text {wod }} \sim 0.11 \mathrm{~s}$, where $t_{\text {wod }}$ stands for the instant of freeboard exceedance in the n umerical simulation. Then, the n umerical sequence is obtained by considering the same time interval, $1 / 25 \mathrm{~s}$, of the video camera. Therefore, the triggering between $n$ umerics and experimental data is done heuristically, and it leav es open the possibility of a time lag between experiments and numerical results. This possible error can not be quantified with the used instrumentation.


Figure 8.6 Initial stage of the w atershipping. Numerical free surfaces (red lines) are superimposed to pictures from the experiment. The time interval betw eentw osnapshots is 0.04 s . Nominal regular incoming waves: $\lambda / D=10.1, H / \lambda=0.08$.

F rom figure 8.6 experimental and numerical free surfaces agree quite well. In particular this is true for the time scale of the phenomenon and for the cavity dimensions. The differences visible in the sequence can partially be explained by meniscus effects at the glass side of the flume, and b y three-dimensional effects in the video images. A light disturbance in the last picture makes it difficult to decide sharply if water impact with the deck already occurred.

F romthe n umerical simulation, the impact occurs at a distance $\simeq 0.2 D$ from the bow, after $\Delta t_{\mathrm{wod}} \simeq 0.13 \mathrm{~s}$ from the instant of the freeboard exceedance.

Analysis of the cavity profile The fair, if not good, agreement, between experiments and n umerics allavs us tose the $n$ umerical medincass in more detail the local features of the phenomenon.

In figure 8.7, the free-surface profile close to the separation point at the bow is compared with


Figure 8.7 Initial stage of the water shipping. Numerical free surfaces, solid lines, and local solution (8.1), lines with circles, are compared. Nominal regular incoming waves: $\lambda / D=10.1, H / \lambda=0.08$.
the local solution (cf. Zhao et al. 1997)

$$
\begin{equation*}
z_{1}=C(t) x_{1}^{2 / 3} \tag{8.1}
\end{equation*}
$$

around a fixed separation point, obtained byassuming potential flow theory and zero gravit y effects.

Similar result can for 2-D flow be derived for the thin free shear layer shape close to a separation point. In expression (8.1), the origin of the local coordinate system $\left(x_{1}, z_{1}\right)$ is at the edge of the deck, the $x_{1}$-axis is along the deck and the $z_{1}$-axis is vertically upwards. The coefficient $C(t)$ is a time dependent parameter which depends on the complete flow, and therefore cannot be determined by a local flow analysis. The agreement of the local solution with the numerical data is good. In particular, the computed free-surface profiles for $\Delta t_{\mathrm{wod}}=t-t_{\mathrm{wod}}=0.03,0.07$ and 0.11 s fit quite well the local solution, when values $C \sim 0.26,0.27$ and 0.25 are used, respectively.

The configuration of the free surface at the impact with the deck is analyzed in figure 8.8. F ar


Figure 8.8 Water impact with the deck. Nominal regular incoming wa ves: $\lambda / D=10.1, H / \lambda=0.08$.
enough from the deck edge, and up to the impact position, the cavit y profile agrees well witla parabolic contour (line with black squares). The latter would be the path of a fluid particle in free fall under the action of the gravity. This and the previous observations suggest the existence of three main stages during the flow ev olution. An initial phase (i) where the gravit y does not matter and a final stage (iii) with free-falling water, joined by an intermediate phase (ii), where both the gravit yand the pressure gradient influence the fluid motion.

Steepness influence on the cavity Figure 8.9 shows the wav eplunging on the deck during the first water shipping caused by three different wavesystems. The steepness of the nominal regular incoming waves is $H / \lambda=0.04,0.06$ and 0.08 , from left to right, respectively, with wavelength $\lambda=10.1 D$ for all the cases. The smallest steepness considered is associated with a quite gentle water on deck. As a consequence, it is practically impossible to detect the ca vit y formation and probably surface tension significantly affects the evolution. F orlarger $H / \lambda$, the cavity is visible and increases more from the second to the third case than from the first to the second one. Since the involv edrate of change of the steepness is kept constant, this suggests a nonlinear dependence of the cavit y dimensions from the wavesteepness.

The first water-on-deck is also examined in figure 8.10. Here the wave steepnessis k ept fixed to $H / \lambda=0.08$. The wavelength $\lambda$ is $7.58 D$, for the case A in the left picture, and $10.1 D$, for the case B in the right picture, corresponding to actual wa ve heights $H=0.606 D$ and $0.808 D$,
respectively. This implies a smaller amount of water shipped in case A. Qualitatively the two ca vities have similar shapes. A more quantitative comparison is given by scaling the free-surface profile digitized from case B (cf. red line in the right picture) by the factor $(H-f)_{\mathrm{A}} /(H-f)_{\mathrm{B}}$, and plotting it overthe case A (cf. the red line in the left picture). The o verall agreement is


Figure 8.9 Influence of the wave steepness on the cavit y.F rom left to riglt: $H / \lambda=0.04,0.06,0.08$. $\lambda / D=10$. for all the cases. The smallest grid dimension is 2 mm .
reasonable and suggests $(H-f)$ as a possible scaling factor. Actually, differences can be detected for the profile of the en trappedcavit y which should be expected because of the different role of surface tension. Besides this, other uncertainties hamper the comparison, such as actual instant of time, optical effects, etc. The agreement between the uppermost free-surface profiles is definitely good.


Figure 8.10 Influence of the w avelengtlon the cavity. Left: case $\mathrm{A}, \lambda / D=7.58$. Right: case B, $\lambda / D=10$. The steepness is $H / \lambda=0.08$ for both cases. The free-surface profile digitized from case B (red line in the right picture) is scaled by the factor $\left[(H-f)_{\mathrm{A}} /(H-f)_{\mathrm{B}}\right]$ and plotted over the left picture for case A. The smallest grid dimension is 2 mm .

### 8.2.4 Water Impact with the Deck

The previous results have shown that water shipping starts with a waveplunging on and impacting against the deck. Here, we briefly analyze the possible effects of the impact for a FPSO. Throughout the section we will refer to full scale dimensions by considering a ship draft of 18 m .

The typical steel stiffeners along the deck are sk ethed in the left diagram of figure 8.11. The deck is designed to stand against a maximum spatially uniform pressure of 60 KPa . In


Figure 8.11 Example of stiffeners on the deck of a FPSO. Left: top view. Right: cross-section of the equivalent beam modeling the deck in the longitudinal direction. Dimensions are in millimeters.
the present two-dimensional analysis, an equivalent beam (cf. right sketch in figure 8.11) is used to model the deck structure along a longitudinal stiffener. The beam is assumed to be simply supported between two consecutive transverse stiffeners. In this framework, to carry out a qualitative in vestigationboth experiments and numerical simulations are considered. In particular, the latter are used to overcomethe lack of information from model tests (e.g. the impact velocity).

Here, we consider the water impact following the shipping of water causeb y incident wa ves with length 182 m , and height $14.55 \mathrm{~m}(\lambda / D=10.1$ and $H / D=0.808)$. The free-surface configuration as obtained by the numerical simulation is given in figure 8.12. The two horizontal arrows indicate the length of the first two equivalent beams along the deck. As we can see, the impact starts close to the middle of the second one. F rom the numerical simulation, an impact velocity of $4.3 \mathrm{~m} / \mathrm{s}$ is estimated. This value is not large, and in particular is close to the orbital velocity in free-wave conditions $(4.4 \mathrm{~m} / \mathrm{s})$. The free-surface shape near the initial impact position is rather blunt with daus focus ature $r \simeq 0.1 \mathrm{~m}$.

The impact phenomenon can th usbe approximated as the impact of a fluid circle against a flat wall and without gravity effects, and therefore described in the initial stage by a Wagner-type approach (cf. F altinsen1990). The related problem is sk etched in figure 8.13, where the main in olv edparameters are indicated. The solution procedure is the same as the one described in section 5.2.1 for the impact of a fluid wedge hitting a flat wall. In particular, parameter $c$ shown in sk etc h8.13 can be obtained as $2 \sqrt{V r t}$ by locally approximating the initial circular shape of the fluid with a parabola. This approach may nb beused at thev ery beginning of the impact,


Figure 8.12 Impact with the dec k (numerical simulation). Close to the impact position the free surface (solid line) is approximated by a circle with radius $r \simeq 0.1 \mathrm{~m}$. The free surface resembles a fluid wedge of $\sim 20$ degrees, inclined of $\sim 26$ degrees with respect to the vertical direction. The tw o horizontal arro ws $\left(b_{1}\right.$ and $\left.b_{2}\right)$ indicate the length of the first and second equivalent beams along the dec k .
when infinite pressures are predicted and the method is not valid since the neglected water compressibility is important. In reality, though high, the pressure cannot exceed the acoustic pressure $p_{\mathrm{ac}}=\rho c_{e} V$. Here $\rho$ is the water density, $c_{e}$ is the sound velocity in water (usually v arying between $1450 \mathrm{~m} / \mathrm{s}$ and $1540 \mathrm{~m} / \mathrm{s}$ ), and $V$ is the impact velocity. In the specific case, the maximum value of $p_{\mathrm{ac}}$ is $\sim 6.6 \mathrm{MPa}$. This is much larger than the design pressure. However since the high pressures are localized in space and time, the effect on the structure is limited. The time duration of the acoustic phase can be estimated through the Wagner method by imposing the maximum pressure equal to the acoustic value

$$
\begin{equation*}
p_{\max }=p_{\mathrm{ac}} \Longrightarrow \frac{\rho}{2}\left\{\frac{d\left[c=2 \sqrt{V t_{\mathrm{ac}} r}\right]}{d t}\right\}^{2}=\rho V c_{e} \quad \underbrace{\Longrightarrow}_{\mathrm{Hp}: V=\text { constant }} \quad t_{\mathrm{ac}}=\frac{r}{2 c_{e}} . \tag{8.2}
\end{equation*}
$$

This gives $t_{\mathrm{ac}} \sim 3.3 \cdot 10^{-5} \mathrm{~s}$ for the present case. Alternatively we can say that the acoustic phase lasts until $\mathrm{d} c_{\text {geom }} / \mathrm{d} t=c_{e}$ ( $c f$. Korobkin 1995), with $c_{\text {geom }}$ obtained as geometric in tersection of the fluid circle with the deck. For very small times, this gives $c=\sqrt{2 V r t}$ and $t_{\mathrm{ac}} \sim 0.9 \cdot 10^{-7}$ $s$. These two estimates giv ean indication of, respectively, the upper and the lo wer limit of the compressibility phase duration, and show that this phase is quite short.

For $t>t_{\mathrm{ac}}$, a Wagner-type method can be used to find the evolution of the pressure distribution along the deck. The duration of this second stage can be estimated as the time interval for half-circle of fluid to hav eimpacted with the deck ( $\beta=90^{\circ}$ in figure 8.13), from the end of the acoustic phase. In this case, byusing the geometrical relationship $c=r \sin \beta$ and the solution for $\mathrm{c}(c=2 \sqrt{V t r})$, we find $t_{\text {circ }} \sim 5.8 \cdot 10^{-3} s$. At this time, the maximum pressure becomes 37 KPa , which is smaller than the design pressure. The time duration of the second impact phase is larger than the first one, and corresponds to $\sim 37 \%$ of the highest natural dry period of the equivalent beam, $T_{\text {dry } 1}=0.0156 \mathrm{~s}(c f$. sk etc h8.11). This means they are of the same order of magnitude and therefore the elastic response of the beam has to be analyzed. We must note that strictly speaking the Wagner method is valid for $\beta \leq 20^{\circ}$. In paragraph 5.2.1 we have


Figure 8.13 Sk etch of the problem of a fluid circle hitting a flat horizotal wall.
seen that in the case of a fluid wedge hitting a flat wall, the maximum pressure predicted by the Wagner method compared well with the pressure obtained with similarity solution at least until a deadrise angle of $45^{\circ}$. Since here we have used this approach up to $\beta=90^{\circ}$ we can expect that $t_{\text {circ }}$ has only been roughly estimated. During this blunt impact phase the region of the beam with important pressure loads is $\sim 2 r=0.08 L_{\text {beam }}$, thus quite small relative to the beam length. The beam evolution and the related stresses can thus be determined in a simplified way, by considering the problem of an initially undeformed beam subjected to a spatial Dirac-delta load, $f(t) \delta\left(x-x_{\text {imp }}\right)$, at the initial impact position. $f(t)$ can be estimated as vertical force on a rigid circle penetrating a flat free surface ( $c f$. F altinsen 1990) and expressed as $\rho C_{s}(t) r V^{2}$. The time dependent coefficient $C_{s}$ has been derived experimentally by Campbell and Weynberg (1980) and is represented bythe formula

$$
C_{s}=\frac{5.15}{1+8.5 \frac{h}{r}}+0.275 \frac{h}{r}
$$

Here $h=V t$ is the instantaneous submergence of the circle and is equal to $r$ when half-circle penetrated the free surface. This means that the end of the blunt impact phase should be given by $t_{\text {circ }}=r / V \sim 2.44 \cdot 10^{-2} s$ which is four times the value predicted above. Since this value is not based on the assumption of small deadrise angle, it should be considered a more realistic estimate than the previous one. An analysis like this shows that the resulting maximum stresses on the beam are safely below the yield stress.

The next stagf the ev olution can be roughly approximated by the impact of a fluid wedge of $20^{\circ}$ hitting asymmetrically the deck (see figure 8.12). In case of a rigid deck, this would giv e a maximum pressure of $\sim 18 \mathrm{KPa}$ on the assumption that the impact velocity is constant and equal to the initial value of $V$. This pressure value was obtained numerically, by taking the free-surface data from the similarity solution of a liquid wedge impacting nonsymmetrically a flat rigid wall (see appendix D). Clearly, this v alue is definitely below the safety limits for the deck. The actual evolution is howev ermore complex. F rom video images of model tests,during this phase, the two jets developing in opposite directions along the deck wet completely the second beam $\left(b_{2}\right)$. The portion of the deck closer to the bow is instead characterized by a cavit y
originated at the impact instant, which is stretched by the flow en tering the deck and above it. As a consequence, the first beam $\left(b_{1}\right)$, under the action of the atmospheric pressure at the beginning of the ca vity formation, suffers loads due to the compressibility of the air entrapped in the cavity. If we assume a uniform pressure in the cavity, and we mod也he air evolution as an adiabatic process of an ideal gas, the pressure $p(t)$ in the cavity can be obtained by

$$
\begin{equation*}
\frac{p(t)}{p_{0}}=\left\{\frac{\mathcal{V}(t)_{0}}{\mathcal{V}(t)}\right\}^{\gamma}, \quad \text { with } \gamma=1.4 \tag{8.3}
\end{equation*}
$$

Here, $p(t)$ and $\mathcal{V}(t)$ are the pressure and the volume at time $t$ and $p_{0}$ and $\mathcal{V}_{0}$ are the corresponding reference values, e.g. the atmospheric pressure ( $p_{0}=1 \mathrm{Atm} \simeq 10^{5} \mathrm{~Pa}$ ) and the air volume in the cavity at the impact instant. As already observed, the cavity is squeezed during the follo wingev olution, and the relation (8.3) would predict unbounded pressure above the first beam. Therefore, this simple analysis is even tually not applicable. However, from the structural point of view, the important factor is the rate of change of the pressure and this one can be predicted byusing the above relation.

In the follo wing, by using equation (8.3) and the pictures taken from the experiments, we hav e carried out a simplified analysis. In the sequence 8.14 , the post-impact evolution is shown


Figure 8.14 Pictures from the experiments showing the evolution of the air cavity at the bow edge. The time increases from left to righ twith a constant interval of 0.38 s (full scale, $D=18 \mathrm{~m}$ ). The digitized cavity profiles (colored lines) are superimposed to the video images.
with snapshots separated in time by 0.38 s . Because of the relatively poor resolution of the images, at least for the present purpose, the cavity profile is not sharply detectable from the pictures (see the discussion in section 7.4), and for each snapshot several different curves are candidates as cavity boundary. Therefore, all of them have been considered and are reported, superimposed to the corresponding video images. F oreach instant of time, the ca vit yvolume has been evaluated and in troduced in relation (8.3) to estimate the pressure inside the cavity. Clearly, because of the uncertainty in the determination of the ca vit yboundary, for each time step several scattered results will be obtained.

Actually, the use of relation (8.3) requires some extra data which are not a vailable from the experiments and our numerical simulations have been used to complement the available experimental information. In particular, the impact instant $t_{\mathrm{imp}}$ is not av ailable from thevideo images, therefore (i) the volume $\mathcal{V}_{0}$ cannot be obtained from the experiments and (ii) the time in terval $t-t_{\mathrm{imp}}$ of each of the considered configurations (see sequence 8.14) is unknown. Here,
$\mathcal{V}_{0}$ has been ev aluatedb yn umerical simulations, and the time of the experimental snapshots is estimated by using the experimental snapshot shown in the left of figure 8.15, previous to the water impact with the deck and occurred 0.76 s before the first snapshot of figure 8.14. Blue and red curves superimposed to the picture represent the n umerical free-surface configurations


Figure 8.15 Left: estimate of the experimental time by comparing with numerical free-surface configurations at $\Delta t_{\mathrm{imp}}=0.57$ (blue line) and 0.65 s (red line). $t_{\mathrm{imp}}$ is the numerical impact instant. Right: estimated pressure evolution by assuming valid equation (8.3). All the quantities are given in full scale ( $D=18 \mathrm{~m}$ ).
at, respectively , $\Delta t_{\text {wod }} \simeq 0.57$ and 0.65 s from the freeboard exceedance. F rom this comparison, we can approximatively consider $\Delta t_{\text {wod }}=0.61 \mathrm{~s}$ as the time for the experimental snapshot.

Eventually, the time instant of all the snapshots is evaluated and the pressure evolution can be computed by using relation (8.3). Results are given by the circles in the right of figure 8.15. As anticipated, different pressure values for the same instant of time refer to the different digitized cavity boundaries. The pressure bandwidth (dashed lines) gives an indication of the order of magnitude of the uncertainty in volved in. In the plot, the horizontal solid line is the design pressure for the deck. It seems reasonable that this value is exceeded during the cavity evolution and likely this occurs for a time interval not small compared with, for instance, the first natural dry beam period $T_{\text {dry1 }}$. The ca vity collapse represents thus a danger for the safety of the deck. F romthe tests, this phase lasts for $t_{\text {coll }}-t_{\mathrm{imp}} \sim 2.57 \mathrm{~s}-1.2 \mathrm{~s}=1.37 \mathrm{~s}$. As all the quantities reported in the present section, also this time interval is given in full scale.

Summarizing, for the second beam $\left(b_{2}\right)$, the water-impact evolution features three phases: (i) acoustic phase, (ii) blunt-impact phase, (iii) and wedge-impact phase. The beam closer to the bow $\left(b_{1}\right)$ is instead subjected only to the air-compressibility phase before to be completely wetted.

During the impact, local damages of the deck as well as hydroelastic excitation can occur and need to be quantitatively in vestigated. We should note that equation (8.3) assumes no air leakage. This is likely to occur in a 3-D flow situation and it can be expected that pressures will be lower. The present n umerical method is not able to describe the flow evolution after the impact. This could however be obtained by matching with a suitable high-speed local solution. With this procedure the impact phenomenon could be described until the cavity collapses.

### 8.3 Water Shipping: Later Stages

### 8.3.1 General Description

The sequence of pictures in figure 8.16 describes the late evolution of the flow field observed


Figure 8.16 Late stages of water shipping on the basic model (case a of figure 7.2) without superstructure along the dec k . Numerical free surfaces (red lines) are superimposed to the experimental video images. Nominal incoming waves: $\lambda=2 \mathrm{~m}, H=0.16 \mathrm{~m}$.
in the experiments in a case without superstructure on the deck. The time increases from top to bottom and from left to right, and the time interval between two consecutive snapshots is 0.04 s . The global phenomenon is a dam breaking-type water on deck. The cavity formed at the beginning the water shipping is collapsed, and bubbles, identifiable as the white region close to the deck, are conv ected bythe main flow propagating forwards. As the time increases, the role of the gravit y becomes important causing the run-down in front of the bow. This finally leads to the end of the water shipping.

We have numerically modeled this stage of the phenomenon by neglecting the initial plunging phase, and byenforcing the initial Kutta-like condition at the edge of the deck. The obtained results are superimposed (red lines) to the experimental images in sequence 8.16. Apparently, though the details of the initial stages of water shipping are neglected, the numerical wave profiles agree well with the experimental ones, with the exception of the wavefront region where the n umerical method predicts a higher propagation velocity. Therefore, the gross flow ev olution is not significantly affected by the phenomena connected with the initial plunging. An ambiguity in the time correspondence between experiments and numerics has to be recalled, as already discussed in section 8.2.3.

### 8.3.2 Wa ve Parameter Analysis

Water level The water-level evolution at the bow is analyzed in figures 8.17-8.18 in terms of the nominal parameters of the incoming waves. Both first and second water-on-deck even tsare


Figure 8.17 Water level at the bow. Influence of the incoming w avenonlinearities in terms of the w av height (left) and of the w avelength(right). Two test results (full and empty symbols) are given for each case.
considered for the ship model with vertical bow (case a in figure 7.2) and without superstructure along the deck. The time histories hav e been shifted to synchronize the first water on deck for all the cases. In the left plot of figure 8.17, the examined (nominal) wa velength is 2 m and three different wa ve heiglts $(0.08,0.12$ and 0.16 m$)$ are considered. Here, for the smallest wa ve height $(H / \lambda=0.04)$, only one water on deck has been observed and it has been shifted to coincide with the second shipping cycles of the other incident wavecases. In the right plot, the waveheight
is constant, 0.12 m , and the wavelengthchanges assuming values of $1.5,2$ and 2.5 m . Therefore also in this case the steepness is not kept constant. F or each of the considered conditions, two test results (full and empty symbols) are given showing a satisfactory repeatability of the experimental results. The water level is made non-dimensional with respect to the exceedance of the freeboard by the wave height $(H-f)$ while the time axis is made non-dimensional by the wav eperiod $T$.

Both plots show an increase of the maximum relative water level at the bow with the steepness. The time interval between the first and the second water-on-deck even tsseems to scale with the waveperiod. In particular, it is close and smaller than $T$.

The left plot of figure 8.18 reports cases with constant steepness $H / \lambda$ and varying the wa velength $\lambda$. The maximum relative water level during the first water on deck is almost the same,


Figure 8.18 Left: water level at the bow for constant steepness. Two test results (full and empty symbols) are given for each case. Right: influence of the steepness on the maximum relative water level at the bow. Empty symbols correspond to fixed $\lambda / D$, full symbols correspond to fixed $H / D$. Only one test result is given for each case.
while a larger difference is observed for the second even t . Howev er, the latter is associated with incoming waves steeper and een less related to the nominal conditions because of the strongest wa ve-body in teraction. These results, together with those in figure 8.17, are presented in more compact way in the right plot of the same figure. Here, the non-dimensional maximum water lev el at the bov $\left(\eta_{\max }-f\right) /(H-f)$ is plotted versus the steepness $H / \lambda$. Only one test result is giv en for eada case. During the first water on deck, $\left(\eta_{\max }-f\right) /(H-f)$ increases almost linearly with the steepness. F or the second water on deck, the effect of changes in $H / D$ and $\lambda / D$ is different, and $\left(\eta_{\max }-f\right) /(H-f)$ can be different ev en when k eeping fixed the steepness.

Water evolution along deck The influence of the nominal incoming wave parameters on the wav efront propagation along the deck is considered in figure 8.19. This is made in terms of the waveheight (left) and of the wavelength (right), by using the same cases considered in figure 8.17. As in that figure, the time is made non-dimensional by $T$ and the instantaneous wetted length of the deck $\left(\Delta x_{\text {bow }}\right.$, measured with sensor $\left.\mathrm{fd}_{1}\right)$ is made non-dimensional by $(H-f)$. Two tests (full and empty symbols) are shown for each studied case, and the time histories are shifted


Figure 8.19 Wave frort along the deck. Influence of the incoming wave nonlinearities in terms of the w av height (left) and of the w avelength(right). Two test results (full and empty symbols) are given for each case.
to hav e correspondence of the starting of the first water shipping. The body geometry is the basic one (case a of figure 7.2 ) without superstructure along the deck.

It is in teresting to note that the ev olution of the non-dimensional $\Delta x_{\text {bow }}$ is quite similar for the different cases, both during the first and the second events. In the first water on deck, the curve for the case with steepness $H / \lambda=0.06$ and wavelength-to-draftratio $\lambda / D=10.1$ (triangles) reaches a non-dimensional maximum value of $\sim 1.5$. This is not the real maximum distance covered by the water which is definitely larger, as observed from video recordings of the tests. The reason of the difference is explained in chapter 7 and is related to the fact that, at a certain instant during the water ev olution, the flux of water in vadingthe deck becomes zero together with the water level on the deck close to the bow. This experimental error may not be quantified a priori since it depends on the sensor sensitivity and on the extension of the deck region with almost-zero water lev el. The results suggest that the wavefront velocity along the deck behav es as $k \sqrt{g(H-f)^{2} / \lambda}$, $k$ being a time dependent parameter weakly dependent on the incoming waves.

### 8.4 Influence of the Stem Angle

A positive stem angle should reduce the amount of shipped water by increasing the wav ereflection from the ship. A negative inclination in the upper portion of the bow is however preferred in some designs. This should decrease the intensity of water bow impacts, giving more gentle water shipping, with possible lateral water deviations out of the deck. The latter aspect is intrinsically three-dimensional.

To inv estigate the influence of a bow stem angle, two additional bow configurations hav e been considered, indicated as cases b and c in figure 7.2. They hav e a stem angle of 45 and -45 degrees, respectively. The analysis here carried out is qualitative. This is due to the follo wingreasons. First, in both these alternative cases the fore portion of the bow is closer to the wavemakr than when the basic model with vertical bow is used. Second, the on-model measurements during the experiments for case b are not quantitatively satisfactory because of additional relevant error
sources ( $c f$. section 7.4). Despite this fact, the analysis can give useful information.
Sequences 8.20 and 8.21 show a water shipping caused by prescribed incoming waves 2 m long


Figure 8.20 Geometry with $45^{\circ}$ stem angle, case b in figure 7.2. F reesurface ev olutionduring the w atershipping. The time increases from top to bottom and from left to right with constant time interv al of 0.04 s .
and with a .16 m crest-to-trough height on the ship model with bows b and c , respectively. In both sequences the time increases from top to bottom and from left to right. The two water on deck phenomena occurred approximately after the same time interval from the beginning of the wa vemaker motion in the related test. For theositiv e stem angle the event corresponds to the first shipping. The corresponding ev en in the case of ship model with vertical bow represents also the first water on deck and has been discussed in the previous sections. Differently, the
event related to the negative stem angle is the second ev en t.A previous even t occurred because


Figure 8.21 Geometry with $-45^{\circ}$ stem angle, case c in figure 7.2. Free surface evolution during the w ater shipping. The time increases from top to bottom and from left to right with time interval of 0.04 s for the first three snapshots. Last three photos are related to a different test of the same case, with time intervals of 0.08 and 0.04 s , respectively.
of the reduced wavereflection from the bow. This was however characterized by a quite small amount of shipped water.

Similarly to the vertical bov also in cases band c the water shipping starts in the form of a plunging wavehitting the deck. The positive stem angle causes clearly a lage w avereflection. Locally in front of the bow the wavefield is more deformed and steeper than in the cases of 0 and -45 degrees stem angle. In this flow region a backward wa veo verturningoccurs (see third
and fourth snapshots of sequence 8.20), accompanied by spray formation. The water impact with the deck is blunter and less localized. This leads to higher pressures and greater danger of deck structural damages. The air entrapped in the cavity after the impact collapses very quickly causing bubbles. These form a thick white strip near the deck and are convected by the main flow. In case $c$ the fore part of the bow is fav orableto the wavepropagation. The local crest is smaller and the water shipping starts with a larger front velocity but the resulting impact appears less severe. Summarizing. When the stem angle is reduced the water on deck starts with higher horizontal velocities but gives a less heavy impact with the deck. These two aspects are competitive in terms of the resulting wavefront velocity after the impact. It is not obvious to identify the critical one in determining this quantity which represents an important parameter for the water impacts with superstructures along the deck.

The three bow geometries are compared in figure 8.22 in terms of the water front ev olution



Figure 8.22 Left: w ave fronpropagation along the deck. Geometry with vertical bow (red line, case a in figure 7.2 ), with $45^{\circ}$ stem angle (green line, case b in figure 7.2 ) and with $-45^{\circ}$ stem angle (blue line, case c in figure 7.2). The wavesensor $\mathrm{fd}_{1}$ starts almost at the bow for cases a and c , while starts at 0.25 m from the bow for case b . Right: geometry with $-45^{\circ}$ stem angle. Water shipped during the first water on deck. The smallest grid dimension is 5 mm .
during the water on deck. The time axis of the three curves was a little shifted to make easier the comparison of the results. In the case of positive stem angle the water sensor $\mathrm{fd}_{1}$ giv esa non-zero value after the water covered the distance of 0.25 m from the bow. F or this reason, the relative measurement (green curve in the figure) has been vertically shifted to give 0.25 m as starting value of $\Delta x_{\text {bow }}$. Differently, curves for case a (red line) and case c (blue line) start from zero. Since for case "c" a previous water shipping occurred, the related curve becomes different than zero before the others. It reaches a maximum of about 0.025 m and then increases during the second water on deck. The maximum value measured during the first event is consistent with the maximum distance cov ered by the ater at the end of the first water on deck (cf. right plot of figure 8.22). The water fronts for the cases a and c seem to develop with similar velocities. F urther, after co vered 0.25 m from the bow, their velocities seem to be of the same order of magnitude as the corresponding water front velocity for case $b$.

Figure 8.23 giv esthe free surface configurations when the water flux in vadingthe deck is almost zero. The view is not exactly the same. Howev er, qualitatively the amount of shipped water does not appear significantly different from case a to case c. In the case of negative


Figure 8.23 F ree surface configuration when the water flux on the deck is almost zero. Cases a (left), b (center) and c (right).
stem angle, the free surface appears less smooth than in the other cases and bubbles are clearly observed, mixed with the water.

### 8.5 Impact with a Vertical Wall

### 8.5.1 Water Evolution

Figure 8.24 shows an enlarged view of the water impact occurring when a vertical wall is in-


Figure 8.24 Water impact with a vertical wall at 0.2275 m from the bow. Jet evolution along the structure. Nominal incoming wa ves with $\lambda / D=10.1$ and $H / D=0.808$.
troduced along the deck, at 0.2275 m from the bow. Nominal incoming wa ves have $\lambda=2 \mathrm{~m}$ and $H=0.16 \mathrm{~m}$. The flow field appears quite similar to the impact phenomenon discussed in section 5.1, where the water flow generated after the breaking of a dam hits a vertical wall. The water front approaching the structure resembles a thin half-wedge, and, at the beginning, only the small amount of the fluid sharply deviated upwards bythe obstacle is affected by the phenomenon. A jet originates vertically, and some spray is formed.

Comparison with $\mathbf{n}$ umerical results First stages of the free-surface evolution during the water impact with the vertical wall is reported in figure 8.25 , where the time instant between two pictures is 0.04 s . The red lines are obtained from the numerical simulation, which includes


Figure 8.25 First stages of water impact with a vertical wall at 0.2275 m from the bow. Numerical free surfaces (red lines) are superimposed to the experimental video images. Time interv al betw een $t \mathrm{w}$ o snapshots is $0.04 \mathrm{~s} . \Delta t_{\mathrm{wod}}=t-t_{\mathrm{wod}}$. $t_{\mathrm{wod}}$ is the instant of w ater-on-dek starting in the numerical simulation.
the modeling of the water shipping at the bow. In this case, the initial Kutta-like condition at the edge of the deck has been adopted. The overall agreemert between the experimental water profiles and the n umerical resultsis rather good.

This is also confirmed b ythe comparison between n umerical and experimental water run-up ( $\Delta z_{\text {deck }}$ ) along the vertical wall. The latter is presented in figure 8.26 where two experimental tests (line with squares and line with circles) are compared with the n umerical results (solid


Figure 8.26 Water run-up along the vertical wall placed at 0.2275 m from the bow. Two experimental tests (line with squares and line with circles) are compared with numerical results (solid line). $\Delta t_{\text {wod }}=$ $t-t_{\text {wod }} . t_{\text {wod }}$ is the instant of water-on-deck starting in the numerical simulation.
line). The water run up is given as a function of $\Delta t_{\text {wod }}=t-t_{\text {wod }}$, $t_{\text {wod }}$ being the instant of water-on-deck starting in the numerical simulation. During the first stages, the agreement is rather good. Later, when the experiments approach the maximum run-up along the wall, the n umerical prediction ov erestimates the measured data. In this stage, also the two test results do not agree completely. This behavior is probably explained by three-dimensional flow instabilities follo wing thespray formation during the rise of the water (cf. section 7.4.2).

Waveparameter analysis Experimental visualizations can be used to have a very rough estimate of the wave-fron velocity just before the impact with the wall. The impact velocity is clearly an important parameter affecting the resulting water loading (cf. section 5.2.1). F or instance, during the first water on deck, the impact velocity is $\sim 0.67 \mathrm{~m} / \mathrm{s}$, for prescribed incoming waveswith $H / D=0.606$ and $\lambda / D=7.58$, and $\sim 1.13 \mathrm{~m} / \mathrm{s}$, for wa ves with $H / D=$ 0.808 and $\lambda / D=10.1$. In the latter case, the n umerical solution predicts an impact velocity of $1.2 \mathrm{~m} / \mathrm{s}$. These two experimental conditions correspond to the same wave steepness $H / \lambda=0.08$ and the non-dimensional impact velocity $V / \sqrt{g(H-f)^{2} / \lambda}$ is about and 5 , respectively.

The water run-up along the vertical wall is presented in figure 8.27. In the plots, the nondimensional vertical distance from the deck wetted bythe water, $\Delta z_{\text {deck }} /(H-f)$, is given as a function of the non-dimensional time $t / T$. The wave-heiglt influence is examined in the left plot, while three different values of the wavelength are considered in the right plot, for a fixed


Figure 8.27 Water rise-up along the vertical wall. Influence of the incoming w avenonlinearities in terms of the waveheight (left) and of the wavelength (right).
waveheight. As we can observe, the measurements of water run-up for the case with $H / \lambda=$ 0.06 and $\lambda / D=10.1$ do not agree with the corresponding measurements of water flow along the deck ( $c f$. left plot of figure 8.19). According to sensor $\mathrm{fd}_{1}$, during the first water on deck the shipped water should not reach the wall (the measured distance covered by the water is smaller than the wall-bow distance), conv ersely sensor fw records a water run-up along the wall even during the first water on deck. The disagreement is due to errors in the $\mathrm{fd}_{1}$ measurements, as discussed in c hapter7 an recalled in section 8.3.2.

The relative waverise-up along the wall remains qualitatively similar for all the considered cases. This suggests that the vertical water-front velocity along the superstructure behaves similarly to the horizontal water-front velocity along the deck.

### 8.5.2 Pressure along the Vertical Wall

Comparison with numerical results The pressure evolution on the wall, measured at 0.012 m and at 0.032 m abovethe deck, are reported in the left and right plots of figure 8.28 , respectively. Along the horizontal axis $t=0 \mathrm{~s}$ corresponds to the time instant when the n umerical pressure (thick line in each plot) at the lowest location attains a non-zero value. Two test results are shown for each pressure gauge (full and empty symbols).

Qualitatively the agreement is satisfactory, but the experimental results are not perfectly repeatable. At the lo wer location, the value of the first peak for two test results is roughly the same as the n umericalone, while is larger for the two others. Later on, the repeatability is not exactly ensured. All the test results show two peaks of the same order at the lower location. The first one is almost disappeared at the upper location. This occurs at the beginning of the water run-up and is related to the initial water impact with the superstructure. The second one occurs in the later stages, when the gravity started to matter and is related to the occurrence of a backward water overturningand breaking. The latter phenomena are shown in the sequence 8.29 and are therefore important for green-water loading on the superstructure.


Figure 8.28 Pressure evolution on the vertical wall. Experimental and numerical data. Left: pressure measured at 0.012 m above the $\mathrm{d} \mathbf{e}$. Right: pressure measured at 0.032 m above the deck.


Figure 8.29 Water overturning and breaking after the impact. Nominal incoming waveswith $\lambda / D=10.1$ and $H / D=0.808$.

Waveparameter analysis Time histories of the pressure on the vertical wall at locations $0.012 \mathrm{~m}\left(\Delta z_{\text {bow }} / D=0.06\right)$ and $0.032 \mathrm{~m}\left(\Delta z_{\text {bow }} / D=0.16\right)$ from the deck are given in figures 8.30


Figure 8.30 Pressure evolution at 0.012 m from the deck. Influence of the incoming wave nonlinearities in terms of the waveheight (left) and of the wavelength (right).
and 8.31, respectively. For simplicity of graphical representation, only one test result is shown for each considered case, though we recall the repeatability issue, discussed in section 7.3. The


Figure 8.31 Pressure evolution at 0.032 m from the deck. Influence of the incoming wave nonlinearities in terms of the waveheight (left) and of the wavelength (right).
time is made non-dimensional by the wave period, and the pressure is referred to the lydrostatic term $\rho g(H-f)$, the atmospheric pressure being set zero. Since nominal incowning a ves with $\lambda / D=12.63$ and $H / D=0.606$ do not cause an impact with the superstructure during the first weak ev en $t\left(c f\right.$. right plot of figure 8.19), the measured pressure at both locations ( $\mathrm{pr}_{1}$ and $\mathrm{pr}_{2}$ ) remains atmospheric in the examined time interval.

The non-dimensional pressure seems to be nonlinearly related to the wa ve steepness. Also, the second pressure peak is dominated by the local conditions at the impact, and by the subsequent occurrence of a breaking wave. This can partially explain why the maximum non-dimensional pressure associated with less steep waves can be larger than the mlue caused by steeper incident wa ves. Clearly this represents only a possible reason. Three-dimensional effects are definitely important at this stage and, close to the wall, bubbles are mixed with water. All these factors affect the pressure and make more difficult the interpretation of the experimental results.

## Chapter 9

## Summary and Future Perspectives

The bow deck wetness phenomenon for a moored ship, with blunt bow, in regular head waves, has been idealized and reduced to a simple two-dimensional wa ve-body interaction problem.

In this framework, the problem has been analyzed both bynumerical simulations and bya dedicated experimental activity. On the numerical side, viscous- and surface-tension effects hav e been neglected, and the resulting unsteady fully-nonlinear free-surface flow has been solved by a boundary-integral equation method. Numerical results have been compared with published experimental and analytical solutions for prototype problems connected to the phenomenon of in terest. Reasonable good agreement with reference results enabled us to use this model to gain fundamental insight into water-on-deck occurrence, flow field over the deck, and impact with superstructures.

The performed experiments complemented the numerical analysis, giving a closer view on several aspects, some of them unexpected.

Water on deck occurrence The first crucial aspect of the water-on-deck problem is the prediction of the shipping occurrence. This issue has been addressed n umerically The role of several waveand geometric parameter hav e been discussed.

Two approaches have been applied, both of them are based on the application of a Kuttalike condition at the bow edge. In the first case, the flow is enforced to leave tangentially the bow once the freeboard is reached. Then, the fluid velocity relative to the the ship determines whether the deck will be wetted or the water will be diverted in the opposite direction. In the second one, the Kutta condition is continuously imposed from that moment on.

Initial stages of the water shipping Two-dimensional water on deck model tests have rev ealeddetails of the flow when the water is initially shipped onto the deck. Within a rather small time scale, the shipping of water starts in the form of a plunging breaker, hitting the deck close to the bow. The impact causes locally high pressures and results in the formation of a cavity near the bow. The very high pressures last too short in time and are too concentrated in
space for causing important stresses in the deck. However the pressure rise due to the collapse of the cavity is significant from a structural point of view.

The experiments showed that later on there is no significant cross-flow, preventing any vortex shedding at the bow.

F rom these observations, the contin uous Kutta-lile condition represents the most appropriate condition between the two proposed and implemented. In this way, the n umerical method is able to predict free-surface ev olutionsin reasonable agreement with that observed during the model tests. Therefore, the numerics was used to evaluate the flow conditions at the moment of the impact with the deck. The resulting impact loading has been discussed.

Later stages of the water shipping The observed initial plunging wave hitting the dek is a quite localized phenomenon. After this rapid phase, the observed water shipping develops in the form of a dam breaking-type water on deck. This behavior is also observable in our numerical simulations by enforcing the initial Kutta-like condition.

The agreement between numerics and experimental data was satisfactory in terms both of the free-surface evolution, and of the pressure evaluated on a superstructure along the deck. Therefore, the numerical method with the initial Kutta-like condition has been applied extensively to analyze: type of water shipping, amount of shipped water, and water impact with the deck house.

Global plunging-type water on deck The occurrence of the less common "plunging wave water on deck" has been detected during three-dimensional experiments (see figure 1.4), and features a non-local plunging phenomenon characterizing the whole water shipping. This possibility has been $n$ umerically inv estigated.

F rom the numerical analysis, the occurrence of this extreme and dangerous even $t$ seems to be related to the interaction with a steep wave already prone to break, more than to the e-body in teraction by itself. Howev er, the influence of ship motion to enhance or reduce its severity can not be excluded.

Deck-wetness analysis An analysis concerning the parameters dependence of deck wetness has been carried out, showing that

- For long wav elengths $\lambda$ relative to the draft $D$, the wave steepnessH/ $\lambda$ mainly determines water-on-deck occurrence and severity. The relative amount of shipped water depends nonlinearly on $\mathrm{H} / \lambda$.
- For small $\lambda / L$, where $L$ is ship length, the bow-wavereflection reduces or prevents the shipping of water, ev enfor large wav esteepnesses.
- The stm o verhang reduces the relative amount of shipped water, but its positive effect is less pronounced with respect to that of the freeboard.
- A trim angle (a quasi-steady pitch angle) has a small effect on the amount of shipped water.

Impact with the deck house The impact of shipped water against a deck house has been analyzed, showing that

- In the first stages of the impact gravity does not matter.
- For dam breaking-type water on deck, the water-front velocity $(V)$ and the angle $(\beta)$ between the free surface and the deck at the impact are the relevant parameters.
- The impact flow can be approximated by a zero-gravity similarity solution in the initial stages of the impact. In this case a fluid wedge hitting a straight wall at 90 degrees is studied with $V$ and $\beta$ as input.
- The similarity solution showed that $\left.d\left[P_{\max } / \rho V^{2}\right)\right] / d \beta$ is large only for $\beta>\sim 60^{\circ}$ and is small for $\beta<\sim 40^{\circ}$. In the last case $V$ represents the most important factor influencing the maximum pressure as a squared power. Here $P_{\max }$ is the maximum pressure.
- In the later stages, when gravit y matters, a similarity solution overpredictsthe pressure along the wall.
- In addition to the pressure peak caused by the initial water impact with the superstructure, the experiments showed a second peak of the same order of magnitude in the ev olution of the pressure along the wall. This one occurs in the later stages and is related to the occurrence of a backward overturningof water, plunging on the wetted deck. Therefore, also these late ev en tsare important for green-water loading on the superstructure. Since the present numerical method does not handle free-surface fragmentation phenomena, it is not possible to predict the second pressure peak.
- The stem overhangreduces the water level along the deck but increases the in voled flow velocities. Due to this, it is difficult to find a conclusive statement about its positive or negative effects on water impacts with a superstructure.
- A trim angle (a quasi-steady pitch angle) has a small effect on the water lev el and the velocity of the water flow propagating along the deck, and therefore on the water impact loading on a deck house.
- Reducing the inclination of the wall reduces the water loading during the run-up. When an angle $\alpha=40^{\circ}$ (relative to the vertical direction) is considered, the maximum normal force becomes $\sim 50 \%$ of the maximum normal force in the case of vertical wall. In the considered range of angles, the force reduction seems to be almost linear with $\alpha$.
- The effect of hydroelasticity during the impact on a deck house may in general be neglected.

Simplified methods The use of dam-breaking models and shallow-water approximations of the flow on the deck has been in vestigated. Since a theoretical dam-breaking model does not account for the horizontal fluid motion caused by the flow external to the ship, it can only qualitatively describe the flow on the deck.

Shallow-water approximations can in principle be used in certain domains along the deck. However, they require initial and boundary conditions that are dependent onthe external flow, which are not av ailable without solving the complete ship-wa veinteraction problem.

### 9.1 Future Perspectives

The table 9.1 summarizes the parameters influencing green-water loading in the bow area of a FPSO, and their role as determined by the present study is qualitatively shown.

## RELATIVE IMPORTANCE

| parameter | small |
| :--- | :--- |
| Freeboard |  |
| Stem Angle |  |
| Local Flow at the Bow |  |
| Relative Vertical Motion |  |
| Trim Angle |  |
| Coupled Flow Between |  |
| Deck and Outside |  |
| Local Design of Deck House |  |
| Hydroelasticity during Impact |  |
| Wave Steepness |  |
| 3-D Effects |  |

Table 9.1 Qualitative evaluation of factors influencing green-water loading, based on 2-D studies.
Several aspects of the phenomenon need to be further in vestigatedto achieve a complete quantitative understanding. They require more general models relative to the one used in present work. In the following, relevant studies to develop are indicated and, for some of them, possible methods to attack the problem are suggested.
a) External flow. At present, the actual ship motions, resulting from the interaction with the incoming waves, is not modeled. Clearly, these and the dynamic rise of the water in the bow region hav e profound effects in determining wet-deck occurrence. While ship motion can be probably accurately predicted bysimplified models, finer details of the flow in the bow region will require a three-dimensional nonlinear analysis.
On this ground, a domain-decomposition method can represent the proper approach, balancing accuracy requirements, assumptions on the problem of interest, and computational costs. Within this philosophy, the physical domain can be divided in a suitable number of subdomains. Where appropriate, some of the assumptions can be relaxed and the problem can be simplified applying in each subdomain the proper n umerical model.

Since the problem of in terest is time dependent, and the instantaneous solution of each region depends on the solution in the others, time-by-time a "patching" procedure has to be carried out. This represents the main challenging factor. In the case of a FPSO unit, for instance, a possible decomposition could be the one shown in figure 9.1. When the


Figure 9.1 Sketch of a possible patching in the case of a FPSO unit. Top view.
nonlinearities associated with incoming wa vesare not extreme, ship-wa ve interactions can be described by a second-order method with the exception of a near-bow domain where the fully-nonlinear problem has to be solved to describe the run-up and to predict the water shipping. In this discussion, it is implicitly assumed that the wave-inducedbody motions are properly described bythis simplified model.
b) On-deck hydrodynamics. For dam breaking-type flow, a three-dimensional shallow-water analysis could represent a reasonable compromise between efficiency and accuracy. This simplified description should be used to solve the problem in the deck-subdomain, within the domain-decomposition approach. In this case, the structural response under the action of impacting masses of water should be taken into account, may be through local analysis. Another possibility, more computationally demanding, is represented by a suitable field method for studying wavesplashing. In this case, local wavebreaking, ca vit yformations, and other phenomena can be treated. Limits are related both to the computational costs and to thecuracy , which still have to be assessed for large-scale problems where impact loads and multi-phase flows are expected.
c) Deck wetness for advancing ships. F orward speed affects occurrence and severity of water-on-deck phenomena. Depending on the ship-loading conditions, this can have eithepositiv e or negative effects. Related analyses have to account for interactions between steady and unsteady flows which are expected to be relevant near the ship.
d) Ship dynamics with green water on deck. The behavior of the whole vessel can be seriously modified by the motion of the shipped water, leading to reduced stability, capsize and sinking. This is relevant for smaller vessels. F or larger shipsit is important to investigate the effect on global hull-girder loads, like midship bending moment. A "direct simulation" of such complex behavior would be valuable to provide a global understanding and to give a better basis for ship design and development of classification rules.
e) Water shipping on damaged ships. When the ship hull is damaged water shipping phenomena can more easily occur. Related characteristics and possible damages for the vessel
can be quite different relative to the case of water on deck on undamaged ships and require dedicated studies ( $c f$. Dodworth 2000). Main features of the problem can be in vestigated byusing the n umerical method developed in this work.

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## Appendix A

## Details of the Numerical Method

## A. 1 Tangential Velocity along the Domain Boundary

In the numerical method the tangential velocity $\partial \varphi / \partial \tau$ along the boundary $\partial \Omega$ is in general determined by using the central finite-difference operator

$$
\begin{equation*}
\frac{\partial \varphi}{\partial \tau}{ }_{j}=a_{j-1} \varphi_{j-1}+a_{j} \varphi_{j}+a_{j+1} \varphi_{j+1} \tag{A.1}
\end{equation*}
$$

The coefficients $a_{j-1}, a_{j}$ and $a_{j+1}$ are given by

$$
\begin{equation*}
a_{j-1}=-\frac{a^{2}}{d e n}, a_{j}=\frac{a^{2}-b^{2}}{d e n}, a_{j+1}=\frac{b^{2}}{d e n} \tag{A.2}
\end{equation*}
$$

where

$$
a=\tau_{j+1}-\tau_{j}, b=\tau_{j}-\tau_{j-1}, \text { den }=a b(a+b)
$$

They are substituted by

$$
\begin{equation*}
a_{j}=-\frac{2 a b+b^{2}}{d e n}, a_{j+1}=\frac{2 a b+b^{2}+a^{2}}{d e n}, a_{j+2}=-\frac{a^{2}}{d e n}, \tag{A.3}
\end{equation*}
$$

with

$$
a=\tau_{j+1}-\tau_{j}, b=\tau_{j+2}-\tau_{j+1}, \text { den }=a b(a+b),
$$

and, respectively , b y

$$
\begin{equation*}
a_{j}=\frac{2 a b+b^{2}}{d e n}, a_{j-1}=-\frac{2 a b+b^{2}+a^{2}}{\operatorname{den}}, a_{j-2}=\frac{a^{2}}{d e n}, \tag{A.4}
\end{equation*}
$$

with

$$
a=\tau_{j+1}-\tau_{j}, b=\tau_{j}-\tau_{j-1}, \text { den }=a b(a+b),
$$

when a faw ard or backward derivative is needed.

## A. 2 Velocity Potential and Velocity Components

When both $\varphi$ and $\frac{\partial \varphi}{\partial n}$ are known along $\partial \Omega$, the velocity potential can be ev aluatedev erywhere inside the domain by using the in tegral representation (3.3), which in discrete form results

$$
\begin{equation*}
2 \pi \varphi \simeq \sum_{j}\left\{\varphi_{j+1} \frac{I_{4}-\xi_{j} I_{2}}{\xi_{j+1}-\xi_{j}}+\varphi_{j} \frac{I_{2} \xi_{j+1}-I_{4}}{\xi_{j+1}-\xi_{j}}\right\}-\sum_{j}\left\{\psi_{j+1} \frac{I_{3}-\xi_{j} I_{1}}{\xi_{j+1}-\xi_{j}}+\psi_{j} \frac{I_{1} \xi_{j+1}-I_{3}}{\xi_{j+1}-\xi_{j}}\right\} \tag{A.5}
\end{equation*}
$$

where $\psi=\partial \varphi / \partial n$. The terms $I_{1}, . ., I_{4}$ in equation (A.5) are defined as follows

$$
\begin{aligned}
& I_{1}:=\int_{\xi_{1}}^{\xi_{2}} \ln \left(\sqrt{x^{2}+\eta^{2}}\right) d x \\
&=\frac{1}{2} \xi_{2} \ln \left(\xi_{2}^{2}+\eta^{2}\right)-\xi_{2}+\eta \arctan \left(\frac{\xi_{2}}{\eta}\right)-\frac{1}{2} \xi_{1} \ln \left(\xi_{1}{ }^{2}+\eta^{2}\right)+\xi_{1}-\eta \arctan \left(\frac{\xi_{1}}{\eta}\right) \\
& I_{2}:=\int_{\xi_{1}}^{\xi_{2}} \frac{\eta}{x^{2}+\eta^{2}} d x \\
&=\arctan \left(\frac{\xi_{2}}{\eta}\right)-\arctan \left(\frac{\xi_{1}}{\eta}\right) \\
& I_{3}:=\int_{\xi_{1}}^{\xi_{2}} x \ln \left(\sqrt{x^{2}+\eta^{2}}\right) d x \\
&=\frac{1}{4} \xi_{2}^{2} \ln \left(\xi_{2}^{2}+\eta^{2}\right)+\frac{1}{4} \eta^{2} \ln \left(\xi_{2}^{2}+\eta^{2}\right)-\frac{1}{4} \xi_{2}^{2}-\frac{1}{4} \xi_{1}^{2} \ln \left(\xi_{1}^{2}+\eta^{2}\right)-\frac{1}{4} \eta^{2} \ln \left(\xi_{1}^{2}+\eta^{2}\right)+\frac{1}{4} \xi_{1}^{2} \\
& I_{4}:=\int_{\xi_{1}}^{\xi_{2}} \frac{\eta x}{x^{2}+\eta^{2}} d x \\
&=\frac{1}{2} \ln \left(\xi_{2}^{2}+\eta^{2}\right) \eta-\frac{1}{2} \ln \left(\xi_{1}^{2}+\eta^{2}\right) \eta
\end{aligned}
$$

F urther,from derivation of $\varphi$ the velocity is obtained in the form

$$
\begin{equation*}
2 \pi \nabla \varphi \simeq \sum_{j}\left\{\varphi_{j+1} \frac{\vec{I}_{8}-\xi_{j} \vec{I}_{6}}{\xi_{j+1}-\xi_{j}}+\varphi_{j} \frac{\vec{I}_{6} \xi_{j+1}-\vec{I}_{8}}{\xi_{j+1}-\xi_{j}}\right\}-\sum_{j}\left\{\psi_{j+1} \frac{\vec{I}_{8}-\xi_{j} \vec{I}_{6}}{\xi_{j+1}-\xi_{j}}+\psi_{j} \frac{\vec{I}_{6} \xi_{j+1}-\vec{I}_{8}}{\xi_{j+1}-\xi_{j}}\right\} \tag{A.6}
\end{equation*}
$$

where $\vec{I}_{5}, \ldots, \vec{I}_{8}$ are given by

$$
\begin{aligned}
\vec{I}_{5} & :=\int_{\xi_{1}}^{\xi_{2}}-\frac{\vec{\tau} x+\vec{\nu} \eta}{x^{2}+\eta^{2}} d x \\
& =-\frac{1}{2} \vec{\tau} \ln \left(\xi_{2}^{2}+\eta^{2}\right)-\vec{\nu} \arctan \left(\frac{\xi_{2}}{\eta}\right)+\frac{1}{2} \vec{\tau} \ln \left(\xi_{1}^{2}+\eta^{2}\right)+\vec{\nu} \arctan \left(\frac{\xi_{1}}{\eta}\right)
\end{aligned}
$$

$$
\begin{aligned}
& \vec{I}_{6}:=\int_{\xi_{1}}^{\xi_{2}}\left[2 \frac{\eta(\vec{\tau} x+\vec{\nu} \eta)}{\left(x^{2}+\eta^{2}\right)^{2}}-\frac{\vec{\nu}}{x^{2}+\eta^{2}}\right] d x \\
& =-\frac{-\xi_{2} \vec{\nu} \xi_{1}{ }^{2}-\xi_{2} \vec{\nu} \eta^{2}+\eta \vec{\tau} \xi_{1}{ }^{2}+\xi_{1} \vec{\nu} \xi_{2}{ }^{2}+\xi_{1} \vec{\nu} \eta^{2}-\eta \vec{\tau} \xi_{2}{ }^{2}}{\left(\xi_{2}{ }^{2}+\eta^{2}\right)\left(\xi_{1}{ }^{2}+\eta^{2}\right)} \\
& \vec{I}_{7}:=\int_{\xi_{1}}^{\xi_{2}}-\frac{x(\vec{\tau} x+\vec{\nu} \eta)}{x^{2}+\eta^{2}} d x \\
& =-\vec{\tau} \xi_{2}-\frac{1}{2} \vec{\nu} \eta \ln \left(\xi_{2}{ }^{2}+\eta^{2}\right)+\eta \vec{\tau} \arctan \left(\frac{\xi_{2}}{\eta}\right)+\vec{\tau} \xi_{1}+\frac{1}{2} \vec{\nu} \eta \ln \left(\xi_{1}{ }^{2}+\eta^{2}\right)-\eta \vec{\tau} \arctan \left(\frac{\xi_{1}}{\eta}\right) \\
& \vec{I}_{8}:=\int_{\xi_{1}}^{\xi_{2}}\left[2 \frac{x \eta(\vec{\tau} x+\vec{\nu} \eta)}{\left(x^{2}+\eta^{2}\right)^{2}}-\frac{x \vec{\nu}}{x^{2}+\eta^{2}}\right] d x \\
& =\frac{1}{2}\left(-2 \eta \vec{\tau} \xi_{2} \xi_{1}{ }^{2}-2 \eta^{3} \vec{\tau} \xi_{2}-2 \vec{\nu} \eta^{2} \xi_{1}{ }^{2}+2 \vec{\tau} \arctan \left(\frac{\xi_{2}}{\eta}\right) \xi_{2}{ }^{2} \xi_{1}{ }^{2}+2 \vec{\tau} \arctan \left(\frac{\xi_{2}}{\eta}\right) \xi_{2}{ }^{2} \eta^{2}\right. \\
& +2 \vec{\tau} \arctan \left(\frac{\xi_{2}}{\eta}\right) \eta^{2} \xi_{1}{ }^{2}+2 \vec{\tau} \arctan \left(\frac{\xi_{2}}{\eta}\right) \eta^{4}-\vec{\nu} \ln (\% 2) \xi_{2}{ }^{2} \xi_{1}{ }^{2}-\vec{\nu} \ln (\% 2) \xi_{2}{ }^{2} \eta^{2} \\
& -\vec{\nu} \ln (\% 2) \eta^{2} \xi_{1}{ }^{2}-\vec{\nu} \ln (\% 2) \eta^{4}+2 \eta \vec{\tau} \xi_{1} \xi_{2}{ }^{2}+2 \eta^{3} \vec{\tau} \xi_{1}+2 \vec{\nu} \eta^{2} \xi_{2}{ }^{2} \\
& -2 \vec{\tau} \arctan \left(\frac{\xi_{1}}{\eta}\right) \xi_{1}{ }^{2} \xi_{2}{ }^{2}-2 \vec{\tau} \arctan \left(\frac{\xi_{1}}{\eta}\right) \xi_{1}{ }^{2} \eta^{2}-2 \vec{\tau} \arctan \left(\frac{\xi_{1}}{\eta}\right) \eta^{2} \xi_{2}{ }^{2} \\
& -2 \vec{\tau} \arctan \left(\frac{\xi_{1}}{\eta}\right) \eta^{4}+\vec{\nu} \ln (\% 1) \xi_{1}{ }^{2} \xi_{2}{ }^{2}+\vec{\nu} \ln (\% 1) \xi_{1}{ }^{2} \eta^{2}+\vec{\nu} \ln (\% 1) \eta^{2} \xi_{2}{ }^{2} \\
& \left.+\vec{\nu} \ln (\% 1) \eta^{4}\right) /(\% 2 \% 1) \\
& \% 1:=\xi_{1}{ }^{2}+\eta^{2} \\
& \% 2:=\xi_{2}{ }^{2}+\eta^{2}
\end{aligned}
$$

## A. 3 Numerical Features of the Method

In water-on-deck simulations, the free surface is discretized by at least sixt y points per wa velength. In the vicinity of the ship and on the deck, where a higher accuracy is required, a local refinement has been introduced with a factor from 5 to 15 ténnthe initial discretization.

Once the local refinement during the simulation is started, the free-surface regridding has been independently made for the outer and the inner zone. In each of these, the regridding was dynamically made when the size of some element became too large or too small relative to the mean size of the free-surface panel.

The computational time and memory space requirements v ary according to the specific problem studied. F or example, computations reported in dhapter 4 to study wa ve and ship parameter analysis, typically require 20 Mb memory and about 4 hours CPU time on a PC P entium III 350 MHz .

## A. 4 Example of Convergence Test

All the numerical solutions presented have been verified for independence of the two main discretization parameters: the number of points per reference length, and the number of steps per reference time. Usually, for water shipping caused byincoming waves, the wavelengthand the waveperiod are reasonable reference quantities to be used. F ortime discretization, step of the order of $1 / 50-1$ / 80 the waveperiod is used as initial time step but this is greatly varied during the wave-bodyin teraction by the dynamic procedure to tune the time step. A similar consideration can be done for the spatial discretization because of the dynamic grid refinement.

Therefore, a systematic grid-independence analysis can be easily performed only for cases without the body. In the follo wing, an example of corvergence test is reported. The considered case refers to the experimental set-up discussed in chapters 7 and 8 , without the ship model in the wave flume The motion of the physical wavemakr has been set for wa ves with $H=0.16 \mathrm{~m}$ and $\lambda=2 \mathrm{~m}$, and the measured flap motion has been used to drive the wavemakr in the n umerical simulation. Results are presented in figure A. 1 through the evolution of the wave


Figure A. 1 Example of convergence test. Evolution of the w avelevation at 0.765 m from the w avemadr. Prescribed incoming wave with $H=0.16 \mathrm{~m}$ and $\lambda=2 \mathrm{~m}$. T op: numerical results with 25 (dotted line), 50 (dashed line) and 100 (solid line) points per wavelength. The corresponding time step $\Delta t$ is $1 / 32,1 / 64$ and $1 / 128$ the w av period, respectively. Bottom: n umerical results with 100 nodes along one wav elength (solid line) and experimertal results (dashed line).
elevation at 0.765 m from the vertical position of the wa vemaker. In the top figure, results are superimposed for 25 (dotted line), 50 (dashed line) and 100 (solid line) points per wa velength, and $T / \Delta t=32,64,128$ steps per period $T$ of the incoming wave. F roma practical point of view, the results are superimposed. An enlarged view would show small differences around the minima between the coarsest and the most refined grid. No differences are detectable between simulations with 100 nodes and 200poin ts (not shown) along one wavelength.

In the bottom of the figure the simulation with 100 points per wavelengthis compared with the experimental data measured at the same location. The experimental data have been shifted to correct a systematic constant phase delay. This error source in the experiments is discussed in section 7.4. The agreement with the numerical results is satisfactory, though a certain difference in amplitude can be observed from an enlarged view (not shown) at the beginning of the phenomenon.

## Appendix B

## Boundary Value Problem for $\psi$

Here the boundary-value problem for the function $\psi(\vec{P}, t)=\partial \varphi / \partial t+\vec{V}_{P} \cdot \nabla \varphi$ is determined. In particular, it is shown that this is formally identical to the problem (3.1) for the velocity potential ${ }^{1}$. This means that: (i) $\psi$ is a harmonic function, (ii) with a Neumann condition along the wetted surface of the ship, and (iii) a Dirichlet condition along the free surface.
$\psi$ is a harmonic function By applying the Laplace operator $\nabla^{2}$ to the Bernoulli equation (2.4), we have

$$
\nabla^{2} \underbrace{\left(\frac{\partial \varphi}{\partial t}+\vec{V}_{P} \cdot \nabla \varphi\right)}_{\psi=D_{B O} \varphi / D t}-\nabla^{2} \vec{V}_{P} \cdot \nabla \varphi+\nabla^{2}\left(\frac{1}{2}|\nabla \varphi|^{2}+g z+\frac{p}{\rho}\right)=0 \quad \forall \vec{P} \in \Omega .
$$

Here the second term gives

$$
\nabla^{2}\left(V_{G} \cdot \nabla \varphi+\vec{\omega} \times \overrightarrow{G P} \cdot \nabla \varphi\right)=V_{G} \cdot \nabla\left(\nabla^{2} \varphi\right)+\vec{\omega} \times \overrightarrow{G P} \cdot \nabla\left(\nabla^{2} \varphi\right)+\vec{\omega} \times \nabla^{2} \overrightarrow{G P} \cdot \nabla \varphi
$$

which is zero. By taking the divergence of the Euler equation and byusing $\nabla \cdot \vec{u}=0$ we see that also the third term is zero. Therefore $\psi$ is harmonic.

F ree-surface boundary condition By adding and subtracting the term $\vec{V}_{P} \cdot \nabla \varphi$ to the dynamic free-surface condition

$$
\frac{\partial \varphi}{\partial t}+\frac{1}{2}|\nabla \varphi|^{2}+g \eta=0 \quad \forall \vec{P} \in \partial \Omega_{F S}, \forall t
$$

we obtain

$$
\begin{equation*}
\psi=\vec{V}_{P} \cdot \nabla \varphi-\frac{1}{2}|\nabla \varphi|^{2}-g \eta . \tag{B.1}
\end{equation*}
$$

The right-hand-side of equation (B.1) can be evaluated at each time instant, after the problem for $\varphi$ has been solved and if the body motion is known. Therefore, (B.1) giv es a Dirichlet condition along the free surface for the field of $\psi$.

[^5]Body boundary condition First, we note that

$$
\begin{equation*}
\frac{\partial \psi}{\partial n}=\frac{\partial}{\partial n}\left(\frac{D_{B O} \varphi}{D t}\right) \equiv \frac{D_{B O}}{D t}\left(\frac{\partial \varphi}{\partial n}\right) \tag{B.2}
\end{equation*}
$$

Indeed,

$$
\begin{aligned}
\frac{D_{B O}}{D t}\left(\frac{\partial \varphi}{\partial n}\right) & =\frac{D_{B O}}{D t}(\vec{n} \cdot \nabla \varphi) \\
& =\vec{n} \cdot \frac{D_{B O} \nabla \varphi}{D t}+\frac{D_{B O} \vec{n}}{D t} \cdot \nabla \varphi \\
& =\vec{n} \cdot\left[\frac{\partial \nabla \varphi}{\partial t}+\left(\vec{V}_{P} \cdot \nabla\right) \nabla \varphi\right]+(\vec{\omega} \times \vec{n}) \cdot \nabla \varphi
\end{aligned}
$$

where the term $\left(\vec{V}_{P} \cdot \nabla\right) \nabla \varphi$ can be rewritten as

$$
\begin{aligned}
\left(\vec{V}_{P} \cdot \nabla\right) \nabla \varphi & =\nabla\left(\vec{V}_{P} \cdot \nabla \varphi\right)-(\nabla \varphi \cdot \nabla) \vec{V}_{P}-\nabla \varphi \times\left(\nabla \times \vec{V}_{P}\right) \\
& =\nabla\left(\vec{V}_{P} \cdot \nabla \varphi\right)-\vec{\omega} \times \nabla \varphi+2 \vec{\omega} \times \nabla \varphi
\end{aligned}
$$

thus

$$
\begin{align*}
\frac{D_{B O}}{D t}\left(\frac{\partial \varphi}{\partial n}\right) & =\vec{n} \cdot\left[\nabla\left(\frac{\partial \varphi}{\partial t}\right)+\nabla\left(\vec{V}_{P} \cdot \nabla \varphi\right)+\vec{\omega} \times \nabla \varphi\right]+(\vec{\omega} \times \vec{n}) \cdot \nabla \varphi \\
& =\vec{n} \cdot \nabla\left(\frac{\partial \varphi}{\partial t}+\vec{V}_{P} \cdot \nabla \varphi\right)+\vec{n} \cdot \vec{\omega} \times \nabla \varphi-\vec{n} \cdot \vec{\omega} \times \nabla \varphi  \tag{B.3}\\
& =\frac{\partial}{\partial n}\left(\frac{D_{B O} \varphi}{D t}\right)=\frac{\partial \psi}{\partial n}
\end{align*}
$$

Second, by using the impermeability condition $\partial \varphi / \partial n=\vec{V}_{P} \cdot \vec{n}=\vec{n} \cdot\left(V_{G}+\vec{\omega} \times \overrightarrow{G P}\right)$, we can write the left-hand-side of equation (B.3) as

$$
\begin{aligned}
\frac{D_{B O}}{D t}\left(\frac{\partial \varphi}{\partial n}\right) & =\frac{D_{B O}}{D t}\left[\vec{n} \cdot\left(V_{G}+\vec{\omega} \times \overrightarrow{G P}\right)\right] \\
& =\frac{D_{B O} \vec{n}}{D t} \cdot\left(V_{G}+\vec{\omega} \times \overrightarrow{G P}\right)+\vec{n} \cdot \frac{D_{B O}}{D t}\left(V_{G}+\vec{\omega} \times \overrightarrow{G P}\right) \\
& =\vec{\omega} \times \vec{n} \cdot\left(V_{G}+\vec{\omega} \times \overrightarrow{G P}\right)+\vec{n} \cdot\left(\dot{\vec{V}}_{G}+\frac{D_{B O} \vec{\omega} \times \overrightarrow{G P}}{D t}\right) \\
& =V_{G} \times \vec{\omega} \cdot \vec{n}+\vec{\omega} \times \overrightarrow{G P} \times \vec{\omega} \cdot \vec{n}+\vec{n} \cdot \dot{\vec{V}}_{G}+\vec{n} \cdot \dot{\vec{\omega}} \times \overrightarrow{O P}-\vec{\omega} \times \overrightarrow{O P} \times \vec{\omega} \cdot \vec{n}
\end{aligned}
$$

Each term can be evaluated at any time instant if the body motion is known, and therefore the equation (B.2) is a Neumann condition along the ship wetted surface ${ }^{2}$.

[^6]
## Appendix C

## Verification and Validation of the Method in Shallow-Water Conditions

In green-water loading studies, one has to cope with the wa v e-body interaction problem in which wa ves in teract with a floating body, and, if shipping of water occurs, with the development of a free-surface flow along the ship deck. This appendix is devoted to some verification and validation studies relevant to the latter part of the problem.

## C. 1 Case 1: Collapse of a Semi-Circular Water Column

In the follo wing, the collapse under the action of gravity of a semi-circular body of water is studied. The mass of water is limited by a horizontal rigid and smooth wall, as shown in figure C.1.


Figure C. 1 Gravitational collapse of a semi-circular water column. Sk etchof the problem and nomenclature adopted.

F ree-surfaceevolution Within a potential flow model, the bubble ev olutionat very small times after the collapse can be found analytically. In Penney and Thornhill (1952) this is obtained byusing a series of the form

$$
\begin{equation*}
\sum_{n=0}^{\infty} \mathcal{A}_{2 n}\left(\frac{R}{r}\right)^{2 n} \cos 2 n \theta \tag{C.1}
\end{equation*}
$$

to describe both the geometrical and the fluid-dynamic variables. The problem is then solved by in troducing a small-time expansion of the unknown terms $\mathcal{A}_{2 n}$ which are only time dependent. More specifically, the evolution of $\mathcal{A}_{2 n}$ can be found (i) by substituting in the problem equations the series expansion, and (ii) by solving for the coefficients in the small-time expansions of $\mathcal{A}_{2 n}$. The resulting analytical free-surface ev olution for sufficiently small times reads

$$
\left\{\begin{array}{l}
\mathcal{R}(\theta, t)=\mathcal{R}(\theta, 0)-\frac{g t^{2}}{\pi}\left[1+\sin \theta \log \tan \left(\frac{1}{4} \pi-\frac{1}{2} \theta\right)\right]  \tag{C.2}\\
\mathcal{R}(\theta, 0)=\text { const. }=r
\end{array}\right.
$$

where $r$ is the radius of the initial semi-circular configuration of the bubble. This solution is compared with our numerical results in figure C. 2 with satisfactory agreement, and the two


Figure C. 2 Evolution of an initially semi-circular water column: numerical results (solid lines) and analytical solution (dashed lines) based on the small-time expansion by Penney and Thornhill (1952).
results start to diverge after the non-dimensional time $\tau=t \cdot \sqrt{g / r} \simeq 0.5$. This is reasonable since the applicability of expression (C.2) decreases as time increases. The n umerical evolution of the water bubble on a longer time scale $(\tau=t \sqrt{g / r} \leq 8)$ is presented in figure C.3.

Mass and energy conservation On a longer time scale, the small time expansion is no longer applicable and a first test av ailableto verify the fully-nonlinear $n$ umerical method is checking mass $(\mathcal{M})$ and energy $(\mathcal{E})$ conservation ${ }^{1}$. These are shown in the table of figure C. 3 through the

[^7]

Figure C. 3 Evolution of an initially semi-circular water column: free-surface configurations and relative mass and energy errors by the present method. $\mathcal{M}_{0}$ is the initial mass, $\mathcal{E}_{0}$ is the initial energy, and $\tau=t \cdot \sqrt{g / h}$ is the non-dimensional time. The plot is not in natural scale.
relative errors

$$
\Delta \mathcal{M} / \mathcal{M}_{0}=\left(\mathcal{M}-\mathcal{M}_{0}\right) / \mathcal{M}_{0} \quad \Delta \mathcal{E} / \mathcal{E}_{0}=\left(\mathcal{E}-\mathcal{E}_{0}\right) / \mathcal{E}_{0}
$$

$\mathcal{M}_{0}$ and $\mathcal{E}_{0}$ being the initial mass and energy, respectively. The free-surface configurations shown in the same figure correspond to the time instants reported in the table. The mass error is roughly constant and equal to the $0.3 \%$ during the whole presented evolution. The energy error increases with the time, reaching about the $6 \%$ for the latest time considered, which corresponds to a rather large deformation of the bubble.

In the attempt to ov ercome the limits inherent in the small-time expansion approach, Penney and Thornhill (1952) solved the problem by considering a truncated series (C.1) at $N<\infty$, and obtaining numerically the coefficients from the exact boundary value problem. The results (Penney) for $N=4$ are compared with our n umerical results (present) in tables C.1, through the mass and energy ratios for $\tau \leq 1$.

| $\tau$ | P enney | present |
| :---: | :---: | :---: |
| 0.0 | 1.000 | 1.000 |
| 0.2 | 1.001 | 0.998 |
| 0.4 | 1.005 | 0.998 |
| 0.6 | 1.022 | 0.998 |
| 0.8 | 1.054 | 0.998 |
| 1.0 | 1.059 | 0.998 |


| $\tau$ | P enney | present |
| :---: | :---: | :---: |
| 0.0 | 1.000 | 1.000 |
| 0.2 | 1.006 | 1.002 |
| 0.4 | 1.012 | 0.998 |
| 0.6 | 1.039 | 1.000 |
| 0.8 | 1.111 | 1.000 |
| 1.0 | 1.204 | 1.000 |

Table C. 1 Evolution of an initially semi-circular water column: mass ratio $\mathcal{M} / \mathcal{M}_{0}$ (left table), and energy ratio $\mathcal{E} / \mathcal{E}_{0}$ (right table) for increasing value of the non-dimensional time $\tau=t \cdot \sqrt{g / h} . \mathcal{M}_{0}$ and $\mathcal{E}_{0}$ are the initial mass and energy, respectively.

With this approach, mass and energy are better conserved at the very initial time, and error increases with time more than for the present method, may be indicating the need of a larger number of terms in the truncated series.

Pressure evolution Suddenly after the bubble release, the pressure becomes different than the h ydrostatic one. In more detail, for $R=0$ (see sk etc hC.1) P enney and Thornhill's numerical solution giv esa pressure of $0.622 \rho g r$ when $N=4$ and of $0.628 \rho g r$ when $N=5$, while the present n umerical method gives $0.637 \rho g r$, which is very close to the analytical solution $(2 / \pi) \rho g r \simeq 0.6366 \rho g r$ found by P ohle (1950).

The ev olution of dressure distribution along the wall is analyzed in figure C.4, where the n umerical pressure at four time instants is given together with the corresponding hydrostatic contribution $\rho g \eta$. The atmospheric pressure is set zero. The evolution shows that, at the


Figure C. 4 Evolution of an initially semi-circular water column: total (dashed lines) and hydrostatic (solid lines) pressure distributions at four time instants.
beginning, along the whole wetted wall the pressure is smaller than the hydrostatic contribution. Later on the pressure exceeds this value in some parts of the wall, and then approaches it as the time increases.

## C. 2 Case 2: Collapse of a Rectangular Water Column

The collapse of a rectangular water column $2 L$ long can physically be interpreted as the breaking of a dam delimiting a reservoir of water with length $L$. In the following this problem is discussed by assuming that, after the breaking, the water invades a dry and smooth region.

In left plot of figure C. 5 the evolution of a water column with height $h$ and length $2 L=2 h$ is presented. Here, the $x$-axis is along the horizontal wall and the $z$-axis is vertically upwards along the axis of symmetry of the water column. To avoid numerical difficulties, in the simulation the upper corner at the dam position has been rounded with a local radius of curvature of 0.065 h . The non-dimensional time of the free-surface configurations shown is given in the table, together with the corresponding relative mass and energy errors, which are fairly conserved. The right plot in the same figure shows the pressure evolution along the horizontal wall. The global behavior is qualitatively similar to that of the circular water column. The gravitational collapse appears now faster, and the tendency of the pressure to reach the hydrostatic pressure is slower.

In figure C.6, our numerical free-surface evolution is compared with results by a field method based on a finite difference scheme, giv enin P enney and Thornhill (1952). According to the


Figure C. 5 Collapse of an initially rectangular water column. Left: snapshots of the free surface by present method. The corresponding time instants are given in the table, together with the relative errors of mass and energy. $\mathcal{M}_{0}$ is the initial mass, $\mathcal{E}_{0}$ is the initial energy and $\tau=t \cdot \sqrt{g / h}$. The plot is not in natural scale. Right: total (dashed lines) and hydrostatic (solid lines) pressure distributions at different time instants.
authors, their data agree with experimental results, not shown in the paper. Limiting ourselves to this comparison, it is apparent an initial agreement of the two simulations. Later on the velocity near the wall-free surface contact point becomes faster in the finite difference method, and the predicted water level is higher in a large portion of the domain. Since mass and energy are well conserved bythe present method, this suggests that the finite difference scheme does not conserve mass and energy at this stage.


Figure C. 6 Collapse of an initially rectangular water column: free-surface configurations at three time instants. Present method (solid lines) and finite difference method (dashed lines) by Penney and Thornhill (1952). The plot is not in natural scale.

## C. 3 Case 3: Dam Breaking with an Semi-Infinite Water Reservoir

In the follo wing, we consider the breaking of a dam delimiting a reservoir of water with length $L \rightarrow \infty$. In particular, P ohle (1950) studied the first stages of the phenomenon by using a small-time expansion method and found for the pressure field immediately after the breaking

$$
p^{0}(x, z)=\rho g(h-z)-\frac{8 \rho g h}{\pi^{2}} \sum_{n=0}^{\infty}\left\{\frac{1}{(2 n+1)^{2}} e^{\frac{+(2 n+1) \pi x}{2 h}} \cos \left(\frac{2 n+1}{2 h}\right) \pi z\right\}
$$

The adopted coordinate system is indicated in sketc hC.7, further $h$ represents the initial water height. The pressure along the horizontal wall can be obtained from previous expression by


Figure C. 7 Dam breaking: sketch of the problem.
$\operatorname{setting} z=0$. This is represented by the triangles in the left plot of figure C.8. In the same plot n umerical results for $L / h$ equal to 1 , 2 e 3 are shown (solid lines). In the numerical simulations,


Figure C. 8 Dam breaking. Left: analytical pressure distribution along the horizontal wall by Pohle (1950, triangles) and numerical results (solid lines). The dashed line represents the initial free-surface configuration $(\tau=t \cdot \sqrt{g / h}=0)$ used in the numerical simulation. This is characterized by a local radius of curvature of $0.01 h$ at the upper corner at the dam position $(x / h=0)$. Right: free-surface configurations obtained by the small-time expansion in Pohle (1950, dashed lines) and by present method (solid lines). In the numerical case $L=3 h$ is used.
the upper sharp corner at the dam position (see dashed curve in the figure) has been rounded
with a radius of curvature of $0.01 h$. Results by using $L=3 h$ fit quite well the analytical pressure. This gives both a confidence in the numerical pressure evaluation and shows that the actual value of $L$ is practically ininfluent provided $L / \phi \quad 3$, and in the n umericalsimulation a finite length of the reservoir can be considered, reducing the computational costs. The right plot of the same figure shows the agreement between analytical and numerical $(L / h=3)$ free surfaces at the first stages of the release. F ree-surfaceprofiles at larger times after the breaking are giv enb y figure C.9. In the n umerical simulation the initial upper corner at the dam position is characterized


Figure C. 9 Water ev olution after the dam breaking: experiments by Dressler (1954, solid lines), n umerical results (dashed lines) and shallow water results (dashed-dot lines). $\tau=t \cdot \sqrt{g / h}$, where $h$ is the initial height of the water reservoir.
bya radius of curvature of 0.065 h . We verified that the evolution of the free surface for small times after the breaking (not shown) is practically the same as when a radius of 0.01 h is used. In the simulations reported hereafter, we prefer to use the largest radius which allo wsa simpler handling of the later free-surface ev olutionbecause of the smaller initial curvature. In sequence C. 9 the n umerical solution (dashed lines) is compared with experiments by Dressler (1954, solid lines), with satisfactory agreement during the whole considered time interval. At the beginning of the ev olution, dispersive-waveeffects matter, while for larger times the ev olution can be adequately described by the shallow-water solution by Ritter (1892), also presented in the figure (dashed-dot lines). In the later stages of the ev olution, fully-nonlinear "exact" and shallow-water solutions ov erpredict the experimental wa ve-fron velocity. This may be caused by surface-tension effects during the experiments (cf. section 4.2), and the development of turbulent flow influencing the free-surface evolution, as discussed by Dressler (1954). The author observed that this phenomenon appeared later when a smooth bottom (case of the experimental data shown in figure C.9) was used than in the case of a rough surface.

## C. 4 Case 4: Run-up of Long Waves on a Flat Wall

Experimental data for solitary wavesalong flat inclined structures are availablein literature. The solitary-wavesolution can be found analytically (cf. e.g. Mei 1983), and elevation and velocity potential hav ebeen used in the numerical simulation as initial conditions. The studied problem is shown in sketc h C.10: a tank with a vertical wall on the left side and an inclined wall


Figure C. 10 Run-up of solitary wa ves on a flat wall: sketc h of the problem and nomenclature adopted.
on the right side. The tank, with depth $h$, is taken sufficiently long so that the no-penetration boundary condition on the left wall will not alter significantly the initial evolution of the solitary wave, which starts closer tohat sideof the tank.

The run-up of the solitary wa ve along walls with different inclinations hav e been studied. As an example, figure C. 11 shows the free-surface evolutions for inclinations of $\alpha=15^{\circ}$ (left) and $45^{\circ}$ (right). In both cases, the amplitude of the incident wa ve is $A=0.2 h$, with the crest of the


Figure C. 11 Run-up of solitary waves $(A=0.2 h)$ on a flat wall: n umerical solution. Left: $\alpha=15^{\circ}$. Right: $\alpha=45^{\circ}$. The plots are not in natural scale. $\tau=t \sqrt{g / h}$.
solitary wavelocated initially at a distance $8 h$ from $z$-axis ( $c f$. the sketch C.10).
T oemphasize the free surface profiles, in the plots the vertical scale has been exaggerated. Qualitatively, by keeping constant the ratio $A / h$, as the wall inclination reduces (smaller $\alpha$ ) the water run-up becomes faster andn terests a thinner fluid lay er. In practice, a wall with a small inclination behaves as a bead reached by the wave. The water depth becomes locally shallower and wave-breakingphenomena can occur. In the presented cases, the incident waveis strongly deformed $\mathrm{b} y$ the interaction with the wall. This is apparent, for instance, from the sequence on the right where the water conditions near the wall are shown both before and after the run-up. The reflection from the wall destroys the symmetry of the solitary waveand during the water run-down a second crest appears, though verysmall relative to the primary crest.


Figure C. 12 Run-up of solitary waves on a flat vertical wall ( $\alpha=90^{\circ}$ ): maximum run-up. Numerical results (empty squares) are compared with experiments by Camfield and Street (1967, full triangles) and with analytical solution by Byatt-Smith (1971, solid line).

F or these cases, the experimettal maximum run-up, $R$, is given by Hall and Watts (1953). In more detail, the maximum run-up is defined as the maximum vertical distance between the still water lev eland the in tersection between wall and free surface, and the best-fit of the measured data read

$$
\begin{aligned}
& R_{e x}=3.75 A^{1.12}, \text { for } \alpha=15^{0} \quad \text { and } \\
& R_{e x}=2.15 A^{0.81}, \text { for } \alpha=45^{0}
\end{aligned}
$$

If we consider the case $A=0.2 h$, we hav e

$$
\begin{aligned}
& R_{e x} \simeq 0.6 h \text { and } R_{n u} \simeq 0.7 h \quad\left(\alpha=15^{0}\right) \\
& R_{e x} \simeq 0.6 h \text { and } R_{n u} \simeq 0.5 h \quad\left(\alpha=45^{0}\right)
\end{aligned}
$$

for the experimental $\left(R_{e x}\right)$ and n umerical $\left(R_{n u}\right)$ solutions, respectively.

We now consider the case of a vertical wall $\left(\alpha=90^{\circ}\right)$. The maximum run-up is given in figure C. 12 as a function of $A / h$. Here, n umerical results are compared with experiments byCamfield and Street (1967) and with the weakly-nonlinear analytical solution

$$
\frac{R}{h}=2 \frac{A}{h}+\frac{1}{2}\left(\frac{A}{h}\right)^{2}
$$

obtained by Byatt-Smith (1971), with an error $\mathcal{O}\left[(A / h)^{3}\right]$. For (initial) waveamplitude-todepth ratio $A / h$ sufficiently small all the results are in a reasonable agreement, while for larger amplitudes only the $n$ umerical results follow the experiments.

F or the same geometry the pressure ev olution alongythe ertical wall is shown in figure C. 13 for $A / h=0.36$, where, as can be expected, the resulting pressure deviates from the hydrostatic pressure.


Figure C. 13 Run-up of solitary waves on a flat vertical wall $\left(\alpha=90^{\circ}\right)$ : pressure along the wall for a solitary wave with $A / h=0.36(\tau=t \cdot \sqrt{g / h})$.

## Appendix D

## Liquid Wedge-Flat Wall Impact: Similarity Solution

The similarity solution of a liquid wedge impacting nonsymmetrically a flat wall is discussed here. The problem of interest is sketc hed in figure D.1, where a vedge of water hits at $t=t_{\mathrm{imp}}$ a straight horizontal wall with velocity $(U,-V), \mathrm{U}$ and V being positive quantities. The procedure here described follo wsthe one presented in Zhang et al. (1996) for the case with $U=0$. The wedge has an angle $2 \beta$ and an inclination $\gamma$ from the $z$-axis. Both the gravity and the fluid


Figure D. 1 Impact of a liquid wedge against a flat wall: sk etch of the problem and adopted nomenclature.
viscosity are neglected, and the problem is solved in terms of the velocity potential $\varphi$ due to the
impact. The related boundary valueproblem is in the form

$$
\begin{cases}\nabla^{2} \varphi(x, z, t)=0 & \forall \vec{P} \in \Omega  \tag{D.1}\\ \nabla \varphi=U \vec{i}-V \vec{j} & \text { on } S_{\infty} \\ \frac{\partial \varphi}{\partial z}=0 & \text { on } z=0 \\ \frac{\partial \varphi}{\partial x}=\frac{\partial S_{i}}{\partial t}+\frac{\partial \varphi}{\partial z} \frac{\partial S_{i}}{\partial z} & \text { on } x=S_{i}(z, t) \\ \frac{\partial \varphi}{\partial t}+\frac{1}{2}\left[\left(\frac{\partial \varphi}{\partial x}\right)^{2}+\left(\frac{\partial \varphi}{\partial z}\right)^{2}\right]=0 & \text { on } x=S_{i}(z, t)\end{cases}
$$

where the symbols are defined in sketchD.1. Once the non-dimensional variables

$$
\xi=\frac{x}{V t}, \eta=\frac{z}{V t}, \Phi=\frac{\varphi}{V^{2} t}, \zeta_{i}=\frac{S_{i}}{V t},(i=1,2)
$$

are in troduced, the problem can be rewritten as

$$
\begin{cases}\nabla^{2} \Phi(\xi, \eta)=0 & \forall \vec{P} \in \Omega  \tag{D.2}\\ \nabla \Phi=\frac{U}{V} \vec{i}-\vec{j} & \text { as } \eta \rightarrow \infty \\ \frac{\partial \Phi}{\partial \eta}=0 & \text { on } \eta=0 \\ \frac{\partial \Phi}{\partial \xi}=\zeta_{i}-\eta \frac{d \zeta_{i}}{d \eta}+\frac{\partial \Phi}{\partial \eta} \frac{d \zeta_{i}}{d \eta} & \text { on } \xi=\zeta_{i}(\eta) \\ \Phi-\xi \frac{\partial \Phi}{\partial \xi}-\eta \frac{\partial \Phi}{\partial \eta}+\frac{1}{2}\left[\left(\frac{\partial \Phi}{\partial \xi}\right)^{2}+\left(\frac{\partial \Phi}{\partial \eta}\right)^{2}\right]=0 & \text { on } \xi=\zeta_{i}(\eta)\end{cases}
$$

In this way the free-surface velocity components

$$
u_{i}(\eta)=\left.\frac{\partial \Phi}{\partial \xi}\right|_{\xi=\zeta_{i}(\eta)} \quad \text { and } \quad v_{i}(\eta)=\left.\frac{\partial \Phi}{\partial \eta}\right|_{\xi=\zeta_{i}(\eta)}
$$

remain associated with the equations

$$
\begin{equation*}
u_{i}=\zeta_{i}+\left(v_{i}-\eta\right) \frac{d \zeta_{i}}{d \eta} \tag{D.3}
\end{equation*}
$$

and

$$
\begin{equation*}
\frac{d v_{i}}{d \eta}=\frac{\left(\eta-v_{i}\right) \frac{d \zeta_{i}}{d \eta} \frac{d^{2} \zeta_{i}}{d \eta^{2}}}{1+\left(\frac{d \zeta_{i}}{d \eta}\right)^{2}} \tag{D.4}
\end{equation*}
$$

respectively. The former is simply equation (D.2.A). The latter is obtained bydifferentiating equation (D.2.B) with respect to $\eta$ and by eliminating $u_{i}$ through equation (D.3). This means that the problem can be solved once $\zeta_{i}(\eta)$ is kn wn.

At this stage, we assume that the solution is self-similar, and the problem (D.2) becomes function of the variable $\eta$. Further, we assume the relation

$$
\begin{equation*}
\zeta_{i}=a_{i}+\eta b_{i}+d_{i} e^{-c_{i} \eta} \tag{D.5}
\end{equation*}
$$

between $\eta$ and $\zeta_{i}(\mathrm{i}=1,2)$, as done in the work by Zhang et al. (1996). In (D.5), as $\eta \rightarrow \infty$, only the linear contribution remains, implying that the free surface is wedge shaped far from the wall. Close to the wall an exponential behavior is assumed. The unknown coefficients $a_{i}-d_{i}$ can be determined so that problem (D.2) is satisfied. In particular, the asymptotic condition permits to determine $a_{i}$ and $b_{i}$ as follows

$$
\zeta_{i} \rightarrow(\eta+1) \tan \left(\alpha_{i}\right) \pm \frac{U t}{V t} \quad \text { as } \quad \eta \rightarrow \infty \quad\left\{\begin{array}{l}
a_{i}=\tan \left(\alpha_{i}\right) \\
b_{i}=\tan \left(\alpha_{i}\right) \pm \frac{U}{V}
\end{array} \quad\left(\alpha_{i}=\gamma \pm \beta\right)\right.
$$

By in troducing the expression of $\zeta_{i}$ in (D.4), we can solve analytically the ordinary differential equation for $v_{i}$. This yields an in tegration coefficient $C_{0}$ also to be found. The five unknowns $c_{i}, d_{i}$ and $C_{0}$ are determined byenforcing the conditions

$$
\begin{equation*}
\left.v_{i}\right|_{\eta=0}=0 \quad \text { (a) }\left.\quad v_{i}\right|_{\eta \rightarrow \infty}=-1 \tag{b}
\end{equation*}
$$

and by requiring the conservation of fluid mass and of fluid momentum in the $\xi$-direction during the impact (see sketchD.2). By combining conditions (a) and (b), $C_{0}$ can be eliminated from


Figure D. 2 Impact of a liquid wedge against a flat wall. For the mass conservation: $\operatorname{mass}_{a}=$ mass $_{b}+$ mass $_{c}$. For the fluid momentum conservation in the $\xi$-direction: $\operatorname{mom}_{\xi a}=\operatorname{mom}_{\xi b}+\operatorname{mom}_{\xi c}$. Non-dimensional variables are used.
the first-step unknowns, then the equations for $c_{i}, d_{i}$ become

$$
\begin{array}{ll}
1-2: & \frac{1}{c_{i}}\left(1-\frac{\lambda_{i}}{h_{i}}\right)-\frac{\lambda_{i}}{h_{i}}+\frac{a_{i} e_{i}}{c_{i} h_{i}} \ln \frac{\lambda_{i}-a_{i} e_{i}}{h_{i}-a_{i} e_{i}+c_{i} d_{i} e_{i}}+\frac{\lambda_{i}}{c_{i} h_{i}} \ln 4 \lambda_{i}^{2} \\
& -\frac{\lambda_{i}}{c_{i} h_{i}} \ln 2\left[\lambda_{i} h_{i}+a_{i}\left(a_{i}-c_{i} d_{i}\right)+1\right]=0 \quad(i=1,2) \\
3: & \frac{d_{1}}{c_{1}}-\frac{d_{2}}{c_{2}}-\frac{1}{2}\left(a_{1}-a_{2}\right)=0  \tag{D.6}\\
4: & \frac{3}{4}\left(\frac{d_{1}^{2}}{c_{1}}-\frac{d_{2}^{2}}{c_{2}}\right)+\frac{3 a_{1} d_{1}}{c_{1}}\left(\frac{1}{c_{1}}+1\right)-\frac{3 a_{2} d_{2}}{c_{2}}\left(\frac{1}{c_{2}}+1\right)-\frac{1}{2}\left(a_{1}^{2}-a_{2}^{2}\right)
\end{array}
$$

where $e_{i}=d_{i} /\left|d_{i}\right|, h_{i}=\sqrt{1+\left(a_{i}-c_{i} d_{i}\right)^{2}}$ and $\lambda_{i}=\sqrt{1+a_{i}^{2}}$. Equations (D.6.1-2) do not coincide exactly with the corresponding relations in Zhang et al. (1996), which do not satisfy the asymptotic conditions of the problem, probably because of misprints. The solution of equations (D.6) requires an iterative procedure, and in this work a Newton-Raphson algorithm has been applied.

To evaluate the pressure distribution along the wall, the velocity potential along the structure is needed and a specific boundary value problem is solved, with boundary data obtained from the similarity solution discussed above ( $\Phi$ and its normal derivative along the free surface, and the no-penetration boundary condition on the wall). Onc $\boldsymbol{T}^{\boldsymbol{T}}$ on the w all is known, the pressure can be ev aluated from theBernoulli equation

$$
\begin{equation*}
\frac{p}{\rho V^{2}}=-\left\{\Phi-\eta \frac{\partial \Phi}{\partial \eta}-\xi \frac{\partial \Phi}{\partial \xi}+\frac{1}{2}\left[\left(\frac{\partial \Phi}{\partial \xi}\right)^{2}+\left(\frac{\partial \Phi}{\partial \eta}\right)^{2}\right]\right\} \tag{D.7}
\end{equation*}
$$

## Appendix E

## Simplified Method for Water-Wedge Impacts

A simplified solution of the problem of a water half-wedge hitting a flat wall at 90 degrees is derived here. Some verifications of the method have been presented in section 5.2.1 through comparison with a similarity solution.

The problem of in terest is sketc hed in figure E. 1 where $\beta$ is the half-wedge angle and $V$ is the fluid impact velocity. The potential flow theory is used and the gravit y effects are neglected


Figure E. 1 Sketch of the problem of in terest.
by assuming sufficiently large fluid accelerations during the impact. On the free surface (the half-wedge profile) the common "slamming" condition $\varphi=0$ is enforced, $\varphi$ being the velocity
potential caused by the impact. This boundary condition expresses the flow deviation of $90^{\circ}$ at the wall. Both the "deck" (horizontal wall) and the impacted wall are taken rigid. Finally, the half-wedge angle is assumed asymptotically small. With these assumptions, the boundary value problem for $\varphi$ is solved at each time instant $t$ after the impact ( $t=t_{\mathrm{imp}}$ ). The influence of the deck is modeled byimposing the symmetry about the axis along it and studying the equivalent problem of a fluid wedge with angle $2 \beta$ hitting the wall. Within the assumption of an asymptotically small $\beta$, the free surface condition is transfered along the horizontal lines at $y=0$ and $y=2 V t \tan \beta$ (dash-dotted lines in the sketch E.1). The resulting boundary value problem is shown in the top plot of figure E.2, where $a=2 V t \tan \beta$ and $z$ is the complex variable $x+\mathrm{i} y$. The body boundary condition is $\frac{\partial \varphi}{\partial x}=V$ on $x=0$ between $y=0$ and $2 V t \tan \beta$. A


Figure E. 2 Conformal mapping used in the asymptotic solution for small $\beta$.
solution can be found by conformal mapping (cf. Milne-Thomson 1967) between the physical plane $z$ and an auxiliary complex $\zeta$-plane $(\zeta=\xi+\mathrm{i} \eta)$ by the transformation $\zeta=\cosh \frac{\pi \mathrm{Z}}{\mathrm{a}}$. The complex velocity $d w / d z=u-i v$ in the physical plane is related to the corresponding velocity in the auxiliary plane by

$$
\begin{equation*}
\frac{d w}{d \zeta}=\bar{u}-i \bar{v}=\frac{d w}{d z} \frac{d z}{d \zeta} \tag{E.1}
\end{equation*}
$$

By using this relationship, the boundary conditions

$$
\begin{cases}\bar{v}=\frac{V a}{\pi \sqrt{1-\zeta^{2}}} &  \tag{E.2}\\ \text { along } \mathrm{BC} \\ \bar{u}=0 & \\ \text { along } \mathrm{A}_{\infty}, \mathrm{B}_{\infty}\end{cases}
$$

are obtained in the $\zeta$-plane. This means that the solution can be found by a distribution of
vortices on $\eta=0$ between $\xi=-1$ andl ( $c f$. Newman 1977) with strength

$$
\begin{equation*}
\bar{\gamma}(\xi)=\frac{2}{\pi} \frac{1}{\sqrt{1-\xi^{2}}} f_{-1}^{1} \frac{V a}{\pi \sqrt{1-\xi_{1}^{2}}} \frac{\sqrt{1-\xi_{1}^{2}}}{\xi_{1}-\xi} \mathrm{d} \xi_{1} . \tag{E.3}
\end{equation*}
$$

This in tegral equation ${ }^{1}$ can be analytically solved and yields

$$
\bar{u}=-\frac{\bar{\gamma}}{2}=-\frac{2 V a}{\pi^{2} \sqrt{1-\xi^{2}}} \ln \left\{\tan \frac{\pi y}{2 a}\right\}
$$

for the velocity component in $\xi$ direction. By transforming back to the physical plane we find the complex fluid velocity. In particular, the vertical velocity on the wall is $v=\frac{2 V}{\pi} \ln \left(\tan \frac{\pi y}{2 a}\right)$. This suggests a uniformly valid solution on the form

$$
\begin{equation*}
\frac{d w}{d z}=-\frac{2 V}{\pi} \log \left\{\tanh \frac{\pi z}{2 a}\right\} \tag{E.4}
\end{equation*}
$$

where $\log f(z)=\ln |f(z)|+\mathrm{i} \arg [f(z)]$. The total pressure on the wall is then obtained b y Bernoulli equation

$$
\begin{equation*}
p=-\rho\left\{\frac{\partial \varphi}{\partial t}+\frac{1}{2}\left[(-V+u)^{2}+v^{2}+V^{2}\right]\right\}_{x=0} \tag{E.5}
\end{equation*}
$$

and by using $\varphi=-\int_{y}^{a} v \mathrm{~d} y_{1}$. We must note that equation (E.5) is not consistent with the used free surface condition, where the velocity component $v$ is singular. The maximum pressure occurring at $y=a$ is on the form (triangles in figure 5.11)

$$
\frac{\left.p\right|_{y=a}}{\rho V^{2}}=\frac{8 \tan \beta}{\pi^{2}} \int_{\pi / 4}^{\pi / 2} \ln (\tan \underbrace{l}_{l=\frac{\pi y_{1}}{2 a}}) \mathrm{d} l+\frac{1}{2} .
$$

By in troducing solution (E.4) in the kinematic free surface condition $\partial \eta / \partial t=\partial \varphi / \partial z$ and by in tegrating the latter, the free surface elevation (dashed lines in figure 5.10) can be obtained as

$$
\begin{equation*}
\eta=\underbrace{(x+V t) \tan \beta}_{\left.\eta\right|_{t=t_{\mathrm{imp}}}}-\int_{t_{\mathrm{imp}}}^{t} \frac{2 V}{\pi} \ln \left(\tanh \frac{\pi x}{2 a}\right) \mathrm{d} t . \tag{E.6}
\end{equation*}
$$

The expression for the pressure is logarithmically singular at $y=a$ (and $y=0$ ). The same is true for $\eta$ at $x=0$. This is a consequence of that the body boundary condition, $\partial \varphi / \partial x=V$, is not consistent with the boundary condition $\varphi=0$ on $y=a$ (and $y=0$ ). The latter implies zero horizontal velocity at B (and C).

[^8]
## Appendix F

## Simplified Problem to Evaluate the Added Masses

In the following the solution of the simplified problem $B$ discussed in section 5.2.3 is presented. The definition of the used symbols is given in that section and is not repeated here.


Figure F. 1 Sketch of the problem of interest.

It can be shown that the solution of the problem of interest (see sk etc hF.1) can formally be written as

$$
\begin{equation*}
\varphi_{j}(x, z)=\sum_{n=0}^{\infty} a_{j n} \sin \left[\frac{2 n+1}{2 H} \pi(z-H)\right] e^{\frac{2 n+1}{2 H} \pi x} \tag{F.1}
\end{equation*}
$$

This expression satisfies the free surface condition, the bottom condition and the asymptotic condition for $x \rightarrow-\infty$. The value of the unknown coefficients $a_{j n}$ is thus obtained by enforcing the impermeability condition along the wetted portion $(H)$ of the beam. In particular, the normal velocity component along the beam, $\psi_{j}=a \sin p_{j} z+b \cos p_{j} z+c \sinh p_{j} z+d \cosh p_{j} z$, is
here described as series of the independent functions $\sin \left[\frac{2 n+1}{2 H} \pi(z-H)\right]$. The coefficients $v_{j n}$ of this series are expressed by

$$
v_{j n}=\frac{\left.\int_{0}^{H} \psi_{j}(z) \sin \frac{2 n+1}{2 H} \pi(z-H)\right] d z}{\int_{0}^{H} \sin \left[\frac{2 n+1}{2 H} \pi(z-H)\right] d z}
$$

and can be analytically evaluated. By imposing then the impermeability condition $\partial \varphi_{j} / \partial n=$ $\psi_{j}$, the unknowns $a_{j n}$ can be easily obtained as

$$
a_{j n}=v_{j n} \frac{2 H}{(2 n+1) \pi} .
$$

Once $\varphi_{j}$ is known, the added mass terms,

$$
\begin{equation*}
A_{j n}=\int_{0}^{H} \psi_{j}(z) \varphi_{n}(0, z) d z \tag{F.2}
\end{equation*}
$$

can also be analytically calculated.
T oestimate the distance $x^{*}$ from where the fluid is not affected by the beam (cf. section 5.2.3), the boundary value problem is modified by introducing a rigid vertical wall at a distance $x$ from the beam. The solution can be found also in this case by using the same procedure as discussed above. In particular, the added mass terms can be calculated. By progressively increasing $x$, we can find the distance $x^{*}$ as the smallest $x$ from where onthe actual position of the wall is not important for the terms $A_{j n}$.

## Appendix G

## Wavemaker: Experimental Time Histories

Figures G.1-G. 3 show typical recorded time histories of the measured wavemakr motion in terms of the oscillation angle $\alpha$. The latter is positive for a rotation to wards the waveflume. The basic ship model (case a of figure 7.2) was used in the shown tests. The prescribed incoming wa ves are indicated in the captions. A ramp function of 2 seconds was used at the beginning of the motion. Figure G. 4 shows the typical recorded time histories of the wa vemaker motion when the basic model, and the two alternative bow geometries (case b and c of figure 7.2) are considered. The prescribed incoming waves are 2 m long and with a 0.16 m crest-to-trough height. The different wave reflection from the ship model when mrying the bow geometry is not evident looking at the ev olutionof $\alpha$.


Figure G. 1 Wavemaker motion: angle of oscillation. Nominal incoming w aveswith $\lambda=2 \mathrm{~m}$ and $H=0.08 \mathrm{~m}$ (left) and with $\lambda=2 \mathrm{~m}$ and $H=0.12 \mathrm{~m}$ (right).


Figure G. 2 Wavemaker motion: angle of oscillation. Nominal incoming waveswith $\lambda=2 \mathrm{~m}$ and $H=0.14 \mathrm{~m}$ (left) and with $\lambda=2 \mathrm{~m}$ and $H=0.16 \mathrm{~m}$ (right).



Figure G. 3 Wavemaker motion: angle of oscillation. Nominal incoming was with $\lambda=1.5 \mathrm{~m}$ and $H=0.12 \mathrm{~m}$ (left) and with $\lambda=2.5 \mathrm{~m}$ and $H=0.12 \mathrm{~m}$ (right).


Figure G. 4 Wavemaler motion: angle of oscillation in the case of vertical bow (case a), bow inclined at 45 degrees (case b) and bow inclined at -45 degrees (case c). Nominal incoming waves with $\lambda=2 \mathrm{~m}$ and $H=0.16 \mathrm{~m}$.


[^0]:    ${ }^{1}$ In equation (2.4) $p_{e}$ is the external pressure, $\rho$ is the mass density of the fluid, $g$ means the gravity acceleration, $z=0$ corresponds to the mean free surface and $z$ is a vertical coordinate positive upwards.

[^1]:    ${ }^{1}$ The accuracy of field-discretization methods depends on the "quality" of the grid, and not only on the grid-refinement. This limits the use of surface-tracking methods. Also surface-capturing methods (e.g. lev elset method, V olume-of-Fluidmethod (V OF), cf. Kothe 1998) are based on an underlying grid to solve the fluid dynamic equations and, unless using local grid refinement, suffer of unphysical numerical smoothing of the solution. Lagrangian-meshless methods (e.g. Smooth Particle Hydrodynamics (SPH), Reproducing Kernel P article Method (RKPM), cf. Belytschk oet al. 1996) seem promising but still need verification for the problems presently considered.

[^2]:    ${ }^{1} \tau_{\text {imp }}$ is the non-dimensional impact instant and $\Delta \tau_{\text {imp }}=\tau-\tau_{\text {imp }}$.

[^3]:    ${ }^{1}$ One could question about the fact that a decreasing wetted length is measured, since once the probe has been w etted the signal should remain constant. How eve, below a certain thickness of the layer of water on the deck, capillary effects drive a contraction of the water in the form of isolated wetted regions, with rather unpredictable exten $t$, whila are seen from the probe as a reduction of the wetted length.

[^4]:    ${ }^{2}$ When small and thin wetted regions appear, the probes are working in a regime where differences in sensitivity imply significant differences in the output signal.

[^5]:    ${ }^{1}$ See chapters 2 and 3 for the definition of the used symbols.

[^6]:    ${ }^{2} \vec{V}_{G}$ is the acceleration of $G$.

[^7]:    ${ }^{1}$ Mass and energy are given b y

    $$
    \begin{equation*}
    \mathcal{M}=\int_{\Omega} \rho \mathrm{d} S \quad \text { and } \quad \mathcal{E}=\int_{\Omega} \rho\left(g z+\frac{1}{2}|\overrightarrow{\mid}|^{2}\right) \mathrm{d} S \tag{C.3}
    \end{equation*}
    $$

    respectively. Here $\rho$ is the water density, $\Omega$ is the fluid domain and $\vec{u}$ is the fluid velocit y.

[^8]:    ${ }^{1}$ Symbol $f$ in equation (E.3) indicates a principal value integral.

